

Question

The maximum and minimum magnitudes of the resultant of two forces are 35 N and 5 N respectively. Find the magnitude of resultant force when act orthogonally (Perpendicularly) to each other.

$$\begin{aligned} A + B &= 35 \\ A - B &= 5 \end{aligned}$$

$$\begin{aligned} A &= 20 \\ B &= 15 \end{aligned}$$

$$Ans = \sqrt{20^2 + (5)^2} = 5 \times 5 = 25$$

Question



Two equal forces (P each) act at a point inclined to each other at an angle of 120° .
The magnitude of their resultant is

$$= \sqrt{P^2 + P^2 + 2 \cdot P \cdot P \cdot \cos 120^\circ}$$

A $\frac{P}{2}$

B $\frac{P}{4}$

C P

D $2P$

Ans : (C)

Question



Maximum and minimum magnitudes of the resultant of two vectors of magnitudes P and Q are in the ratio 3 : 1. Which of the following relations is true?

A

$$P = 2Q$$

B

$$P = Q$$

C

$$PQ = 1$$

D

None of these

$$\frac{P+Q}{P-Q} = \frac{3}{1}$$

$$P + Q = 3P - 3Q$$

$$4Q = 2P$$

$$P = 2Q$$

Ans : (A)

Question

For the resultant of the two vectors to be maximum, what must be the angle between them

- A 0°
- B 60°
- C 90°
- D 180°

Ans : (A)

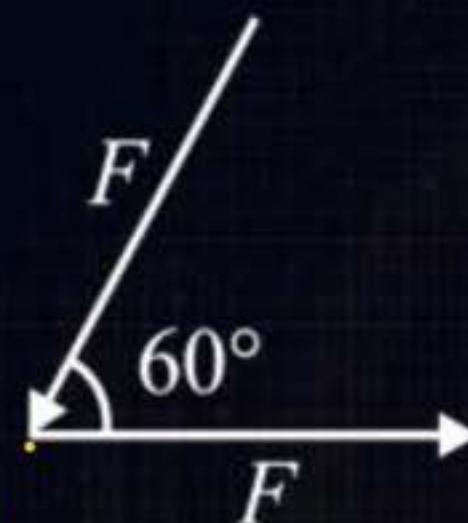
Question

Two forces, each numerically equal to 5 N, are acting as shown in the figure. Then the resultant is

- A 2.5 N
- B 5 N
- C $5\sqrt{3}\text{ N}$
- D 10 N

$$\begin{aligned} F_{\text{net}} &= \sqrt{5^2 + 5^2 + 2 \times 5 \times 5 \cos 60^\circ} \\ &= \sqrt{25 + 25 + 25} = 5\sqrt{3} \end{aligned}$$

$$\begin{aligned} F_{\text{net}} &= \sqrt{5^2 + 5^2 + 2 \times 5 \times 5 \cos 120^\circ} \\ &= 5 \end{aligned}$$



(B)

Ans : (C)

Question

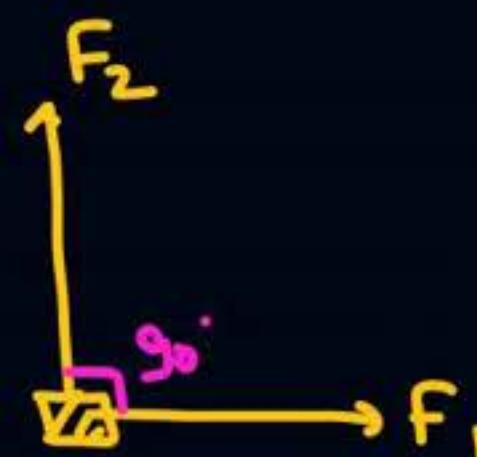
Force F_1 and F_2 act on a point mass in two mutually perpendicular directions. The resultant force on the point mass will be

A $F_1 + F_2$

B $F_1 - F_2$

C $\sqrt{F_1^2 + F_2^2}$

D $F_1^2 + F_2^2$



Ans : (C)

Question

Class Notes

The sum of magnitude of two force \vec{A} and \vec{B} acting at a point is 16 N. If their resultant has magnitude 8 N and direction of resultant is perpendicular to \vec{A} . Find Magnitude of \vec{A} and \vec{B} .

- A 6 N and 10 N
- B 8 N and 8 N
- C 4 N and 12 N
- D 2 N and 14 N

Ans : (A)

Question

The vector sum of the forces of 10 newton and 6 newton can be:

- A 2 N
- B 8 N
- C 18 N
- D 20 N

$$C_{\max} = 10 + 6 = 16$$

$$C_{\min} = 10 - 6 = 4$$

$$4 < C < 16$$

Ans : (B)

Question

Which of the following pair of forces will never give a resultant force of 2 N?

A 2 N and $2\text{ N} \Rightarrow 0 \leq C \leq 4$

B 1 N and $1\text{ N} \Rightarrow 0 \leq C \leq 2$

C 1 N and $3\text{ N} \Rightarrow 2 \leq C \leq 4$

D 1 N and $4\text{ N} \Rightarrow 3 \leq C \leq 5$

Ans D

Ans : (D)

Question



If three forces $\vec{F}_1 = \underline{3i} - 4\hat{j} + 5\hat{k}$, $\vec{F}_2 = \underline{-3i} + 4\hat{j}$.and $\vec{F}_3 = 5\hat{k}$ are acted on a body, then the direction of resultant force on the body is:

A Along x-axis

$$\vec{F}_{\text{net}} = 0\hat{i} + 0\hat{j} + 10\hat{k}$$

B Along y-axis

$$\vec{F}_{\text{net}} = 10\hat{k}$$

C ✓ Along z-axis

D In indeterminate form

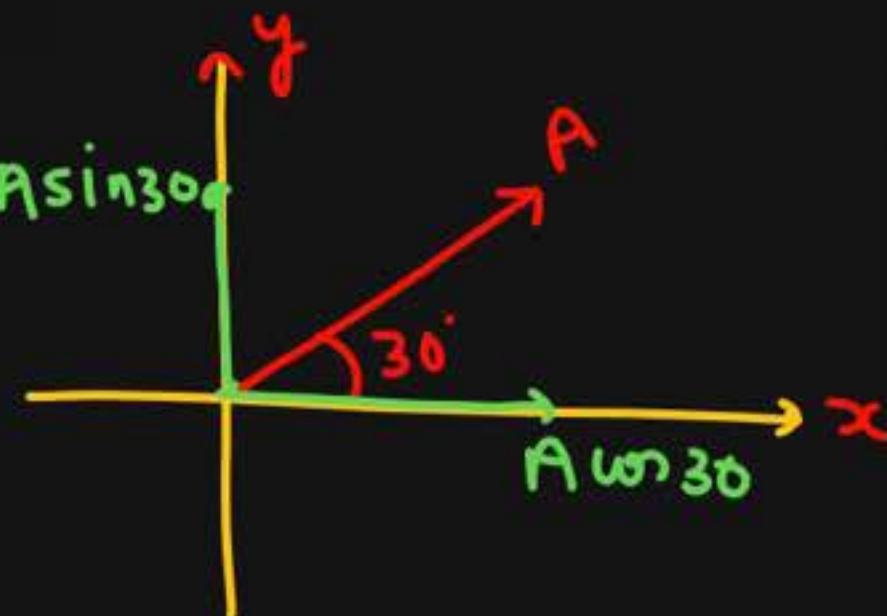
Ans. (C)

Question

P
W

A vector lying in x-y plane has a magnitude $\underline{3}$, and makes an angle 30° with the x-axis. Find its components along X axis and Y axis respectively.

- A $\frac{3}{2}, \frac{\sqrt{3}}{2}$
- B $\frac{3}{2}, \frac{3\sqrt{3}}{2}$
- C $\frac{\sqrt{3}}{2}, \frac{3}{2}$
- D $\frac{3\sqrt{3}}{2}, \frac{3}{2}$



$$\begin{aligned}\vec{A} &= 3 \cos 30 \hat{i} + 3 \sin 30 \hat{j} \\ &= 3 \frac{\sqrt{3}}{2} \hat{i} + \frac{3}{2} \hat{j}\end{aligned}$$

Ans. (D)

Question

P
W

$$d_1 =$$

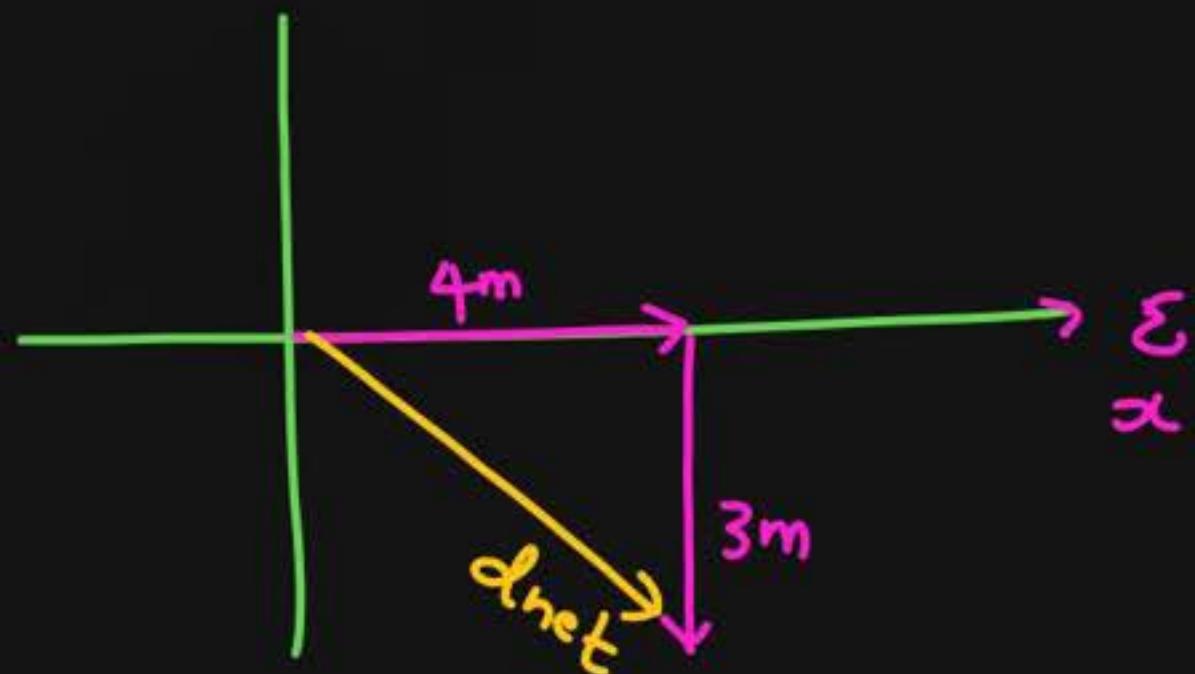
A boy walks 4 m east and then 3 m south. Find the resultant displacement of the boy.

$$d_1 = 4\hat{i}$$

$$\vec{d}_2 = -3\hat{j}$$

$$\vec{d} = 4\hat{i} - 3\hat{j}$$

- A 4 m
- B 5 m
- C 7 m
- D 3 m



Ans. (B)

Question



If a particle moves from point $P(2, 3, 5)$ to point $Q(3, 4, 5)$. Its displacement vector be

$$\overrightarrow{PQ} = \hat{i} + \hat{j}$$

- A $\hat{i} + \hat{j} + 10\hat{k}$
- B $\hat{i} + \hat{j} + 5\hat{k}$
- C $\hat{i} + \hat{j}$
- D $2\hat{i} + 4\hat{j} + 6\hat{k}$

Ans. (C)

Question

P
W

$\vec{A} = 2\hat{i} + \hat{j}$, $B = 3\hat{j} - \hat{k}$ and $\vec{C} = 6\hat{i} - 2\hat{k}$. Value of $\underline{\underline{\vec{A} - 2B + 3C}}$ would be

$$-2\vec{B} = -6\hat{j} + 2\hat{k}$$

$$3\vec{C} = 18\hat{i} - 0\hat{j} - 6\hat{k}$$

A $20\hat{i} + 5\hat{j} + 4\hat{k}$

B ~~$20\hat{i} - 5\hat{j} - 4\hat{k}$~~

C $4\hat{i} + 5\hat{j} + 20\hat{k}$

D $5\hat{i} + 4\hat{j} + 10\hat{k}$

Ans. $\Rightarrow 20\hat{i} - 5\hat{j} - 4\hat{k}$

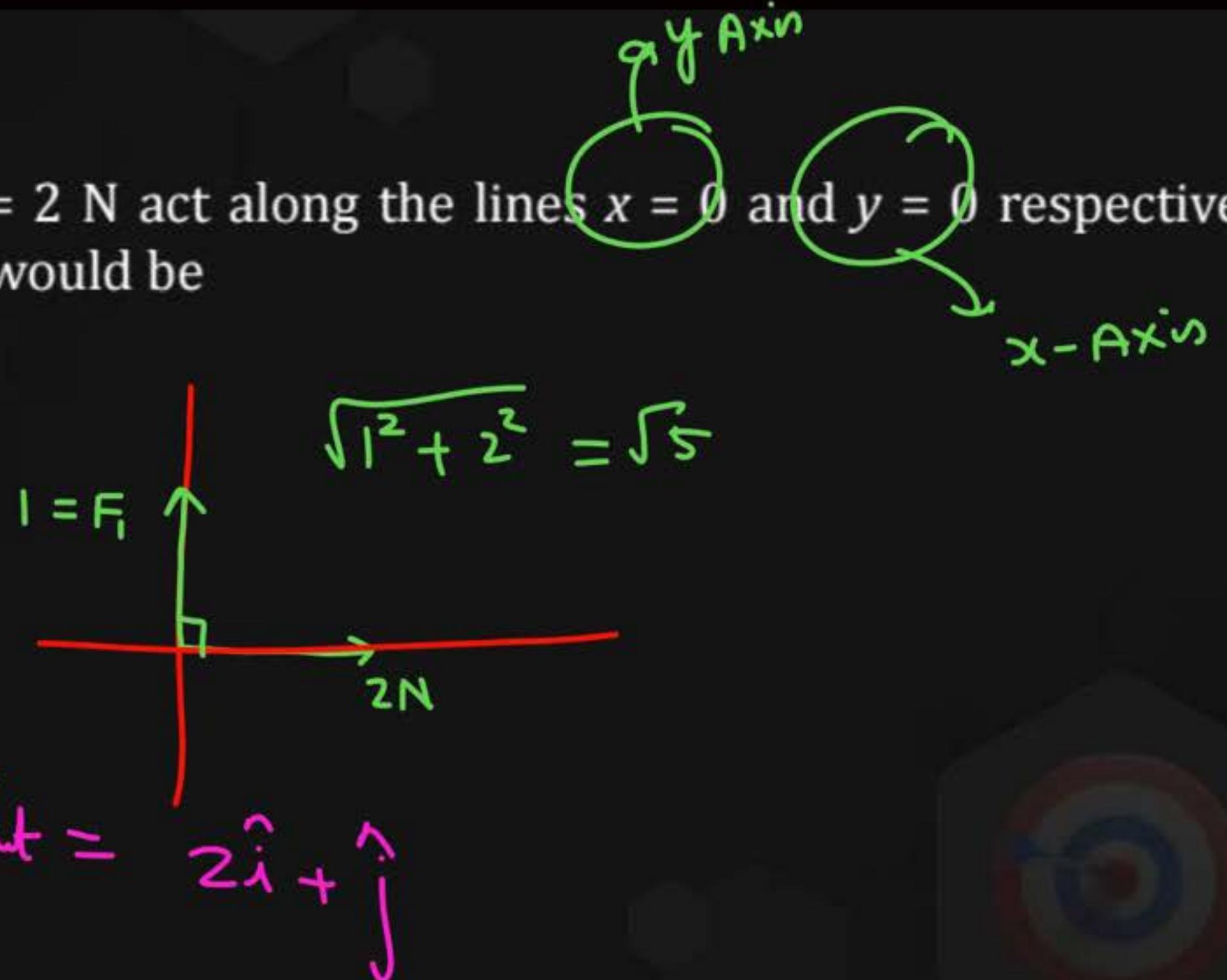
Ans. (B)

Question

P
W

Two force $F_1 = 1 \text{ N}$ and $F_2 = 2 \text{ N}$ act along the lines $x = 0$ and $y = 0$ respectively.
Then the resultant of forces would be

- A $\hat{i} + 2\hat{j}$
- B $\hat{i} + \hat{j}$
- C $3\hat{i} + 3\hat{j}$
- D $2\hat{i} + \hat{j}$



Ans. (D)

Question



Following forces starts acting on a particle at rest at the origin of the co-ordinate system simultaneously

$$\vec{F}_1 = -4\hat{i} - 5\hat{j} + 5\hat{k}, \vec{F}_2 = 5\hat{i} + 8\hat{j} + 6\hat{k},$$
$$\vec{F}_3 = -3\hat{i} + 4\hat{j} - 7\hat{k} \text{ and } \vec{F}_4 = 2\hat{i} - 3\hat{j} - 2\hat{k}$$

then the particle will move

$$\vec{F}_{\text{net}} = 0\hat{i} + 4\hat{j} + 2\hat{k}$$

y, z

- A In x-y plane
- B In y-z plane
- C In x-z plane
- D Along x-axis

Ans. (B)

Question



The vector sum of the forces of 10 newton and 6 newton can be:

A

2 N



B

8 N



C

18 N



D

20 N



$$10 - 6 \leq C \leq 10 + 6$$

$$4 \leq C \leq 16$$

Ans. (B)

Question



The unit vector along $\hat{i} + \hat{j}$ is :

A \hat{k}

B $\hat{i} + \hat{j}$

C $\frac{\hat{i} + \hat{j}}{\sqrt{2}}$

D $\frac{\hat{i} + \hat{j}}{2}$

C $\frac{\hat{i} + \hat{j}}{\sqrt{2}}$

Ans. (C)

Question



The unit vector parallel to the resultant of the vectors $\vec{A} = 4\hat{i} + 3\hat{j} + 6\hat{k}$ and $\vec{B} = -\hat{i} + 3\hat{j} - 8\hat{k}$ is:

A

$$\frac{1}{7}[3\hat{i} + 6\hat{j} - 2\hat{k}]$$

B

$$\frac{1}{7}[3\hat{i} + 6\hat{j} + 2\hat{k}]$$

C

$$\frac{1}{49}[3\hat{i} + 6\hat{j} + 2\hat{k}]$$

D

$$\frac{1}{49}[3\hat{i} + 6\hat{j} - 2\hat{k}]$$

$$\vec{A} + \vec{B} = 3\hat{i} + 6\hat{j} - 2\hat{k} = \vec{C}$$

$$\hat{C} = \frac{3\hat{i} + 6\hat{j} - 2\hat{k}}{\sqrt{3^2 + 6^2 + 2^2}}$$

Ans. (A)

Question

If $\vec{A} + \vec{B}$ is a unit vector along x -axis and $\underline{\vec{A} = \hat{i} - \hat{j} + \hat{k}}$, then what is \vec{B} ?

A $\hat{j} + \hat{k}$

B $\hat{j} - \hat{k}$

C $\hat{i} + \hat{j} + \hat{k}$

D $\hat{i} + \hat{j} - \hat{k}$

$$\begin{aligned}\vec{A} + \vec{B} &= \hat{i} \\ \cancel{\hat{i} - \hat{j} + \hat{k}} + \vec{B} &= \cancel{\hat{i}} \\ \underline{\vec{B}} &= \underline{\hat{j} - \hat{k}}\end{aligned}$$

Ans. (B)

Question



The vectors $5\hat{i} + 8\hat{j}$ and $2\hat{i} + 7\hat{j}$ are added. The magnitude of the sum of these vector is

A $\sqrt{274}$

B 38

C 238

D 560

$7\hat{i} + 15\hat{j}$

$\sqrt{7^2 + (15)^2}$

$$\begin{array}{r} 49 \\ 225 \\ \hline 274 \end{array}$$

Ans. (A)

Question

Q

P
W

A particle is in a unidirectional potential field where the potential energy (U) of a particle depends on the x -coordinate given by $U_x = k(1 - \cos ax)$ & k and ' a ' are constants. Find the physical dimensions of ' a ' & k .

$$U(x) = k - k \cos ax$$

Pot. Energy

U

$$m L^2 T^{-2}$$

$$aL = 1$$

$$a = L^{-1}$$

Ans - L^1
 $m L^2 T^{-2}$

Question

②



The time period (T) of a spring mass system depends upon mass (m) and spring constant (k) and length of the spring (l) [$k = \frac{\text{Force}}{\text{Length}}$]. Find the relation among T, m, l and k using dimensional method.

$$T \propto m^x k^y l^z$$

$$m^0 L^0 T^1 = m^x (m T^{-2})^y L^z$$

$$m^0 L^0 T^1 = m^{x+y} L^z T^{-2y}$$

$$-2y = 1$$

$$y = -\frac{1}{2}$$

$$k \equiv \frac{m L T^{-2}}{L}$$

$$k \equiv m^0 L^0 T^{-2}$$

$$\boxed{x=0}$$

$$x+y=0$$

$$x - \frac{1}{2} = 0$$

$$\boxed{x = \frac{1}{2}}$$

$$\underline{\text{Ans}} \quad T = \alpha \sqrt{\frac{m}{k}}$$

$$\underline{\text{Ans}} \quad T = k' m^{\frac{1}{2}} k^{-\frac{1}{2}} l^0$$

$$T = k' \frac{\sqrt{m}}{\sqrt{k}} = k' \sqrt{\frac{m}{k}}$$

A satellite is orbiting around a planet. Its orbital velocity (v_0) is found to depend upon

- (A) Radius of orbit (R)
- (B) Mass of planet (M)
- (C) Universal gravitation constant (G)

Class Notes
Check

$$V_0 = K \sqrt{\frac{GM}{R}}$$

$$V_0 \propto R^x M^y G^z$$

: : : :
x y z

Question

④



A assume that the largest stone of mass ' m ' that can be moved by a flowing river depends upon the velocity of flow v , the density d and the acceleration due to gravity g . If ' m ' varies as the K^{th} power of the velocity of flow, then find the value of K .

$$m \propto v^K d^l g^m$$

$$(L T^{-1})^K (M L^{-3})^l (L T^{-2})^m$$

$$M^1 L^0 T^0 = M^l L^{K-3l+m} \cdot T^{-K-2m}$$

Compare

$$l=1$$

$$K=6$$

$$-K-2m = 0 \Rightarrow -K = 2m$$

$$K-3l+m = 0$$

$$m = -\frac{K}{2}$$

$$K-3 \times 1 + m = 0$$

$$K+m = 3$$

$$K - \frac{K}{2} = 3$$

$$\frac{K}{2} = 3 \Rightarrow K = 6$$

Which of the following functions of A and B may be performed if A and B possess different dimensions?

- A $\frac{A}{B}$ ✓
- B $A + B$ ✗
- C $A - B$ ✗
- D None of these

Ans (A)

Question

⑥



The velocity v of a particle at time t is given by $v = at + \frac{b}{t+c}$, where a , b and c are constants. The dimensions of a , b and c are respectively:-

A

 ~~LT^{-2}, L and T~~

B

 L^2, T and LT^2

C

 LT^2, LT and L

D

 L, LT and T^2

$at \longrightarrow$ velocity

$$aT = LT^{-1}$$

$$a = LT^{-2}$$

$$c = T$$

$\frac{b}{t+c} \longrightarrow$ Velocity

$$\frac{b}{T} = LT^{-1}$$

$$b = L$$

Ans (A)

If area (A), velocity (v), and density (ρ) are base units, then the dimensional formula of force can be represented as:-

~~A~~ $Av\rho$ $\xrightarrow{L^2 \cdot LT^{-1} \cdot \frac{m}{L^3} = MLT^{-2}}$

B $Av^2\rho$ $\xrightarrow{L^2 \cdot (LT^{-1})^2 \cdot \frac{m}{L^3} = MLT^{-2}}$ MLT^{-2} $=$ Force

C $Av\rho^2$

D $A^2v\rho$

Ans (B)

Question

(8)

P
W

F A T

If force, acceleration and time are taken as fundamental quantities, then the dimensions of length will be:

A

FT²

L

$$m L T^{-2} \cdot T^2 = m L$$

B

$$F^{-1} A^{-2} T^{-1} = \frac{1}{F A^2 T} = \frac{1}{m L T^{-2} (L T^{-2})^2 \cdot T} = \frac{1}{m L^3 T^{-5}}$$

C

FA²T

$$L T^{-2} \cdot T^2 = L$$

D

AT²

Ans (C)

P

Question



Find the value of

(i) $\cos(-60^\circ) = \cos 60^\circ = \frac{1}{2}$

(ii) $\tan 210^\circ = \tan(180^\circ + 30^\circ) = +\frac{1}{\sqrt{3}}$

(iii) $\sin 300^\circ$

(iv) $\boxed{\cos 120^\circ}$

\downarrow
 \downarrow
 \downarrow
 \downarrow

$\sin(360^\circ - 60^\circ) = -\frac{\sqrt{3}}{2}$

Ans. (i) $\frac{1}{2}$, (ii) $\frac{1}{\sqrt{3}}$, (iii) $-\frac{\sqrt{3}}{2}$, (iv) $-\frac{1}{2}$

Question



Use the approximation $(1 + x)^n \approx 1 + nx$, $|x| \ll 1$, to find approxima

(i) $\sqrt{99}$

(ii) $\frac{1}{1.01}$

$$\begin{aligned}\sqrt{100-1} &= (100-1)^{\frac{1}{2}} = [100(1-0.01)]^{\frac{1}{2}} = 10(1-0.01)^{\frac{1}{2}} \\ &= 10\left(1-\frac{1}{2} \times 0.01\right) \\ &= 10(1-0.005) \\ &= 10 \times 0.995 \\ &= \underline{9.95}\end{aligned}$$

Ans. (i) 9.95, (ii) 0.99

Question



$$m L^2 T^{-2}$$

In system called the star system we have 1 star kilogram = 10^{20} kg. 1 starmeter = 10^8 m, 1 starsecond = 10^3 s then calculate the value of 1 joule in this system.

$$1 J' = \frac{10^{20} \text{ kg} \cdot (10^8 \text{ m})^2}{(10^3 \text{ s})^2}$$

$$1 J' = 10^{30} \frac{\text{kg m}^2}{\text{sec}^2} = 10^{30} \text{ J}$$

$$\frac{1 J'}{10^{30}} = 1 J = 10^{-30} J'$$

Ans. (10^{-30} star joule)

Question

Find the approximate value of

(i) $(1.003)^3 = (1 + 0.003)^3 = 1.009$

(ii) $(1.003)^{-3} \rightarrow (1 + 0.003)^{-3} = 1 - 0.009 = .991$

(iii) $\left(\frac{1}{1.005}\right)^3$

(iv) $\sqrt{98}$ $\rightarrow (1.005)^{-3} = (1 + 0.005)^{-3} = 1 - 0.015 = .985$

Class $(100-z)^{\frac{1}{2}} = 10(1 - 0.02)^{\frac{1}{2}} = 10(1 - 0.01) = \underline{\underline{9.9}}$

Ans. (i) 1.009, (ii) .991, (iii) .985, (iv) 9.9

Question



Convert following into radian

- (i) 45°
- (ii) 60°
- (iii) 90°
- (iv) 120°
- (v) 150°

$$\frac{\pi}{180}$$

Class

$$45 \times \frac{\pi}{180} = \frac{\pi}{4}$$

Ans. (i) $\pi/4$, (ii) $\pi/3$, (iii) $\pi/2$, (iv) $2\pi/3$, (v) $5\pi/6$

Question



Convert following into degree $\pi = 180^\circ$ ✓

(i) $\frac{4\pi}{3}$

(ii) $\frac{8\pi}{3}$

(iii) 4π

$\frac{8 \times 180}{3} = 480^\circ$

Ans. (i) 240° , (ii) 480° , (iii) 720°

H/W

P.E.

$$\textcircled{1} \quad U = \frac{A\sqrt{x}}{B+x^2} \quad B = L^2$$

D.F. of A.B is

$$m L^2 T^{-2} = \frac{A L^{\frac{1}{2}}}{L^2} = A L^{3/2}$$

$$A = m L^{\frac{7}{2}} T^{-2}$$

$$m L^{\frac{7}{2}} T^{-2} L^2 = \checkmark$$

P
W

(2)

$$P = \frac{\alpha}{\beta} e^{-\frac{\alpha x}{kT}}$$

$k \rightarrow$ Boltzmann const
 $T \rightarrow$ temp.

$P \rightarrow$ pressure

KT की dim put कर
 $\frac{RTE}{2}$

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* JEE main 2025

$$\text{dim. } \gamma \frac{\alpha x}{kT} = 1$$

$$\frac{\alpha L}{mL^2 T^2} = 1 \Rightarrow \alpha = mL T^{-2}$$

$$U = \frac{3}{2} kT$$

$$kT = mL^2 T^{-2}$$

$$\alpha = mL T^{-2}$$

$$\frac{mLT^{-2}}{L^2} = \frac{\alpha}{\beta} = \frac{mLT^{-2}}{\beta}$$

$$\beta = L^2$$

P
W

check the following equation dimensionally

$$(a) h = \frac{\alpha s \cos \theta}{\gamma \cdot \rho g} \stackrel{?}{=} \frac{m L T^{-2}}{L L \frac{m}{L^3} L T^2} = L$$

$h \rightarrow$ height

$s \rightarrow$ surface tension = $\frac{F}{L}$

$\gamma \rightarrow$ radius

$\rho \rightarrow$ density

$g \rightarrow$ acceleration due to gravity

$T^{-1} \neq LT^{-1}$

wrong (b)

frequency

 $v = \sqrt{\frac{P}{\rho}}$

pressure

density

$$\sqrt{\frac{m L T^{-2}}{L^2 \frac{m}{L^3}}} = \sqrt{L^2 T^{-2}}$$

जीव Last pages जरूर देखना



Q. Time period of a simple pendulum depends on 'm' of block
 length of string (l) & acc due to gravity 'g'
 Derived the formula for time period.

$$\left. \begin{array}{l} T \propto m^x \\ T \propto l^y \\ T \propto g^z \end{array} \right\} \text{यहाँ से ज्ञान ?}$$

$$T \propto m^x l^y g^z$$

$$T = K m^x l^y g^z$$

dimensionless
const
दोनों पक्षों की



$$T = K m^x l^y g^z$$

$$m^0 l^0 T^{-1} = m^x l^y (l T^{-2})^z$$

$$= m^x l^y l^z T^{-2z}$$

$$m^0 l^0 T^1 = m^x l^{y+z} T^{-2z}$$

Compare

$$x = 0,$$

$$y + z = 0$$

$$-2z = 1 \Rightarrow z = -\frac{1}{2}$$

$$y = -z = -\left(-\frac{1}{2}\right) = \frac{1}{2}$$

$$T = K m^0 l^{\frac{1}{2}} \cdot g^{-\frac{1}{2}} = \frac{K \sqrt{l}}{\sqrt{g}}$$

$$T = K \sqrt{\frac{l}{g}}$$

(E) Energy of a particle performing SHM depends on mass (m) of object, Amplitude (A), frequency f of motion
Derive the relation b/w them.

ਪੰਜਾਬ ਕਦਮ

Get Dimensions

$E \propto m^x A^y f^z$

$E = k m^x A^y f^z$

$$m L^2 T^{-2} = m^x L^y (T^{-1})^z$$

$$m^1 L^2 T^{-2} = m^x L^y T^{-3}$$

Componere.

$$\begin{array}{l} x = 1 \\ y = 2 \\ -z = -1 \\ z = 2 \end{array}$$

$$E = k M A^2 f^2$$

Q Suppose

Force depends on mass(m), speed (v), and radius ' r '

Derive the relation b/w them

$$F = K m^x v^y r^z$$

$$m L T^{-2} = m^x (L T^{-1})^y L^z$$

$$m^1 L T^{-2} = m^x L^y T^{-y}$$

Compare power

$$x = 1$$

$$-y = -2$$

$$y = 2$$

$$y + z = 1$$

$$2 + z = 1$$

$$z = -1$$

प्रताग्री

$$F = K m^1 \cdot v^2 \cdot r^{-1}$$

$$F = K \frac{m v^2}{r}$$

en अभी कुछ
नहीं पता

Q A satellite is revolving around the earth such that time period T of satellite depends on M (mass of earth), gravitational const (G), and radius of orbit r , Derive the formula for time period of satellite

$$T = K m^{-\frac{1}{2}} G^{\frac{1}{2}} r^{3/2}$$

✓

$2x$

3 → इवान्दी
नोटी

$$T = K m^x G^y r^z$$

$$T = m^x (m^{-1} L^3 T^{-2})^y L^z$$

$$m^0 L^0 T^1 = m^{x-y} L^{3y+3} T^{-2y}$$

$$\begin{cases} -2y = 1 \\ y = -\frac{1}{2} \end{cases}$$

$$x - y = 0$$

$$x = y \quad \therefore \quad x = -\frac{1}{2}$$

$$G = m^{-1} L^3 T^{-2}$$

$$3y + 3 = 0$$

$$3 = -3y = +3/2$$

~~H/W~~

P
W

Q A satellite is revolving around the earth such that

Orbital velocity v_o of satellite depends on M (mass of earth), gravitational cons. (G), and radius of orbit r ,

Derive the formula for Orbital velocity of satellite

$$G = m^{-1} L^3 T^{-2}$$

$$G = m^{-1} L^3 T^{-2}$$

Q.

A quantity f is given by $f = \sqrt{\frac{hc^5}{G}}$ where c is speed of light, G universal gravitational constant and h is the Planck's constant. Dimension of f is that of:

(JEE Main-2020)

- A** Momentum
- B** Area
- C** Energy
- D** Volume

Ans : (C)

Q.

Amount of solar energy received on the earth's surface per unit area per unit time is defined a solar constant. Dimension of solar constant is: (JEE Main-2020)

A $ML^2 T^{-2}$

B MLT^{-2}

C $M^2 L^0 T^{-1}$

D $ML^0 T^{-3}$

Ans : (D)

Q.

~~Tough~~ Go... gently (J)

In a typical combustion engine the work done by a gas molecule is given

$W = \alpha^2 \beta e^{\frac{-\beta x^2}{kT}}$, where x is the displacement, k is the Boltzmann constant and T is the temperature. If α and β are constants, dimensions of α will be:

(JEE Main-2021)

- A [MLT⁻²]
- B [M⁰LT⁰]
- C [M²LT⁻²]
- D [MLT⁻¹]

Ans : (B)

Q.

The force is given in terms of time t and displacement x by the equation $F = A \cos Bx + C \sin Dt$. The dimensional formula of AD/B is: **(JEE Main-2021)**

A $[M^0 L T^{-1}]$

B $[M L^2 T^{-3}]$

C $[M^1 L^1 T^{-2}]$

D $[M^2 L^2 T^{-3}]$

Ans : (B)

Q.

Match List-I with List-II.

List-I

- (a) Torque
- (b) Impulse
- (c) Tension
- (d) Surface Tension

List-II

- (i) MLT^{-1}
- (ii) MT^{-2}
- (iii) ML^2T^{-2}
- (iv) MLT^{-2}

(JEE Main-2021)

A

(a)-(iii), (b)-(i), (c)-(iv), (d)-(ii)

B

(a)-(ii), (b)-(i), (c)-(iv), (d)-(iii)

C

(a)-(i), (b)-(iii), (c)-(iv), (d)-(ii)

D

(a)-(iii), (b)-(iv), (c)-(i), (d)-(ii)

Ans : (A)

Q.

An expression of energy density is given by $u = \frac{\alpha}{\beta} \sin\left(\frac{\alpha x}{k t}\right)$, where α, β are constants, x is displacement, k is Boltzmann constant and t is the temperature. The dimensions of β will be: **(JEE Main-2022)**

- A** $[ML^2 T^{-2} \theta^{-1}]$
- B** $[M^0 L^2 T^{-2}]$
- C** $[M^0 L^0 T^0]$
- D** $[M^0 L^2 T^0]$

Ans : (D)

Q.

Match the list-I with List -II.

List I

- A. Torque
- B. Stress
- C. Latent Heat
- D. Power

List II

- I. Nms^{-1}
- II. J kg^{-1}
- III. Nm
- IV. Nm^{-2}

Choose the correct answer from the options given below:

(JEE Main-2022)

A

A-III, B-II, C-I, D-IV

B

A-III, B-IV, C-II, D-I

C

A-IV, B-I, C-III, D-II

D

A-II, B-III, C-I, D-IV

Ans : (B)

Q.

In Vander Waals equation $\left[P + \frac{a}{V^2}\right] [V - b] = RT$; P is pressure, V is volume, R is universal gas constant and T is temperature. The ratio of constants a/b is dimensionally equal to: (JEE Main-2022)

- A** P/V
- B** V/P
- C** PV
- D** PV^3

Ans : (C)

⑯ $E = \frac{B^2 - x^2}{At}$

find D.F of A & B

$$B^2 = L^2$$

$$B = L$$

$$\frac{m L^2 T^{-2}}{A} = \frac{L^2}{A \cdot T}$$

$$A = \frac{L^2}{T(m L^2 T^{-2})}$$

$$A = m^{-1} L^0 T^{+1}$$

H/W (1g)

$$P = \frac{A - t^2}{B + x^2} \cdot C$$

(momentum)

(20)

$$P = \frac{A + t^2}{B - x^2} \cdot C$$

Pressure π

to find (21)

$$F = \frac{A - x^2}{B} + Ct + Dx$$

find D.F of $\frac{A \cdot B}{C \cdot D}$

~~H/W~~ ~~obj II page → 9~~, (1,2)

Exercise 1, 2, 5, 8,

HCV pdf download graph

H/W

calculation OP

P
W

(let)

$$y = \sin \theta$$

angle \Rightarrow Dimensionless.

Dimensionless, number $[-1, 1]$

$$\textcircled{1} \quad y = \sin A \Rightarrow A = [m^o L^o T^o]$$

$$\textcircled{2} \quad y = \sin(Ax) \quad Ax = 1 \quad (\text{dimensionless})$$

$$A \cdot L = 1$$

$$A = L^{-1}$$

$$\textcircled{3} \quad y = \sin(At)$$

$$AT = 1$$

$$A = T^{-1}$$

$$\textcircled{4} \quad y = \sin\left(\frac{A}{x^2}\right)$$

$$\frac{A}{L^2} = 1$$

$$A = L^2$$

⑤ $y = \sin(Ax^2 + Bt^3)$

2 nos Number Σ
b/w $[-1, 1]$

Dimensionally

$$\left\{ \begin{array}{l} Ax^2 = 1 \\ AL^2 = 1 \\ A = L^{-2} \end{array} \quad \begin{array}{l} Bt^3 = 1 \\ BT^3 = 1 \\ B = T^{-3} \end{array} \right.$$

$y =$ Number
Dimensions

$$⑥ y = \sin \left(\frac{A}{x^2} + Bt^2 + Ct \right)$$

$$\frac{A}{x^2} = 1 \quad (\text{Dimensionality}) \Rightarrow Bt^2 = 1$$

$$B = T^{-2}$$

$$\frac{A}{L^2} = 1 \quad \boxed{A = L^2}$$

$$CT = 1$$

$$C = T^{-1}$$

$$y = m^0 L^0 T^0$$

$$\frac{AB}{C} = \frac{L^2 \cdot T^{-2}}{T^{-1}} = L^2 T^{-1}$$

velocity

$y = v \sin \left(Ax^2 + \frac{B}{t} \right)$

$$AL^2 = 1 \quad A = L^{-2}$$

$$\frac{B}{T} = 1 \quad B = T$$

$y = \text{Velocity} \equiv LT^{-1}$

P
W

⑧ $y = A \sin(Px^2 + \frac{\theta}{t} + R.v)$

Amplitude (meter)

Velocity

$$y = L$$

- P W
- 1 2
2 -3
3 -4
4 None

D.F. of $\frac{PQ}{yR}$ is given by $m^\alpha L^\beta T^\gamma$

find $\alpha + \beta + \gamma$

$P = L^{-2}$

$Q = T$

$Rv = 1$

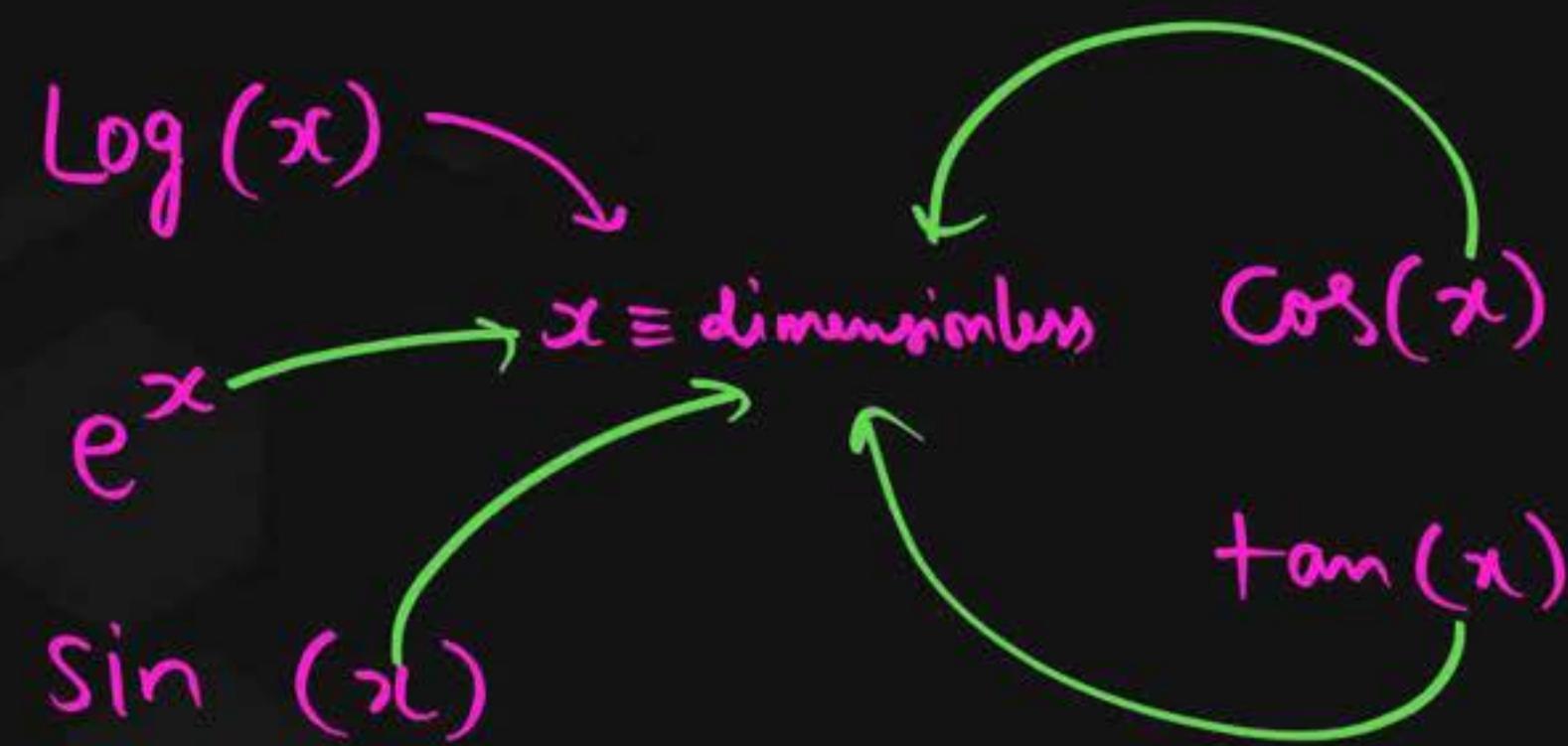
$R LT^{-1} = 1$

$R = L^T T$

$\frac{PQ}{yR}$

$\frac{L^{-2} \cdot T}{L \cdot L^{-1} T} = L^{-2}$

$\alpha = 0$
 $\beta = -2$
 $\gamma = 0$



$y = \log (x)$

dimensionless

$$y = \sin\left(Ax^2 + \frac{B}{t}\right)$$

Q

$$y = \log\left(Ax^2 + \frac{B}{t}\right)$$

$$AL^2 = 1$$

$$\frac{B}{T} = 1$$

A = L⁻²

B = T

$$Q \quad q = Q_0 e^{-\frac{t}{\tau}}$$

find D.F. of τ

$$\boxed{e = 2.718 \text{ maths}}$$

$$\boxed{\pi = 3.14}$$

$$\frac{t}{\tau} = 1 \text{ (dimensionally)}$$

$$\boxed{t = \tau}$$

$$\boxed{\tau = T^1}$$

$$Q \quad y = \log\left(\frac{A}{t^2} - Bt\right)$$

find D.F. of A, B

$$A = T^2$$

$$B \cdot L T^{-1} = 1$$

$$\boxed{B = L^{-1} T}$$

$$\underline{\text{Any}} \rightarrow T^2 \cdot L^{-1} T$$

$$\boxed{L^{-1} T^3}$$

$$Q \quad y = Q e^{\frac{(Ax^2 + B/t^2 - C)t}{t^2}}$$

find D.F. of A, B, C

$$A = L^{-2}, \quad B = T^2, \quad C = T^{-1}$$

$$L^{-2} \cdot T^2 \cdot T^{-1} = \boxed{L^{-2} T^+}$$

P W

Amplitude (m)

$$\text{Q} \quad y = A \log \left(Bx^2 + \frac{C}{t^3} - 5Dt^3 + \frac{E}{F+t} - \frac{G}{x^2} \right)$$

find D.F. of $A \cdot B \cdot C \cdot D \cdot E \cdot F \cdot G. = ?$

$$A = L, \quad B = L^{-2}, \quad C = T^3, \quad D = T^{-3}, \quad F = T, \quad E = T, \quad G = L^2$$

Ω

Potential Energy

$$U = K \left(1 - \sin(ax) \right)$$

$ax = 1$ (dimensionally)



find D.F. of K & a

$$a = L^{-1}$$

$$\frac{DF \text{ of } U}{DF \text{ of } K} = DF \text{ of } a$$

$$\frac{ML^2T^{-2}}{ML^2T^{-2}} = 1$$

Ω

(meter)

$$y = A \sin\left(\frac{Bx}{C+t}\right)$$

find D.F. of B & C

$$C = T, A = L,$$

$$\frac{Bx}{C+t} \longrightarrow \text{dimensions}$$

$$\frac{BL}{T} = 1$$

$$B = L^{-1}T^{-1}$$

$$q = Q_0 e^{-t/\tau}$$

$-\frac{t}{\tau} \rightarrow \text{dimensionless}$

$$(-1) \left(\frac{t}{\tau} \right) \Rightarrow 1$$

$$\frac{t}{\tau} = 1$$

$$\tau = T$$

$$P = P_0 e^{5\alpha t^2}$$

$$\alpha t^2 \rightarrow \text{dimensionless}$$
$$\alpha = T^{-2}$$

$$A = A_0 e^{2t/\tau}$$

$$\frac{2t}{\tau} \rightarrow \text{dimensionless}$$

$$\frac{t}{\tau} \rightarrow 1$$

$$\tau = T$$

H|W

P
W

$$\textcircled{1} \quad U = \frac{A\sqrt{x}}{B+x^2}$$

D.F. of A.B is

②

$$P = \frac{\alpha}{\beta} e^{-\frac{\alpha x}{kT}}$$

JEE mains 2021, 22,

* JEE main 2025

 $K \rightarrow$ Boltzmann const $T \rightarrow$ temp.

check the following equation dimensionally

$$(a) h = \frac{2s \cos \theta}{\gamma \rho g}$$

h → height s → surface tension
 γ → radius ρ → density
 g → acceleration due to gravity

$$(b) v = \sqrt{\frac{P}{\rho}}$$

frequency pressure
 density

अब Last pages जरूर देखना



$$F = \frac{A - x^2}{B} + Cx + Dx$$

$$C = m L T^{-3}$$

$$D = m T^{-2}$$

$$A = L^2$$

$$B = m^{-1} L T^{+2}$$

$$\frac{m^{-1} L^3 T^{+2}}{m^2 L T^{-5}} = m^{-3} L^2 T^{+7}$$

moment

$$\textcircled{0} \quad P = \frac{A + t^2}{B + x^2} \cdot c$$

$B = l^2$

$A = T^2$

MLT⁻¹ = $\frac{T^2}{l^2} \cdot c$

$c = m l^3 T^{-3}$

pressure

$$P = \frac{A + t^2}{B - x^2} \cdot c$$

$$\frac{MLT^{-2}}{l^2} = \frac{T^2}{l^2} \cdot c$$

$c = m L T^{-4}$

P
W

$A = T^2$

$B = l^2$

3. Suppose you are told that the linear size of everything in the universe has been doubled overnight. Can you test this statement by measuring sizes with a metre stick? Can you test it by using the fact that the speed of light is a universal constant and has not changed? What will happen if all the clocks in the universe also start running at half the speed?
4. If all the terms in an equation have same units, is it necessary that they have same dimensions? If all the terms in an equation have same dimensions, is it necessary that they have same units?
5. If two quantities have same dimensions, do they represent same physical content?
6. It is desirable that the standards of units be easily available, invariable, indestructible and easily reproducible. If we use foot of a person as a standard unit of length, which of the above features are present and which are not?
7. Suggest a way to measure:
 - (a) the thickness of a sheet of paper,
 - (b) the distance between the sun and the moon.

OBJECTIVE I

1. Which of the following sets cannot enter into the list of fundamental quantities in any system of units?
 - (a) length, mass and velocity,
 - (b) length, time and velocity,
 - (c) mass, time and velocity,
 - (d) length, time and mass.
2. A physical quantity is measured and the result is expressed as nu where u is the unit used and n is the numerical value. If the result is expressed in various units then
 - (a) $n \sim \text{size of } u$
 - (b) $n \sim u^3$
 - (c) $n \sim \sqrt{u}$
 - (d) $n \sim \frac{1}{u}$
3. Suppose a quantity x can be dimensionally represented in terms of M , L and T , that is, $[x] = M^a L^b T^c$. The quantity mass
 - (a) can always be dimensionally represented in terms of L , T and x ,
 - (b) can never be dimensionally represented in terms of
4. A dimensionless quantity
 - (a) never has a unit,
 - (b) always has a unit,
 - (c) may have a unit,
 - (d) does not exist.
5. A unitless quantity
 - (a) never has a nonzero dimension,
 - (b) always has a nonzero dimension,
 - (c) may have a nonzero dimension,
 - (d) does not exist.
6.
$$\int \frac{dx}{\sqrt{2ax - x^2}} = a^n \sin^{-1} \left[\frac{x}{a} - 1 \right].$$
The value of n is
 - (a) 0
 - (b) -1
 - (c) 1
 - (d) none of these.You may use dimensional analysis to solve the problem.

OBJECTIVE II

1. The dimensions $ML^{-1}T^{-2}$ may correspond to
 - (a) work done by a force
 - (b) linear momentum
 - (c) pressure
 - (d) energy per unit volume.
2. Choose the correct statement(s):
 - (a) A dimensionally correct equation may be correct.
 - (b) A dimensionally correct equation may be incorrect.
 - (c) A dimensionally incorrect equation may be correct.
 - (d) A dimensionally incorrect equation may be incorrect.
3. Choose the correct statement(s):
 - (a) All quantities may be represented dimensionally in terms of the base quantities.
 - (b) A base quantity cannot be represented dimensionally in terms of the rest of the base quantities.
 - (c) The dimension of a base quantity in other base quantities is always zero.
 - (d) The dimension of a derived quantity is never zero in any base quantity.

EXERCISES

1. Find the dimensions of
 - (a) linear momentum,
 - (b) frequency and
 - (c) pressure.
2. Find the dimensions of
 - (a) angular speed ω ,
 - (b) angular acceleration α ,
 - (c) torque Γ and
 - (d) moment of inertia I .Some of the equations involving these quantities are

$$\omega = \frac{\theta_2 - \theta_1}{t_2 - t_1}, \quad \alpha = \frac{\theta_2 - \theta_1}{t_2 - t_1}, \quad F = Fr \text{ and } I = mr^2.$$

The symbols have standard meanings.

3. Find the dimensions of

- (a) electric field E ,
- (b) magnetic field B and
- (c) magnetic permeability μ_s .

The relevant equations are

$$F = qE, \quad F = quB, \quad \text{and} \quad B = \frac{\mu_s I}{2\pi a};$$

where F is force, q is charge, v is speed, I is current, and a is distance.

4. Find the dimensions of

- (a) electric dipole moment p and
- (b) magnetic dipole moment M .

The defining equations are $p = qd$ and $M = IA$; where d is distance, A is area, q is charge and I is current.

5. Find the dimensions of Planck's constant h from the equation $E = hv$ where E is the energy and v is the frequency.

6. Find the dimensions of

- (a) the specific heat capacity c ,
- (b) the coefficient of linear expansion α and
- (c) the gas constant R .

Some of the equations involving these quantities are $Q = mc(T_2 - T_1)$, $I_t = I_d[1 + \alpha(T_2 - T_1)]$ and $PV = nRT$.

7. Taking force, length and time to be the fundamental quantities find the dimensions of

- (a) density,
- (b) pressure,
- (c) momentum and
- (d) energy.

8. Suppose the acceleration due to gravity at a place is 10 m/s^2 . Find its value in cm/(minute) 2 .

9. The average speed of a snail is 0.020 miles/hour and that of a leopard is 70 miles/hour. Convert these speeds in SI units.

10. The height of mercury column in a barometer in a Calcutta laboratory was recorded to be 75 cm. Calculate this pressure in SI and CGS units using the following data : Specific gravity of mercury = 13.6 , Density of water = 10^3 kg/m^3 , $g = 9.8 \text{ m/s}^2$ at Calcutta. Pressure = $h\rho g$ in usual symbols.

11. Express the power of a 100 watt bulb in CGS unit.

12. The normal duration of I.Sc. Physics practical period in Indian colleges is 100 minutes. Express this period in microcenturies. $1 \text{ microcentury} = 10^{-6} \times 100 \text{ years}$. How many microcenturies did you sleep yesterday?

13. The surface tension of water is 72 dyne/cm. Convert it in SI unit.

14. The kinetic energy K of a rotating body depends on its moment of inertia I and its angular speed ω . Assuming the relation to be $K = kI^\alpha \omega^\beta$ where k is a dimensionless constant, find α and β . Moment of inertia of a sphere about its diameter is $\frac{2}{5}Mr^2$.

15. Theory of relativity reveals that mass can be converted into energy. The energy E so obtained is proportional to certain powers of mass m and the speed c of light. Guess a relation among the quantities using the method of dimensions.

16. Let I = current through a conductor, R = its resistance and V = potential difference across its ends. According to Ohm's law, product of two of these quantities equals the third. Obtain Ohm's law from dimensional analysis. Dimensional formulae for R and V are $ML^2I^{-1}T^{-2}$ and $ML^3T^{-3}I^{-1}$ respectively.

17. The frequency of vibration of a string depends on the length L between the nodes, the tension F in the string and its mass per unit length m . Guess the expression for its frequency from dimensional analysis.

18. Test if the following equations are dimensionally correct :

(a) $h = \frac{2S \cos\theta}{\rho g}$,	(b) $v = \sqrt{\frac{P}{\rho}}$,
(c) $V = \frac{\pi P r^4 t}{8\eta l}$,	(d) $v = \frac{1}{2\pi} \sqrt{\frac{mgf}{I}}$;

where h = height, S = surface tension, ρ = density, P = pressure, V = volume, η = coefficient of viscosity, v = frequency and I = moment of inertia.

19. Let x and a stand for distance. Is $\int \frac{dx}{\sqrt{a^2 - x^2}} - \frac{1}{a} \sin^{-1} \frac{x}{a}$ dimensionally correct ?

□

ANSWERS

OBJECTIVE I

1. (b) 2. (d) 3. (d) 4. (c) 5. (a) 6. (a)

OBJECTIVE II

1. (c), (d) 2. (a), (b), (d) 3. (a), (b), (c)

EXERCISES

1. (a) MLT^{-1} (b) T^{-1} (c) $ML^{-1}T^{-2}$
2. (a) T^{-1} (b) T^{-2} (c) ML^2T^{-3} (d) ML^2
3. (a) $MLT^{-3}I^{-1}$ (b) $MT^{-2}I^{-1}$ (c) $MLT^{-2}I^{-1}$
4. (a) LTI (b) L^2I
5. ML^2T^{-1}
6. (a) $L^2T^{-2}K^{-1}$ (b) K^{-1} (c) $ML^2T^{-2}K^{-1}(\text{mol})^{-1}$

7. (a) $FL^{-1}T^2$ (b) FL^{-1} (c) PT (d) FL
8. 36×10^{-6} cm/(minute)²
9. 0.0089 m/s, 31 m/s
10. 10×10^{-4} N/m², 10×10^7 dyne/cm²
11. 10^6 erg/s
12. 1.9 microcenturies
13. 0.072 N/m
14. $a = 1, b = 2$
15. $E = kmc^2$
16. $V = IR$
17. $\frac{k}{L} \sqrt{\frac{F}{m}}$
18. all are dimensionally correct
19. no

□

Application of dimension Analysis

① Correctness of formula

② We can find D.F. of unknown phy quantity

$$\text{Q} \quad F = \frac{G m_1 m_2}{r^2}$$

D.F. of G = ?

$$G = \frac{F r^2}{m_1 m_2} \Rightarrow \frac{MLT^{-2} \cdot L^2}{MM} = [M^{-1} L^3 T^{-2}]$$

$$\text{Q} \quad F = 6\pi r \eta v$$

D.F. of η

$$\eta = \frac{F}{6\pi r v}$$

$$v \Rightarrow \frac{MLT^{-2}}{L LT^{-1}} = [ML^{-1} T^{-1}]$$

Q Find DF of specific heat const.

$$\Delta Q = m s \Delta T$$

heat energy given

Change in temp

$$\Delta Q = m s \Delta T$$

$$s = \frac{\Delta Q}{m \Delta T}$$

$$s = \frac{\Delta Q}{m \Delta T} = \frac{ML^2T^{-2}}{m K}$$

$$DF \ni k = [M^0 L^2 T^{-2} K^{-1}]$$



$$Q = mL$$

heat given
energy

Df of $L \Rightarrow$

- (A) $m L^2 T^{-2}$
- (B) $m^0 L^2 T^{-2}$
- (C) $m^0 L T^{-2}$
- (P) other

Latent heat of fusion

$$Q = mL$$
$$L = \frac{Q}{m} \Rightarrow \frac{m L^2 T^{-2}}{M}$$

$[m^0 L^2 T^{-2}]$

Q Bolzmann Const (κ)

find the DF of bolzmann const.

$$U = \frac{3}{2} \kappa T$$

temp.

internal Energy
(kinetic energy)

$$\kappa = \frac{2U}{3T}$$

$$\kappa \Rightarrow \frac{m l^2 T^{-2}}{T} = m l^2 T^{-3}$$

$$\kappa \Rightarrow \frac{m l^2 T^{-2}}{\pi} = [m l^2 T^{-2} K^{-1}]$$

$$\textcircled{4} \quad v = \frac{A}{B+t}$$

find DF of \dot{B}

B में t जुड़ रहा है

$$B \Rightarrow \text{time} \Rightarrow B = m^0 l^0 T^{-1}$$

$$\textcircled{5} \quad v = A \sin[B(c+t)]$$

↓
time

find DF of \dot{c}

$$c = [m^0 l^0 T^{-1}]$$

(6) $x = At$

Displacement

time

D.F. of A = ?

$At \rightarrow$ Displacement

$$AT = L$$

$$A = \frac{L}{T} = LT^{-1}$$

P
W

$$t \rightarrow \text{time}$$

$$\textcircled{+} \quad x = At + Bt^2 + Ct^3$$

Displacement

$$Ct^3 \rightarrow \text{Displacement}$$

$$CT^3 = L$$

$$C = LT^{-3}$$

$At \rightarrow \text{Displacement}$

$$AT = L$$

$$A \Rightarrow \frac{L}{T} = LT^{-1}$$

$Bt^2 \rightarrow \text{Displacement}$

$$BT^2 = L$$

$$B \Rightarrow LT^{-2}$$

$$(8) \quad v = At + Bx$$

$v \rightarrow$ velocity

$t \rightarrow$ time

$x \rightarrow$ Displacement

find D.F. of A & B

$At \longrightarrow$ velocity

$$AT = LT^{-1}$$

$$A = \frac{LT^{-1}}{T} = LT^{-2} \checkmark$$

$Bx \longrightarrow$ velocity

$$BL = LT^{-1}$$

$$\boxed{B \Rightarrow T^{-1}}$$

(b) find D.F. of $\frac{A}{B}$

$$\frac{LT^{-2}}{T^{-1}} = \boxed{LT^{-1}}$$

$$\textcircled{9} \quad v = At^2 + Bx^2 + Ct^3$$

$$\begin{aligned} CT^3 &= LT^{-1} \\ C &= LT^{-4} \end{aligned}$$

find D.F. of A, B, C

$v \rightarrow$ velocity
 $t \rightarrow$ time
 $x \rightarrow$ displacement

$$AT^2 = LT^{-1}$$

$$A \Rightarrow LT^{-3}$$

$$BL^2 = LT^{-1}$$

$$B \Rightarrow L^{-1}T^{-1}$$

$x \rightarrow$ Displacement

$t \rightarrow$ time

$v \rightarrow$ velocity, speed

$F \rightarrow$ force

$Cx \rightarrow$ displacement

$$CL = L$$

$C = 1 \rightarrow$ dimensionless

$$\text{Ans} C = [m^0 L^0 T^0]$$

$$(10) \quad x = At + \frac{B}{t} + Cx$$

find D.F. of A, B, C

$At \rightarrow$ Displacement

$$A \cdot T = L \Rightarrow A = LT^{-1}$$

$\frac{B}{t} \rightarrow$ Displacement

$$\frac{B}{T} = L \quad B = LT$$

इसका Notes लें
दोपी साध सुने
कर

⑪ $v = At + \frac{B}{t} + Cx$

$$AT = LT^{-1}$$

$$\boxed{A = LT^{-2}}$$

$$\frac{B}{t} = LT^{-1}$$

$$\boxed{B = LT^{-1}, T = L}$$

$$CL = LT^{-1}$$

$$\boxed{C = T^{-1}}$$

⑫ $v = Ax^2 + Bx + \frac{C}{t^2}$

$$AL^2 = LT^{-1}$$

$$\boxed{A = L^{-1}T^{-1}}$$

$$BL = LT^{-1}$$

$$\boxed{B = T^{-1}}$$

$$\frac{C}{t^2} = LT^{-1}$$

$$\boxed{C = LT}$$

$$\textcircled{13} \quad F = At + Bx$$

$$AT = m LT^{-2}$$

$$\boxed{A \Rightarrow m LT^{-3}}$$

$$B \cdot L = m LT^{-2}$$

$$\boxed{B \Rightarrow m L^0 T^{-2}}$$

$$\textcircled{14} \quad F = \frac{A}{t} + Bx^2$$

$$mLT^{-2} = \frac{A}{t}$$

$$\boxed{A = m LT^{-1}}$$

$$BL^2 = m LT^{-2}$$

$$\boxed{B = m L^{-1} T^{-2}}$$

$$\textcircled{15} \quad F = AV + \frac{B}{x^2}$$

$$F = AV$$

$$A = \frac{F}{V} = \frac{m LT^{-2}}{L T^{-1}}$$

$$= m L^0 T^{-1}$$

$$mLT^{-2} = \frac{B}{L^2}$$

$$\boxed{B = m L^3 T^{-2}}$$

16

$$v = \frac{A}{B+t} \quad \text{find DF of } A \text{ & } B$$

$$B+t \Rightarrow \boxed{B \geq T}$$

$$v \Rightarrow \frac{A}{\text{time} + \text{time}} = \frac{A}{\text{time}}$$



$$v \Rightarrow \frac{A}{\text{time}}$$

$$LT^{-1} = \frac{A}{T}$$

$$\boxed{A = LT^{-1} \cdot T = L}$$

(7)

$$v = \frac{At}{B^2 - x^2}$$

B^2 से x^2 घट रहा है

DF of B^2 = DF of x^2

$$B^2 = L^2$$

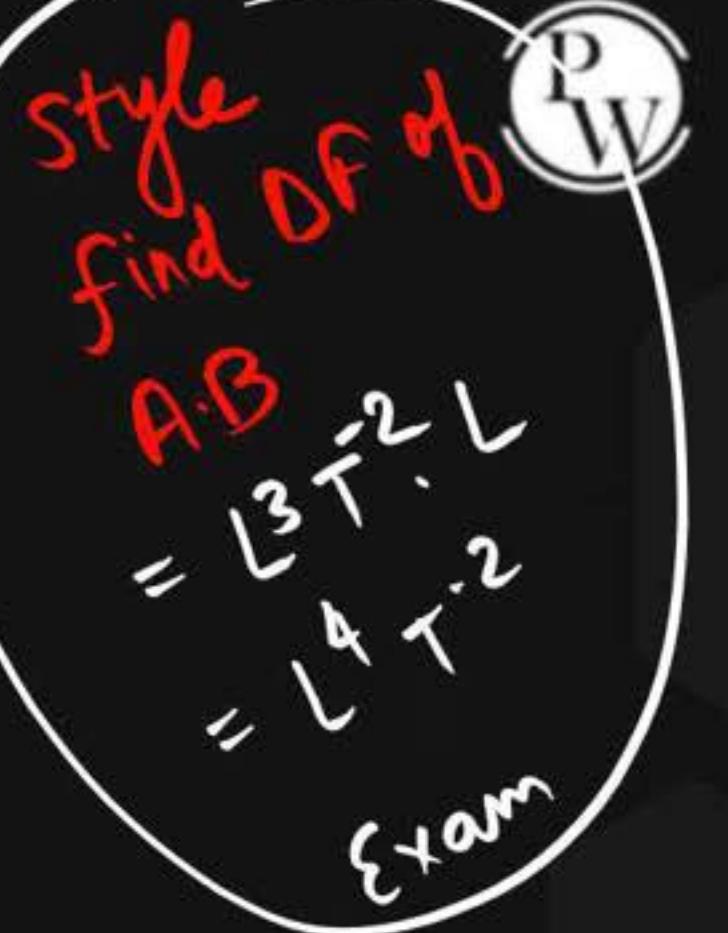
$$\boxed{B = L}$$

$$v = \frac{At}{L^2}$$

$$LT^{-1} = \frac{AT}{L^2}$$

$$A = \frac{LT^{-1} L^2}{T} = L^3 T^{-2}$$

$$\boxed{A = L^3 T^{-2}}$$



⑯ $E = \frac{B^2 - x^2}{At}$

find D.F of A & B

$$B^2 = L^2$$

$$\boxed{B = L}$$

$$\frac{m L^2 T^{-2}}{L^2} = \frac{L^2}{A \cdot T}$$

$$A = \frac{L^2}{T(m L^2 T^{-2})}$$

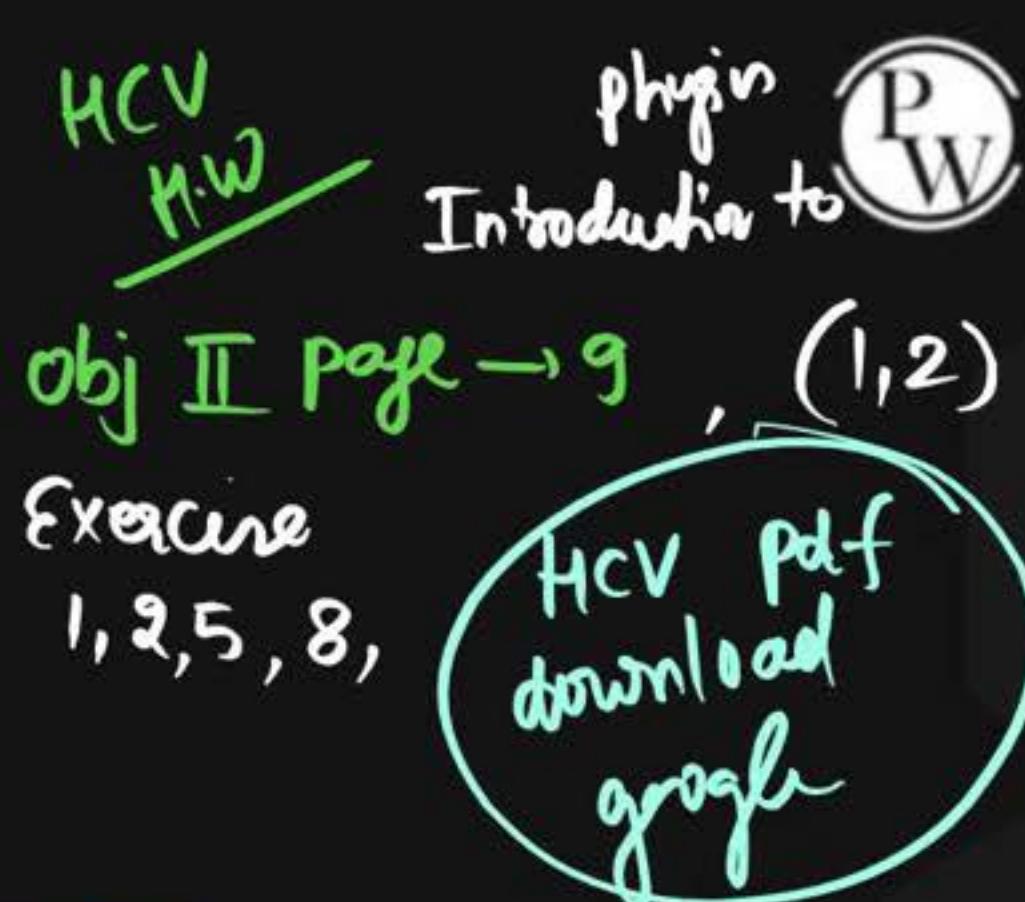
$$\boxed{A = m^{-1} L^0 T^{+1}}$$

H1W
(1g) $P = \frac{A - t^2}{B + x^2} \cdot C$
(momentum)

(20) $P = \frac{A + t^2}{B - x^2} \cdot C$
Pressure

tough
(21) $F = \frac{A - x^2}{B} + Ct + Dx$

find D.F of $\frac{A \cdot B}{C \cdot D}$



calculation
OP 2

Q.

Match List-I with List-II :

List-I

- (a) h (Planck's constant) ✓
- (b) E (kinetic energy) ✓
- (c) V (electric potential) ✓
- (d) P (linear momentum) ✓ $m \text{ L T}^{-1}$

List-II

- (i) $[\text{M L T}^{-1}]$
- (ii) $[\text{M L}^2 \text{ T}^{-1}]$
- (iii) $[\text{M L}^2 \text{ T}^{-2}]$
- (iv) $[\text{M L}^2 \text{ I}^{-1} \text{ T}^{-3}]$

Choose the correct answer from the options given below:

(JEE Main-2021)

A

(a)→(iii), (b)→(iv), (c)→(ii), (d)→(i)

B

(a)→(ii), (b)→(iii), (c)→(iv), (d)→(i)

C

(a)→(i), (b)→(ii), (c)→(iv), (d)→(iii)

D

(a)→(iii), (b)→(ii), (c)→(iv), (d)→(i)

Ans : (B)

Notes
রেখা লিখানো
রেখা লিখানো

Q.

Match List-I with List-II.

List-I

- (a) Torque
- (b) Impulse
- (c) Tension
- (d) Surface Tension

List-II

- (i) MLT^{-1}
- (ii) MT^{-2}
- (iii) ML^2T^{-2}
- (iv) MLT^{-2}

(JEE Main-2021)

**P
W**

Choose the most appropriate answer from the option given below :

A

(a)-(iii), (b)-(i), (c)-(iv), (d)-(ii)

B

(a)-(ii), (b)-(i), (c)-(iv), (d)-(iii)

C

(a)-(i), (b)-(iii), (c)-(iv), (d)-(ii)

D

(a)-(iii), (b)-(iv), (c)-(i), (d)-(ii)

Ans : (A)

Q find dimensional formula of plank const

P
W

$$E = h\nu \rightarrow \text{frequency}$$

$$\rightarrow \text{plank const}$$

Energy of one photon

$$h = \frac{E}{\nu}$$

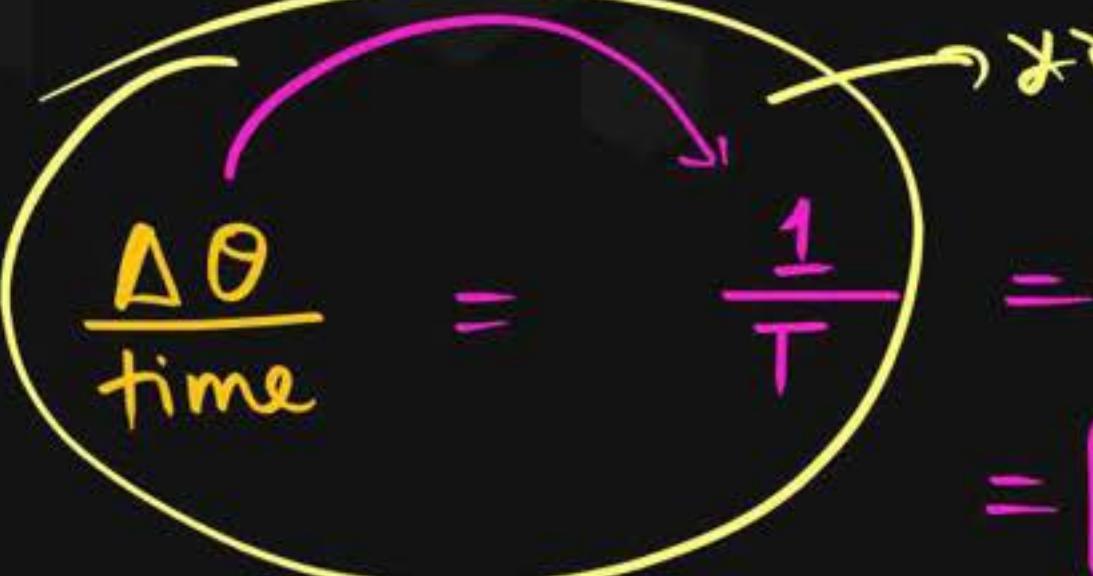
$$\frac{m l^2 T^{-2}}{T^{-1}}$$

$$= [m l^2 T^{-1}]$$

$$\boxed{\text{frequency} = \frac{1}{T} \Rightarrow T^{-1}}$$

$$m l^2 T^{-2+1}$$

Solve


$$\text{Angular velocity} = \frac{\Delta\theta}{\text{time}} = \frac{1}{T} = T^{-1}$$
$$= [m^0 L^0 T^{-1}]$$

Velocity $\rightarrow [m^0 L T^{-1}]$

रवृत्तिपथ

Angular velocity $\rightarrow [m^0 L^0 T^{-1}]$

Circular motion की परिभ्रष्टि

Q5

Resistance = ?

$$V = i R$$

Current
Pot-difference

$$R = \frac{V}{i} \Rightarrow \frac{ML^2T^{-3}A^{-1}}{A}$$

$$[ML^2T^{-3}A^{-2}]$$

PW

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এ

Q.

