

## **Department of Electrical Engineering**

**P**ower **E**lectronics **G**roup

**MACHINE DRIVES AND POWER ELECTRONICS DIVISION**

**Indian Institute of  
Technology Kharagpur**

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# **Development of a Soft-Switching Inverter Topology for Electric Vehicles**

*Submitted in fulfilment  
Of the Requirements for the Project*

In the department of Electrical Engineering under the  
Power Electronics Group, IIT Kharagpur

*By*

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*Under the supervision of*

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**Department of Electrical Engineering**

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**Kharagpur July 2022**

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**CERTIFICATE**

This is to certify that the project report entitled “**Development of a Soft-Switching Inverter Topology for Electric Vehicles**” submitted by **Nilabha Das** to Indian Institute of Technology, Kharagpur is a record of bona fide work carried out by him under my supervision and guidance.

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# Abstract

In this Project Quasi Resonance DC Link Inverter, Modified Quasi Resonance DC Link Inverter, Quasi Z source Inverter and Quasi Z source Inverter with Soft Switching was designed and implemented. Quasi Resonance DC Link Inverter consists of Quasi Resonance circuit in order to provide reduced voltage gradient ( $dv/dt$ ) across inverter to decrease High Frequency Parasitic effects like EMI Noise and to provide Zero voltage switching (ZVS) to all switches of inverter, such that switching losses can be reduced and inverter switching frequency can be increased to reduced harmonics in the AC output of inverter and size of passive components is reduced. Quasi Z source inverter provides voltage boosting to input of inverter without adding additional switch at input of the inverter, when input battery voltage is low and high speed operation is required for Electric vehicle operation. Quasi Z source with soft switching provides both qualities of these two circuits in one circuit, voltage boosting as well as reduced voltage gradient across inverter by soft switching for all the switches of Inverter.

Modified Space Vector Pulse Width Modulation technique was used in order to improve DC Bus utilization. All the topologies were simulated and analyzed in MATLAB.

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# List of symbols

|                               |  |
|-------------------------------|--|
| $V_{DC}$                      | DC Link Voltage                            |
| $S_{DC}$                      | DC Link Series Switch                      |
| $S_{r1}$                      | Resonance circuit switch                   |
| $D_r$                         | Resonance circuit Diode                    |
| $I_o$                         | Inverter input current before switching    |
| $I_{ox}$                      | Inverter input current after switching     |
| $C_r$                         | Resonance Capacitor                        |
| $C$                           | Total Capacitance across inverter legs     |
| $C_o$                         | Equivalent output capacitances of IGBTs    |
| $L_r \text{ \& } L_c$         | Resonance circuit Inductance               |
| $I_{tp1} \text{ \& } I_{tp2}$ | Resonance circuit trip currents            |
| PWM                           | Pulse width modulation                     |
| SVPWM                         | Space vector Pulse width modulation        |
| QRDCLI                        | Quasi Resonance DC link Inverter           |
| ZVS                           | Zero Voltage Switching                     |
| ZCS                           | Zero current switching                     |
| $V_{Cr\_peak}$                | Maximum Voltage across resonance capacitor |
| $V_C$                         | Maximum Voltage across inverter legs       |
| QZSI                          | Quasi Z Source Inverter                    |
| $L_1 \text{ \& } L_2$         | Quasi Z source Inverter Inductors          |
| $C_1 \text{ \& } C_2$         | Quasi Z Source Inverter Capacitors         |
| D                             | Shoot Through Duty Ratio                   |
| $V_{in}$                      | Input DC Battery Voltage                   |

|               |  |
|---------------|--|
| M             | Modulation Index                                   |
| ST            | Shoot Through                                      |
| NST           | Non Shoot Through                                  |
| PID           | Proportional Plus Integral Plus Derivative         |
| $K_P$         | Proportional Controller Coefficient                |
| $K_I$         | Integral Controller Coefficient                    |
| $S_1$ & $S_2$ | QZS with soft switching auxiliary circuit switches |

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# Chapter 1

## Introduction

### 1.1 Introduction

The global push for greenhouse gas emission reduction and higher fuel costs have made the development of electric vehicles (EVs) more urgent than ever. In an EV, traction drive system is one of the key subsystem. High switching frequency in pulse width modulation (PWM) converters reduces the weight and size of passive components and thus reduces the cost as well as weight of power converters. In hard switching inverters switching frequency is limited by losses in the semiconductor devices during switching. Switching with large  $dv/dt$  reduces the switching losses. On the other side bigger voltage gradients ( $dv/dt$ ) combined with long feeders lead to high-frequency (HF) parasitic effects, like EMI interference to components, overvoltage at motor terminals, capacitive currents in the insulation, etc.[3]. Also a major problem with EV Drives are reduction of Input Battery voltage level, as the time passes, after certain run and usage, EV battery voltage level gets reduced. For High speed Operation, more voltage is needed at input of motor. If Battery voltage is low or goes below a certain level then it is not able to supply sufficient amount of power to motor and motor has to run at lower speed, thus a reliable boosting topology is required.

The common solution for mitigating HF parasitic effects is the use of EMI filters. But In order to improve the power density, EMI filter size is of concern. Reduction of voltage gradient can also be provided with the help of quasi resonant converters. Resonant converters consist of combination of active and passive switches and passive components (inductors and capacitors). The main operating principle of these converters is to bring a low voltage across and/or low current through semiconductor devices during a switching status change through resonance.

Thus voltage gradient is reduced across inverter results in reduction of EMI interference as well as switching losses are also reduced due to ZVS turn on and turn off. Main problem with DC-link resonant inverters is over voltage stress across semiconductor devices, for that Modified quasi resonance DC Link inverter is developed, that limits voltage across switching devices to not go more than Input DC voltage. Thus all these arrangements provide suitable EV operation.

The Quasi Z source Inverter (QZSI) with its wide range voltage boosting ability is suitable for the application, where a three phase AC motor is supplied by a lower battery voltage. It does not use any additional switch at the input of inverter. Voltage boosting can also be provided by boost converter at the input of inverter but it uses additional switch, thus overall cost of system increases. QZSI provides unique features that can not be obtained by traditional Voltage source(VSI) and Current source inverter(CSI). The VSI is a buck(step down) inverter, it means ac output voltage is limited below and can not exceed dc input voltage. The upper and lower devices of VSI cannot be turned on simultaneously either by purpose or by EMI noise, otherwise a shoot through would occur and destroy the devices. Thus Dead time is provided between two switches of same phase leg, that creates distortion in waveform. The CSI is a boost(step up) inverter, it means ac output voltage has to be greater than dc input voltage. In CSI at least one of upper leg switches and one lower leg switches has to be turned on, otherwise an open circuit across large input source inductor will destroy switches of CSI, this also creates distortion in the waveform. The QZSI overcomes above problems of VSI and CSI. It can work as both buck and boost inverter. When battery input voltage level is more than a certain level, it works as buck inverter and if Input battery voltage level is lesser, it provides boost operation by shoot through of all the switches of inverter. Thus it reduces total cost and further improves efficiency of traction drive system and provides a reliable operation.

At the last QZSI with soft switching is proposed. QZSI provides voltage boosting by shoot through operation, which is hard switching, so this topology is proposed to provide soft switching to reduce voltage gradient as well as voltage boosting for higher speed operation.

## 1.2 Motivation

Resonant converters are already successfully implemented in DC-DC converters, Improving efficiency, reducing losses. Similarly resonance in inverters is used to achieve control of rate of rise of voltage across load[1] and soft switching of all inverter switches. The Quasi Z source Inverter provides both buck boost ability of inverter by shoot through

of switches of inverter and resonance operation without using additional switch. Proposed

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Quasi Z source Inverter with soft switching provides both qualities of QRDCLI and QZSI. In this project in part A an inverter topology having quasi resonant circuit in DC-Link and in part B an inverter topology having quasi Z source circuit in DC Link and in part C proposed inverter topology quasi Z source with soft switching is implemented.

### 1.3 Objectives

Development of Inverter topologies suitable for an EV application, such that it will have following objectives.

- To reduce High voltage gradient( $dv/dt$ ) across inverter, such that High Frequency parasitic effects like EMI interference to components, overvoltage at terminal of motor, capacitive current of insulation etc. are reduced as well as switching losses of inverter switches is reduced due to ZVS turn on and turn off.
- To limit voltage stress across all the switches of inverter as well as across switches of auxiliary circuit.
- To improve Input DC Bus utilization by using Modified Space vector Pulse width modulation.
- To provide Voltage boosting at the input of inverter, when Input battery voltage is less or when higher speed operation is required for an EV by Quasi Z source Inverter (QZSI) without adding additional switch at the input of inverter.
- To provide both soft switching, reduced high voltage gradient and voltage boosting for inverter operation by proposed QZSI with soft switching.
- To provide reliable operation for electric vehicle motor operation by isolating DC input from inverter switches during shoot through or by connecting a medium between them during shoot through.

### 1.4 Organization

Chapter 1 deals with introduction to thesis, and literature survey on existing topologies. Chapter 2 with explanation of operation of selected Quasi resonant DC-link inverter (QRDCLI) topology, modified QRDCLI topology with voltage clamping circuit. Chapter 3 with design of QRDCLI. Chapter 4 deals simulation results of QRDCLI. Chapter 5 with Space vector pulse width modulation (SVPWM) and its implementation. Chapter 6 with explanation of operation of selected Quasi Z source inverter (QZSI) topology, design of QZSI and simulation results of QZSI. Chapter 7 with Feedforward-feedback control for DC side of QZSI. Chapter 8 with Proposed QZSI with soft switching and then Conclusions and future scope followed by references.

## Chapter 2

# Quasi Resonance DC-Link Inverter

### 2.1 Introduction

Selected topology [1] of quasi resonant DC-link inverter was shown in Fig 1. This topology consists of a quasi-resonant circuit with three additional active switches and inductor and capacitor.

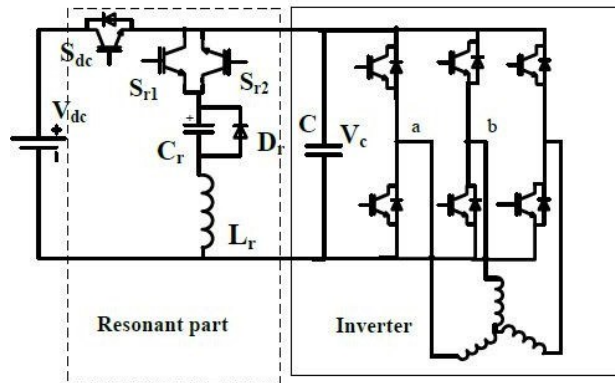


Fig. 1 Basic QRDCL inverter Circuit

Circuit shown in Fig 1 consists of eight modes of operation. Each mode was explained below with equivalent circuit in each mode. Simplified equivalent topology of Fig 1 is shown in Fig 2(When inverter is feeding a motor during one switching interval load can be assumed as constant current source).  $S_{INV}$  represents the inverter legs. On is equivalent to all switches of inverter legs are on. Off represents normal operation of inverter.

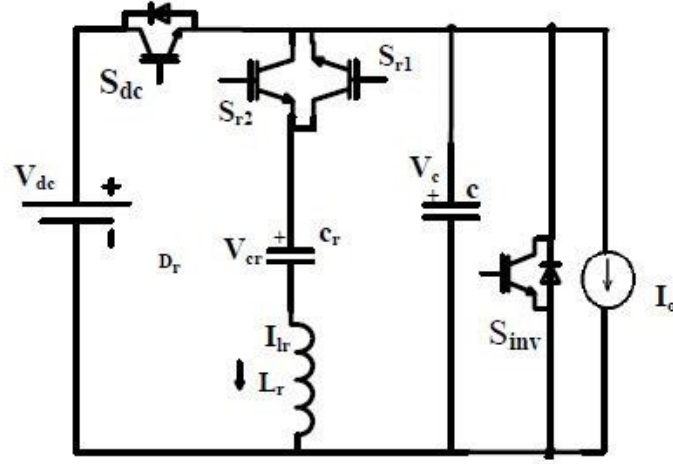


Fig.2 Equivalent circuit of basic QRDCL inverter

## 2.2 Present Circuit and Operation

### Mode 0(M0)

In this mode Inverter is in steady state. Switch  $S_{DC}$  is on and inverter is connected to the source. In each leg respective switches are turned on according to the voltage vector required. The equivalent circuit is shown in Fig 3.

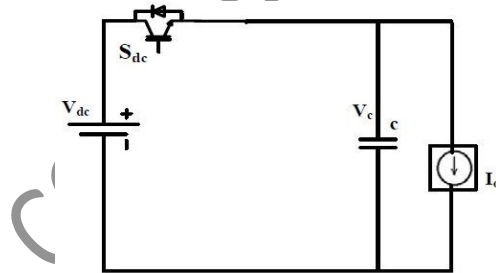


Fig. 3 equivalent circuit of Mode 0

### Mode I(MI)

Whenever any change in applied vector of inverter accordingly inverter leg switches has to change. In order to achieve reduced  $dv/dt$  across inverter and Zero voltage switching of inverter switches, voltage across legs has to reduce to zero by resonance [1]. After switching, voltage across inverter legs has to restore to DC-bus voltage by resonance. During charging and discharging of inverter leg capacitors( $C$ ), resonant circuit has to support the load current based on direction of load. In this mode energy required to operate resonance is stored in resonant capacitor( $C_r$ ) and inductor ( $L_r$ ). The equivalent circuit is shown in Fig 4.

At  $t=t_0$ , switch  $S_{r1}$  will be turned on under Zero current switching. Current through inductor and voltage across capacitor  $C_r$  start increasing. Energy required for resonance

and load was stored in  $L_r$  (voltage rise across  $C_r$  is less). When current reaches to trip current  $I_{p1}$ , mode I will be end. Voltage and current wave forms are shown in Fig 12.

