$$P(P, I) + P(P', I) = \beta p + \alpha (1 - p)$$