Check the correctness of following formula

$$(a) F = \frac{mv^2}{r^2} \Rightarrow ?$$

$F \rightarrow$ force

$m \rightarrow$ mass

$v \rightarrow$ speed

$r \rightarrow$ radius

Dimension of LHS $\Rightarrow [MLT^{-2}]$

$$\text{Dimension of RHS} \Rightarrow \frac{M(LT^{-1})^2}{L^2}$$

$$= \frac{ML^2T^{-2}}{L^2} = [ML^0T^{-2}]$$

Dimension of LHS \neq dimension of RHS

Relation not \approx , formula is incorrect

Q A planet is orbiting around earth with orbital velocity V

Correct

$$V = \sqrt{\frac{GM}{r}} \quad \text{check ?}$$

$$G \Rightarrow [m^{-1} L^3 T^{-2}]$$

$M \rightarrow$ mass of earth

$r \rightarrow$ radius of orbit

$G \rightarrow$ gravitational const

RHS

$$\sqrt{\frac{m^{-1} L^3 T^{-2} M}{L}} = \sqrt{L^2 T^{-2}} = LT^{-1}$$

Dimensional formula

$$LT^{-1} = \underline{\underline{LHS}}$$

$$\text{LHS} = \text{RHS}$$

Q Time period of simple pendulum is given by

$$T = 2\pi \sqrt{\frac{l}{g}}$$

?

RHS $2\pi \sqrt{\frac{l}{g}}$

$T \rightarrow$ time period
 $l \rightarrow$ length of pendulum
 $g \rightarrow$ Acc. due to gravity

$$\sqrt{\frac{L}{T^2}} = \sqrt{T^2} = T$$

LHS = RHS

Dimensionally Correct

Q Time period of spring block system is given by

P
W

$$T = 2\pi \sqrt{\frac{m}{k}}$$

time period

$m \rightarrow$ mass of block

$k \rightarrow$ spring const

$$\left(k = \frac{\text{Force}}{\text{length}} \right) = \frac{MLT^{-2}}{L} = M T^{-2}$$

RHS

$$\sqrt{\frac{M}{M T^{-2}}} = \sqrt{T^2}$$

$$= T \Rightarrow$$

LHS = RHS

Correct

Kinetic Energy = $\frac{1}{3}mv^2$ (किसी ने कहा)
 Let

Correct = ?

Incorrect = ?

$$\underline{\text{RHS}} \rightarrow m(LT^{-1})^2 = [mL^2T^{-2}]$$

Dimensionally

But numerically ^{Correct} wrong

Overall formula is wrong

पूछा तो देला

~~$KE = \frac{1}{2}mv^2$~~

Check = ?

$$\underline{\text{RHS}} \rightarrow m(LT^{-1})^2 [mL^2T^{-2}]$$

Dimensionally

Correct
Numerically correct
Overall correct ✓

$$G = ?$$

$$F = \frac{G m_1 m_2}{r^2}$$

$$G = \frac{F r^2}{m_1 m_2} \Rightarrow \frac{m_1 L T^{-2} \cdot L^2}{m_1 m_2}$$

$$\left[m^{-1} L^3 T^{-2} \right]$$

$$U_1 + U_2 = U_3 \Rightarrow$$



Same Unit

Same dimensional (D.F.)

Same formula

physical Ques

$$U_f - U_i = \Delta U$$

$$U_f - U_i = \Delta U$$

$$U_f - U_i = \Delta U$$

Q particle initial speed
= 10 m/s
final speed = 15 m/s

Change in speed = ΔV

$$\Delta V = V_f - V_i$$

$$5 \text{ m/s} = 15 \text{ m/s} - 10 \text{ m/s}$$

Dimensional
formulae

$$\frac{L}{T} = LT^{-1}$$

$$[M^0 LT^{-1}]$$

$$[M^0 LT^{-1}]$$

$$[MLT^{-1}]$$

$$[ML^{-3}T^0]$$

Derived Physical Quantity

$$① \text{ Speed} = \frac{\text{Distance}}{\text{time}} \longrightarrow m/\text{sec} \longrightarrow cm/\text{sec}$$

$$② \text{ Velocity} = \frac{\text{Displacement}}{\text{time}} \longrightarrow m/\text{sec} \longrightarrow cm/\text{sec}$$

$$③ \text{ momentum } p = m \times v$$

$$④ \text{ Density} = \frac{\text{mass}}{\text{Vol}^n} \longrightarrow kg/m^3$$

Unit
(mks)

Unit
CGS

gm cm/sec

gm/cm³

~~$[MLT^{-1}] \neq MLT^{-1} K^0 A^0$~~

momentum $P = mv$ mass

velocity = Displacement $\frac{x}{t}$

P
W

DF. of $P = M \frac{L}{T} = [MLT^{-1}]$

dimension of mass $\rightarrow 1$
length $\rightarrow 1$
time $\rightarrow -1$

Next Class

$$\text{Area} = \text{Length} \times \text{width} \Rightarrow$$

Volⁿ

$$L \cdot L = L^2 \Rightarrow [m^0 L^2 T^0]$$

$$\text{Density} = \frac{\text{mass}}{\text{Vol}^n}$$

$$L \cdot L \cdot L \Rightarrow L^3 \Rightarrow [m^0 L^3 T^0]$$

$$\text{speed} = \frac{\text{Distance}}{\text{time}} \rightarrow \frac{L}{T} \Rightarrow LT^{-1}$$

$$\text{velocity} = \frac{\text{Displacement}}{\text{time}} \rightarrow \frac{L}{T} \Rightarrow LT^{-1}$$

Dimension of Length in Area = 2

P
W

Dimensional formulae

Area \longrightarrow Length \times width

Volume \longrightarrow L \times B \times H

$$\text{Density} = \frac{\text{mass}}{\text{Vol}^n}$$

Distance

Displacement

$$\text{Speed} = \frac{\text{Distance}}{\text{time}}$$

$$\text{Velocity} = \frac{\text{Displacement}}{\text{time}}$$

$$L \cdot L \Rightarrow [m^0 L^2 T^0]$$

$$L \cdot L \cdot L \Rightarrow [m^0 L^3 T^0]$$

$$\frac{M}{L^3} \Rightarrow [m L^{-3} T^0]$$

$$[m^0 L^1 T^0]$$

$$[m^0 L^1 T^0]$$

$$\frac{L}{T} \rightarrow [m^0 L T^{-1}]$$

$$\frac{L}{T} \rightarrow [m^0 L T^{-1}]$$

D.F
Same

* velocity $\longrightarrow LT^{-1} = [m^0 LT^{-1}]$

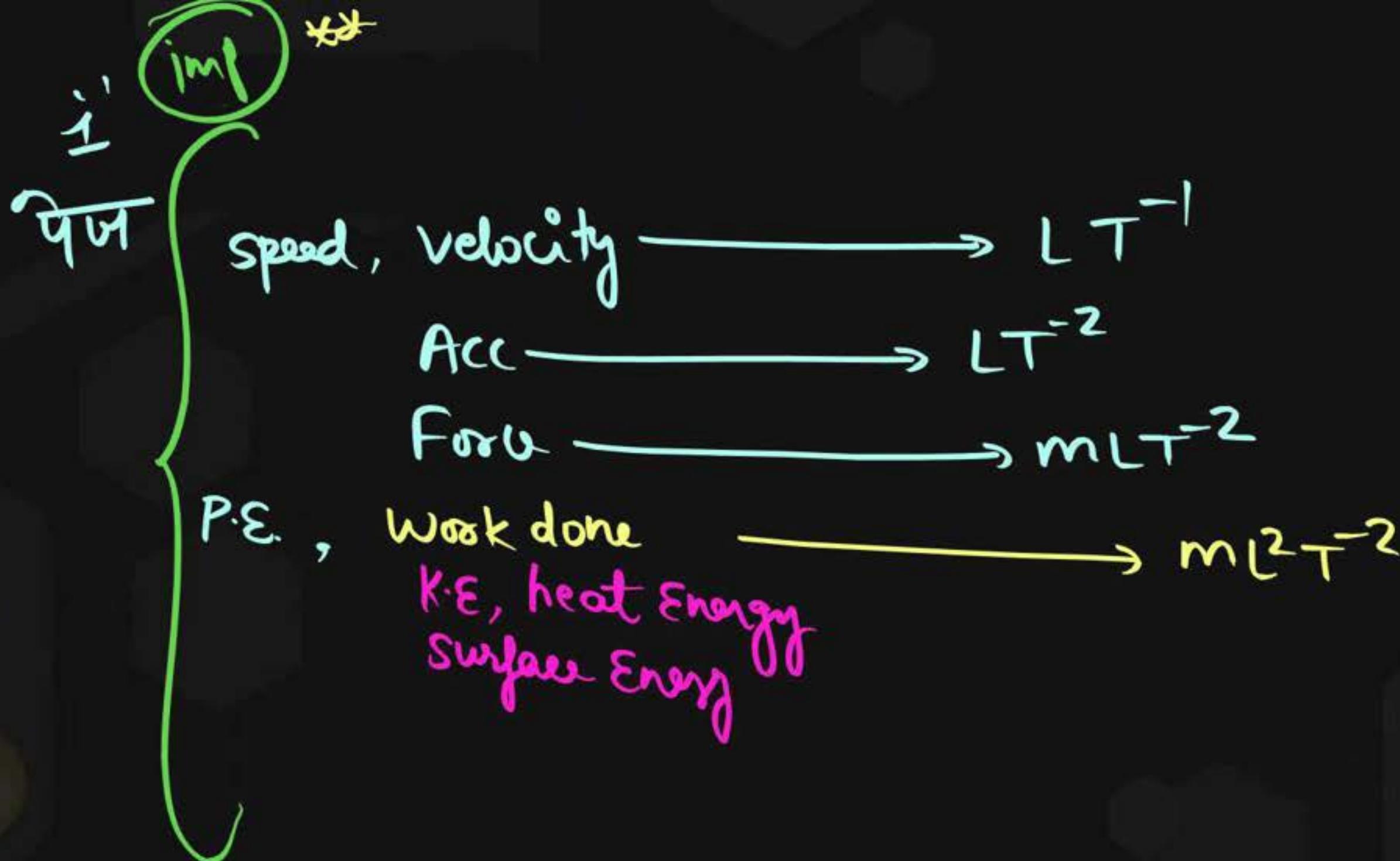
* acceleration = $\frac{\text{Velocity}}{\text{time}}$ $\longrightarrow \frac{LT^{-1}}{T} = LT^{-2} \Rightarrow [m^0 LT^{-2}]$

Force $(F = m\ddot{a}) \longrightarrow [MLT^{-2}]$

momentum $p = mv \longrightarrow [MLT^{-1}]$

Impulse 'J' = $F \times t \longrightarrow [MLT^2 \cdot T] = [MLT^{-1}]$

D.F same
But ?



- Pressure = $\frac{\text{Force}}{\text{Area}}$ $\Rightarrow \frac{m L T^{-2}}{L^2} \Rightarrow [m L^{-1} T^{-2}]$

रुटना

- Work done

$$W = F \times \text{displacement} \Rightarrow m L T^{-2} \cdot L \Rightarrow [m L^2 T^{-2}]$$

~~सेक्ष.~~
~~सेक्ष.~~

- Torque = Force \times (perpendicular Distance) $\Rightarrow [m L T^{-2} \cdot L]$
 $= [m L^2 T^{-2}]$

- moment of inertia $= m R^2$ $\Rightarrow [m L^2] \checkmark$

mass \downarrow
 Distance from axis \downarrow

$[m L^2 T^0] \checkmark$

Ques $G = [m^{-1} L^3 T^{-2}]$

 $\alpha = -1$ $\beta = 3$ $\gamma = -2$

If Dimensional formula of G is given by $m^\alpha L^\beta T^\gamma$

find value of $|\alpha| + |\beta| + |\gamma| = 1 + 3 + 2 = 6$

find

$$\alpha + \beta + \gamma = -1 + 3 - 2 = 0$$

find

$$\frac{\beta\gamma}{\alpha} \Rightarrow \frac{3 \times (-2)}{-1} \Rightarrow 6$$

$$U_1 + U_2 = U_3 \Rightarrow$$

Same Unit
Same dimensional (D.F.)
Same formula

Same physical Quesn

$$U_f - U_i = \Delta U = \text{change in } U$$

Q particle initial Speed
= 10 m/s

final speed = 15 m/s

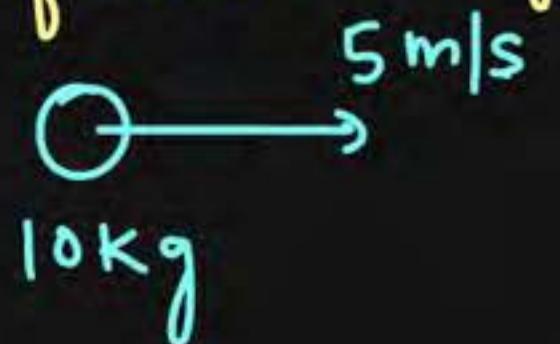
Change in Speed = ΔU

$$\Delta U = V_f - V_i$$

$$5 \frac{\text{m}}{\text{s}} = 15 \frac{\text{m}}{\text{s}} - 10 \frac{\text{m}}{\text{s}}$$

find momentum in mks & CGS system if a particle of mass 10 kg is moving with velocity 5 m/s. (east).

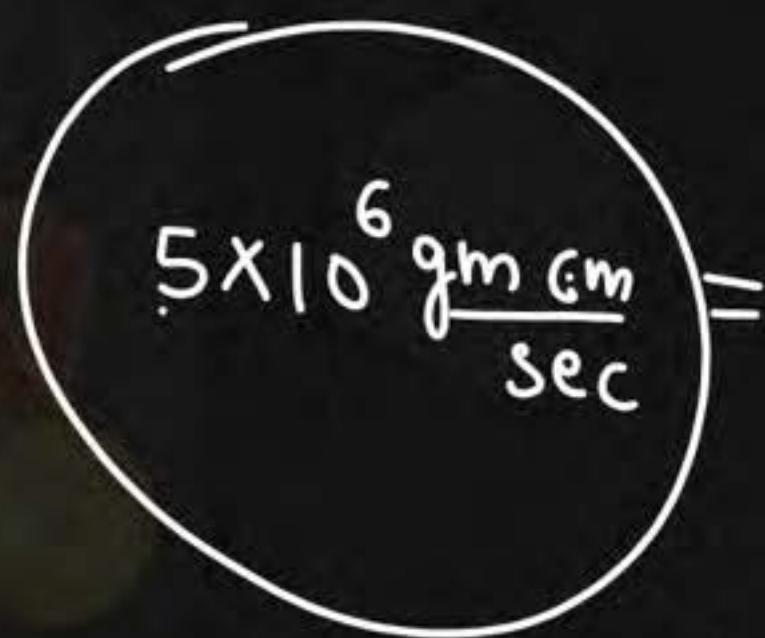
Q.



$$\text{momentum} = P = m \times v$$

$$= 10 \text{ kg} \times 5 \text{ m/s}$$

$$= 50 \frac{\text{kg m}}{\text{sec}} \quad \text{= mks syst}$$



$$= 50 \times \frac{1000 \text{ gm} \times 100 \text{ cm}}{\text{sec}}$$

Convert into CGS

momentum (CGS) system

Q

$$\text{Density} = 6 \text{ kg/m}^3 = 6 \frac{\text{kg}}{\text{m}^3}$$

Convert into CGS system

$$\text{Density} = 6 \times \frac{1000 \text{ gm}}{(100 \text{ cm})^3} = \frac{6 \times 1000 \text{ gm}}{10^6 \text{ cm}^3} = 6 \times 10^{-3} \text{ gm/cm}^3$$

Q Convert into mks system

$$\text{Density} = .6 \text{ gm/cc} = \frac{.6 \text{ gm}}{(\text{cm})^3}$$

$$= \frac{.6 \times \left(\frac{1 \text{ kg}}{1000} \right)}{\left(\frac{1 \text{ m}}{100} \right)^3}$$

$$= \frac{.6 \times 10^6}{1000} = 600 \text{ kg/m}^3$$

$$1 \text{ kg} = 1000 \text{ gm}$$

$$1 \text{ gm} = \frac{1 \text{ kg}}{1000}$$

Dimensional
formulae

$$\frac{L}{T} = LT^{-1}$$

$$[M^0 LT^{-1}]$$

$$[m^0 LT^{-1}]$$

$$[MLT^{-1}]$$

$$[ML^{-3}T^0]$$

Derived Physical Quantity

$$① \text{ Speed} = \frac{\text{Distance}}{\text{time}} \longrightarrow m/\text{sec} \longrightarrow cm/\text{sec}$$

$$② \text{ Velocity} = \frac{\text{Displacement}}{\text{time}} \longrightarrow m/\text{sec} \longrightarrow cm/\text{sec}$$

$$③ \text{ momentum } p = m \times v$$

$$④ \text{ Density} = \frac{\text{mass}}{\text{Vol}^n} \longrightarrow kg/m^3$$

Unit
(mks)

Unit
Cgs

gm cm/sec

gm/cm³

P
W

Dimensional formula of Density

$$\text{Density} = \frac{\text{mass}}{\text{volr}} \rightarrow \frac{M}{L \cdot L \cdot L} = \frac{m}{L^3} \Rightarrow [m L^{-3} T^0]$$

→ mass की Dimension क्या है	\Rightarrow	power = 1
→ " Length "	\Rightarrow	-3
→ " time "	\Rightarrow	0
→ " temp "	\Rightarrow	0

$$\text{Area} = \text{Length} \times \text{width} \Rightarrow$$

Volⁿ

$$L \cdot L = L^2 \Rightarrow [m^0 L^2 T^0]$$

$$\text{Density} = \frac{\text{mass}}{\text{Vol}^n} \rightarrow \frac{M}{L^3} \Rightarrow m^1 L^{-3} \Rightarrow [m L^{-3} T^0]$$

$$\text{speed} = \frac{\text{Distance}}{\text{time}} \rightarrow \frac{L}{T} \Rightarrow L T^{-1}$$

$$\text{velocity} = \frac{\text{Displacement}}{\text{time}} \rightarrow \frac{L}{T} \Rightarrow L T^{-1}$$

Dimension of Length in Area = 2

P
W

Dimensional formulae

Q.

mvr

If E, L, M and G denote the quantities as energy, angular momentum, mass and constant of gravitation respectively, then the dimensions of P in the formula $P = EL^2M^{-5}G^{-2}$ are :-

- A $[M^0 L^1 T^0]$
- B $[M^{-1} L^{-1} T^2]$
- C $[M^1 L^1 T^{-2}]$
- D $[M^0 L^0 T^0]$

$$\frac{EL^2}{m^5 G^2} = \frac{m L^2 T^{-2} (m L^2 T^{-1})^2}{m^5 (m^{-1} L^3 T^{-2})^2}$$

$$\frac{m^3 L^6 T^{-4}}{m^3 L^6 T^{-4}} = 1$$

(JEE Main-2021)

Ans : (D)

Q.

If force (F), length (L) and time (T) are taken as the fundamental quantities.

μ/ω Then what will be the dimension of density: $m L^{-3}$

(JEE Main-2021)

A

$$[FL^{-4} T^2]$$

= संघर्ष का साध

B

$$[FL^{-3} T^2]$$

C

$$[FL^{-5} T^2]$$

D

$$[FL^{-3} T^3]$$

$$\frac{FT^2}{L^4} = \frac{MLT^{-2}T^2}{L^4} = \frac{m}{L^3}$$

Ans : (A)

Q.

If momentum $[P]$, area $[A]$ and time $[T]$ are taken as fundamental quantities,
 $\text{H} \backslash \omega$ then the dimensional formula for coefficient of viscosity is: (JEE Main-2022)

A

$$[PA^{-1}T^0]$$

sqrt

B

$$[PA T^{-1}]$$

C

$$[PA^{-1}T]$$

D

$$[PA^{-1}T^{-1}]$$

$$\frac{P}{A} = \frac{m L T^{-1}}{L^2}$$

$$= m L^{-1} T^{-1}$$

$$F = 6\pi\lambda\eta v$$

$$\eta = \frac{F}{6\pi\lambda v} = \frac{m L T^{-2}}{L L T^{-1}}$$

$$\boxed{\eta = m L^{-1} T^{-1}}$$

class

Ans : (A)

Question

*Stan level ques
21179K*

Next class ñ

SET II adda

P
W

The gas equation for n moles of a real gas is: $\left(P + \frac{n^2 a}{V^2} \right) (V - nb) = nRT$ where P is the pressure, V is the volume, T is the absolute temperature, R is the molar gas constant and a, b are arbitrary constants. Which of the following have the same dimensions as those of PV ?

dimentionally

A

nRT

B

$n^2 a / V$

C

Pb

D

ab / V^2 *= तुम्हारा सवाल*

$$P = \frac{n^2 a}{V^2}$$

$$PV = \frac{n^2 a}{V}$$

$$V = nb \quad (\text{dimentionally})$$

$$b = \frac{V}{n}$$

$$\frac{PV}{n} = \frac{PV}{n} = \frac{PV}{\text{mol}}$$

Question

$$m l^2 T^{-2}$$

In a new unit system, 1 unit of time is equal to 10 second, 1 unit of mass is 5 kg and 1 unit of length is 20 m. In this new system of units, 1 unit of energy is equal to

$$= \frac{5 \text{ kg} \times (20 \text{ m})^2}{(10 \text{ sec})^2}$$

$$= 20 \text{ J}$$

- A** 20 Joule
- B** 1/20 Joule
- C** 4 Joule
- D** 16 Joule

(A)

Question



Which of the following statements is correct about conversion of units, for example

$$1 \text{ m} = 100 \text{ cm}$$

- A** Conversion of units have identical dimensions on each side of the equal sign but not the same units.
- B** Conversion of units have different dimensions on each side of the equal sign but have same unit
- C** If a larger unit is used then numerical value of physical quantity is large.
- D** Due to conversion of units physical quantity to be measured will change.

(A)

Question

Class

$$\textcircled{Q} \quad -\frac{5}{6} + \frac{1}{2} + \frac{1}{3} = \frac{-5+3+2}{6} = 0$$



A gas bubble oscillates with a time period T proportional to $P^a d^b E^c$ where P is pressure, d is the density and E is the energy. The values of a, b & c are

A

$$a = \frac{3}{2}, b = -\frac{1}{3}, c = \frac{1}{2}$$

B

$$a = -\frac{5}{6}, b = \frac{1}{3}, c = \frac{1}{2}$$

C

$$a = -\frac{5}{6}, b = \frac{1}{2}, c = \frac{1}{3}$$

D

$$a = \frac{3}{2}, b = -\frac{1}{3}, c = \frac{1}{2}$$

$$T = K P^a d^b E^c$$

$$= \cdot (m L^{-1} T^{-2})^a (m L^3)^b (m L^2 T^{-2})^c$$

$$\frac{F}{A}$$

$$M^0 L^0 T^1 = M^{a+b+c} L^{-a-3b+2c} T^{-2a-2c}$$

$$\begin{aligned} a+b+c &= 0 \\ -a-3b+2c &= 0 \end{aligned}$$

$$-2a-2c = 1$$

$$-2a-2c =$$

$$2 \times \frac{5}{6} - \frac{2}{3} = \frac{5}{3} - \frac{2}{3} = 1$$

(c)

Question

Class

$$\textcircled{Q} \quad -\frac{5}{6} + \frac{1}{2} + \frac{1}{3} = \frac{-5+3+2}{6} = 0$$



A gas bubble oscillates with a time period T proportional to $P^a d^b E^c$ where P is pressure, d is the density and E is the energy. The values of a, b & c are $\frac{F}{A}$

A

$$a = \frac{3}{2}, b = -\frac{1}{3}, c = \frac{1}{2}$$

B

$$a = -\frac{5}{6}, b = \frac{1}{3}, c = \frac{1}{2}$$

C

$$a = -\frac{5}{6}, b = \frac{1}{2}, c = \frac{1}{3}$$

D

$$a = \frac{3}{2}, b = -\frac{1}{3}, c = \frac{1}{2}$$

$$T = K P^a d^b E^c P^d A^e$$

$$M^0 L^0 T^1 = \frac{(M L^{-1} T^{-2})^a (M L^{-3})^b (M L^2 T^{-2})^c (M L T^{-1})^d}{(M^0 L^0 T^1)^{K+d}}$$

Variable

Unknown

तीन बराबर

 $a, b, c, d = ?$ Variable

Question

The energy E of an oscillating body in simple harmonic motion depends on its mass m , frequency n and amplitude A as $E = k(m)^x(n)^y(A)^z$. Find the value of $(2x + y + z)$.

$$\frac{1}{T^{-1}}$$

Class

Question

The value of Stefan's constant in CGS system is $\sigma = 5.67 \times 10^{-5} \text{ erg s}^{-1} \text{ cm}^{-2} \text{ K}^{-4}$. Its value in SI units is

$$\begin{aligned}\sigma &= \frac{5.67 \times 10^{-5} \text{ J}}{\text{s.} \left(\frac{1}{100} \text{ m}\right)^2 \text{ K}^4} \times \frac{1 \text{ J}}{10^7} \\ &= 5.67 \times 10^{-5+4-7} \left(\frac{\text{J}}{\text{sec. m}^2 \cdot \text{K}^4} \right) \\ &= 5.67 \times 10^{-8}\end{aligned}$$

Ans - $5.67 \times 10^{-8} \text{ J} \cdot \text{s}^{-1} \text{m}^{-2} \text{ K}^{-4}$

$$1 \text{ J} = 10^7 \text{ erg}$$

$$1 \text{ erg} = \frac{1 \text{ J}}{10^7}$$

Question

$$x \cdot y = \sqrt{xyz}$$

$$x \cdot x = \sqrt{xx} = \sqrt{x^2} = x$$

$$x^2 = \sqrt{xx}$$

$$x = \sqrt{\sqrt{xyz}} \equiv y = 3$$

Consider three physical quantities x, y and z . Operations $x + y$ and $y - z$ are valid with these physical quantities. Which of the following conclusions can you make?

- A** The operation $x \pm z$ is also valid.
- B** If dimension of any of the three is known, dimension of other two can be predicted.
- C** If dimension of product of any two of them is known, dimension of all of them can be predicted.
- D** If dimension of quotient of any two of them is known, dimension of all of them can be predicted.

$$\boxed{x, y, z} \equiv \text{Same D.F. एवं}$$

$$x \cdot y = L^2 \text{ (let)}$$

$$x \cdot x = x^2 = L^2$$

$$x = L$$

Dimension
of x

A, B, C

Question

Viscous force acting on a spherical ball is given by $F = 6\pi\eta rv$, where r is radius of the ball, v is the velocity of the ball & η is coefficient of viscosity. Dimension formula of η is given by $[\eta] = M^a L^{-b} T^{-c}$. Find the value of $a + b + c$

Class

$$\eta = \frac{F}{6\pi rv}$$

Q

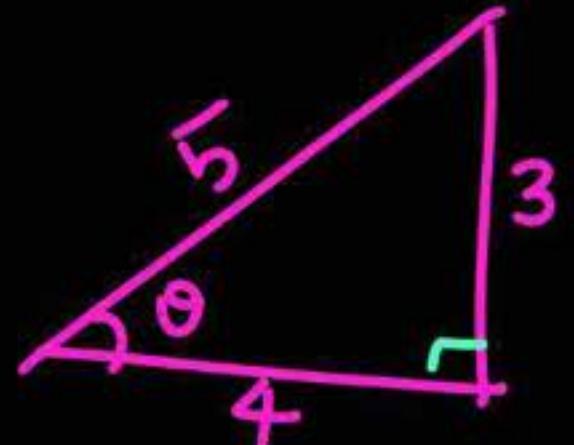
$$\cos \theta = \frac{4}{5}$$

find $\sin \theta = \frac{3}{5}$

$$\tan \theta = \frac{3}{4}$$

$$\cot \theta = \frac{4}{3}$$

$$\sec \theta = \frac{5}{4}$$



Q. In a hypothetical system

$$1 \text{ unit of mass} = 10 \text{ kg}$$

$$1 \text{ Unit of length} = 4 \text{ m}$$

$$1 \text{ Unit of Sec} = 2 \text{ sec}$$

$$\text{m L T}^{-2}$$

① Find value of 1 unit of force

$$1 \text{ Unit of force} = 10 \text{ kg} \cdot 4 \text{ m} \cdot (2 \text{ sec})^{-2} = \frac{10 \times 4}{4} \frac{\text{kg m}}{\text{sec}^2}$$

- ② Find value of 5 Unit of force in newton = 10 N
- ③ what is numerical value of 1 Newton in this new system.

In a hypothetical system (Alien system)

1 Unit of mass = 10 kg

" " length = 4 m

" " time = 2 sec

- ① ✓
- ② ✗

① 1 Unit of force = 10 N

② Numerical value of 1 N in this system.

10 N = 1 Unit of force in new system

$$10 \text{ N} = 1 \text{ N}' = 1 \text{ ওজ্বল}$$

$$1 \text{ N} = \frac{1}{10} \text{ N}'$$

Q In a alien system

1 unit of mass = 5 kg

1 unit of length = $\frac{1}{2}$ m

1 unit of time = 10 sec.

^{xout} C value of 20N in new system

$$1N = 40N'$$

$$20N = 20 \times 40N' = 800N'$$

① 1 unit of force in new system in terms of newton. $= \frac{5 \times \frac{1}{2}}{100} \frac{\text{kg m}}{\text{sec}^2}$
 $(1N')$
 $= \frac{1}{40} N$

② Numerical value of 1N in this system.

$$1N = \frac{1}{40} N$$

$$\boxed{1N = 40 N'}$$



Q In a alien system

$$1 \text{ unit of mass} = 5 \text{ kg}$$

$$1 \text{ unit of length} = \frac{1}{2} \text{ m}$$

$$1 \text{ unit of time} = 10 \text{ sec.}$$

$$m L^2 T^{-2}$$

④ 1 unit of Energy in new system in terms of Joule = $\frac{5 \text{ kg} \cdot \left(\frac{1}{2} \text{ m}\right)^2}{(10 \text{ sec})^2}$

$$1 J' = \frac{5}{400} \frac{\text{kg m}^2}{\text{sec}^2} = \frac{1}{80} \text{ J}$$

⑤ Numerical value of $1 J'$ in this system.

$$1 J' = \frac{1}{80} \text{ J}$$

$$1 J = 80 J'$$

⑥ Value of $20 J$ in this system.
 $= 1600 J'$

Q Convert 1N in dyne

Value of 1N in dyne

S.I. एकारा	3-एकारा (CGS)
$m_1 = 1 \text{ kg}$	$m_2 = 1 \text{ gm} = \frac{1}{1000} \text{ kg}$
$L_1 = 1 \text{ m}$	$L_2 = 1 \text{ m} = \frac{1}{100} \text{ m}$
$T_1 = 1 \text{ sec}$	$T_2 = 1 \text{ sec}$
$\frac{1 \text{ N}}{n_1 = 1}$	$n_2 = x$ MLT⁻²

$$n_1 U_1 = n_2 U_2$$

$$\frac{1 \times \cancel{\frac{\text{kg} \cdot \text{m}}{\text{sec}^2}}}{\cancel{\text{sec}^2}} = x \cancel{\frac{\text{kg}}{1000}} \cdot \frac{1}{100} \text{ m}$$

परिवर्तन की मदद से यह लिखा जा सकता है।
 यह विधि विकल्पों का अनुपयोग करके लिखा जा सकता है।
 यह विधि विकल्पों का अनुपयोग करके लिखा जा सकता है।
 यह विधि विकल्पों का अनुपयोग करके लिखा जा सकता है।
 यह विधि विकल्पों का अनुपयोग करके लिखा जा सकता है।

$$1 = \frac{x}{1000000}$$

$x = 10^5$

In a hypothetical system.

$$\begin{aligned} \text{1 unit of mass} &= 20 \text{ kg} \\ \text{, length} &= 2 \text{ m} \\ \text{, time} &= 2 \text{ sec.} \end{aligned}$$

Find the numerical value of 40N
in this system

EMRT

$$1N' = \frac{20 \text{ kg} \cdot 2 \text{ m.}}{(2 \text{ sec})^2} = 10 \frac{\text{kg m}}{\text{sec}^2}$$

$$1N' = 10 \text{ N}$$

$$\underline{4N' = 40 \text{ N}}$$

Ans

4

$$\begin{aligned} 10N &= 1N' \\ 1N &= \frac{1}{10} N' \\ 40N &= \frac{40}{10} N' \\ &= 4N' \end{aligned}$$

BOOK	40N = x N'
EHTI	

$$\begin{aligned} m_1 &= 1 \text{ kg} \\ L_1 &= 1 \text{ m} \\ T_1 &= 1 \text{ sec} \\ n_1 &= 40 \end{aligned}$$

3-NAT

$$\begin{aligned} m_2 &= 20 \text{ kg} \\ L_2 &= 2 \text{ m} \\ T_2 &= 2 \text{ sec} \\ N_2 &= ? \end{aligned}$$

$$n_1 U_1 = n_2 U_2$$

$$40 \times \frac{\text{kg m}}{\text{sec}^2} = n_2 \cdot \frac{20 \text{ kg} \cdot 2 \text{ m}}{(2 \text{ sec})^2}$$

$$n_2 = \frac{40 \times 4}{40}$$

$$\boxed{n_2 = 4}$$

Q In a hypothetical system

$$m^2 \cdot t^{-2}$$

$$1 \text{ unit of mass} = 10 \text{ kg}$$

$$\text{,, , length} = 2 \text{ m}$$

$$\text{,, , time} = 2 \text{ sec}$$

① 1 unit of energy in this system

$$1 \text{ J}' = \frac{10 \text{ kg} (2 \text{ m})^2}{(2 \text{ sec})^2} = 10 \frac{\text{kg m}^2}{\text{sec}^2}$$

$$1 \text{ J}' = 10 \text{ J}$$

Numerical value

② Value of 20 J in this system

$$10 \text{ J} = 1 \text{ J}'$$

$$20 \text{ J} = 2 \text{ J}'$$

$$\text{Ans } \frac{2}{2}$$

~~$$20 = n_2 \times \frac{10 \times 2}{2}$$~~

$$n_2 = 2$$

Q.

If momentum (P), area (A) and time (T) are taken to be the fundamental quantities then the dimensional formula for energy is:

मुद्रा

P
W

(JEE Main-2020)

- A** $[PA^{-1} T^{-2}]$
- B** $[PA^{1/2} T^{-1}]$
- C** $[P^2 AT^{-2}]$
- D** $[P^{1/2} AT^{-1}]$

 m_1

$$\begin{aligned} E &= P^x A^y T^z \\ &= (m L T^{-1})^x (L^2)^y T^z \end{aligned}$$

$$m L^2 T^{-2} = m^x L^{x+2y} T^{-x+z}$$

Compose

$$x=1, \quad x+2y=2$$

$$1+2y=2$$

$$y = \frac{1}{2}$$

$$-x+z = -2$$

$$-1+z = -2$$

$$z = -1$$

$$E = P^1 A^{\frac{1}{2}} T^{-1}$$

Ans : (B)

Q.

If momentum (P), area (A) and time (T) are taken to be the fundamental quantities then the dimensional formula for energy is:

मूल

P
W

(JEE Main-2020)

m^{-2} = Optimal check नहीं

 $m L^2 T^{-2}$

A

 $[PA^{-1} T^{-2}]$

B

 $[PA^{1/2} T^{-1}]$

C

 $[P^2 A T^{-2}]$

D

 $[P^{1/2} A T^{-1}]$

(A)

$$\frac{P}{A T^2} = \frac{m L T^{-1}}{L^2 T^2} = m L^{-1} T^{-3}$$

(B)

$$\frac{P \cdot A^{\frac{1}{2}}}{T} \equiv \frac{m L T^{-1} \cdot \sqrt{L^2}}{T} = m L^2 T^{-2}$$

match

Ans : (B)

Q.

$$mv \tau \Rightarrow M L^2 T^{-1}$$

If time (t), velocity (v), and angular momentum (ℓ) are taken as the fundamental units. Then the dimension of mass (m) in terms of t, v and ℓ is:

P
W

(JEE Main-2021)

A ~~$[t^{-1} v^1 \ell^{-2}]$~~

$$m = t^x v^y \ell^z$$

B ~~$[t^1 v^2 \ell^{-1}]$~~

$$= T^x (L T^{-1})^y (M L^2 T^{-1})^z$$

C $[t^{-2} v^{-1} \ell^1]$

$$M^1 L^0 T^0 = M^z L^{y+2z} T^{x-y-z}$$

D $[t^{-1} v^{-2} \ell^1]$

$$\boxed{T^z = 1}$$

$$y+2z=0$$

$$\boxed{y=-2}$$

$$x-y-z=0$$

$$x+2-1=0$$

$$\boxed{x=-1}$$

Ans : (D)

Q.

If E , L , M and G denote the quantities as energy, angular momentum, mass and constant of gravitation respectively, then the dimensions of P in the formula $P = EL^2M^{-5}G^{-2}$ are :-

A $[M^0 L^1 T^0]$

B $[M^{-1} L^{-1} T^2]$

C $[M^1 L^1 T^{-2}]$

D $[M^0 L^0 T^0]$

(JEE Main-2021)

Ans : (D)

Q.

If force (F), length (L) and time (T) are taken as the fundamental quantities.

μ/ω Then what will be the dimension of density:

(JEE Main-2021)

A

$$[FL^{-4} T^2]$$

B

$$[FL^{-3} T^2]$$

C

$$[FL^{-5} T^2]$$

D

$$[FL^{-3} T^3]$$

Ans : (A)

Q.

If momentum [P], area [A] and time [T] are taken as fundamental quantities, then the dimensional formula for coefficient of viscosity is : (JEE Main-2022)

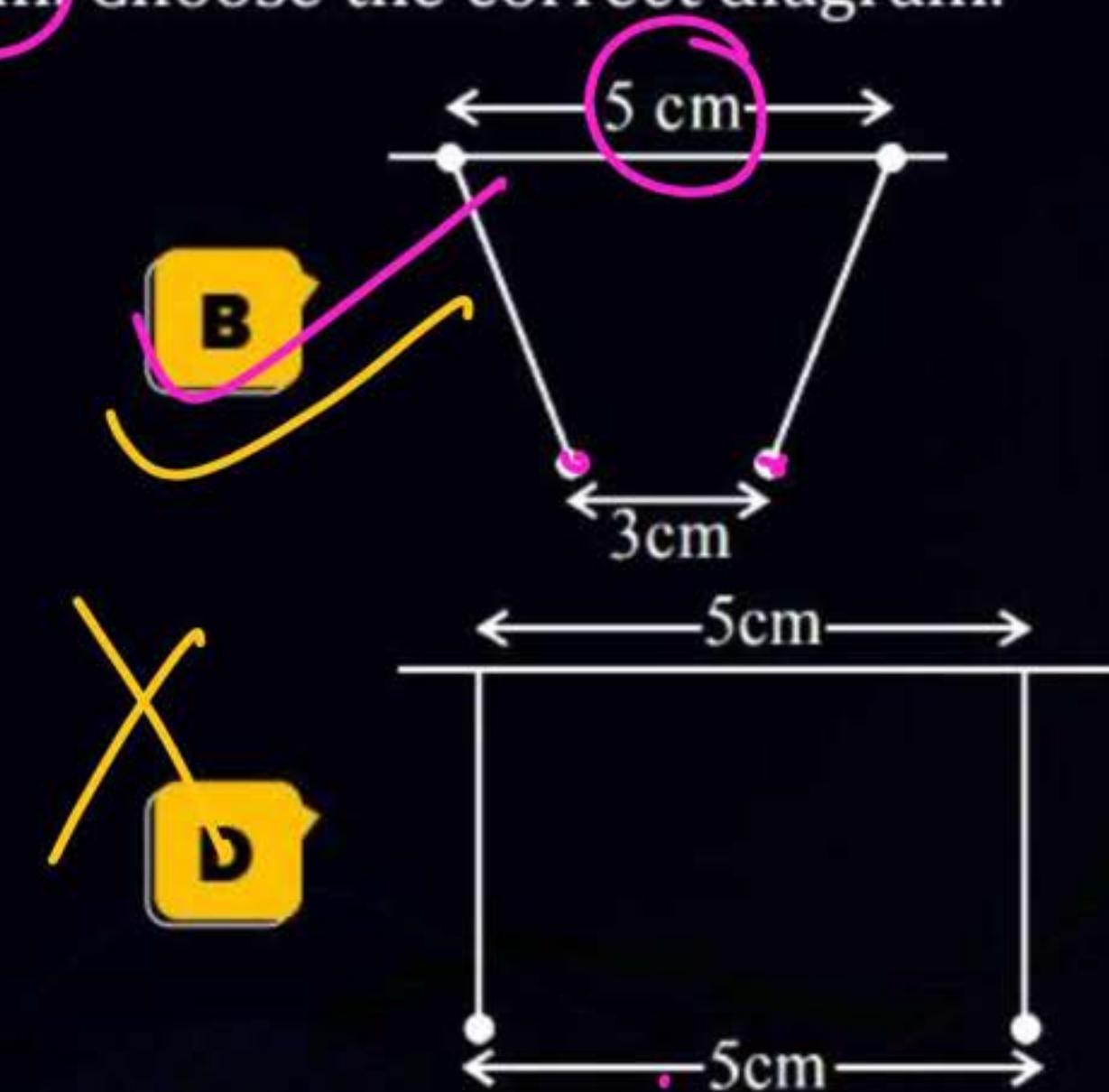
$$F = 6\pi\lambda\eta v$$

- A** $[P A^{-1} T^0]$
- B** $[PA T^{-1}]$
- C** $[P A^{-1} T]$
- D** $[P A^{-1} T^{-1}]$

Ans : (A)

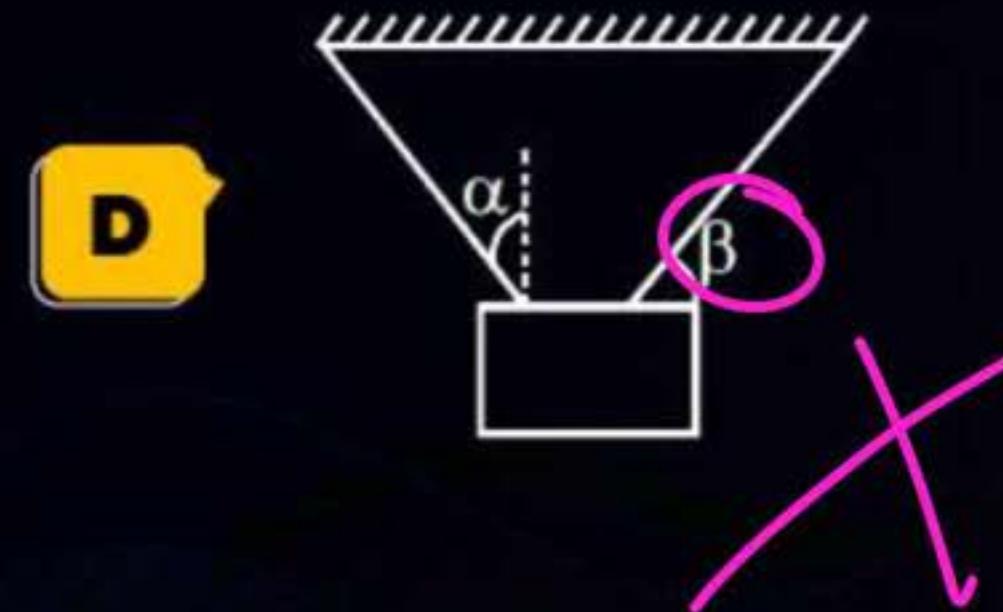
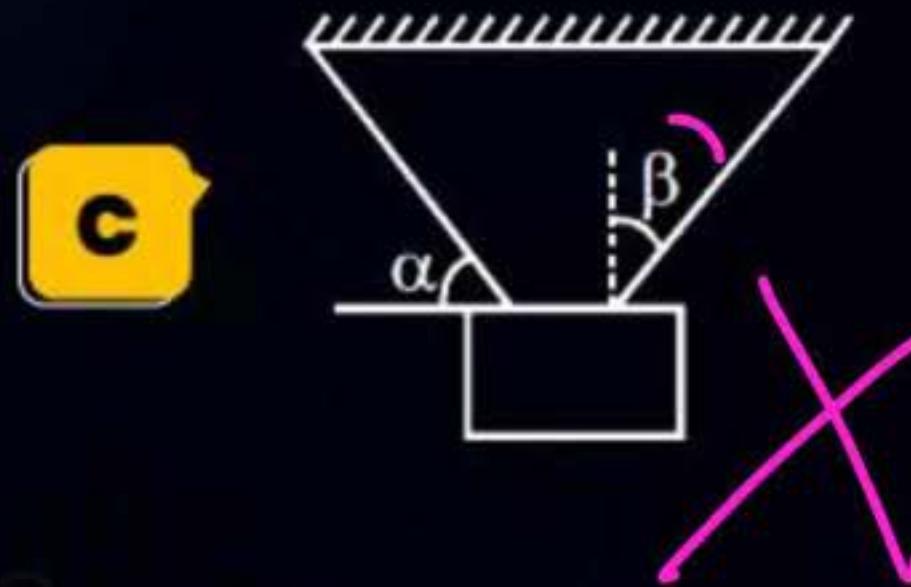
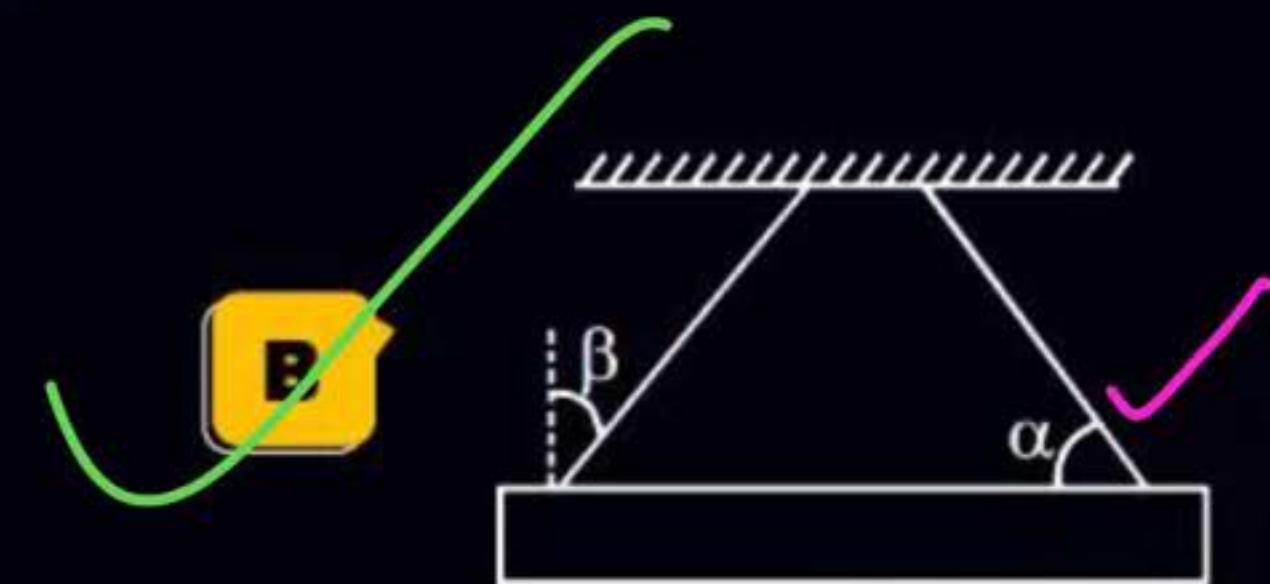
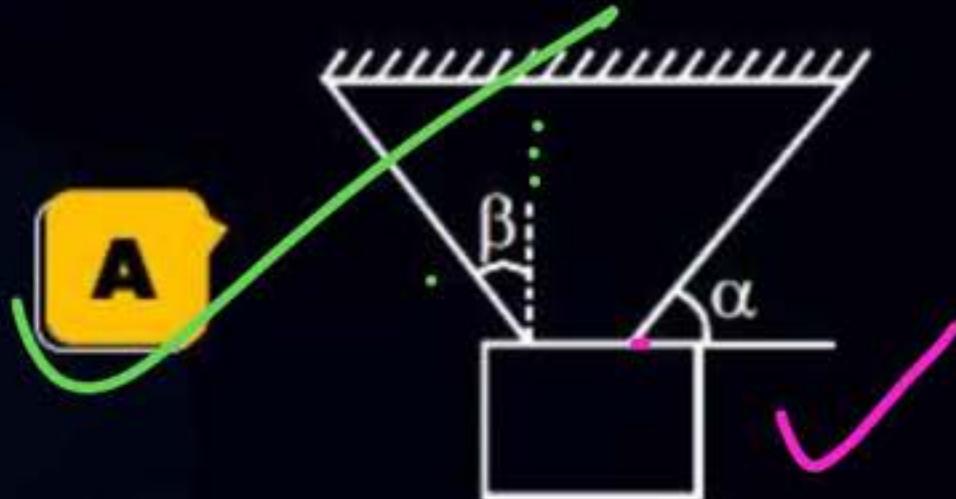
Question

Two oppositely charge particles attract to each other. Two charge particles having equal and opposite charge are suspended from a horizontal rod through two string of same length the separation between the suspension points being 5 cm. In equilibrium, the separation between the particles is 3 cm. Choose the correct diagram.



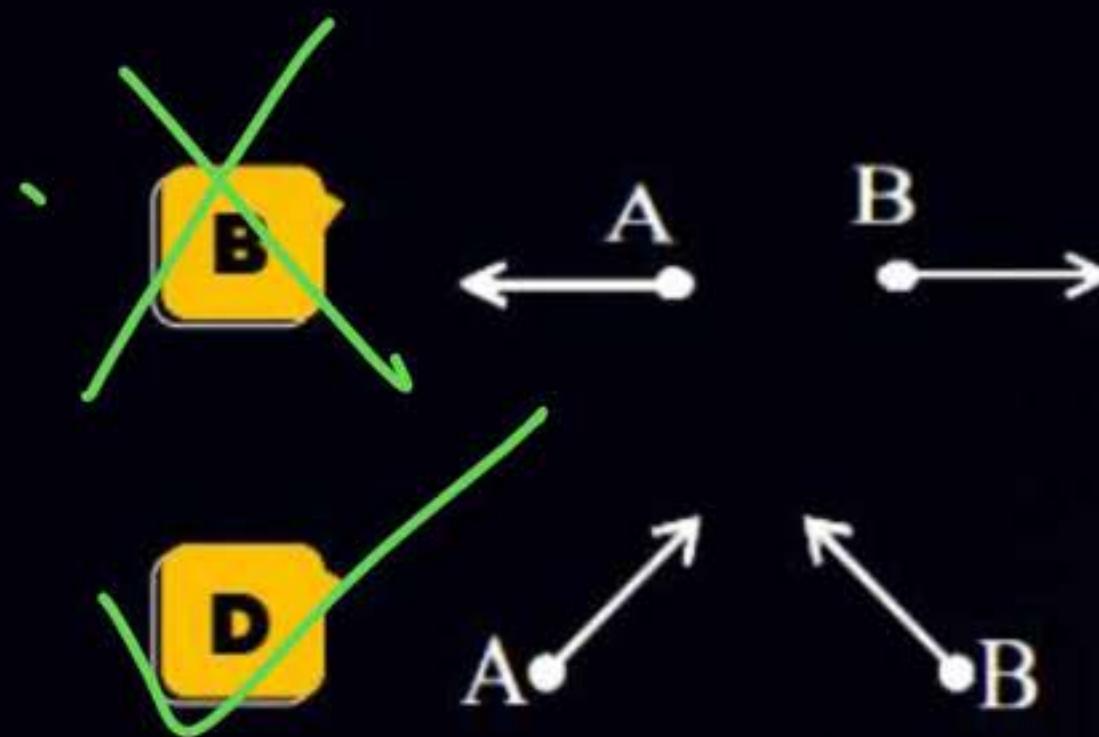
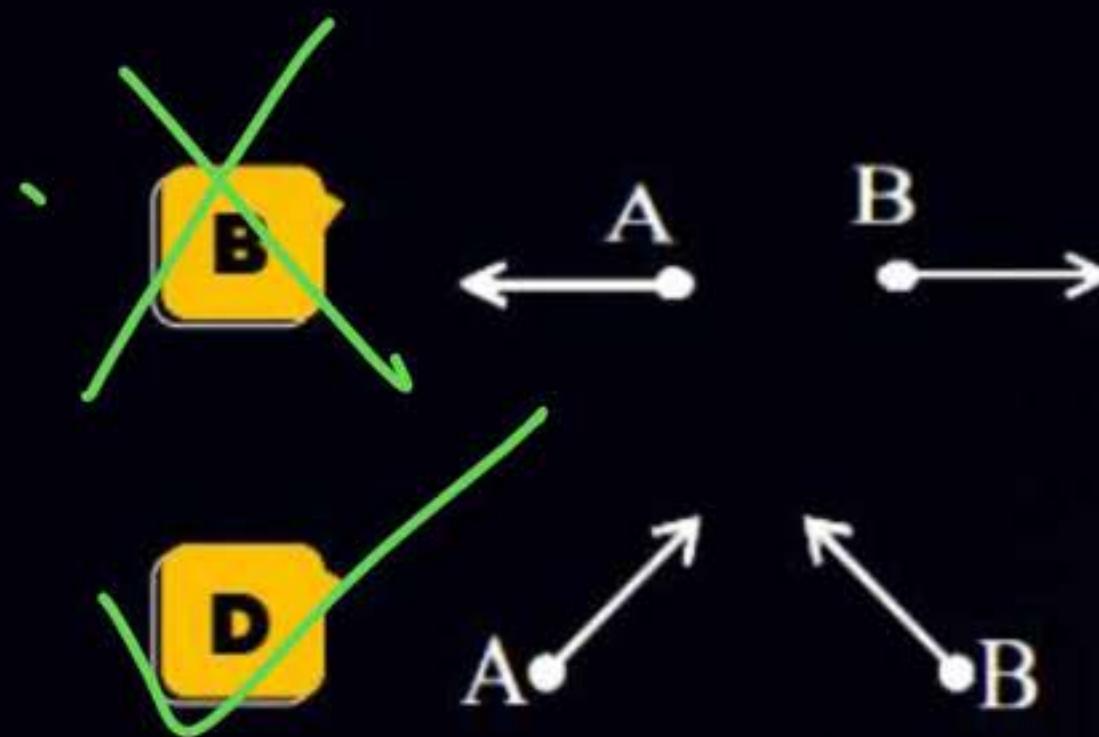
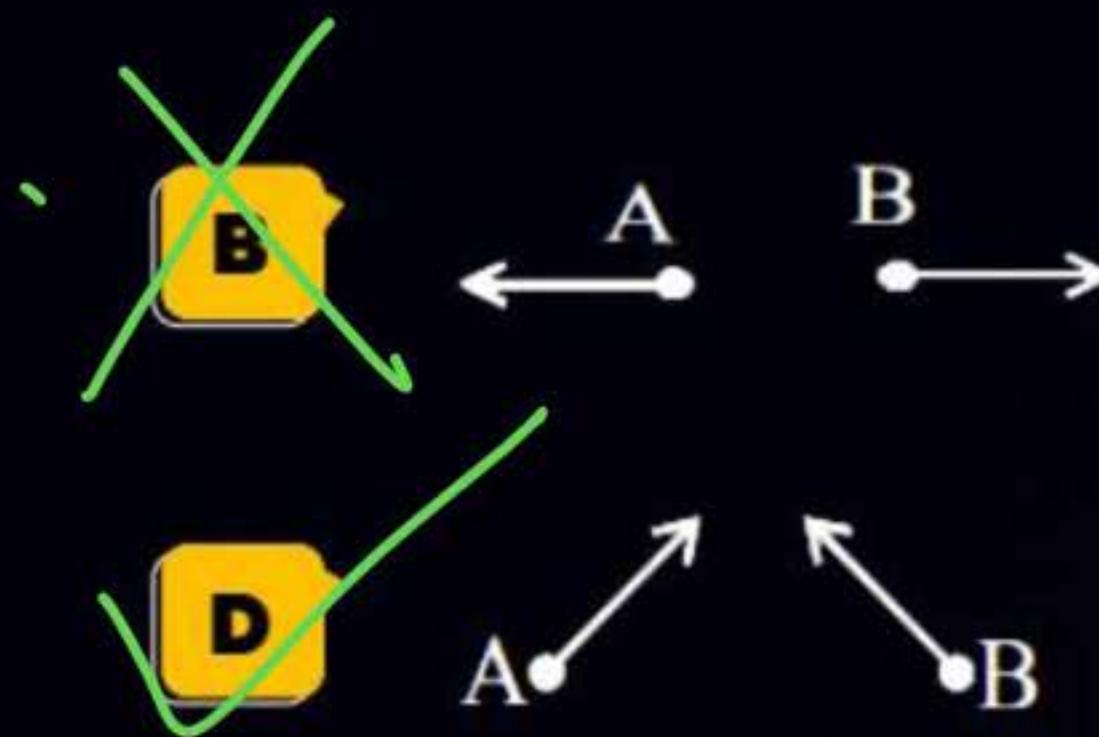
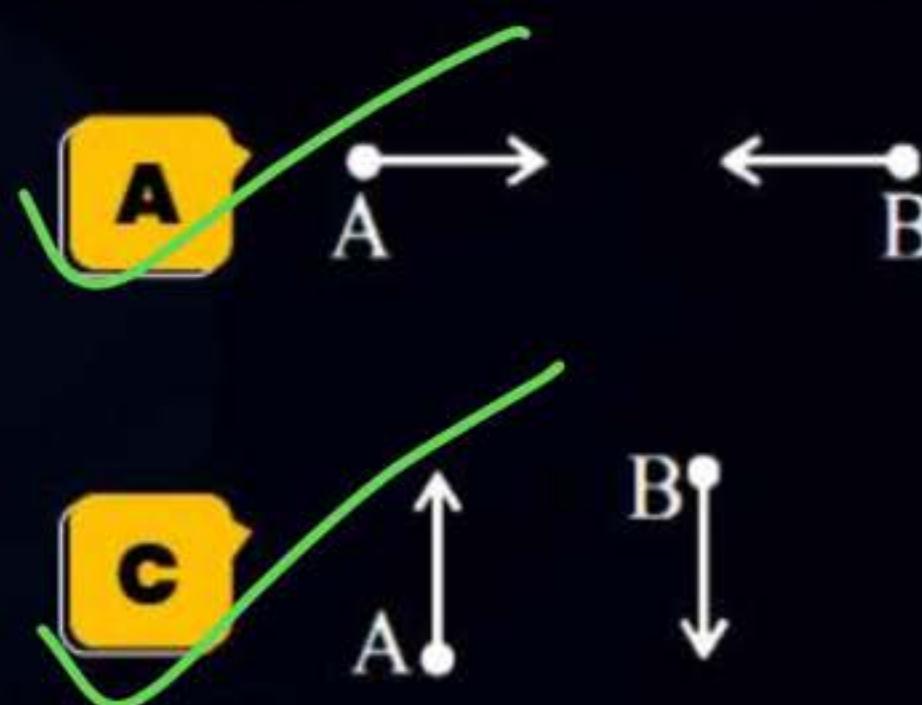
Question

A body of mass m is suspended by two strings (right string equals an angle α with horizontal & left an angle β with vertical). Choose the correct diagrams showing the situation.



Question

Two objects are said to approach each other if separation between them is decreasing and recede if separation between them is increasing with time. The following diagrams show location and direction of velocity of the two objects. Choose the situation in which they are approaching



Question

E, m, L, G denote energy, mass, angular momentum & gravitation constant respectively.

The dimensions of $\frac{E L^2}{m^5 G^2}$ will be that of :

- A** angle
- B** length
- C** mass
- D** time

Class

$$\frac{m L^2 T^{-2} \cdot (m L^2 T^{-2})^2}{m^5 (m^{-1} L^3 T^{-2})^2} = 1$$

Dimension

Question

Which of the following combinations of three dimensionally different physical quantities P, Q, R can never be a meaningful quantity?

A $PQ - R$

B PQ/R

C $(P - Q)/R$

D $(PR - Q^2)/QR$

Ans C —

Question

~~21179K~~ Next class 

The gas equation for n moles of a real gas is: $\left(P + \frac{n^2a}{V^2}\right)(V - nb) = nRT$ where P is the pressure, V is the volume, T is the absolute temperature, R is the molar gas constant and a, b are arbitrary constants. Which of the following have the same dimensions as those of PV ?

A nRT

B n^2a/V

C Pb

D ab/V^2

Question

The answer to Q.5.226 of I.E. Irodov is $\Delta\lambda = -\lambda \sqrt{\frac{2\Psi}{mv^2}} \cos \theta$. Here symbols have their usual notations. Ψ can represent

- A kinetic energy
- B power
- C force
- D pressure

Wavelength

$$\Delta\lambda = -\lambda \sqrt{\frac{2\Psi}{mv^2}} \cos \theta$$

Change in Wavelength

dimensions

dimensions

$$\Psi \equiv mv^2$$

Question

Class Notes

The dimensions of $\frac{a}{b}$ in the equation $P = \frac{a-t^2}{bx}$ where P is pressure, x is distance and t is time, are

Solve

$$a = T^2$$

$$a = T^2$$

$$m^{-1}L^{-2} = \frac{T^2}{b \cdot L}$$

$$b = m^{-1}L^0 T^{-4}$$

$$\frac{a}{b} = \frac{T^2}{m^{-1}L^0 T^{-4}} = m^1 L^0 T^{-2}$$

- A $[M^2 L T^{-3}]$
- B $[MT^{-2}]$
- C $[LT^{-3}]$
- D $[ML^3 T^{-1}]$

Question

Which of the following physical quantities represents the dimensional formula

$$[M^1 L^{-2} T^{-2}]$$

Clear

$$\frac{ML^2T^{-2}}{L^2} = ML^0T^{-2}$$

- A Energy/Area
- B Pressure
- C Force \times length
- D Pressure per unit length

$$\frac{MLT^{-2}}{L^2 \cdot L} = ML^2T^{-2}$$

Question

The time dependence of a physical quantity p is given by $p = p_0 e^{(-\alpha t^2)}$ where α is constant and t is time. The constant α

- A** is dimensionless
- B** has dimensions T^{-2}
- C** has dimensions T^2
- D** has dimensions of p

$$\propto t^2 = 1$$

$$\propto T^2 = 1$$

$$\propto = T^{-2}$$

Conversion of Unit

P
W

① $P = 20 \frac{\text{Kg m}}{\text{sec}}$ Convert into CGS $\rightarrow \frac{20 \times 1000 \text{ gm.} \times 100 \text{ cm}}{\text{sec}}$
 $= 2 \times 10^6 \frac{\text{gm cm}}{\text{sec}}$ ✓

$$\text{force} \rightarrow \text{MLT}^{-2}$$

Q Convert 1N into dyne dyne \rightarrow Unit of force
 Convert 1N into CGS system in CGS System.

Sol

$$1\text{N} = \frac{1\text{Kg m}}{\text{sec}^2}$$

convert
into CGS system

$$\frac{1 \times 1000 \text{gm}}{\text{sec}^2} \times 100 \text{cm}$$

$$= 10^5 \frac{\text{gm} \cdot \text{cm}}{\text{sec}^2}$$

Unit of
force
CGS
system

$$= 10^5 \text{ dyne}$$

Q

$$375 \text{ N} \xrightarrow[\text{CGS}]{\text{convert into}} \rightarrow$$

$$375 \frac{\text{kg m}}{\text{sec}^2} \xrightarrow[\text{CGS} \checkmark]{\text{CGS}} \frac{375 \times 1000 \text{ gm} \times 100 \text{ cm}}{\text{sec}^2}$$

$$= 37500000$$

$$= 375 \times 10^5$$

$\frac{\text{gm cm}}{\text{sec}^2}$
dynes

Q

Convert 1 Joule into CGS system
 " " "

erg

(erg → Unit of energy in
CGS system)

$$1 \text{ J} = 1 \frac{\text{kg m}^2}{\text{sec}^2}$$

convert
into CGS

$$\frac{1 \times 1000 \text{ gm} \times (100 \text{ cm})^2}{\text{sec}^2}$$

$$= 10^7 \frac{\text{gm cm}^2}{\text{sec}^2}$$

$$= 10^7 \text{ erg.}$$

$m L T^{-2}$

$$\text{Q} m=5 \text{kg}, a=3 \text{m/sec}^2$$

$$F = m \cdot a$$

$$= 5 \text{kg} \cdot 3 \text{m/sec}^2$$

$$= 15 \boxed{\text{kg m/sec}^2}$$

$$= 15 \text{ N}$$

SKC

$$1 \text{N} = \frac{1 \text{kgm}}{\text{sec}^2}$$

$$1 \text{ dyne} = \frac{1 \text{ gm cm}}{\text{sec}^2}$$

$$1 \text{ Joule} = \frac{1 \text{ kgm}^2}{\text{sec}^2}$$

$$1 \text{ erg} = \frac{1 \text{ gm} \cdot \text{cm}^2}{\text{sec}^2}$$

$$1 \text{m} = 100 \text{cm}$$

Q.

कार्य

In a hypothetical system

EMRI Method

$$1 \text{ unit of mass} = 20 \text{ kg}$$

$$1 \text{ unit of length} = 5 \text{ m}$$

$$1 \text{ unit of time} = 2 \text{ sec.}$$

a) Find value of 1 unit of force

$$1 \text{ unit of force} = 20 \text{ kg} \cdot 5 \text{ m} (2 \text{ sec})^{-2}$$

$$= \frac{20 \times 5}{4} \frac{\text{kg} \cdot \text{m.}}{\text{sec}^2}$$

$$= 25 \text{ N}$$

(b) find the value
of 1 unit of energy

$$20 \text{ kg} (5 \text{ m})^2 (2 \text{ sec})^{-2}$$

$$= \frac{20 \times 25}{4} \frac{\text{kg} \cdot \text{m}^2}{\text{sec}^2}$$

$$= 125 \text{ Joule.}$$

Q.

In a hypothetical system

P
W

1 unit of mass = 20 kg

1 Unit of length = 5 m

1 Unit of sec = 2 sec.

① Find value of 1 unit of force

m-2 Book काली method

Q.

In a hypothetical system

BY

P
W

1 unit of mass = 5 kg

1 Unit of length = 2 m

1 Unit of sec = 2 sec.

② Find the value of
1 Unit of energy

① Find value of 1 unit of force

$$5 \text{ kg} \cdot 2 \text{ m} \cdot (2 \text{ sec})^{-2}$$

$$= \frac{10}{4} \text{ kg m/sec}^2 = 2.5 \text{ N}$$

$$\frac{5 \text{ kg} \cdot (2 \text{ m})^2}{(2 \text{ sec})^2} = \frac{5 \text{ kg m}^2}{\text{sec}^2}$$

= 5 Joule.

Q. Time period of a simple pendulum depends on 'm' of block
length of string (l) & acc due to gravity g
Derived the formula for time period.

P
W

$$T = k m^x l^y g^z$$

$$M^0 L^0 T^1 = M^x L^y (L T^{-2})^z$$

$$1 = k m^x$$



$$T = K m^x l^y g^z$$

$$m^0 l^0 T^{-1} = m^x l^y (l T^{-2})^z$$

$$= m^x l^y l^z T^{-2z}$$

$$m^0 l^0 T^1 = m^x l^{y+z} T^{-2z}$$

Compare

$$x=0,$$

$$y+z=0$$

$$-2z=1 \Rightarrow z=-\frac{1}{2}$$

$$y=-z=-\left(-\frac{1}{2}\right)=\frac{1}{2}$$

$$T = K m^0 l^{\frac{1}{2}} \cdot g^{-\frac{1}{2}} = \frac{K \sqrt{l}}{\sqrt{g}}$$

$$T = K \sqrt{\frac{l}{g}}$$

(E) $E = K m^x A^y f^z$ Ans
Q Energy of a particle performing SHM depends on
mass (m) of object , Amplitude (A), frequency f of motion
Derive the relation b/w them.

प्र० सा कदम

जो Dimensionless हैं

$$E \propto m^x A^y f^z$$

$$ml^2 T^{-2} = m^x l^y (T^{-1})^z$$

$$ml^2 T^{-2} = m^x l^y T^{-z}$$

Compare.

$$x = 1$$

$$y = 2$$

$$-3 = -2$$

$$z = 2$$

$$E = K m A^2 f^2$$

Q Suppose force depends on mass(m), speed(v), and radius 'r'
Derive the relation b/w them

$$F = K m^x v^y r^z$$

$$m L T^{-2} = m^x (L T^{-1})^y L^z$$

$$m^1 L T^{-2} = m^x L^y T^{-y}$$

Compare power

$$x = 1$$

$$-y = -2$$

$$y = 2$$

$$y + z = 1$$

$$2 + z = 1$$

$$z = -1$$

प्रताग्री

$$F = K m^1 v^2 r^{-1}$$

$$F = K \frac{m v^2}{r}$$

en अभी कुछ
नहीं पता

Q A satellite is revolving around the earth such that

time period T of satellite depends on M (mass of earth), gravitational const (G), and radius of orbit r ,

Derive the formula for time period of satellite

$$T = K m^{\frac{1}{2}} G^{\frac{1}{2}} r^{\frac{3}{2}}$$

✓

$2 \times$

$3 \rightarrow$ इवान्दी
लिखी

$$T = K m^x G^y r^z$$

$$T = m^x (m^{-1} L^3 T^{-2})^y L^z$$

$$m^0 L^0 T^1 = m^{x-y} L^{3y+z} T^{-2y}$$

$$x - y = b$$

$$x = y \Rightarrow x = -\frac{1}{2}$$

$$\begin{cases} -2y = 1 \\ y = -\frac{1}{2} \end{cases}$$

$$G = m^{-1} L^3 T^{-2}$$

$$3y + z = 0$$

$$3 = -3y = +3/2$$

H/w Q A satellite is revolving around the earth such that
 Orbital velocity v_o of satellite depends on M (mass of earth), gravitational cons. (G), and radius of orbit r ,
 Derive the formula for orbital velocity of satellite

$$v_o = k m^{\frac{1}{2}} G^{\frac{1}{2}} r^{-\frac{1}{2}}$$

$$v_o = k M^x G^y r^z$$

$$LT^{-1} = M^x (m^{-1} L^3 T^{-2})^y L^z$$

$$m^0 LT^{-1}$$

$$= m^{x-y} L^{3y+z} T^{-2y}$$

① ✓

② ✗

③ try to fit

$$G = m^{-1} L^3 T^{-2}$$

$$y = \frac{1}{2}, x-y = 0$$

$$x-y = \frac{1}{2}$$

$$3y+z=1$$

$$\frac{3}{2} + z = 1 \Rightarrow z = -\frac{1}{2}$$

Q.

$$E = h\nu \quad h = \frac{E}{\nu}$$

A quantity f is given by $f = \sqrt{\frac{hc^5}{G}}$ where c is speed of light, G universal gravitational constant and h is the Planck's constant. Dimension of f is that of:

(IIT Main-2020)

- A** Momentum
- B** Area
- C** Energy
- D** Volume

$$\sqrt{\frac{m L^2 T^{-2}}{T^{-1}} \times \frac{(L T^{-1})^5}{m^{-1} L^3 T^{-2}}} = \sqrt{m^2 L^4 T^{-4}} \\ = \boxed{m L^2 T^{-2}}$$

Ans : (C)

Q.

Amount of solar energy received on the earth's surface per unit area per unit time is defined a solar constant. Dimension of solar constant is: (JEE Main-2020)

A $ML^2 T^{-2}$

B MLT^{-2}

C $M^2 L^0 T^{-1}$

D $ML^0 T^{-3}$

$$\text{Solar const} = \frac{E}{\text{Area of one square meter}} = \frac{m L^2 T^{-2}}{L^2 \cdot T^{-1}}$$

⇒ $m' L^0 T^{-3}$

Ans : (D)

Q.

Tough Go... gently (J)

In a typical combustion engine the work done by a gas molecule is given

$W = \alpha^2 \beta e^{\frac{-\beta x^2}{kT}}$, where x is the displacement, k is the Boltzmann constant and T is the temperature. If α and β are constants, dimensions of α will be:

(JEE Main-2021)

- A [MLT⁻²]
- B [M⁰LT⁰] $\beta = m T^{-2}$
- C [M²LT⁻²]
- D [MLT⁻¹]

$$\frac{\beta L^2}{m L^2 T^{-2}} = 1$$

$$\boxed{\beta = m T^{-2}}$$

$$W = \alpha^2 \beta e^{(\quad)}$$

~~$ML^2 T^{-2} = \alpha^2 m T^{-2}$~~

~~$\alpha^2 = L^2$~~

$$\alpha = L$$

Ans : (B)

Q.

The force is given in terms of time t and displacement x by the equation $F = A \cos(Bx) + C \sin(Dt)$. The dimensional formula of AD/B is: (JEE Main-2021)

A

$$[M^0 L T^{-1}]$$

B

$$[M L^2 T^{-3}]$$

C

$$[M^1 L^1 T^{-2}]$$

D

$$[M^2 L^2 T^{-3}]$$

$$\begin{aligned} D &= T^{-1} \\ B &= L^{-1} \end{aligned}$$

$A \rightarrow$ force

$$\frac{AD}{B} = \frac{MLT^{-2} \cdot T^{-1}}{L^{-1}}$$

$$ML^2 T^{-3}$$

Ans : (B)

Q.

Match List-I with List-II.