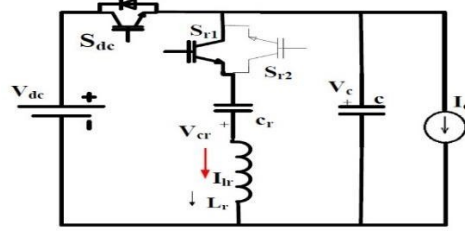


Fig. 4 equivalent circuit of Mode I

### Mode II(M2)

At  $t=t_1$  mode II will start. At  $t=t_1$  switch  $S_{DC}$  is turned off. Since current through  $L_r$  has to follow same direction as at  $t=t_1$ , inductor current starts discharging capacitor  $C$ , voltage across inverter legs becomes zero by resonance with decreased  $dv/dt$  slope at the end of mode II. This mode is analysed for  $dv/dt$  measurement.

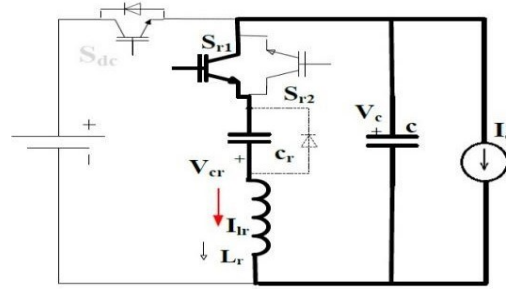


Fig. 5 equivalent circuit of Mode II

### Mode III(M3)

After discharging capacitor  $C$  at  $t=t_2$ , (i.e. voltage across inverter legs reached to zero) inductor ( $L_r$ ) current continue to flow through anti parallel diodes across inverter leg IGBTs. All inverter switches can be turned on under ZVS at this instance (i.e.  $S_{INV}$  can be turned on under Zero voltage condition). When inductor current reaches to zero, voltage across capacitor  $C$  reaches to peak voltage ( $V_{cr \text{ peak}}$ ), storing the total energy. The equivalent circuit of inverter in this mode is shown in Fig 6.

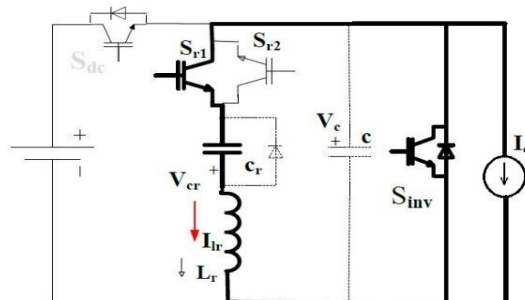


Fig. 6 equivalent circuit of Mode III

### Mode IV(M4)

This mode starts at  $t=t_3$ . In this mode, voltage across resonant capacitor remains at  $V_{cr}(t_3)$ . switch  $S_{r1}, S_{r2}, S_{DC}$  will remain off. Current  $i_L$  remains at zero until  $S_{r2}$  turned on.  $S_{INV}$  Continuous to be on (i.e. all inverter switches are turned on). This is equivalent to null vector. This duration can be controllable. The equivalent circuit in this mode is shown in Fig 7.

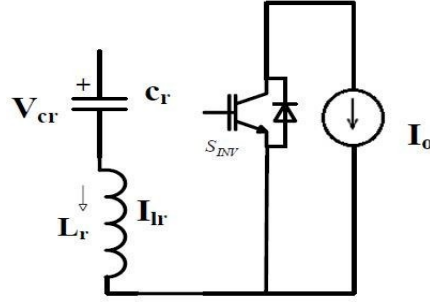


Fig. 7 equivalent circuit of Mode IV

### Mode V(M5)

This mode starts at  $t=t_4$ . To apply new switching sequence, and to recharge the voltage across  $V_{c2}$  to DC-bus voltage by resonance with reduced  $dv/dt$ ,  $S_{r2}$  will be turned on. Capacitor  $C_r$  starts discharging. Current through inductor  $L_r$ , start increasing as shown in Fig 12. When current through inductor reaches to trip current  $I_{tp2}$ , this mode will end. The equivalent circuit in his mode is shown in Fig 8.

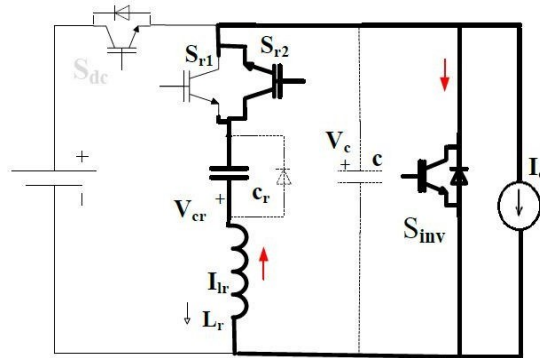


Fig. 8 equivalent circuit of ModeV

### Mode VI(M6)

This mode start when inductor current reaches trip current  $I_{tp2}$ . according to active vector respective inverter switches will be turned off under ZVS, remaining switches will be kept on (i.e.  $S_{INV}$  will be turned off in equivalent circuit). As a result of resonance between  $C$ ,  $C_r$ ,  $L_r$ . Capacitor  $C$  starts charging with reduced  $dv/dt$ , and  $C_r$  continuous to discharge. The equivalent circuit of inverter in this mode is shown in Fig 9. when voltage across  $C_r$  reached to zero diode  $D_r$  become forward biased and starts conducting thus avoiding  $C_r$  to charge in reverse direction.

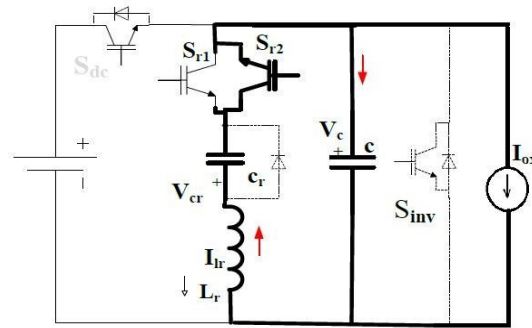


Fig. 9 equivalent circuit of Mode VI

### Mode VII(M7)

This mode starts at  $t=t_6$  when capacitor  $C_r$  completely discharges to zero, and diode  $D_r$  start conducting. Capacitor  $C$  will continuous to charge towards DC-bus voltage with reduced  $dv/dt$ . This mode ends when voltage across capacitor  $C$  is equal to DC-bus voltage, the switch  $S_{DC}$  can be turned on under zero voltage condition. Inductor  $L_r$  supplies both current to charge  $C$  and load current in this mode. The equivalent circuit of inverter in this mode is shown in Fig 10.

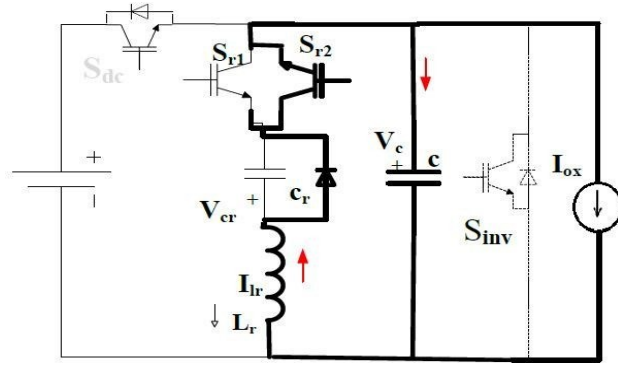


Fig. 10 equivalent circuit of Mode VII

### Mode VIII(M8)

This mode starts at  $t=t_7$ , Since capacitor  $C$  charged to full DC bus voltage the current through inductor  $L_r$ , starts decreasing towards zero. Some part of inductor current delivered to load remaining sent back to DC-source by turning the anti-parallel diode of switch  $S_{DC}$ . This mode ends at  $t=t_8$  when inductor  $L_r$  current reaches to zero thus entering in to mode 0. The equivalent circuit of inverter in this mode is shown in Fig 11.

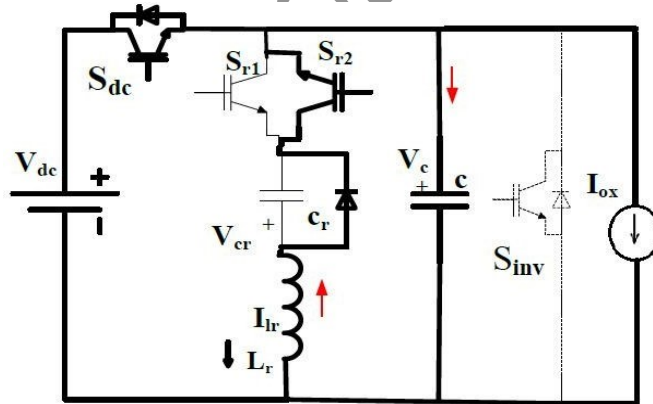


Fig. 11 equivalent circuit of Mode VIII

## 2.3 Typical Voltage and Current Waveform

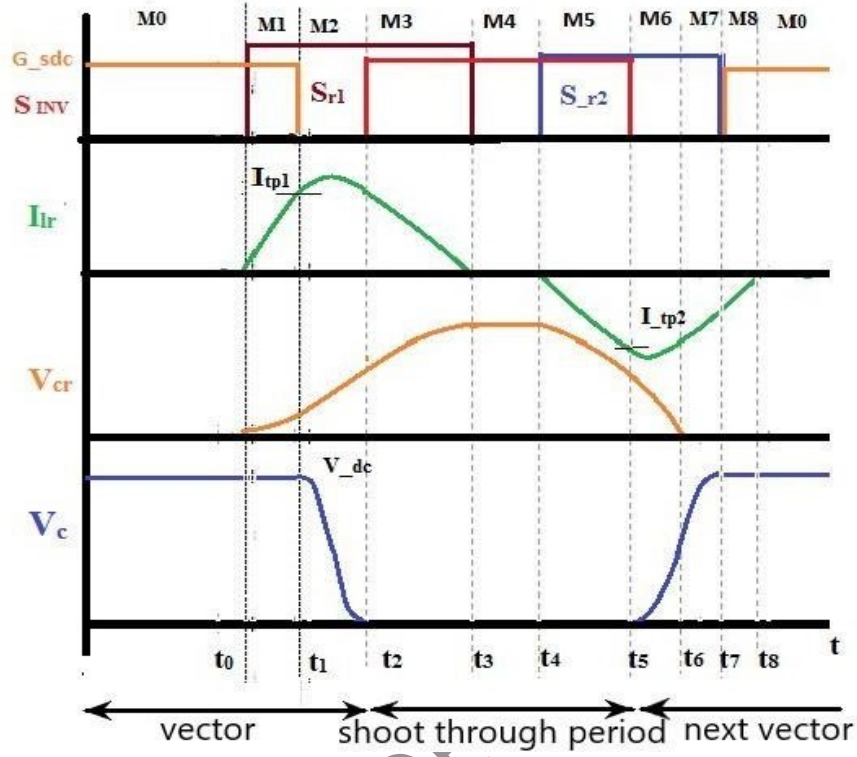


Fig 12 Typical voltage and current waveforms for QRDCL inverter

## 2.4 Proposed Modification

During turn off of  $S_{r1}$  and  $S_{r2}$ , switches has to recover through resonant inductor ( $L_r$ ). As a result  $L_r$  and output capacitance of switches undergo resonance (as  $C_r$  is large compared with output capacitance of switches voltage variation across  $C_r$  significantly less). This resonance causes voltage across  $S_{r1}$  and  $S_{r2}$  to rise up to twice the DC-bus voltage (for  $S_{r1}$ ) or twice the peak voltage across  $C_r$  (for  $S_{r2}$ ) respectively. In order to avoid over voltage stress across switches  $S_{r1}$  and  $S_{r2}$  topology in Fig 1 modified as shown in Fig 13. Coupled inductor  $L_c$  and diode  $D_c$  are used to clamp the voltage across  $S_{r1}$  to dc-bus voltage, and position of diode  $D_r$  is changed to clamp voltage across  $S_{r2}$  to peak voltage across  $C_r$ . The basic modes of operation of circuit in Fig 13 remain same as topology in Fig 1. Operation of circuit in topology Fig 13 is explained bellow.



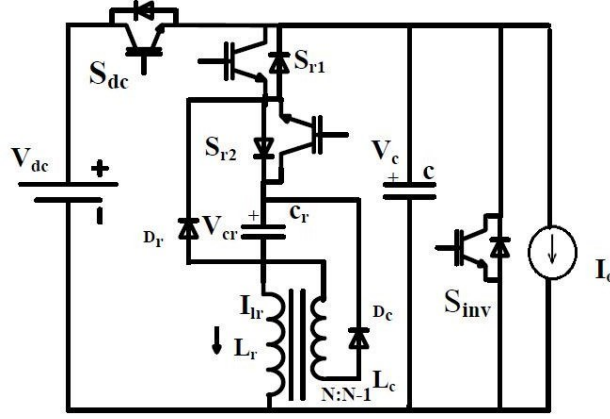


Fig. 13 Modified equivalent circuit of QRDCL Inverter

Mode 0,1,2 are same as in Basic Topology. In mode 3,  $V_{cr} > 0$ ,  $D_c$  remains off. At end of mode 3, at  $t = t_3$ , diode across  $S_{r2}$  will be off first (gate pulse to  $S_{r1}$  is still high).  $S_{r2}$  has to recover through resonant inductor  $L_r$ , during recovery, switch of  $S_{r2}$  and inductor  $L_r$  under goes resonance. Voltage across  $S_{r2}$  has to reach peak voltage across  $V_{cr}$ . Due to resonance between  $S_{r2}$ ,  $L_r$ , voltage across  $S_{r2}$  reaches to twice the peak voltage across resonant capacitor  $C_r$ . This resonance occurs in basic topology. But in Modified Topology, whenever voltage across  $S_{r2}$  reach more than peak voltage across capacitor  $C_r$ , voltage across inductor  $L_r$  become positive. Cathode of diode  $D_r$  at zero potential (since  $V_c = 0$ ) positive voltage across  $L_r$  forward bias diode  $D_r$ , keeping voltage across resonant inductor zero when voltage across  $S_{r2}$  reached to zero. Thus avoiding over voltage across  $S_{r2}$ . Equivalent circuit of modified topology at end of mode III is shown in Fig 14.

