



# LENGUAJES FORMALES Y AUTOMATAS

TAREA: Lema del bombeo para lenguajes  
libres de contexto - COMPROBAR  $a^n b^n c^n$

Universidad Nacional Autónoma de México  
Facultad de Estudios Superiores Aragón  
Ingeniería en Computación

**Materia:** Lenguaje formales y autómatas.

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**N° Cuenta:** 422012511

**Tarea:** Comprobar  $a^n b^n c^n$ .

**Grupo:** 1507

**Semestre:** 2024-I

**Horario:** Lunes, Miércoles, Viernes - 11:30 am-12:50 pm

**Fecha de entrega:** 16/10/2023.

**Nota:** Profesor agregué hasta los ejemplos de la comprobación  
vistos en clases.



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# Pumping Lemma CFL

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## Lema del bombeo para Lenguajes Libres de Contexto

1. Suponer que el lenguaje a prueba es LLC
2.  $\exists n \mid n \in \mathbb{N} \quad |w| > n \quad \forall w \in L$
3.  $w \mid w = xyzuv \mid x, y, z, u, v \in \Sigma$

$$|yzuv| < n$$

$$|yu| \geq 1$$

$$4. \forall k \mid k \in \mathbb{N} \cup \{\emptyset\}$$

$$w' = xy^kzuv^k$$

$$w' \in L$$

$$L = \{a^n b^n c^n \mid n \in \mathbb{N}\}$$

1. Suponer que  $L$  sí es LLC
2.  $\exists n \mid n \in \mathbb{N} \quad w = a^n b^n c^n$   
 $|w| = 3n > n \quad \checkmark$

$$3. xy z u v = w$$

$$n = n$$

$$|yzuv| < n$$

$$|yu| \geq 1$$

$$(1) a^n b^n c^n = w$$

$$x = a^n$$

$$y = b^{n-1}$$

$$z = \lambda$$

$$u = \lambda$$

$$v = bc^n$$

$$k = 1$$

$$w' = a^n b^{n-1} bc^n \quad \checkmark$$

$$k = 0$$

$$w' = a^n b c^n \quad \times$$

$$(2) a^n b^n c^n = w$$

$$x = \lambda$$

$$y = \lambda$$

$$z = \lambda$$

$$v = a^{n-i} \quad i > 1 \quad i < n$$

$$v = a^i b^n c^n$$

$$k = 0$$

$$w' = \lambda \lambda^k \lambda a^{k(a-i)} a^i b^n c^n \quad \times$$

$$i < n$$



$$|yzu| \leq n$$

$$|yu| \geq 1$$

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$$(3) a^n b^n c^n = w$$

$$k=0$$

$$j > 1$$

$$x = \lambda$$

$$y = \lambda$$

$$z = a^i$$

$$u = a^j$$

$$v = a^{n-i-j} b^n c^n$$

$$i+j < n$$

$$w' = a^i a^{n-i-j} b^n c^n \quad \times$$

(4)

$$a^n b^n c^n = w$$

$$k=0$$

$$x = \lambda$$

$$i+l \geq 1$$

$$y = a^i$$

$$z = a^j$$

$$u = a^l$$

$$v = a^{n-i-j-l} b^n c^n$$

$$i+j+l < n$$

$$w' = \lambda a^{xi} a^j a^l a^{n-i-j-l} b^n c^n$$

$$w' = a^j a^{n-i-j-l} b^n c^n \quad \times$$

$$w' = a^{n-i-l} b^n c^n$$

$$i+l = 0$$

$$i+l \geq 1$$

(5)

$$a^n b^n c^n = w$$

$$k=0$$

$$x = a^{n-i-j-l}$$

$$y = a^i$$

$$z = a^j$$

$$u = a^l$$

$$v = b^n c^n$$

$$w' = a^{n-i-j-l} a^{xi} a^j a^l b^n c^n$$

$$w' = a^{n-i-j-l} b^n c^n$$

$$w' = a^{n-i-j} b^n c^n \quad \times$$

$$(6) a^n b^n c^n = w$$

Para B)

$$b^n c^n = b^{nk} c^{nk}$$

$$x = a^i$$

$$y = a^j$$

$$z = a^l$$

$$u = b^n c^n$$

$$v = a^{n-i-j-l}$$

$$k=0$$

$$w' = a^i a^{jk} a^l (b^n c^n)^k a^{n-i-j-l}$$

$$w' = a^i a^l a^{n-i-j-l}$$

$$\times$$



$$w = x y^k z u v$$

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7)  $a^n b^n c^n = w$

$$\begin{aligned} x &= a^n \\ y &= b^{n-1} \\ z &= \lambda \\ u &= b \\ v &= b^{n-i-j} c^n \end{aligned}$$

$$k=0$$

$$\begin{aligned} w' &= a^n (b^{n-1})^k (\lambda) (b^k) b^{n-i-j} c^n \\ w' &= a^n (b^{n-1})^0 b^0 b^{n-i-j} c^n \\ w' &= a^n b^{n-i-j} c^n \end{aligned}$$