(JEE Main-2021)

P
W

List-I

- (a) Torque
- (b) Impulse
- (c) Tension
- (d) Surface Tension



List-II

- (i) MLT^{-1}
- (ii) MT^{-2}
- (iii) ML^2T^{-2}
- (iv) MLT^{-2}

Choose the most appropriate answer from the option given below :

A

(a)-(iii), (b)-(i), (c)-(iv), (d)-(ii)

B

(a)-(ii), (b)-(i), (c)-(iv), (d)-(iii)

C

(a)-(i), (b)-(iii), (c)-(iv), (d)-(ii)

D

(a)-(iii), (b)-(iv), (c)-(i), (d)-(ii)

Ans : (A)

$$\text{Q} \quad \overrightarrow{A} = 3\hat{i} + 4\hat{j} + 5\hat{k}$$

$$\overrightarrow{B} = 2\hat{i} + 3\hat{j} - 2\hat{k}$$

$$\overrightarrow{A} + \overrightarrow{B} = 5\hat{i} + 7\hat{j} + 3\hat{k}$$

$$\text{Q} \quad \overrightarrow{A} = 3\hat{i} + 4\hat{j} + 6\hat{k}$$

$$2\overrightarrow{A} = 6\hat{i} + 8\hat{j} + 12\hat{k}$$

$$= 2(3\hat{i} + 4\hat{j} + 6\hat{k})$$

$$-3\overrightarrow{A} = -9\hat{i} - 12\hat{j} - 18\hat{k}$$

$$\text{Q} \quad \overrightarrow{A} = 6\hat{i} + 3\hat{j} + 2\hat{k}$$

$$\overrightarrow{B} = \hat{i} + 6\hat{j} + 5\hat{k}$$

$$\overrightarrow{A} + \overrightarrow{B} = 7\hat{i} + 9\hat{j} + 7\hat{k}$$

$$\text{Q} \quad \overrightarrow{A} = 7\hat{i} + 3\hat{j} + 8\hat{k}$$

$$\overrightarrow{B} = 5\hat{i} + \hat{j} + 2\hat{k}$$

$$\overrightarrow{A} - \overrightarrow{B} = 2\hat{i} + 2\hat{j} + 6\hat{k}$$

$$\textcircled{1} \quad \vec{A} = 3\hat{i} + 2\hat{j} + 5\hat{k}$$

$$\vec{B} = 2\hat{i} + 3\hat{j} + 4\hat{k}$$

$$\textcircled{2} \quad \vec{A} + \vec{B} = 5\hat{i} + 5\hat{j} + 9\hat{k}$$

$$\textcircled{3} \quad \vec{A} - \vec{B} = \hat{i} - \hat{j} + \hat{k} \equiv$$

$$\textcircled{4} \quad |\vec{A} + \vec{B}| = \sqrt{5^2 + 5^2 + 9^2}$$

$$\textcircled{5} \quad |\vec{A} - \vec{B}| = \sqrt{3}$$

$$\textcircled{6} \quad 2\vec{A} + 3\vec{B} = 12\hat{i} + 13\hat{j} + 22\hat{k}$$

$$(6) \quad |2\vec{A} + 3\vec{B}| = \sqrt{(12)^2 + (13)^2 + (22)^2}$$

$$\textcircled{7} \quad 2\vec{A} - 3\vec{B} = 0\hat{i} + (4 - 9)\hat{j}$$

$$+ (10 - 12)\hat{k}$$

$$= -5\hat{j} - 2\hat{k}$$

Q $\vec{A} = 2\hat{i} + \hat{j} + \hat{k}$
 $\vec{B} = 4\hat{i} + \hat{j} + 4\hat{k}$

find a vector \vec{C} whose magnitude is 20 and dir^n is
opposite to $4\vec{A} + \vec{B}$

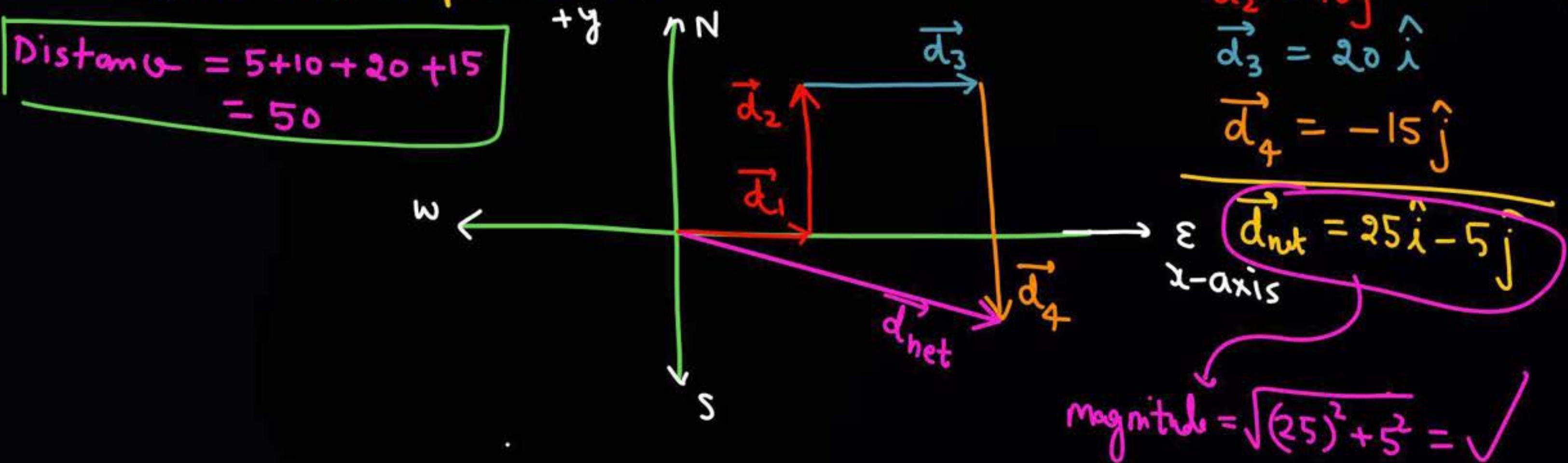
$$4\vec{A} + \vec{B} = 12\hat{i} + 5\hat{j} + 8\hat{k}$$

Ans $\Rightarrow -20 \times \left(\frac{12\hat{i} + 5\hat{j} + 8\hat{k}}{\sqrt{12^2 + 5^2 + 8^2}} \right)$

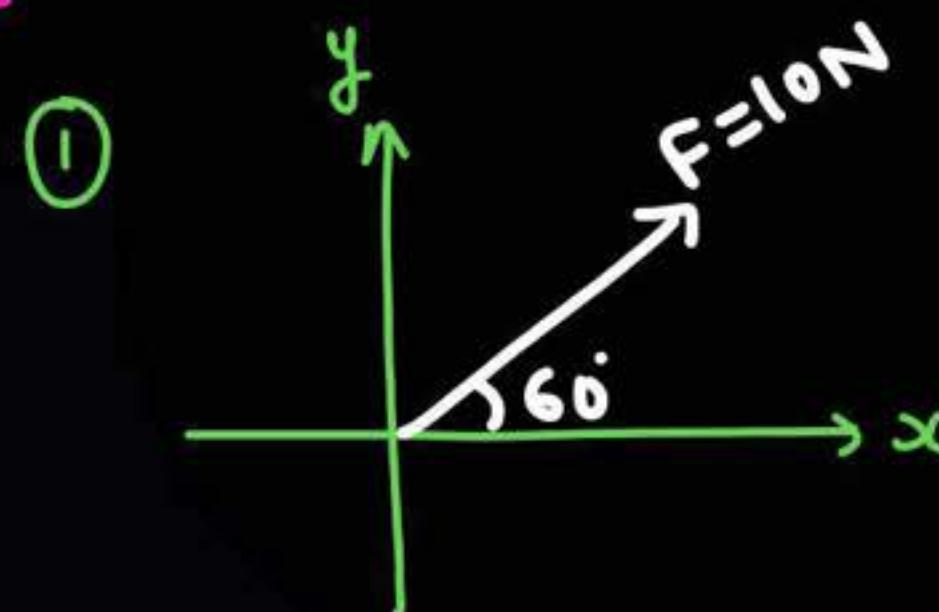
mihus

Kinematics

Q A man move 5m along east, then turn left & move 10m along north, then turn right and move 20m east & then turn right to south & move 15m. find net displacement, Distance travel



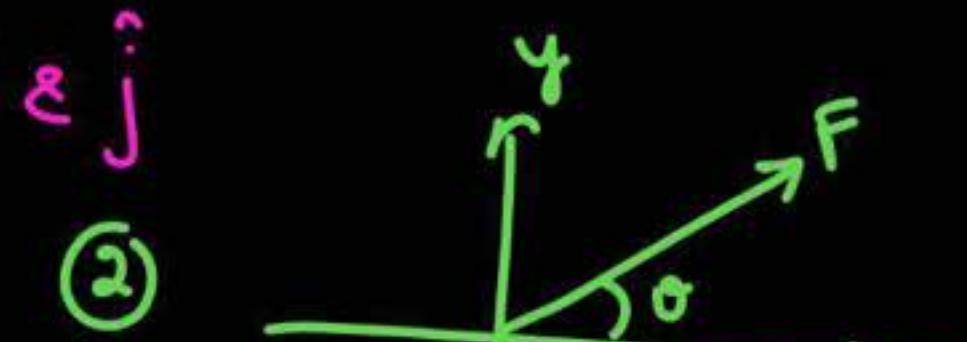
Q Resolve the vector into \hat{i} & \hat{j}



$$\vec{F} = 10\cos 60 \hat{i} + 10\sin 60 \hat{j}$$

$$= 10 \times \frac{1}{2} \hat{i} + 10 \frac{\sqrt{3}}{2} \hat{j}$$

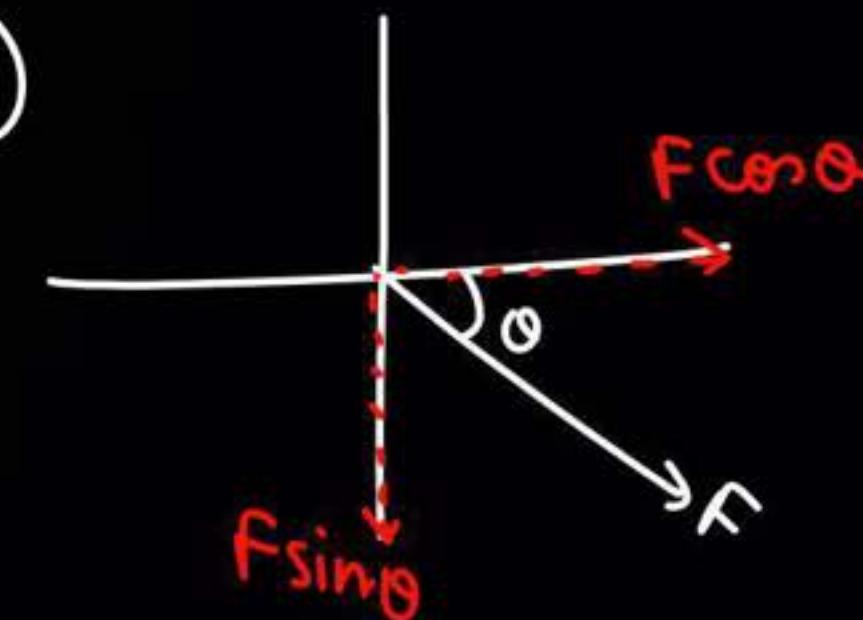
$$\boxed{\vec{F} = 5\hat{i} + 5\sqrt{3}\hat{j}}$$



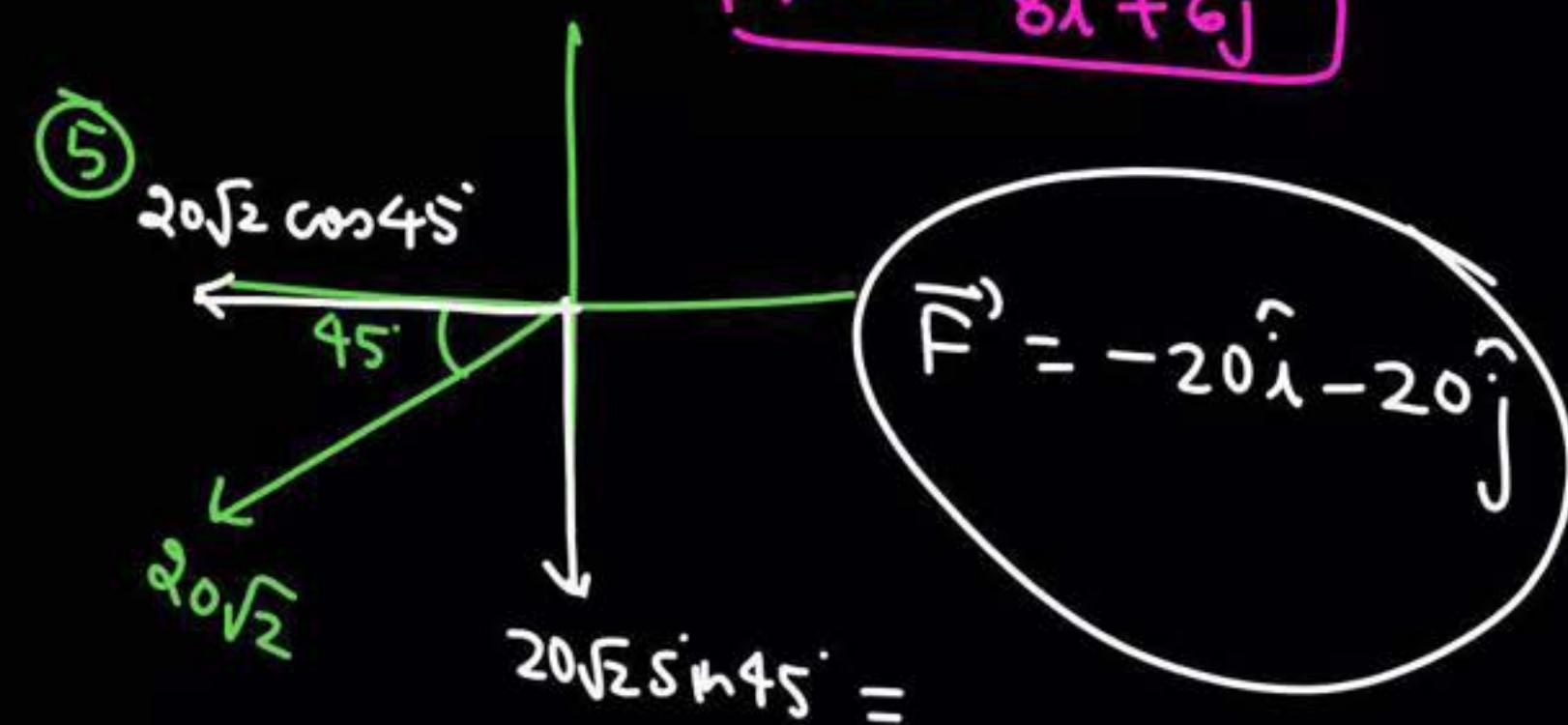
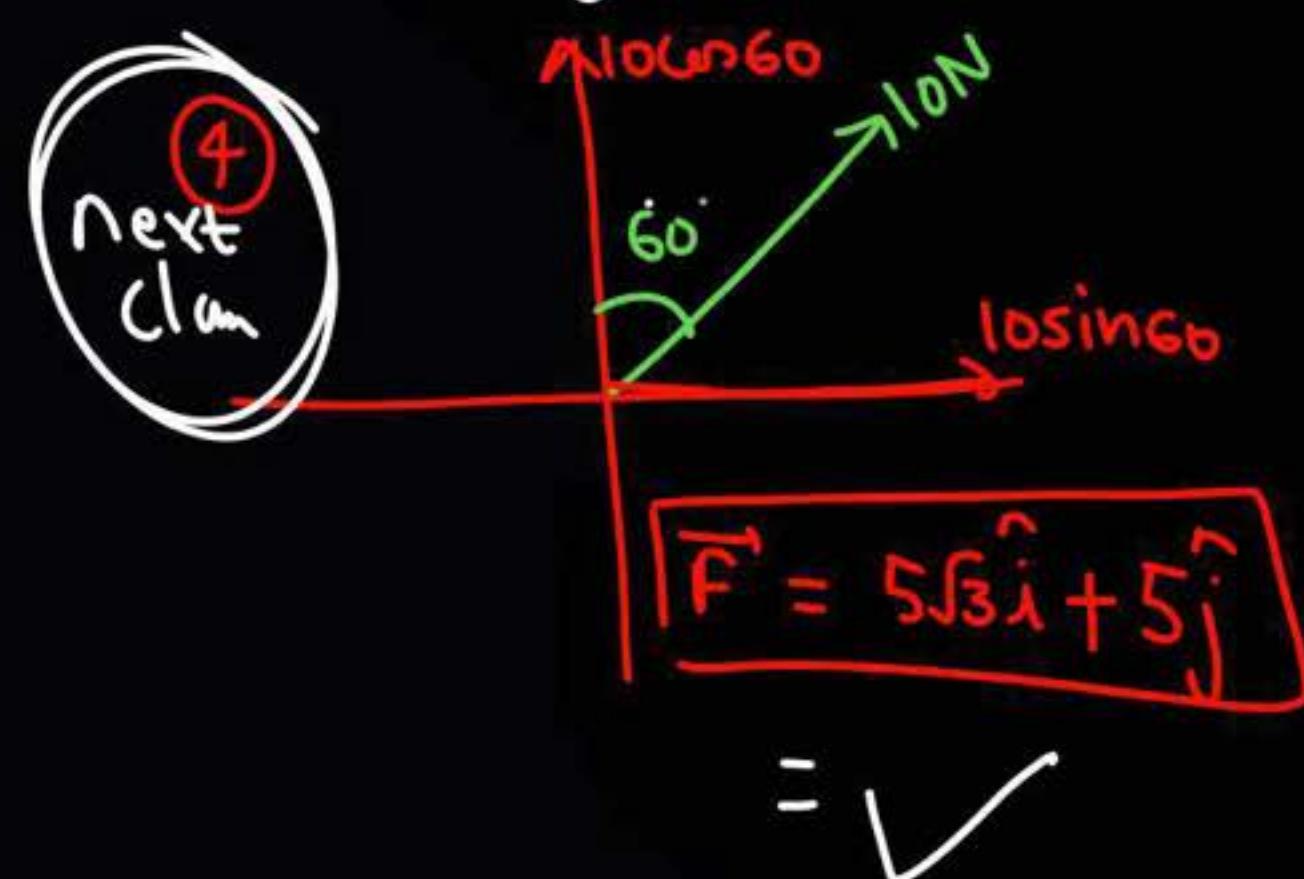
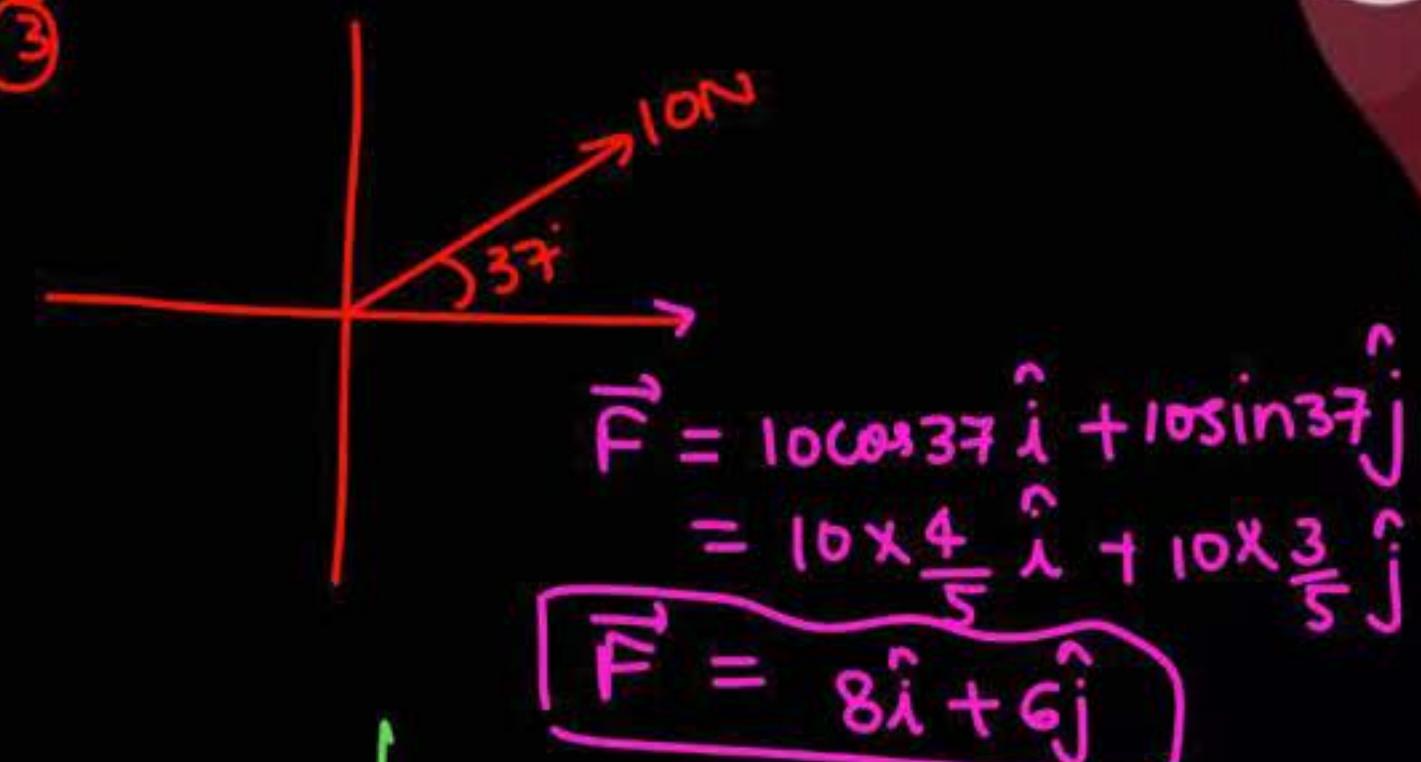
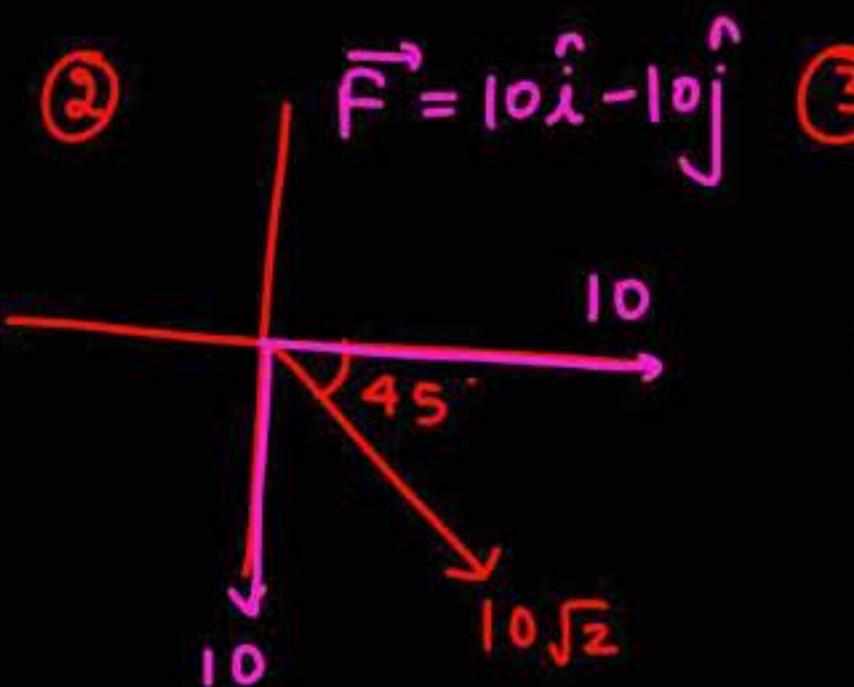
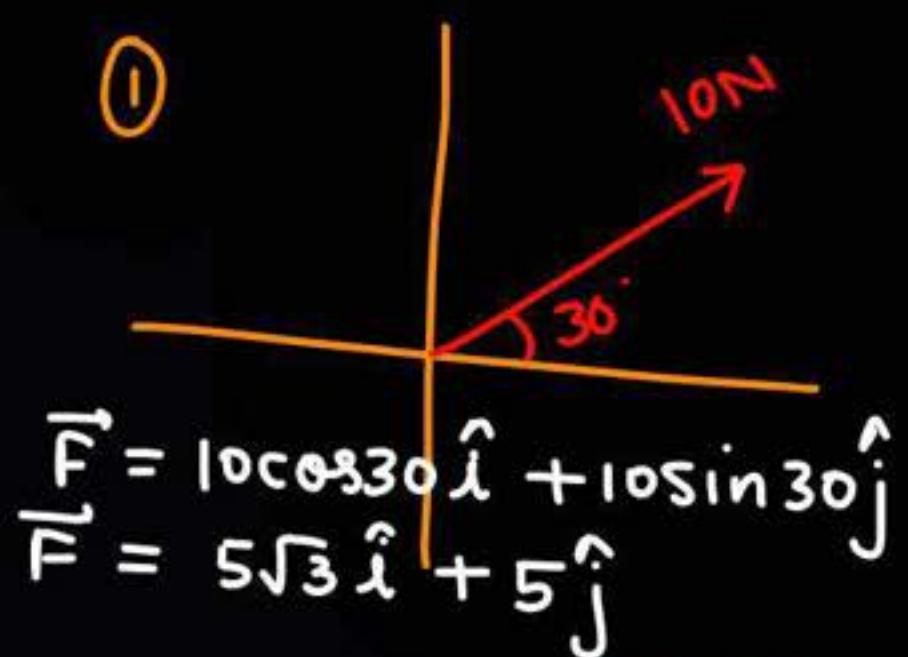
$$\vec{F} = F \cos \theta \hat{i} + F \sin \theta \hat{j}$$



$$\vec{F} = -F \cos \theta \hat{i} + F \sin \theta \hat{j}$$



$$\vec{F} = F \cos \theta \hat{i} - F \sin \theta \hat{j}$$



Q If angle b/w \vec{A} & \vec{B} is 30° .

$$A = 10$$

$$B = 20$$

find $|\vec{A} - \vec{B}|$ = magnitude of $\vec{A} - \vec{B}$

① m₁ direct

$$D = \sqrt{A^2 + B^2 - 2AB \cos \theta}$$

\vec{A} & \vec{B} form 30° angle

m₂

$$\begin{aligned} D &= \sqrt{A^2 + B^2 + 2AB \cos(180 - \theta)} \\ &= \sqrt{100 + 400 + 2 \times 10 \times 20 \cos 150^\circ} \\ &= \sqrt{500 + 2 \times 10 \times 20 \left(-\frac{\sqrt{3}}{2}\right)} \\ &= \sqrt{500 - 200\sqrt{3}} \end{aligned}$$

$$\begin{aligned} D &= \sqrt{100 + 400 - 2 \times 10 \times 20 \frac{\sqrt{3}}{2}} \\ &= \sqrt{500 - 200\sqrt{3}} \end{aligned}$$



$$\begin{aligned}
 \vec{AB} &= P \cdot V \cdot \text{of } B - P \cdot V \cdot \text{of } A \\
 &= (7-2)\hat{i} + (8-3)\hat{j} + (9-4)\hat{k} \\
 &= 5\hat{i} + 5\hat{j} + 5\hat{k}
 \end{aligned}$$

| (2, 4, 7)
 | P → Q
→ Q
(3, 9, 5)

$\vec{r} = \hat{i} + 5\hat{j} - 2\hat{k}$

magnitude of a vector.

$$\vec{A} = 2\hat{i} + 3\hat{j} + 4\hat{k}$$

$$\begin{aligned}\text{magnitude of } A &= \sqrt{2^2 + 3^2 + 4^2} \\ &= \sqrt{4 + 9 + 16} \\ &= \sqrt{29}\end{aligned}$$

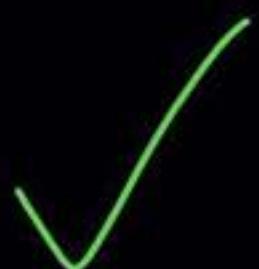
$$\vec{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$$

$$\text{mag. of } \vec{A} = \sqrt{A_x^2 + A_y^2 + A_z^2}$$

Q $\vec{A} = 2\hat{i} - 3\hat{j} + 4\hat{k}$

$$\text{mag. of } \vec{A} = \sqrt{2^2 - 3^2 + 4^2} \quad \times$$

$$= \sqrt{2^2 + 3^2 + 4^2}$$



find magnitude of \vec{A} in following cases

① $\vec{A} = 3\hat{i} + 4\hat{j}$
 $A = \sqrt{3^2 + 4^2} = 5$

② $\vec{A} = -3\hat{i} + 4\hat{j}$
 $A = \sqrt{3^2 + 4^2} = 5$

③ $\vec{A} = 3\hat{i} - 4\hat{j}$
 $A = 5$

④ $\vec{A} = -3\hat{i} - 4\hat{j}$
 $A = 5$

⑤ $\vec{A} = 6\hat{i} + 2\hat{j} + 3\hat{k}$
 $A = \sqrt{6^2 + 2^2 + 3^2} = 7$

⑥ $\vec{A} = 5\hat{i} - 12\hat{j} + 13\hat{k}$
 $A = \sqrt{5^2 + 12^2 + 13^2} = 13\sqrt{2}$

⑦ $\vec{A} = \hat{i} + \hat{j} + \hat{k}$
 $A = \sqrt{1^2 + 1^2 + 1^2} = \sqrt{3}$

⑧ $\vec{A} = \hat{i} - \hat{j} + \hat{k}$
 $A = \sqrt{1^2 + 1^2 + 1^2} = \sqrt{3}$

find magnitude of \vec{A} in following cases

$$\textcircled{1} \quad \vec{A} = 3\hat{i} + 4\hat{j}$$

$$A = \sqrt{3^2 + 4^2} = 5$$

$$\textcircled{2} \quad \vec{A} = -3\hat{i} + 4\hat{j}$$

$$A = \sqrt{3^2 + 4^2} = 5$$

$$\textcircled{3} \quad \vec{A} = 3\hat{i} - 4\hat{j}$$

$$A = 5$$

$$\textcircled{4} \quad \vec{A} = -3\hat{i} - 4\hat{j}$$

$$A = 5$$

$$\vec{A} = \frac{6\hat{i} + 2\hat{j} + 3\hat{k}}{7}$$

$$\textcircled{5} \quad \vec{A} = 6\hat{i} + 2\hat{j} + 3\hat{k}$$

$$A = \sqrt{6^2 + 2^2 + 3^2} = 7$$

$$\textcircled{6} \quad \vec{A} = 5\hat{i} - 12\hat{j} + 13\hat{k}$$

$$A = \sqrt{5^2 + 12^2 + 13^2} = 13\sqrt{2}$$

$$\textcircled{7} \quad \vec{A} = \hat{i} + \hat{j} + \hat{k}$$

$$A = \sqrt{1^2 + 1^2 + 1^2} = \sqrt{3}$$

$$\textcircled{8} \quad \vec{A} = \hat{i} - \hat{j} + \hat{k}$$

$$A = \sqrt{1^2 + 1^2 + 1^2} = \sqrt{3}$$

$$\textcircled{9} \quad \vec{A} = \hat{i} - \hat{j}$$

$$A = \sqrt{1^2 + 1^2} = \sqrt{2}$$

$$\textcircled{10} \quad \vec{A} = \hat{i} - \hat{k}$$

$$A = \sqrt{1^2 + 0^2 + 1^2} = \sqrt{2}$$

$$\textcircled{11} \quad \vec{A} = \hat{i}$$

$$A = 1$$

$$\textcircled{12} \quad \vec{A} = \hat{k}$$

$$A = 1$$

Unit vector

$$\textcircled{3} \quad \vec{A} = \hat{j} - \hat{k}$$

$$A = \sqrt{1^2 + 1^2} = \sqrt{2}$$

$$\textcircled{14} \quad \vec{A} = \frac{\hat{i}}{\sqrt{2}} + \frac{\hat{j}}{\sqrt{2}}$$

$$A = \sqrt{\left(\frac{1}{\sqrt{2}}\right)^2 + \left(\frac{1}{\sqrt{2}}\right)^2} = \sqrt{\frac{1}{2} + \frac{1}{2}} = 1$$

$$\textcircled{15} \quad \vec{A} = \frac{\hat{i}}{\sqrt{3}} - \frac{\hat{j}}{\sqrt{3}} - \frac{\hat{k}}{\sqrt{3}}$$

$$A = \sqrt{\left(\frac{1}{\sqrt{3}}\right)^2 + \left(\frac{1}{\sqrt{3}}\right)^2 + \left(\frac{1}{\sqrt{3}}\right)^2} = 1$$

Unit vector = ऐसा vector whose magnitude is 1

Q $\vec{A} = 3\hat{i} + 4\hat{j}$

mag. of $\vec{A} = \sqrt{3^2 + 4^2} = 5$

Unit vector along \vec{A}

or

$$\hat{A} = \frac{\vec{A}}{|A|} = \frac{3\hat{i} + 4\hat{j}}{5} = \frac{3}{5}\hat{i} + \frac{4}{5}\hat{j}$$

$$\vec{A} = |A| \cdot \hat{A}$$

div
 unit vector
 magnitude

$$\hat{A} = \frac{\vec{A}}{|A|}$$

$$\text{Q} \quad \vec{A} = 3\hat{i} - 4\hat{j}$$

$$\hat{A} = \frac{\vec{A}}{|A|} = \frac{3\hat{i} - 4\hat{j}}{5}$$

$$\text{Q} \quad \vec{A} = 2\hat{i} + 6\hat{j} - 3\hat{k}$$

$$\hat{A} = \frac{2\hat{i} + 6\hat{j} - 3\hat{k}}{7} = \frac{2}{7}\hat{i} + \frac{6}{7}\hat{j} - \frac{3}{7}\hat{k}$$

$$\text{Q} \quad \vec{A} = \hat{i} + \hat{j}$$

$$\hat{A} = \frac{\hat{i} + \hat{j}}{\sqrt{2}}$$

$$\text{Q} \quad \vec{A} = \hat{i} - \hat{j} - \hat{k}$$

$$\hat{A} = \frac{\hat{i} - \hat{j} - \hat{k}}{\sqrt{3}}$$

$$\text{Q} \quad \vec{A} = 5\hat{i} + 5\hat{j}$$

$$\hat{A} = \frac{5\hat{i} + 5\hat{j}}{5\sqrt{2}} = \frac{5(\hat{i} + \hat{j})}{5\sqrt{2}} = \frac{\hat{i} + \hat{j}}{\sqrt{2}}$$

Q

A bird is flying with speed 10m/s in the direction of a vector $\vec{A} = 3\hat{i} + 4\hat{j}$. find velocity of bird.

$$Ev = 10 \text{ m/s}$$

$\vec{v} = (\text{magnitude})(\text{direction})$

$$\vec{v} = 10 \cdot \hat{A} = 10 \times \left(\frac{\hat{3i} + \hat{4j}}{5} \right) = 2(\hat{3i} + \hat{4j})$$

$$\hat{A} = \frac{\hat{3i} + \hat{4j}}{5}$$

$$\vec{v} = 6\hat{i} + 8\hat{j} \text{ (m/s)}$$

Q Find a vector whose magnitude is 20 and dir is parallel to (or along or towards) $\vec{A} = 6\hat{i} - 8\hat{j}$

Ans $20 \hat{A} = 20 \frac{6\hat{i} - 8\hat{j}}{\sqrt{6^2 + 8^2}} = 20 \left(\frac{6\hat{i} - 8\hat{j}}{10} \right)$

$= 12\hat{i} - 16\hat{j}$

Q find force \vec{F} in vector form if its magnitude is 21 N

and direction is (a) parallel to $6\hat{i} - 3\hat{j} + 2\hat{k} = \vec{A}$

(b) opposite to $6\hat{i} - 3\hat{j} + 2\hat{k} = \vec{A}$

(a) $\vec{F} = 21 \cdot \hat{A} = 21 \left(\frac{6\hat{i} - 3\hat{j} + 2\hat{k}}{7} \right) = 18\hat{i} - 9\hat{j} + 6\hat{k}$

(b) $\vec{F} = 21(-\hat{A}) = -21 \hat{A} = - (18\hat{i} - 9\hat{j} + 6\hat{k})$
 $= -18\hat{i} + 9\hat{j} - 6\hat{k}$

Q

A bird is flying with speed 10 m/s from point A to directly point B. find Velocity of bird.



$$\vec{AB} = 4\hat{i} + 0\hat{j} - 3\hat{k} = 4\hat{i} - 3\hat{k}$$

$$\vec{v} = 10 \times \hat{AB} = 10 \times \left(\frac{4\hat{i} - 3\hat{k}}{5} \right) = 8\hat{i} - 6\hat{k}$$

प्र० ४ ग्व

Q Initial speed of मिडिय is 10 m/s along $\vec{A} = 3\hat{i} - 4\hat{j}$
and net force on the मिडिय is 50 N in the Dirⁿ of \vec{B}
mass of मिडिय is 2 kg $\vec{B} = [6\hat{i} + 8\hat{j}]$

① find velocity of मिडिय at $t = 14 \text{ sec}$

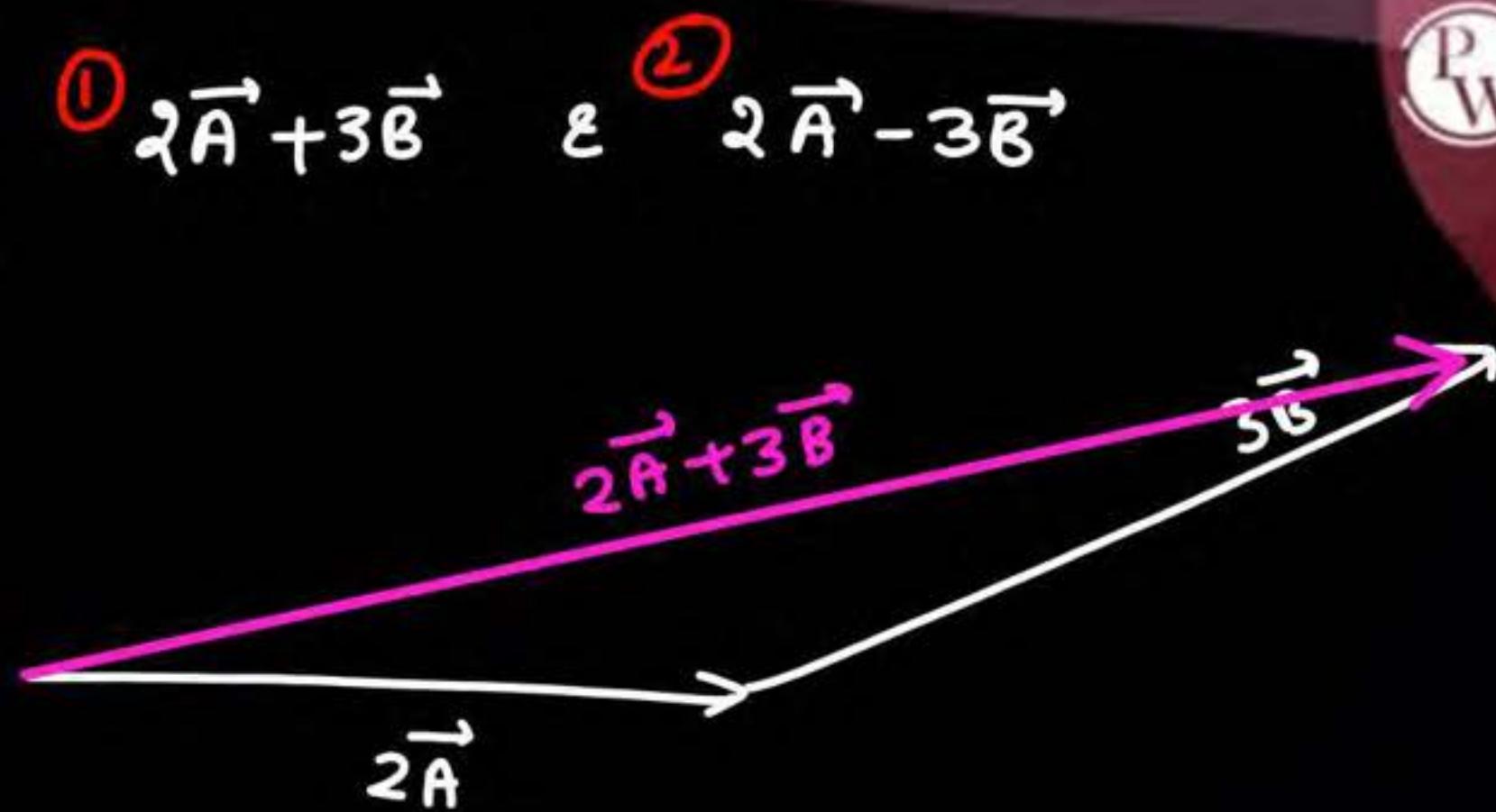
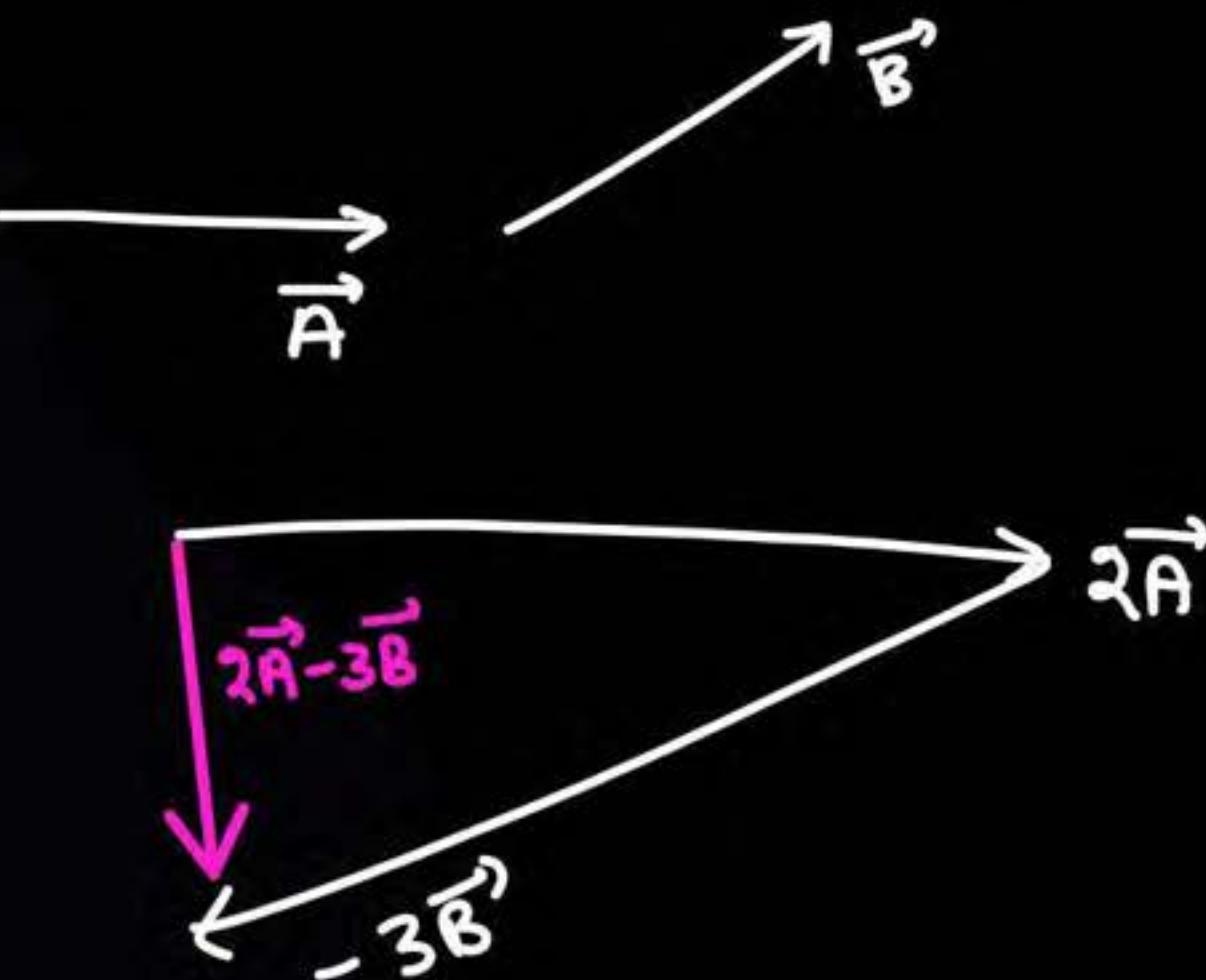
$$v = u + at$$
$$u_i = 10 \cdot \hat{A} = 10 \cdot \frac{3\hat{i} - 4\hat{j}}{5}$$

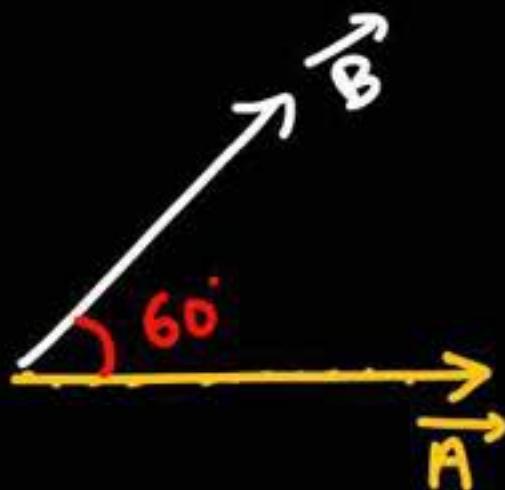
$$\vec{F} = 50 \hat{B} = 50 \times \frac{6\hat{i} + 8\hat{j}}{10}$$
$$\vec{F} = 30\hat{i} + 40\hat{j}$$

$$\vec{a} = \frac{\vec{F}}{m} = 15\hat{i} + 20\hat{j}$$

Q

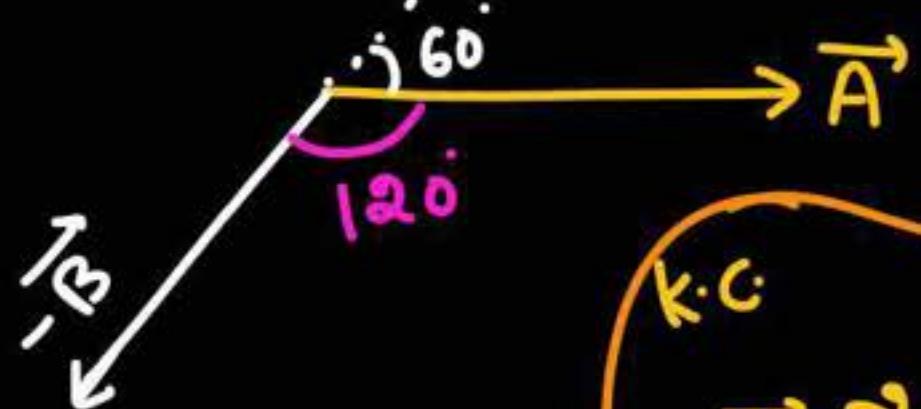
Draw rough diagram of ① $2\vec{A} + 3\vec{B}$ & ② $2\vec{A} - 3\vec{B}$





Angle between \vec{A} & \vec{B} = 60°

Angle between \vec{A} & $-\vec{B}$ = $180 - 60^\circ$
= 120°



K.C

\vec{A} और \vec{B} के बीच
आगे angle θ है
तो \vec{A} और $-\vec{B}$ के
बीच $180 - \theta$ होगा।

Q magnitude of \vec{A} & \vec{B} is 10 & 20 Unit, angle between \vec{A} & \vec{B} is 60°

(A) find mag. of resultant of \vec{A} & \vec{B} and angle made by this resultant

$$\vec{C} = \vec{A} + \vec{B}$$

$$C = \sqrt{10^2 + 20^2 + 2 \times 10 \times 20 \cos 60^\circ} = 10\sqrt{7}$$

with \vec{A}

$$\tan \alpha = \frac{B \sin \theta}{A + B \cos \theta} = \frac{20 \sin 60^\circ}{10 + 20 \cos 60^\circ}$$

(B) If vector \vec{B} is reversed and added to \vec{A} , find mag. of new resultant and angle made by this with \vec{A}

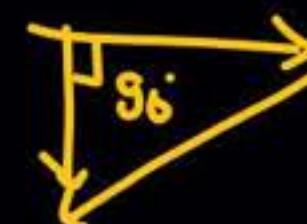
$$\vec{D} = \vec{A} - \vec{B} = \vec{A} + (-\vec{B})$$

$$C = \sqrt{10^2 + 20^2 - 2 \times 10 \times 20 \times \cos 60^\circ}$$

$$= \sqrt{360}$$

$$\tan \alpha = \frac{B \sin \theta}{A - B \cos \theta} = \frac{20 \sin 60^\circ}{10 - 20 \cos 60^\circ} = \frac{10\sqrt{3}}{0}$$

$$\alpha = 90^\circ$$



(B) $\vec{A} \text{ एवं } \vec{B}$ के बीच angle = 60°
 $\vec{A} \perp \vec{B}$ = 120°

$$\vec{D} = \vec{A} - \vec{B}$$

$$\begin{aligned}
 D &= \sqrt{10^2 + (20)^2 + 2 \times 10 \times 20 \times \cos 120^\circ}, \quad \tan \alpha = \frac{20 \sin 120^\circ}{10 + 20 \cos 120^\circ} \\
 D &= \sqrt{10^2 + 20^2 + 2 \times 10 \times 20 \cos(180^\circ - 60^\circ)} \\
 &= \sqrt{10^2 + 20^2 + 2 \times 10 \times 20 \left(-\frac{1}{2}\right)} \\
 &= \sqrt{100 + 400 - 200} \\
 &= \sqrt{300} \\
 &= \frac{20 \sqrt{3}/2}{10 + 20 \left(-\frac{1}{2}\right)} = \frac{10\sqrt{3}}{0}
 \end{aligned}$$

$\alpha = 90^\circ$



*** K.C.

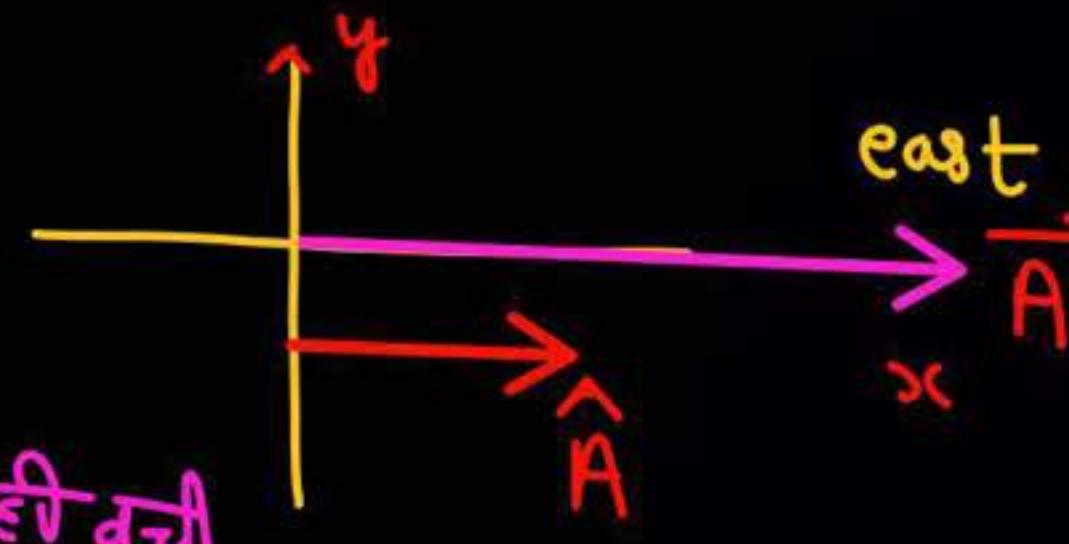
\vec{A}, \hat{A} = parallel vectors

\hat{A} → Unit vector

ये ऐसा Vector हैं
जिसका magnitude 1
और dirⁿ $\frac{\vec{A}}{|\vec{A}|}$ की तरफ को है

Q $\vec{A} = 5\text{ N east}$

$\hat{A} = \text{east}$
dirⁿ ही कही



Q A particle is moving with speed 10 m/s along +x Axis
find velocity $\vec{v} = 10 \text{ m/s } \hat{i}$
"Dir"

Q A particle is moving with speed 20 m/s along -y Axis
 $\vec{v} = 20 \text{ m/s } (-\hat{j}) = -20\hat{j}$

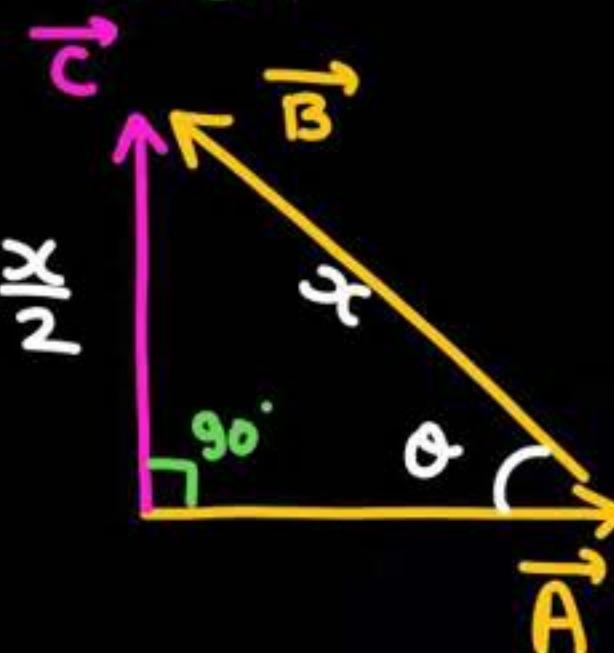
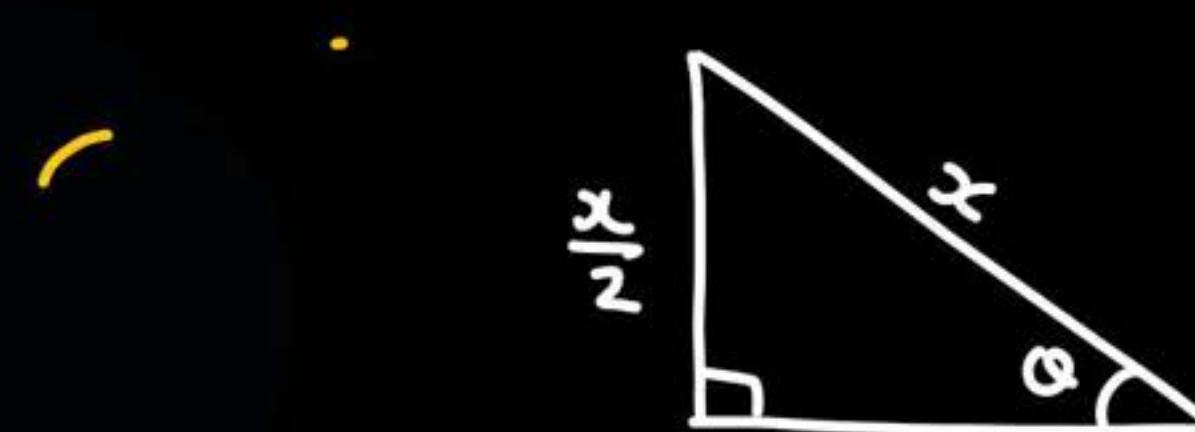
Q Resultant of \vec{A} & \vec{B} is perpendicular to \vec{A}

and its magnitude is equal to half of magnitude of \vec{B}

Find the angle between \vec{A} & \vec{B} .

m-2

$$\vec{A} + \vec{B} = \vec{C}$$



$$\sin \theta = \frac{x/2}{x} = \frac{1}{2}$$

$$\theta = 30^\circ$$

Aus ~~30~~

$$\begin{aligned} \text{Ans} &\rightarrow 180 - 30 \\ &= 150^\circ \end{aligned}$$

Q

Two vector \vec{A} & \vec{B} have same magnitude 'a' and resultant has magnitude R. Now \vec{B} is doubled and added to \vec{A} and now new resultant become $a\sqrt{3}$. Find angle between \vec{A} & \vec{B} .

$$\vec{A} + \vec{B} = \vec{R}$$

$$R = \sqrt{a^2 + a^2 + 2 \cdot a \cdot a \cdot \cos\theta}$$

$$\cos\theta = -\frac{1}{2}$$

$$\theta = 120^\circ$$

$$R_{\text{new}} = \sqrt{a^2 + (2a)^2 + 2 \cdot a \cdot 2a \cdot \cos\theta}$$

$$a\sqrt{3} = \sqrt{a^2 + 4a^2 + 4a^2 \cos\theta}$$

$$3a^2 = 5a^2 + 4a^2 \cos\theta$$

$$-2a^2 = 4a^2 \cos\theta$$

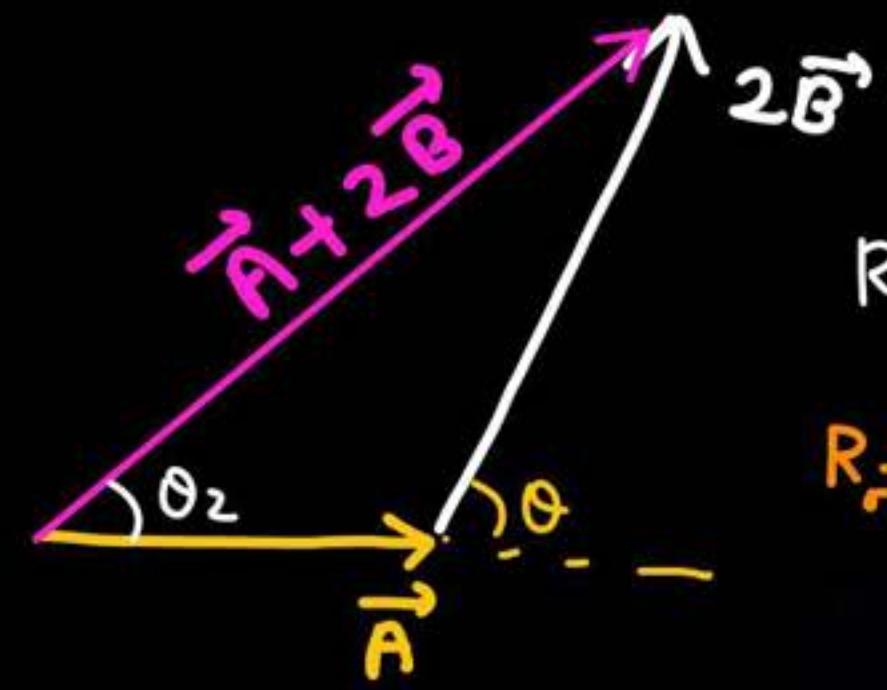
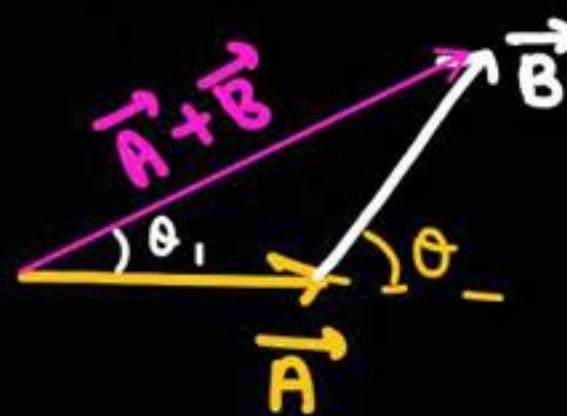
$$\vec{A} \text{ & } \vec{B}$$

$$2\vec{B} + \vec{A} \times$$

$$2\vec{B} + \vec{A} \checkmark$$

Q \vec{A} has magnitude 10N, \vec{B} has magnitude 20N
 angle between \vec{A} & \vec{B} is 60° . If \vec{B} is doubled
 and added to \vec{A} find new resultant.

उत्तर = 40



$$\begin{aligned}
 R_{\text{नया}} &= \sqrt{10^2 + (40)^2 + 2 \times 10 \times 40 \cos 60^\circ} \\
 R_{\text{नया}} &= \sqrt{100 + 1600 + 800 \times \frac{1}{2}} \\
 &= \sqrt{2100} \\
 &= 10\sqrt{21} \text{ N}
 \end{aligned}$$

$$C_{\max} = A + B$$

$$C_{\min} = A - B$$

Q. \vec{A} has magnitude 10 N
 \vec{B} " " 6 N

find Range of magnitude of resultant of $\vec{A} \pm \vec{B}$

$$C_{\max} = A + B = 10 + 6 = 16$$

$$C_{\min} = |A - B| = 10 - 6 = 4$$

$$\boxed{4 \leq C \leq 16} \Rightarrow [4, 16]$$

Q magnitude of \vec{A} is 8 N (angle not given)

" " " \vec{B} is 6 N

which of the following can be the magnitude of $\vec{A} + \vec{B}$

- (A) 10 N ✓
- (B) 12 N ✓
- (C) 4 N ✓
- (D) 2 N ✓
- (F) 2.0001 N ✓
- (F) 1.9999 N ✗

- (G) 13 N ✓
- (H) 14 N ✓
- (I) 13.999 N ✓
- (J) 14.0001 N ✗
- (K) 16 N ✗

$$C_{\max} = A + B = 14$$

$$C_{\min} = A - B = 2$$

$$2 \leq C \leq 14$$

Q.

If magnitude of resultant of $\vec{A} \in \vec{B}$ has max value
30 N and has min value 20 N. Find $\frac{A}{B}$ (Ratio of magnitudes)

$$\vec{C} = \vec{A} + \vec{B}$$

$$C_{\max} = A + B = 30$$

$$C_{\min} = \underline{A - B = 20}$$

$$\boxed{\begin{array}{l} A = 25 \\ B = 5 \end{array}}$$

Q. magnitude of resultant of $\vec{A} \& \vec{B}$ is 5 Unit.

where magnitude of \vec{A} is $5\sqrt{3}$ Unit & magnitude of \vec{B} is 5 Unit.

Find angle between $\vec{A} \& \vec{B}$.

$$\vec{C} = \vec{A} + \vec{B}$$

$$c = \sqrt{A^2 + B^2 + 2AB \cos \theta}$$

$$5 = \sqrt{(5\sqrt{3})^2 + 5^2 + 2 \times 5\sqrt{3} \times 5 \cos \theta}$$

~~$$25 = 75 + 25 + 50\sqrt{3} \cos \theta$$~~

$$50\sqrt{3} \cos \theta = -75$$

$$\cos \theta = \frac{-75}{50\sqrt{3}} = -\frac{\sqrt{3}}{2}$$

(A)

60°

(B)

150°

(C)

120°

(D)

-30°

(E)

30°

(F)

180°

(G)

210°

(H)

240°

(I)

270°

(J)

300°

(K)

330°

(L)

360°

(M)

450°

(N)

480°

(O)

510°

(P)

540°

(Q)

570°

(R)

600°

(S)

630°

(T)

660°

(U)

690°

(V)

720°

(W)

750°

(X)

780°

(Y)

810°

(Z)

840°

(AA)

870°

(BB)

900°

(CC)

930°

(DD)

960°

(EE)

990°

(FF)

1020°

(GG)

1050°

(HH)

1080°

(II)

1110°

(JJ)

1140°

(KK)

1170°

(LL)

1200°

(MM)

1230°

(NN)

1260°

(OO)

1290°

(PP)

1320°

(QQ)

1350°

(RR)

1380°

(SS)

1410°

(TT)

1440°

(UU)

1470°

(VV)

1500°

(WW)

1530°

(XX)

1560°

(YY)

1590°

(ZZ)

1620°

(AA)

1650°

(BB)

1680°

(CC)

1710°

(DD)

1740°

(EE)

1770°

(FF)

1800°

(GG)

1830°

(HH)

1860°

(II)

1890°

(JJ)

1920°

(KK)

1950°

(LL)

1980°

(MM)

2010°

(NN)

2040°

(OO)

2070°

(PP)

2100°

(QQ)

2130°

(RR)

2160°

(SS)

2190°

(TT)

2220°

(UU)

2250°

(VV)

2280°

(WW)

2310°

(XX)

2340°

(YY)

2370°

(ZZ)

2400°

(AA)

2430°

(BB)

2460°

(CC)

2490°

(DD)

2520°

(EE)

2550°

(FF)

2580°

(GG)

2610°

(HH)

2640°

(II)

2670°

(JJ)

2700°

(KK)

2730°

(LL)

2760°

(MM)

2790°

(NN)

2820°

(OO)

2850°

(PP)

2880°

(QQ)

2910°

(RR)

2940°

(SS)

2970°

(TT)

3000°

(UU)

(VV)

(WW)

(XX)

(YY)

Q magnitude of \vec{A} is 10

" " \vec{B} is 20

angle between $\vec{A} \& \vec{B}$ is 60° .

① find magnitude of resultant of $\vec{A} \& \vec{B}$

$$C = \sqrt{(10)^2 + (20)^2 + 2 \times 10 \times 20 \times \cos 60^\circ} = \sqrt{700}$$

② find angle made by resultant of $\vec{A} \& \vec{B}$ with \vec{A}

$$\tan \alpha = \frac{B \sin \theta}{A + B \cos \theta} = \frac{20 \sin 60^\circ}{10 + 20 \cos 60^\circ} = \frac{20 \frac{\sqrt{3}}{2}}{10 + 20 \times \frac{1}{2}}$$

$$\tan \alpha = \frac{\sqrt{3}}{2}$$

Q Two vector \vec{A} & \vec{B} having equal magnitude 'a' are at angle 60° . find magnitude of $\vec{A} + \vec{B}$ and angle made by resultant of $\vec{A} + \vec{B}$ with \vec{A}

$$c = \sqrt{A^2 + B^2 + 2AB \cos \theta}$$

$$\begin{aligned} c &= \sqrt{a^2 + a^2 + 2aa \cos 60^\circ} \\ &= a\sqrt{3} \end{aligned}$$

$$\tan \alpha = \frac{B \sin \theta}{A + B \cos \theta} = \frac{a \sin 60^\circ}{a + a \cos 60^\circ}$$

$$\tan \alpha = \frac{\sqrt{3}/2}{1 + \frac{1}{2}} = \frac{\sqrt{3}}{3} = \frac{1}{\sqrt{3}}$$

$$\boxed{\alpha = 30^\circ}$$

tough दूरी कर सोल्व

Q2

Sum of magnitude of \vec{A} & \vec{B} is 16N. magnitude of resultant of \vec{A} & \vec{B} is 8N when resultant is perpendicular to the \vec{A} .
find magnitude of \vec{A} & \vec{B} .

$\theta \rightarrow$ नहीं पता

$$\vec{A} + \vec{B} = 16 \times$$

$$A + B = 16$$

$$\vec{A} + \vec{B} = \vec{C}$$

$$\text{mag. of } \vec{C} = 8$$

$$C = \sqrt{A^2 + B^2 + 2AB \cos \theta}$$

$$64 = A^2 + B^2 + 2AB \cos \theta$$

देखे \vec{C} के साथ 90° angle बनाया

$$\alpha = 90^\circ$$

$$\tan \alpha = \frac{B \sin \theta}{A + B \cos \theta}$$

$$\tan 90^\circ = \frac{B \sin \theta}{A + B \cos \theta}$$

$$A + B \cos \theta = 0$$

$$A + B = 16$$

$$A + B \cos 30^\circ = 0 \Rightarrow B \cos 30^\circ = -A$$

$$64 = A^2 + B^2 + 2AB \cos 30^\circ$$

$$64 = A^2 + B^2 + 2A(-A)$$

$$64 = A^2 + B^2 - 2A^2$$

$$64 = B^2 - A^2 = (B+A)(B-A)$$

$$64 = (B+A)(B-A)$$

$$64 = 16(B-A)$$

$$4 = B-A$$

$$B - A = 4$$

$$B + A = 16$$

$$\begin{array}{|l} B = 10 \\ A = 6 \end{array}$$

Ans

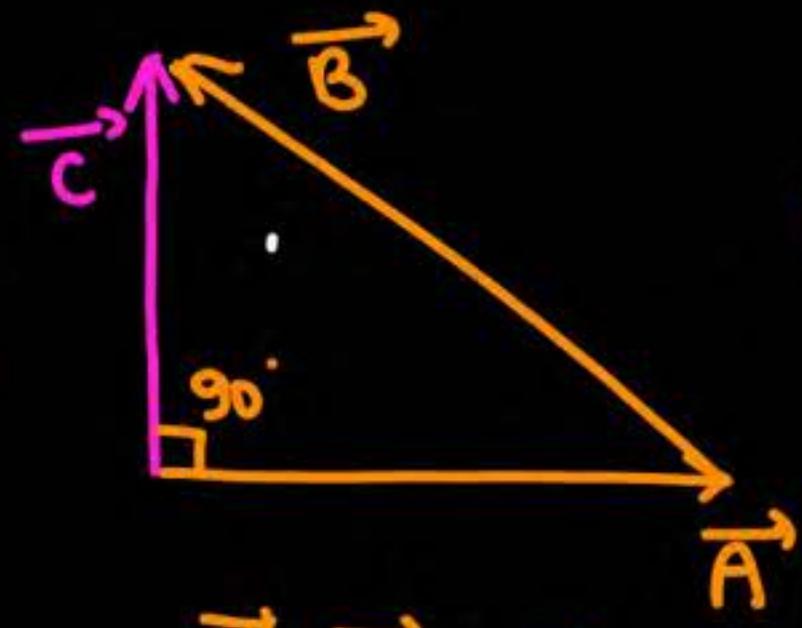
tough
Q

Sum of magnitude of \vec{A} & \vec{B} is 16N. magnitude of resultant of \vec{A} & \vec{B} is 8N when resultant is perpendicular to the \vec{A} .
find magnitude of \vec{A} & \vec{B} .

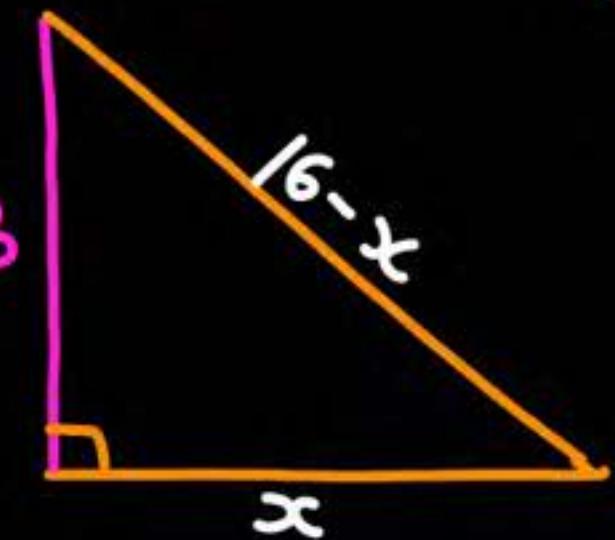
अटटा method

Method 2

\triangle का निकाला करो



=



$$8^2 + x^2 = (16-x)^2$$

Solve

$$x = 6$$

$$\begin{cases} A = 6 \\ B = 16 - x = 16 - 6 \\ B = 10 \end{cases}$$

Q Two vector \vec{A} & \vec{B} having same magnitude x (given)

Find magnitude of resultant of \vec{A} & \vec{B} if angle between them is 60° .

$$A = x$$

$$B = x$$

$$C = \sqrt{A^2 + B^2 + 2AB \cos \theta}$$

$$= \sqrt{x^2 + x^2 + 2 \cdot x \cdot x \cos 60^\circ}$$

$$= \sqrt{x^2 + x^2 + 2x^2 \frac{1}{2}}$$

$$\boxed{C = x\sqrt{3}}$$

Q

Two vector \vec{A} & \vec{B} having same magnitude. x .

Find magnitude of resultant of \vec{A} & \vec{B} if angle between them is 120° .

$$C = \sqrt{A^2 + B^2 + 2AB \cos \theta}$$

$$C = \sqrt{x^2 + x^2 + 2 \cdot x \cdot x \cdot \cos 120^\circ}$$

$$= \sqrt{2x^2 + 2x^2 \left(-\frac{1}{2}\right)}$$

$$\boxed{C = x}$$

Q Two vector \vec{A} & \vec{B} having same magnitude x .