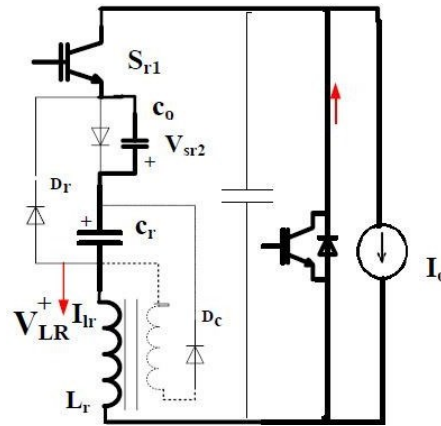


Fig. 14 equivalent circuit of Modified QRDCL inverter at end of Mode III

In mode IV, V, VI, VII diode  $D_c$  remains off. At end of mode VIII i.e. at  $t=t_8$  current through inductor  $L_r$  become zero. When  $L_r$  current become zero anti parallel diode across switch  $S_{r1}$  has to block the DC-bus voltage since is still on. For the Basic Topology, during recovery of anti-parallel diode across  $S_{r1}$ , output capacitance of switch  $S_{r1}$  and resonant inductor  $L_r$  start resonating. As a result of this resonance, the voltage across switch rises to twice the DC-link voltage, but for modified topology, when voltage across switch cross beyond DC-bus voltage, voltage across inductor  $L_r$  will become negative. Negative voltage across inductor  $L_r$  results in forward bias of diode  $D_c$  (voltage across  $V_{cr}$  is zero at  $t=t_8$ ). Energy stored in inductor  $L_r$  due to recovery of switch  $S_{r1}$  will be fed to capacitor  $C_r$ . Capacitor  $C_r$  is large compared to output capacitance of switch, voltage rise across capacitor  $C_r$  is 3-4 percent of peak voltage across  $C_r$ . Thus clamping switch voltage to DC-bus voltage.

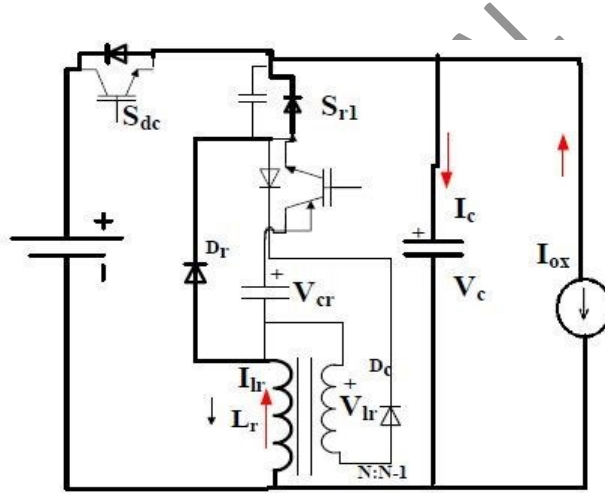


Fig. 15 equivalent circuit of modified QRDCL inverter at the end of mode VIII

## Chapter 3

# Resonance circuit elements and Trip current calculation

### 3.1 Design Considerations

The resonant circuit is designed to commute peak load current of 7A in positive and negative direction. DC Link voltage is 400V. The specifications to design the quasi resonant dc link inverter circuit parameters are as follows:

1. The inverter input voltage must be pulled down to zero by resonance with reduced  $dv/dt$  and for zero voltage switching (ZVS) of inverter switches and again boosted to the DC source voltage.
2. The trip currents should be as small as possible in order to reduce the circuit power loss.
3. It is important to minimize the peak values of the resonant voltage and the resonant current in order to reduce the stress on circuit devices.
4. The resonant transition interval must be designed to be much shorter than inverter's switching cycle time.
5. At the end of mode 7 current through Inductor  $L_r$  must be greater than or equal to inverter input current, otherwise DC link capacitor discharges to meet load demand until  $S_{DC}$  is turned on again.
6.  $I_{tp1}$  decides the total energy required to discharge capacitor C voltage to zero in mode II and restore the voltage  $V_c$  to DC-bus voltage.

7. Trip current  $I_{tp2}$  ensures that Voltage across  $C_r$  drops to zero before recharging of  $C$  to DC bus voltage.

Specification1 is important for soft switching. It is not possible to satisfy all other design objectives simultaneously. The simulations are done for different values of the resonant elements. The proper values of resonant components can be obtained from the simulations.

### 3.2 Calculation of Trip currents

Calculative method to derive expression for  $I_{tp1}$  and  $I_{tp2}$  is presented in [1]. The resonant cycle is heavily influenced by the initial load current  $I_o$  and by  $I_{ox}$  at the next switching state. In mode M1, The energy required to operate complete resonance is stored in inductor  $L_r$ . In mode 2, Inductor has to discharge capacitor  $C$  to zero voltage, and has to support the load based on direction of current and in mode 3, the remaining energy in inductor is supplied to  $C_r$ , The energy required for operation of resonant circuit in Mode M6,M7 ,M8 has to stored in  $C_r$  .The Deriving Equation for  $I_{tp1}$  is as follows

$$I_i = \sqrt{\left(\frac{V_{dc}}{Z_s} + I_o + I_{ox}\right)^2 - \left(\frac{V_{dc}}{Z_s}\right)^2} - I_o \quad (1)$$

$$I_{tp1} = \sqrt{\left(\frac{V_{dc}}{Z_o}\right)^2 - \left(\frac{V_{dc}}{Z_o} - \frac{I_i^2 Z_o}{2V_{dc}}\right)^2} \quad (2)$$

The value of  $I_{tp2}$  must satisfy two needs [1]. First the current  $i_{L1}$  must be large enough to ensure that the oscillation is completed and  $V_c$  reaches the supply value  $V_{dc}$ . Second, the capacitor voltage  $V_{cr}$  must be zero at the end of a resonant cycle. For ease of calculation and reduction of modes we can assume that  $V_c$  reaches to  $V_{dc}$  same that when  $V_{cr}$  reaches to zero.

$$\frac{1}{2} C_r V_{cr(t5)}^2 + \frac{1}{2} L_r I_{tp2}^2 = \frac{1}{2} L_r I_{peak}^2 \quad (3)$$

$$-i_r = -\sqrt{(I_{tp2} + aI_{ox})^2 + \left(\frac{V_{cr(t3)}}{Z_2}\right)^2 - \left(\frac{V_{dc}}{Z_2}\right)^2} - aI_{ox} \quad (4)$$

Trip currents  $I_{tp1}$  and  $I_{tp2}$  can be solved by solving above equations.

### 3.3 Resonance Inductor ( $L_r$ )

The resonant inductor is connected in series with  $S_{r1}$  and  $S_{r2}$ . In order to operate these two switches under zero current switching, the current rise in inductor during rise time of device should not be more than 10% of minimum peak current through switch. The minimum peak current is almost near to first trip current ( $I_{tp1}$ ),  $I_{tp1}$  is considered for calculation of inductor  $L_r$ ,  $I_{tp1}$  is found out to be 14A. The rise time of switch  $S_{r1}$  is 20ns from data sheets. The voltage across inductor, when  $S_{r1}$  on will be  $V_{dc}$  for short period. Then voltage equation across inductor will be

$$V_{dc} = -L_r \frac{di}{dt} \quad (di = 1.4A, dt = 20ns, V_{dc} = 400V) \quad (5)$$
$$L_r = 7.81\mu H$$

### 3.4 Resonance Capacitor( $C_r$ )

In mode 4, the resonant capacitor holds the total energy required for resonant operation. And from mode 6,7 the energy in capacitor must be support the load during M6,M7 ,charge the capacitor  $C$  to  $V_{dc}$ , and at end of mode inductor  $L_r$  current must be more than or equal to load current .Peak voltage across capacitor must be less than  $V_{dc}$  ,by selecting value of peak voltage across capacitor ,and from that  $C_r$  is calculated. The calculated value is used to calculate circuit time intervals, and peak current in inductor. Several number of iterations are performed for different values of  $V_{crpeak}$ . The values for which the entire switching can be done in less than 2us seconds is chosen .The corresponding value of  $C_r = 40nF$ .

### 3.5 Selection of Capacitor C

In order to select capacitor  $C$ , the operation of inverter in mode 6-7 is considered. At starting of mode 6 new switching state is applied i.e. turning off  $S_{INV}$ . The inductor  $L_r$  , $C_r$ ,  $C$  will operate in resonance and charge capacitor  $C$ . The voltage rise across  $S_{INV}$  during fall time of switch  $S_{INV}$  should be less than 10% of full voltage across switch (10% of  $V_{dc}$ ). From device data sheet fall time of device is 20ns. Maximum charging current is  $I_{tp2}$  to be three times the load current. From capacitor current equation

$$I_c = C \frac{dv}{dt} \quad (6)$$

Solving above equation  $C = 4nF$ .

### 3.6 Simulation Specifications for QRDCLI

|                             |        |
|-----------------------------|--------|
| Output Power                | 2.1KW  |
| Output Line to Line Voltage | 245V   |
| Maximum Load current        | 7A     |
| Input DC voltage            | 400V   |
| Resonance Capacitor (Cr)    | 40nF   |
| Resonance Inductor (Lr)     | 7.81uH |
| DC Link Capacitor(C)        | 4nF    |

Table 1. Simulation Specification for QRDCLI

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## Chapter 4

### Simulation Results for QRDCL Inverter

Equivalent circuits of basic and modified topology were simulated in PSPICE 17.2 and exact circuit in MATLAB 2017b. Following are the results from PSPICE 17.2.

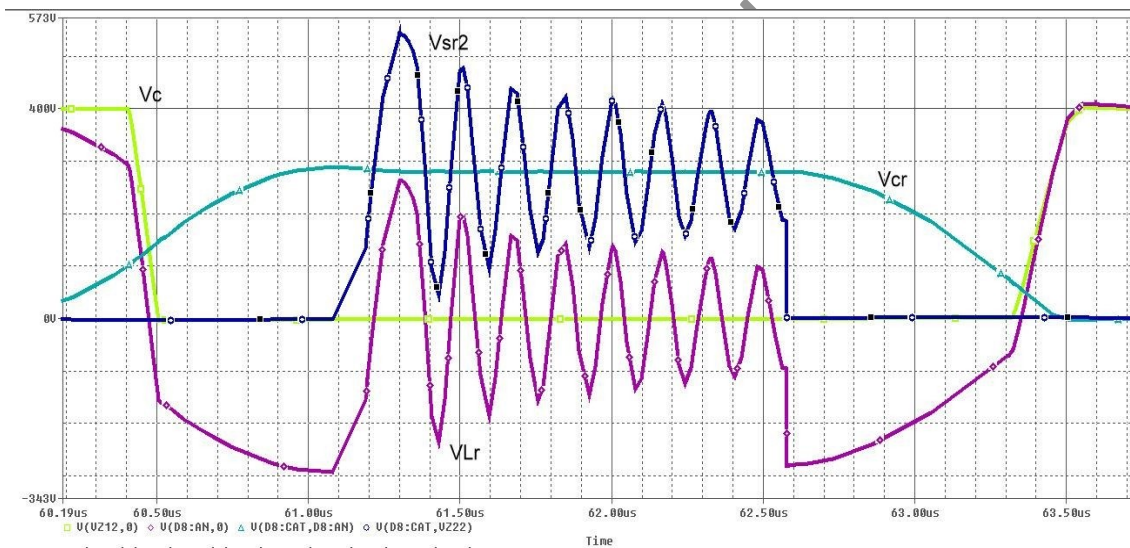


Fig. 16 Voltage across Sr2 ,C,Cr,Lr in basic topology

Fig.16 Shows oscillations of Vsr2 after mode 3 in basic topology, this is because of resonance between output capacitor of Vsr2 and Inductor Lr. Vsr2 goes above Vdc voltage.

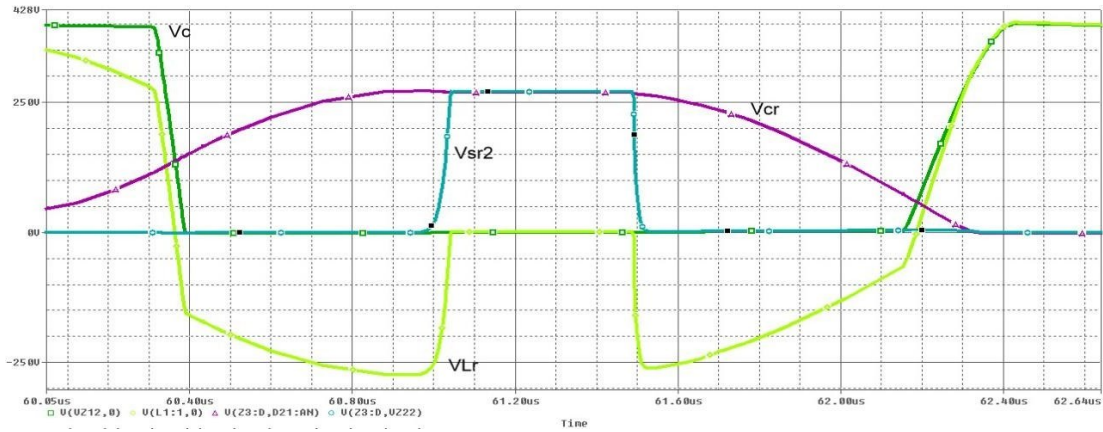


Fig.17 Voltage across Sr2,C,Cr,Lr in modified topology

Fig.17 shows Vsr2 is clamped to Vdc(400V) by clamp circuit in modified topology.

