

SC1007 Data Structures and Algorithms

Tutorial 4: Analysis of Algorithm

- Q1 The function subset() below takes two linked lists of integers and determines whether the first is a subset of the second. Assume there are no duplicate numbers in each list.
 - (a) When will the worst case happen?
 - **(b)** In the worst case, how many item comparison operations will be made?
 - (c) Give the worst-case time complexity of subset as a function of the lengths of the two lists.
 - (d) Write down the worst-case time complexity in asymptotic notations in terms of the lengths of the two lists.

```
# Check whether integer X is an element of linked list Q

def element(X, Q):
    found = False # Flag whether X has been found

while Q is not None and not found:
    found = (Q.item == X)
    Q = Q.next
    return found

# Check whether L is a subset of M

def subset(L, M):
    success = True # Flag whether L is a subset so far

while L is not None and success:

success = element(L.item, M)

L = L.next

return success
```

4-1

Q2 Find the number of print called in the following functions. Write down its time complexity in Θ notation in terms of N.

Hint: For repetition structure, compute the number of inner loops and outer loops. For recursive structure, write down the number of print W(N) in terms of W(N-1). Then use backward substitutions or forward substitutions to express W(N) in terms of N. You may refer to the series shown in lecture.

```
def Q2a(N):
    j = 1
    while j <= N:
    k = 1
    while k <= N:
    print("SC 1007")
    k *= 2
    j *= 3

def Q2b(N):
    if N > 0:
    for i in range(N):
        print("SC 1007")
    Q2b(N - 1)
    Q2b(N - 1)
```

4-2

Q3 A sequence, x_1, x_2, \ldots, x_n , is said to be cyclically sorted if the smallest number in the sequence is x_i for some i, and the sequence, $x_i, x_{i+1}, \ldots, x_n, x_1, x_2, \ldots$, x_{i-1} is sorted in increasing order. Design an algorithm to find the minimal element in the sequence in $O(\log n)$ time. What is the worst-case scenario?