Find magnitude of resultant of \vec{A} & \vec{B} if angle between them is 90°

$$C = \sqrt{A^2 + B^2 + 2AB \cos \theta}$$

$$C = \sqrt{x^2 + x^2 + 2 \cdot x \cdot x \cdot \cos 90^\circ}$$

$$= \sqrt{x^2 + x^2 + 0}$$

$$\boxed{C = x\sqrt{2}}$$

Q If magnitude of \vec{A} is 10N
and magnitude of \vec{B} is 6N

$$\vec{A} + \vec{B} = \vec{C}$$

① If angle between \vec{A} & \vec{B} is 60° find magnitude of resultant of \vec{A} & \vec{B}

$$C = \sqrt{100 + 36 + 2 \times 10 \times 6 \cos 60^\circ} = \sqrt{136 + 60} = \sqrt{196} = 14$$

② If angle between \vec{A} & \vec{B} is 90° find magnitude of resultant of \vec{A} & \vec{B}

$$C = \sqrt{10^2 + 6^2 + 2 \times 10 \times 6 \cos 90^\circ} = \sqrt{10^2 + 6^2} = \sqrt{136}$$

③ If angle between \vec{A} & \vec{B} is 60°
and \vec{B} become twice to its initial value & added to \vec{A} find magni
of new resultat

Q If magnitude of \vec{A} is 10N
and magnitude of \vec{B} is 6N

$$\vec{A} + \vec{B} = \vec{C}$$

(3)

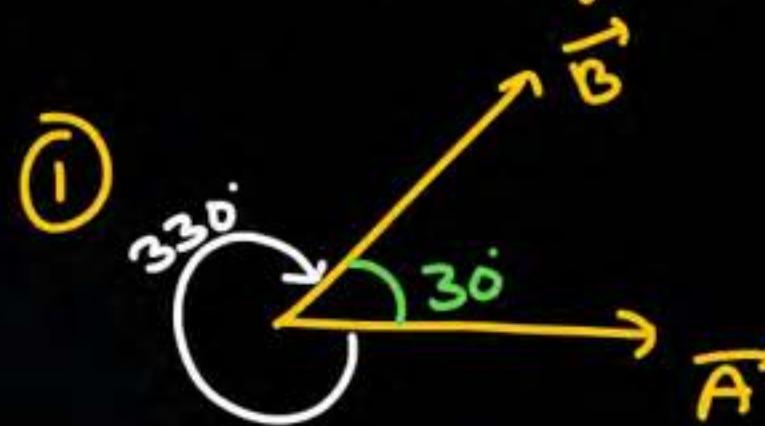
If angle between \vec{A} & \vec{B} is 60°

and \vec{B} become twice to its initial value & added to \vec{A} find magni
of new resultant

$$\begin{aligned} C &= \sqrt{100 + 144 + 120} \\ &= \sqrt{364} \end{aligned}$$

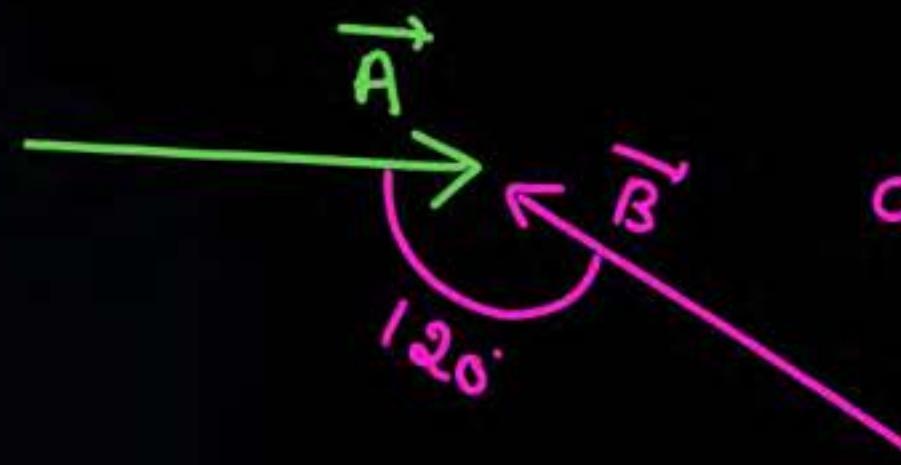
$$C_{\text{new}} = \sqrt{10^2 + (12)^2 + 2 \times 10 \times 12 \cos 60^\circ}$$

find angle b/w \vec{A} & \vec{B}



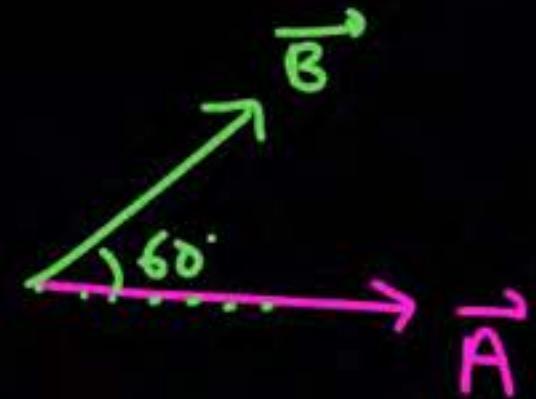
angle b/w vectors = 30° ✓
= 330° ✗

②



angle between Vectors
= 120°

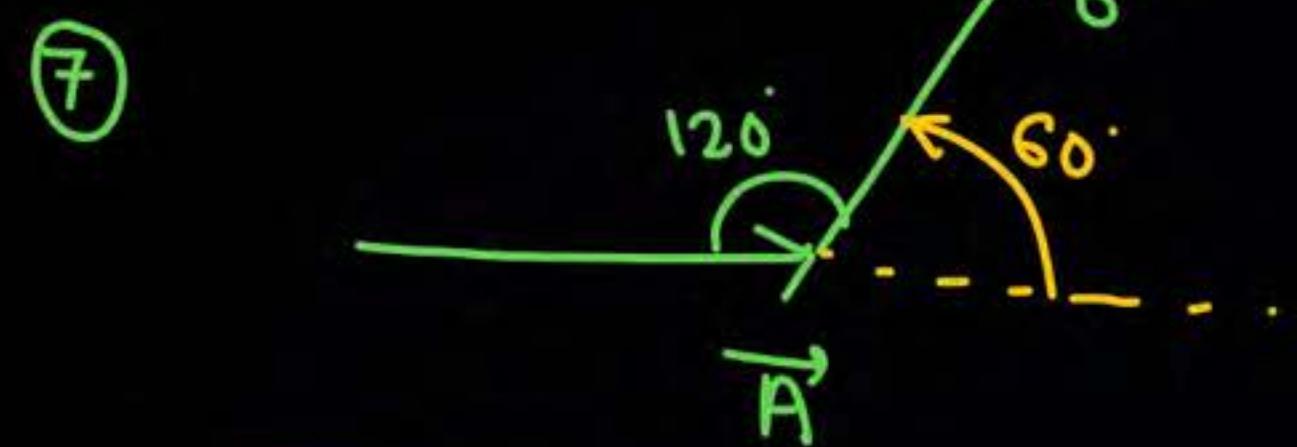
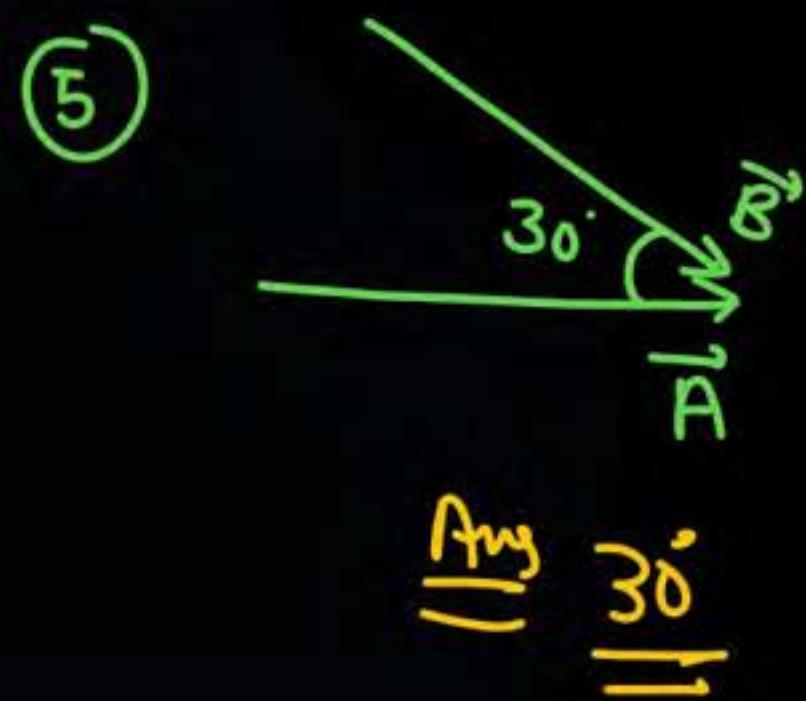
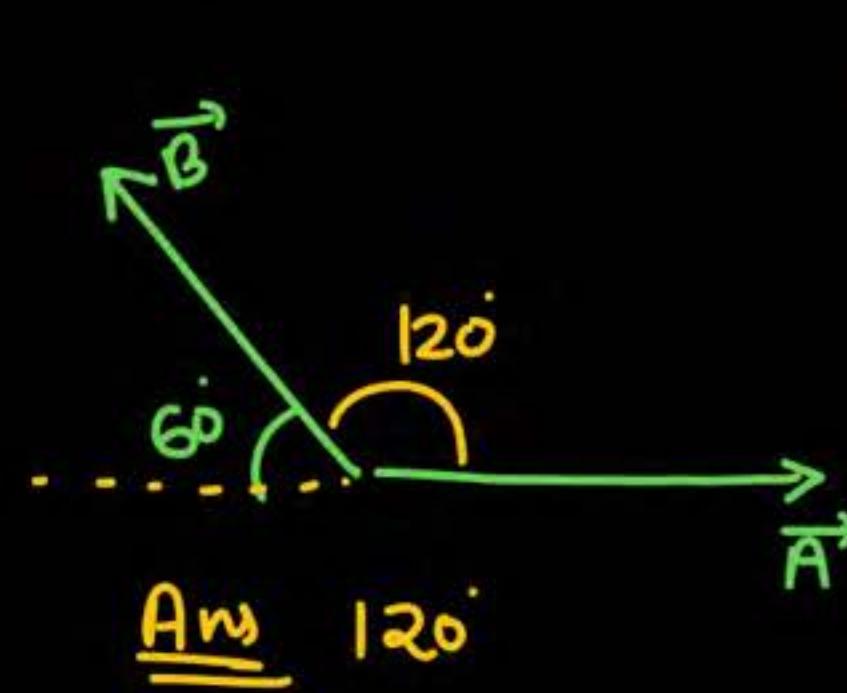
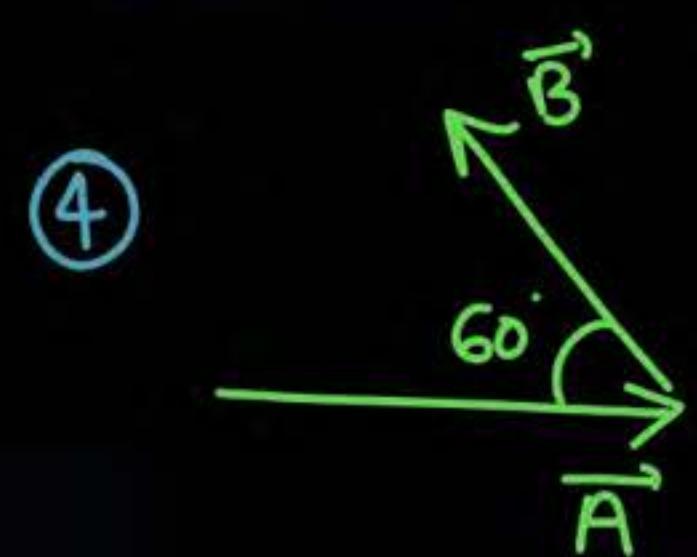
③



SOL

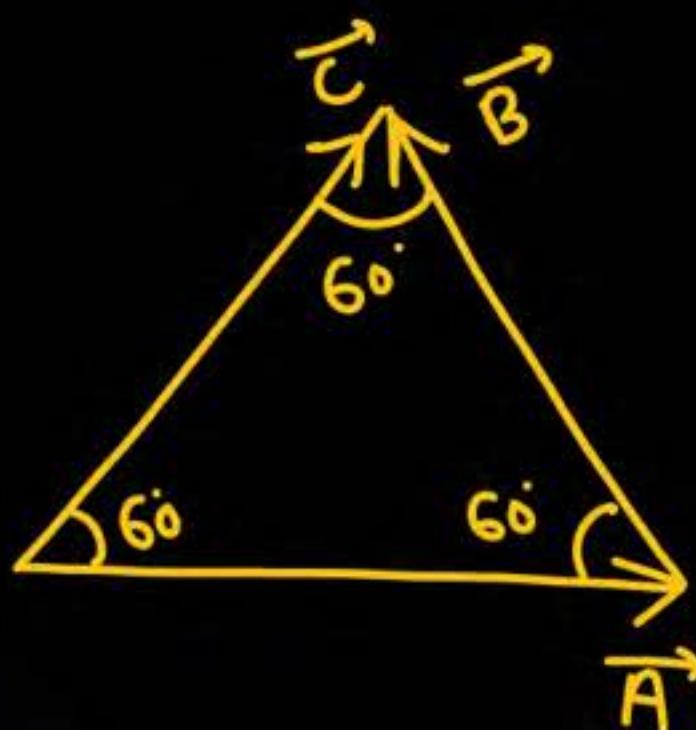


P
W



A_W = 60°

8

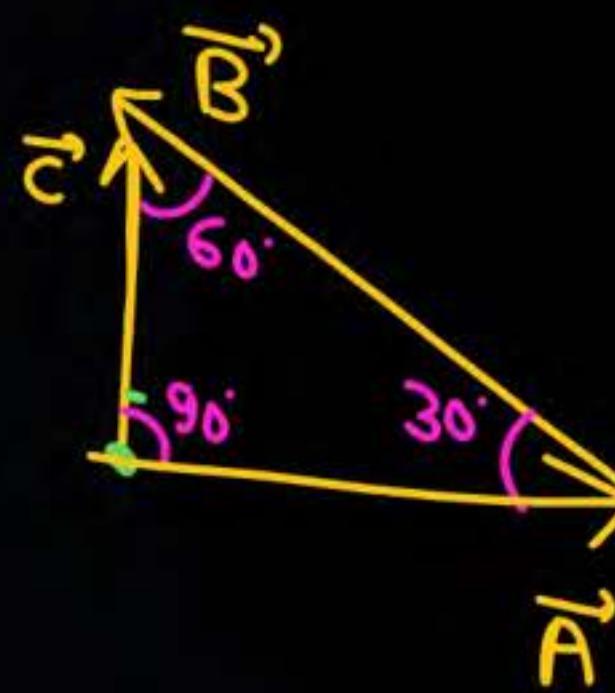


Angle between \vec{A} & \vec{B} = 120°

$$\text{“} \quad \text{“} \quad \overline{B} \& \overline{C} = 60$$

$$\vec{A} \text{ } \& \text{ } \vec{c} = 60^\circ$$

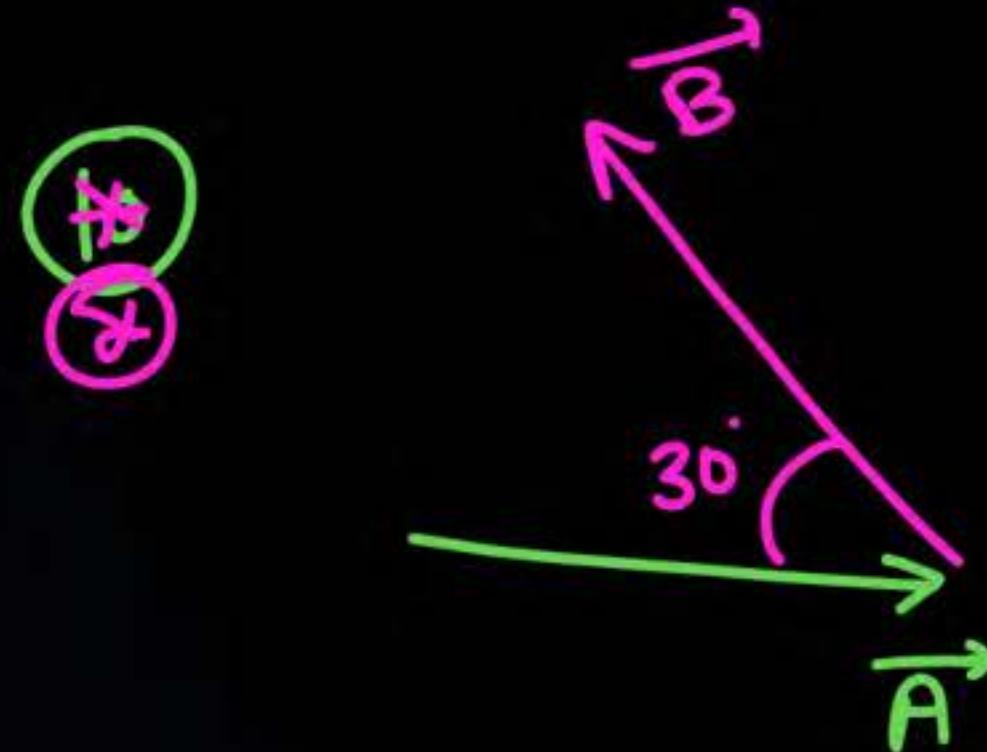
9



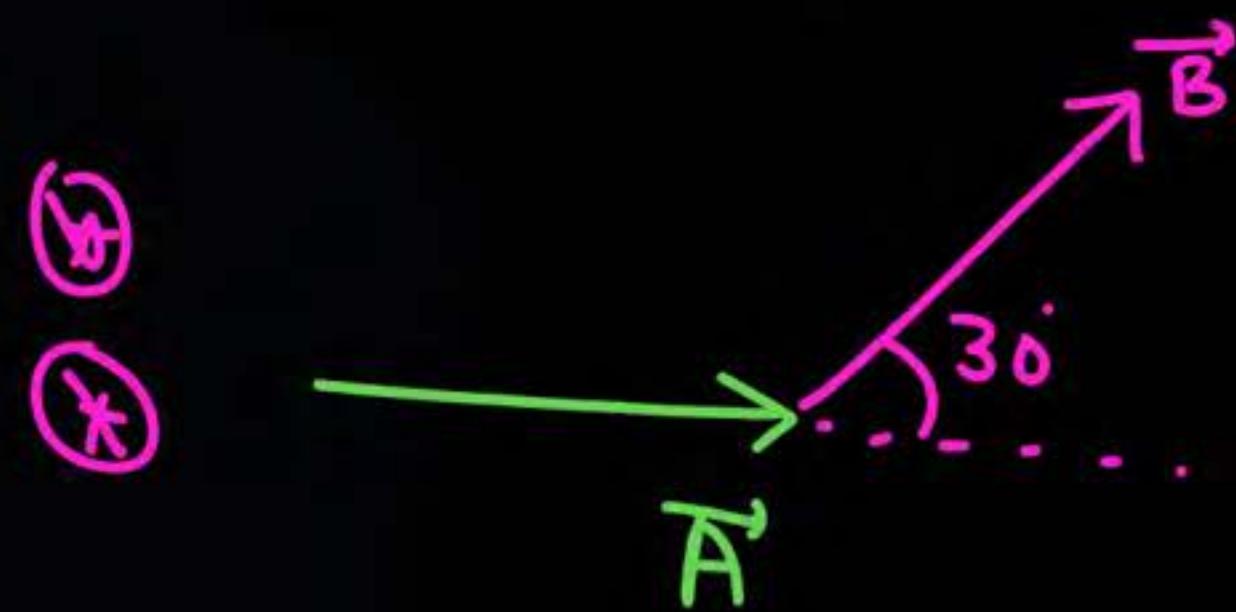
$$\text{Angle between } \vec{A} \text{ & } \vec{B} = 180 - 30 = 150^\circ$$

$$\therefore B + C = 60$$

$$\text{“} \vec{A} \otimes \vec{C} = g_0 \text{”}$$



Angle b/w \vec{A} & \vec{B} = $180 - 30 = 150^\circ$



Angle b/w \vec{A} & \vec{B} = 30°

$\vec{A} + \vec{B}$  Addition of \vec{A} & \vec{B} = ?
Resultant of \vec{A} & \vec{B} = ?

$\vec{A} + \vec{B}$ और $A + B$ = दोनों अलग-चीज़ें

परिवर्तन का नदी दृश्य
में गुलजारी

$$\vec{A} + \vec{B} = \vec{C}$$

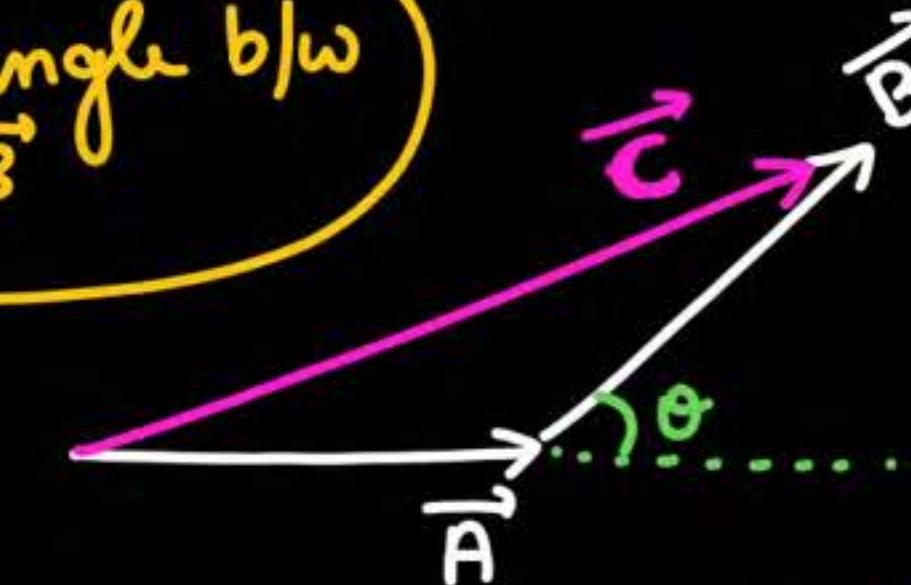
magnitude of $\vec{A} = A$

$$\vec{B} = \Theta$$

$$" " \bar{c} = 0$$

length of \vec{c} = mag. of \vec{c}

$\theta \rightarrow$ angle b/w
 \vec{A} & \vec{B}



$$(B \sin \theta)^2 + (A + B \cos \theta)^2 = c^2$$

$$B^2 \sin^2 \theta + A^2 + B^2 \cos^2 \theta + 2AB \cos \theta$$

$$A^2 + B^2(\sin^2 \theta + \cos^2 \theta) + 2AB \cos \theta = c^2$$

$$c = \sqrt{a^2 + b^2 + 2ab \cos \theta}$$

$$\cos\theta = \frac{SR}{B}$$

$$SR = B \cos \theta$$

$$\sin \theta = \frac{PR}{B}$$

$$PR = B \sin \theta$$

 Q Two forces 10N and 20N are acting on a block having 60° angle between them. find magnitude of resultant of them

$$C = \sqrt{A^2 + B^2 + 2AB \cos \theta}$$

$$= \sqrt{(10)^2 + (20)^2 + 2 \times 10 \times 20 \times \cos 60^\circ}$$

$$= \sqrt{500 + 200} = \sqrt{700} \text{ Ans}$$

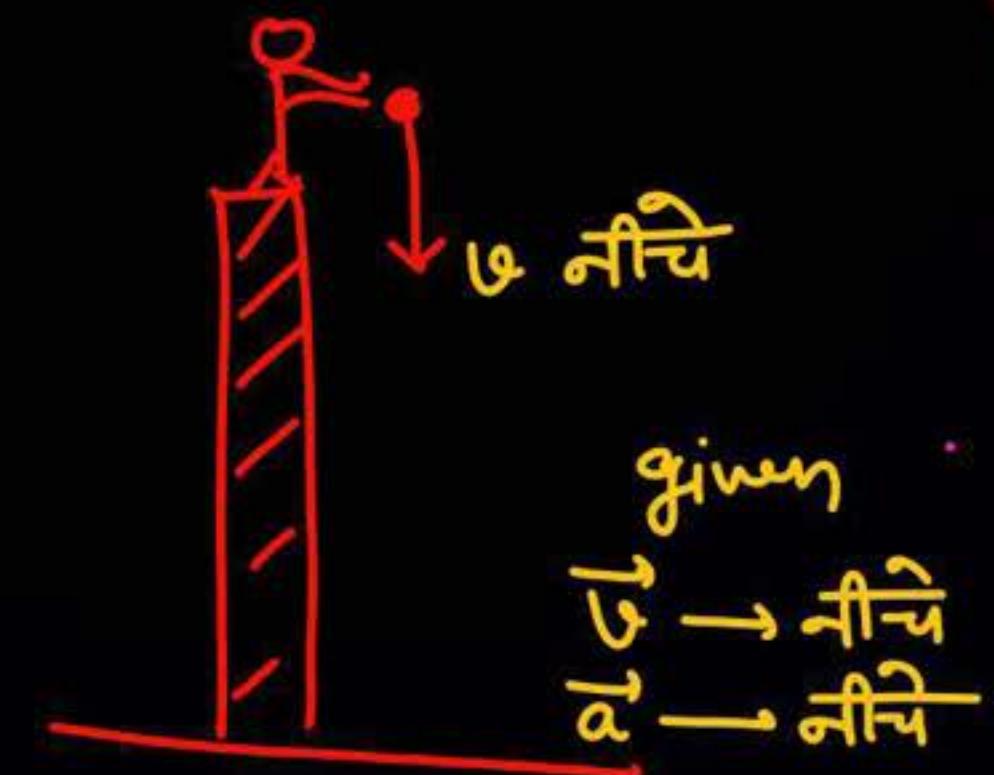
Q



$\vec{v} \rightarrow$ ऊपर
 $\vec{a} \rightarrow$ नीचे } Kinematics

\vec{v}, \vec{a} are antiparallel.

(2)



given

$\vec{v} \rightarrow$ नीचे
 $\vec{a} \rightarrow$ नीचे

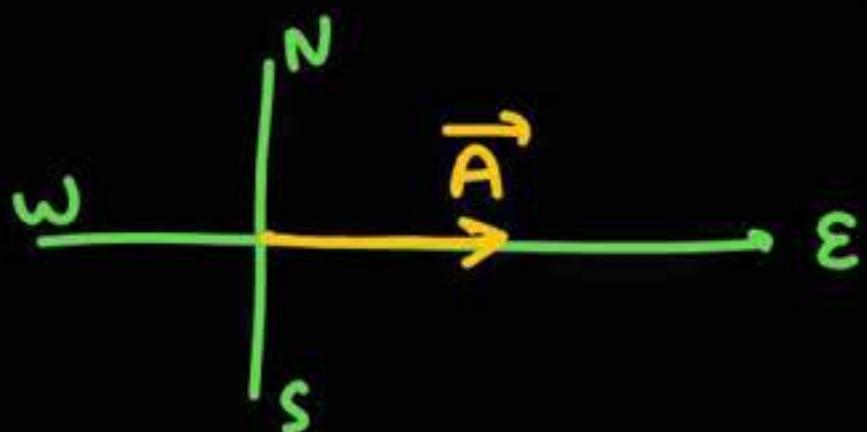
No lag \Rightarrow thumb up
 lag \Rightarrow " down

\vec{v}, \vec{a} are parallel
vector

Q

$$\vec{F} = 10N \text{ (along east)}$$

newton
(force)



find, draw

$$2\vec{A} = 20N \text{ (along east)}$$

$$3\vec{A} = 30N \quad (" ")$$

$$\frac{\vec{A}}{2} = \frac{1}{2}\vec{A} = 5N \quad (")$$



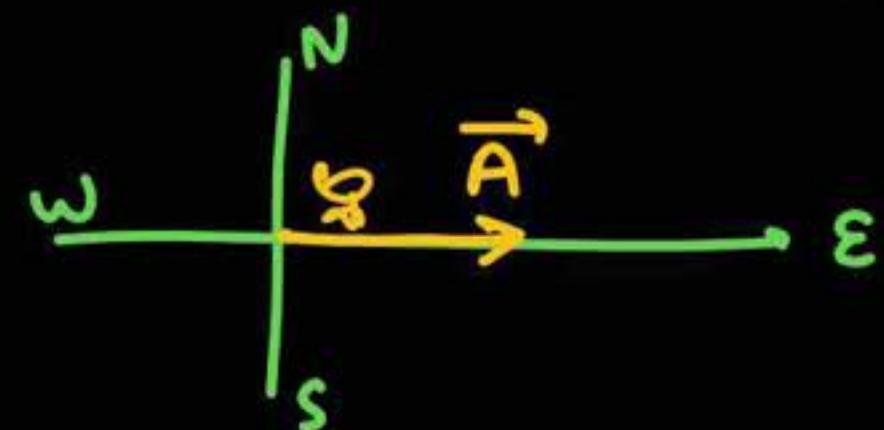
$$-2\vec{A} = 20N \text{ (west)}$$

$$-5\vec{A} = 50N \text{ (west)}$$

/

Q

$$\vec{v} = 10 \text{ m/s (along east)}$$



find, draw

$$2\vec{v} = 20 \text{ m/s (along east)}$$

$$3\vec{v} = 30 \text{ m/s (" ")}$$

$$\frac{\vec{v}}{2} = \frac{1}{2}\vec{A} = 5 \text{ m/s (" ")}$$



Q $t^2 - 3t + 2 = 0$

find t_1 & t_2

$$t_1 = \frac{3 + \sqrt{9 - 4 \times 2 \times 1}}{2} = \frac{3+1}{2} = 2$$

$$t_2 = \frac{3 - \sqrt{9 - 4 \times 2 \times 1}}{2} = \frac{3-1}{2} = 1$$

$$ax^2 + bx + c = 0$$

* $b^2 - 4ac > 0 \longrightarrow$ two root

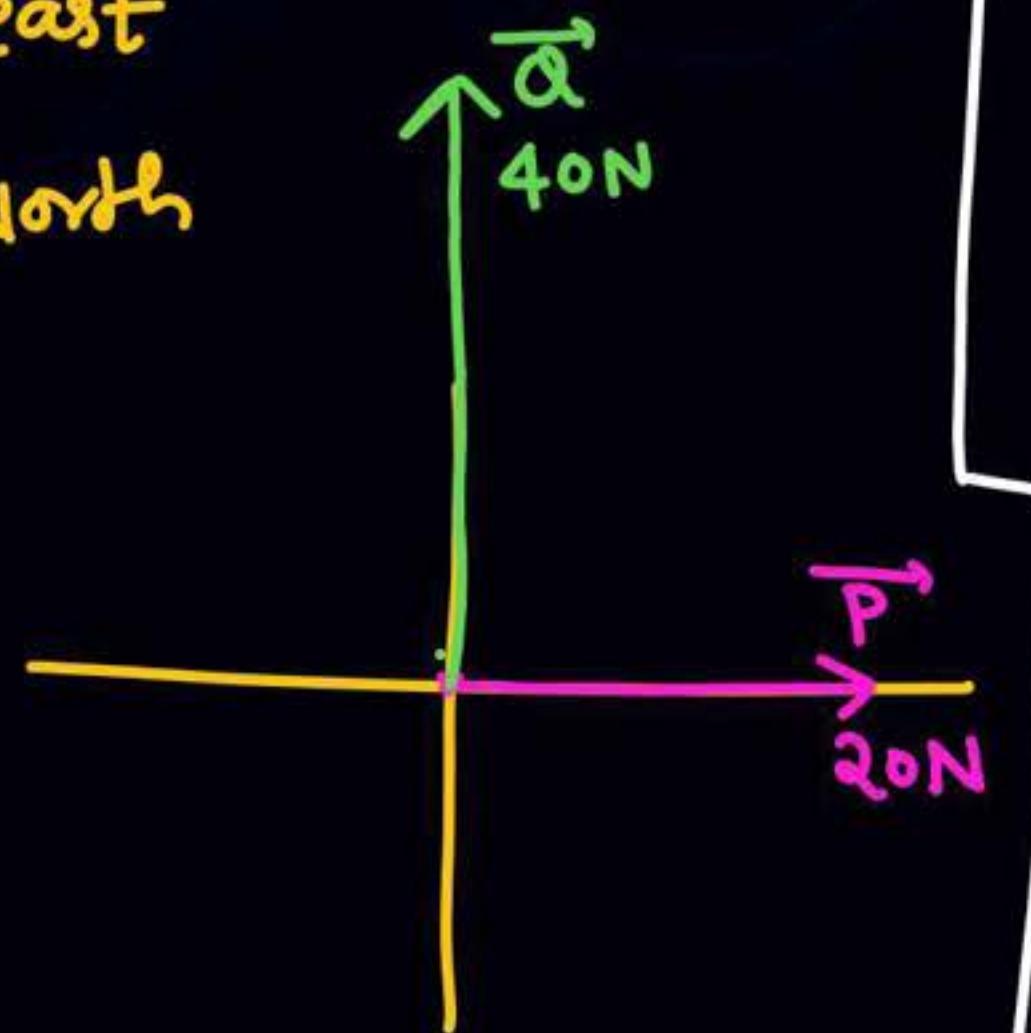
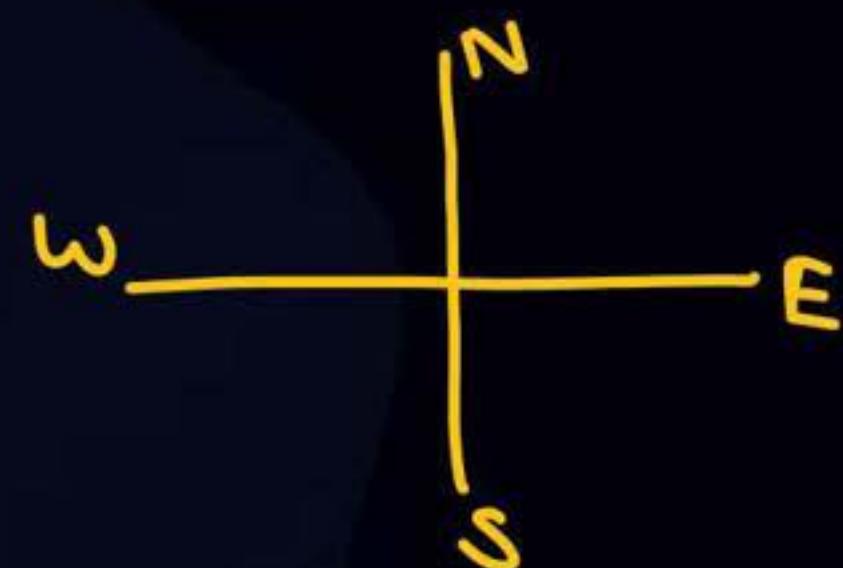
* $b^2 - 4ac = 0 \longrightarrow$ 1 root

* $b^2 - 4ac < 0 \longrightarrow$ No real root
imaginary root

Q Represent vector \vec{P} & vector $\vec{\alpha}$

$\vec{P} = 20\text{ N}$ along east

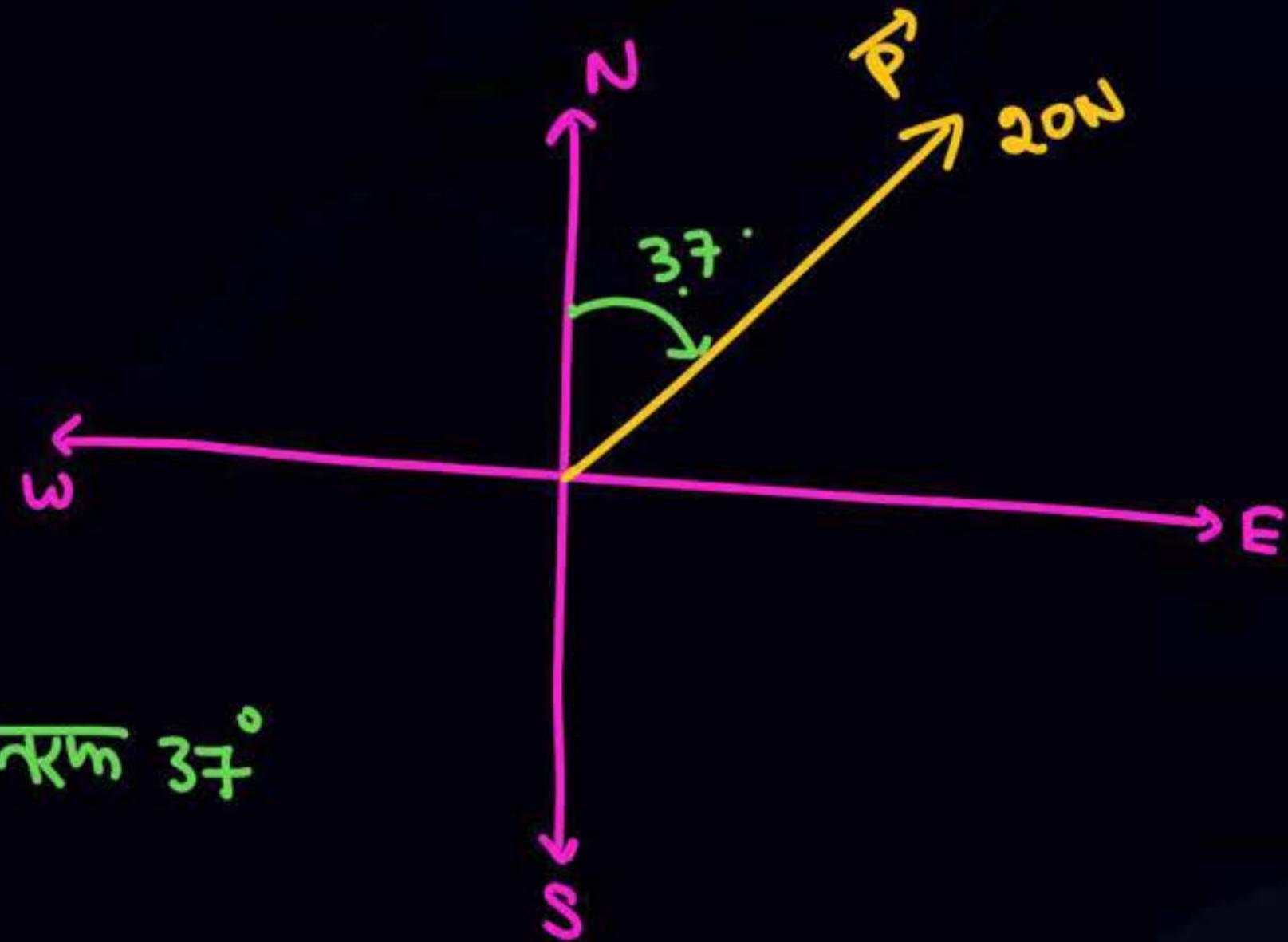
$\vec{\alpha} = 40\text{ N}$ along North



Q Represent
 \vec{P} of magnitude
20 N in direction
of 37° east of
north.

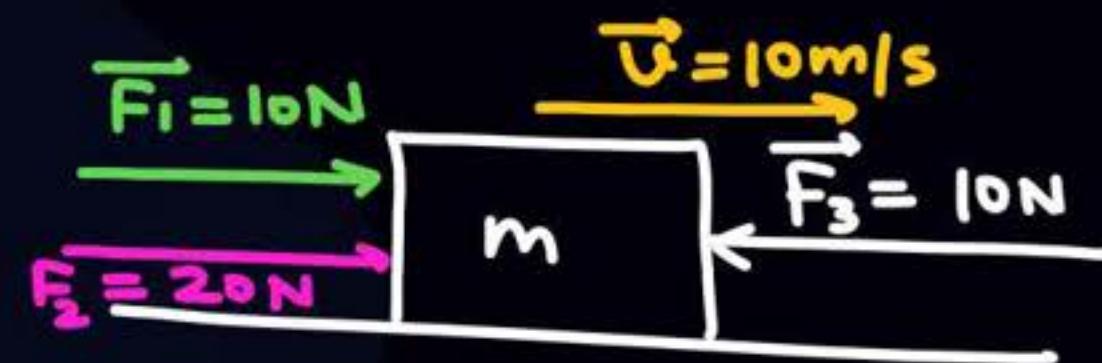
Q Represent
 \vec{P} of magnitude
20 N in direction
of 37° east of
north

III
North से East की तरफ 37°



② parallel vector → Two vectors are said to be parallel if they have same direction.

Q Block is moving with velocity 10 m/s along east dirⁿ



here

$\vec{F}_1 \& \vec{F}_2$ are parallel vector ✓

" " " ^ equal vector ✗

$\vec{F}_1 \& \vec{v}$ one parallel vector ✓

$\vec{F}_2 \& \vec{v}$

$\vec{F}_1 \& \vec{F}_3$ are antiparallel

$\vec{v} \& \vec{F}_3$

" "

" "



$$\textcircled{1} \quad \vec{A} = 4\hat{i} - 2\hat{j}$$

$$\vec{B} = 3\hat{i} + 4\hat{j}$$

$$264 - 264 = 0$$

$$\textcircled{1} \quad \text{Component of } \vec{A} \text{ parallel to } \vec{B} = A \cos \theta = \frac{\vec{A} \cdot \vec{B}}{|\vec{B}|} = \frac{12 - 8}{5} = \frac{4}{5}$$

"

$$\text{" Vector form" } = \frac{4}{5} \cdot \hat{B} = \frac{4}{5} \left(\frac{3\hat{i} + 4\hat{j}}{5} \right) = \frac{12\hat{i} + 16\hat{j}}{25}$$

$$\textcircled{2} \quad \text{Component of } \vec{A} \text{ perpendicular to } \vec{B} = \vec{A} - \vec{A}_{||}$$

$$= (4\hat{i} - 2\hat{j}) - \frac{12\hat{i} + 16\hat{j}}{25}$$

$$= \frac{88\hat{i} - 66\hat{j}}{25}$$

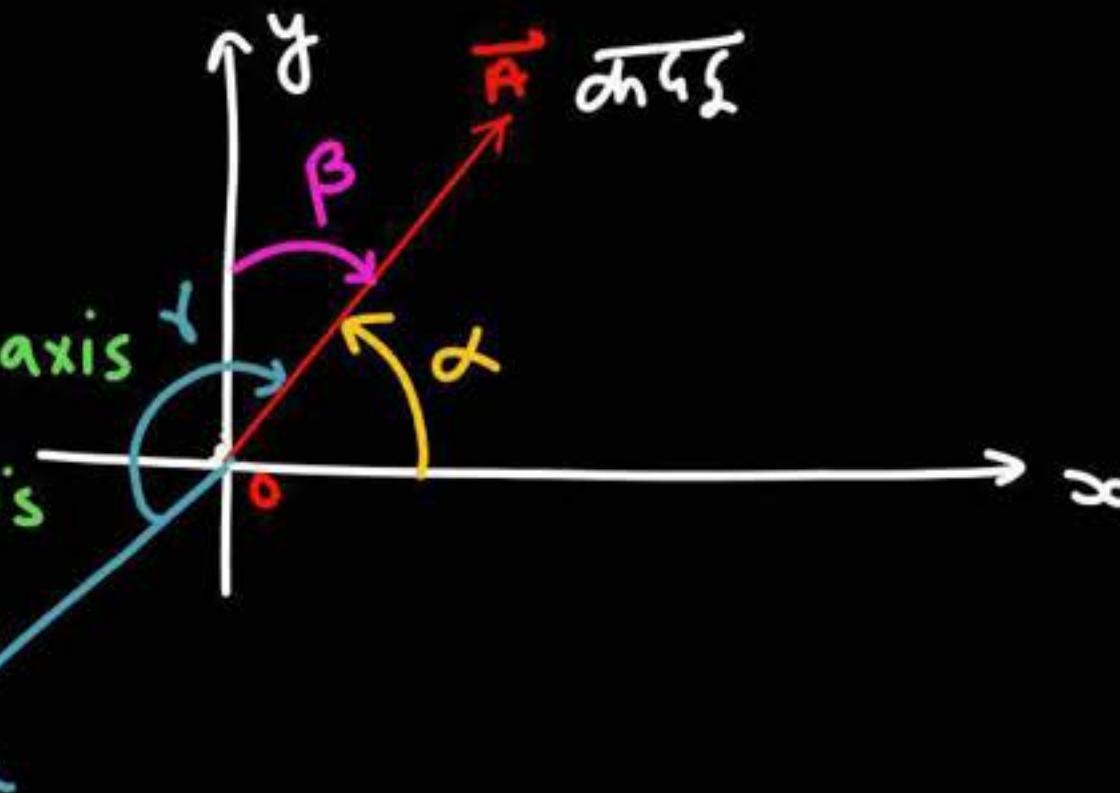
Direction Cosine

$$\vec{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$$

If \vec{A} makes angle α with $+x$ -axis

" " " +y-axis
" " " +z-axis

β
 γ



Component of \vec{A} along x-Axis = $A \cos \alpha = A_x$

Component of \vec{A} along y-Axis = $A \cos \beta = A_y$

Component of \vec{A} along z-Axis = $A \cos \gamma = A_z$

$$\cos \alpha = \frac{A_x}{A}$$

$$\cos \beta = \frac{A_y}{A}$$

$$\cos \gamma = \frac{A_z}{A}$$

$$\text{Q} \quad \vec{A} = 2\hat{i} + 3\hat{j} + 6\hat{k}$$

$$A = |\vec{A}| = \sqrt{2^2 + 3^2 + 6^2} = 7$$

$$\cos \alpha = \frac{A_x}{A} = \frac{2}{7}$$

$$\cos \beta = \frac{A_y}{A} = \frac{3}{7}$$

$$\cos \gamma = \frac{A_z}{A} = \frac{6}{7}$$

direction cosine



Silly

$$\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$$

$$\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma = 1 \times \\ = 2 \checkmark$$

$$\rightarrow 1 - \sin^2 \alpha + 1 - \sin^2 \beta + 1 - \sin^2 \gamma = 1$$

$$\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma = 2.$$

$$\text{Q} \quad \vec{A} = 3\hat{i} + 4\hat{j} + 5\hat{k}$$

$$A = \sqrt{3^2 + 4^2 + 5^2} = 5\sqrt{2}$$

① Direction cosine

$$\cos \alpha = \frac{3}{5\sqrt{2}}$$

$$\cos \beta = \frac{4}{5\sqrt{2}}$$

$$\cos \gamma = \frac{5}{5\sqrt{2}} = \frac{1}{\sqrt{2}}, \quad Y = 45^\circ$$

②

Component of \vec{A} along x -axis = $3\hat{i}$

③

" " y " = $4\hat{j}$

④

" " z " = $5\hat{k}$

* ⑤

" on $x-y$ plane = $3\hat{i} + 4\hat{j}$

* ⑥

" on $y-z$ plane = $4\hat{j} + 5\hat{k}$

$\hat{i} \hat{j} \hat{k} \hat{i} \hat{j} \hat{k} \hat{i} \hat{j} \hat{k}$

K.C.

Same seq $\equiv +$ Remainder }
diff seq $= -$ Remainder }

Q

$$\vec{a} = 3\hat{i} + 4\hat{j}$$

$$\vec{b} = 2\hat{i} + 5\hat{j}$$

$$\hat{i} \times \hat{i} = 0$$

$$\hat{j} \times \hat{j} = 0$$

Q

$$\vec{a} = 4\hat{i} + 7\hat{j}$$

$$\vec{b} = 2\hat{i} + 3\hat{j}$$

$$\textcircled{1} \quad \vec{a} \times \vec{b} = ?$$

$$\textcircled{2} \quad \vec{b} \times \vec{a} = ?$$

$$\vec{a} \times \vec{b} = (3\hat{i} + 4\hat{j}) \times (2\hat{i} + 5\hat{j})$$

$$= 6\hat{i} \times \hat{i} + 15\hat{i} \times \hat{j} + 8\hat{j} \times \hat{i} + 20\hat{j} \times \hat{j}$$

$$= 0 + 15\hat{k} - 8\hat{k} + 0$$

$$= 7\hat{k} = \vec{c}$$

$$\vec{c} \perp \vec{a}, \vec{c} \perp \vec{b}$$

$$\text{Q} \quad \vec{a} = 4\hat{i} + 7\hat{j}$$
$$\vec{b} = 2\hat{i} + 3\hat{j}$$

$$\vec{a} \times \vec{b} = (4\hat{i} + 7\hat{j}) \times (2\hat{i} + 3\hat{j})$$
$$= 0 + 12\hat{k} - 14\hat{k} + 0$$
$$= -2\hat{k}$$

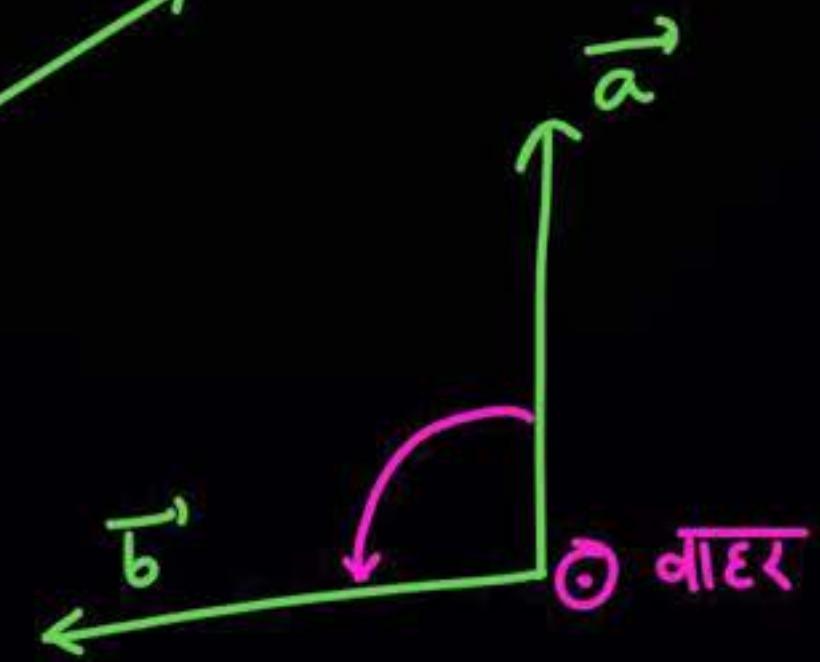
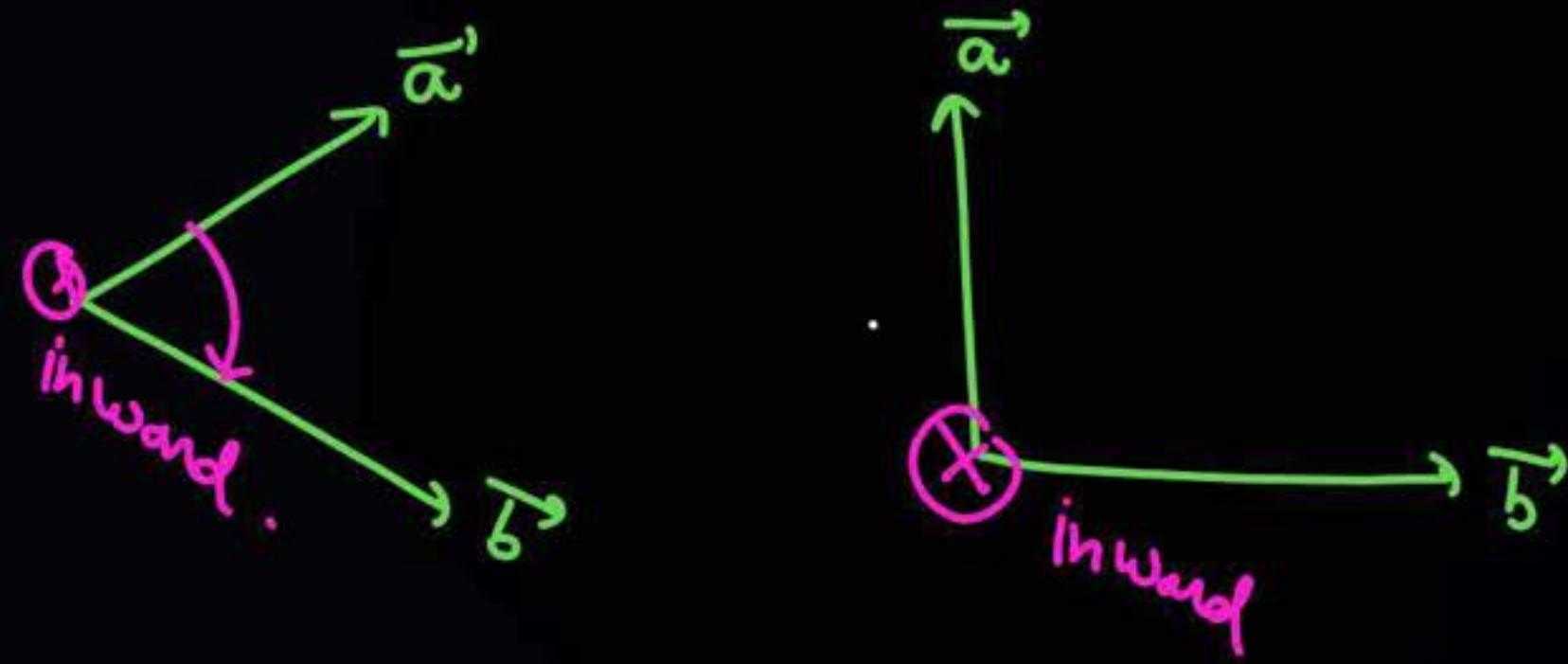
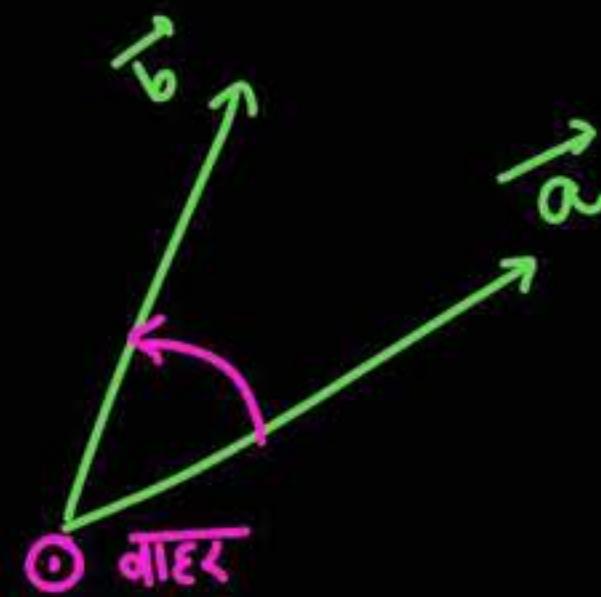
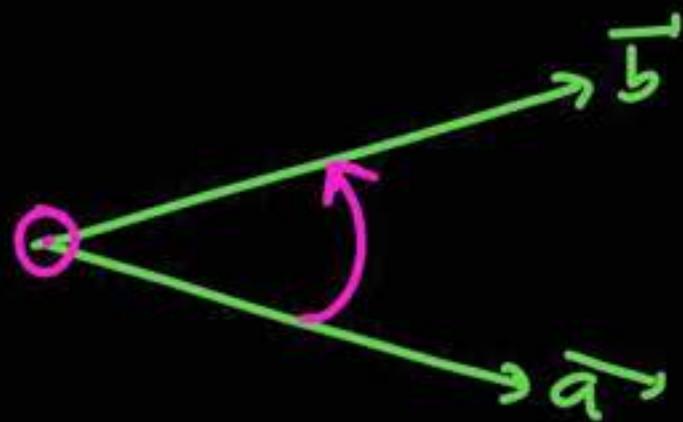
$$\vec{b} \times \vec{a} = (2\hat{i} + 3\hat{j}) \times (4\hat{i} + 7\hat{j})$$
$$= 0 + 14\hat{k} - 12\hat{k} + 0$$

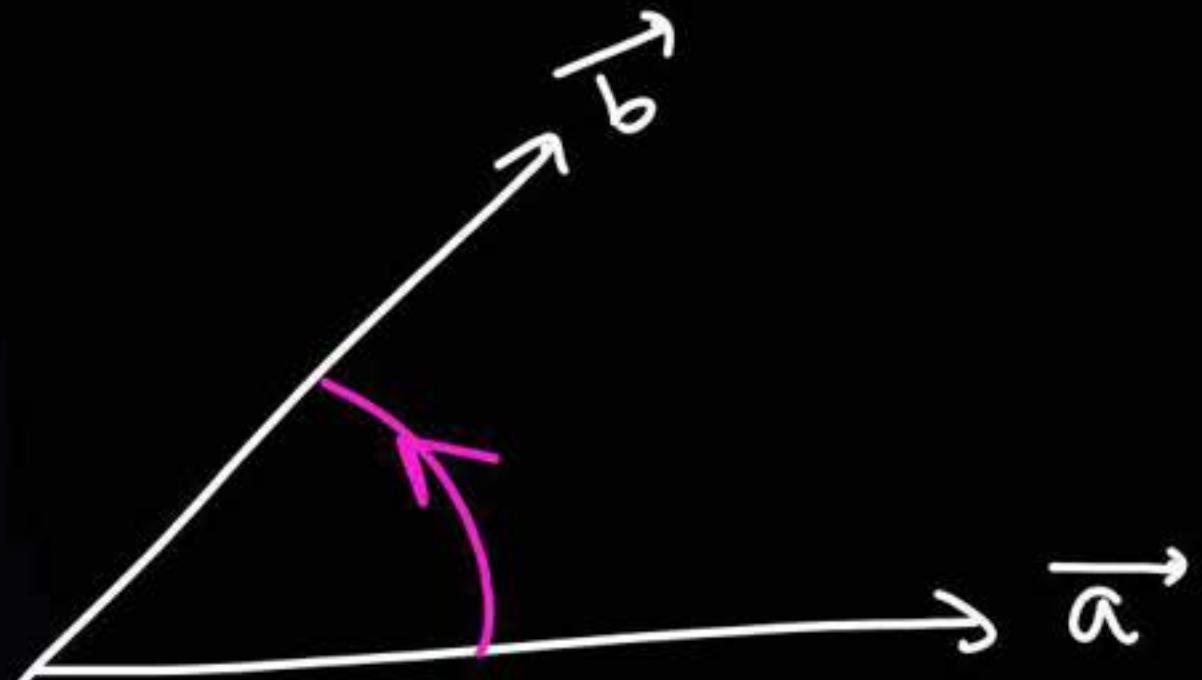
$$\boxed{\vec{b} \times \vec{a} = + 2\hat{k}}$$

$$\boxed{\vec{a} \times \vec{b} = - \vec{b} \times \vec{a}}$$

Q Find dir of $\vec{a} \times \vec{b}$

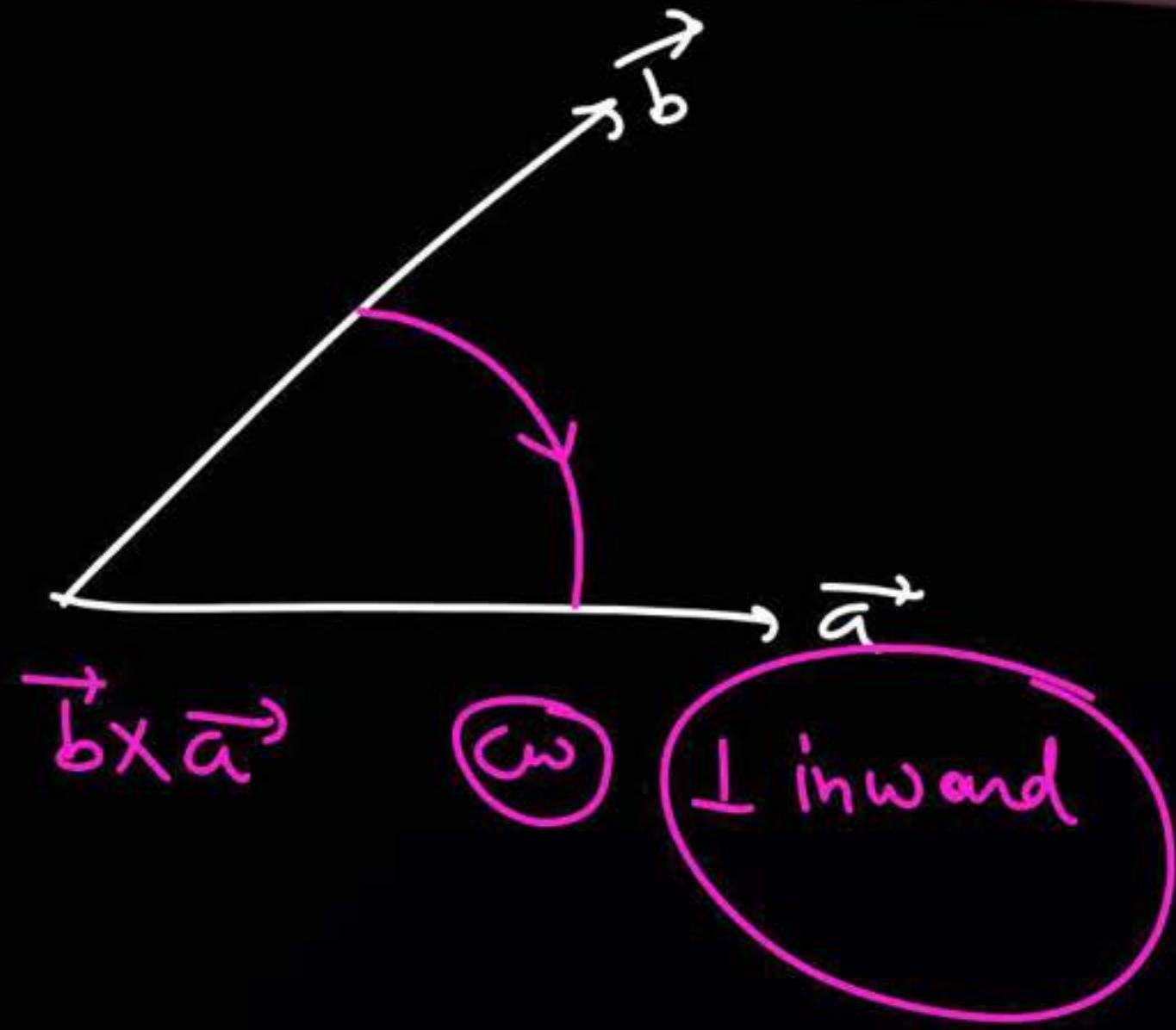
PW

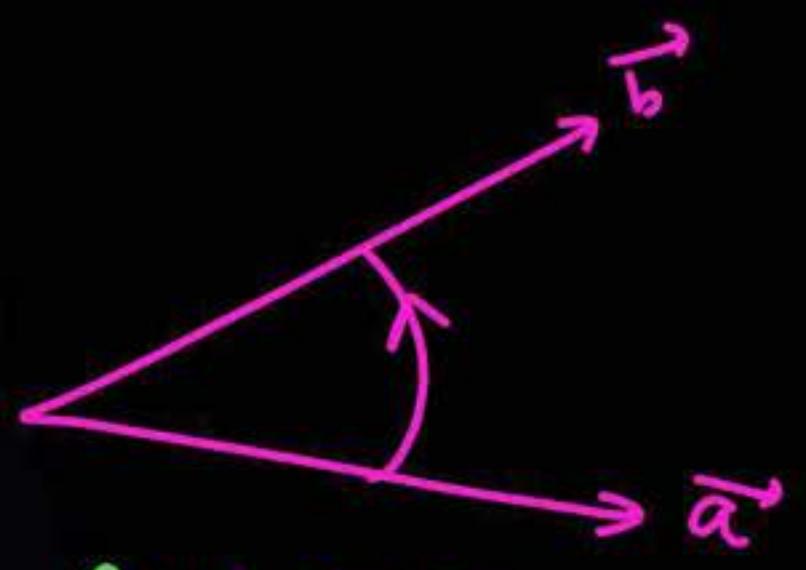




$$\vec{a} \times \vec{b} = \text{dir}^n$$

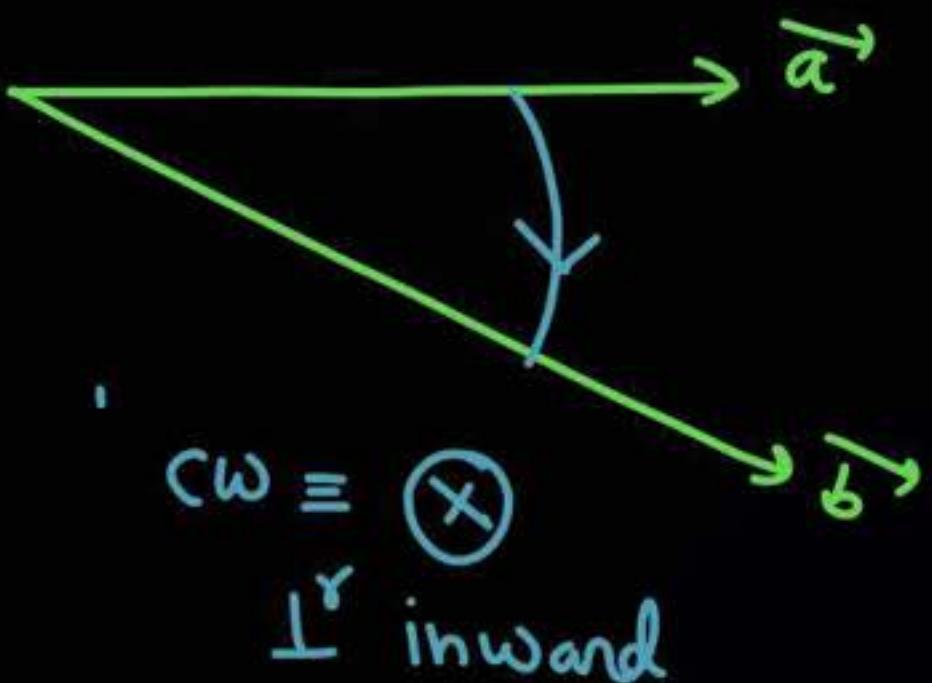
$$A_{\text{CW}} = \cancel{\text{dist}}$$





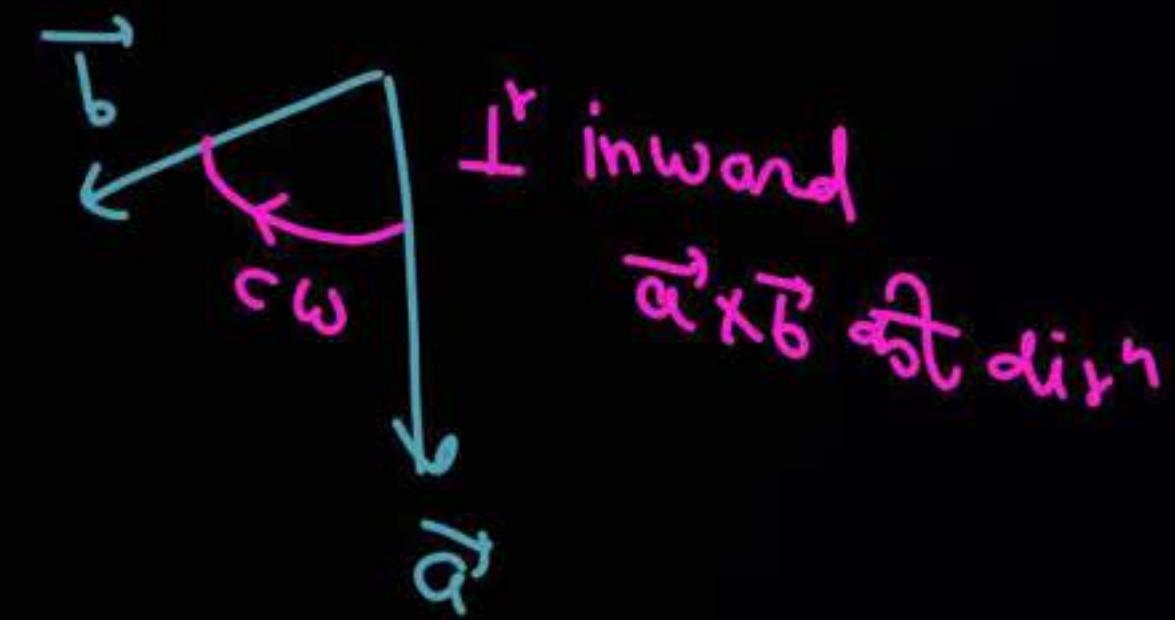
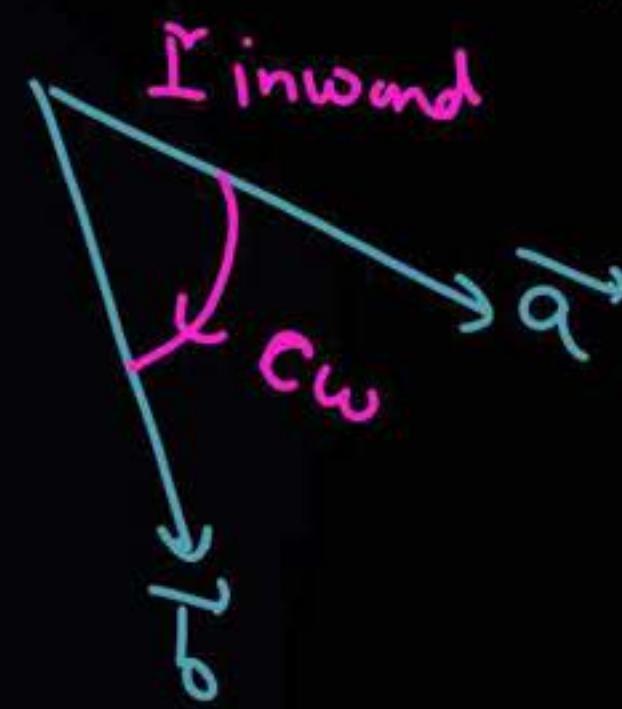
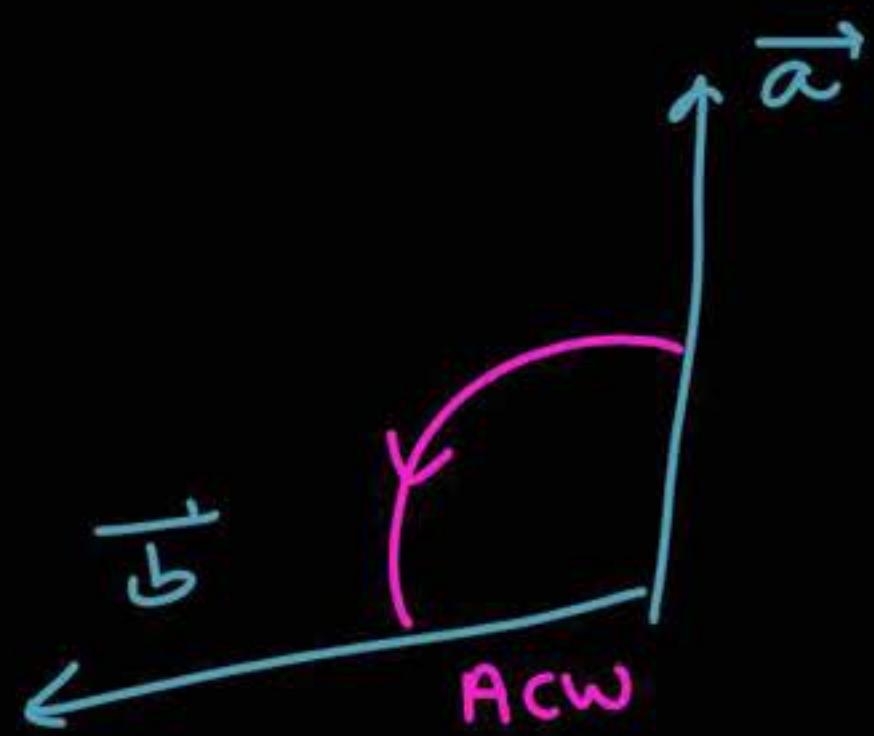
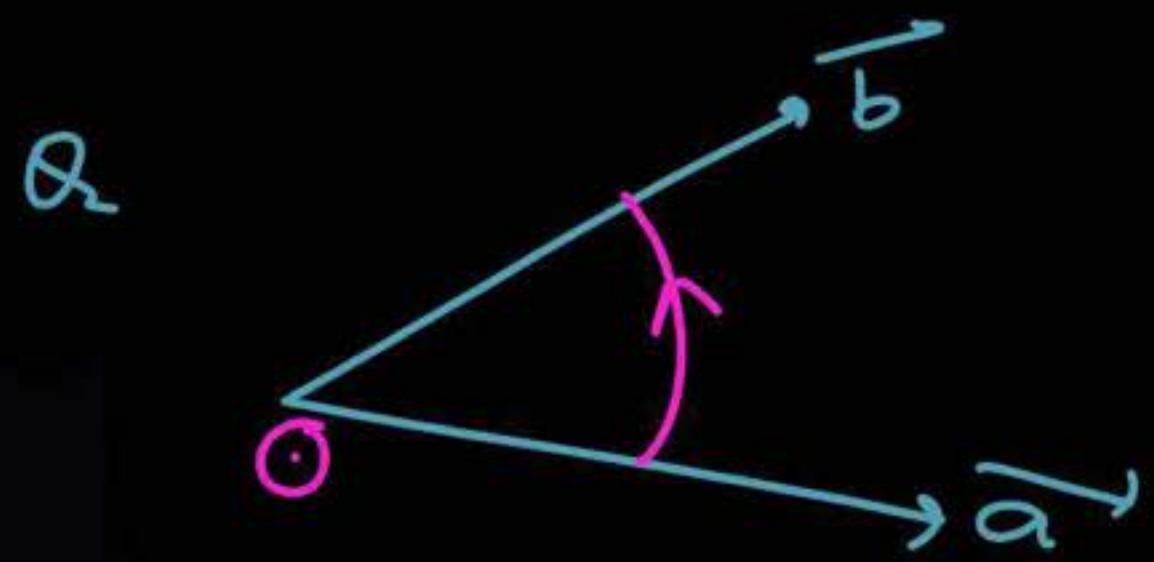
ACW sense

$$\odot = (\perp^y \text{ outward})$$



CW = \times

\perp^y inward



Imp. Points

$$\hat{i} \cdot \hat{i} = 1$$

$$\hat{i} \cdot \hat{j} = \hat{j} \cdot \hat{k} = \hat{i} \cdot \hat{k} = 0$$

$\vec{A} \cdot \vec{B} = AB \cos \theta$

$$\hat{j} \cdot \hat{j} = 1$$

$$\hat{k} \cdot \hat{k} = 1$$

$$\text{If } \vec{A} \perp \vec{B} \Rightarrow \vec{A} \cdot \vec{B} = 0$$

$$\vec{A} \cdot \vec{A} = A^2$$

$$(\vec{A} + \vec{B}) \cdot (\vec{C} + \vec{D}) = \vec{A} \cdot \vec{C} + \vec{A} \cdot \vec{D} + \vec{B} \cdot \vec{C} + \vec{B} \cdot \vec{D} = 0$$

$$\vec{A} \cdot \vec{B} = \vec{B} \cdot \vec{A} = AB \cos 0^\circ$$

$$\vec{A} = 2\hat{i} - 5\hat{j} + 7\hat{k}$$

$$\vec{B} = 3\hat{i} + 4\hat{j} + 5\hat{k}$$

$$\vec{A} \cdot \vec{B} = 6 - 20 + 35 = 21$$

Q find $\vec{A} \cdot \vec{B}$

① $\vec{A} = 3\hat{i} + 4\hat{j} + 5\hat{k}$
 $\vec{B} = 2\hat{i} - 3\hat{j} - 4\hat{k}$
 $\vec{A} \cdot \vec{B} = 6 - 12 - 20 = -26$

② $\vec{A} = \hat{i} - \hat{k}$
 $\vec{B} = \hat{j} + \hat{k}$
 $\vec{A}' = \hat{i} + 0\hat{j} - \hat{k}$
 $\vec{B}' = 0\hat{i} + \hat{j} + \hat{k}$

 $\vec{A} \cdot \vec{B} = 0 + 0 - 1 = -1$

③ $\vec{A} = \hat{i} - \hat{j} + 2\hat{k}$
 $\vec{B} = 4\hat{i} + 8\hat{j} + 2\hat{k}$
 $\vec{A} \cdot \vec{B} = 4 - 8 + 4 = 0$

④ $\vec{A} = \hat{i} - \hat{j} = \hat{i} - \hat{j} + 0\hat{k}$
 $\vec{B} = \hat{i} + \hat{k} = \hat{i} + 0\hat{j} + \hat{k}$
 $\vec{A} \cdot \vec{B} = 1 + 0 + 0 = 1$