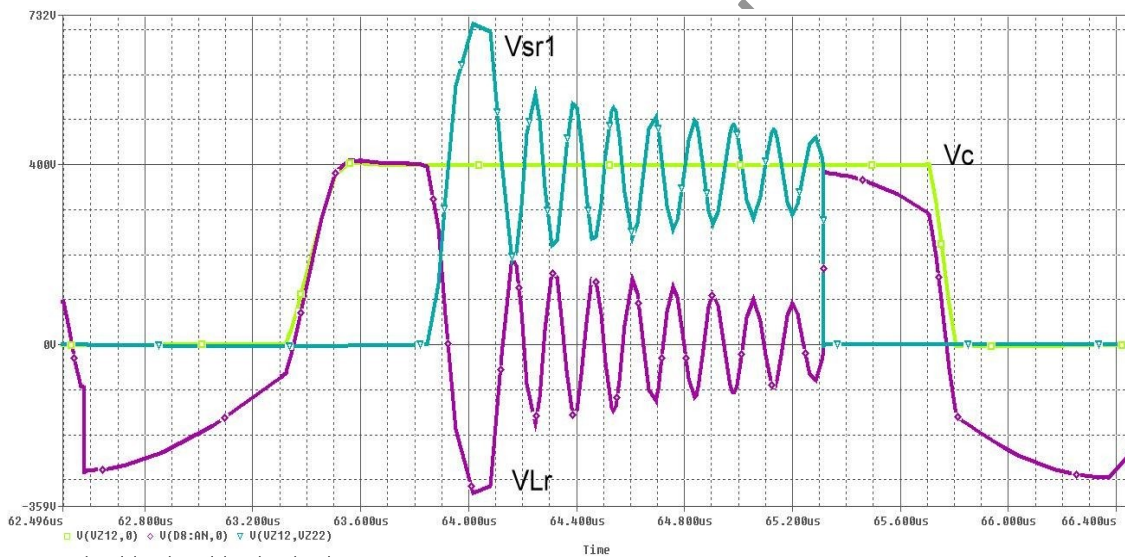


Fig.18 Voltage across Sr1, C ,Lr in basic topology

Fig.18 shows oscillation of Vsr1 at end of mode 8 in basic topology. this is because of resonance between output capacitor of Sr1 and inductor Lr. Vsr1 goes above Vdc voltage.



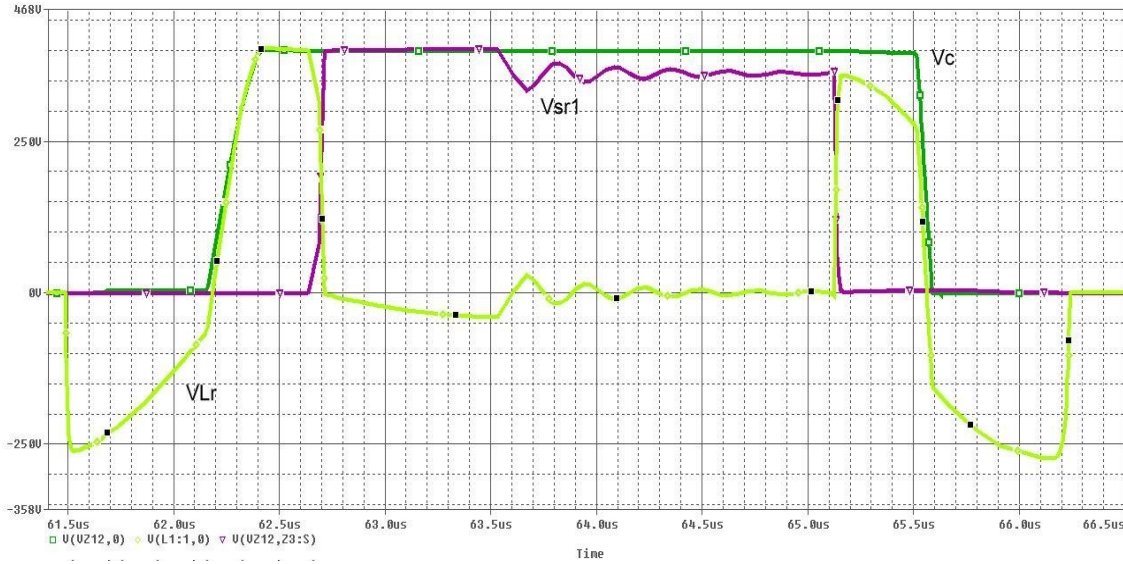


Fig.19 Voltage across Sr1, C ,Lr in modified topology

Fig.19 shows voltage Vsr1 is clamped to Vdc voltage by clamp circuit in modified topology. With  $L_r=7.81\mu\text{H}$ ,  $C_r=40\text{nF}$ ,  $C=4\text{nF}$ . voltage gradients are  $2857\text{V}/\mu\text{s}$  during discharge of Capacitor C and  $1600\text{V}/\mu\text{s}$  during recharge of Capacitor C. With  $L_r=30\mu\text{H}$ ,  $C_r=0.47\mu\text{F}$ ,  $C=0.14\mu\text{F}$ , maximum voltage gradients are  $600\text{V}/\mu\text{s}$ . Simulations were performed for first set of inductors and capacitors. Since voltage change across input is not steep now, THD of load current will also reduce. From Fig.19.1 THD of load current with VSI is 10.16%, but with QRDCLI, THD is 7.28%.

|                                      |         |        |  |                                     |         |        |  |
|--------------------------------------|---------|--------|--|-------------------------------------|---------|--------|--|
| Sampling time = 1e-08 s              |         |        |  | Sampling time = 1e-08 s             |         |        |  |
| Samples per cycle = 2e+06            |         |        |  | Samples per cycle = 2e+06           |         |        |  |
| DC component = 0.06192               |         |        |  | DC component = 0.09099              |         |        |  |
| Fundamental = 6.733 peak (4.761 rms) |         |        |  | Fundamental = 6.887 peak (4.87 rms) |         |        |  |
| THD = 7.28%                          |         |        |  | THD = 10.16%                        |         |        |  |
| 0 Hz (DC):                           | 0.92%   | 90.0°  |  | 0 Hz (DC):                          | 1.32%   | 90.0°  |  |
| 50 Hz (Fnd):                         | 100.00% | -34.8° |  | 50 Hz (Fnd):                        | 100.00% | 233.5° |  |
| 100 Hz (h2):                         | 1.81%   | 78.7°  |  | 100 Hz (h2):                        | 2.59%   | 78.7°  |  |
| 150 Hz (h3):                         | 1.77%   | 73.4°  |  | 150 Hz (h3):                        | 2.53%   | 73.3°  |  |
| 200 Hz (h4):                         | 1.72%   | 68.2°  |  | 200 Hz (h4):                        | 2.45%   | 68.2°  |  |
| 250 Hz (h5):                         | 1.45%   | 85.7°  |  | 250 Hz (h5):                        | 2.36%   | 63.4°  |  |
| 300 Hz (h6):                         | 1.58%   | 59.2°  |  | 300 Hz (h6):                        | 2.27%   | 59.0°  |  |
| 350 Hz (h7):                         | 1.74%   | 66.4°  |  | 350 Hz (h7):                        | 2.17%   | 55.0°  |  |
| 400 Hz (h8):                         | 1.44%   | 51.4°  |  | 400 Hz (h8):                        | 2.06%   | 51.3°  |  |
| 450 Hz (h9):                         | 1.37%   | 48.1°  |  | 450 Hz (h9):                        | 1.97%   | 48.0°  |  |

Fig.19.1 Load current THD comparison between VSI and QRDCLI

# Chapter 5

## Space Vector PWM

For all the topologies in this project, for PWM, we are using space vector PWM (SVPWM). In SVPWM reference is a resultant space vector, which rotates in space according to frequency of modulating three phase waves and by position of this space vector in different six sector, we can find out time duration of corresponding active vector and null vector for that sector.

In Quasi Resonance DC Link Inverter, whenever there is change (transition) in switching status from one active vector to next active vector or active vector to null vector, resonance circuit has to be operated for reduced  $dv/dt$  across inverter and for ZVS of all the switches of the inverter.

### 5.1 Triangle comparison based SVPWM

Triangle comparison based SVPWM is different than computational SVPWM. In computational SVPWM, mathematical formulas are used for calculation of time duration of two active vectors ( $T_A, T_B$ ) and null vectors ( $T_0, T_7$ ). In MATLAB implementing computation SVPWM become a bit complicated because two sampling time needs to be used, one of calculating  $T_{AB07}$  at starting of switching time period (100us) and other for turning on and off switching devices (1ns). So one modification is made in form of Triangular comparison based SVPWM.

In Triangle comparison based SVPWM, one common voltage  $V_{CM}$  is added to all three reference voltages, such that switching sequence of active vector and null vector is same as that of computational SVPWM and time duration of vector  $T_{AB07}$  is also

approximately same.

## 5.2 Calculation of common Voltage ( $V_{CM}$ )

Suppose that  $V_a, V_b, V_c$  are the three reference voltages. One common voltage  $V_{CM}$  is added such that switching sequence of vectors and time durations of vectors  $T_{AB07}$  remains. Suppose  $V_a^*, V_b^*, V_c^*$  are the reference voltage after addition of common voltage. Then

$$V_a^* = V_a + V_{CM} \quad (7)$$

$$V_b^* = V_b + V_{CM} \quad (8)$$

$$V_c^* = V_c + V_{CM} \quad (9)$$

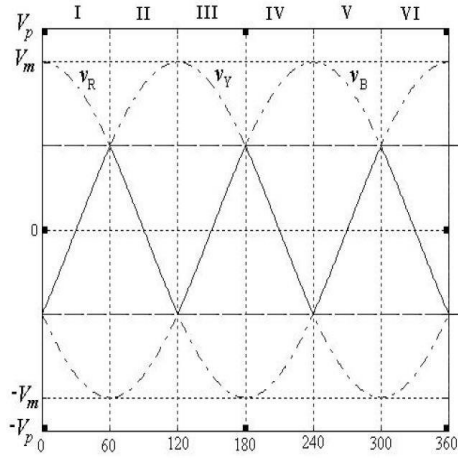


Fig 20.  $V_{MAX}, V_{MIN}, V_{MID}$  in six sectors

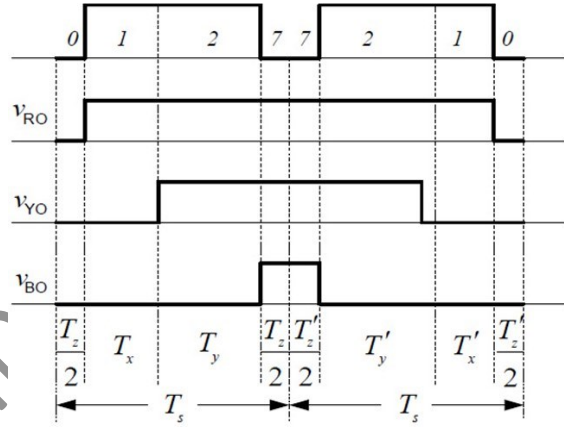


Fig. 21 active, null vector time in SVPWM sector1

Now in any of switching period these  $V_a^*, V_b^*, V_c^*$ , depending on their magnitude and polarity, will be  $V_{MAX}^*, V_{MID}^*, V_{MIN}^*$ . Null vector period at starting of SVPWM is same as half of null vector at mid duration. Thus

$$\begin{aligned} V_p - V_{MAX}^* &= V_{MIN}^* - V_n \text{ where } V_p = 1 \text{ and } V_n = -1 \\ V_{MAX}^* + V_{MIN}^* &= 0 \\ V_{MAX} + V_{MIN} \\ V_{CM} &= -\frac{V_{MAX} + V_{MIN}}{2} = 0.5V_{MID} \end{aligned} \quad (10)$$

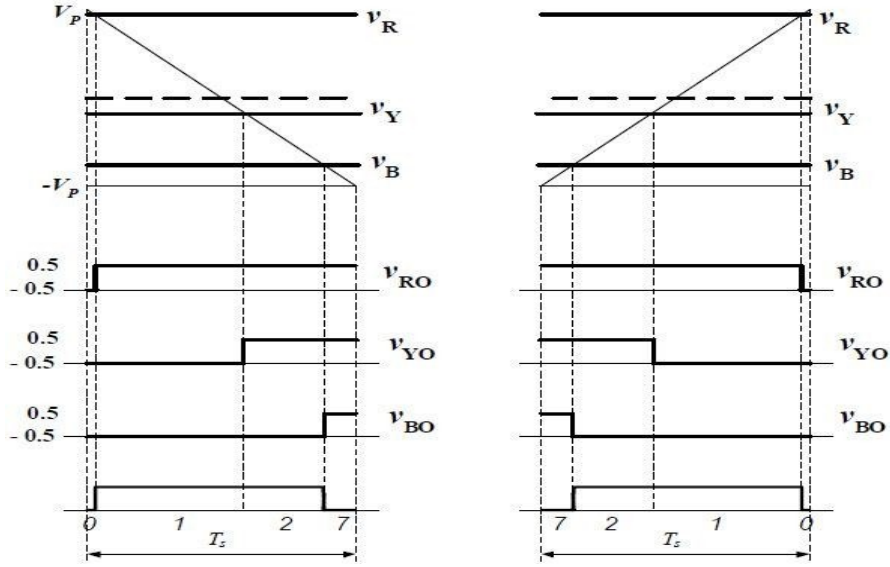


Fig.22 triangular comparison based SVPWM

These  $V_{CM}$  is to be added in each reference voltage  $V_{abc}$  to get  $V_{abc}^*$ .  $V_{abc}^*$  is compared with Triangular carrier wave (Frequency 10KHz) to get switching gate pulses for all switches of Inverter. Using SVPWM we can get 15% more modulation index, thus DC bus utilization increases. Fig.22 shows Triangular comparison based SVPWM. Fig.23 shows shoot through duration in one switching period.



Fig.23 shoot through duration (red) in one switching period for QRDCLI

## Chapter 6

# Quasi Z Source Inverter

### 6.1 Introduction

If battery voltage decreases after a certain run and higher speed operation is required for an EV, motor won't be getting enough voltage from DC side for its High speed operation. Battery life also decreases due to aging. Thus we need boosting of voltage to supply sufficient ac output voltage without decreasing reliability and efficiency of drive system. Although VSI with boost converter increases overall efficiency of drive system by regulating DC Link voltage, but it brings additional cost due to added additional switch at the input. Therefore one topology Z source inverter (ZSI) was invented [2] and its modification Quasi Z source inverter(QZSI) is used here[4]. The QZSI does not use additional switch at the input, thus reduce cost , also it increases efficiency and provides reliable operation for drive system.