X

8)  $a^n b^n c^n = w$

$$\begin{aligned} x &= a^n \\ y &= \lambda \\ z &= b^i \\ u &= b^j \\ v &= b^{n-i-j} c^n \end{aligned}$$

$$k=0$$

$$\begin{aligned} w' &= a^n \cancel{b^i} \cancel{b^k} b^{n-i-j} c^n \\ w' &= a^n b^i b^{n-i-j} c^n \\ w' &= a^n b^{n-j} c^n \end{aligned}$$

X

$$i, j \geq 1$$

$$i+j < n$$

9)  $a^n b^n c^n = w$

$$\begin{aligned} x &= a^n \\ y &= b^{n-1} \\ z &= \lambda \\ u &= b \\ v &= c^n \end{aligned}$$

$$k=0$$

Para B)

$$\begin{aligned} w' &= a^n (b^{n-1})^k (\lambda) (b^k) (c^n) \\ w' &= a^n c^n \end{aligned}$$

X

Case

10)  $a^n b^n c^n = w$

$$\begin{aligned} x &= a^n \\ y &= \lambda \\ z &= \lambda \\ u &= b^{n-i-j} \\ v &= b^{i+j} c^n \end{aligned}$$

$$k=0$$

$$\begin{aligned} w' &= a^n \cancel{\lambda} \cancel{\lambda} (b^{n-i-j})^k (b^{i+j} c^n) \\ w' &= a^n b^{i+j} c^n \end{aligned}$$

X



$$|yzv| < n$$

$$|yv| \geq 1$$

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11)  $a^n b^n c^n = w$

$$k=0$$

X

$$x = a^n$$

$$y = \lambda$$

$$z = \lambda$$

$$v = b^{n-i+j}$$

$$v = b^n c^n$$

$$w' = a^n (b^{n-i+j})^k b^n c^n$$

$$w' = a^n b^n c^n$$

Si, pero no cumple ✓

$$|yzv| < n \quad |yv| \geq 1$$

12)  $a^n b^n c^n = w$

$$k=0$$

$$x = a^{n-i-j-l}$$

$$y = a^i$$

$$z = a^j$$

$$v = a^l$$

$$v = b^n c^n$$

$$w' = a^{n-i-j-l} a^i a^j a^l b^n c^n$$

$$w' = a^{n-i-l} b^n c^n$$

X

13)  $a^n b^n c^n$

$$k=0$$

$$x = a^n$$

$$y = b^{n-i-j-e}$$

$$z = b^i$$

$$v = b^j$$

$$v = b^e c^n$$

$$w' = a^n b^{(n-i-j-e)k} b^i b^{jk} b^n c^n$$

$$w' = a^n b^i b^n c^n$$

$$w' = a^n b^{n+i} c^n$$

X

14)  $a^n b^n c^n$

Para c)

$$k=0$$

$$x = a^n b^n$$

$$y = c^{n-1}$$

$$z = c^1$$

$$v = \lambda$$

$$v = \lambda$$

$$w' = a^n b^n c^{(n-1)k} c^1 (A)(A)$$

$$w' = a^n b^n c^1$$

X



$$w = x y^k z^k u v$$

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15  $a^n b^n c^n = w$

$k=0$

$x = a^n b^n$

$y = c^i$

$z = c^j$

$u = c^{n-i-j}$

$v = \lambda$

$w' = a^n b^n \cancel{c^{ik}} \cancel{c^j} \cancel{c^{(n-i-j)k}} (a)$

$w' = a^n b^n c^j$

X

16

$a^n b^n c^n = w$

$k=0$

$x = a^n b^n$

$y = c^{n-i}$

$z = c$

$u = \lambda$

$v = \lambda$

$w' = a^n b^n \cancel{c^{n-ik}} c (a)(a)$

$w' = a^n b^n c$

X

17

$a^n b^n c^n = w$

$k=0$

$x = a^n b^n$

$y = c^i$

$z = c^j$

$u = c^k$

$v = c^{n-i-j-k}$

$w' = a^n b^n \cancel{c^{ik}} \cancel{c^j} \cancel{c^k} \cancel{c^{n-i-j-k}} (a)(a)(a)$

$w' = a^n b^n c^i c^{n-i+j-k}$

$w' = a^n b^n c^{n-i-k}$

X