अमांदे वेक्टर
उपकृति उनका डोट प्रोडक्ट
यू८७० द्वारा

JEE main
गत
स्कूल

$$\text{Q} \quad \vec{A} = 2\hat{i} - 3\hat{j} + 4\hat{k}$$

$$\vec{B} = \alpha\hat{i} + 2\hat{j} + 5\hat{k}$$

If $\vec{A} \perp \vec{B}$ find α

$$\vec{A} \cdot \vec{B} = 0$$

$$2\alpha - 6 + 20 = 0$$

$$2\alpha + 14 = 0$$

$$\boxed{\alpha = -7}$$

Q Find angle b/w \vec{A} & \vec{B}

$$\vec{A} = \hat{i} + \hat{j}$$

$$\vec{B} = 3\hat{i} + 4\hat{j}$$

$$\underline{\vec{A} \cdot \vec{B} = AB \cos \theta}$$

$$7 = \sqrt{2} 5 \cos \theta$$

मत $\cos \theta = \frac{7}{5\sqrt{2}}$

$$\theta = \cos^{-1}\left(\frac{7}{5\sqrt{2}}\right)$$

$$\vec{A} \cdot \vec{B} = 3+4$$

$$= 7$$

* ज्या $\vec{A} \cdot \vec{B} = AB \cos \theta$

$$\cos \theta = \frac{\vec{A} \cdot \vec{B}}{AB}$$

Q $\vec{A} = 3\hat{i} + 4\hat{j} + 5\hat{k}$ $A = \sqrt{3^2 + 4^2 + 5^2}$

$$\vec{B} = 2\hat{i} + 3\hat{j} + 6\hat{k}$$

$$= 5\sqrt{2}$$

$$B = \sqrt{2^2 + 3^2 + 6^2}$$

$$\underline{\vec{A} \cdot \vec{B} = 6 + 12 + 30 = 48}$$

$$\vec{A} \cdot \vec{B} = AB \cos \theta$$

$$48 = 5\sqrt{2} 7 \cos \theta$$

$$\cos \theta = \frac{48}{35\sqrt{2}}$$

Q Find the angle between \vec{A} & \vec{B}

$$\begin{aligned} \textcircled{1} \quad \vec{A} &= \hat{i} + \hat{j} + \hat{k} \\ \vec{B} &= \hat{i} - \hat{j} + \hat{k} \\ \vec{A} \cdot \vec{B} &= 1 - 1 + 1 = 1 \end{aligned}$$

$$1 = \sqrt{3} \sqrt{3} \cos \theta$$

$$\cos \theta = \frac{1}{3}$$

$$\begin{aligned} \textcircled{2} \quad \vec{A} &= \hat{i} + \hat{j} \\ \vec{B} &= \hat{i} - \hat{j} \\ \vec{A} \cdot \vec{B} &= 1 - 1 = 0 \end{aligned}$$

$$\theta = 90^\circ$$

$$\begin{aligned} \textcircled{3} \quad \vec{A} &= 3\hat{i} + 4\hat{j} + 5\hat{k} \\ \vec{B} &= 2\hat{i} - 4\hat{j} + 2\hat{k} \\ \vec{A} \cdot \vec{B} &= 6 - 16 + 10 = 0 \end{aligned}$$

$$\theta = 90^\circ$$

$$\begin{aligned} \textcircled{4} \quad \vec{A} &= 3\hat{i} + 4\hat{j} + 5\hat{k} \\ \vec{B} &= 6\hat{i} + 8\hat{j} + 10\hat{k} \end{aligned}$$

$$A = 5\sqrt{2}$$

$$B = 10\sqrt{2}$$

$$\vec{A} \cdot \vec{B} = 18 + 32 + 50 = 100$$

$$\vec{A} \cdot \vec{B} = AB \cos \theta$$

$$100 = 5\sqrt{2} \cdot 10\sqrt{2} \cos \theta$$

$$\cos \theta = 1$$

\vec{A} & \vec{B} are parallel

$$\theta = 0^\circ$$

$$\overrightarrow{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$$

$$\overrightarrow{B} = B_x \hat{i} + B_y \hat{j} + B_z \hat{k}$$

Q $\overrightarrow{A} = 3\hat{i} + 4\hat{j} + 5\hat{k}$

$$\overrightarrow{B} = 6\hat{i} + 8\hat{j} + 10\hat{k} = 2[3\hat{i} + 4\hat{j} + 5\hat{k}]$$

$$\frac{3}{6} = \frac{4}{8} = \frac{5}{10} = \frac{1}{2}$$

$$\overrightarrow{B} = 2\overrightarrow{A}$$

$\overrightarrow{A} \uparrow \uparrow \text{ to } \overrightarrow{B}$

If

$$\frac{A_x}{B_x} = \frac{A_y}{B_y} = \frac{A_z}{B_z} = n$$

$n > 0 \Rightarrow \overrightarrow{A}$ is parallel to \overrightarrow{B}

$n < 0 \Rightarrow \overrightarrow{A}$ is antiparallel to \overrightarrow{B}

Q $\overrightarrow{A} = 4\hat{i} + 6\hat{j}$

$$\overrightarrow{B} = 12\hat{i} + 18\hat{j}$$

$$\frac{4}{12} = \frac{6}{18}$$

$$\overrightarrow{A} \uparrow \uparrow \overrightarrow{B}$$

$$\text{Q} \quad \vec{A} = 3\hat{i} - 4\hat{j} + 5\hat{k}$$

$$\begin{aligned}\vec{B} &= -9\hat{i} + 12\hat{j} - 15\hat{k} \\ &= -3(3\hat{i} - 4\hat{j} + 5\hat{k})\end{aligned}$$

$$\frac{3}{-9} = \frac{-4}{12} = \frac{5}{-15}$$

$\Rightarrow -\frac{1}{3}$
Antiparallel

$$\vec{B} = -3\vec{A}$$



$$\text{Q} \quad \vec{A} = 2\hat{i} + 3\hat{j} + 4\hat{k}$$

$$\vec{B} = 4\hat{i} + 6\hat{j} - 8\hat{k}$$

- ~~(a)~~ \vec{A} is parallel to \vec{B}
~~(b)~~
~~(c)~~

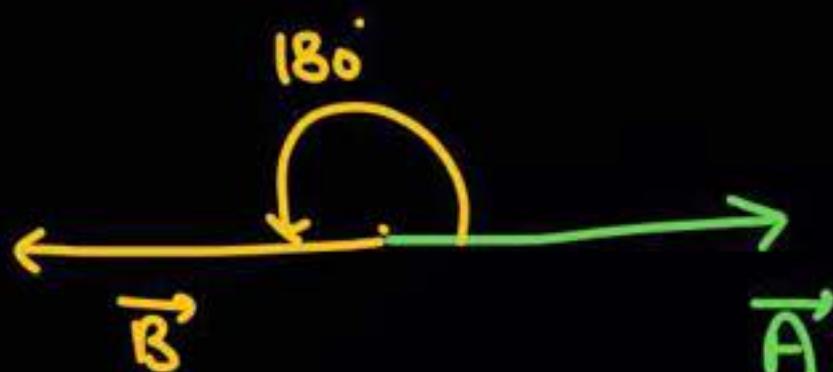
∴ antiparallel
कूप नहीं है, कदम है



\vec{A}, \vec{B} |||| एं anti parallel एं या \perp हैं, या $\overline{\text{नहीं}}$

$$\cos\theta = \frac{\vec{A} \cdot \vec{B}}{AB} = \text{निकालती}$$

If	$\theta = 0$	parallel
	$\theta = 180$	Antiparallel
	$\theta = 90$	\perp



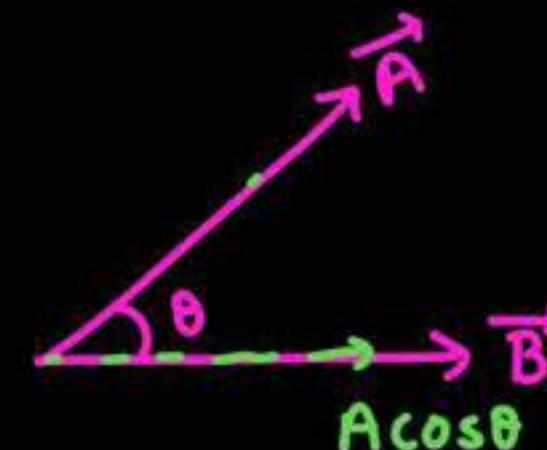
Q

$$\vec{A} = 3\hat{i} + 4\hat{j}$$

$$\vec{B} = \hat{i} + \hat{j}$$

$$\vec{A} \cdot \vec{B} = AB \cos \theta$$

$$AC \cos \theta = \frac{\vec{A} \cdot \vec{B}}{B}$$



Component of \vec{A} along $\vec{B} = AC \cos \theta$

towards

parallel to $= -\frac{\vec{A} \cdot \vec{B}}{B} = \frac{3+4}{\sqrt{2}} = \frac{7}{\sqrt{2}}$ (scalar)

Component of \vec{A} along \vec{B} (in vector form)

$$= \frac{7}{\sqrt{2}} \cdot \hat{B} = \frac{7}{\sqrt{2}} \left(\frac{\hat{i} + \hat{j}}{\sqrt{2}} \right) = \frac{7}{2} (\hat{i} + \hat{j}) = \frac{7}{2} \vec{B}$$

$$\text{Q} \quad \vec{A} = \hat{i} + 3\hat{j}$$

$$\vec{B} = 3\hat{i} + 4\hat{j}$$

Component of \vec{A} along \vec{B} = $A \cos \theta = \frac{\vec{A} \cdot \vec{B}}{B} = \frac{3+12}{5} = 3$

 Vector form $\Rightarrow 3\hat{B} = 3 \cdot \left(\frac{3\hat{i} + 4\hat{j}}{5} \right) = \frac{3}{5}(3\hat{i} + 4\hat{j})$

ऐसा vector बताओ whose magnitude is 3 & dir is along \vec{B}

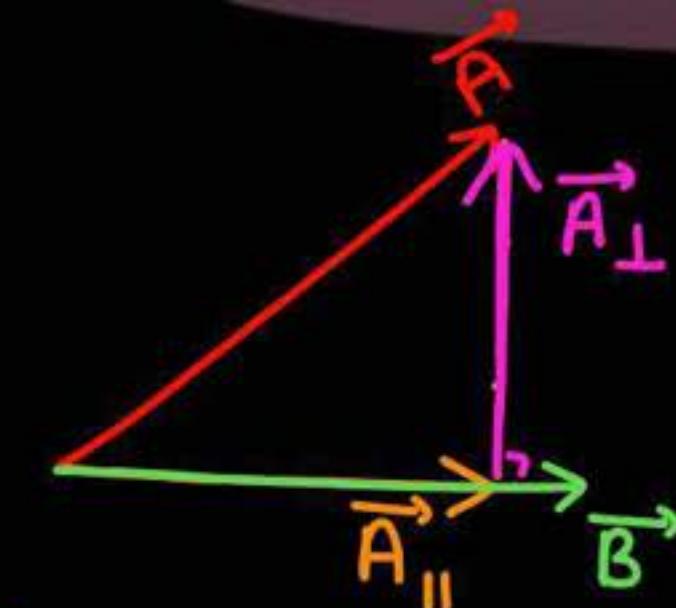
Component of \vec{A} along $\vec{B} = \frac{\vec{A} \cdot \vec{B}}{B}$

Vector form = $\left(\frac{\vec{A} \cdot \vec{B}}{B} \right) \cdot \hat{B}$

Q

$$\vec{A} = \hat{i} + 3\hat{j}$$

$$\vec{B} = 3\hat{i} + 4\hat{j}$$



Component of \vec{A} parallel to \vec{B}
or along

$$= \frac{3}{5}(3\hat{i} + 4\hat{j}) = \vec{A}_{||}$$

$$\vec{A}_{||} + \vec{A}_{\perp} = \vec{A}$$

Component of \vec{A} perpendicular to \vec{B} =

Vector form = ?

$$\vec{A}_{\perp} = \vec{A} - \vec{A}_{||} = (\hat{i} + 3\hat{j}) - \frac{3}{5}(3\hat{i} + 4\hat{j})$$

$$= \underline{\frac{-4\hat{i} + 3\hat{j}}{5}}$$

$$\text{Q} \quad \vec{A} = 2\hat{i} + 3\hat{j}$$

$$\vec{B} = \hat{i} + \hat{j}$$

① Component of \vec{A} along \vec{B} = $\frac{\vec{A} \cdot \vec{B}}{|\vec{B}|} = \frac{2+3}{\sqrt{2}} = \frac{5}{\sqrt{2}}$

∴ Vector = $\frac{5}{\sqrt{2}} \cdot \hat{B} = \frac{5}{\sqrt{2}} \cdot \frac{\hat{i} + \hat{j}}{\sqrt{2}} = \frac{5}{2}(\hat{i} + \hat{j}) =$

② Component of \vec{A} perpendicular to \vec{B} = $\vec{A} - \vec{A}_{||} = 2\hat{i} + 3\hat{j} - \frac{5\hat{i} + 5\hat{j}}{2} = \frac{-3\hat{i} + \hat{j}}{2}$

Q which of the following vector is must be Unit vector

X ① $\vec{A} = \hat{i} + \hat{j}$

$$|\vec{A}| = \sqrt{1^2 + 1^2} = \sqrt{2} \quad \vec{A} \rightarrow \text{not unit vector.}$$

✓ ② $\vec{A} = \frac{\hat{i}}{\sqrt{2}} - \frac{\hat{j}}{\sqrt{2}}$ $|\vec{A}| = \sqrt{\left(\frac{1}{\sqrt{2}}\right)^2 + \left(-\frac{1}{\sqrt{2}}\right)^2}$

✓ ③ $\vec{A} = \frac{\hat{j}}{\sqrt{2}} + \frac{\hat{k}}{\sqrt{2}}$

✓ ④ $\vec{A} = \frac{\hat{i}}{\sqrt{3}} + \frac{\hat{j}}{\sqrt{3}} + \frac{\hat{k}}{\sqrt{3}}$

$$|\vec{A}| = \sqrt{\left(\frac{1}{\sqrt{3}}\right)^2 + \left(\frac{1}{\sqrt{3}}\right)^2 + \left(\frac{1}{\sqrt{3}}\right)^2}$$
$$= \sqrt{\frac{1}{3} + \frac{1}{3} + \frac{1}{3}} = 1$$

⑤ $\vec{A} = \frac{\vec{P} + \vec{Q} + \vec{R}}{|\vec{P} + \vec{Q} + \vec{R}|}$

⑥ $\vec{A} = \frac{\vec{P} + \vec{Q} - \vec{R}}{|\vec{P} + \vec{Q} - \vec{R}|} = \frac{\vec{S}(\text{let})}{|\vec{S}|}$

$$\vec{P} + \vec{Q} + \vec{R} = \vec{S} \text{ (let)}$$

$$\vec{A} = \frac{\vec{S}}{|\vec{S}|}$$

⑦ $\vec{A} = \frac{\vec{P} + \vec{Q} + \vec{R}}{|\vec{P} + \vec{Q} - \vec{R}|}$

\vec{A} must be Unit vector \Rightarrow wrong

$$\textcircled{7} \quad \vec{A} = \frac{\vec{P} + \vec{Q} + \vec{R}}{|\vec{P} + \vec{Q} - \vec{R}|} = \frac{9\hat{i} + 14\hat{j}}{\sqrt{5}} = \text{magnitude} \sqrt{\left(\frac{9}{\sqrt{5}}\right)^2 + \left(\frac{14}{\sqrt{5}}\right)^2} \neq 1$$

Let

$$\begin{cases} \vec{P} = 2\hat{i} + 3\hat{j} \\ \vec{Q} = 3\hat{i} + 5\hat{j} \\ \vec{R} = 4\hat{i} + 6\hat{j} \end{cases}$$

$$\vec{P} + \vec{Q} - \vec{R} = \hat{i} + 2\hat{j}$$

$$|\vec{P} + \vec{Q} - \vec{R}| = \sqrt{1^2 + 2^2} = \sqrt{5}$$

$$\vec{P} + \vec{Q} + \vec{R} = 9\hat{i} + 14\hat{j}$$

Q If \vec{A} is Unit vector find Value of α

$$\vec{A} = \cdot 6\hat{i} + \alpha\hat{j}$$

$$|\vec{A}| = 1$$

$$\sqrt{(-6)^2 + \alpha^2} = 1$$

$$\cdot 36 + \alpha^2 = 1$$

$$\alpha^2 = 1 - \cdot 36$$

$$\alpha^2 = \cdot 64$$

$$\boxed{\alpha = \pm \cdot 8}$$

$$\alpha = \cdot 8 \quad \checkmark$$

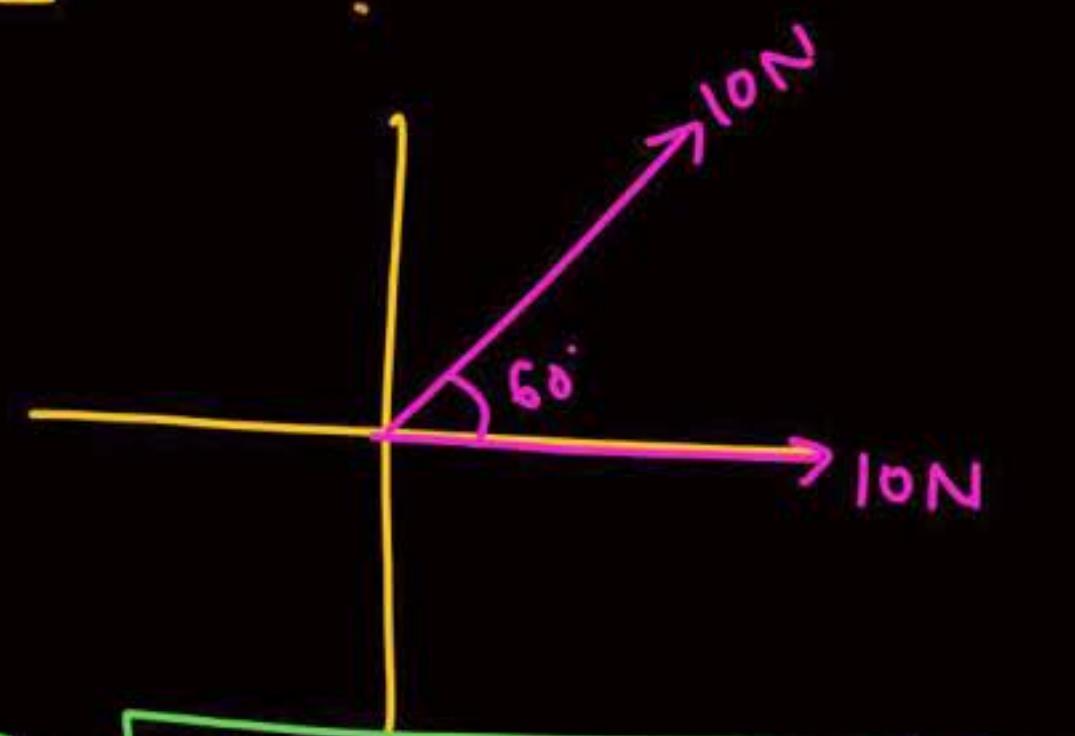
$$\alpha = -\cdot 8 \quad \checkmark$$

$$\vec{A} = \cdot 6\hat{i} + \cdot 8\hat{j}$$

$$\vec{A} = \cdot 6\hat{i} - \cdot 8\hat{j}$$

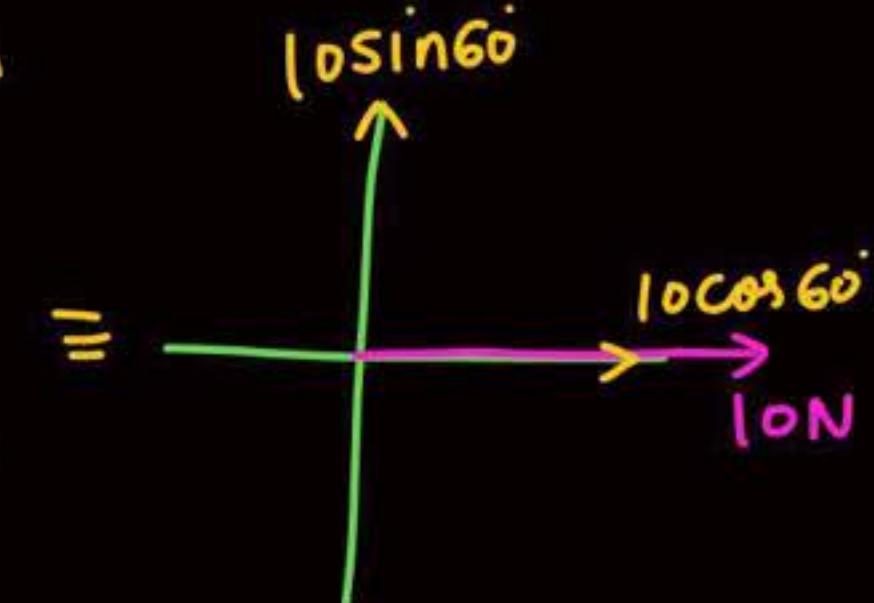
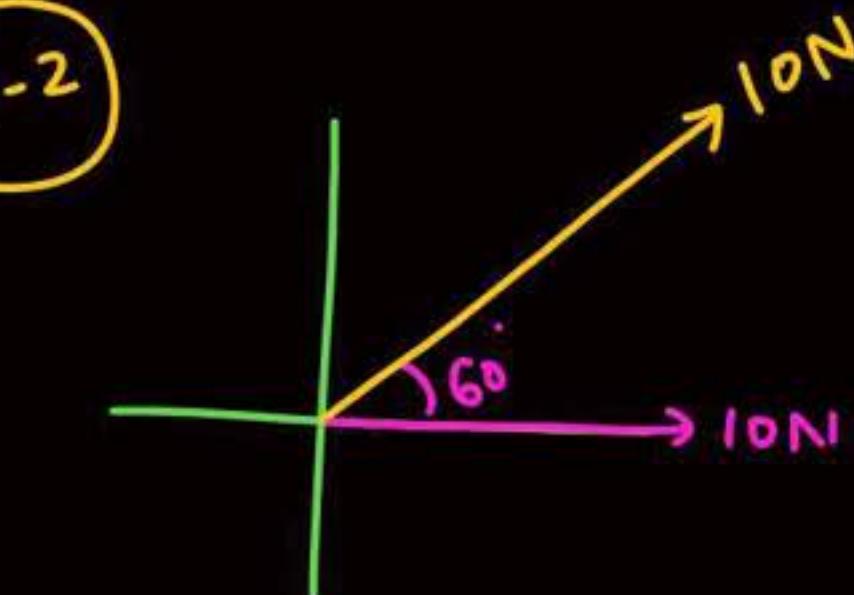
Q

Find net force

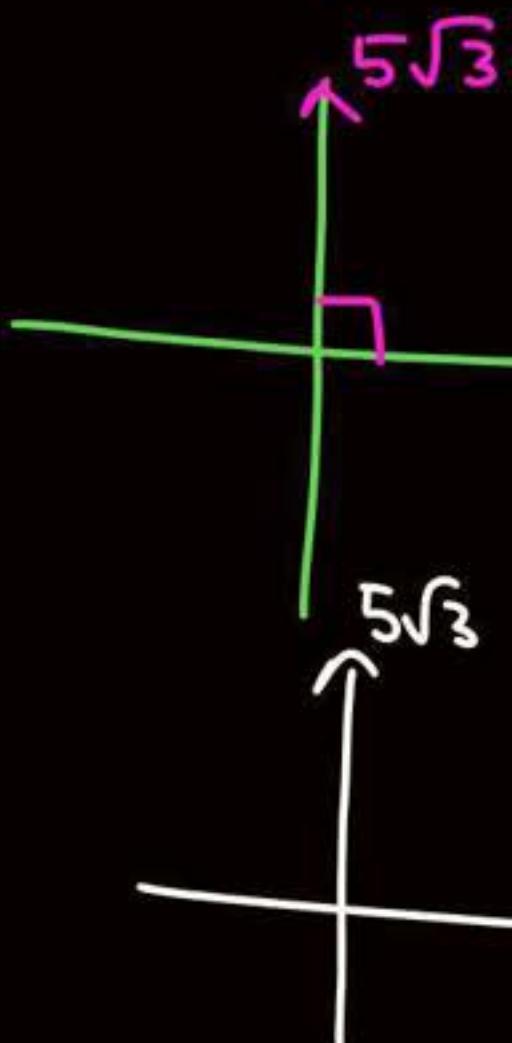


$$c = \sqrt{10^2 + 10^2 + 2 \times 10 \times 10 \cos 60}$$
$$= 10\sqrt{3}$$

M-2

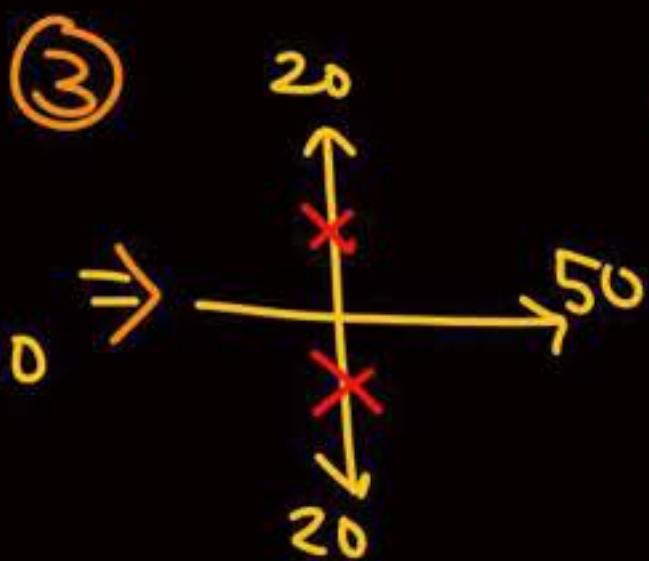
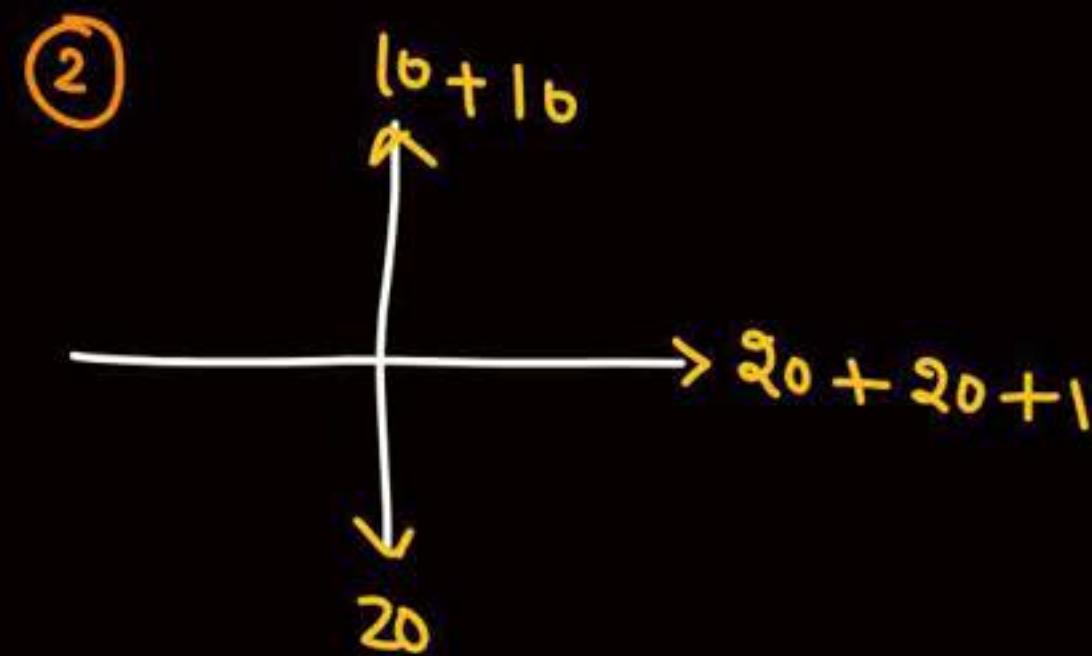
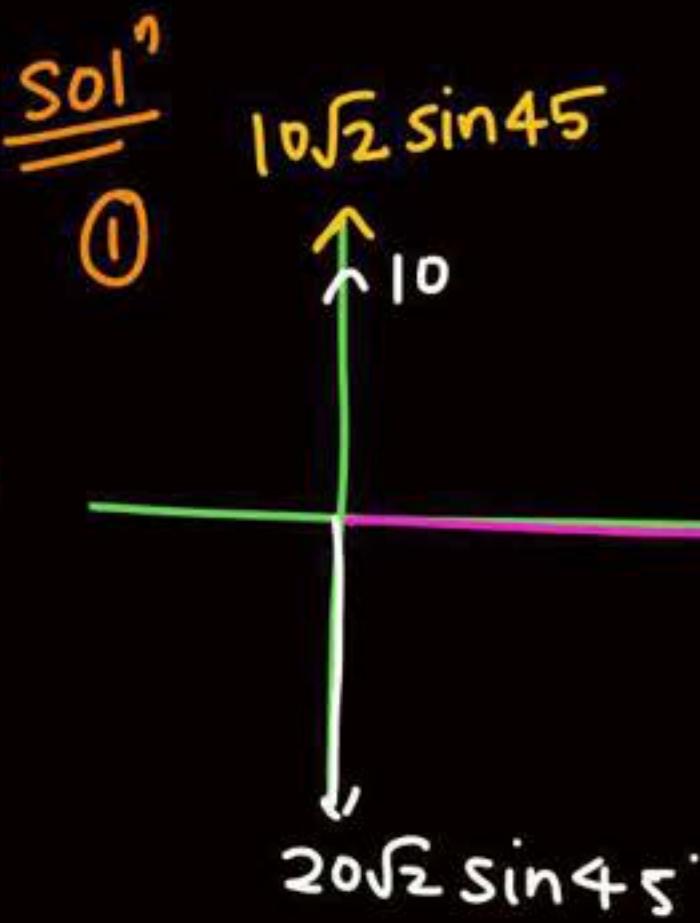
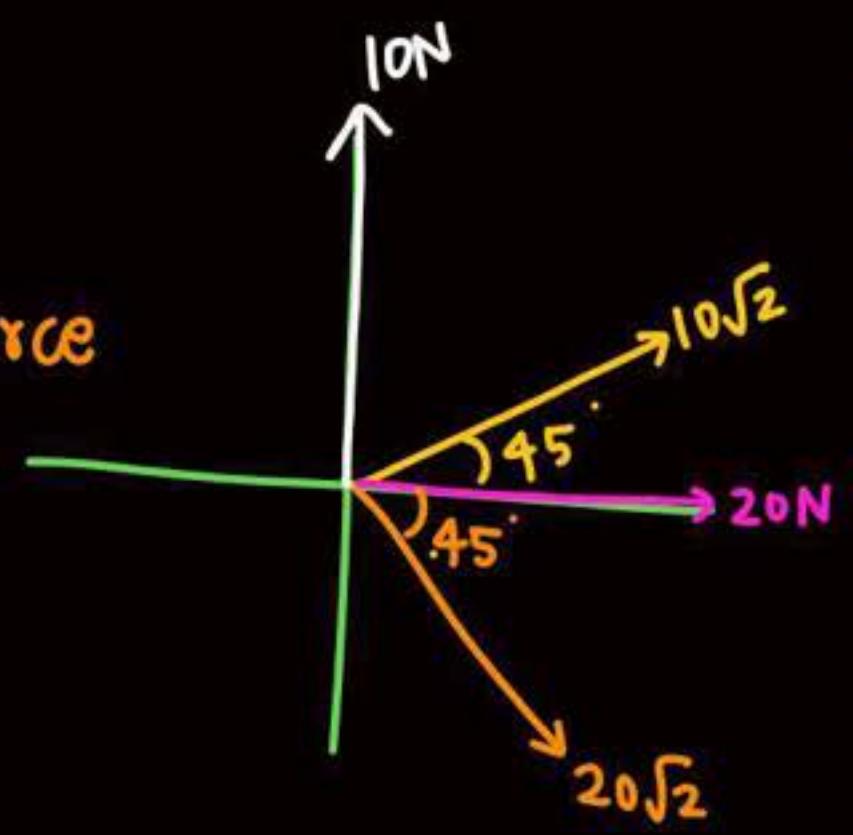


$$\vec{F}_{net} = 15\hat{i} + 5\sqrt{3}\hat{j}$$



$$|\vec{F}_{net}| = \sqrt{15^2 + (5\sqrt{3})^2}$$
$$= \sqrt{225 + 75}$$
$$= 10\sqrt{3}$$

Q find net force



④

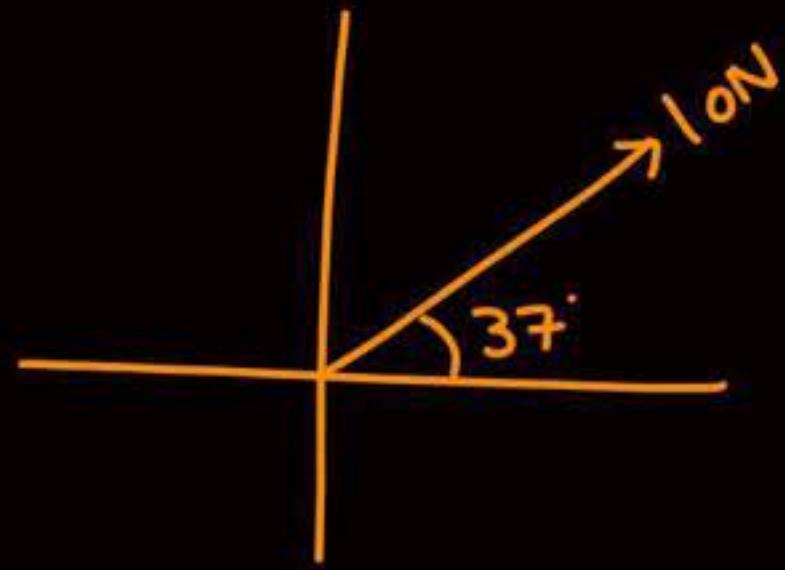
K.C.

* सभी forces को x-y में ताली

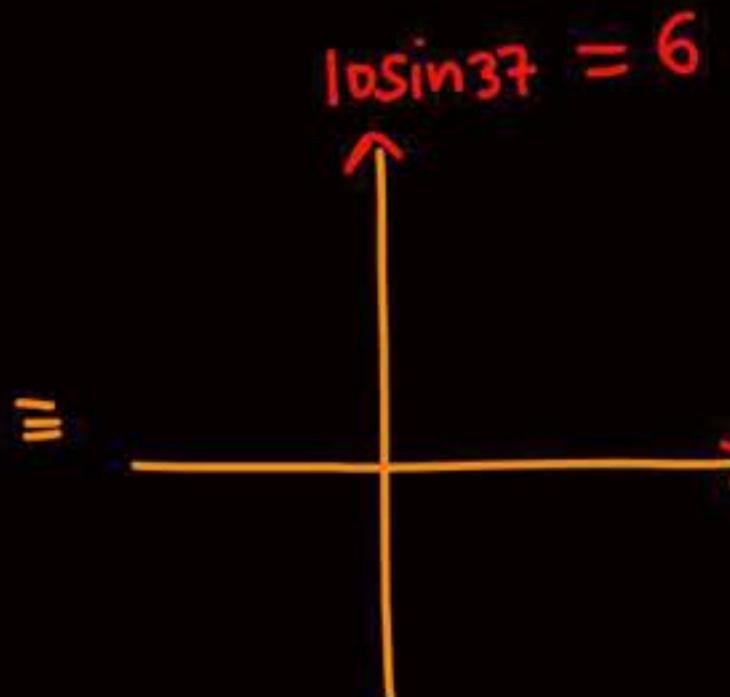
* (x-y) में collect ✓

$$\vec{F}_{\text{net}} = 50\hat{i}$$

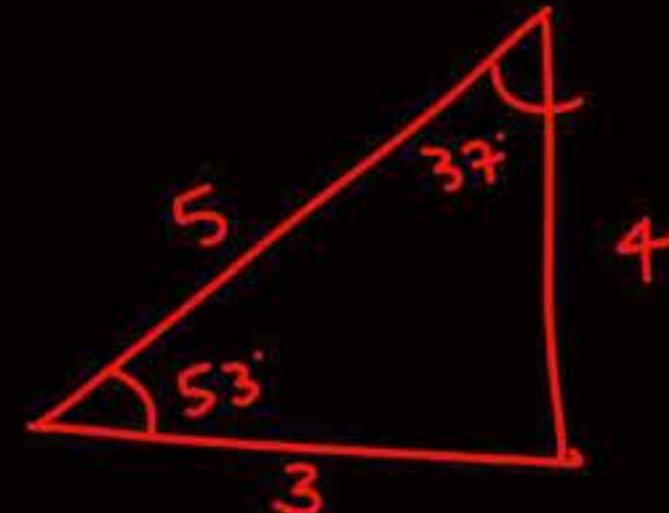
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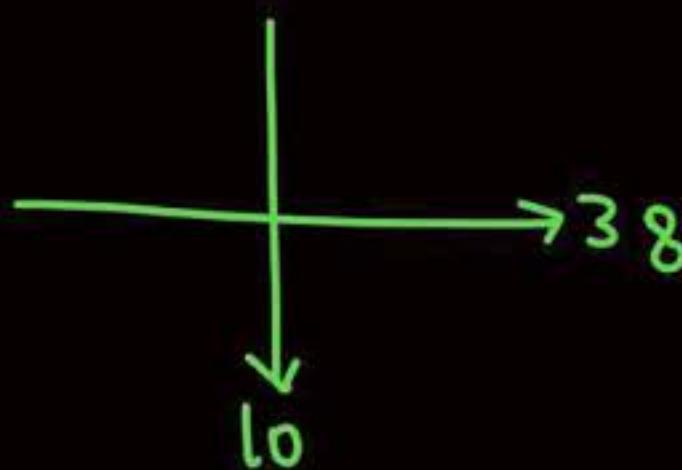
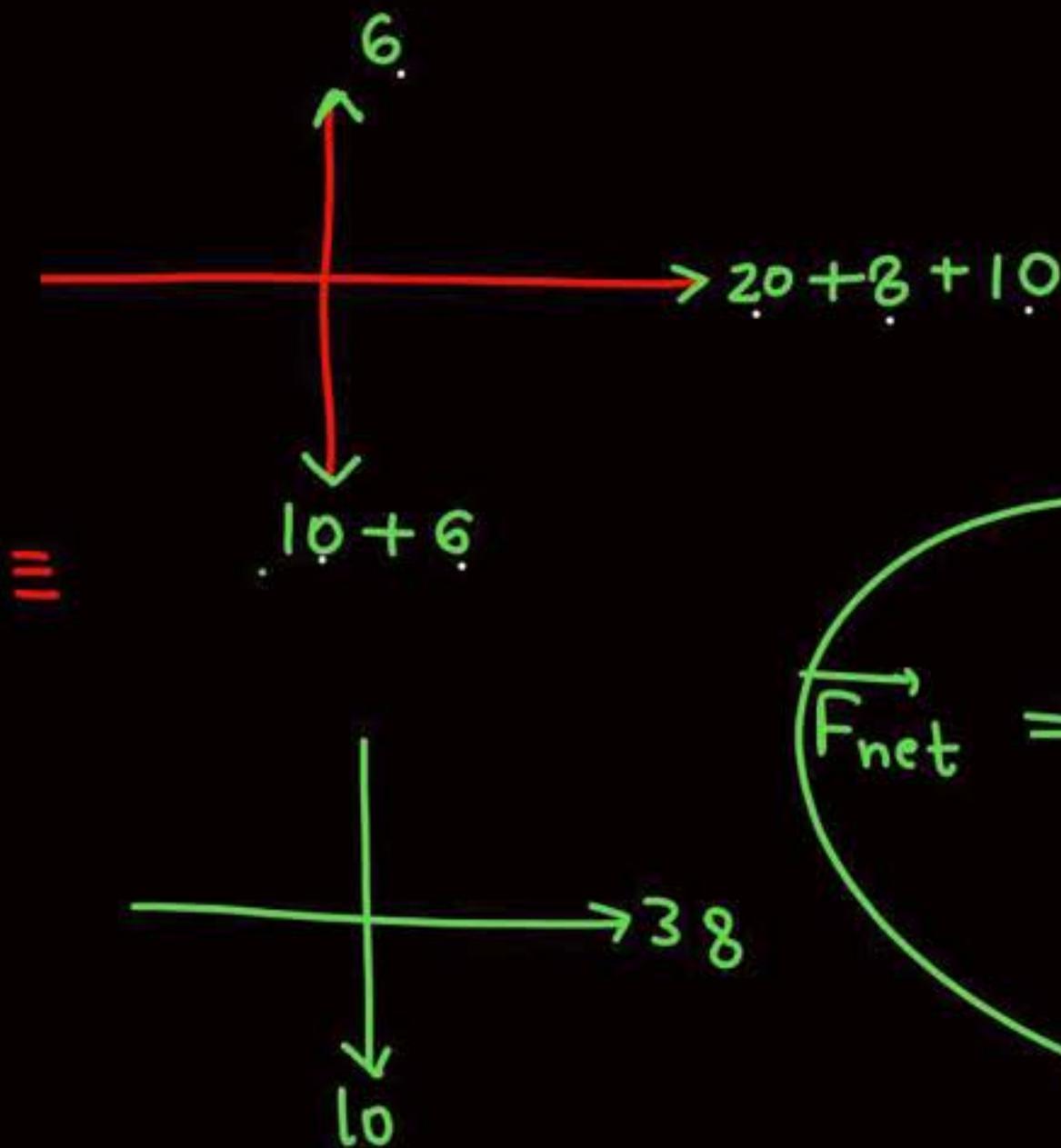
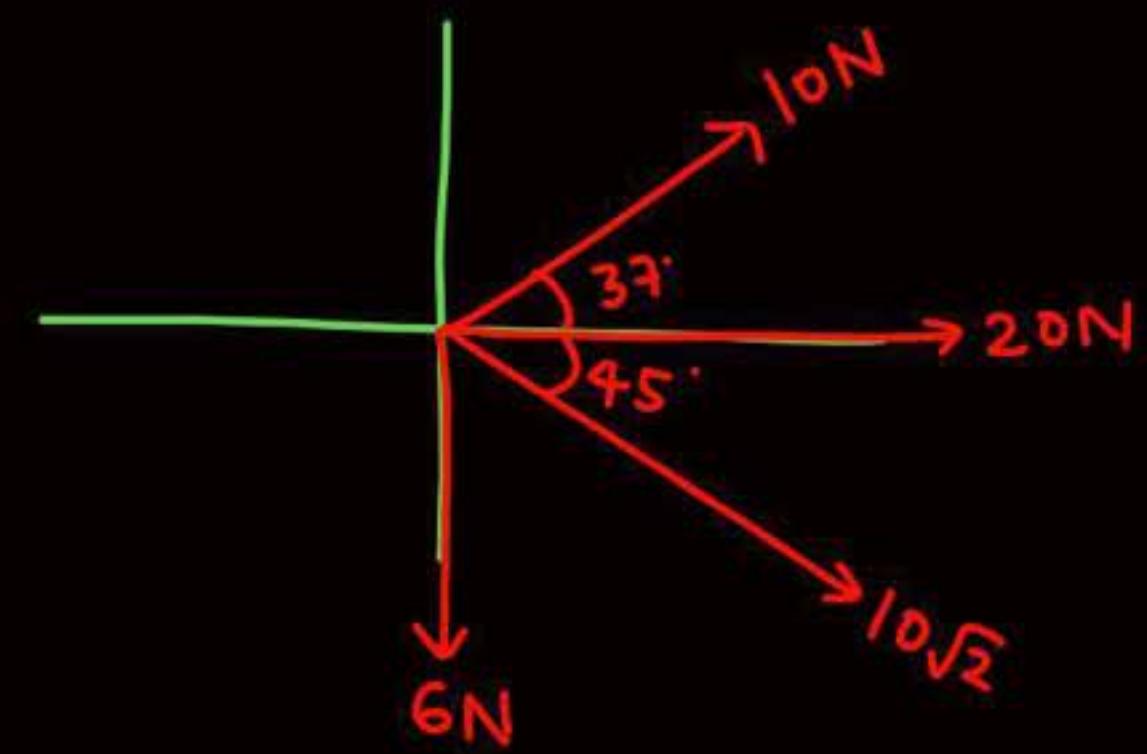


$$\rightarrow 10 \cos 37^\circ = 8$$



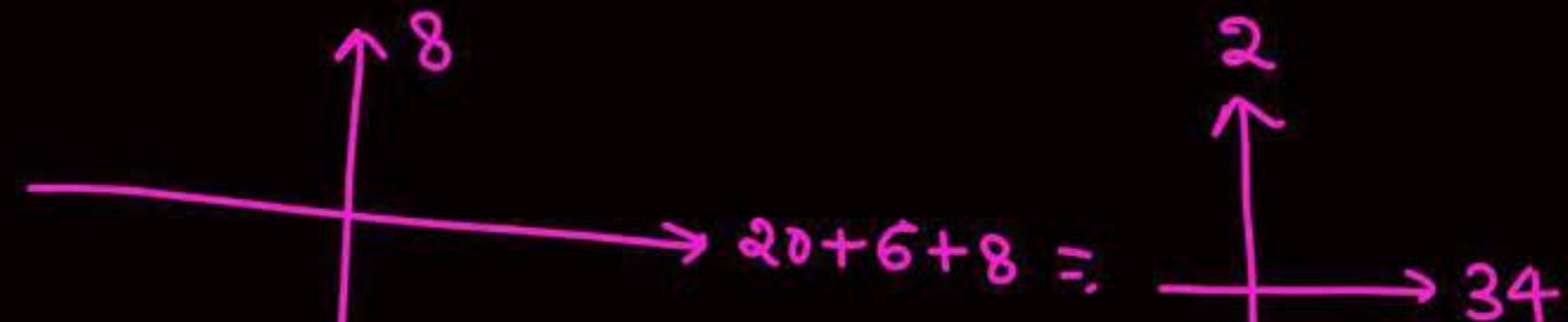
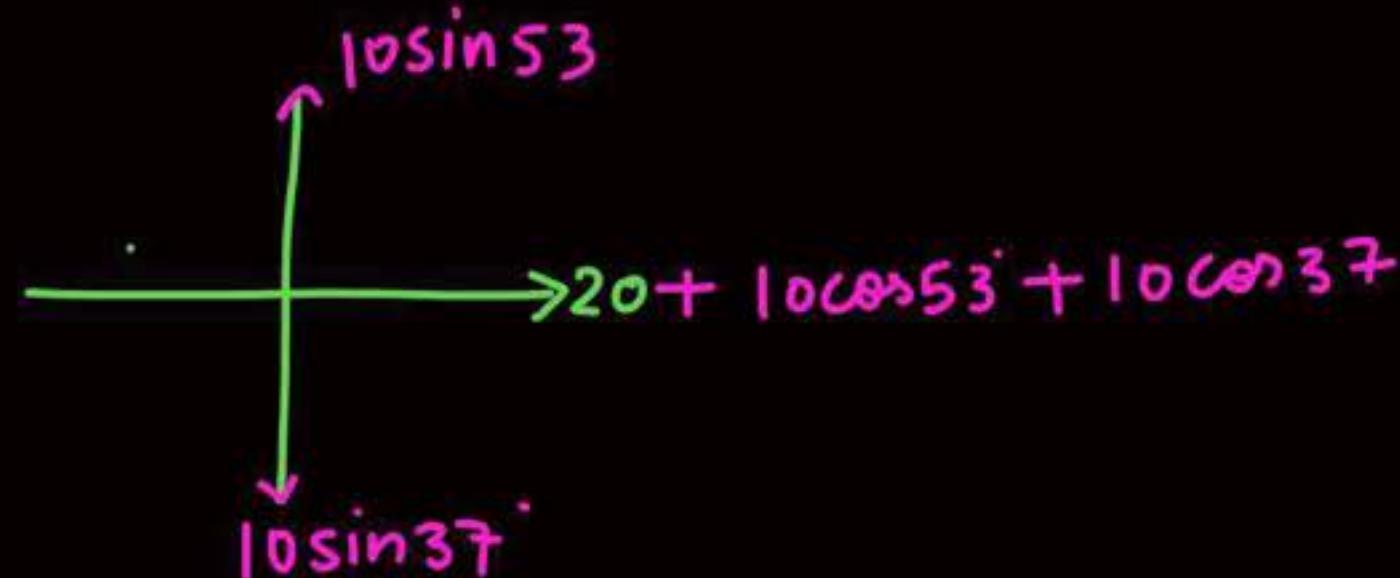
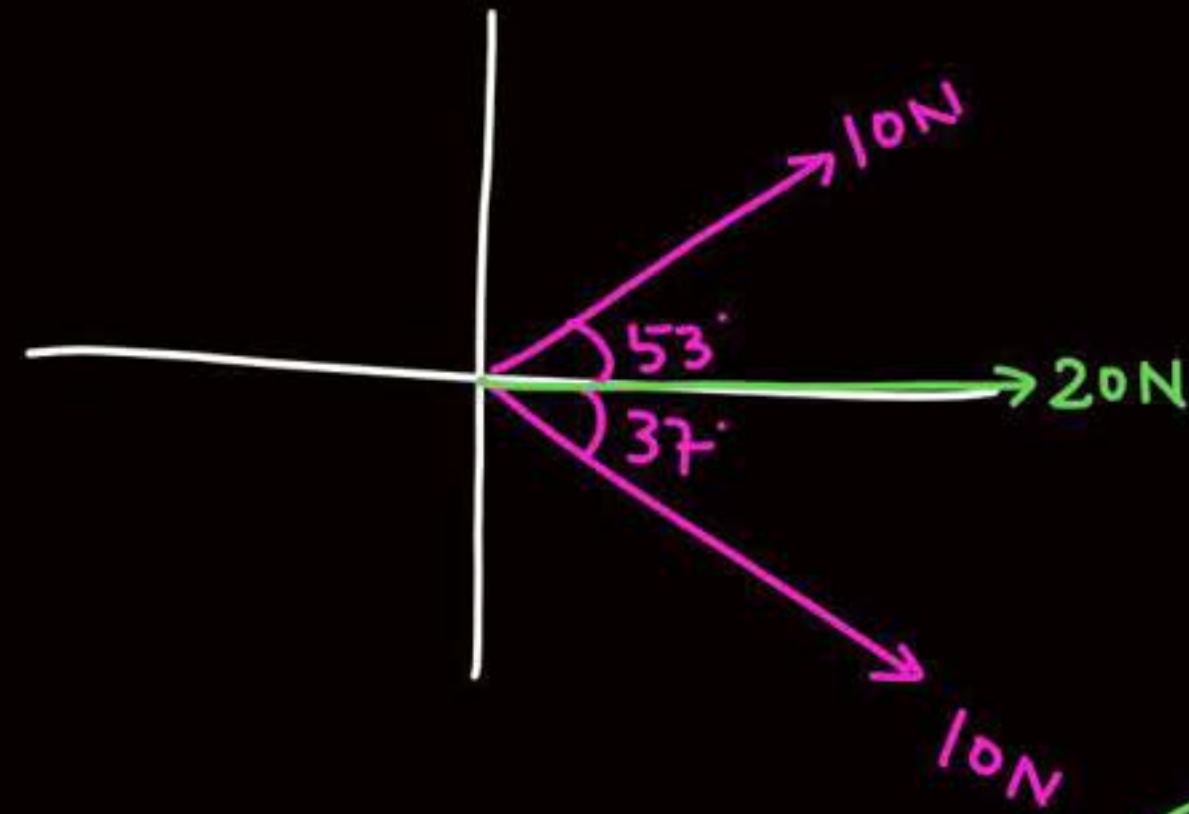
$\sin 37^\circ = \frac{3}{5} = \cos 53^\circ$
 $\cos 37^\circ = \frac{4}{5} = \sin 53^\circ$

Q Find net force

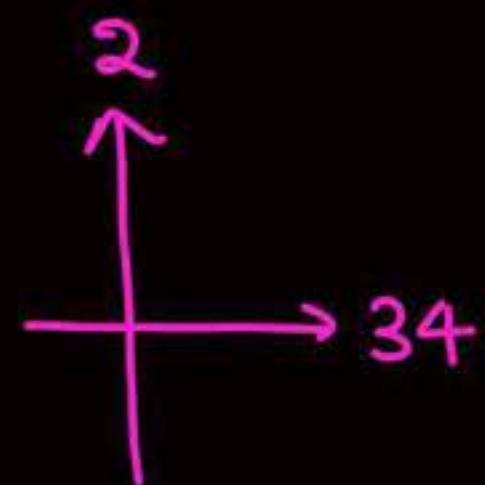


$$F_{\text{net}} = 38\hat{i} - 10\hat{j}$$

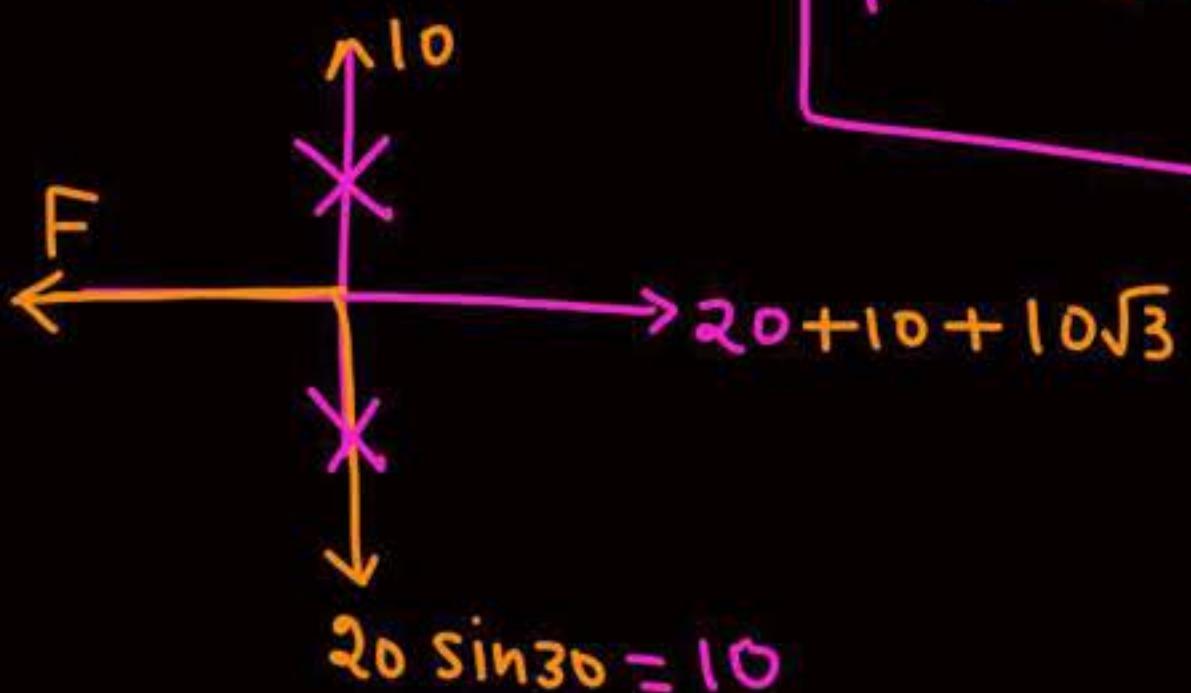
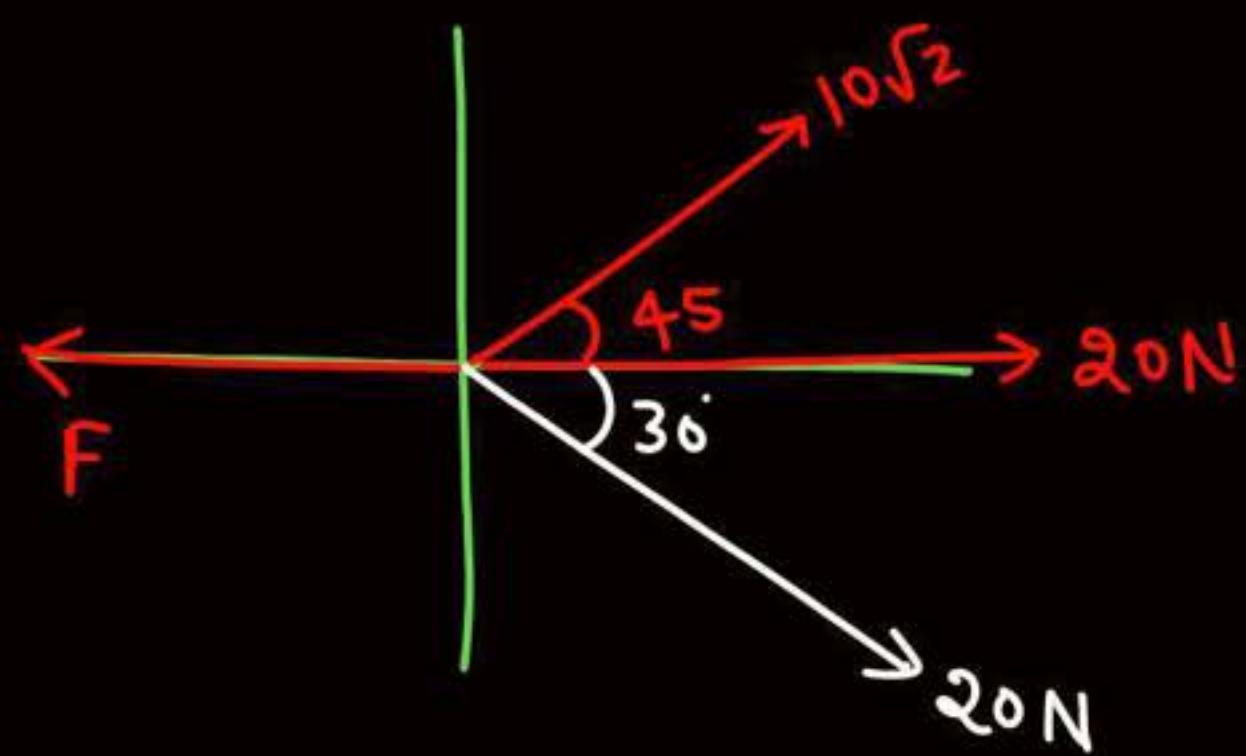
Q Find net force



$$\vec{F}_{\text{net}} = 34\hat{i} + 2\hat{j}$$



Q Find the value of F so that net force is zero.

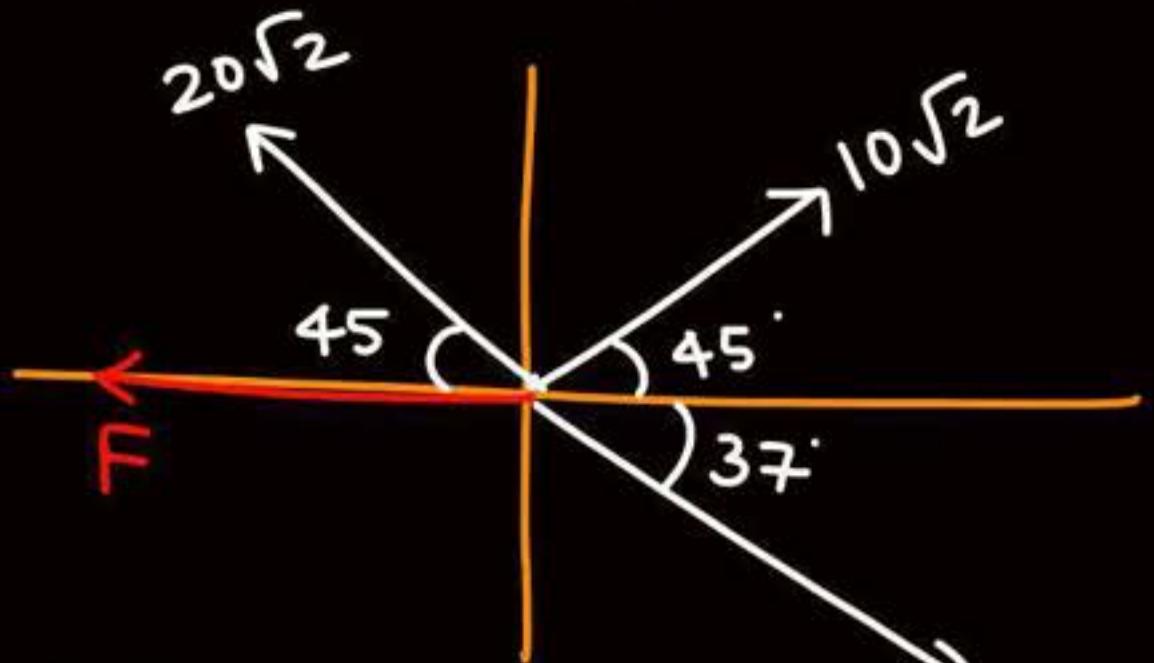


$$F = 30 + 10\sqrt{3}$$

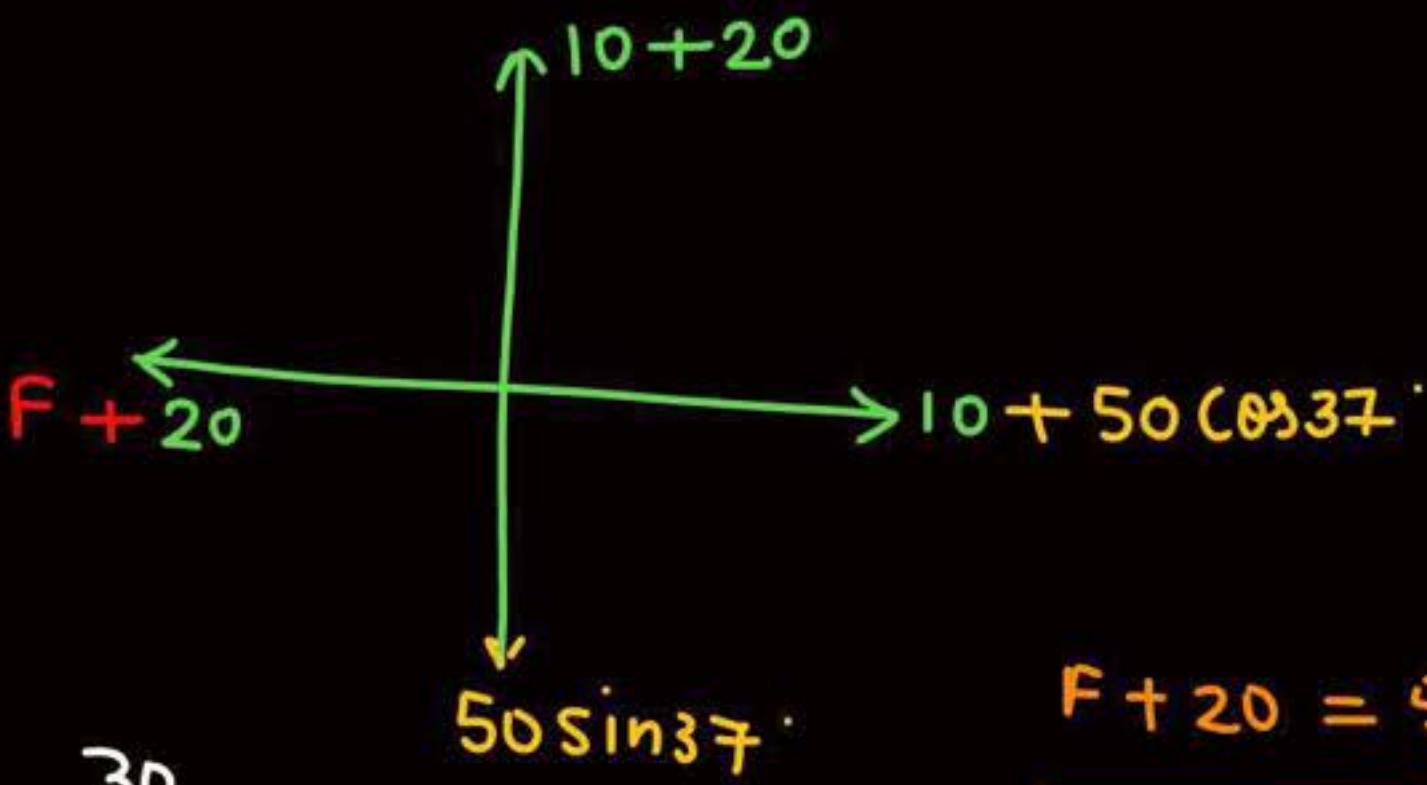
Ans

Q

Find value of F if $\vec{F}_{\text{net}} = 0$

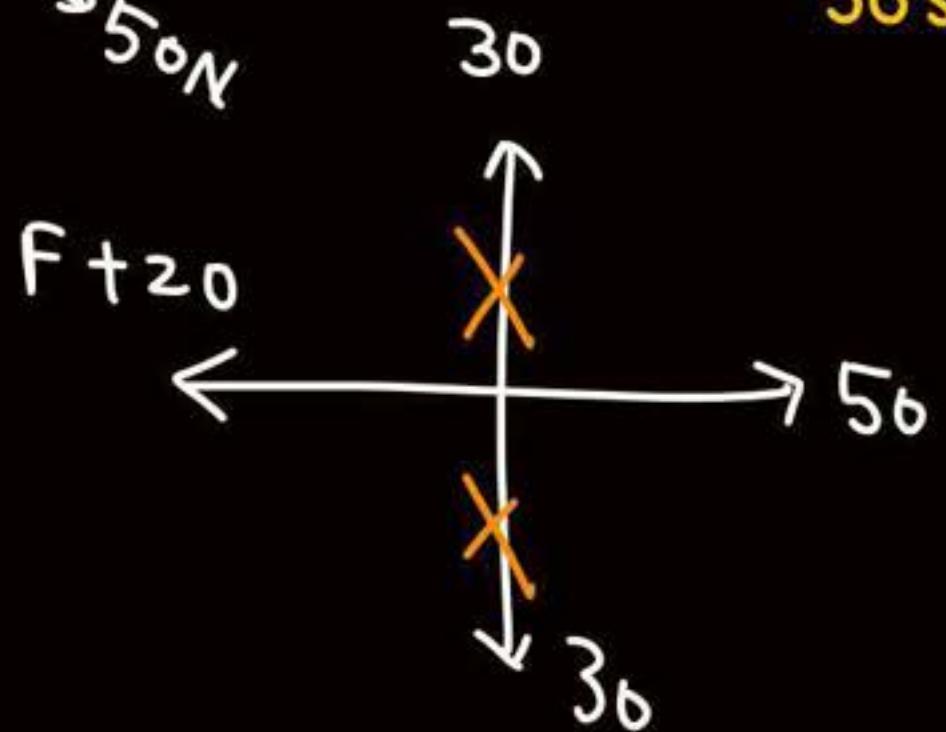


$$\boxed{\vec{F} = -30\hat{i}}$$



$$F+20 = 50$$

$$\boxed{F = 30}$$



①

$$\begin{aligned}\vec{A} &= 2\hat{i} + 3\hat{j} \\ \vec{B} &= 4\hat{i} + 5\hat{j} \\ \hline \vec{A} \cdot \vec{B} &= 8 + 15 = 23\end{aligned}$$

②

$$\begin{array}{r} \vec{A} = 5\hat{i} + 3\hat{j} \\ \vec{B} = 4\hat{i} + 10\hat{j} \\ \hline \vec{A} \cdot \vec{B} = 20 + 30 = 50 \end{array}$$

③

θ

$$\begin{aligned}\overrightarrow{A} &= 2\hat{i} + 3\hat{j} + 4\hat{k} \\ \overrightarrow{B} &= 3\hat{i} + 4\hat{j} + 5\hat{k}\end{aligned}$$

$$\begin{aligned}\overrightarrow{A} \cdot \overrightarrow{B} &= 6 + 12 + 20 \\ &= 38\end{aligned}$$

④

Ω

$$\begin{aligned}\overrightarrow{A} &= 3\hat{i} + 2\hat{j} + 3\hat{k} \\ \overrightarrow{B} &= 2\hat{i} + 3\hat{j} + 4\hat{k}\end{aligned}$$

$$\overrightarrow{A} \cdot \overrightarrow{B} = 6 + 6 + 12 = 24$$

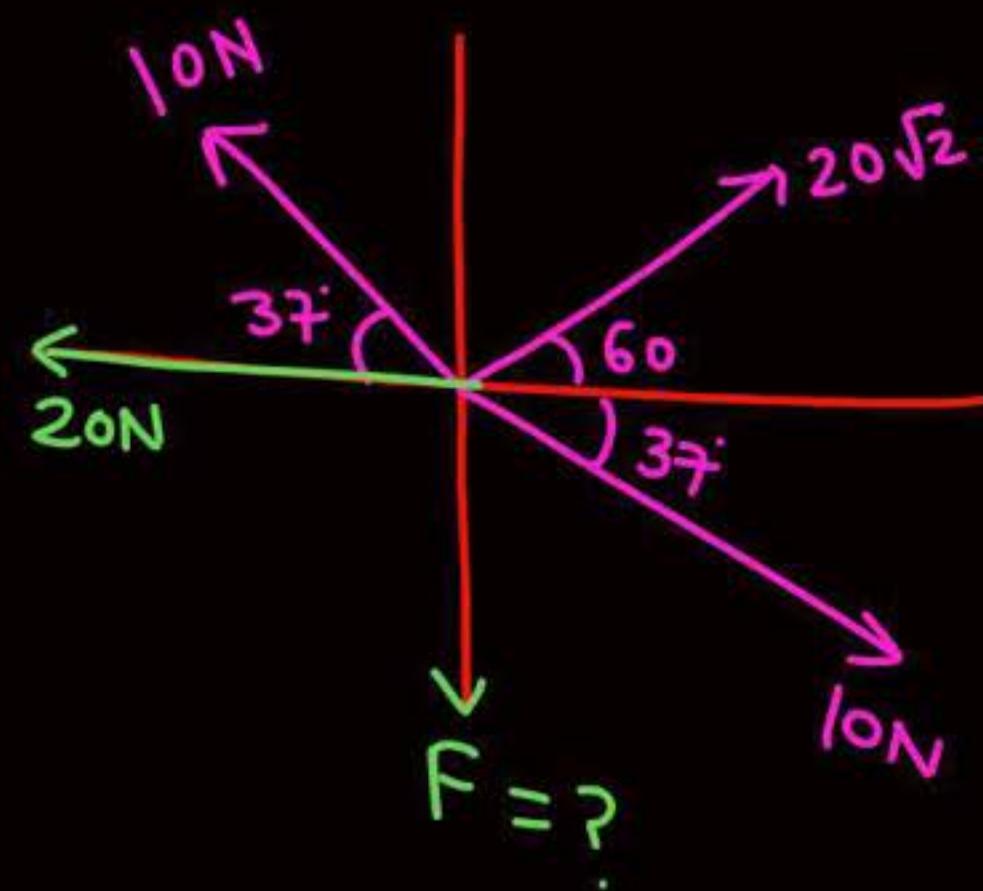
⑤

$$\begin{aligned}\overrightarrow{A} &= 2\hat{i} - 3\hat{j} \\ \overrightarrow{B} &= 5\hat{i} + 2\hat{j}\end{aligned}$$

$$\overrightarrow{A} \cdot \overrightarrow{B} = 10 - 6 = 4$$

Q

Find the value of F so that \vec{F}_{net} is zero



Ans $\rightarrow 20$

Q Find value of a & b so that $\vec{F}_{\text{net}} = 0$

$$\vec{F}_1 = a\hat{i} + 5\hat{j} + 3\hat{k}$$

$$\vec{F}_2 = (b-3)\hat{i} - b\hat{j} - 3\hat{k}$$

Sol'n next page
But पहले solve करो

Soln

$$\vec{F}_1 = a\hat{i} + 5\hat{j} + 3\hat{k}$$

$$\vec{F}_2 = (b-3)\hat{i} - b\hat{j} - 3\hat{k}$$

$$\vec{F}_{\text{net}} = \vec{F}_1 + \vec{F}_2 = (a+b-3)\hat{i} + (5-b)\hat{j} + (3-3)\hat{k}$$

$$\vec{F}_{\text{net}} = 0 \Rightarrow a+b-3=0, \quad 5-b=0$$
$$a+b=3 \quad b=5$$

$$b=5, \quad a+b=3$$

$$a+5=3$$

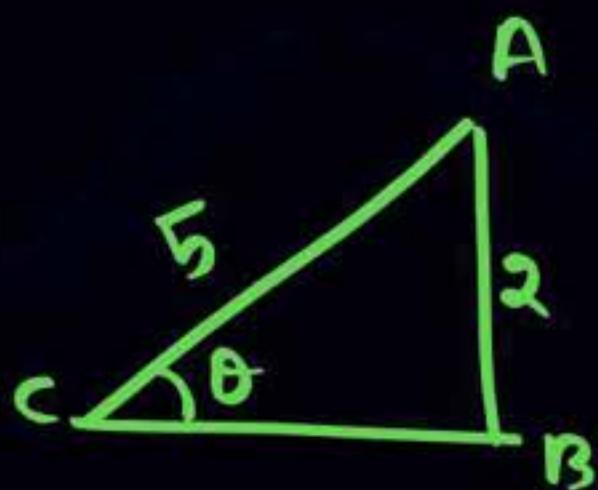
$$a=-2$$

Trigonometry

Q

$$\sin \theta = \frac{2}{5}$$

$$\tan \theta = \frac{2}{\sqrt{21}}$$



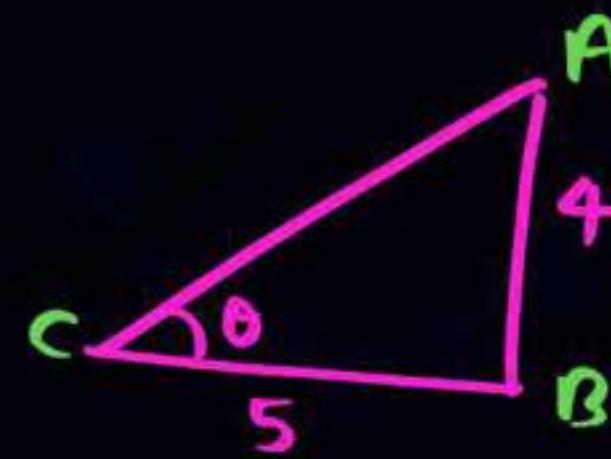
$$CB = \sqrt{25 - 4} = \sqrt{21}$$

Vector & Trigonometry

P
W

$$\tan \theta = \frac{4}{5}$$

~~$$\sin \theta = \frac{3}{5}$$~~



$$\sin \theta = \frac{AB}{AC} = \frac{4}{\sqrt{41}}$$

$$\begin{aligned}AC &= \sqrt{25 + 16} \\&= \sqrt{41}\end{aligned}$$

$$\cos 120^\circ = \cos(180^\circ - 60^\circ) = -\frac{1}{2}$$

$$\cos 150^\circ = \cos(180^\circ - 30^\circ) = -\frac{\sqrt{3}}{2}$$

$$\cos 210^\circ = \cos(180^\circ + 30^\circ) = -\frac{\sqrt{3}}{2}$$

$$\cos 240^\circ = \cos(180^\circ + 60^\circ) = -\frac{1}{2}$$

$$\sin 120^\circ = \sin(180^\circ - 60^\circ) = +\frac{\sqrt{3}}{2}$$

$$\sin 240^\circ = \sin(180^\circ + 60^\circ) = -\frac{\sqrt{3}}{2}$$

$$\sin 150^\circ = \sin(180^\circ - 30^\circ) = +\frac{1}{2}$$

$$\tan 150^\circ = \tan(180^\circ - 30^\circ) = -\frac{1}{\sqrt{3}}$$

$$\tan 210^\circ = \tan(180^\circ + 30^\circ) = +\frac{1}{\sqrt{3}}$$

$$\tan 300^\circ = \tan(360^\circ - 60^\circ) = -\sqrt{3}$$

$$\sin 300^\circ = \sin(360^\circ - 60^\circ) = -\frac{\sqrt{3}}{2}$$

$$\cos 300^\circ = \cos(360^\circ - 60^\circ) = +\frac{1}{2}$$

* * *

$$\cos 0^\circ = 1$$

$$\cos 180^\circ = -1$$

$$\sin 0^\circ = \sin 180^\circ = \sin 360^\circ = 0$$

$$\sin 270^\circ = \sin(180 + 90) = -1$$

$$\sin 270^\circ = -1$$

$$\cos 270^\circ = 0$$

* * *

$$\cos 0^\circ = 1$$

$$\cos 120^\circ = -\frac{1}{2}$$

$$\cos 150^\circ = -\frac{\sqrt{3}}{2}$$

$$\cos 135^\circ = -\frac{1}{\sqrt{2}}$$

$$\cos 180^\circ = -1$$

Homework

$\cos 330^\circ =$

$\cos 300^\circ =$

$\tan 240^\circ =$

$\tan 210^\circ =$

$\sin 210^\circ =$

$$\sin 135^\circ =$$

$$\cos 150^\circ =$$

$$\cos 180^\circ =$$

$$\sin 180^\circ =$$

$$\tan 180^\circ =$$

$$\tan 0^\circ =$$

$$\sin 150^\circ =$$

$$\sin 127^\circ =$$

$$\cos 127^\circ =$$

$$\sin 143^\circ =$$

$$\cos 143^\circ =$$

$$\tan 143^\circ =$$

$$\sin 217^\circ =$$

$$\cos 217^\circ =$$

$$\tan 217^\circ =$$

Basic maths =

① — ये physics का chapter नहीं हैं

- * ② * यहाँ 11th maths के only के topic पढ़ो / Revise
जिनकी जरूरत हो। 11th class की phy. से पड़ने
वाली हैं
- ③ ये हाले maths हैं... detail में पढ़ो। तो 1 साल की
कम है

Conversion of rad into degree.