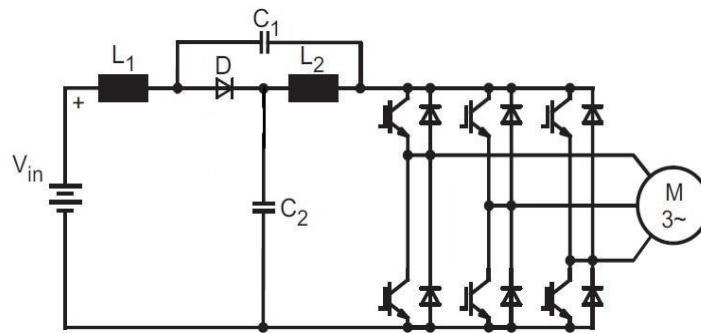


Fig.24 Quasi Z source Inverter

There are basically two switching state possible, while operating QZSI. Shoot Through state and Non Shoot Through state .Non shoot through state consists of Active state and Zero state. Shoot through state is used for boosting of voltage. The operation of both states are discussed below.

## 6.2 Modes of Operation

### 6.2.1 Shoot through State

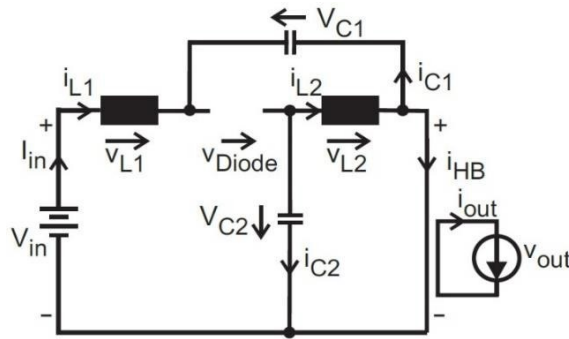


Fig.25 QZSI in shoot through duration

In shoot through state, all the switches of inverter are turned on. capacitor C1,C2 gives energy to Inductor L1,L2 by resonance. The minimum duration of null vector( $T_{o\_min}$ ) is calculated in any of the switching period by deriving relation between shoot through duty ratio and modulation index for required AC output voltage and Shoot through state is applied for that minimum duration of null vector (000 or 111),thus diode of QZSI gets reversed biased and capacitors C1 and C2 gives their energy to inductor ,thus energy of inductor increases, which it gives to capacitor in next state.

### 6.2.2 Non Shoot through State

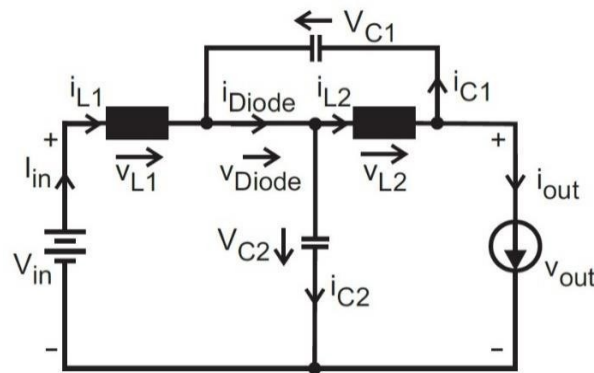


Fig.26 QZSI in Non shoot through duration

In non shoot through state, inductor transfers their energy to capacitor ,thus boosted voltage ( $V_{c1} + V_{c2}$ ) appears across input of inverter and effective input voltage of inverter increases thus boosting of voltage happens.

### 6.3 Switching average for inductor current and capacitor voltage

All the switching average value of Current ( $i_{L1}, i_{L2}$ ) and Voltage ( $V_{C1}, V_{C2}$ ) is calculated below using volt second balance across inductor and current second balance through capacitor.  $t_A$  is non shoot through duration,  $t_{ST}$  is shoot through duration.

$$V_{L1} = \frac{(V_{in}-V_{c2})t_A T_s + (V_{in}+V_{c1})t_{ST} T_s}{T_s} = 0 \quad (11)$$

$$V_{L2} = \frac{(-V_{c1})t_A T_s + (V_{c2})t_{ST} T_s}{T_s} = 0 \quad (12)$$

$$I_{C1} = \frac{(i_{L2}-i_o)t_A T_s + (-i_{L1})t_{ST} T_s}{T_s} = 0 \quad (13)$$

$$I_{C2} = \frac{(i_{L1}-i_o)t_A T_s + (-i_{L2})t_{ST} T_s}{T_s} = 0 \quad (14)$$

Hence

$$V_{c1} = \frac{V_{in} D}{1-2D} \quad (15)$$

$$V_{c2} = \frac{V_{in}(1-D)}{1-2D} \quad (16)$$

$$I_{L1} = I_{L2} = \frac{i_o(1-D)}{1-2D} \quad (17)$$

Where  $V_{C1}$  is average voltage across  $C1$ ,  $V_{C2}$  is average voltage across  $C2$  and  $I_{L1}, I_{L2}$  average current through  $L1$  and  $L2$ ,  $D$  is shoot through duty ratio.

## 6.4 QZSI Design for EV operation

For Design of QZSI, we took Load as 10KW ,230 V<sub>LL</sub> rms .Using SVPWM DC link minimum Voltage( $V_{DC \min}$ ) =  $\frac{230}{0.612 \times 1.15} = 326.8$  volt. It means that if battery voltage  $> V_{DC \min}$  , normal VSI operation will be there and no need of voltage boosting operation .If Battery Voltage  $< V_{DC \min}$  ,and High speed operation is required, we need to do Boost operation .This Boost duration we are applying in every switching period and it equals to time duration of minimum null vector duration in any switching period, which is shown in Fig.27.

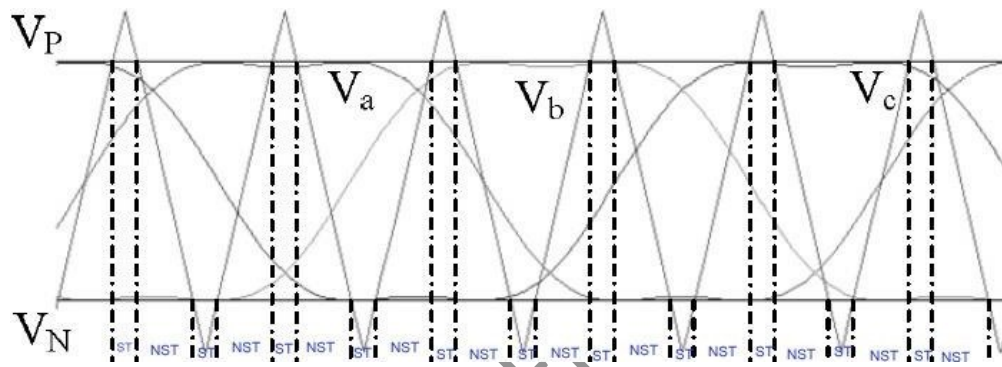


Fig.27 Shoot through duration in switching periods

### 6.4.1 Duty Ratio and Modulation Index Relation

From Fig.27 relation between Modulation index(M) and Shoot through duty ratio(d) is

$$d = 1 - \frac{\sqrt{3}}{2} M \quad \text{or} \quad M = \frac{1-d}{\sqrt{3}/2} \quad (18)$$

During Non shoot through Period voltage appearing across input of inverter is

$$V_{dc} = V_{C1} + V_{C2} = \frac{V_{in}}{1-2d} \quad (19)$$

Thus from relation  $V_{LL\_rms} = 0.612 \times M \times V_{dc}$  ,we get desired shoot through duty(d) and then Modulation Index(M). Suppose  $V_{Battery}$  has come to 230 Volt ,which is very less than 326.8 V .in this case from above formula put  $V_{in}=230$  V .We get  $d = 0.2282$  and  $M = 0.8911$ . From eq.19 duty ratio limit is 0.5, but we generally don't go upto that because then capacitor won't have enough energy to charge inductor and output voltage of QZS decreases.



### 6.4.2 Selection of Inductor

Inductor is selected based on current ripple consideration, If we consider loss of inverter and motor = 90% ,then  $I_{L \text{ avg}} = \frac{10KW/0.9}{230 \text{ V}} = 48.3A$ ,Considering a Shoot through

duration of inductor, From  $V_L = L \frac{di}{dt}$ .

$$L \geq \frac{V_L}{I_{L \text{ avg}}} \frac{dt}{di} \quad (20)$$

Considering Inductors during Shoot through period and current ripple as 5% of average value, dt as half of shoot through time and  $V_L$  as 328.6 V. we get

$$L1, L2 \geq 1540.6\mu H$$

### 6.4.3 Selection of Capacitor

Capacitor is selected based on Voltage ripple consideration, suppose for both capacitor , Voltage ripple across them is 5%, From shoot through duration

$$I_c = C \frac{dV}{dt} \quad (21)$$

$$C \geq \frac{I_c}{C \frac{dV}{dt}}$$

Considering Capacitor C1,during Shoot through period and voltage ripple as 5% of average value, dt as half of duty cycle time,  $I_c$  as average inductor current.we get

$$C1 \geq 114.2\mu F$$

Thus we take  $C_1 = C_2 = 114.2\mu F$

### 6.4.4 Simulation specifications

|                                       |          |
|---------------------------------------|----------|
| Output Power                          | 10KW     |
| Output Line voltage                   | 230 V    |
| Input Battery Voltage                 | 230 V    |
| Quasi Resonance Inductor L1,L2        | 1540.6uH |
| Quasi Resonance Capacitor C1,C2       | 114.2uF  |
| Shoot through duration every $T_{sw}$ | 22.82us  |
| Modulation Index                      | 0.8911   |

Table 2. Simulation Specifications for QZSI

## 6.5 Simulation Results for QZSI

Open Loop Control for QZSI was simulated in MATLAB 2017b. Simulation results are as follows. Here S.T. represent Shoot through Duration, N.S.T. represent Non Shoot through duration. DC side waveforms are for one switching period (100us).

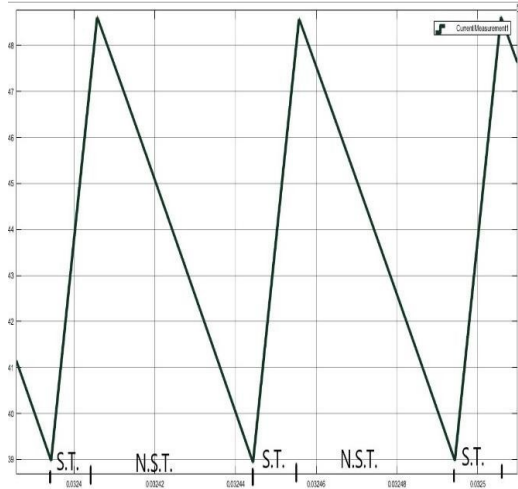


Fig.28 current through inductor 2

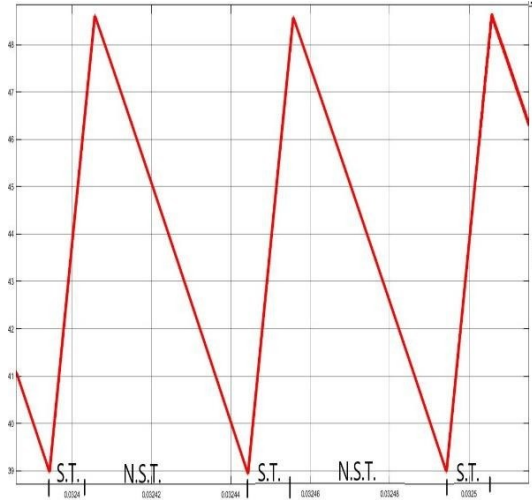


Fig.29 current through inductor 1

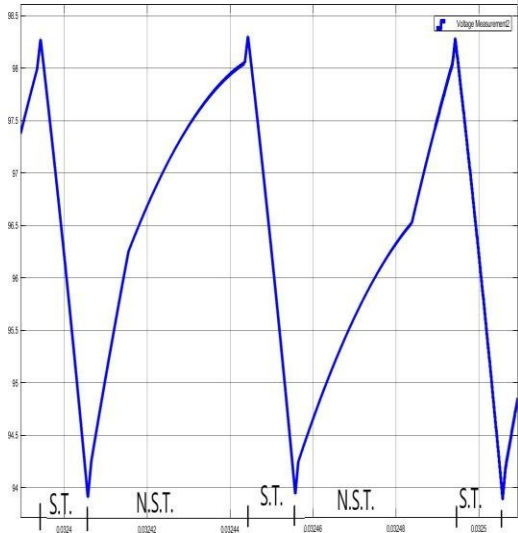


Fig.30 Voltage across capacitor 1

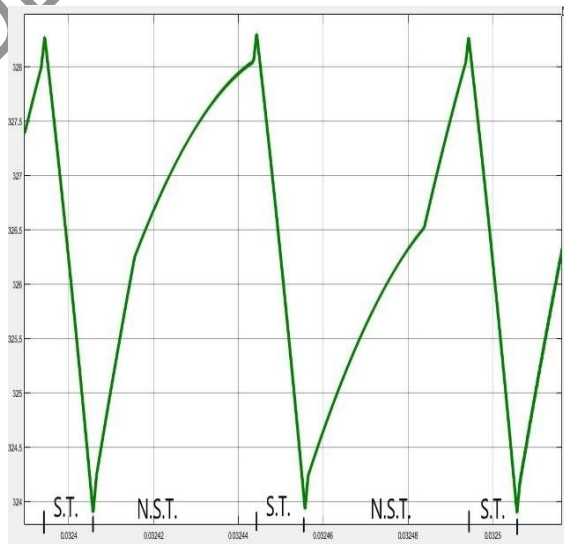


Fig.31 Voltage across capacitor 2

Fig. 28 and 29 shows current through inductor 1 and 2 ,since voltage across both inductor are same in all states, thus average value and waveform will also be same. From

waveform in Shoot through state(ST) inductor current increases,because capacitor gives energy to inductor in S.T. state.Average value of both inductors are 44A.

