$$\#N = \frac{{}^{2n}\mathbf{C}_2 \cdot {}^{2n-2}\mathbf{C}_2 \cdot {}^{2n-4}\mathbf{C}_2 \cdots {}^{4}\mathbf{C}_2 \cdot {}^{2}\mathbf{C}_2}{n!}$$