① $\frac{\pi}{2}$ rad. $\xrightarrow[\text{into degree}]{\text{Convert}}$ $\frac{180}{2} = 90^\circ$

② $\frac{\pi}{3}$ rad. $\xrightarrow[""]$ $\frac{180}{3} = 60^\circ$

③ $\frac{\pi}{6}$ rad. $\xrightarrow{} \frac{180}{6} = 30^\circ$

π की खण्ड
180° रख दे

④ $\frac{2\pi}{3}$ rad $\xrightarrow[\text{degree}]{\text{Convert into}} \frac{2 \times 180}{3} = 120^\circ$

⑤ $\frac{5\pi}{6}$ rad $\xrightarrow[\text{"}]{\text{"}} \frac{5 \times 180}{6} = 150^\circ$

⑥ 2π rad. $\xrightarrow[\text{"}]{\text{"}} 2 \times 180 = 360^\circ$

⑦ $\frac{2\pi}{3}$ rad $\xrightarrow[\text{"}]{\text{"}} \frac{2 \times 180}{3} = 120^\circ$

⑧ $\frac{7\pi}{6}$ rad $\xrightarrow[\text{"}]{\text{"}} 210^\circ$

Conversion of degree into radian

$$90^\circ \xrightarrow[\text{radian}]{\text{Convert into}} 90 \times \frac{\pi}{180} = \frac{\pi}{2} \text{ rad}$$

$$60^\circ \xrightarrow[""]{} 60 \times \frac{\pi}{180} = \frac{\pi}{3} \text{ rad}$$

$$45^\circ \xrightarrow{} 45 \times \frac{\pi}{180} = \frac{\pi}{4} \text{ rad}$$

$\frac{\pi}{180}$ से multiply कर दो

$$\pi \text{ rad} \equiv 180^\circ$$

$$1^\circ = \frac{\pi}{180} \text{ rad.}$$

**

rad

$$2^\circ \longrightarrow \frac{2\pi}{180} = \frac{\pi}{90}$$

$$4^\circ \longrightarrow \frac{\pi}{45}$$

$$3^\circ \longrightarrow \frac{3\pi}{180} = \frac{\pi}{60}$$

$$5^\circ \longrightarrow \frac{5\pi}{180} = \frac{\pi}{36}$$

Convert into
radian

 120°

$$\frac{120\pi}{180} = \frac{2\pi}{3} \text{ rad}$$

 240°

$$\frac{4\pi}{3} \text{ rad}$$

 210°

$$\frac{210\pi}{180} = \frac{7\pi}{6} \text{ rad}$$

 720°

$$4\pi \text{ rad}$$

 750°

$$\frac{750\pi}{180} = \frac{25\pi}{6} \text{ rad}$$

 150°

$$\frac{5\pi}{6} \text{ rad}$$

$$\textcircled{1} \quad \sin 2^\circ \approx 2 \times \frac{\pi}{180} \approx \frac{\pi}{90} = \frac{3.14}{90} \approx .03488$$

$$\textcircled{2} \quad \sin 3^\circ \approx 3 \frac{\pi}{180} = \frac{\pi}{60} = \frac{3.14}{60}$$

$$\textcircled{3} \quad \sin 4^\circ \approx 4 \frac{\pi}{180} = \frac{\pi}{45}$$

$$\textcircled{4} \quad \sin 8^\circ \approx \frac{8\pi}{180}$$

Small angle approximation

P
W

* $\sin \theta \approx \theta$

($\theta < 10^\circ$ Best)

* $\tan \theta \approx \theta$ ($\theta < 10^\circ$ Best)

* $\sin \theta \approx \tan \theta \approx \theta$ (if θ is very small)
 $\theta < 10^\circ$ Best

① $\tan 8^\circ = \frac{8\pi}{180}$

② $\sin 8^\circ = \frac{8\pi}{180}$

③ $\sin 10^\circ = \frac{10\pi}{180}$

④ $\tan 5^\circ = \frac{5\pi}{180}$

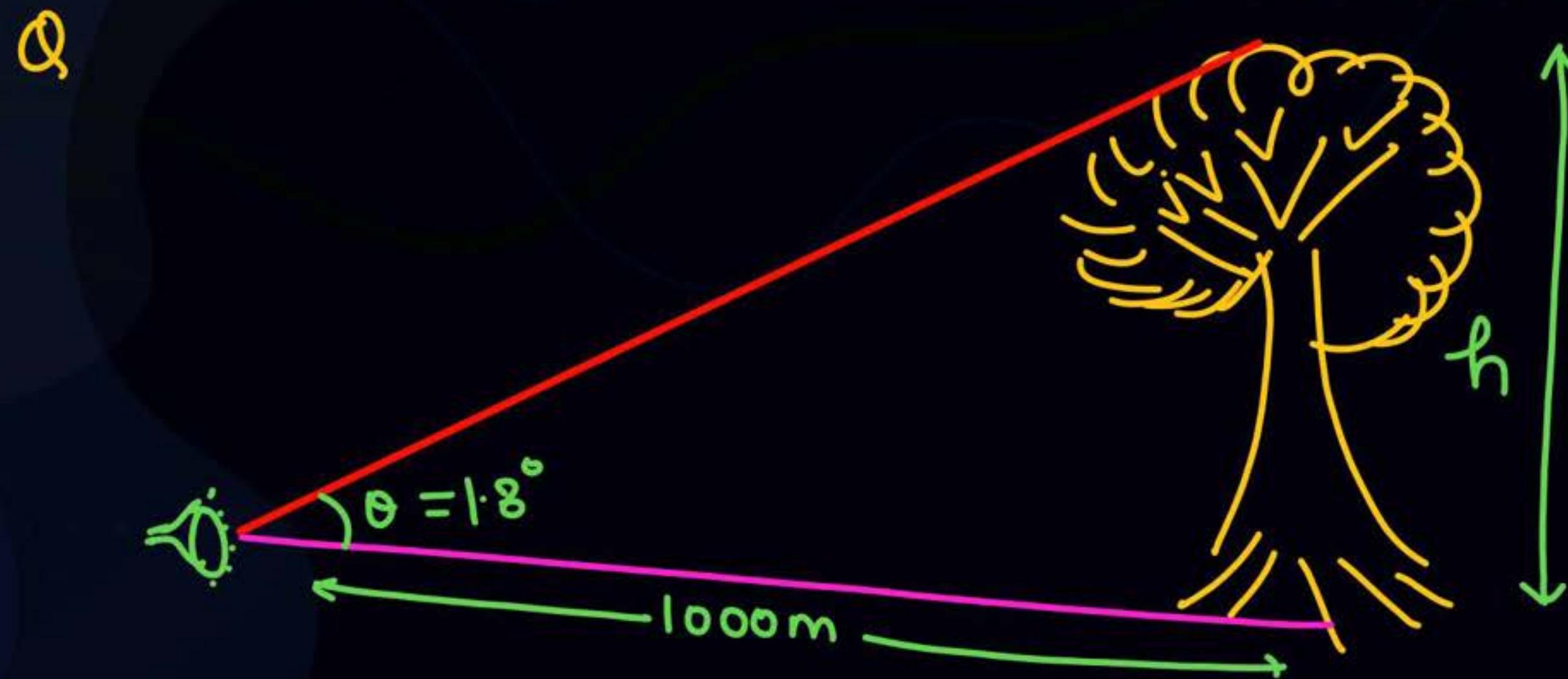
$\sin 2^\circ \approx \tan 2^\circ$

$\sin 5^\circ \approx \tan 5^\circ$

if θ is very small

$\theta < 5^\circ$

$\cos \theta \rightarrow 1$



$$\tan 1.8^\circ = \frac{h}{1000}$$

$$\begin{aligned} h &= 1000 \cdot \tan 1.8^\circ = 1000 \times 1.8 \times \frac{\pi}{180} \\ &= 10\pi = \underline{31.4} \text{ m} \end{aligned}$$

$$\sin 2^\circ \approx \underline{.0348}^{99} \text{ (calc)}$$

$$\tan 2^\circ \approx \underline{.0349}$$

$$\sin 2^\circ \approx 2 \cdot \frac{\pi}{180} = \frac{\pi}{90} = \frac{3.14}{90} = .0348$$

$(\sin \theta \approx \theta)$

$$\sin 5^\circ \approx .0871$$

$$\tan 5^\circ = .0874$$

|||
Approx equal

$$\sin \theta \approx \theta \text{ rad}$$

$$\sin 2^\circ \approx 2 \cdot \frac{\pi}{180} = \frac{\pi}{90} = \frac{3.14}{90} = \underline{\underline{0.03488}}$$

$$\sin 3^\circ \approx 3 \cdot \frac{\pi}{180} = \frac{\pi}{60} = \frac{3.14}{60} = 0.0523$$

- * $\pi \text{ rad} = 180^\circ$
- * $1^\circ = 60' \text{ (minute)}$

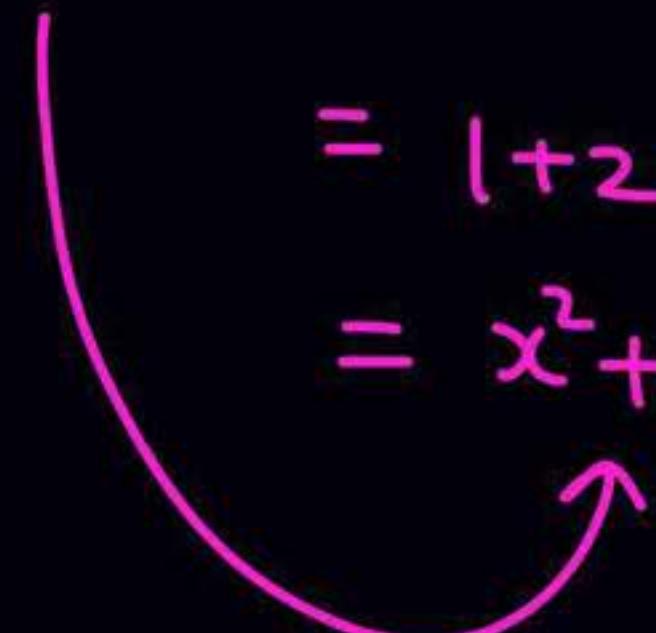
Binomial Expansion

अभी
हमारे काम का तरीका

$$(1+x)^n = 1 + nx + \frac{n(n-1)x^2}{1 \times 2} + \frac{n(n-1)(n-2)x^3}{1 \times 2 \times 3} + \dots$$

$n=2$ put

$$\begin{aligned}(1+x)^2 &= 1 + 2x + \frac{2 \cdot 1 \cdot x^2}{1 \cdot 2} + \dots \\ &= 1 + 2x + x^2 \\ &= x^2 + 1 + 2x\end{aligned}$$



$$(1+x)^n = 1 + nx + \dots$$

$$\frac{n(n-1)x^2}{1 \times 2} + \dots$$

Neglect it

* If $x \ll 1$

$$(1+x)^n \approx 1+nx$$

Q. $(1.0003)^5 = (1 + 0.0003)^5$

$$= 1 + 5 \times 0.0003$$

$$= \underline{1.0015}$$

$$\text{Q} \quad (1.004)^2 \approx (1 + 0.004)^2 = 1.008$$

$$\text{Q} \quad (1.006)^3 \approx 1.018$$

$\boxed{\text{Calc} \approx 1.01810}$

$$\text{Q} \quad (1.007)^4 \approx \underline{1.028}$$

$\boxed{\text{Approximat.}}$

$$\text{Q} \quad \sqrt{1.008} \\ = (1 + 0.008)^{\frac{1}{2}}$$

$$= \left(1 + \frac{1}{2} \times 0.008\right)$$

$$= \frac{1.004}{\text{.}}$$

$$\text{Q} \quad \sqrt{1.00} \approx 1.003$$

Revision

$$\textcircled{1} \quad \frac{3\pi}{2} \longrightarrow \frac{3 \times 180}{2} = 270^\circ$$

θ is very small
 $\cos \theta \longrightarrow 1$

$$\textcircled{2} \quad 210^\circ \longrightarrow 210 \times \frac{\pi}{180} = \frac{7\pi}{6}$$

$$\begin{aligned} \textcircled{3} \quad \sin \theta &\approx \theta \\ \tan \theta &\approx \theta \\ \sin \theta \approx \theta &= \tan \theta \end{aligned} \quad \left. \begin{array}{l} \vdots \\ \theta < 10^\circ \\ \text{Best} \end{array} \right\} \checkmark$$

$$(1+x)^n \approx 1+nx \quad \boxed{\text{If } x \ll 1}$$

$$(1-x)^n = 1-nx \quad (\text{if } x \ll 1)$$

Q $(1 + 0.003)^4 \approx 1 + 4 \times 0.003 = \underline{1.012}$.

 calc 1.01205

$$(1 + 0.003)^{-3} = 1 + (-3)x 0.003 = 1 - 3 \times 0.003 = 1 - 0.009 = 0.991$$

$$(1 + 0.004)^{-2} = 1 - 0.008 = 0.992$$

$$(1 - 0.007)^2 = 1 - 0.014 = 0.986$$

$$(1 - 0.002)^3 = 1 - 3 \times 0.002 = 1 - 0.006 = 0.994$$

$$(0.996)^3 = (1 - 0.004)^3 = 1 - 0.012 = \underline{0.988}$$

$$(1 \pm x)^n = 1 \pm nx$$

if $x \ll 1$

$$(1.007)^3 = 1.021$$

$$(1.009)^{\frac{1}{3}} = 1 + \frac{1}{3} \times 0.009 = 1.003$$

$$(1.008)^{\frac{1}{2}} = (1+0.008)^{\frac{1}{2}} = 1.004$$

$$\sqrt{1.006} = (1+0.006)^{\frac{1}{2}} = 1 + \frac{1}{2} \times 0.006 = \underline{1.003}$$

$$\frac{1}{1.006} = (1.006)^{-1} = (1+0.006)^{-1} = 1 - 0.006 = 0.994$$

$$\frac{1}{0.998} = (0.998)^{-1} = (-0.002)^{-1} = 1 + 0.002 = 1.002$$

$$\left(\frac{1}{0.997}\right)^2 = (0.997)^{-2} = (1-0.003)^{-2}$$

$$= 1 + 0.006 = \underline{\underline{1.006}}$$

find

$$\tan 4^\circ = \frac{4 \cdot \pi}{180}$$

$$\tan 5^\circ = \frac{5 \cdot \pi}{180} \quad \checkmark$$

$$\tan 8^\circ = \frac{8 \cdot \pi}{180} \quad \checkmark$$

S.K.C

$$\boxed{\begin{array}{l} \pi = 180^\circ \quad \times \\ \pi \text{ rad} = 180^\circ \\ \pi = \frac{22}{7} = 3.14 \end{array}}$$

$$\sin 120^\circ = \sin(180^\circ - 60^\circ) = +\frac{\sqrt{3}}{2}$$

मारा ✓
उसे follow करेंगे.

$$\sin(90^\circ + 30^\circ) = +\cos 30^\circ = +\frac{\sqrt{3}}{2} = \text{दूर रही}$$

$90^\circ, 270^\circ$ में तोड़े
तो

$$\sin \rightleftharpoons \cos$$

$$\tan \rightleftharpoons \cot$$

$180^\circ, 360^\circ$ में
तोड़ रहे हो तो
मत change करी

① $\sin 150^\circ = \sin(180^\circ - 30^\circ) = +\sin 30^\circ = +\frac{1}{2}$

↳ $\sin(90^\circ + 60^\circ) = +\cos 60^\circ = +\frac{1}{2}$

② $\sin 210^\circ = \sin(180^\circ + 30^\circ) = -\sin 30^\circ = -\frac{1}{2}$

↳ $\sin(270^\circ - 60^\circ) = -\cos 60^\circ = -\frac{1}{2}$

$$\textcircled{3} \quad \sin 240^\circ = \sin(180^\circ + 60^\circ) = -\sin 60^\circ = -\frac{\sqrt{3}}{2}$$

$$\hookrightarrow \sin(270^\circ - 30^\circ) = -\cos 30^\circ = -\frac{\sqrt{3}}{2}$$

$$\textcircled{4} \quad \cos 240^\circ = \cos(180^\circ + 60^\circ) = -\cos 60^\circ = -\frac{1}{2}$$

$$\hookrightarrow \cos(270^\circ - 30^\circ) = -\sin 30^\circ = -\frac{1}{2}$$

$$\textcircled{3} \quad \tan 240^\circ = \tan(180^\circ + 60^\circ) = +\tan 60^\circ = \sqrt{3}$$

$$\hookrightarrow \tan(270^\circ - 30^\circ) = +\cot 30^\circ = \sqrt{3}$$

$$\textcircled{4} \quad \cos 300^\circ = \cos(360^\circ - 60^\circ) = +\cos 60^\circ = \frac{1}{2}$$

$$\hookrightarrow \cos(270^\circ + 30^\circ) = +\sin 30^\circ = \frac{1}{2}$$

$$\textcircled{5} \quad \sin 300^\circ = \sin(360^\circ - 60^\circ) = -\frac{\sqrt{3}}{2}$$

$$\hookrightarrow \sin(270^\circ + 30^\circ) = -\cos 30^\circ = -\frac{\sqrt{3}}{2}$$

$\sin(90^\circ - \theta) = \cos \theta$
 $\cos(90^\circ - \theta) = \sin \theta$
 $\tan(90^\circ - \theta) = \cot \theta$
 $\cot(90^\circ - \theta) = \tan \theta$

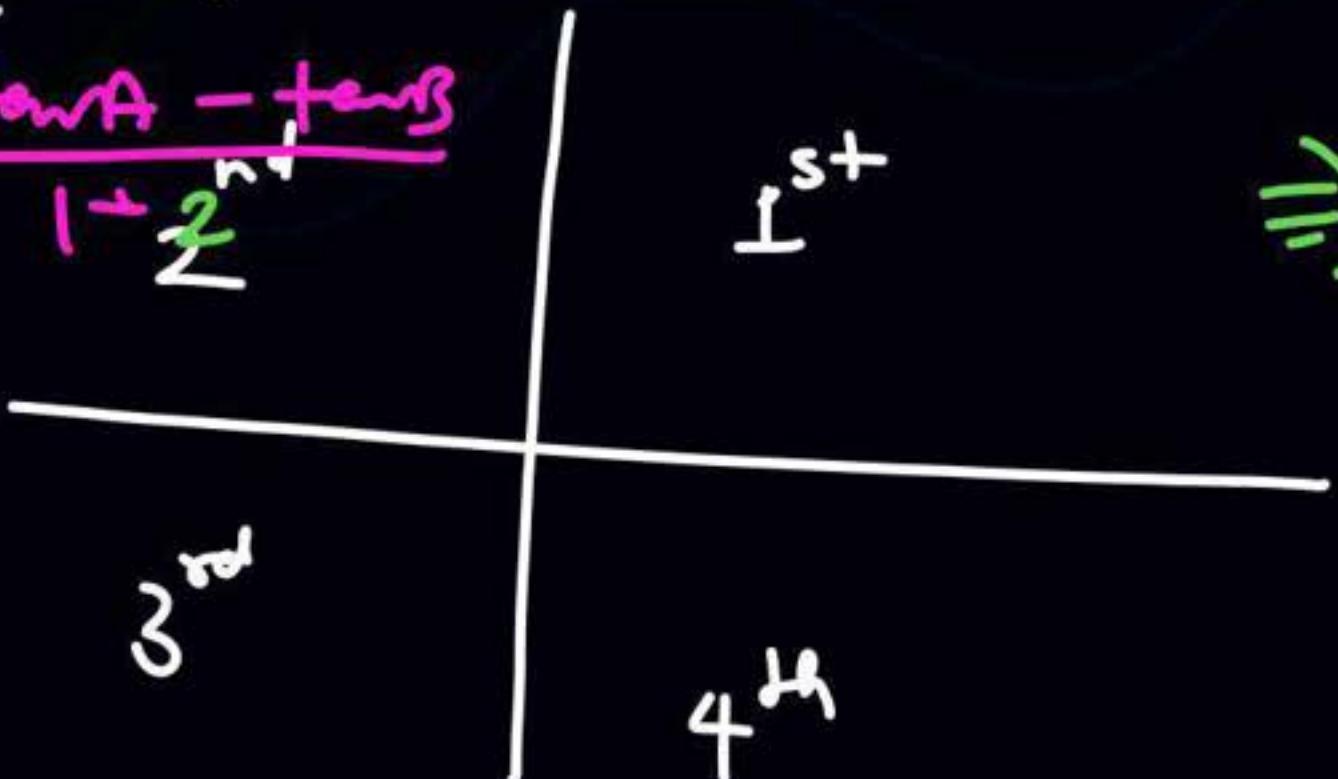
10th class

$$\tan 15^\circ = \tan(45^\circ - 30^\circ)$$

$$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

$$\tan 45^\circ = 1^0$$

Sign



$$\Rightarrow \text{Bild } \varepsilon \uparrow$$

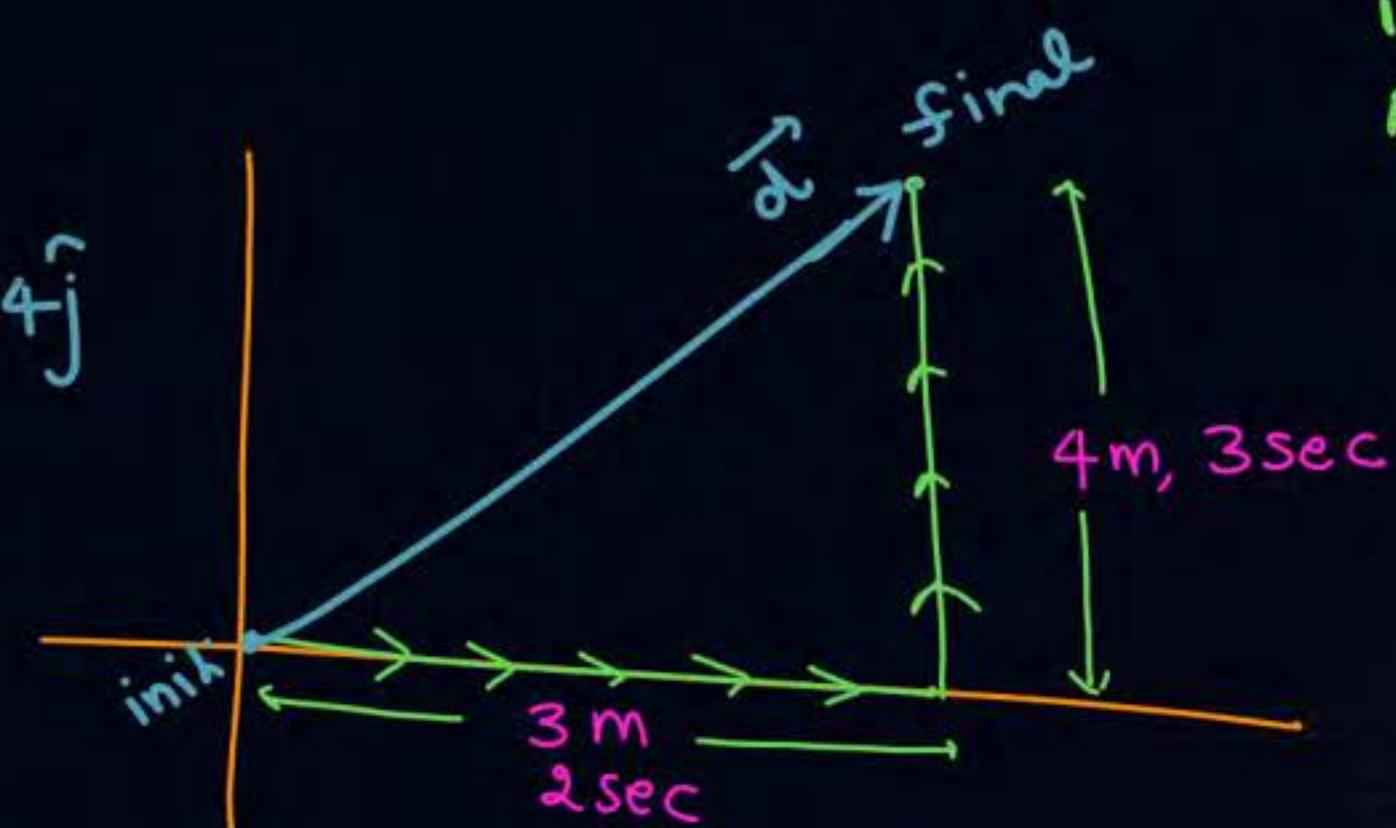
Q2

$$\text{Displacement} = \vec{d} = 3\hat{i} + 4\hat{j}$$

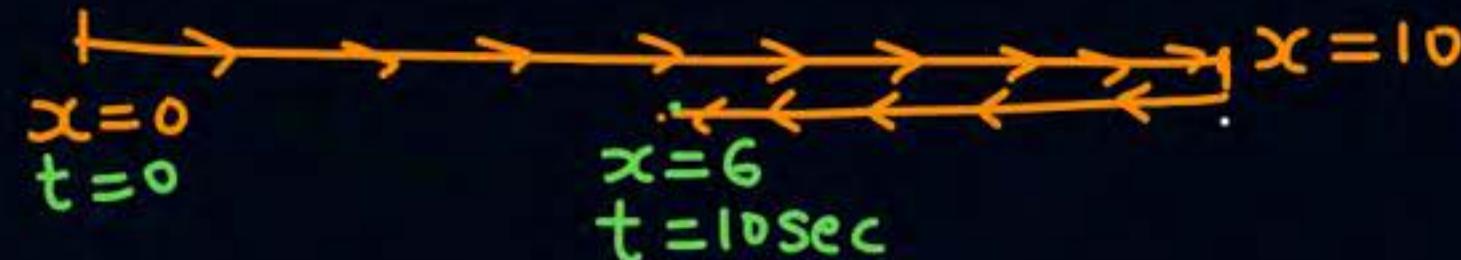
$$\begin{aligned}\text{Average Velocity} &= \frac{3\hat{i} + 4\hat{j}}{2+3} \\ &= \frac{3\hat{i} + 4\hat{j}}{5}\end{aligned}$$

magnitude \Rightarrow Displacement = 5
 time = $2+3=5 \text{ sec}$

$$\text{Avrg velocity} = \frac{5}{5} = 1 \text{ m/s}$$



if displacement = 0
 Avg velocity = 0

Q₁

$$\text{Displacement} = 6$$

$$\text{Avg Velocity} = \frac{6}{10}$$

$$\text{Distance} = 10 + 4 \\ = 14$$

$$\text{Avg speed} = \frac{14}{10}$$

Q₂

$$\text{distance} = 10$$

$$\text{displacement} = 10 \text{ (magnitude)}$$

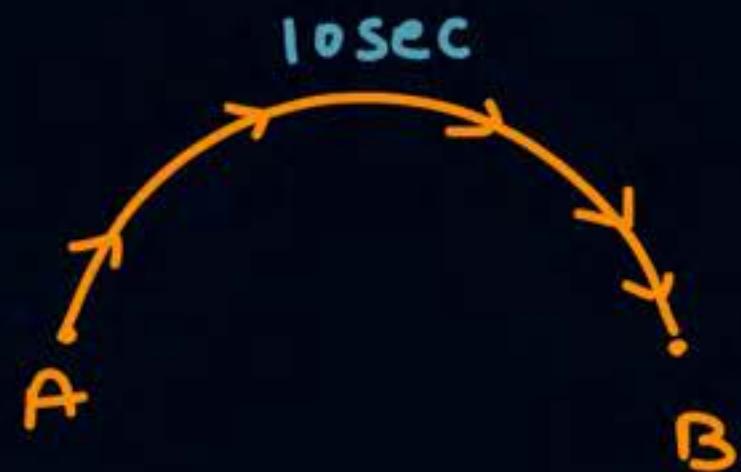
$$\text{Avg velocity} = \frac{10}{5} \text{ (magnitude)}$$

$$\text{Avg speed} = \frac{10}{5}$$

Q

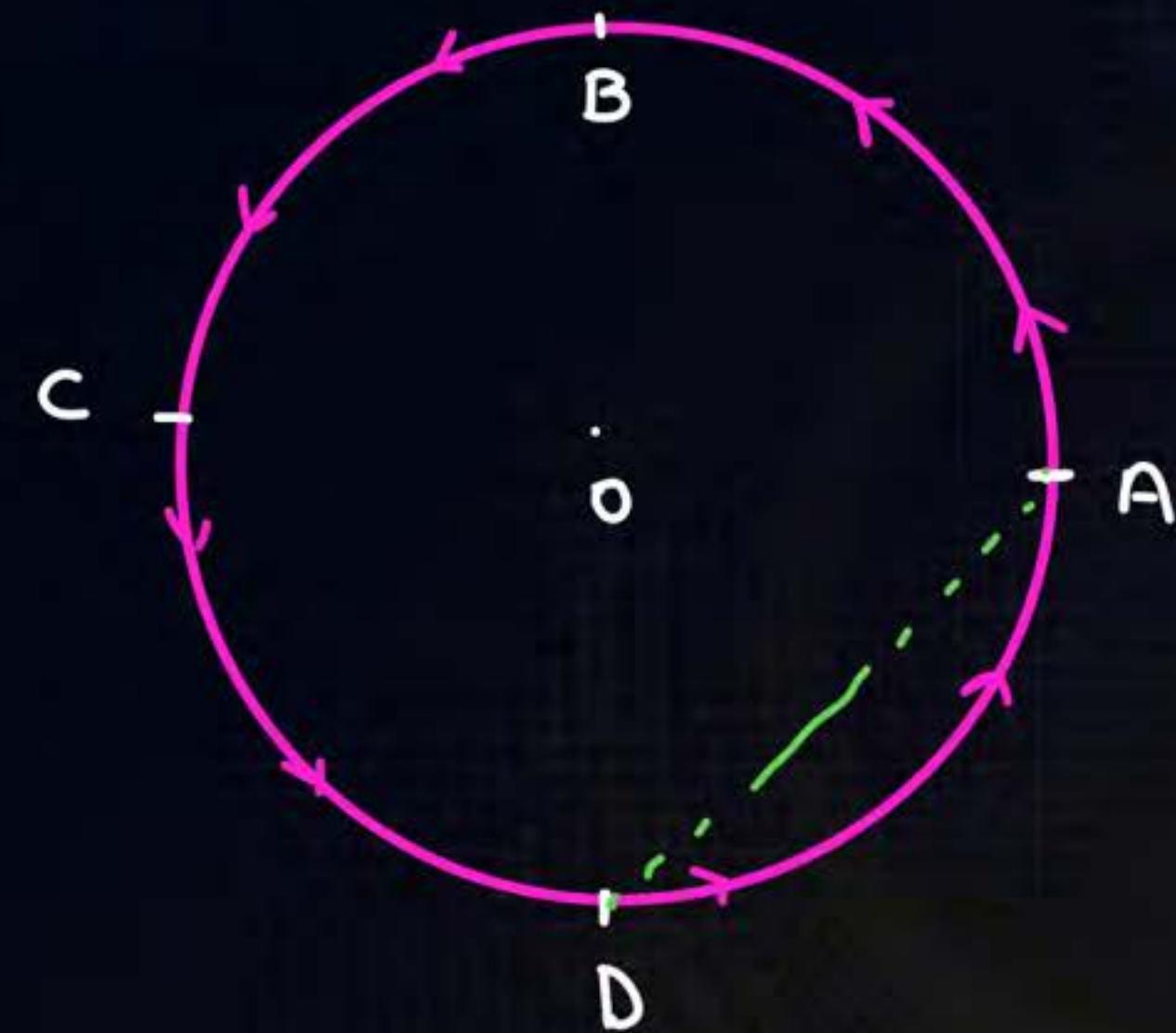
$$\text{Avg. Speed} = \frac{\pi R}{10}$$

$$\text{Avg Velocity (magnitude)} = \frac{2R}{10} = \frac{R}{5}$$



Q A particle is performing Uniform circular motion with
const speed v , having time period T anticlockwise.

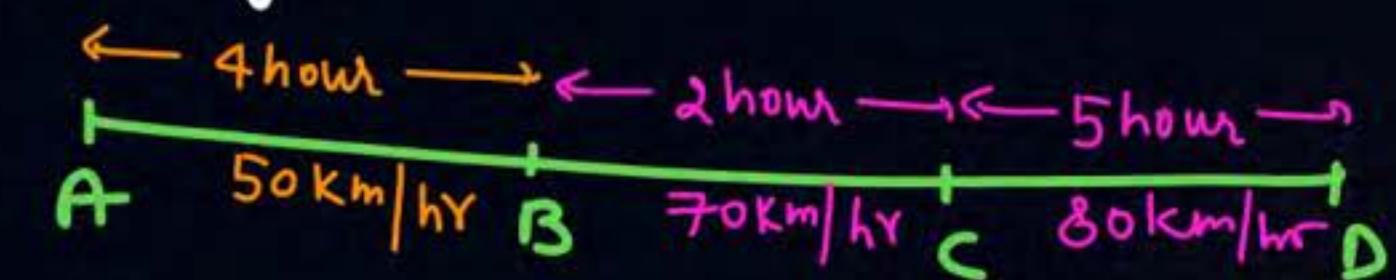
	Avg Speed	Avg velocity
$A \rightarrow B$	$\frac{2\pi R/4}{T/4} = \frac{2\pi R}{T}$	$\frac{R\sqrt{2}}{T/4}$
$A \rightarrow B \rightarrow C$	$\frac{\pi R}{T/2} = \frac{2\pi R}{T}$	$\frac{2R}{T/2}$
$A \rightarrow B \rightarrow C \rightarrow D$	$\frac{\frac{3}{4}2\pi R}{3T/4} = \frac{2\pi R}{T}$	$\frac{R\sqrt{2}}{3T/4}$
$A \rightarrow B \rightarrow C \rightarrow D \rightarrow A$	$\frac{2\pi R}{T}$	O



9th class

P
W

Q A car is moving along $+x$ axis, in 1st four hour it travel with speed 50 km/hr, in next 2 hour it move with 70 km/hr and in last part of journey it travel for 5 hour with 80 km/hr find Avg speed.



$$\text{Avg Speed} = \frac{50 \times 4 + 70 \times 2 + 80 \times 5}{4 + 2 + 5} = \frac{200 + 140 + 400}{11} = \checkmark$$

$$\text{Avg velocity} = \frac{\Delta \vec{x}}{\Delta t} = \frac{\vec{x}_f - \vec{x}_i}{\Delta t}$$

time interval.

1D motion



If a particle is moving on x-axis only

$$\text{Avg Velocity} = \frac{\vec{x}_f - \vec{x}_i}{\text{time}} = \frac{\Delta \vec{x}}{\Delta t}$$

Q A particle is moving on the x-axis. St its x-co-ordinate w.r.t time changes as

$$\textcircled{1} \quad t=0 \longrightarrow t=2 \text{ sec}$$

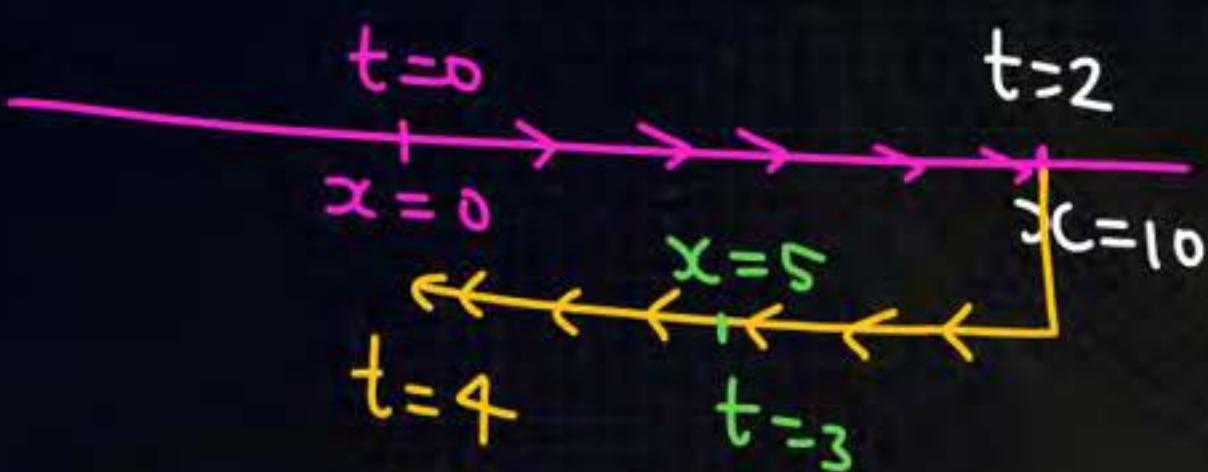
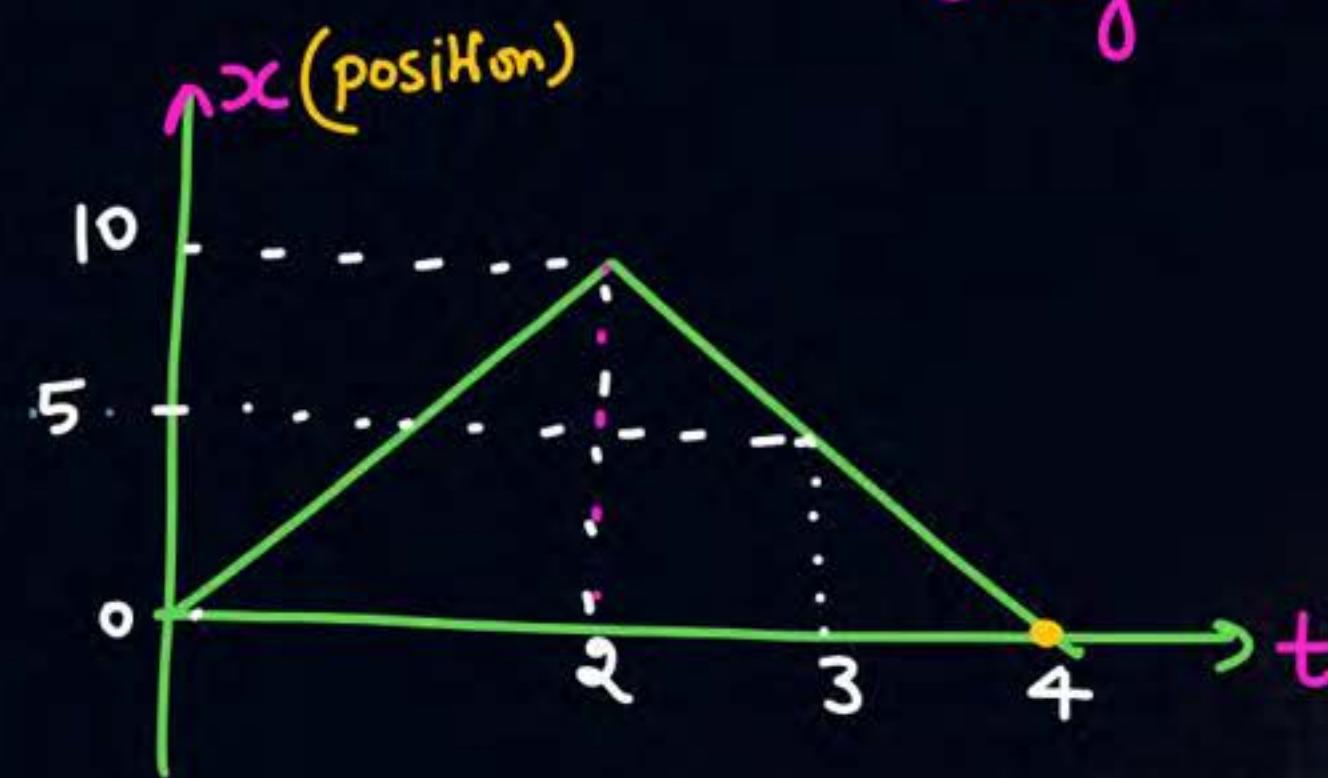
$$\text{Avg velocity} = \frac{10}{2} = 5$$

$$\text{Avg velocity} = \frac{x_f - x_i}{\text{time}} = \frac{10 - 0}{2}$$

$$\textcircled{2} \quad t=0 \longrightarrow t=3$$

$$\text{Avg Velocity} = \frac{x_f - x_i}{\text{time}} = \frac{5 - 0}{3}$$

$$\text{Avg Speed} = \frac{15}{3} = 5$$

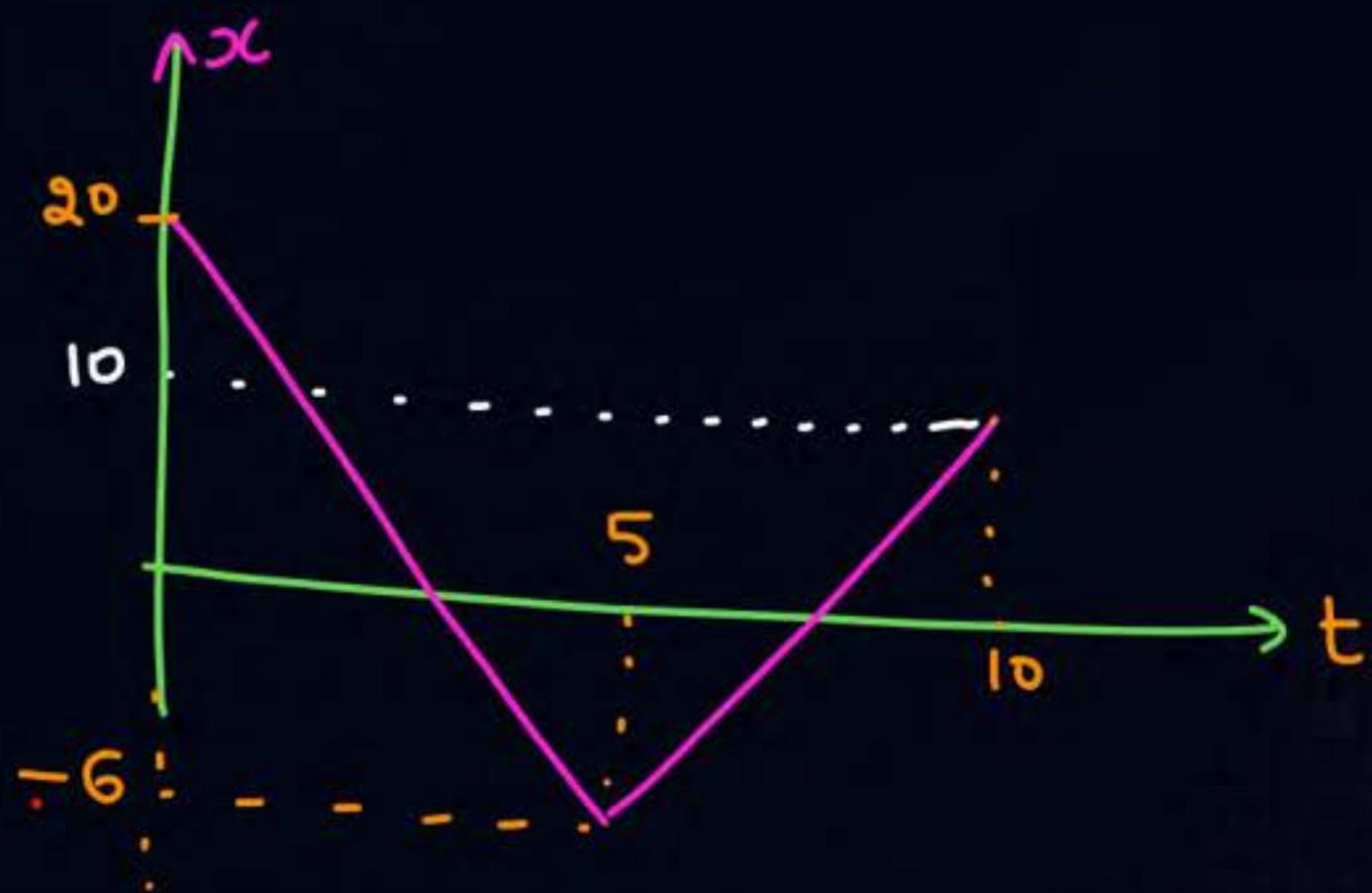


Q $t=0 \rightarrow t = 5$

$$\text{Avg velocity} = \frac{x_f - x_i}{\text{time}}$$
$$= \frac{(-6) - (+20)}{5}$$
$$= -\frac{26}{5}$$

Q2 $t=0 \rightarrow t = 10$

$$\text{Avg velocity} = \frac{10 - 20}{10}$$



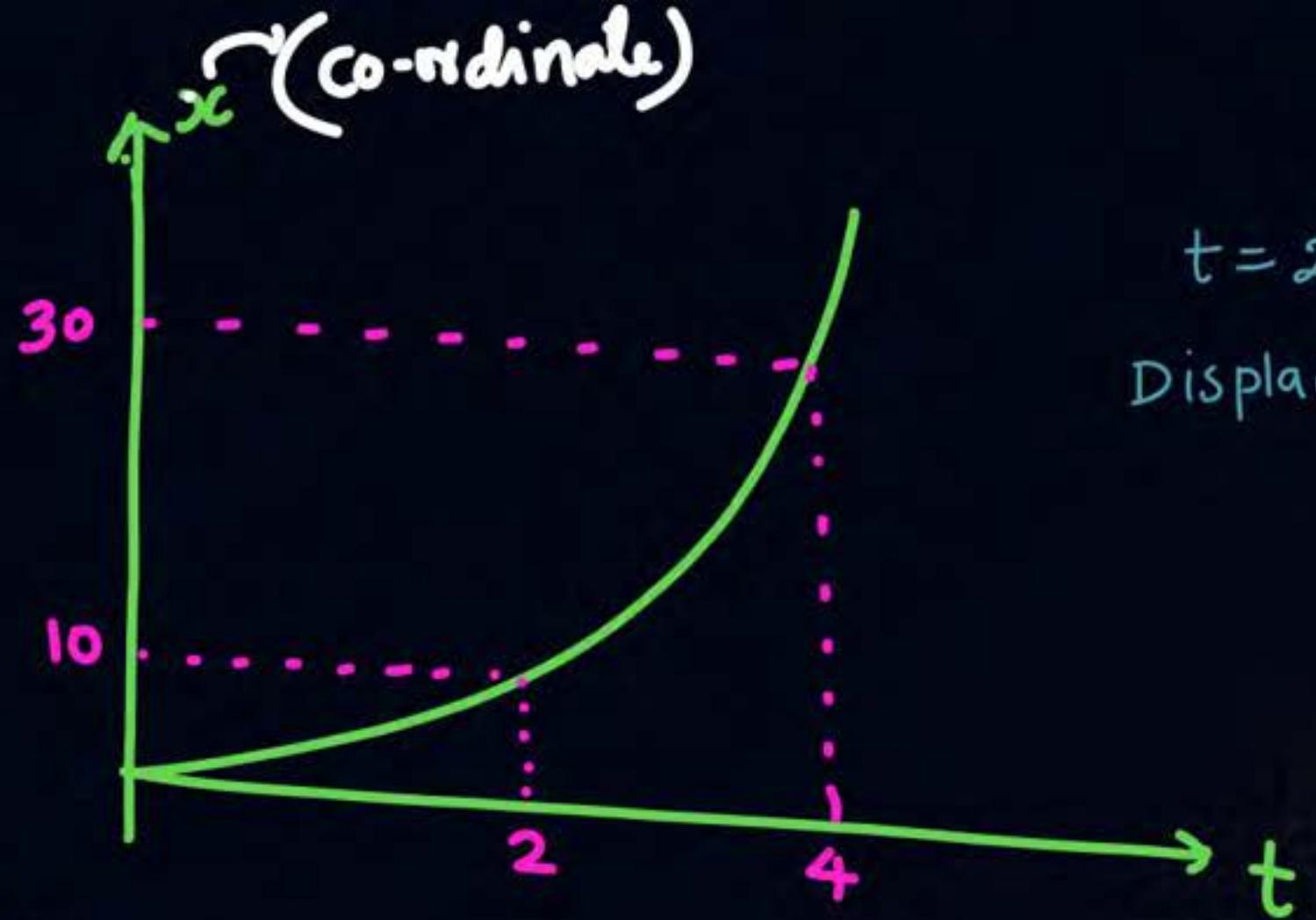
Q

find average velocity from

$t = 2 \rightarrow t = 4 \text{ sec}$

Avg velocity = $\frac{x_f - x_i}{\text{total time}}$

$$= \frac{30 - 10}{4 - 2} = \frac{20}{2} = 10$$



$$t = 2 \rightarrow t = 4$$

$$\text{Displacement} = 20$$

$$= 30 - 10 = 20$$



thank you



Q

initial

$$(2, 3, 4)$$

final

$$(7, 5, 9)$$

$$\vec{d} = \text{displacement} = \vec{r}_f - \vec{r}_i = 5\hat{i} + 2\hat{j} + 5\hat{k}$$

Q

final

$$(-5, 0, 0)$$

initial

$$(0, 0, 0)$$

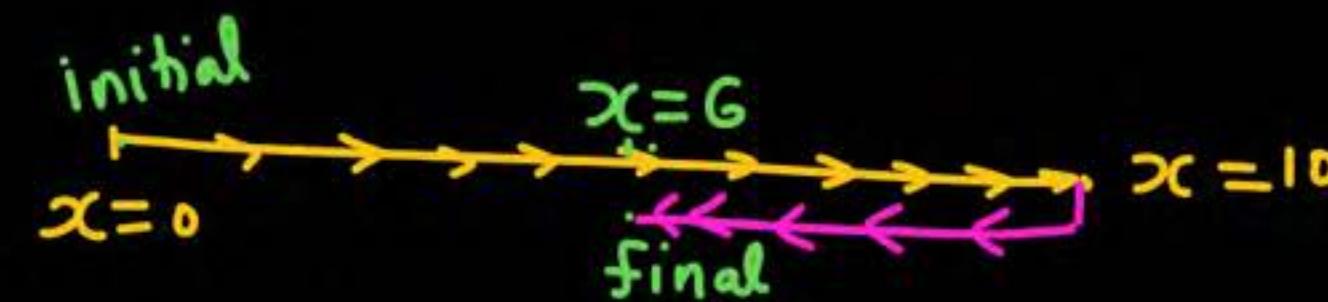
$$\text{Displacement} = -5\hat{i}$$

Q



- Displacement \rightarrow Same
- Distance $\rightarrow \overline{314159} = \text{diff} \checkmark = \text{depends on path.}$

Q

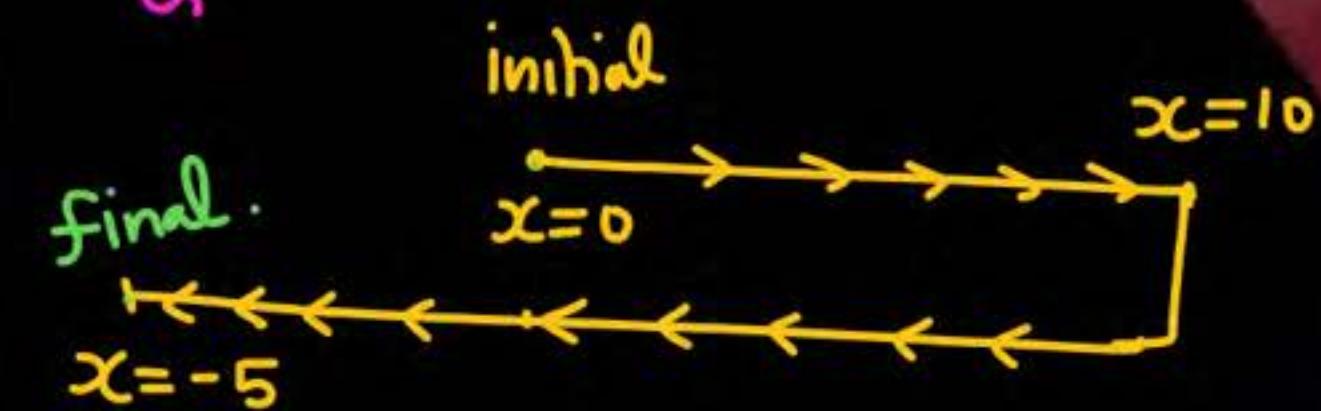


$$\text{Distance travelled} = 10 + 4 = 14$$

$$\text{Displacement} = 6 \text{ (magnitude)}$$

$$\text{Displacement (vector)} = 6\hat{i}$$

Q



$$\begin{aligned}\text{Distance} &= 10 + 10 + 5 \\ &= 25\end{aligned}$$

$$\text{Displacement} = -5\hat{i}$$





distance = 10

Displacement = $10\hat{i}$



Distance = | Displacement |

Q2

$$\text{Distance} = 4 + 3 = 7 \text{ m}$$

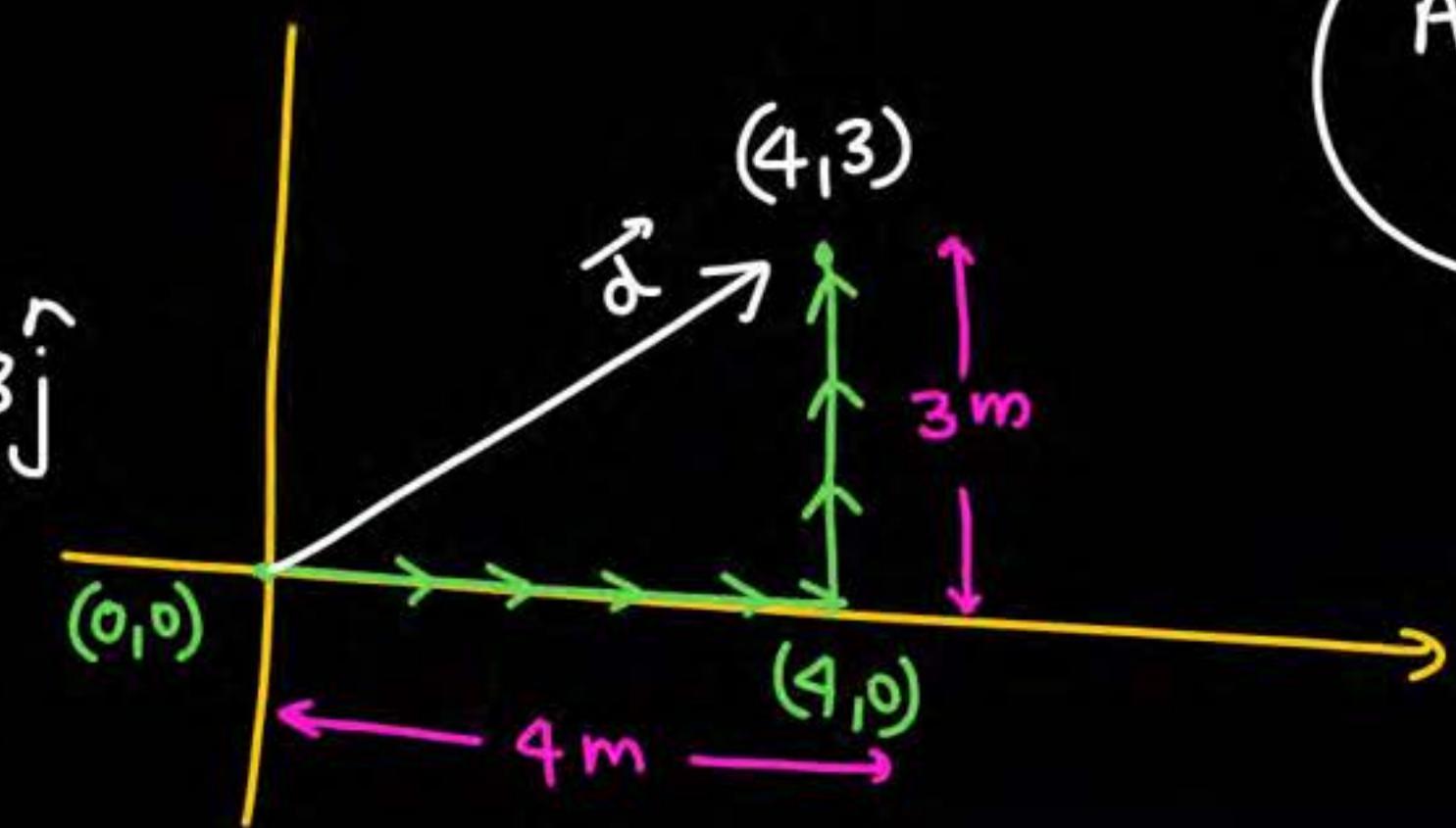
$$\text{Displacement} = \vec{d} = 4\hat{i} + 3\hat{j}$$

magnitude of

$$\begin{aligned}\text{displacement} &= \sqrt{4^2 + 3^2} \\ &= 5\end{aligned}$$

here

$$\text{Distance} > |\text{Displacement}|$$



$$\vec{d}_1 = 4\hat{i}$$

$$\vec{d}_2 = 3\hat{j}$$

$$\vec{d}_{\text{net}} = 4\hat{i} + 3\hat{j}$$

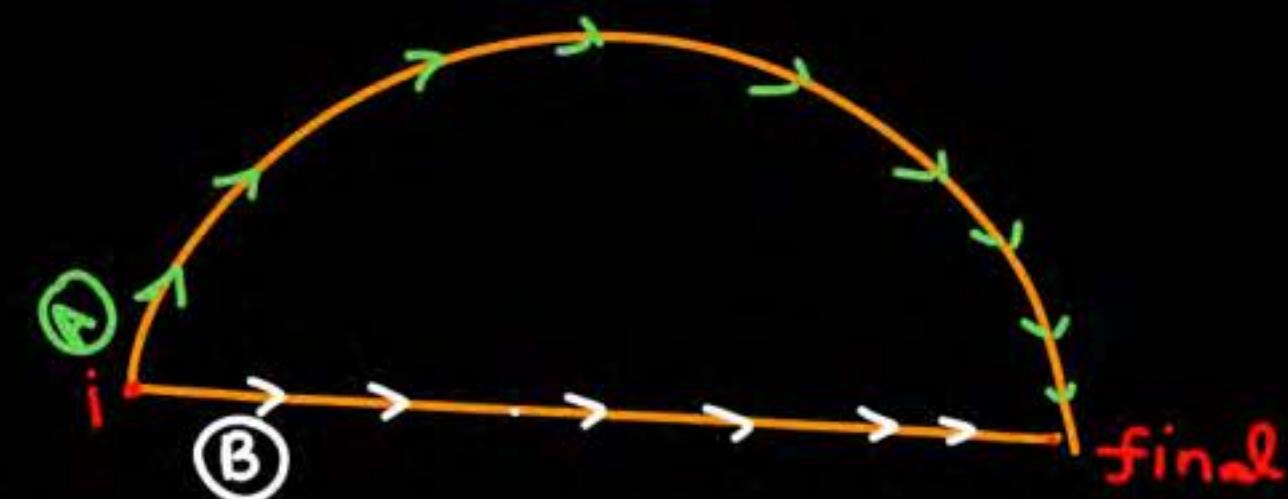
$$\vec{A} + \vec{B}$$

$$A + B$$

Q

(A) → semicircle

(B) → st. line



Q

A particle move 5m along east , then 6m along north
and 10m in upward direction.

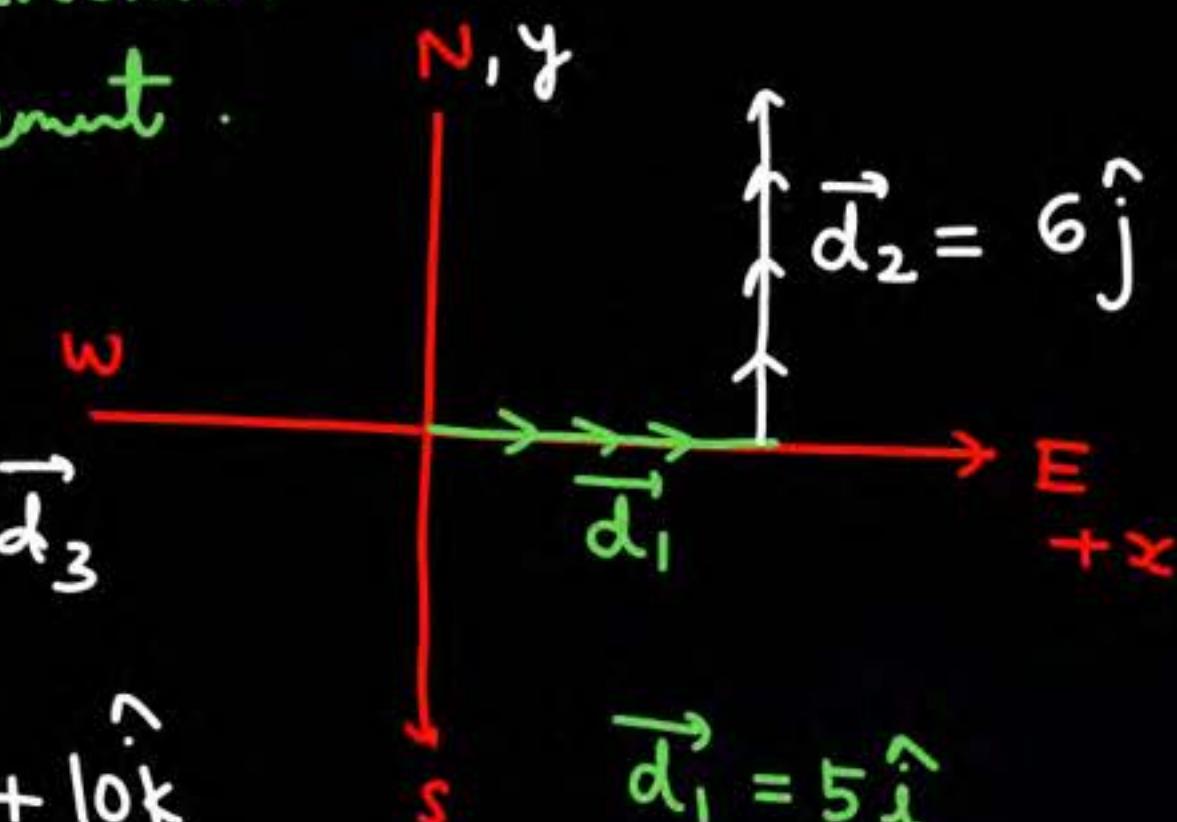
find distance & displacement .

$$\text{Distance} = 5 + 6 + 10 = 21$$

$$\text{Displacement} = \vec{d}_{\text{net}} = \vec{d}_1 + \vec{d}_2 + \vec{d}_3$$

$$= 5\hat{i} + 6\hat{j} + 10\hat{k}$$

$$\text{Magnitude} = \sqrt{5^2 + 6^2 + 10^2}$$

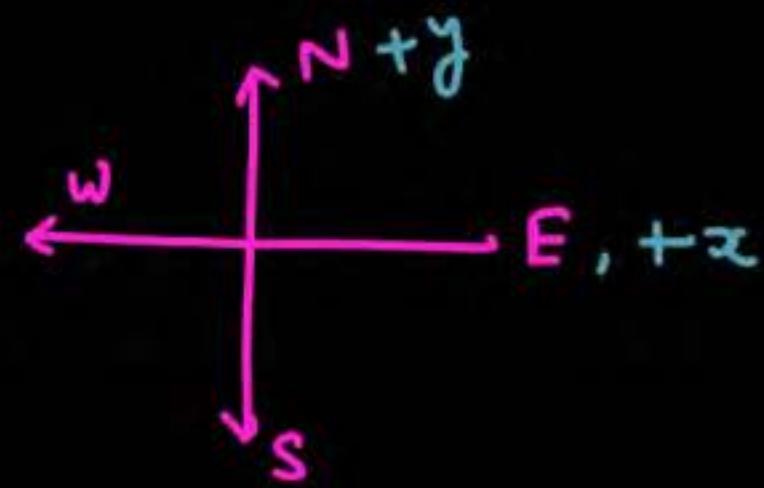


$$\vec{d}_1 = 5\hat{i}$$

$$\vec{d}_3 = 10\hat{k}$$

Q2 A particle moves

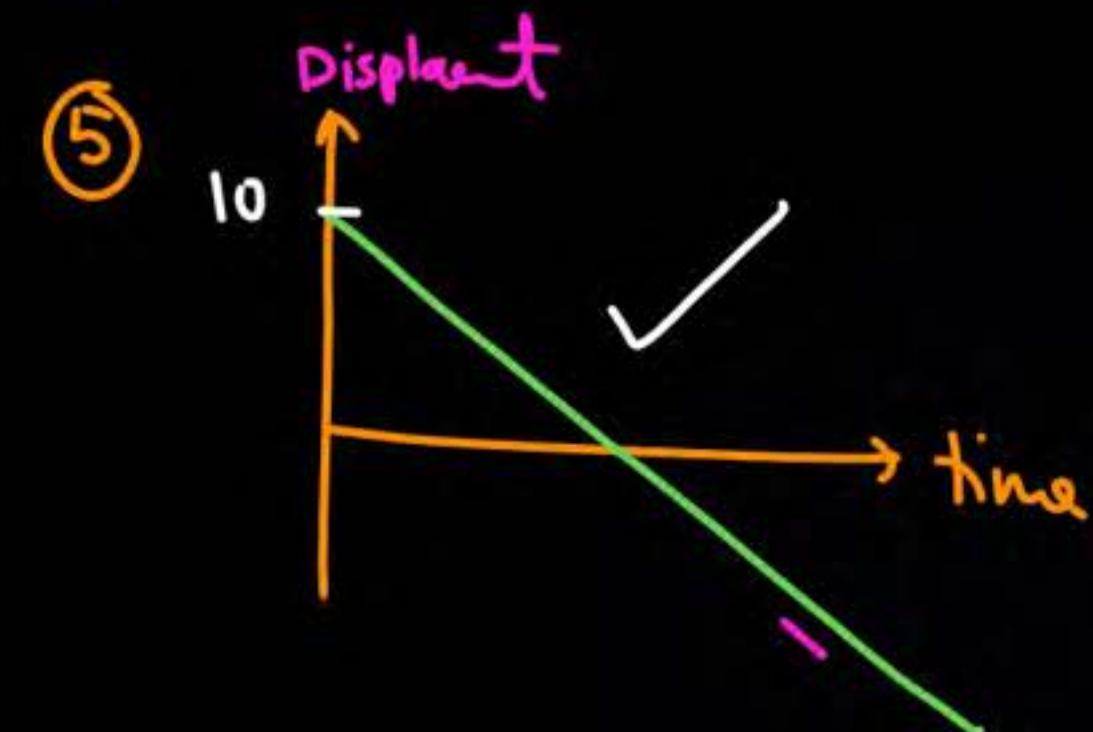
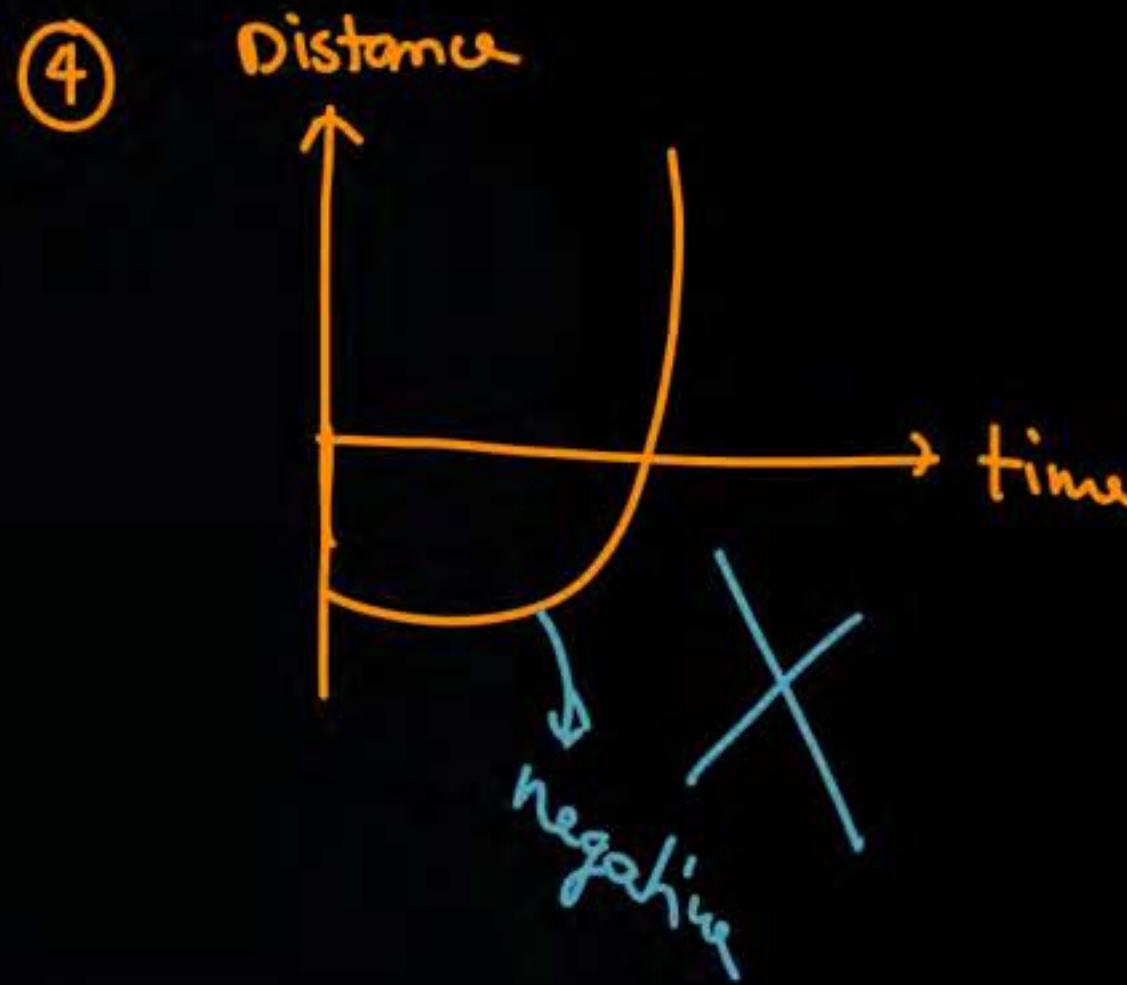
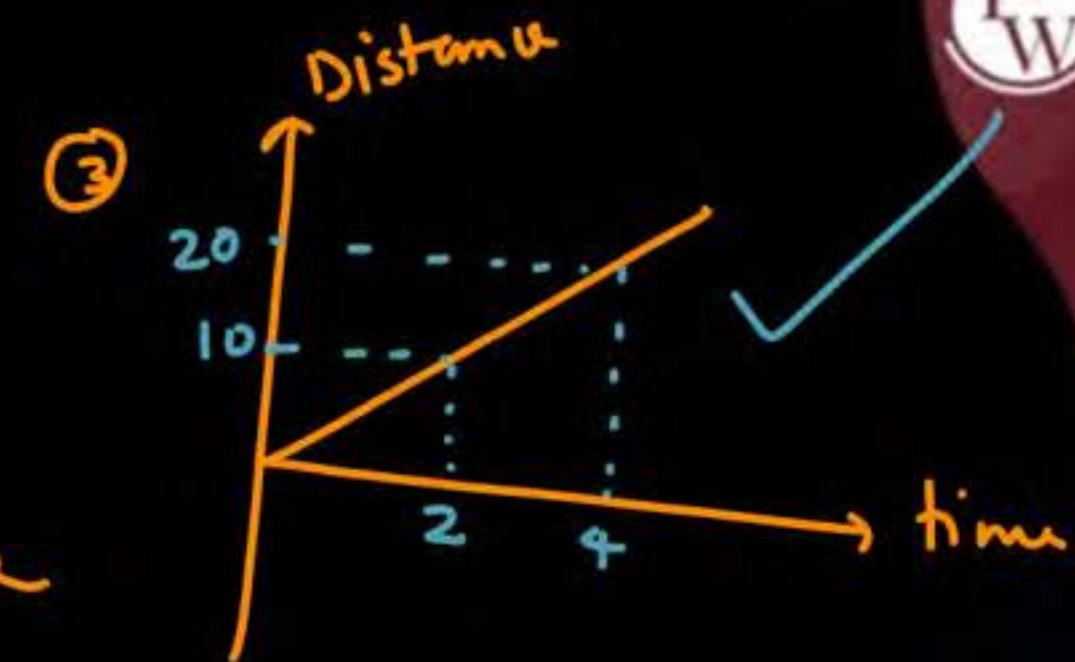
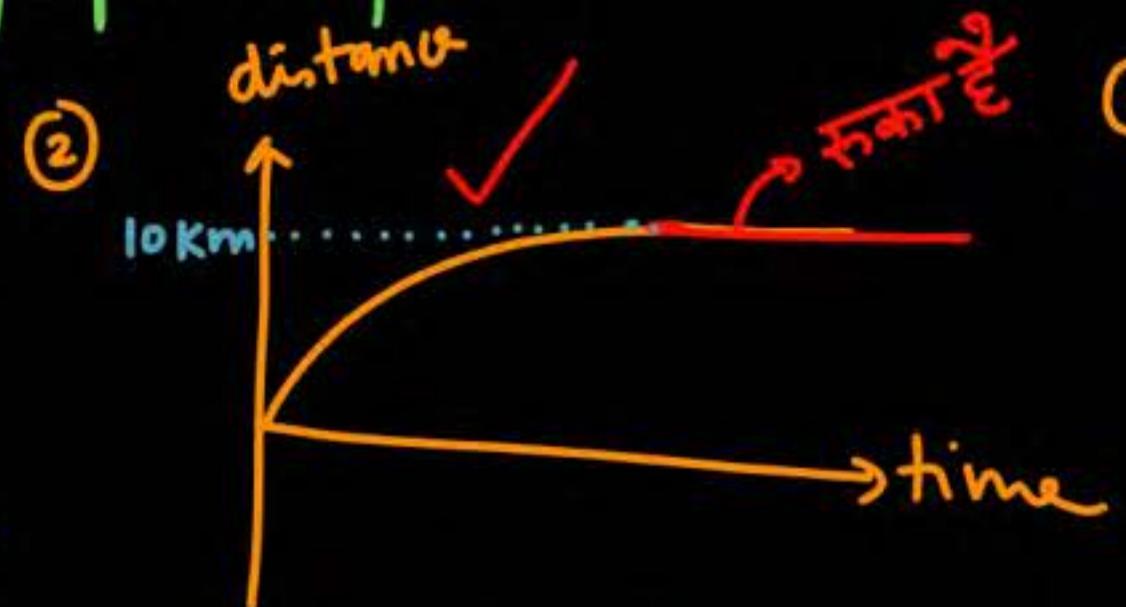
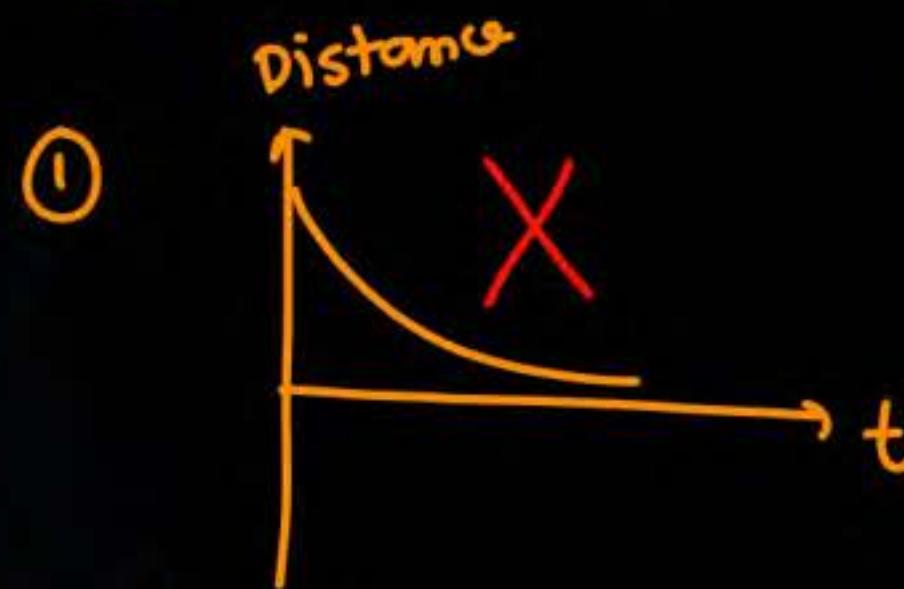
$$\begin{aligned}10 \text{ m east} &= \vec{d}_1 = 10\hat{i} \\5 \text{ m north} &= \vec{d}_2 = 5\hat{j} \\6 \text{ m south} &= \vec{d}_3 = -6\hat{j} \\8 \text{ m west} &= \vec{d}_4 = -8\hat{i} \\15 \text{ m east} &= \vec{d}_5 = 15\hat{i} \\20 \text{ m north} &= \vec{d}_6 = 20\hat{j}\end{aligned}$$

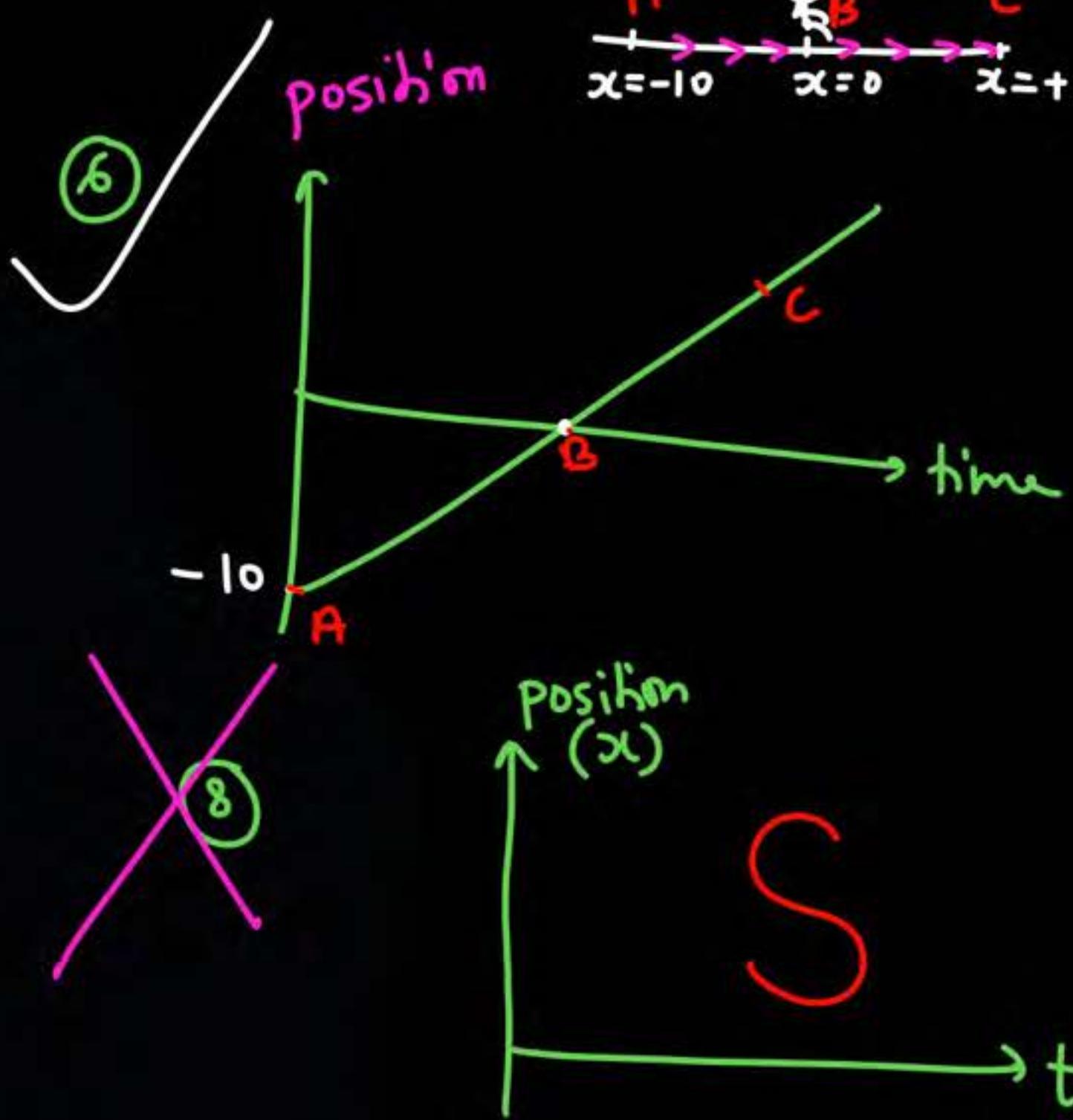


$$\begin{aligned}\vec{d}_{\text{net}} &= (\text{Add}) = (10 - 8 + 15)\hat{i} + (5 - 6 + 20)\hat{j} \\&= 17\hat{i} + 19\hat{j}\end{aligned}$$

$$\text{distance} = 10 + 5 + 6 + 8 + 15 + 20$$

Q which of the graph is possible.