Fig.30 and 31 shows voltage across capacitor 1 and capacitor 2.by switching averaging, we came to know both capacitor voltages differ by  $V_{input}(230V)$ ,which is also shown in waveform. In S.T. state capacitor voltage decreases,because it gives energy to inductor. $V_{C1} = 96V, V_{C2} = 326.8V$

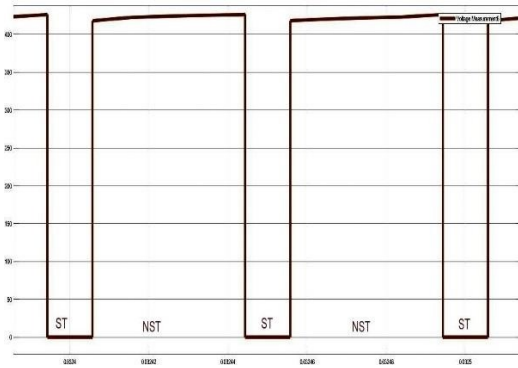


Fig.32 Voltage across inverter input

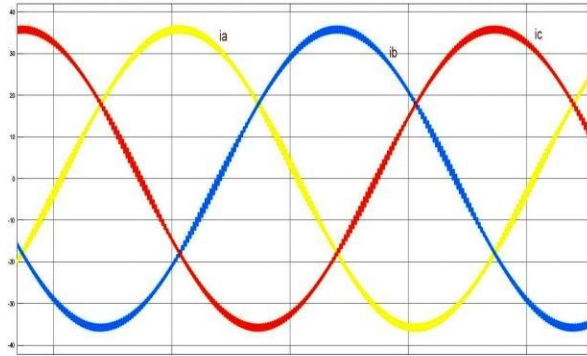


Fig.33 Output three phase current

Fig.32 shows voltage across input of inverter. In S.T. state it is zero because all the switches of inverter are turned on, in N.S.T. state it is sum of  $V_{C1}$  and  $V_{C2}$ , which is 423V, thus effective voltage across input increases and we get boosted voltage at input of inverter and desired ac output voltage  $230V_{LL}$ . Figure 33 shows three phase ac load current. Fig. 33.1 shows open loop  $V_{C2}$  and  $i_{L1}$  response. By analyzing transient state, we need closed loop control.

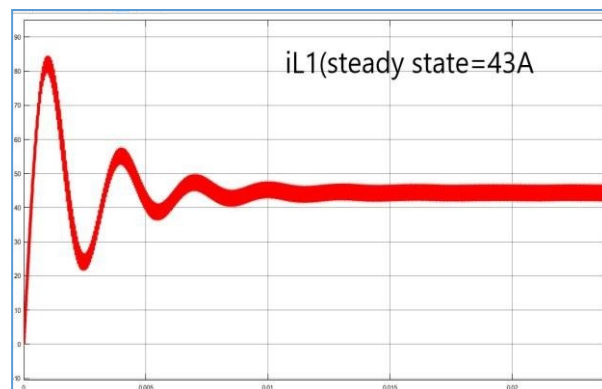
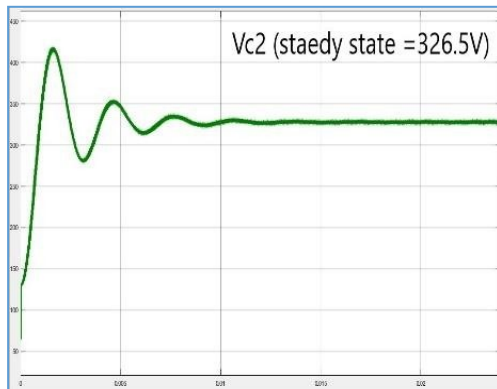


Fig.33.1  $V_{C2}$  and  $i_{L1}$  Open loop response

# Chapter 7

## Feedforward-Feedback control for DC Side QZSI

### 7.1 Introduction

Feedforward uses the measurement of an input disturbance to the plant as additional information for enhancing single-loop PID control performance. This measurement provides an “early warning” that the controlled variable will be upset some time in the future. With this warning the feedforward controller has the opportunity to adjust the manipulated variable (duty ratio here) before the controlled variable (voltage or current here) deviates from its set point [6]. Note that the feedforward controller does not use an output of the process. This is the first example of a controller that does not use feedback control; hence the new name feedforward. Feedforward is usually combined with feedback so that important features of feedback are retained in the overall strategy.

Comparison of feedforward and feedback principles

|            | Feedforward   | Feedback                          |
|------------|---|-----------------------------------|
| advantages | Compensates for a disturbance before the process output is affected | Provides zero steady state offset |
|            | Does not affect the stability of the control system                 | Effective for all disturbance     |

|               |  |  |
|---------------|--|--|
| Disadvantages | Cannot eliminate steady state offset             | Does not take control action until the process output variable has deviated from its set point |
|               | Requires a sensor and model for each disturbance | Affects the stability of the closed loop control system  |

Table 3. Advantages and Disadvantages of Feedback and Feedforward control

The feedforward controller ensures perfect control, if the models used are perfect or the measured disturbance is the only disturbance experienced by the process. Neither of conditions 1 or 2 is generally satisfied. Therefore feedforward control is always combined with feedback control.

Equation for Inductors and Capacitors during shoot through State

$$L_1 \frac{di_{L1}}{dt} = V_{in} + V_{C1} \quad (22)$$

$$L_2 \frac{di_{L2}}{dt} = V_{C2} \quad (23)$$

$$C_1 \frac{dv_{C1}}{dt} = -i_{L1} \quad (24)$$

$$C_2 \frac{dv_{C2}}{dt} = -i_{L2} \quad (25)$$

Equation for Inductors and Capacitors during non-shoot through State

$$L_1 \frac{di_{L1}}{dt} = V_{in} - V_{C2} \quad (26)$$

$$L_2 \frac{di_{L2}}{dt} = -V_{C1} \quad (27)$$

$$C_1 \frac{dv_{C1}}{dt} = i_{L2} - i_o \quad (28)$$

$$C_2 \frac{dv_{C2}}{dt} = i_{L1} - i_o \quad (29)$$

Multiplying Shoot through equations with d and non-shoot through equations with (1-d) and add

$$L_1 \frac{di_{L1}}{dt} = V_{in} + (V_{c1} + V_{c2})d - V_{c2} \quad (30)$$

$$C_2 \frac{dv_{c2}}{dt} = -i_{L2}d + (i_{L1} - i_o)(1 - d) \quad (31)$$

$$\frac{L_1}{(V_{c1} + V_{c2})} \frac{di_{L1}}{dt} + \frac{V_{c2} - V_{in}}{(V_{c1} + V_{c2})} = d \quad (32)$$

$$\frac{C_2}{(1 - 2d)} \frac{dv_{c2}}{dt} + \frac{i_o(1 - d)}{(1 - 2d)} = i_{L1} \quad (33)$$

From above equations(32,33) first terms are output of controller and second terms are feedforward terms. Inner current loop controls  $i_{L1}$  and outer voltage loop controls  $v_{c2}$ . Bandwidth of outer loop should be less than 1/10 of inner loop. For first equation,  $i_{L1}$  and  $d$  are taken variables, others are constant. For second equation,  $V_{c2}$  and  $i_{L1}$  are taken as variable, others as constant.

## 7.2 Controller Design

First we need to design inner current loop. For feedforward control, equations are linearized and we get first order transfer function, thus controller design becomes easy. By state space analysis ,transfer functions we get of order 4, but controller design for them is complex[8]. Neglecting the feedforward term, Open loop transfer function  $\frac{i_{L1}(s)}{d(s)}$  becomes

$$\frac{i_{L1}(s)}{d(s)} = \frac{(V_{c1} + V_{c2})}{L_1 s} = \frac{K}{s} \text{ where } K = \frac{(V_{c1} + V_{c2})}{L_1} \quad (34)$$

Based on the design consideration discussed in last section,  $(V_{c1} + V_{c2}) = 423.6V$  and  $L_1 = 1540.6\mu H$ . First we will see, whether only proportional controller is sufficient or not. With Proportional controller coefficient ( $K_P$ ), Open loop transfer function becomes

$$\frac{i_{L1}(s)}{d(s)} = \frac{K_P(V_{c1} + V_{c2})}{L_1 s} = \frac{K}{s} \text{ where } K = \frac{K_P(V_{c1} + V_{c2})}{L_1} \quad (35)$$

Thus Closed loop transfer function

$$\frac{i_{L1}^*(s)}{i_{L1}} = \frac{K}{s + K} \quad (36)$$

Thus bandwidth for current loop

$$\omega_i = K = \frac{K_P(V_{C1} + V_{C2})}{L_1} \quad (37)$$

If  $\omega_i = 6000$  rad/s (less than 1/10 of switching frequency) ,  $K_P = 0.021843$

From Fig.34, it is clear that only  $K_P$  is sufficient for inner loop controller design, thus we don't need to add  $K_I$ , since  $i_{L1}$  steady state error is very less.

Now we will see outer loop controller design. Outer loop bandwidth will be less than 1/10 of inner loop, thus it will see inner loop as constant equal to unity. From eq.38 outer loop OLTF is

$$\frac{v_{C2}(s)}{i_{L1}(s)} = \frac{1 - 2d}{C_2 s} \quad (38)$$

First we will see, whether only proportional controller is sufficient or not. with Proportional controller coefficient ( $K_P$ ) , Open loop transfer function becomes

$$\frac{v_{C2}(s)}{i_{L1}(s)} = \frac{K_P(1 - 2d)}{C_2 s} = \frac{K}{s} \text{ where } K = \frac{K_P(1 - 2d)}{C_2} \quad (39)$$

Thus Closed loop transfer function

$$\frac{v_{C2}^*(s)}{v_{C2}(s)} = \frac{K}{s + K} \quad (40)$$

Bandwidth for outer loop  $\omega_v = K = \frac{\omega_i}{10} = 600$  rad/s. here  $d = 0.2281$  and  $C_2 = 114.6 \mu F$  gives  $K_P = 0.1264$ . From Fig.35 ,it is clear, that only proportional controller is not sufficient ,because steady state error is very high(10% here). Thus we will use proportional plus integral (PI) controller ( $K_P + \frac{K_I}{s}$ ). with PI controller coefficient ( $K_P$  and  $K_I$ ) , Open loop transfer function becomes

$$\frac{v_{C2}^*(s)}{i_{L1}(s)} = \frac{(K_P + \frac{K_I}{s})(1 - 2d)}{C_2 s} = \frac{(K_P + \frac{K_I}{s})}{C'_2 s} \text{ where } C'_2 = \frac{C_2}{1 - 2d} \quad (41)$$

Closed loop transfer function becomes

$$\frac{v_{C2}^*(s)}{v_{C2}(s)} = \frac{K_P s + K_I}{s^2 + \frac{K_P}{C'_2} s + \frac{K_I}{C'_2}} \quad (42)$$

For second order system, with critical damping response, damping ratio ( $\epsilon$ ) =1 gives fastest response without overshoot.

$$\text{Bandwidth } (\omega_v) = \frac{1}{\text{Time constant}} = \sqrt{\frac{K_I}{C'_2}} \text{ and } 2\epsilon\omega_n = \frac{K_P}{C'_2} \quad (43)$$

After putting different values of bandwidth ( $\omega_v$ ), at  $\omega_v = 463 \text{ rad/s}$ ,  $K_P = 0.144$  and  $K_I = 45.2422$  gives best steady state and transient response. Fig 36

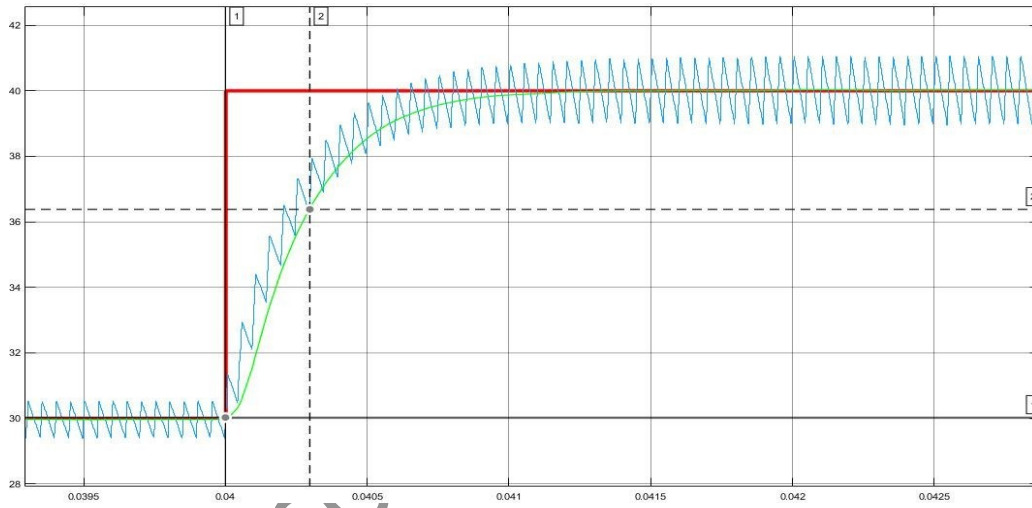


Fig.34 inner current loop step response

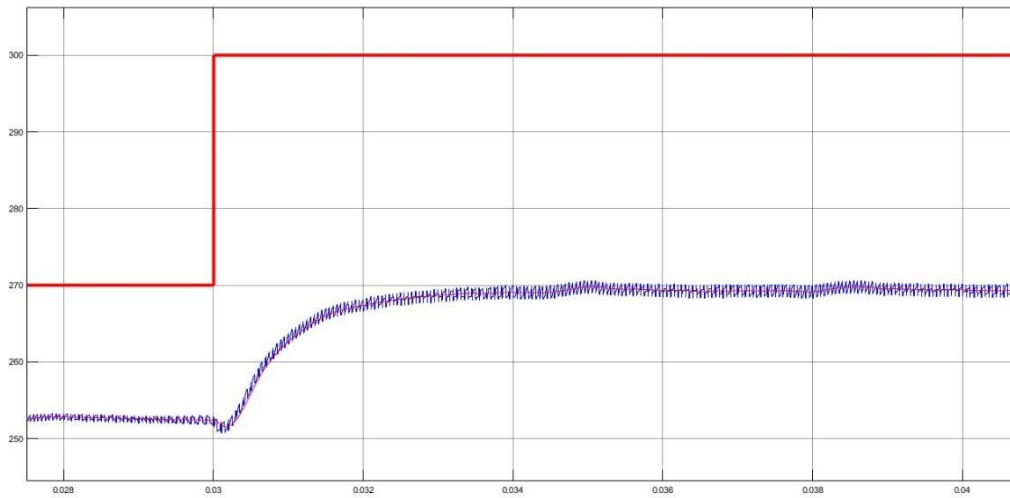


Fig.35 outer voltage loop response with only P controller



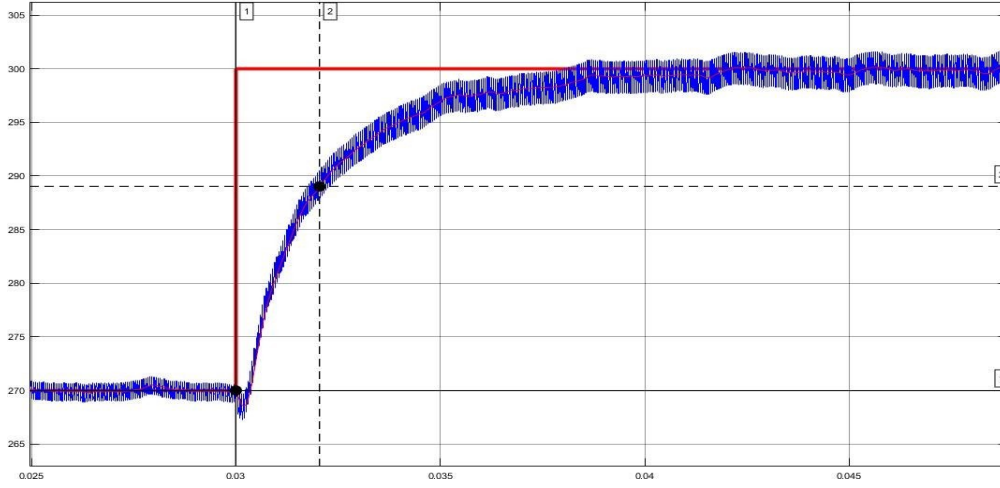
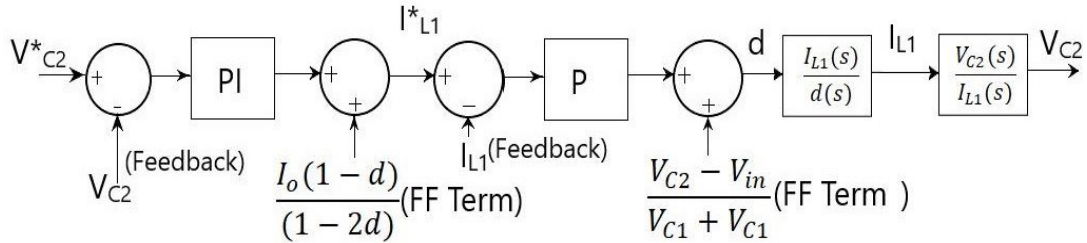


Fig.36 Outer voltage loop response with PI controller

Fig.37 shows current  $i_{L1}$  response, reference is step input, changing from 30A to 40A at 0.04s, time constant is 297us. Fig.34 shows voltage  $V_{C2}$  response with only P controller, reference is step input changing from 270V to 300V at 0.03s. steady state error is 10%, thus we need PI controller. Fig.35 shows voltage  $V_{C2}$  response with PI controller, thus steady state error is very less. Fig.36 shows block diagram of feedforward-feedback control.



$$\frac{V_{C2}(s)}{I_{L1}(s)} = \frac{1-2d}{C_2 s}$$

$$\frac{I_{L1}(s)}{d(s)} = \frac{V_{C1} + V_{C2}}{L_1 s}$$

Fig. 37 Feedforward Feedback control for QZSI

## Chapter 8

# Proposed Quasi Z source inverter with Soft Switching

### 8.1 Introduction

So far we have discussed Quasi Resonance DC Link Inverter for reduced  $dv/dt$  across inverter to decrease high frequency parasitic effects and for soft switching of Inverter switches and Quasi Z source inverter for voltage boosting, when input battery voltage is low and high speed operation is required. However, if we want above mentioned qualities to both topologies in one topology, the cascaded connection will increase total number of components, resulting a severe compromise to its size, cost, weight and complexity. In Quasi Z source inverter, the shoot through current is two times the inductor current, which contributes high voltage gradient ( $dv/dt$ ) across inverter, EMI noises and switching losses operating in the hard switching condition.

Proposed Quasi Z source inverter with soft switching is shown in Fig.36. Quasi resonance part, which is also auxiliary circuit is connected between Inverter and Quasi Z source for providing reduced  $dv/dt$  and soft switching of all switches of inverter [5]. Circuit shown in Fig.38 consists of five modes of operation. Each mode is explained below with equivalent circuit.

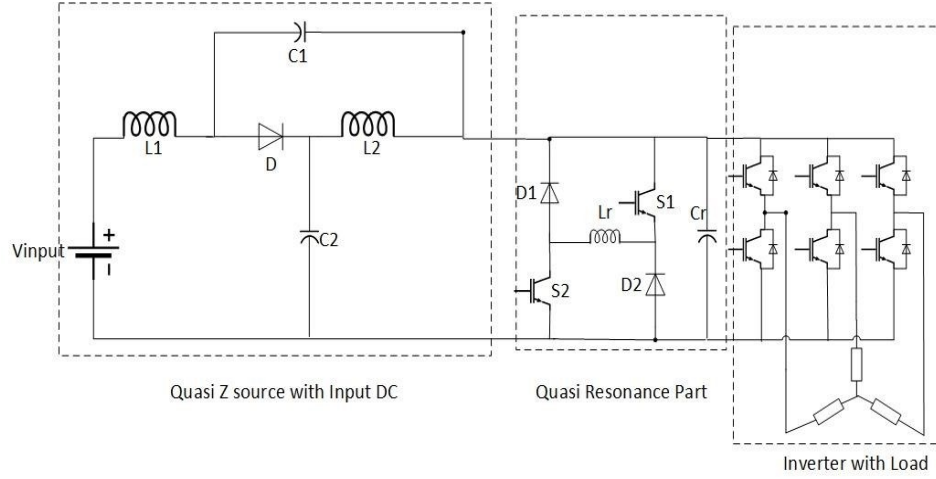


Fig.38 Proposed QZSI with soft switching

Simplified equivalent of topology in Fig.36 in one switching period is shown in Fig.37 (when inverter is feeding a load during one switching interval, load can be assumed as constant current source).  $S$  presents the inverter leg.  $S$  on is equivalent to all switches of inverter legs are on.  $S$  off represents normal operation of inverter. Five modes of operation are explained below.

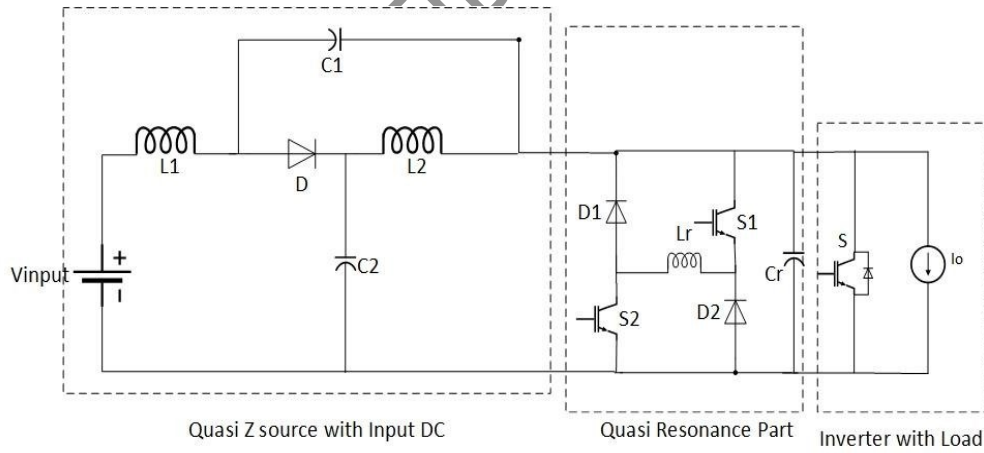


Fig.39 Equivalent circuit of QZSI with soft switching

## 8.2 Present Circuit and Operation

Quasi Z source operation will be same as discussed in last topology, here we will mainly discuss operation of quasi resonance part.

### Mode 0(M0)

In this mode inverter is in steady state. Switch  $S_1$ ,  $S_2$ ,  $S$  are off and diode  $D$  is on. Boosted voltage of Quasi Z source is applied to inverter input, which is sum of voltage across  $C_1$  and  $C_2$ . Diode  $D$  is on, because while going from shoot through to non shoot through,  $V_{Cr}$  gets charged, when  $V_{Cr} > (V_{C1} + V_{C2})$ , diode  $D$  becomes on.

$$i_D = i_{L1} + i_{L2} - I_o = 2i_L - I_o \quad (44)$$

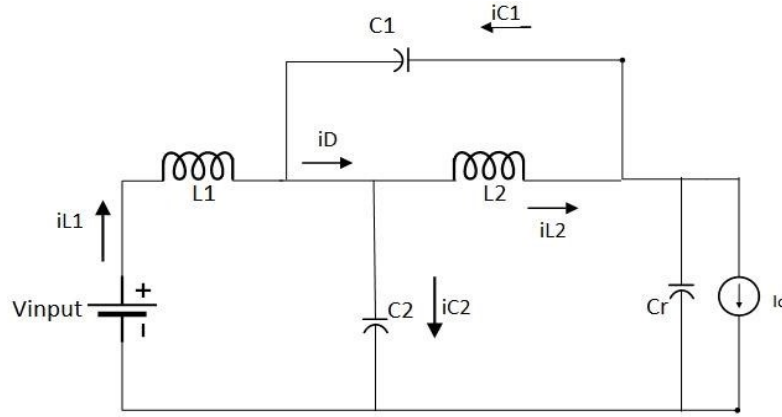


Fig.40 Equivalent circuit of Mode 0

### Mode I(M1)

Whenever any change in applied vector of inverter accordingly inverter leg switches has to change. In order to achieve reduced voltage gradient as well as ZVS of inverter switches, voltage across legs has to reduce to zero by resonance. Since voltage across inverter input ( $V_{cr}$ ) is clamped to  $V_{C1} + V_{C2}$ , first  $V_{cr}$  should be pulled down to zero by resonance, for that diode  $D$  should be turned off. Thus switches  $S_1$  and  $S_2$  from auxiliary circuit are tuned on under Zero current switching (ZCS) some time before active vector transition under Zero switching condition (ZVS) simultaneously with same gate pulse, such that current through diode is pulled down to zero and then  $V_{cr}$  can be reduced to zero by resonance.

$$i_D = i_{L1} + i_{L2} - I_o - i_{Lr} = 2i_L - I_o - i_{Lr} \quad (45)$$

When  $i_{Lr}$  is increased sufficiently such that,  $(I_o + i_{Lr}) > 2i_L$ , diode D turns off.

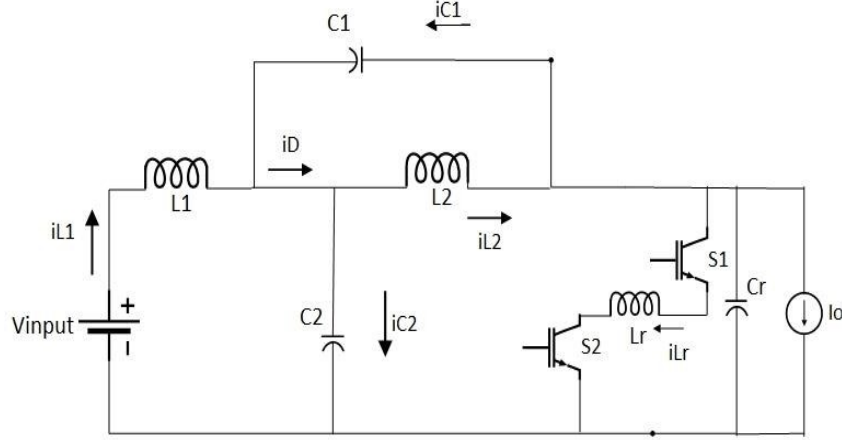


Fig.41 Equivalent circuit of Mode 1

### Mode II(M2)

Now capacitor  $C_r$  is not clamped to  $V_{C1} + V_{C2}$ , and it starts giving its energy to inductor  $L_r$ . At the end of Mode II,  $V_{cr}$  becomes zero by resonance with reduced  $dv/dt$ .

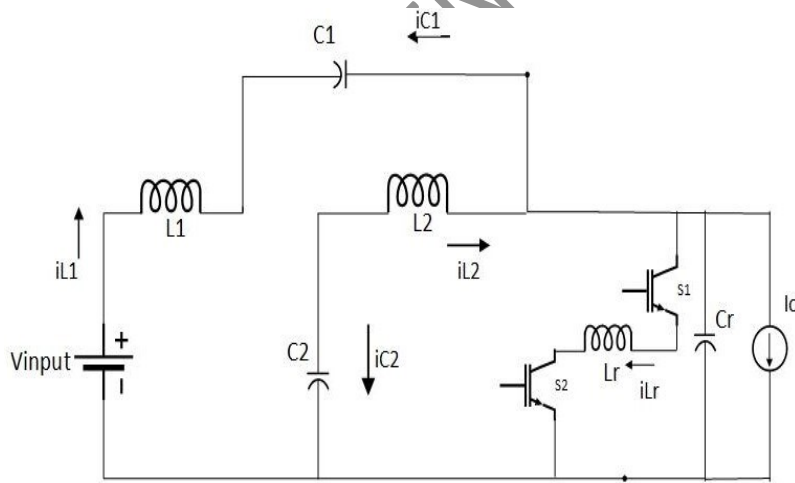


Fig.42 Equivalent circuit of Mode 2

### Mode III(M3)

Since  $V_{cr}$  has become zero with reduced voltage gradient, antiparallel diode of inverter switches are turned on and in this situation, all switches of inverter can be turned on under zero voltage switching condition(ZVS). This mode has adjustable time period

according to how much boost, QZS circuit required for voltage boost. In this mode Capacitors of QZS gives energy to inductors of QZS and  $i_{L1}$  and  $i_{L2}$  increases.