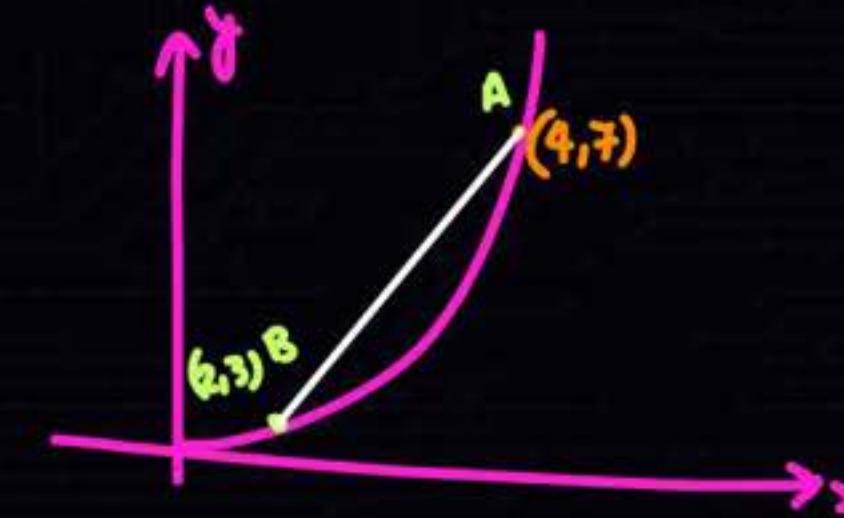
displacement = change in position

$$\vec{d} = \vec{x}_f - \vec{x}_i$$

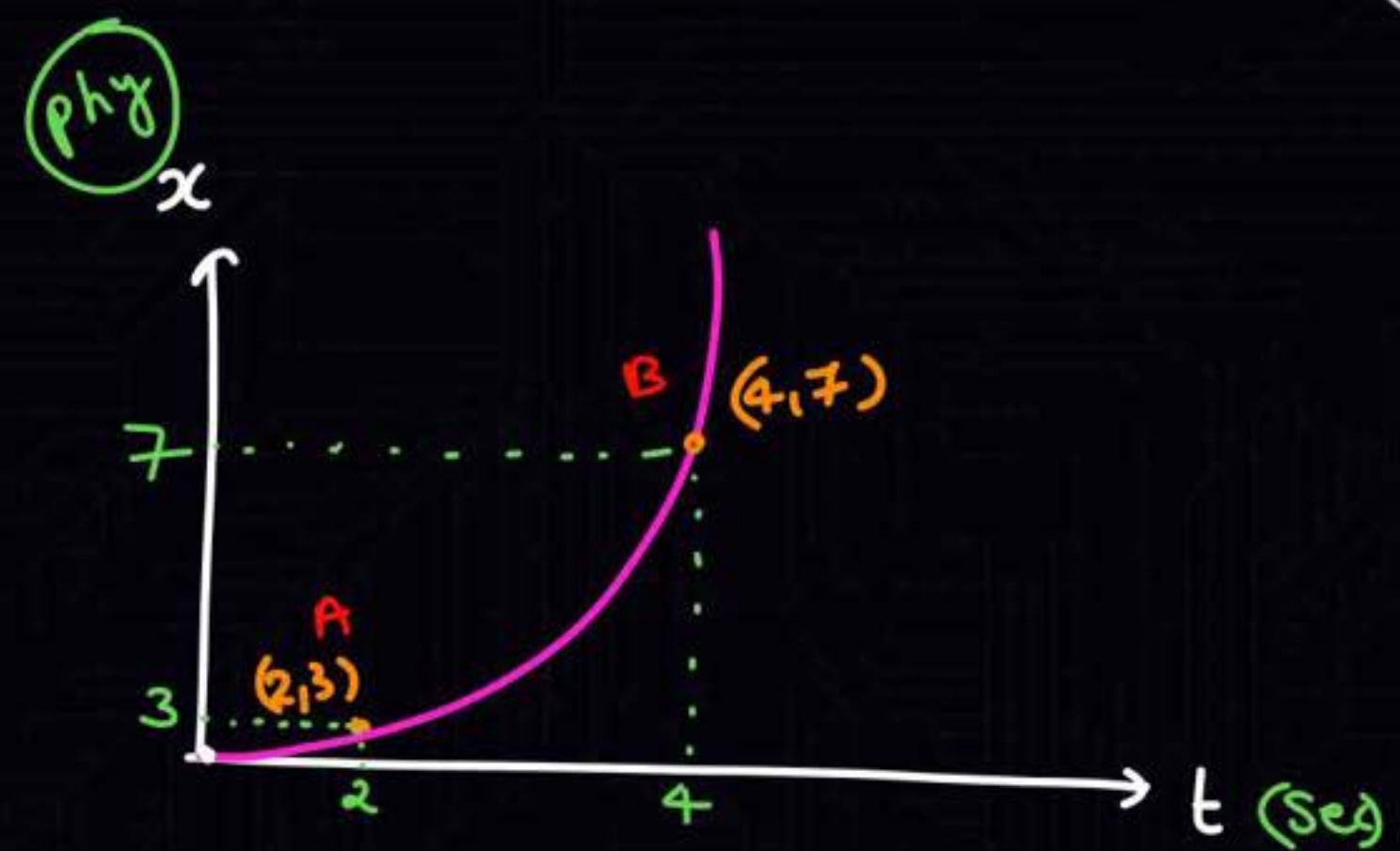
Slope

$$\text{Slope} = \frac{y_2 - y_1}{x_2 - x_1}$$

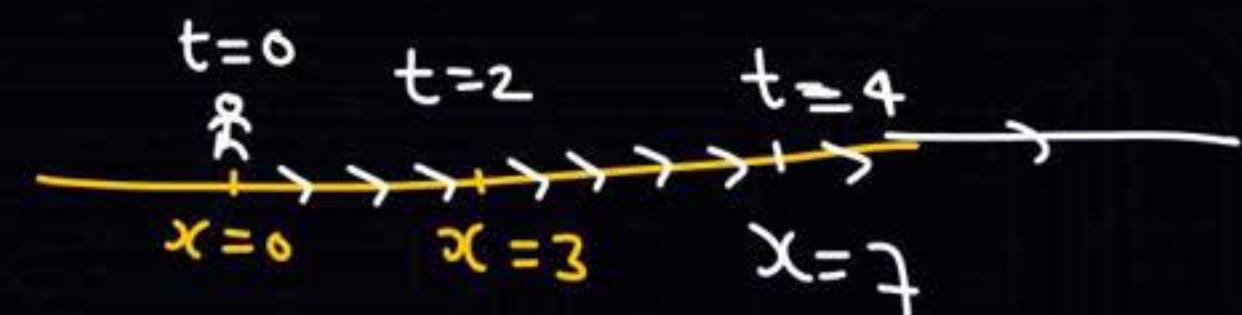
$$\text{Slope} = \frac{7-3}{4-2} = 2$$

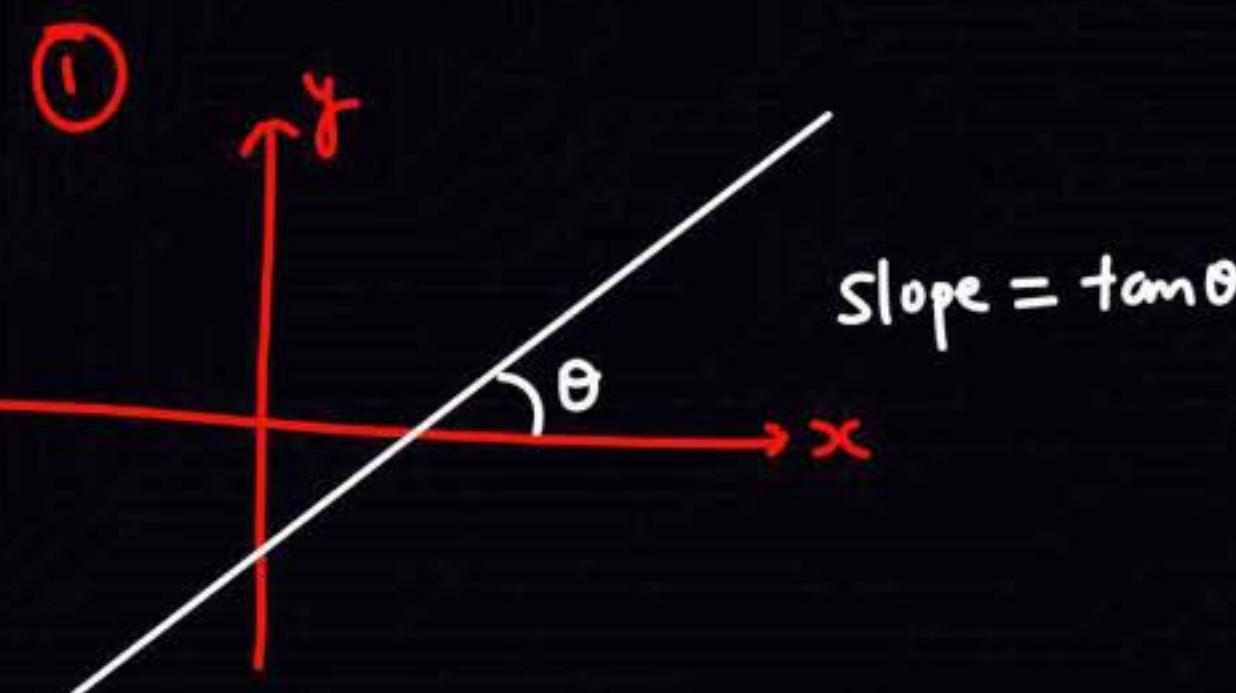


$$\text{Slope} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\text{change in } y}{\text{change in } x}$$



$$\text{Avg velocity } (A \rightarrow B) = \frac{x_f - x_i}{t_2 - t_1} = \frac{7 - 3}{4 - 2} = 2$$

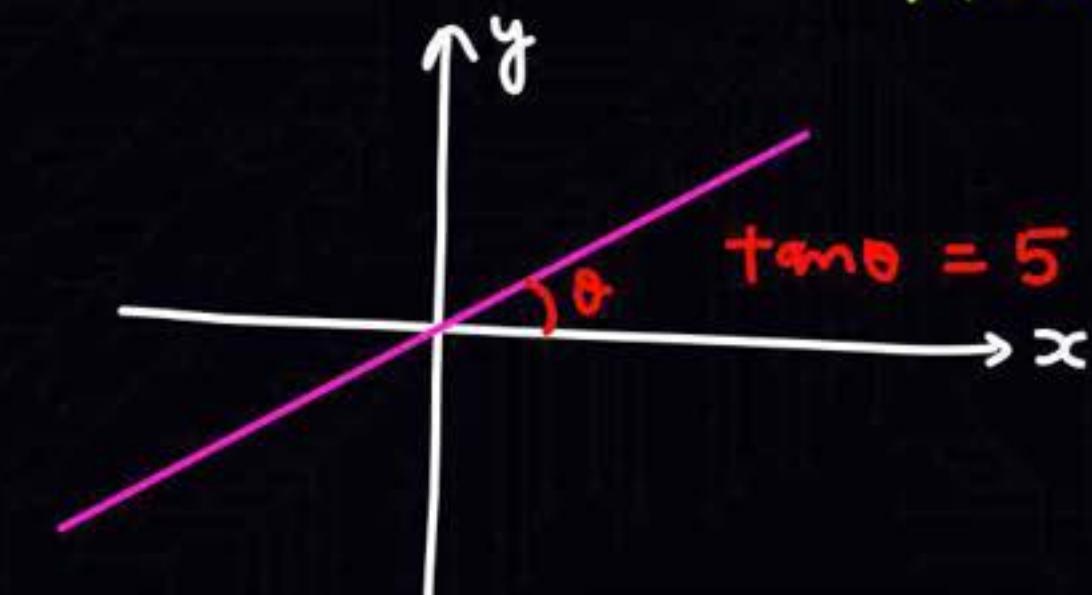




②

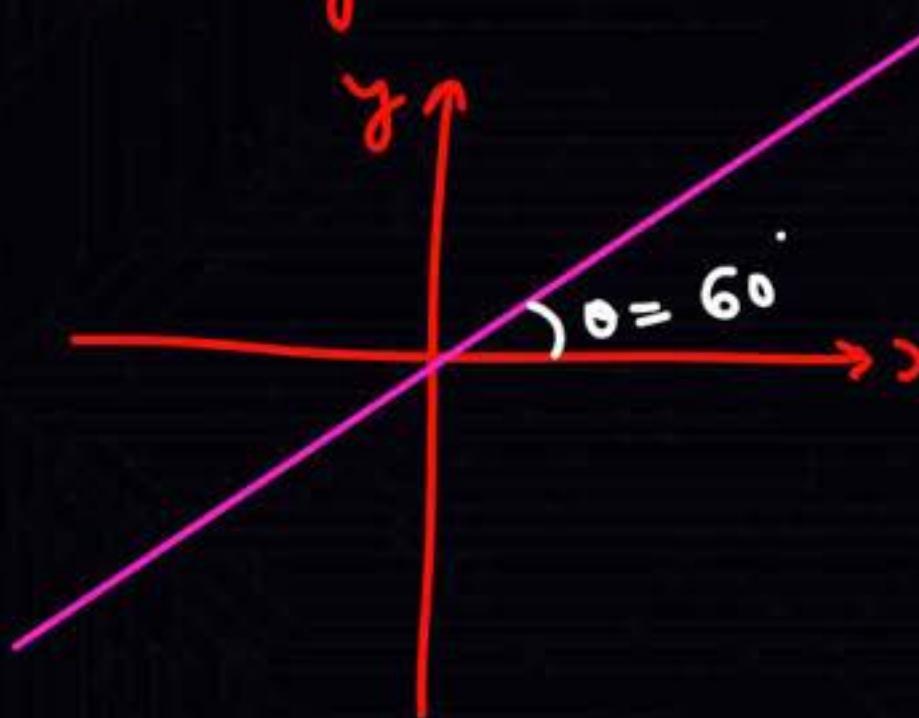
$$y = 5x$$

$m = 5 = \text{Slope}$



③

$$y = x\sqrt{3}$$



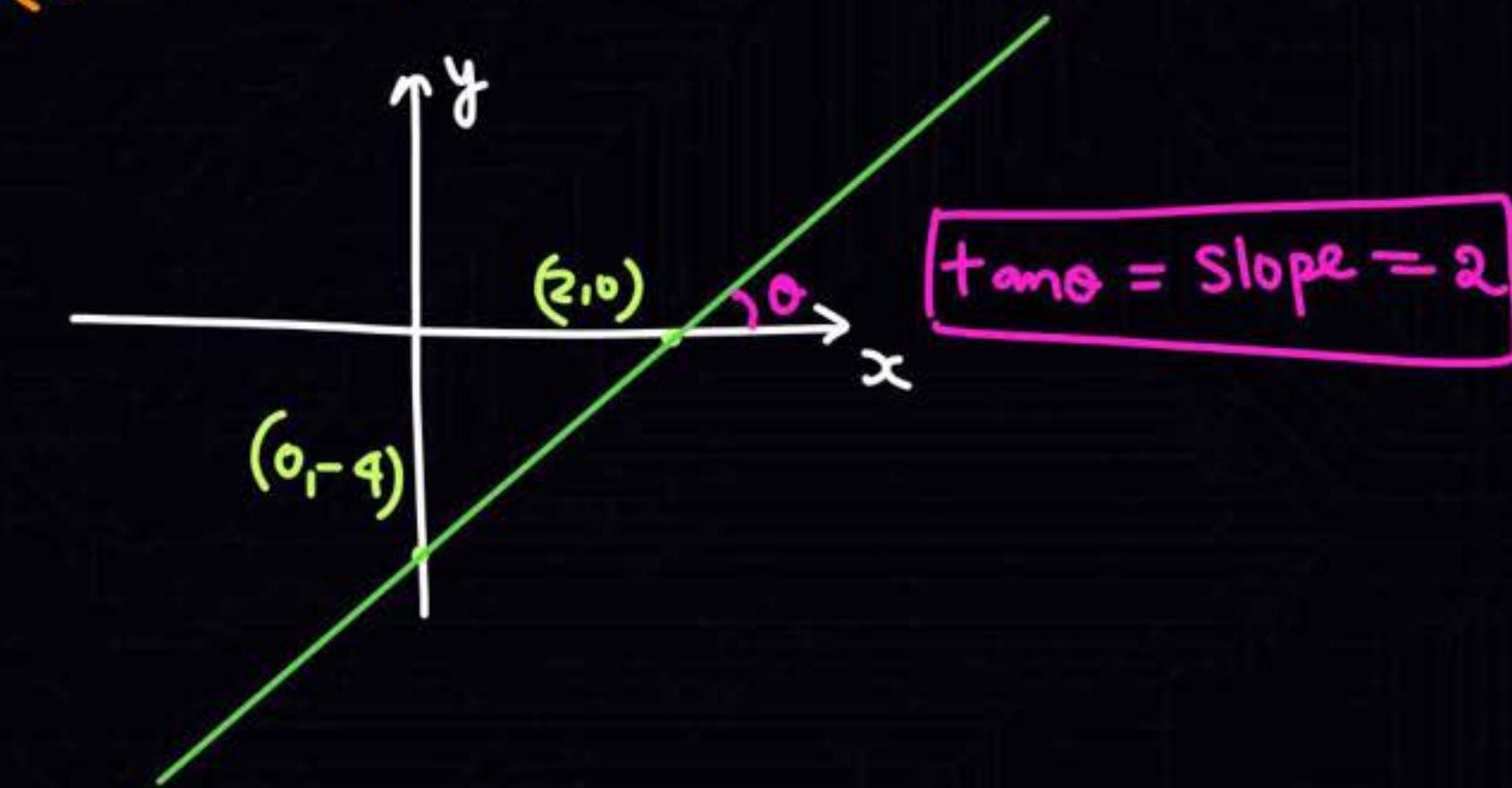
$$\text{slope} = \sqrt{3} = \tan \theta$$

$$\theta = 60^\circ$$

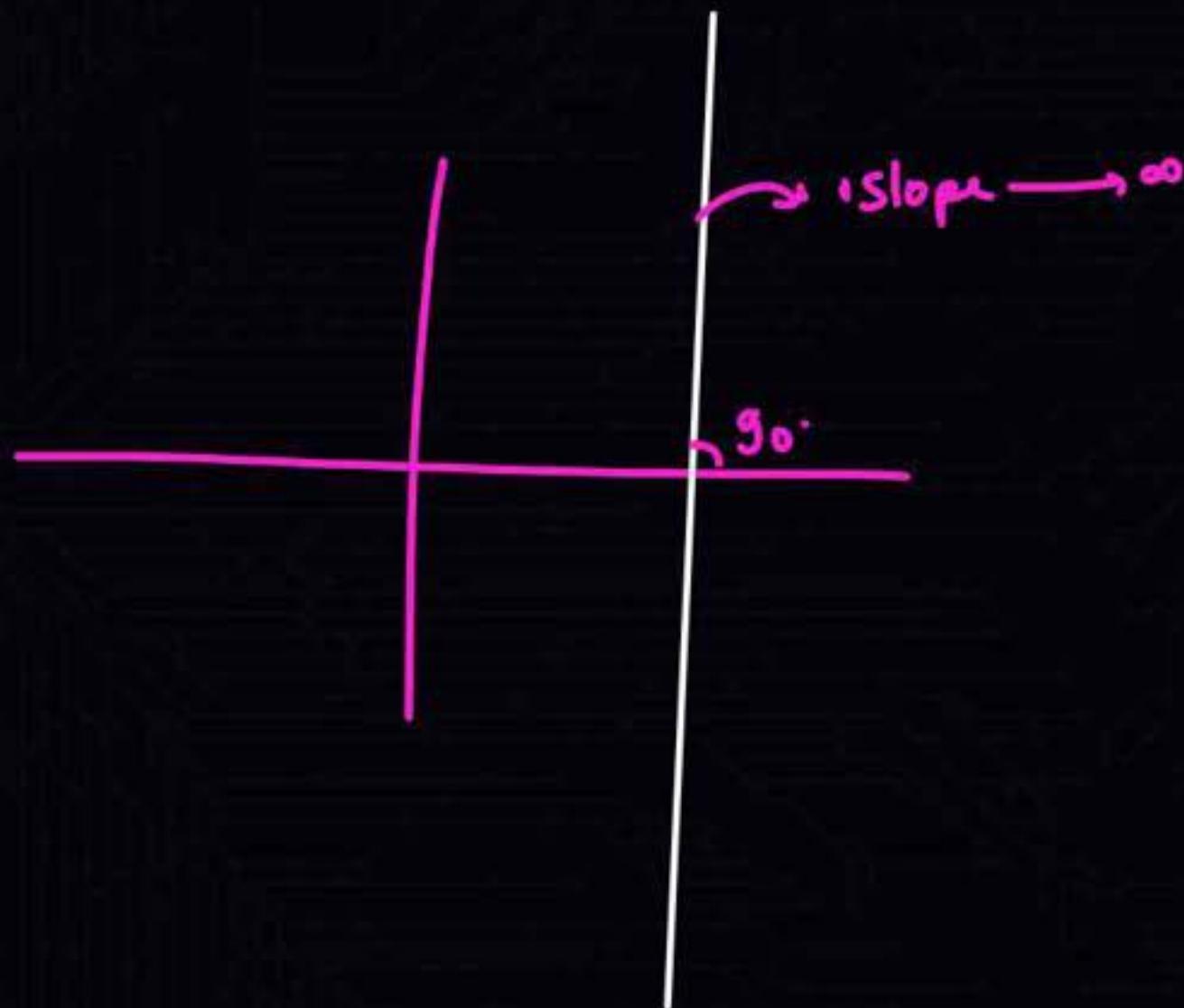
$$y = 2x - 4 \quad (\text{draw}) \rightarrow (\text{not imp in physics})$$

$$(x=0, y=-4) = (0_1 - 4)$$
$$(y=0, x=2) = (2, 0)$$

slope = 2 \Rightarrow +ve



$$\tan \theta = \text{Slope} = 2$$

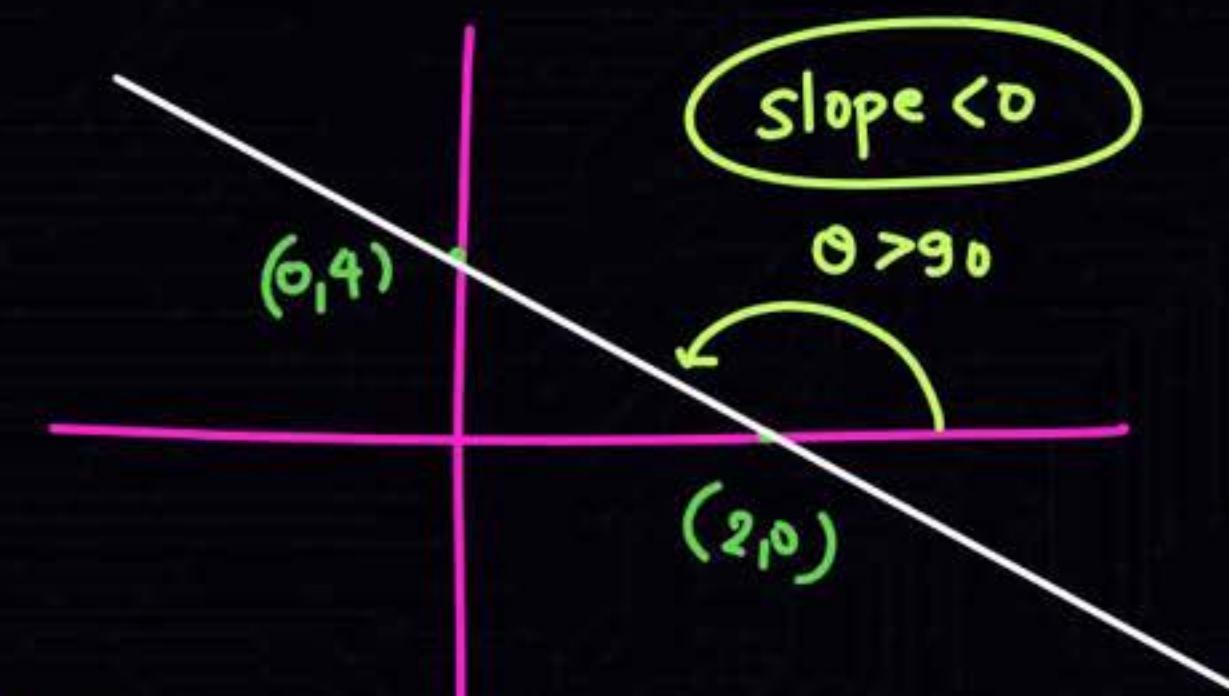


$$y = -2x + 4$$

$$\begin{pmatrix} x=0, & y=4 \\ y=0, & x=2 \end{pmatrix}$$

$$\text{slope} = -2$$

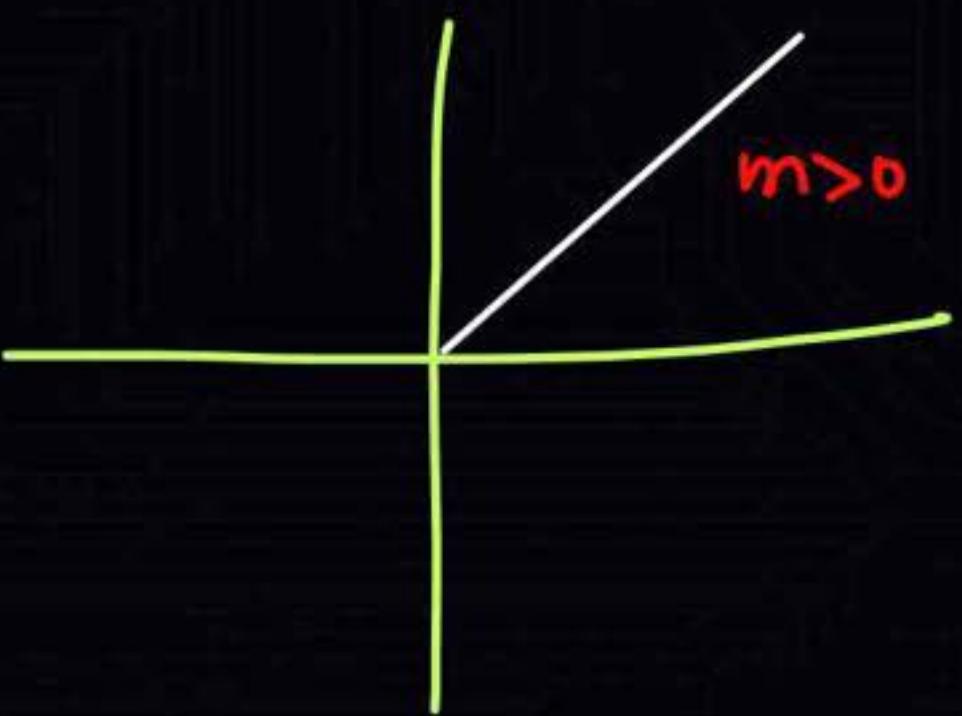
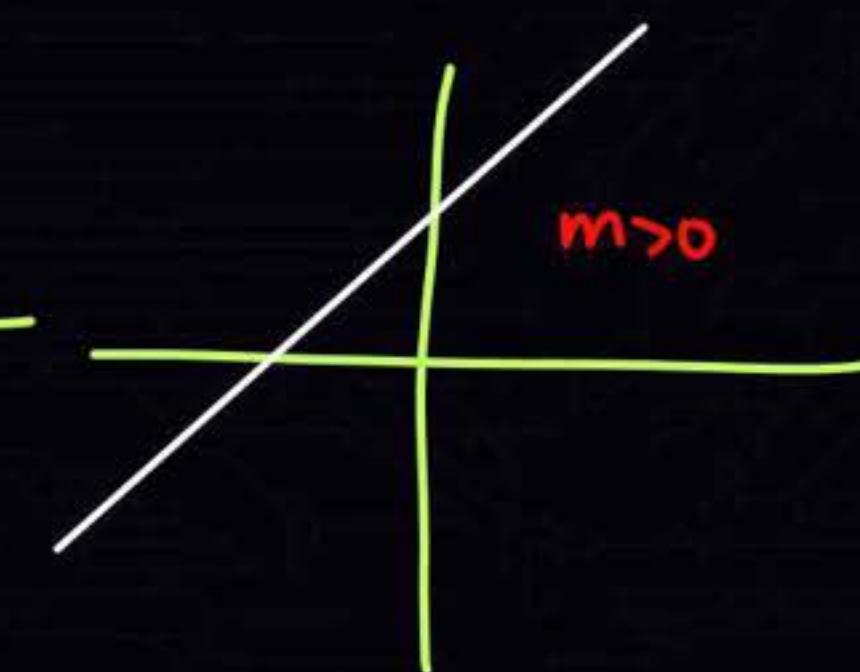
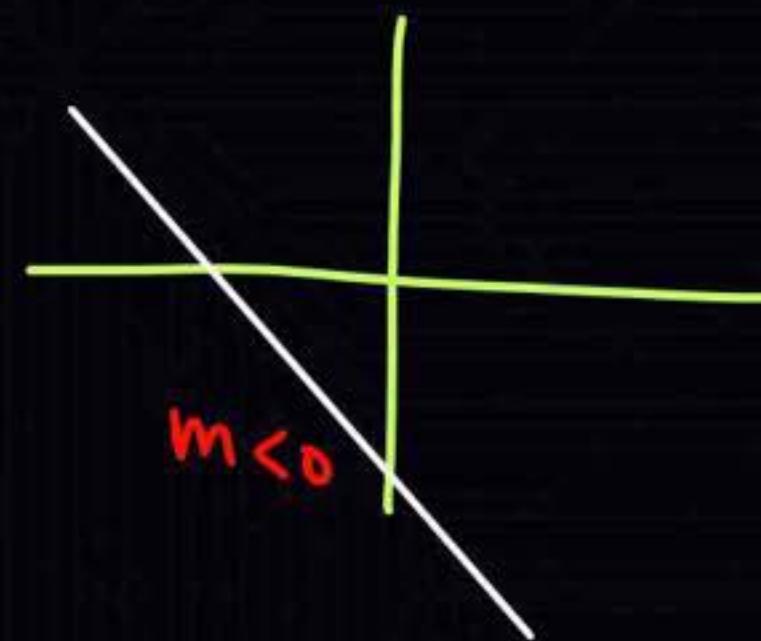
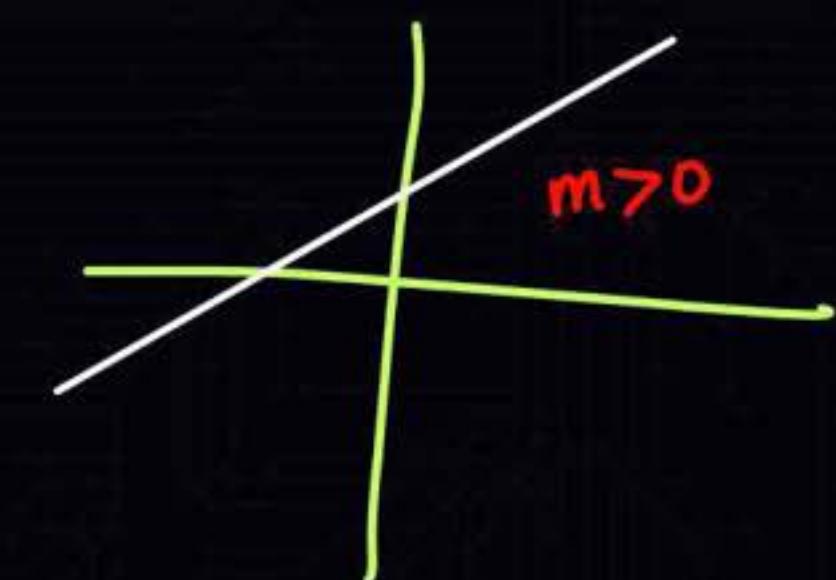
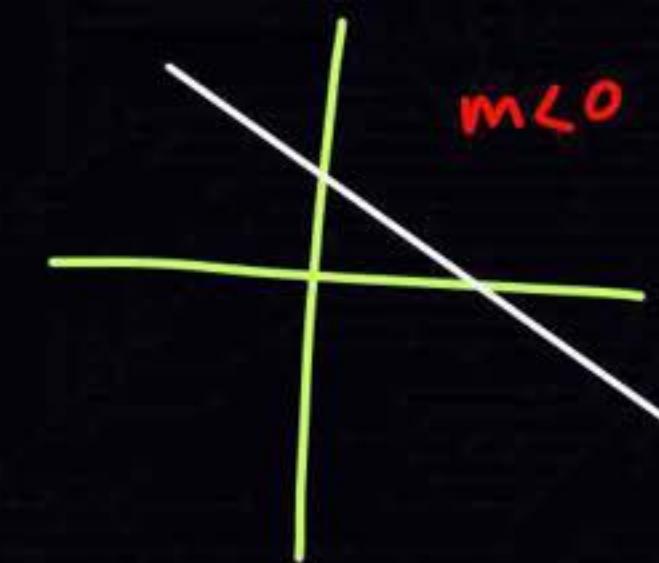
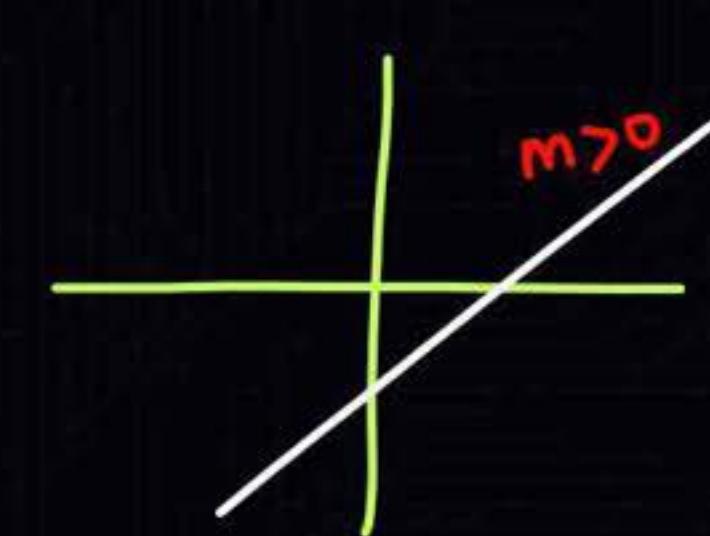
$$\tan \theta = -2$$



$$\begin{aligned} y &= mx + c \\ 2y &= 8x + 16 \end{aligned}$$

$$\boxed{\text{slope} = 8x}$$

$$\begin{aligned} y &= 4x + 8 \\ \text{slope} &= 4 \end{aligned}$$



$$y = x^n$$

$$\frac{dy}{dx} = nx^{n-1}$$

$$\textcircled{1} \quad y = x^3$$

$$\frac{dy}{dx} = 3x^{3-1} = 3x^2$$

$$\textcircled{2} \quad y = x^5$$

$$\frac{dy}{dx} = 5x^4$$

$$\textcircled{3} \quad y = x^7$$

$$\frac{dy}{dx} = 7x^6$$

$$\textcircled{4} \quad y = x^9$$

$$\frac{dy}{dx} = 9x^8$$

$$\textcircled{5} \quad y = 2x^5$$

$$\begin{aligned}\frac{dy}{dx} &= 2 \times 5x^4 \\ &= 10x^4\end{aligned}$$

$$\textcircled{6} \quad y = x^3$$

$$\frac{dy}{dx} = 3x^2$$

$$\textcircled{7} \quad y = t^3$$

$$\frac{dy}{dt} = 3t^2$$

$$\textcircled{8} \quad x = t^3$$

$$\frac{dx}{dt} = 3t^2$$

$$\textcircled{9} \quad x = t^5$$

$$\frac{dx}{dt} = 5t^4$$

$$\textcircled{10} \quad x = t^7$$

$$\frac{dx}{dt} = 7t^6$$

$$\textcircled{1} \quad y = x^n$$

$$\frac{dy}{dx} = nx^{n-1}$$

$$\textcircled{2} \quad y = \sin x$$

$$\frac{dy}{dx} = \frac{d}{dx}(\sin x) = \cos x$$

\Downarrow

means

differentiation of $\sin x$ w.r.t. x
is $\cos x$

$$\textcircled{3} \quad y = \cos x$$

$$\frac{dy}{dx} = \frac{d}{dx} \cos x = -\sin x$$

$$\textcircled{4} \quad y = \tan x$$

$$\frac{dy}{dx} = \frac{d}{dx}(\tan x) = \sec^2 x$$

$$\textcircled{5} \quad y = \cot x$$

$$\frac{dy}{dx} = \frac{d(\cot x)}{dt} = -\operatorname{cosec}^2 x$$

$$* \frac{d}{dx}(\csc x) = -\csc x \cot x$$

$$* \frac{d}{dx}(x^n) = nx^{n-1}$$

$$* \frac{d}{dx} \cot x = -\operatorname{cosec}^2 x$$

$$* \frac{d}{dx} \sin x = \cos x$$

$$* \frac{d}{dx} e^x = e^x$$

$$* \frac{d}{dx}(\cos x) = -\sin x$$

$$* \frac{d}{dx}(\ln x) = \frac{1}{x}$$

$$* \frac{d}{dx}(\tan x) = \sec^2 x$$

$$* \frac{d}{dx}(\sec x) = \sec x \tan x$$

Q

$$x = \frac{t^3}{3} - 3t^2 + 9t + 21$$

$$v = t^2 - 6t + 9 + 0 = (t-3)^2$$

$$v = 0$$

$$t^2 - 6t + 9 = 0$$

$$t = 3 \text{ sec}$$

~~$t = 3$ is turning point~~

$$v = (t-3)^2 > 0$$

→ $v \rightarrow$ always +ve
No turning point



x

$$Q \quad x = 3t^2 - 12t + 10$$

$$\textcircled{1} \quad t=0, \quad t=2, \quad t=3,$$

$$\left. \begin{array}{l} \rightarrow v = 6t - 12 \\ \rightarrow a = 6 = \text{const} \end{array} \right\}$$

	x	v	a
$t=0$	10	-12	6
$t=2$	-2	0	6
$t=3$	+1	6	6

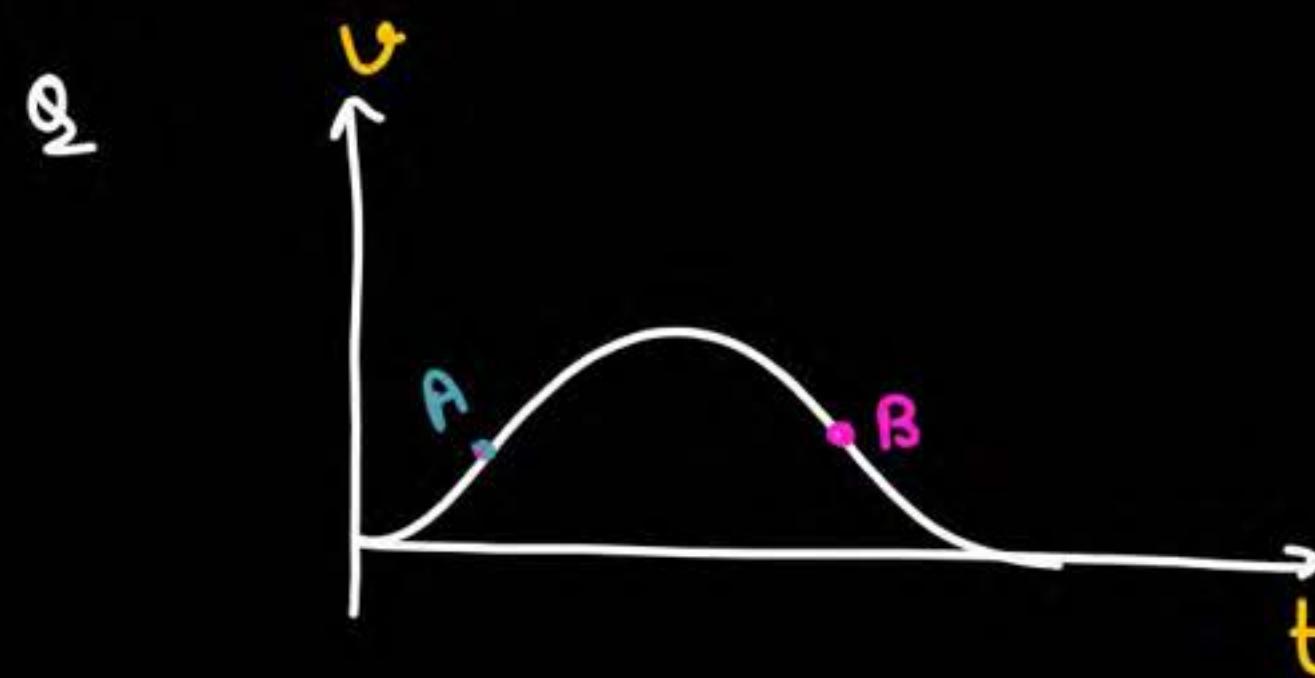
$\textcircled{2}$ find x & a when particle comes to rest

$$v = 0, \quad v = 6t - 12 = 0$$

$$t = 2$$

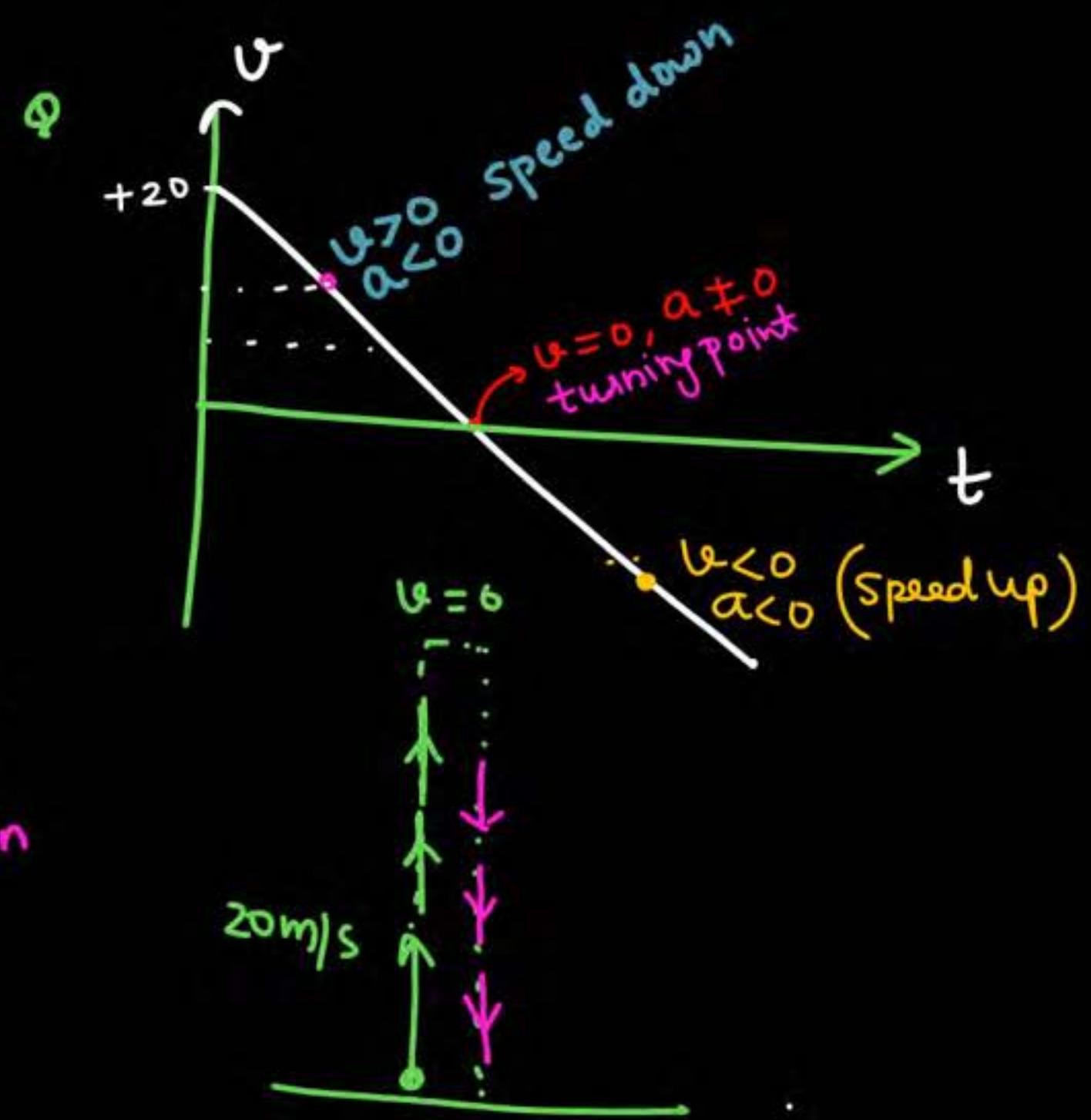
$$t = 2, \quad x = -2$$

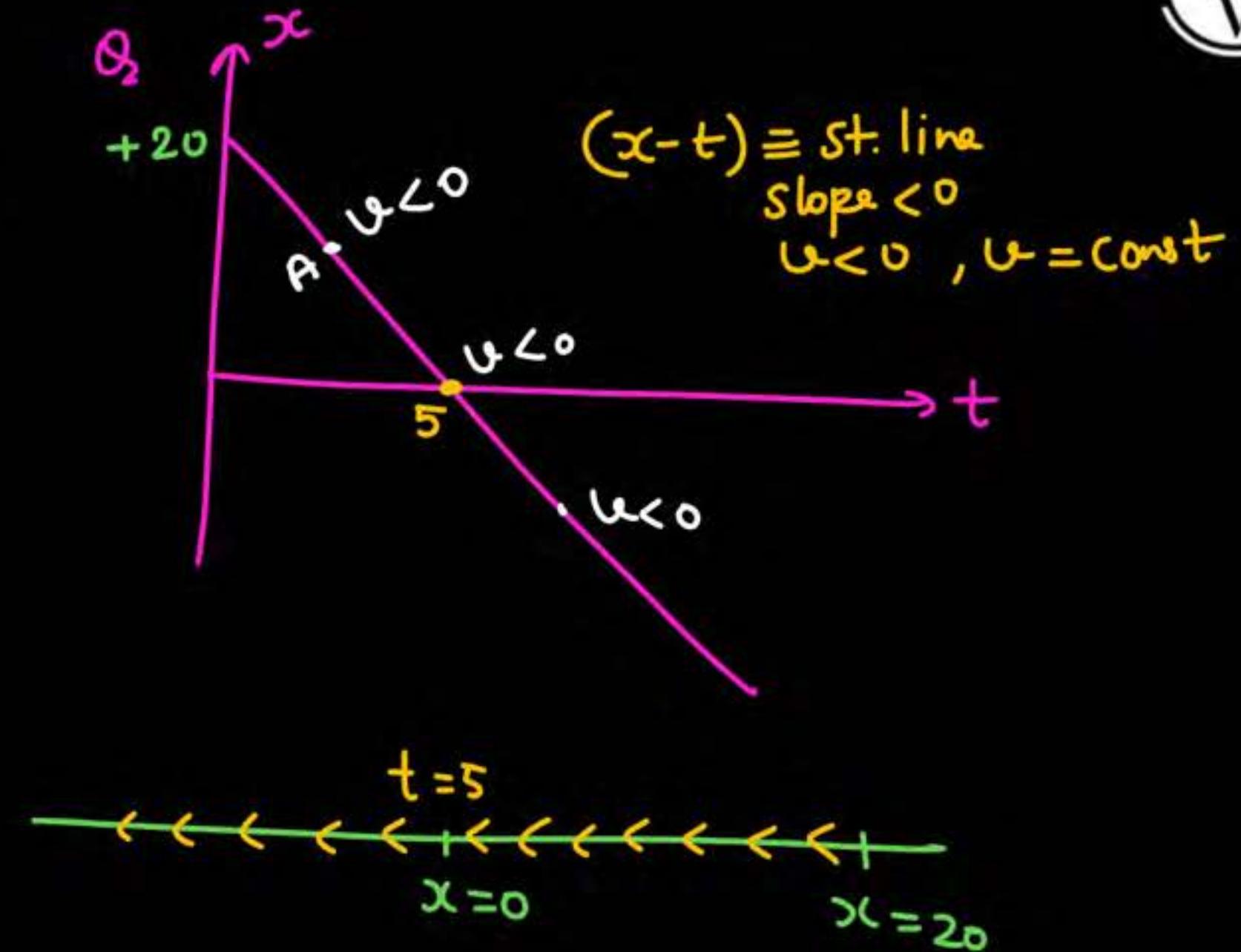
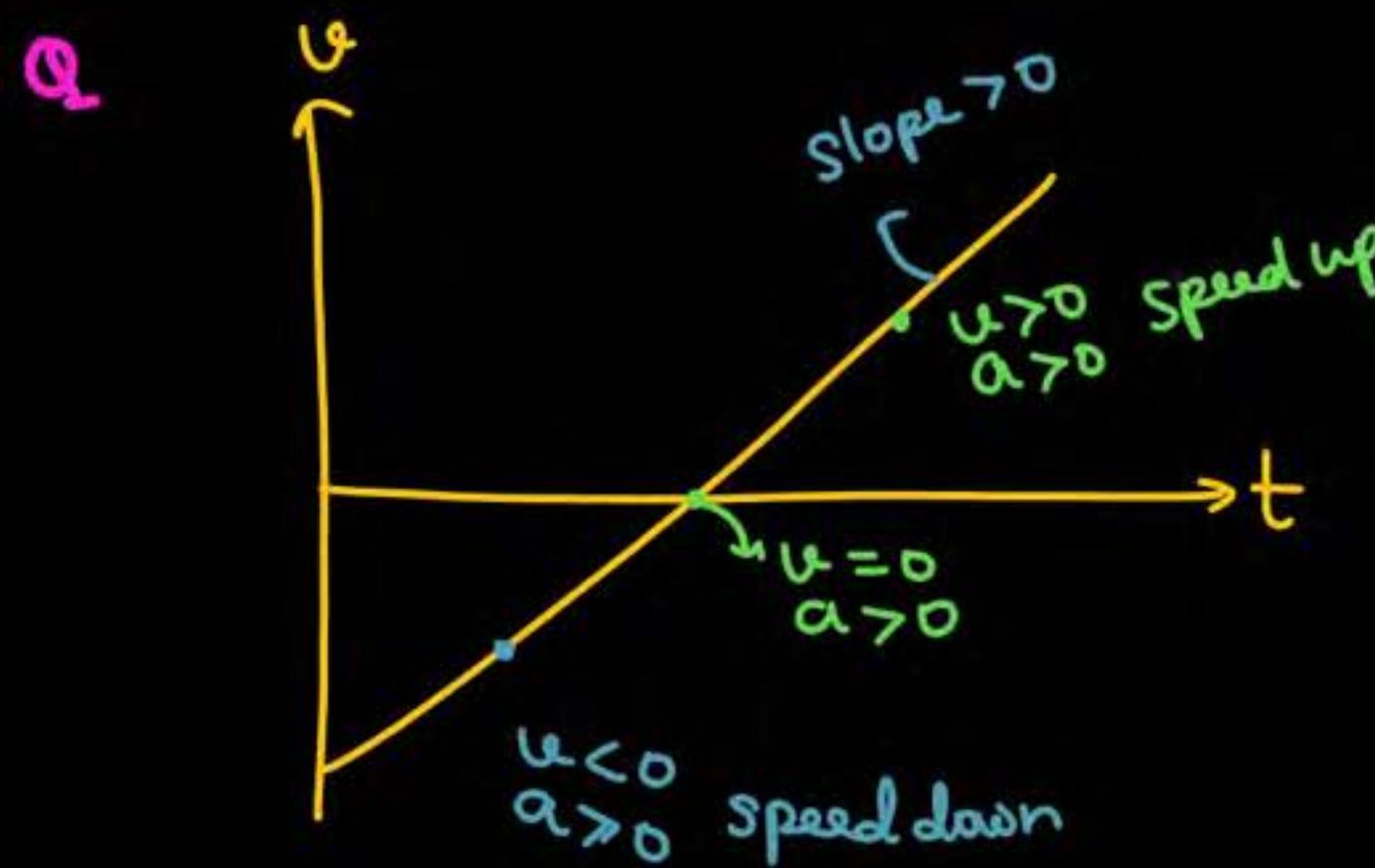
$$a = 6$$

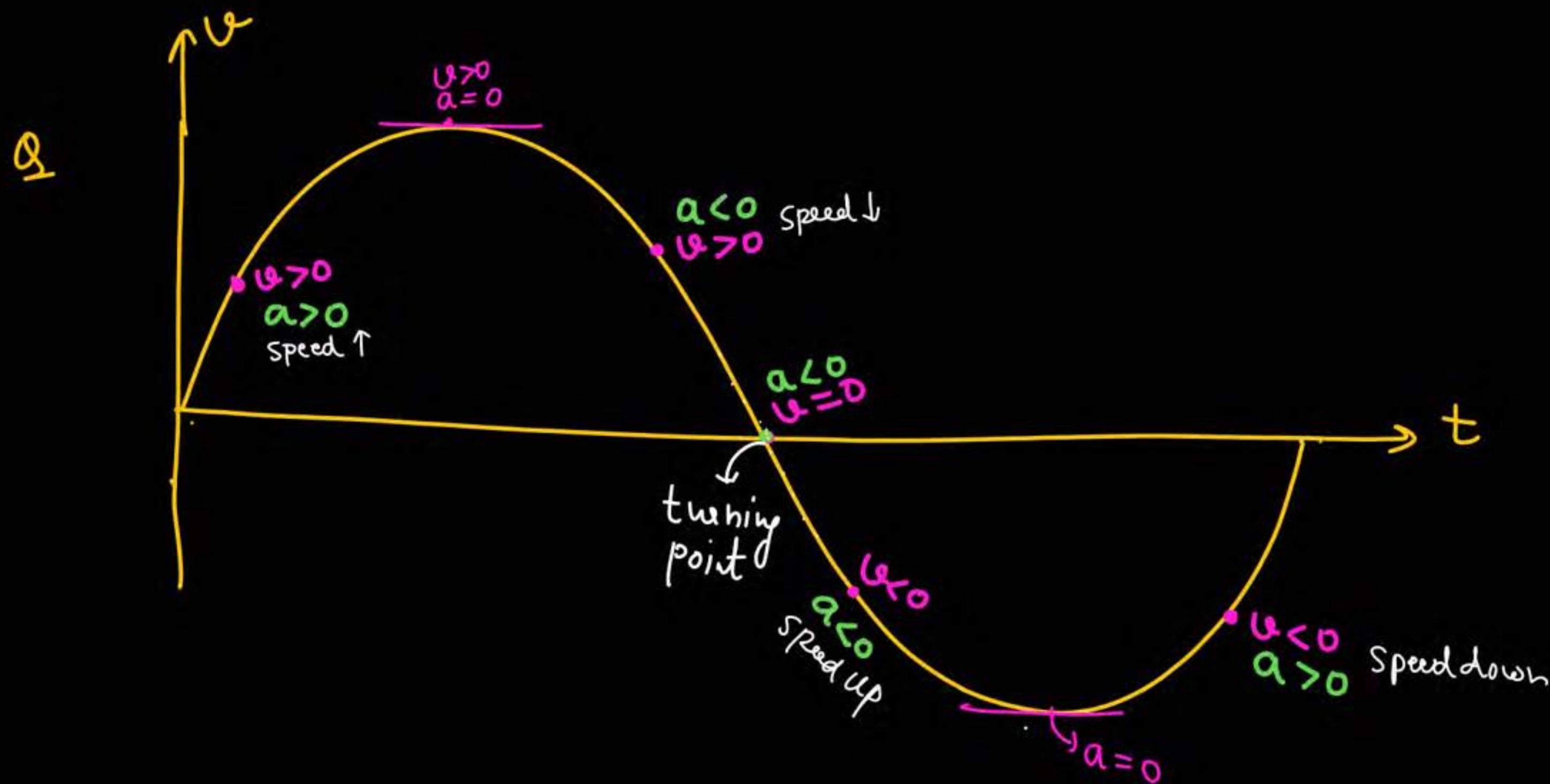


$v_A > 0, a_A > 0 \Rightarrow$ Speed up

$v_B > 0, a_B < 0 \Rightarrow$ Speed down







Ω
 x


logical तरीका

$$v_A > 0, v_B > 0$$

(slope) at B > (slope) at A

$$v_B > v_A$$

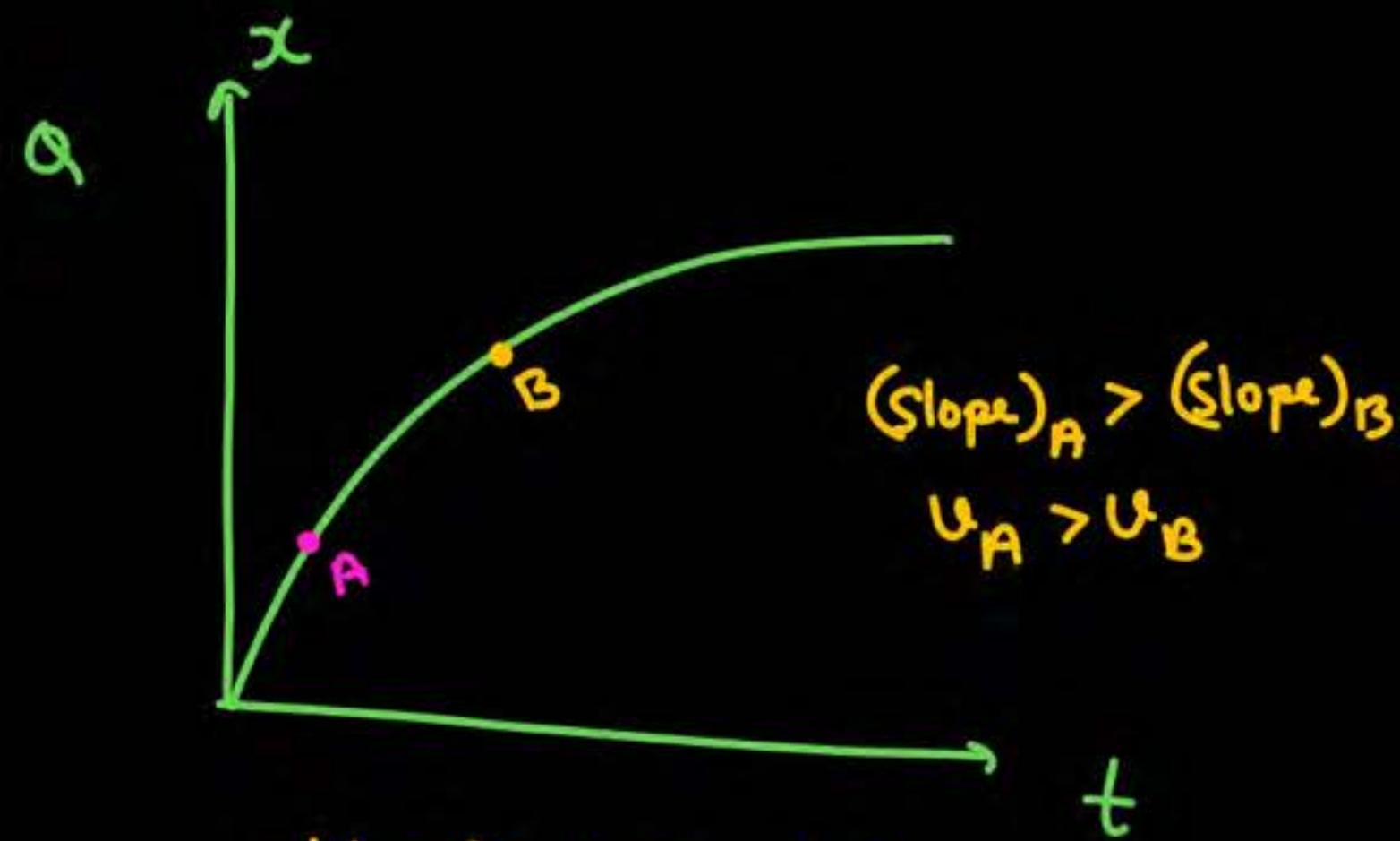
speed up

$$v > 0 \\ a > 0$$


 x


$$v > 0 \\ \text{Speed up} \\ a > 0$$



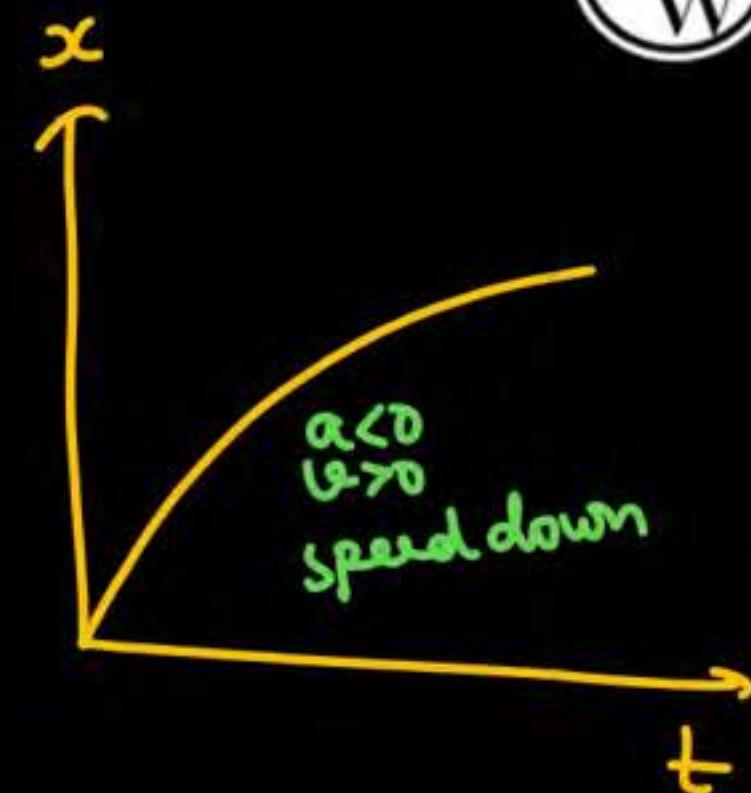
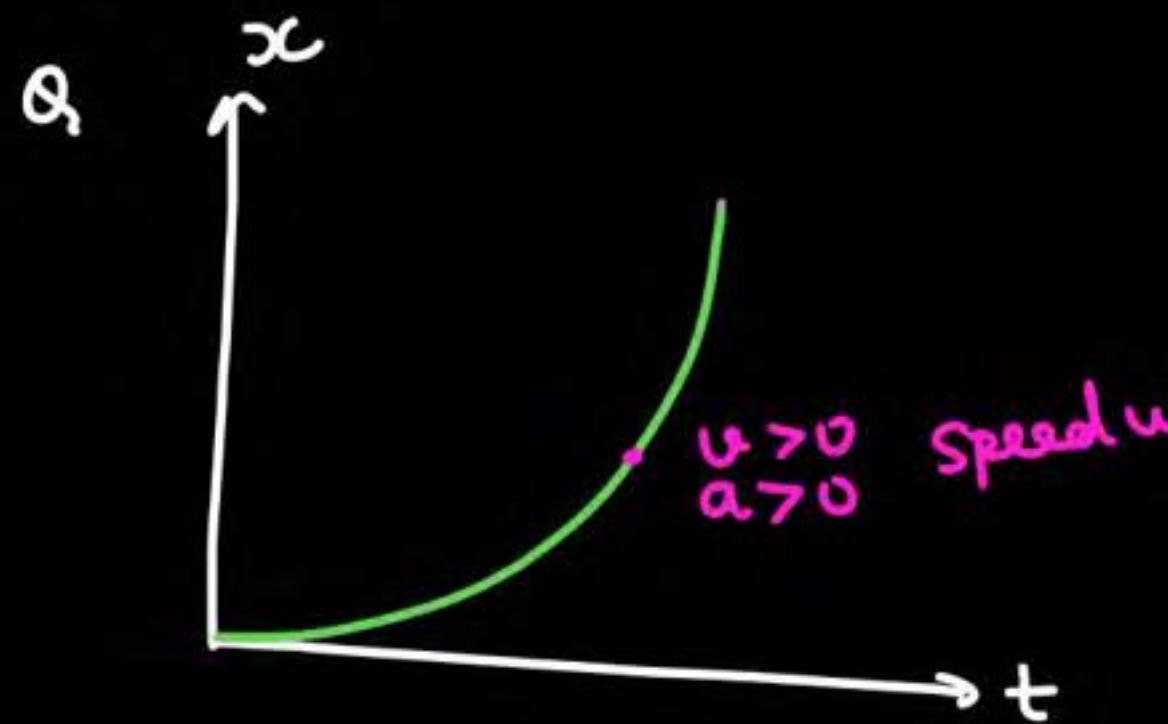


time $\uparrow \Rightarrow$ Speed \downarrow

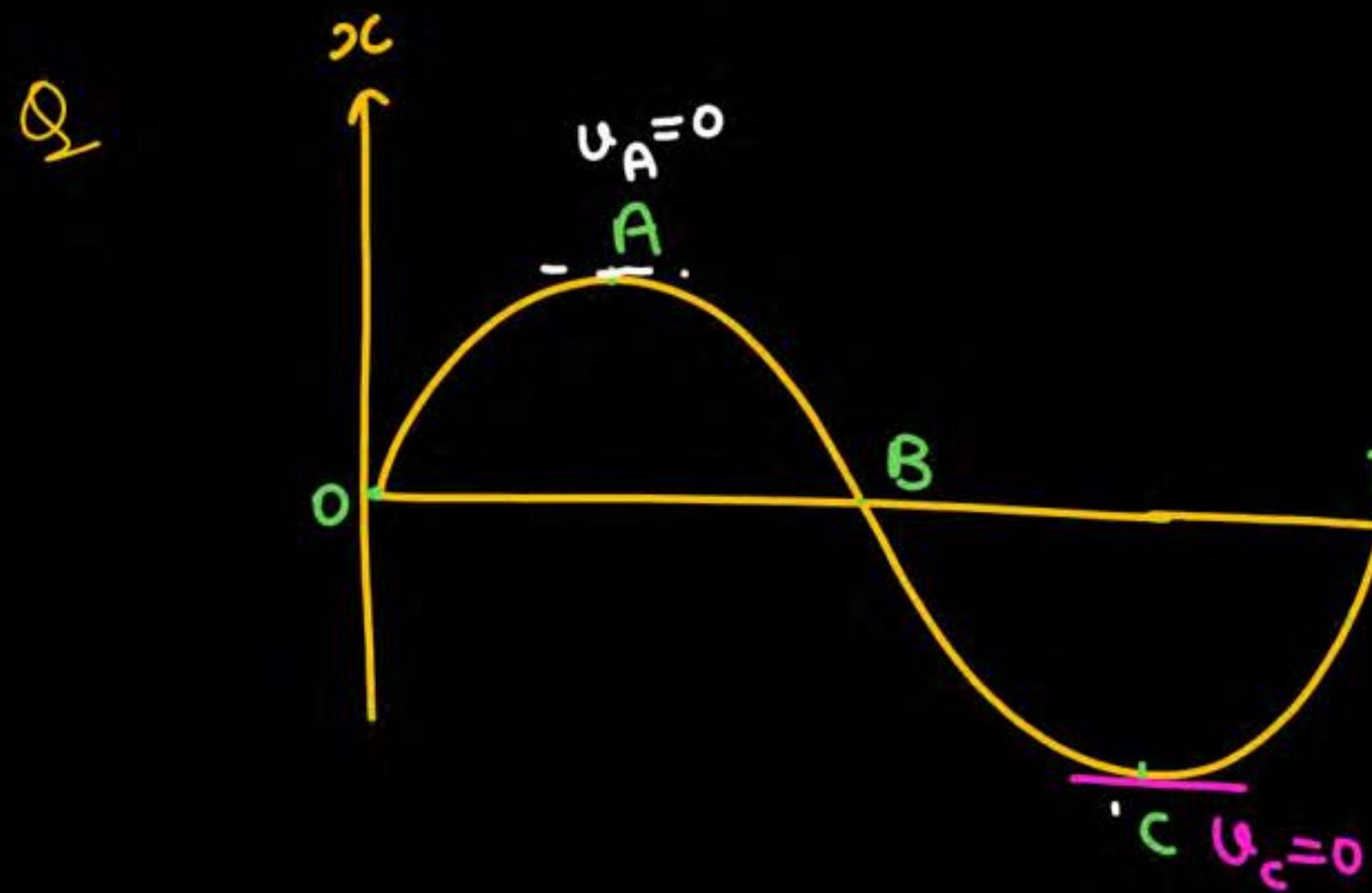
$$v > 0, a < 0$$

t

P
W

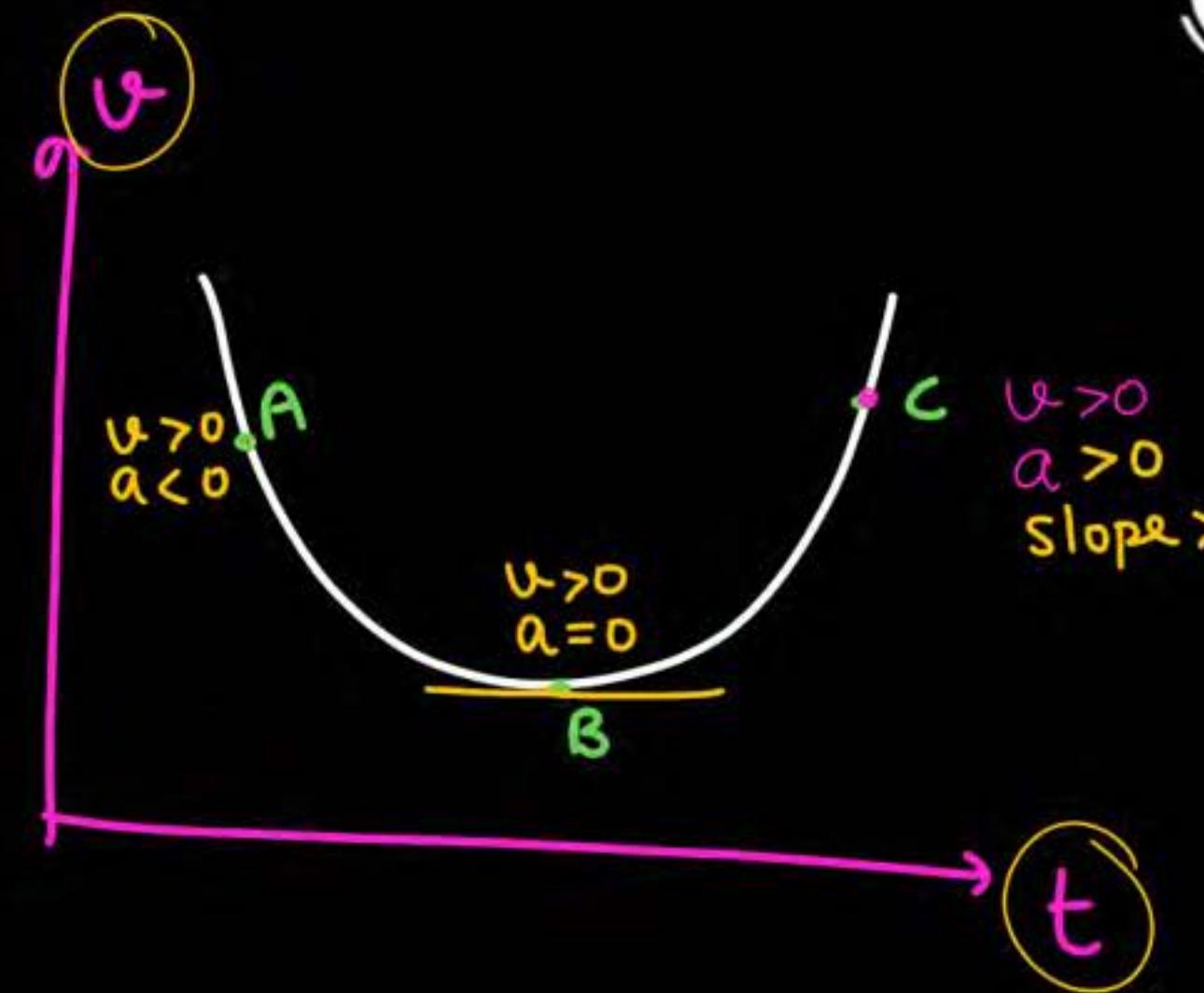
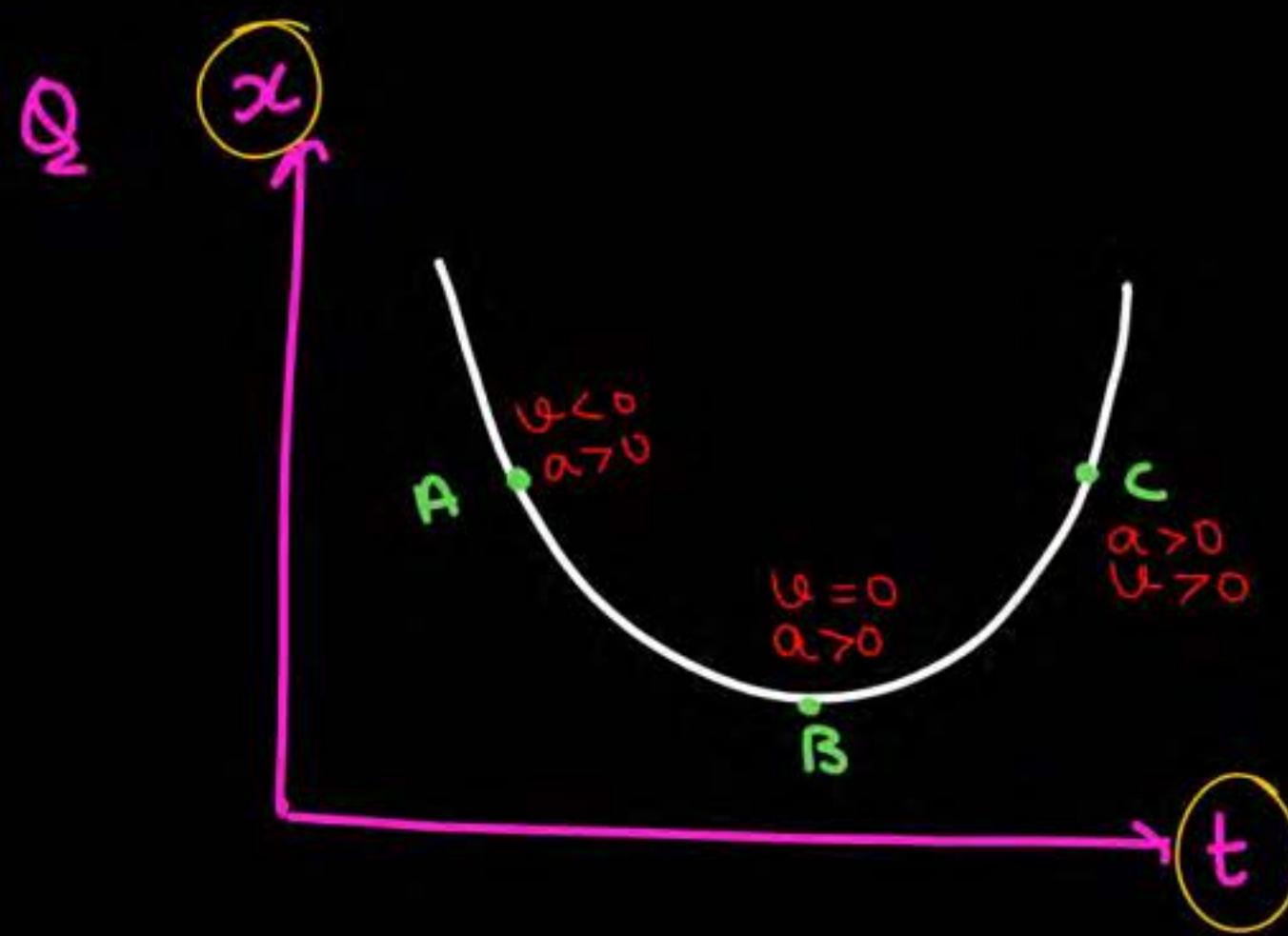