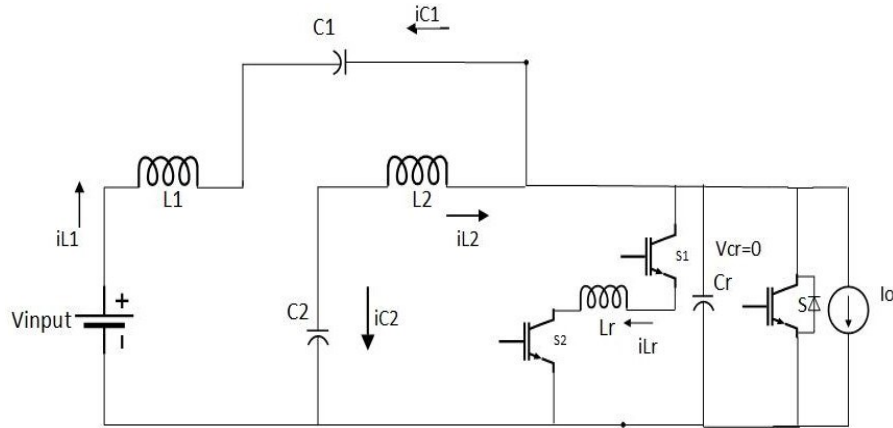


Fig.43 Equivalent circuit of Mode 3

#### Mode IV(M4)

To apply new switching state, and to recharge  $C_r$  again to  $V_{C1}+V_{C2}$  by resonance with reduced  $dv/dt$ , according to active vector respective inverter switches will be turned off, remaining switches are kept on, switch  $S$  as well as  $S_1S_2$  is turned off under ZVS in equivalent circuit. Now  $i_{Lr}$  starts flowing from  $D1$  and  $D2$  and  $C_r$  is charged to  $V_{C1}+V_{C2}$ , thus diode  $D$  is turned on.

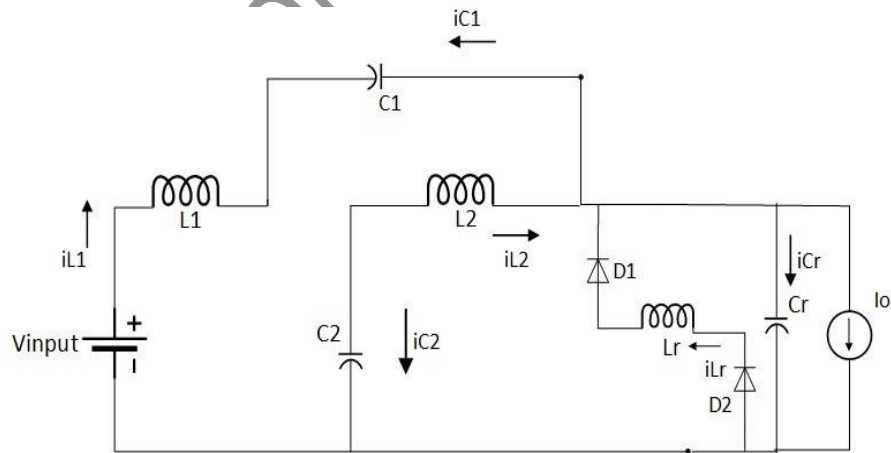


Fig.44 Equivalent circuit of Mode 4

#### Mode V(M5)

When  $V_{Cr} > (V_{C1} + V_{C2})$ , diode  $D$  gets forward biased, and boosted voltage applied to input of inverter. Diode  $D$  carried addition current flowing from  $L_r$ . Capacitor  $C_1$  and

$C_2$  gets more energy, but since  $L_r$  value is very low, its energy will be low and it does not affect boost operation much and that can be taken care by closed loop by adjusting duty ratio of shoot through time period. This mode ends with  $i_{Lr}$  becomes zero.

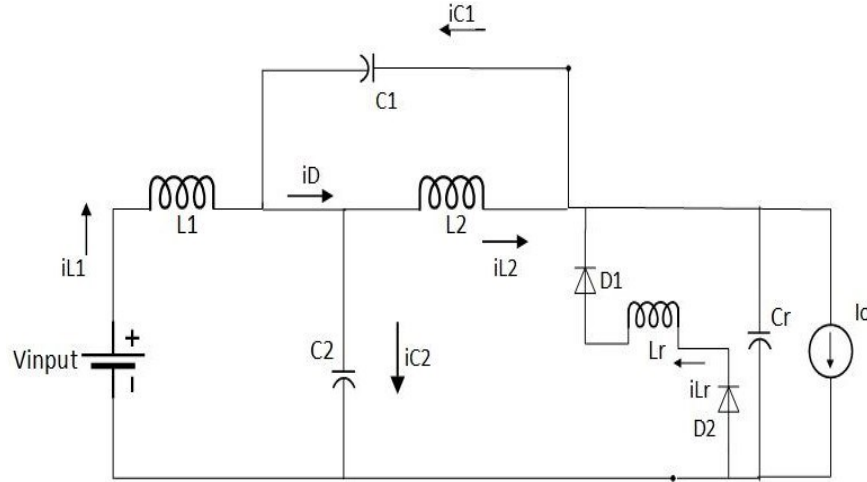


Fig.45 Equivalent circuit of Mode 5

### 8.3 Typical current and voltage waveform

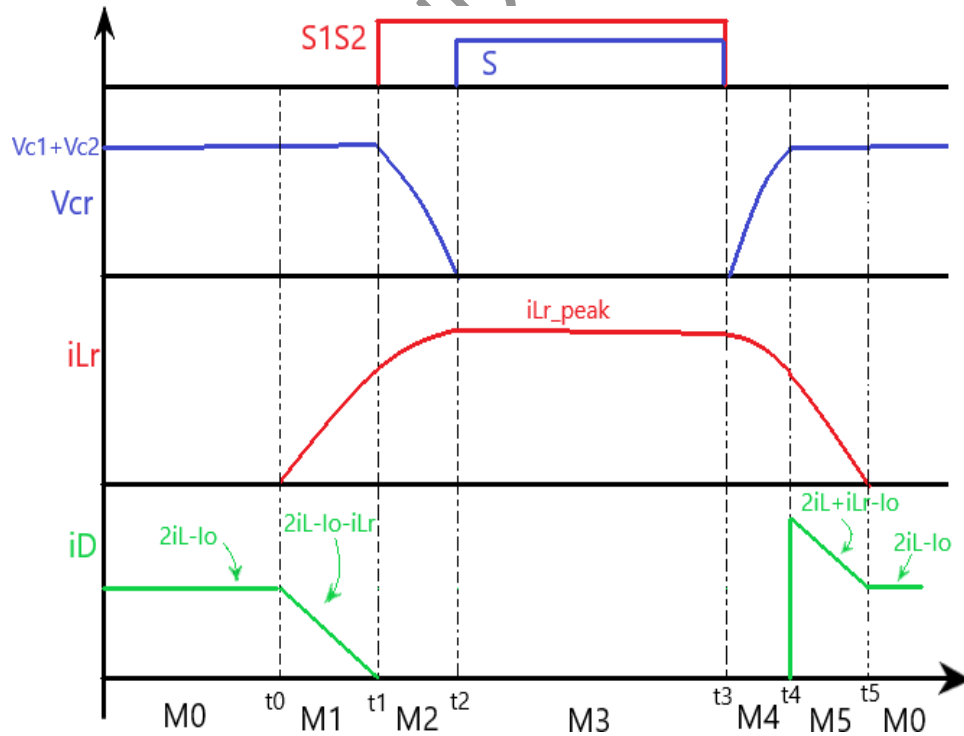


Fig. 46 Typical Voltage and current waveform

## 8.4 Simulation Parameters

| Parameters                | Value   |
|---------------------------|---------|
| Input DC Voltage          | 230V    |
| Inductor $L_1, L_2$       | 1540uH  |
| Capacitor $C_1, C_2$      | 114.6uF |
| Resonance Inductor $L_r$  | 4uH     |
| Resonance Capacitor $C_r$ | 30nF    |
| Load current $I_o$        | 30A     |
| Switching Frequency       | 10KHz   |
| Shoot through duty ratio  | 0.2     |

Table 4. Simulation Specifications for Proposed QZSI with soft switching

## 8.5 Simulation waveforms for QZSI with soft switching

Equivalent circuit of Proposed QZSI with soft switching was simulated in MATLAB 2017b. switching time period was 100us. shoot through duty ratio was 0.2, thus 20us shoot through period.

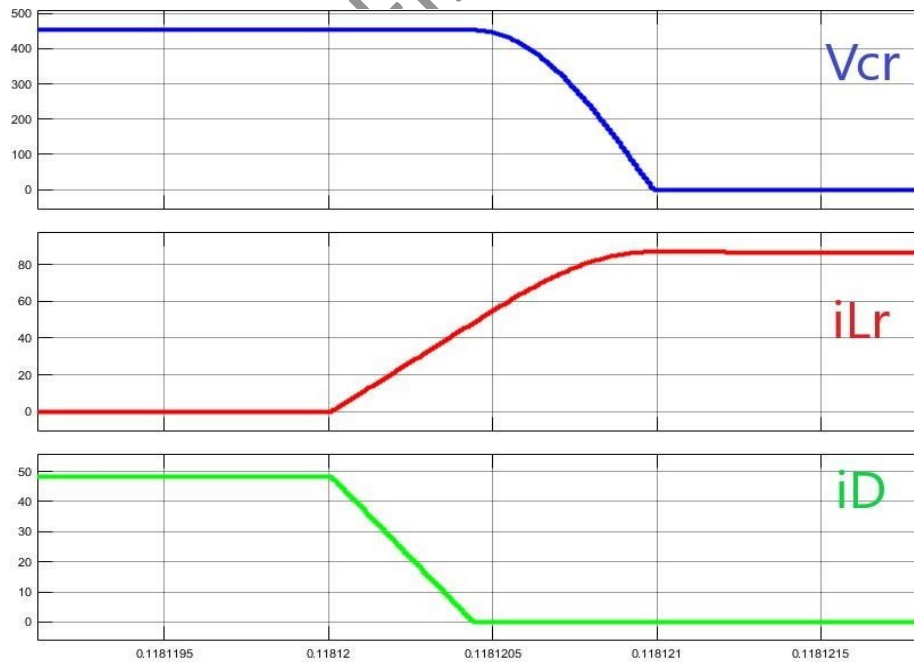


Fig.47 Waveforms during discharge of  $C_r$  voltage



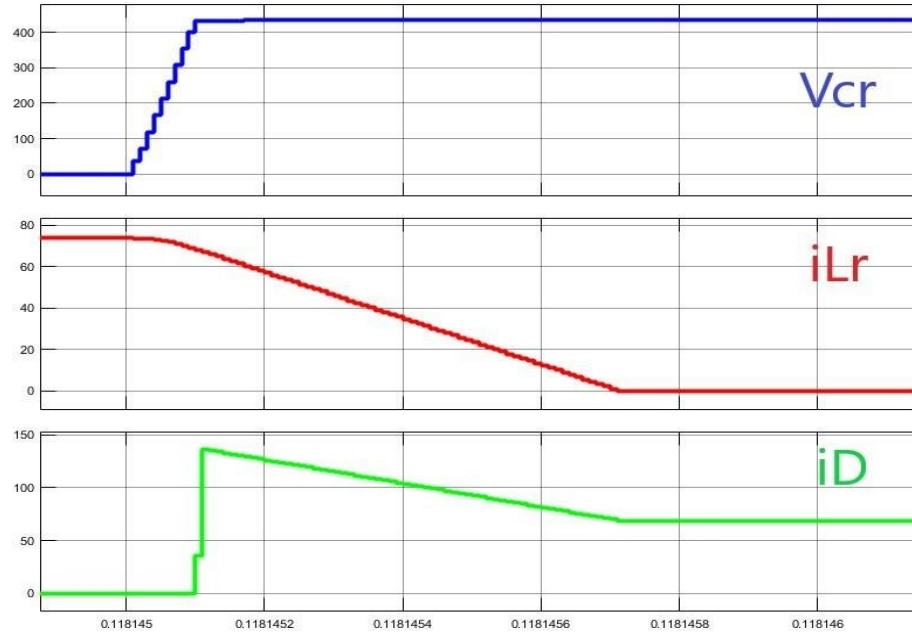


Fig.48 Waveforms during recharge of  $C_r$  voltage

Fig.47 shows discharge of capacitor  $C_r$ , maximum current flowing through  $L_r$  is 86.8A. Fig.48 shows recharge of capacitor  $C_r$ . according to QZS operation  $V_{C1} + V_{C2} = 390$ , but here it is 450V, because of extra energy provide by  $L_r$  during mode 5, but that will be taken care by closed loop control. From the figures during discharge of  $C_r$ , voltage gradient across inverter is 900V/us and during recharge, it is around 3000V/us. By changing resonance elements, we can change voltage gradients as well as resonance time duration. THD of line current will decrease for Proposed QZSI with soft switching compared to QZSI.

# Chapter 9

## Conclusion and Future works

### Conclusion

Quasi Resonance DC Link inverter was designed and simulated for reduced voltage gradient and lossless switching. A modified SVPWM technique is used to improve DC bus utilization. Problem with excess voltage stress across resonance switches was solved using modified topology and switch voltages were clamped to DC bus voltage using voltage clamping circuit.

Quasi Z source inverter was designed and simulated for voltage boosting for high speed operation of drive without using additional switch at the input. SVPWM technique was used for PWM and shoot through period was provided for minimum null vector duration in any of the switching time period of SVPWM. Thus desired AC output voltage was obtained. Quasi Z source inverter with soft switching was proposed, which provides desired voltage boosting as well as reduced voltage gradient to reduce EMI interferences and soft switching. The operations of all the topologies were verified in simulation software, ensures suitable, efficient and reliable for an EV application

### Scope for future works

Open loop control is performed for QRDCL inverter and QZSI with soft switching and closed loop Feedforward-Feedback control is performed for DC Side QZS inverter in simulation platforms. Future extension of this project will be practical implementation of all the topologies for PMSM and induction motor drives.

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