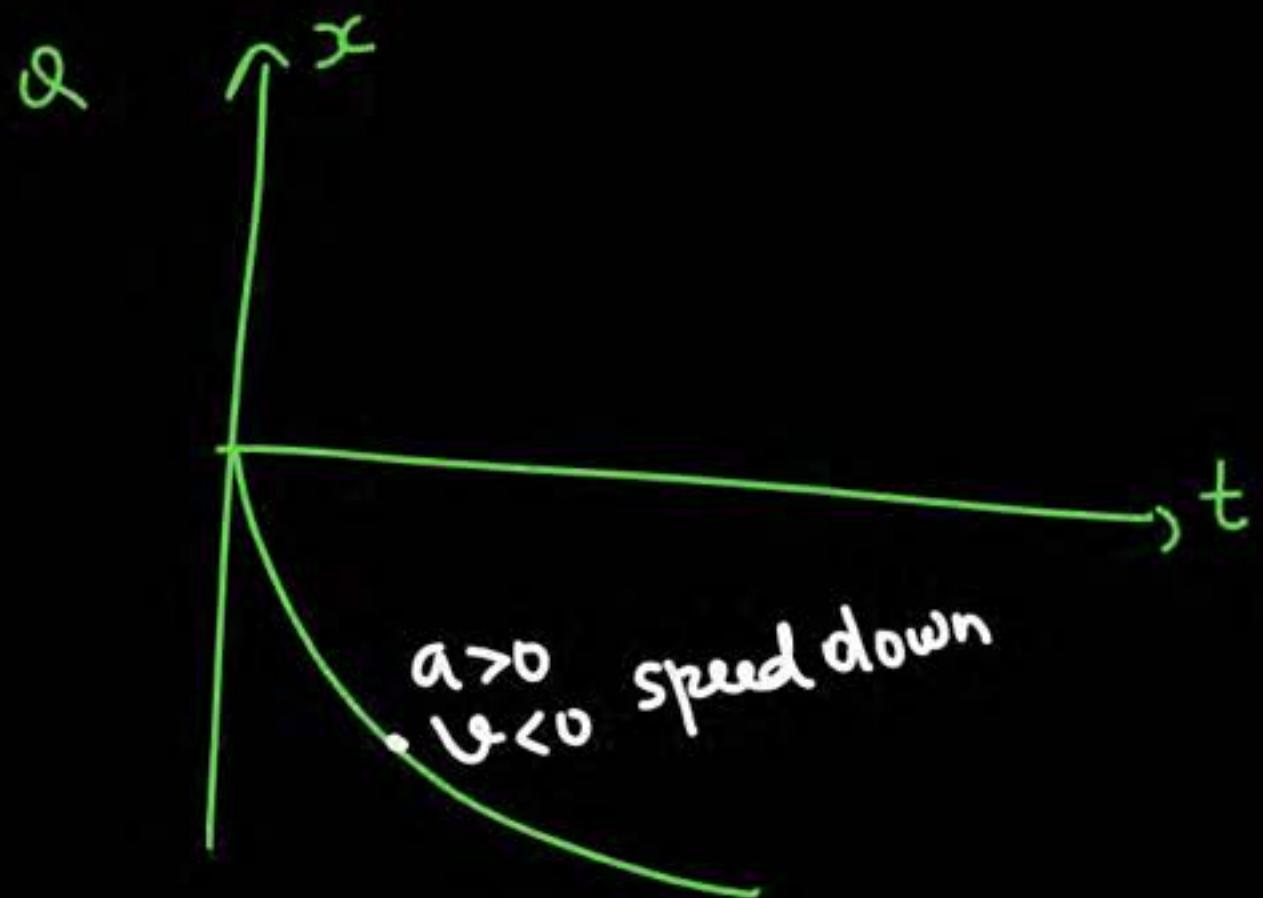
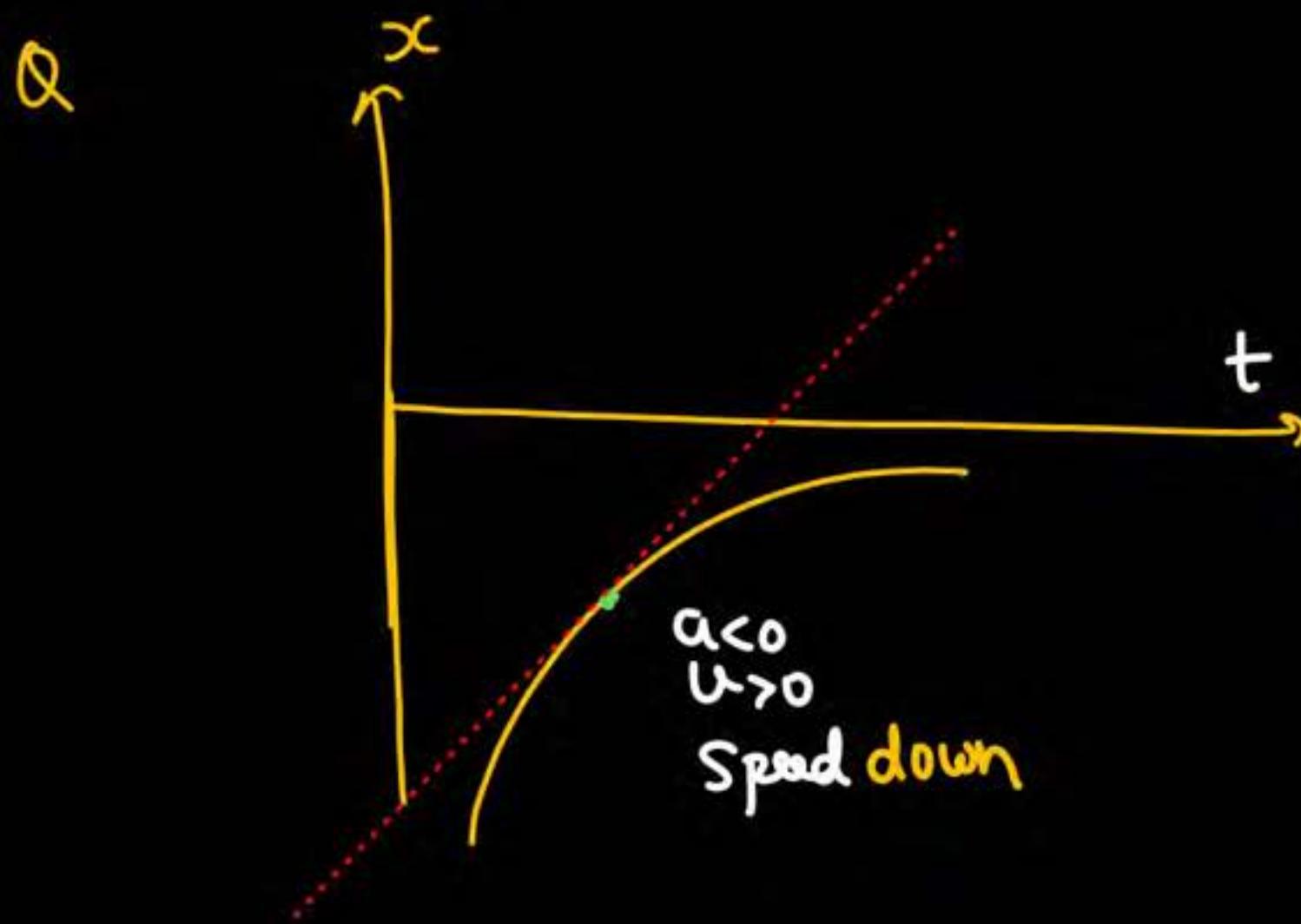
P
W

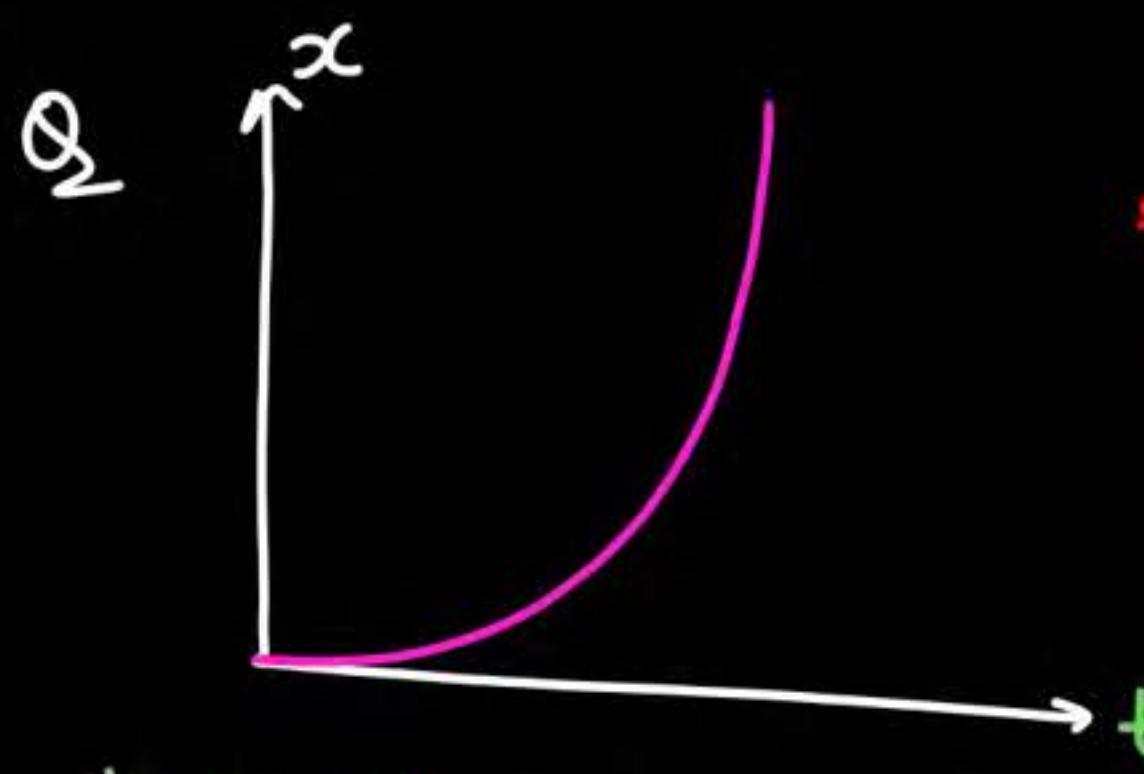


	ω	a	
$O \rightarrow A$	+	-	Speed $\uparrow \downarrow$
$A \rightarrow B$	-	-	Speed \downarrow
$B \rightarrow C$	-	+	Speed \uparrow
$C \rightarrow D$	+	+	Speed \downarrow
			Speed up

P
W



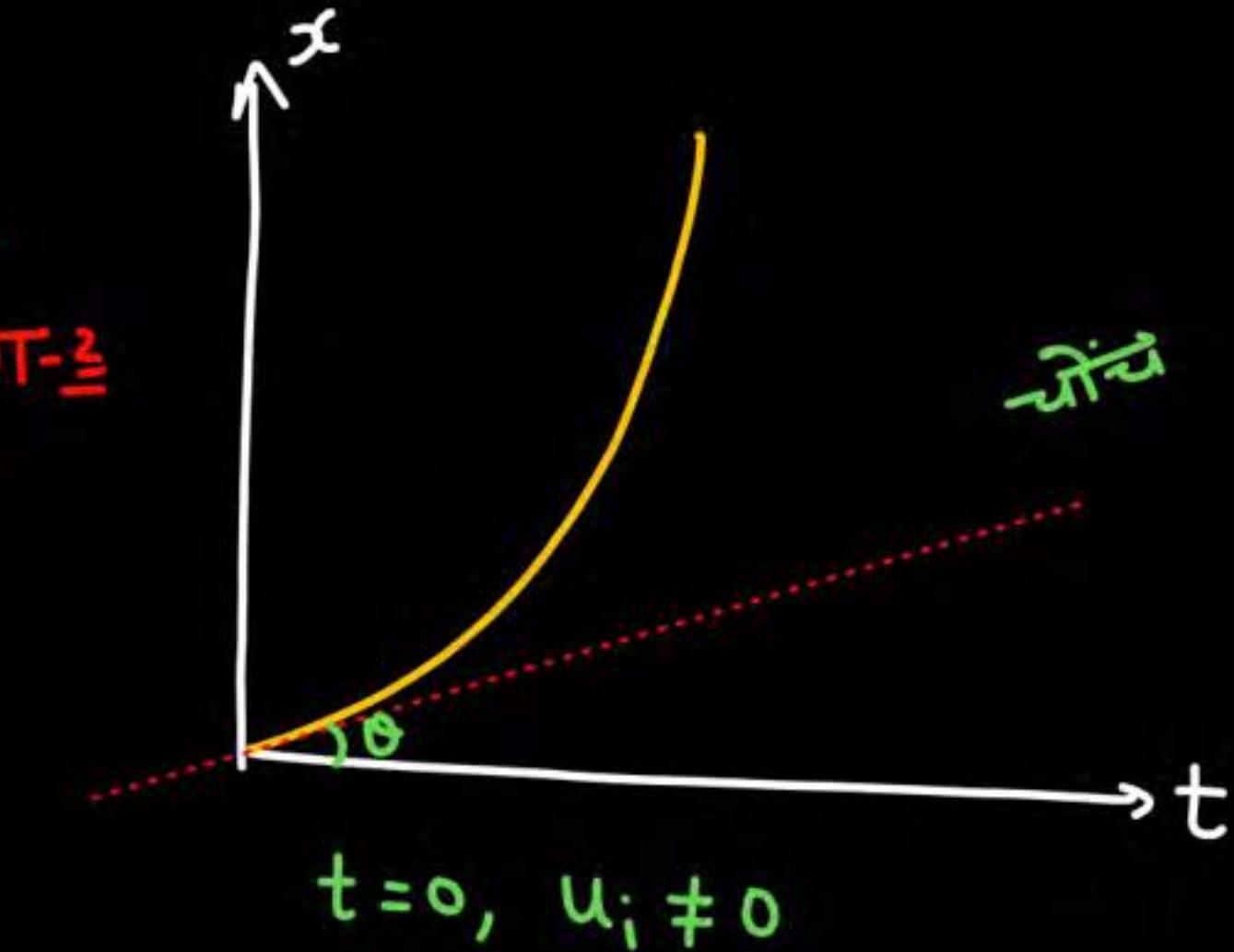




$$t=0, \text{ Slope} = 0 \\ v=0$$

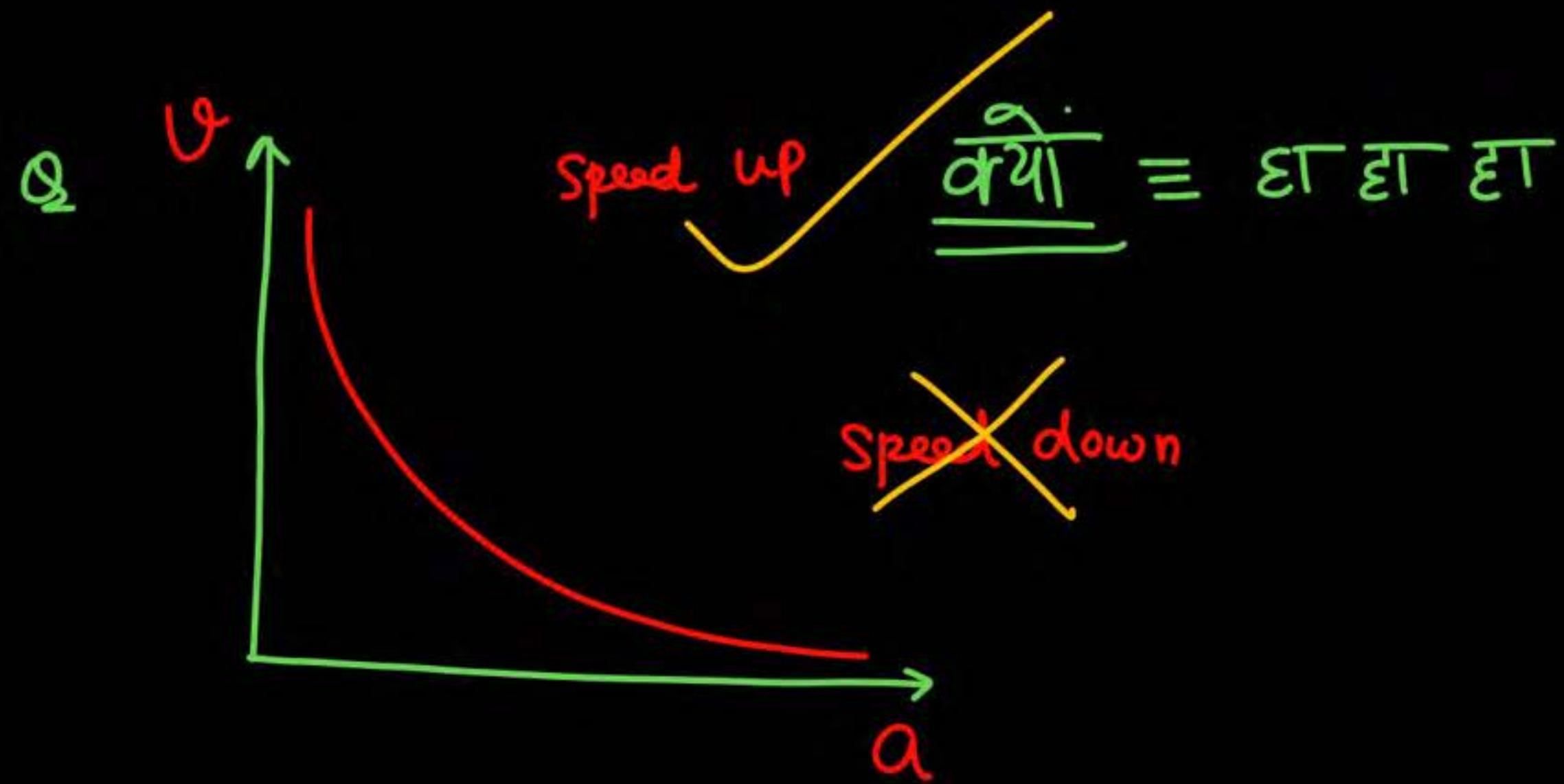
particle start motion from rest.

दिनी
अलग-2
है



$$t=0, v_i \neq 0$$

नोट



Q

$$x = t^2 - 4t + 5$$

find average speed from

SOL

$$\textcircled{1} \quad t=0, x_i = 5$$

$$t=4, x_f = 5$$

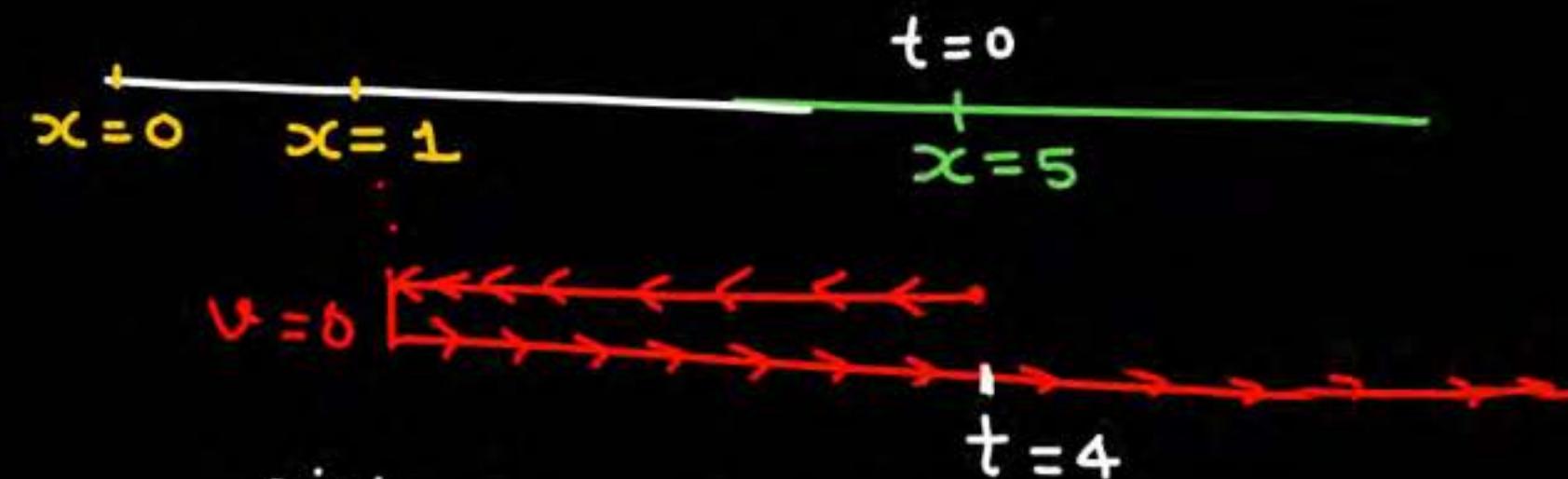
$$\textcircled{2} \quad \begin{array}{l} \text{turning point} \equiv ? \\ v = 0 \end{array}$$

$$v = 2t - 4 = 0$$

$$\boxed{t = 2 \text{ sec}}$$

$$\begin{aligned} t = 2, x &= 2^2 - 4 \times 2 + 5 \\ &= 1 \end{aligned}$$

$$t = 0 \longrightarrow t = 4$$



$$\text{Distance } t=0 \rightarrow t=4 = 4 + 4$$

$$\text{Average speed} = \frac{8}{4} = 2$$

Q $x = t^2 - 2t + 10$

find average speed from $t=0 \longrightarrow t=3$ sec

Solⁿ

$$t=0, x_i = 10$$

$$t=3, x_f = 9 - 6 + 10 = 13$$

$$v = 2t - 2 = 0$$

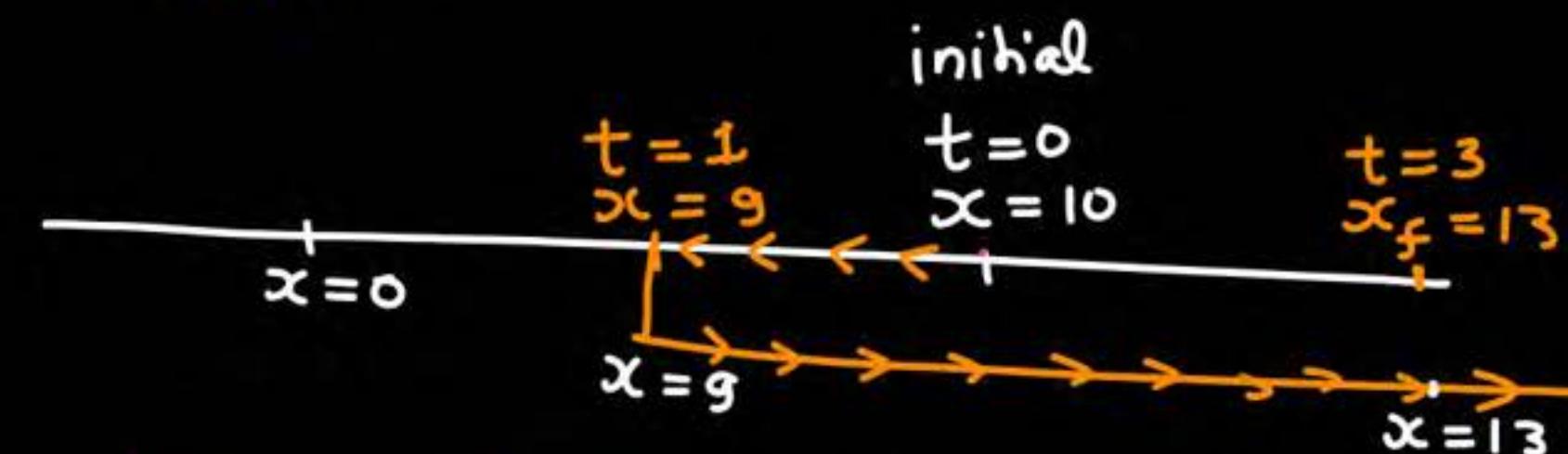
$$2t = 2$$

$$\boxed{t=1}$$

\approx turning point

$$t=1, x = 1^2 - 2 \times 1 + 10$$

$$x = 9$$



Average speed = $\frac{1+4}{3} = \frac{5}{3}$

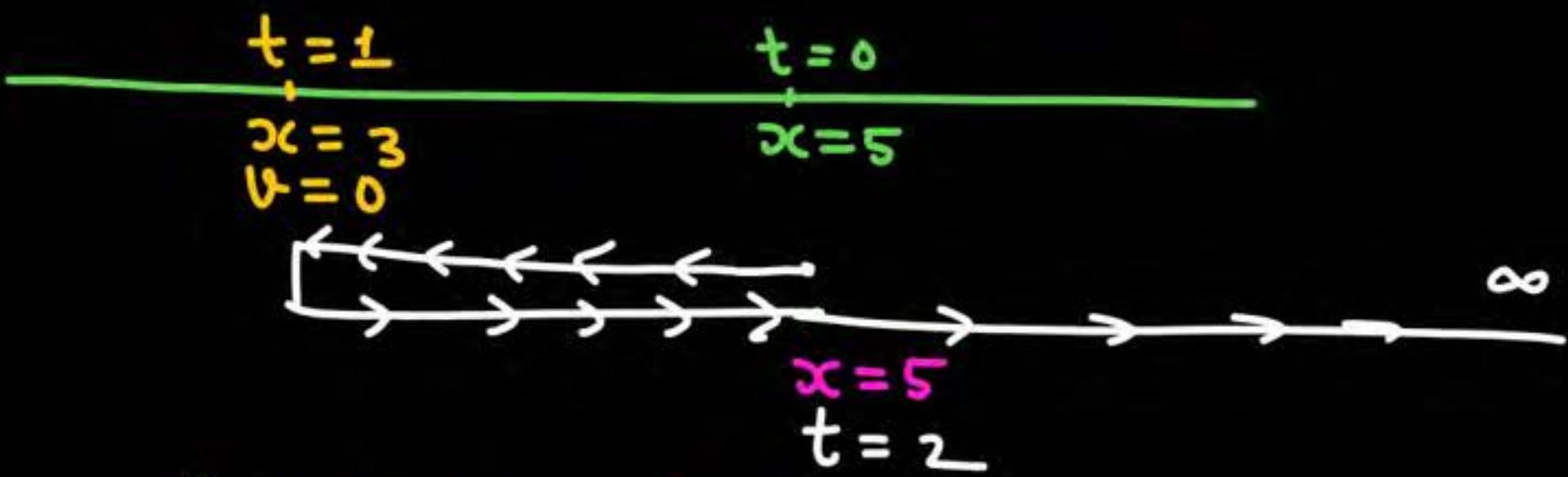
$$\text{Q. } x = 2t^2 - 4t + 5$$

$t=0 \longrightarrow t=2$ average speed = ?

(*) $t=2, x_f = 8 - 8 + 5 = 5$

(**) $v = 4t - 4 = 0$
 $t=1$

$t=1, x = 2 - 4 + 5 = 3$



Avg Speed = $\frac{2+2}{2} = 2$

Q

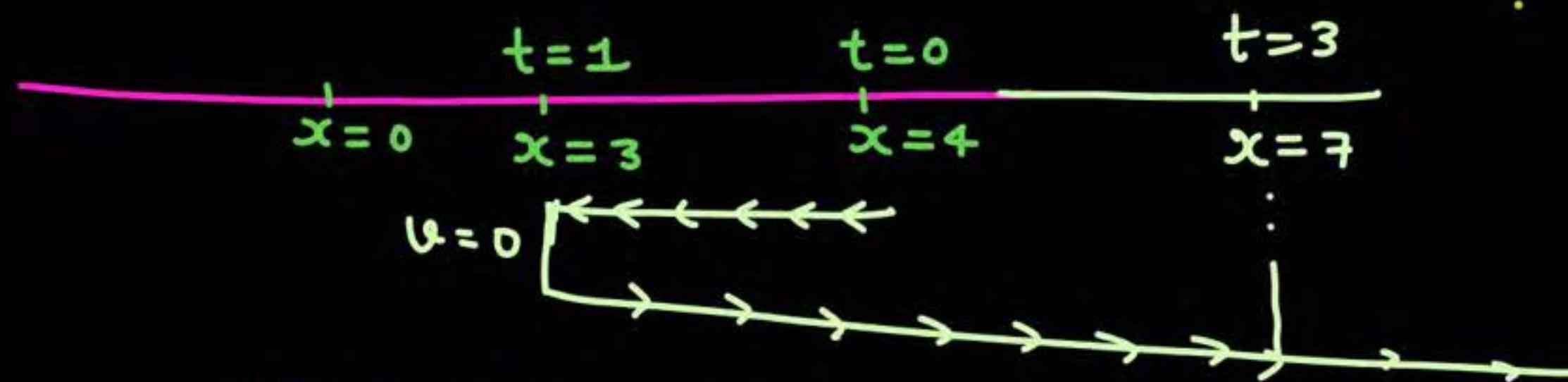
$$x = t^2 - 2t + 4$$

find average speed $t=0 \longrightarrow t=3 \text{ sec}$.

$$v = 2t - 2 = 0$$

$$\boxed{t = 1 \text{ sec}}$$

$$x = 1 - 2 + 4 = 3$$



$$\text{Average velocity} = \frac{1+4}{3} = 5/3$$

$$v = 4t - 4$$

$$\underline{Q} \quad x = 2t^2 - 4t + 2$$

$$t=0 \longrightarrow t=3$$

$$\text{Average Speed} = \frac{2+8}{3} = \frac{10}{3}$$

$$t=0, x=2$$

$$v = 4t - 4 = 0$$

$$(t=1)$$

$$x = 2 - 4 + 2 = 0$$

$$t=3$$

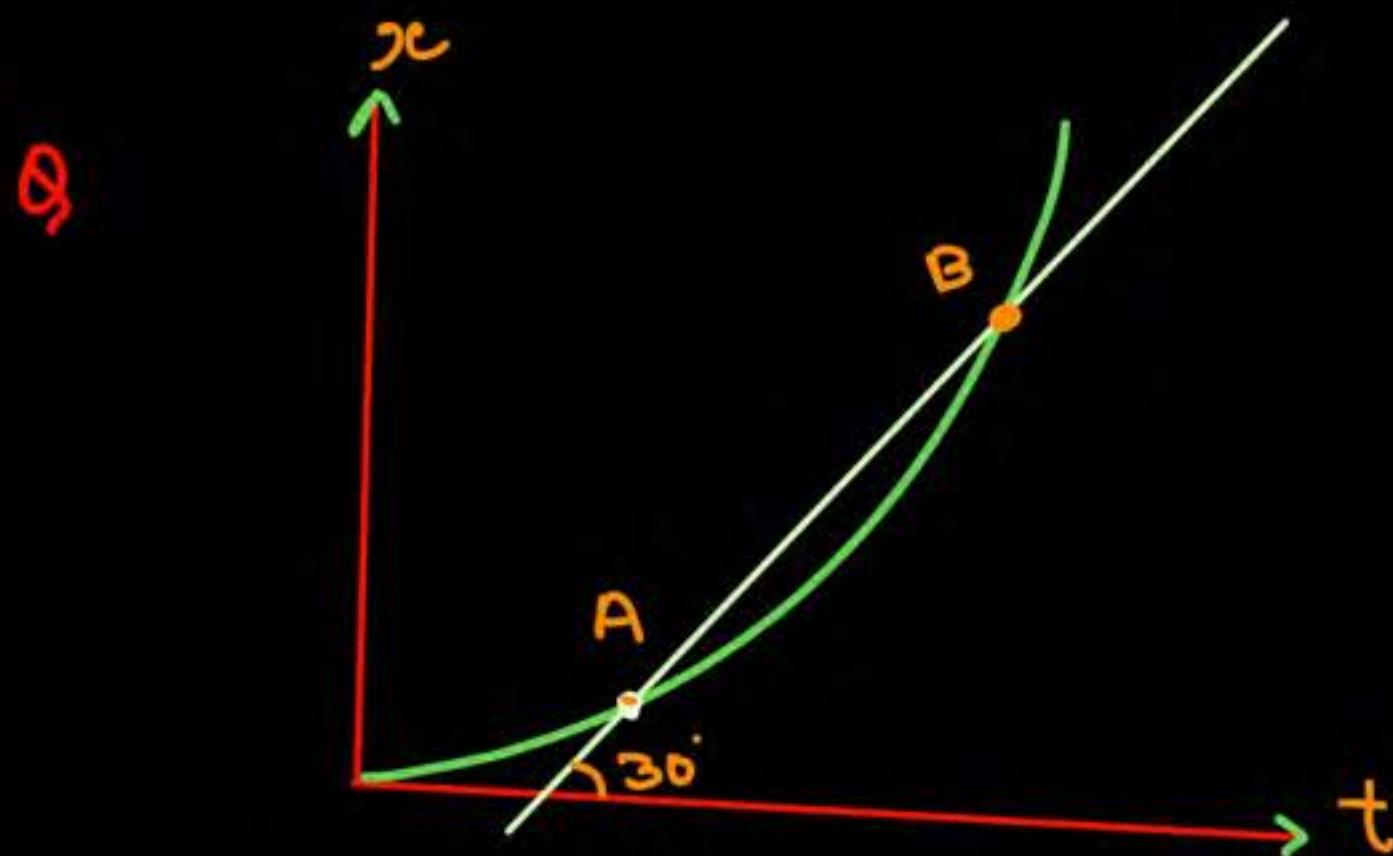
$$x = 18 - 12 + 2 = 8$$

$$t=1 \\ x=0$$

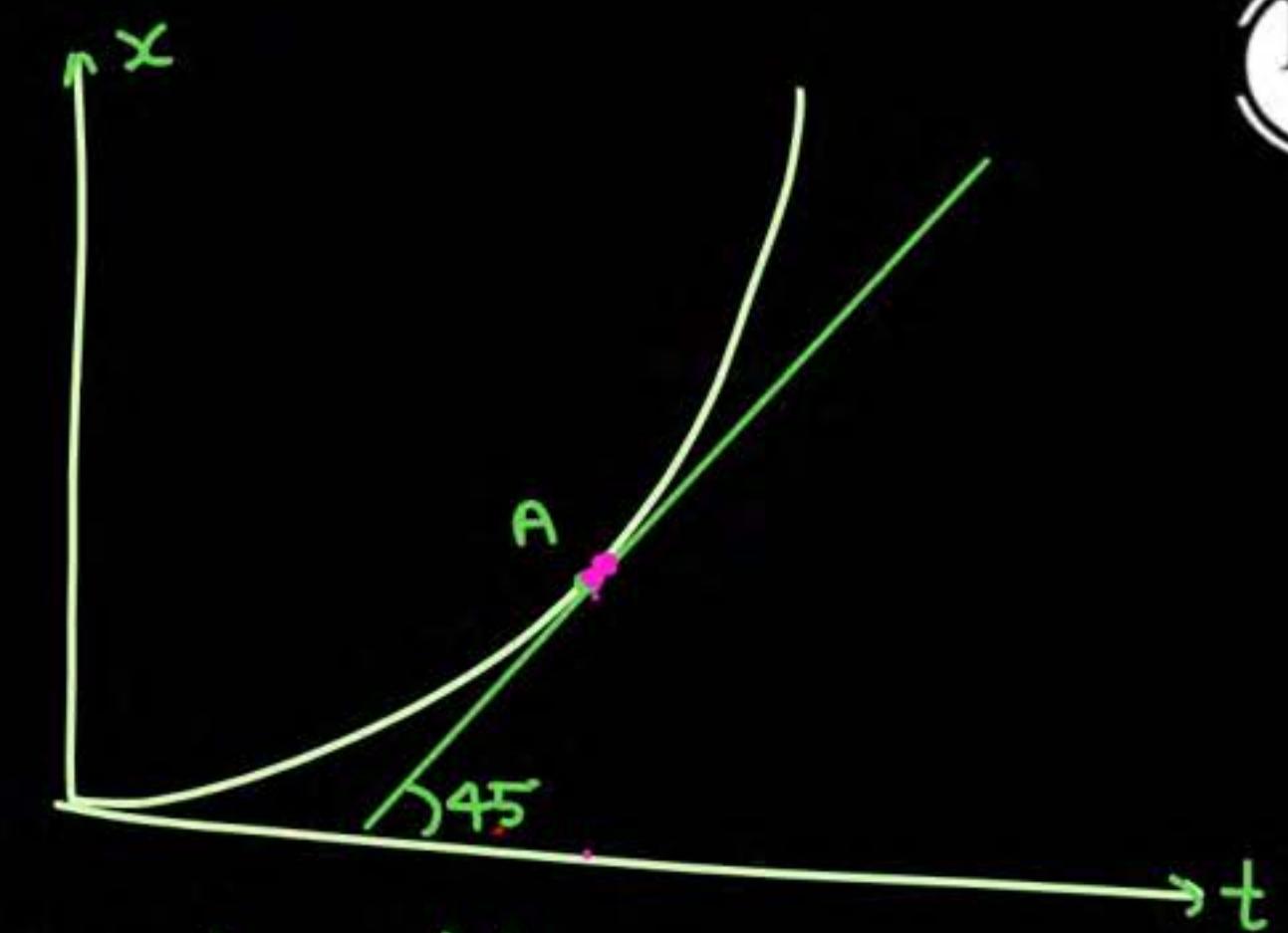
$$t=0 \\ x=2$$

$$t=3 \\ x=8$$



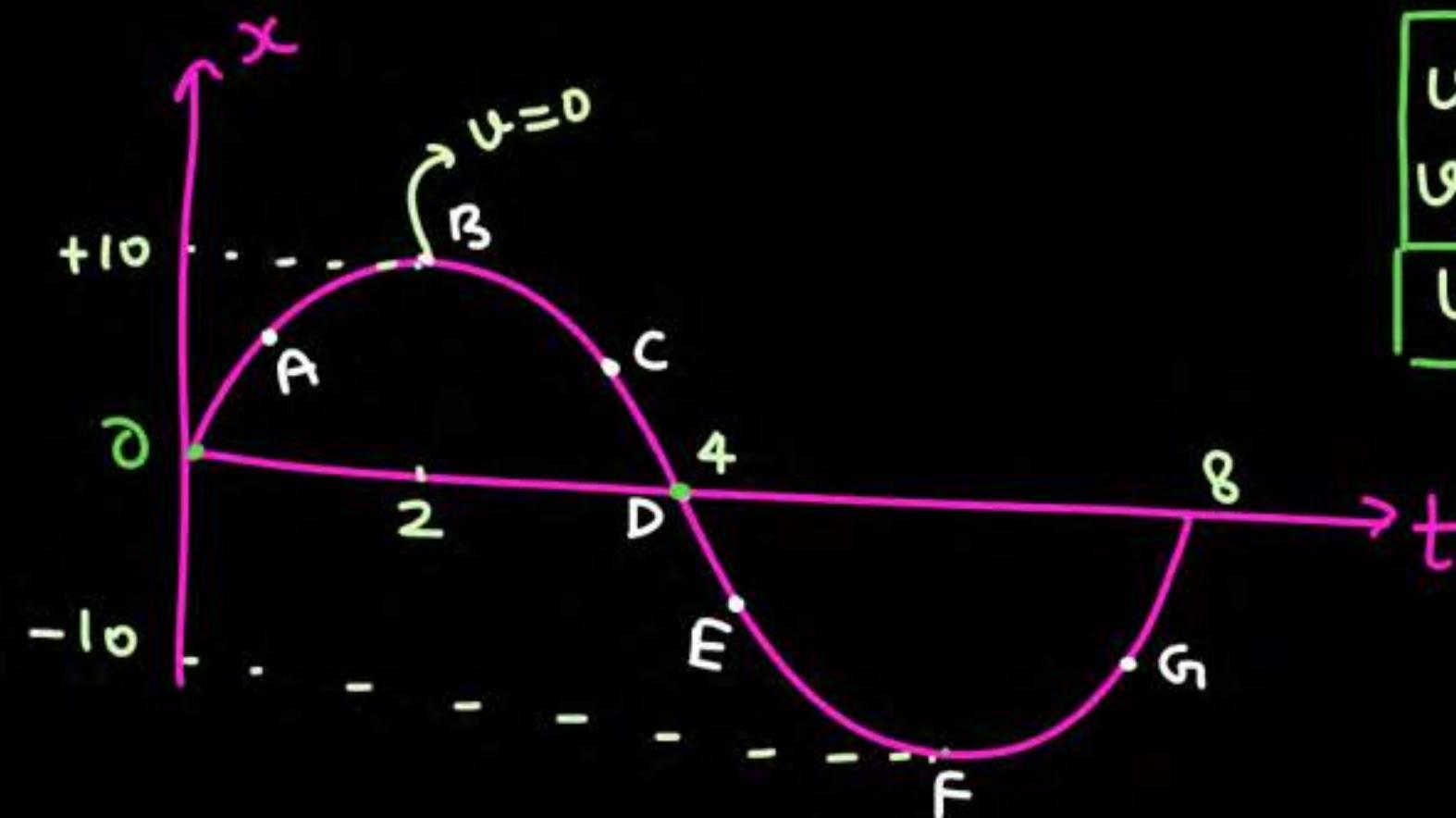


Average velocity \equiv slope of line AB
b/w A & B $= \tan 30^\circ$

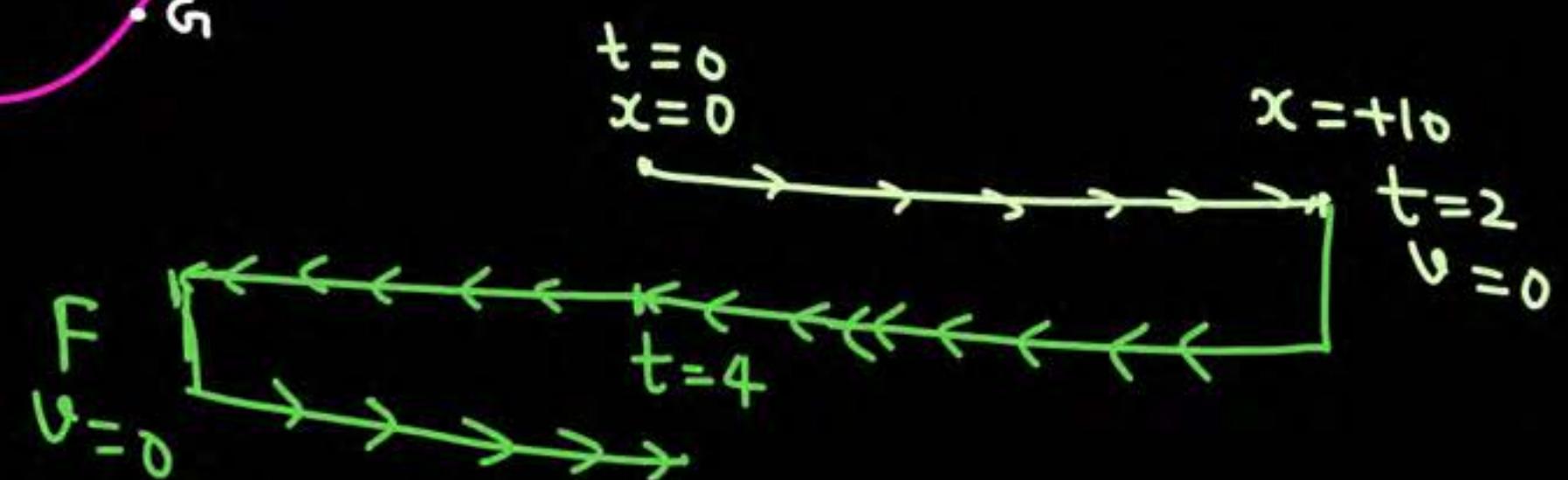


Velocity at 'A' $\equiv \tan 45^\circ = 1$

(4)



$v_A > 0$	$v_G > 0$
$v_B = 0$	$v_F = 0$
$v_C, v_D, v_E \equiv -v_e$	



$$Q \quad v = t^2 + 4t + 10$$

① find acc at $t = 1$ sec

$$a = \frac{dv}{dt} = 2t + 4$$

$$t = 1, \quad a = 2 + 4 = 6$$

② $t = 0 \longrightarrow t = 3$

$$\text{Average acc} = \frac{\vec{v}_f - \vec{v}_i}{\text{total time}}$$

$$t = 3, \quad v_f = 9 + 12 + 10 = 31$$

$$t = 0, \quad v_i = 10$$

$$\text{Avg acc} = \frac{31 - 10}{3 - 0} = 7$$

$$Q_2 \quad x = t^3 + 2t^2 + 5t$$

find velocity & acc at $t=2\text{sec}$

$$v = \frac{dx}{dt} = 3t^2 + 4t + 5, \quad t=2, \quad v = 12 + 8 + 5 = 25$$

$$a = \frac{dv}{dt} = 6t + 4$$

$$t=2, \quad a = 12 + 4 = 16$$

$$\vec{a} = \frac{d\vec{v}}{dt} = \frac{d^2\vec{x}}{dt^2}$$

$$Q_2 \quad x = 4t^2 - 16t + 20$$

find turning point

$$v = 0$$

$$v = \frac{dx}{dt} = 8t - 16$$

$$\boxed{v=0, t=2 \text{ sec}}$$

Unstackable ques

Q₂

$$x = \frac{t^3}{3} - 3t^2 + 9t + 21$$

find turning point

Ans

$$t = 3$$

turning point

21

Q H.W 2 page exis GT

P
W

Q $x = 3t^2 - 12t + 10$

- find
- ① x, v, a at $t=0, t=2, t=3$ sec
 - ② find value of $x \& a$ when particle comes to at rest.
 - ③ find average velocity, average speed, average acc from $t=0$ $\xrightarrow{ } t=3$ sec

Homework

$$\underline{Q} \quad y = \pi x^2$$
$$\frac{dy}{dx} = \pi 2x$$

$$\underline{Q} \quad A = \pi r^2$$
$$\frac{dA}{dr} = \pi 2r$$

$$\underline{Q} \quad y = \pi x^3$$
$$\frac{dy}{dx} = \pi 3x^2$$

$$\underline{Q} \quad V = \left(\frac{4}{3}\pi\right) r^3$$

$$\frac{dV}{dr} = \frac{4\pi}{3} 3r^2$$

$$\textcircled{1} \quad y = t^2 - 4t + 10$$

$$\frac{dy}{dt} = 2t - 4$$

$$\frac{d^2y}{dt^2} = 2 - 0$$

$$\textcircled{2} \quad y = t^3 - 4t^2 + 10$$

$$\frac{dy}{dt} = 3t^2 - 8t + 0$$

$$\frac{d^2y}{dt^2} = 6t - 8$$

$$\textcircled{1} \quad x = t^2 - 4t + 10$$

$$\frac{dx}{dt} = 2t - 4 + 0$$

$$\frac{d^2x}{dt^2} = 2 - 0$$

$$\textcircled{2} \quad \textcolor{blue}{x} = t^3 - 4t^2 + 10$$

$$v = \frac{dx}{dt} = 3t^2 - 8t + 0$$

$$\textcolor{blue}{\frac{d^2x}{dt^2}} = 6t - 8 + 0$$

$$\text{Q} \quad y = \sin x$$

$$\frac{dy}{dx} = \cos x$$

$$\frac{d^2y}{dx^2} = -\sin x$$

$$\text{Q} \quad P = \ln t$$

find $\frac{dP}{dt}$ at $t = 10 \text{ sec}$

$$\frac{dP}{dt} = \frac{1}{t}$$
$$= \frac{1}{10}$$

Q

$$y = x^2 + 3x$$

find

$$\frac{dy}{dx}$$

at $x=4$

~~$y = 16 + 12 = 28$~~

~~$\frac{dy}{dx} = 0$~~

$$\frac{dy}{dx} = 2x + 3$$

$x = 4$

Put

$$\boxed{\begin{aligned}\frac{dy}{dx} &= 2x + 3 \\ &= 2 \times 4 + 3 \\ &= 11\end{aligned}}$$

$$\text{Q} \quad y = x^3$$

find $\frac{dy}{dx}$, at $x=2$

Solⁿ

$$y = x^3$$

$$\frac{dy}{dx} = 3x^2$$

$$\text{at } x=2, \quad \frac{dy}{dx} = 3 \times 2^2$$

$$= 12 \quad \text{Ans}$$

Similarly
find \Rightarrow

$$\text{Q} \quad y = t^2$$

find $\frac{dy}{dt}$ at $t=10 \text{ sec}$

$$\frac{dt}{dt} = 2t \Rightarrow \frac{dy}{dt} = 2 \times 10 = 20$$

*
Ans

$$x = t^2 + 2t$$

find $\frac{dx}{dt}$ at $t=3 \text{ sec}$

$$\frac{dx}{dt} = 2t+2$$

$$\frac{dx}{dt} = 8$$

$$\text{Q} \quad x = t^3 - 2t^2 + 5$$

find $\frac{dx}{dt}$ and $\frac{d^2x}{dt^2}$ at $t=2 \text{ sec}$

d

$$x = t^3 - 2t^2 + 5$$

$$t=2, \frac{dx}{dt} = ?$$

$$\frac{dx}{dt} = 3t^2 - 4t + 0 \quad \text{put}$$

$$\frac{dx}{dt} = 3 \times 2^2 - 4 \times 2 = 12 - 8 = \underline{\underline{4}}$$

$$\frac{d^2x}{dt^2} = 6t - 4$$

$$t=2$$

put

$$\frac{d^2x}{dt^2} = 6 \times 2 - 4 = \underline{\underline{8}}$$

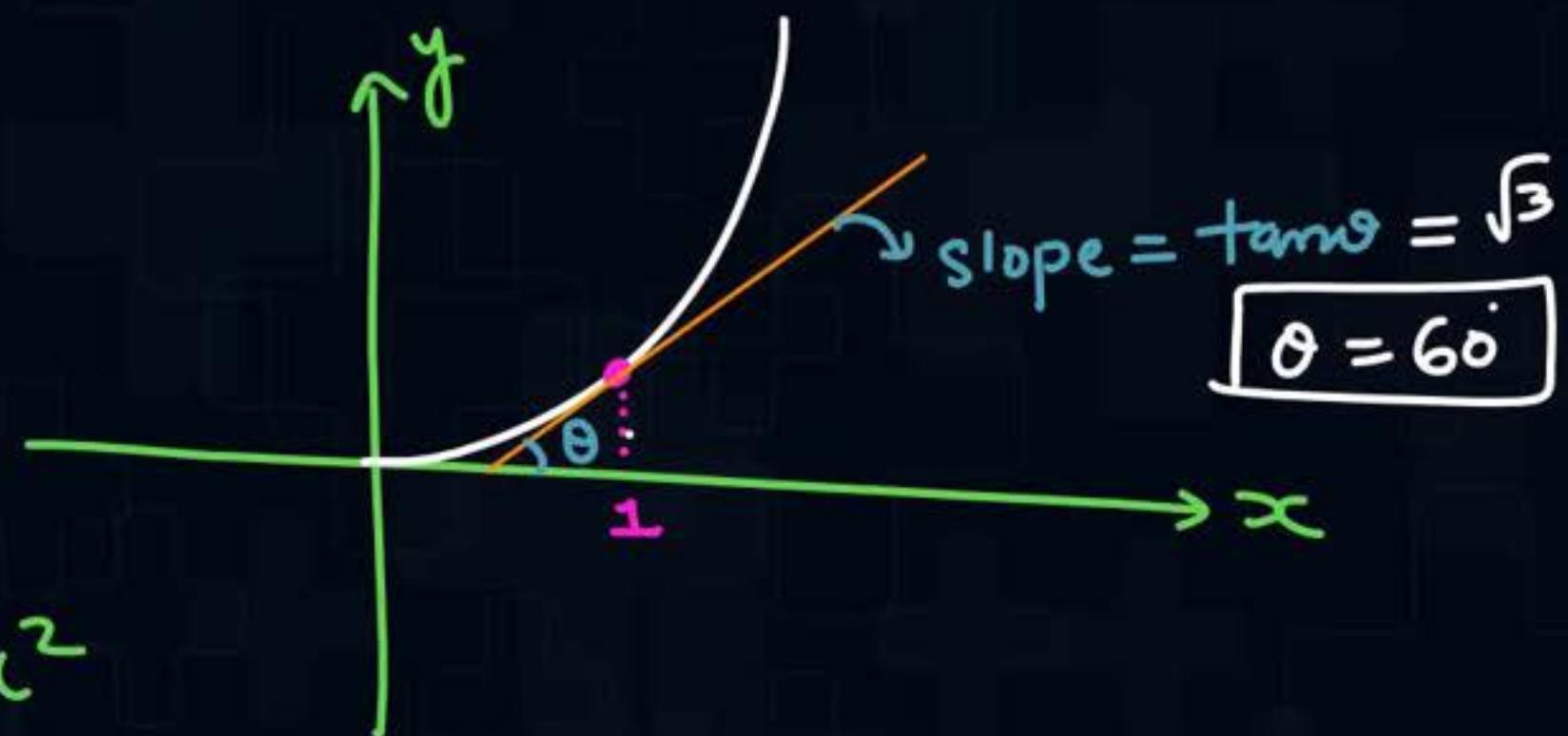
$$\Omega \quad y = \frac{x^3}{\sqrt{3}}$$

find $\frac{dy}{dx}$ at $x=1$

$$\frac{dy}{dx} = \frac{1}{\sqrt{3}} \cdot 3x^2 = \sqrt{3}x^2$$

$$\text{At } x=1 \Rightarrow \frac{dy}{dx} = \frac{3}{\sqrt{3}} \cdot 1^2 = \sqrt{3} = \text{slope}$$

$\frac{dy}{dx} = \text{slope of tangent at that point}$



Q

$$x = t^3 - 4t^2 + 5$$

$$\frac{dx}{dt} \text{ at } t=2 \text{ sec}$$

$$\frac{d^2x}{dt^2} \text{ at } t=2 \text{ sec.}$$

$$\frac{dx}{dt} = 3t^2 - 8t + 0$$

$$\frac{d^2x}{dt^2} = 6t - 8$$

Q

$$x = t^2 - 4t + 20$$

find value of $x, \frac{dx}{dt}, \frac{d^2x}{dt^2}$
at $t = 2 \text{ sec}$

$$\textcircled{1} \quad y = 5x^3$$

$$\begin{aligned}\frac{dy}{dx} &= 5\left(\frac{d}{dx}x^3\right) \\&= 5 \times 3x^2 \\&= 15x^2\end{aligned}$$

$$\textcircled{2} \quad y = Kx^3$$

Const

$$\begin{aligned}y &= K \frac{d(x^3)}{dx} \\y &= Kx(3x^2)\end{aligned}$$

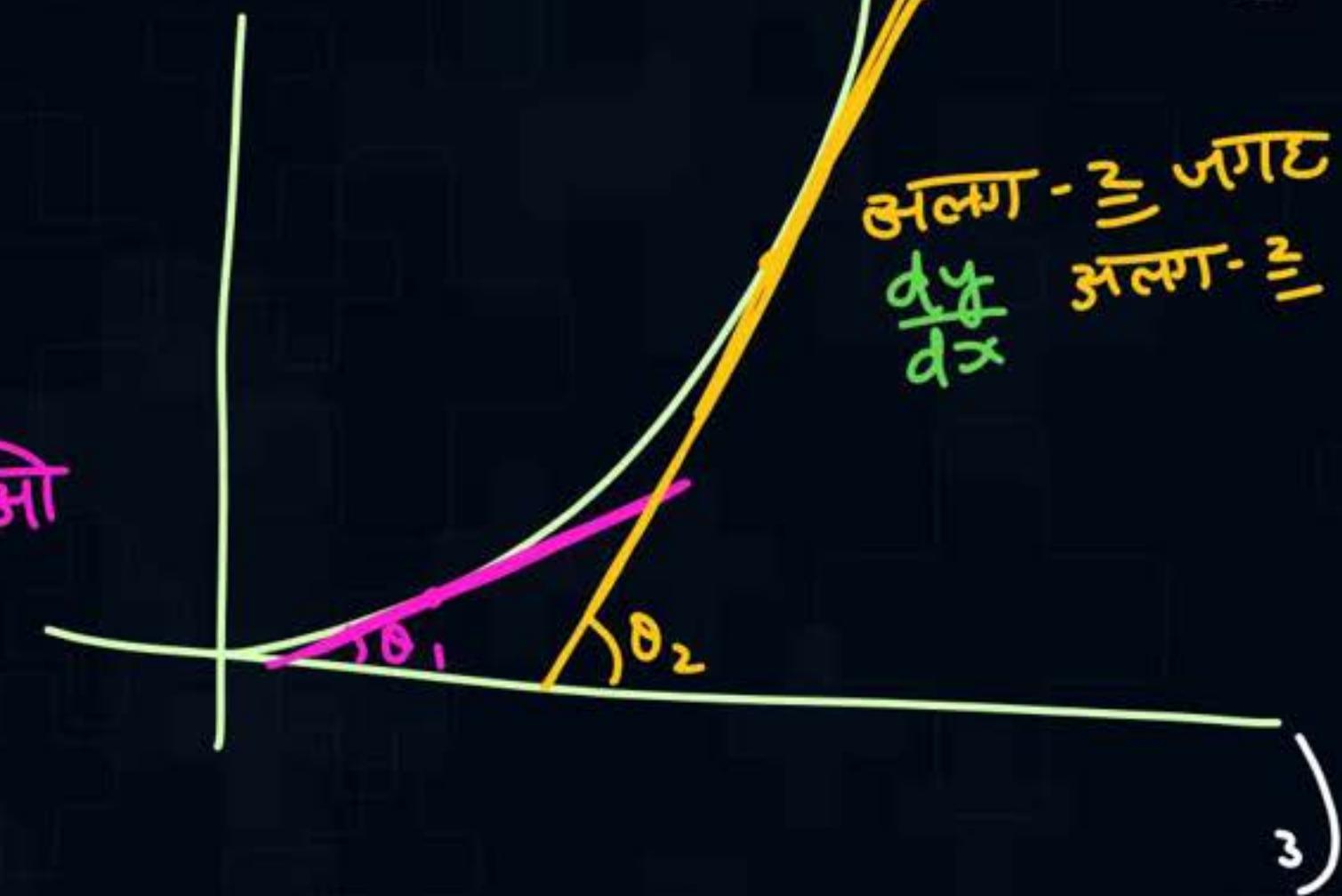
$$\textcircled{3} \quad y = \pi x^3$$
$$\frac{dy}{dx} = \pi 3x^2$$
$$\textcircled{4} \quad y = \pi + x^3$$
$$\frac{dy}{dx} = 0 + 3x^2$$

$$Q \quad y = \frac{x^3}{\sqrt{3}}$$

find $\frac{dy}{dx}$ at $x=1$



"
इस graph में $x=1$ पर tangent बनाओ
अस tangent का slope = $\frac{dy}{dx}$



#

$$y = x^3$$

$$\frac{dy}{dx} = 3x^2$$

differentiation of y wrt x

①

$$y = x^3$$

⇒

$\frac{dy}{dt} \rightarrow$ diff of y wrt time

$$\frac{dy}{dt} = 3x^2 \cdot \frac{dx}{dt}$$

②

$$y = x^5$$

$$\frac{dy}{dt} = 5x^4 \frac{dx}{dt}$$

③

$$y = x^7$$

$$\frac{dy}{dt} = 7x^6 \frac{dx}{dt}$$

④

$$y = 5x^2$$

$$\frac{dy}{dt} = 10x \left(\frac{dx}{dt} \right)$$

$$\textcircled{5} \quad y = \pi x^2$$

$$\frac{dy}{dt} = \pi 2x \cdot \frac{dx}{dt}$$

$$\textcircled{6} \quad A = \pi r^2$$

$$\frac{dA}{dr} = \pi 2r$$

$$\textcircled{7} \quad A = \pi r^2$$

$$\frac{dA}{dt} = \pi 2r \cdot \frac{dr}{dt}$$

$$\textcircled{8} \quad y = \pi x^2$$

$$\frac{dy}{dx} = \pi 2x$$

$$\textcircled{9} \quad y = \frac{4}{3}\pi x^3$$

$$\frac{dy}{dx} = \frac{4}{3}\pi 3x^2$$

$$\frac{dy}{dt} = \frac{4}{3}\pi 3x^2 \left(\frac{dx}{dt} \right)$$

$$\textcircled{10} \quad y = \sin x$$

$$\frac{dy}{dx} = \cos x$$

$$\frac{dy}{dt} = \cos x \frac{dx}{dt}$$

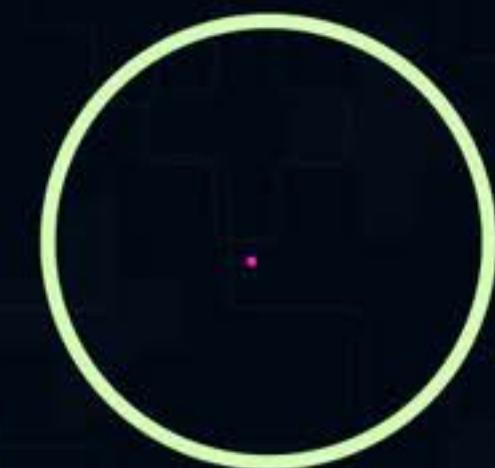
Q

Radius of a circle increases wrt time with the rate of +5 m/sec.
 find rate of change of area wrt time when radius is 10m.

$$A = \pi r^2$$

$$? = \frac{dA}{dt} = \pi 2r \frac{dr}{dt}$$

$$\frac{dr}{dt} = 5, r = 10$$



$\frac{dy}{dx} \rightarrow$ Rate of change of y wrt x

$\frac{dA}{dt} \rightarrow$ Rate of change of Area
wrt time

$\frac{dr}{dt} \rightarrow$ Rate of change of radius
wrt time

$$\frac{dA}{dt} = \pi \cdot 2 \cdot 10 \cdot 5 = 100\pi$$

Q If radius of a sphere is increasing at the rate of 10 m/sec,
at what rate vol' of sphere will change, when radius is 3 m.

$$V = \frac{4}{3}\pi r^3$$

$$\frac{dv}{dt} = \frac{4\pi}{3} 3r^2 \frac{dr}{dt}$$

$$\frac{dv}{dt} = \frac{4\pi}{3} \cdot 3(3)^2 \times 10 = \underline{\underline{360\pi}}$$

1

Q A particle is moving on X-axis such that its x-co-ordinate w.r.t time changes as

$$x = t^2 - 4t + 10$$

① find velocity at $t = 3 \text{ sec}$

$$v = \frac{dx}{dt} = 2t - 4 + 0$$

$$t=3, v = 2 \times 3 - 4 = 2$$

$$v = 2 \text{ m/s}$$

② find velocity at $t = 4 \text{ sec}$

$$v = 2t - 4 \quad \text{put}$$

$$v = 2 \times 4 - 4$$

$$v = 4$$

③ find initial velocity = at $t = 0$

$$v = 2t - 4$$

$$t=0, v = 0 - 4 = -4$$

$$Q \quad x = t^2 - 6t + 10$$

① find velocity at $t=0, t=3, t=6$ sec = Inst. velocity

$$v = 2t - 6$$

$$t=0, v = -6$$

$$t=3, v = 0$$

$$t=6 \quad v = 2 \times 6 - 6$$

$$v = +6.$$

② find average velocity $t=0 \rightarrow t=3$

$$\text{Avg velocity} = \frac{x_f - x_i}{t_2 - t_1}$$

$$t=0, x_i = 0 - 0 + 10$$

↳ $x_i = 10$

$$t=3, x_f = 3^2 - 6 \times 3 + 10 = 1$$

$$\text{Avg velocity} = \frac{1 - 10}{3 - 0} = -3$$

H1*

③ find average speed
from $t=0 \rightarrow t=4$

$$Q \quad x = t^2 - 4t + 5$$

① find velocity at $t=0, t=2, t=4$ sec

$$v = \frac{dx}{dt}$$

$$v = 2t - 4$$

$$\boxed{t=0, v=-4}$$

$$\boxed{t=2, v=0}$$

$$\boxed{t=4, v=4}$$

② find average velocity from $t=0$ to $t=4$ sec

$$t=0, x_i = 5$$

$$t=4, x_f = \cancel{t^2} - 4 \times 4 + 5 = 5$$

$$\text{Avg velocity} = \frac{x_f - x_i}{\text{duration}} = \frac{5-5}{4} = 0$$

$$\textcircled{1} \quad y = x^n$$

$$\frac{dy}{dx} = \frac{d x^n}{dx} = n x^{n-1}$$

$$\textcircled{3} \quad y = x^{-5}$$

$$\frac{dy}{dx} = -5 x^{-5-1} = -5 \cdot x^{-6}$$

$$\frac{dy}{dx} = \frac{-5}{x^6}$$

$$\textcircled{1} \quad y = x^5$$

$$\frac{dy}{dx} = 5 x^{5-1} = 5 x^4$$

$$\textcircled{2} \quad y = x^7$$

$$\frac{dy}{dx} = 7 x^6$$

$$\textcircled{4} \quad y = \frac{1}{x^2} = x^{-2}$$

$$\frac{dy}{dx} = -2x^{-2-1} = \frac{-2}{x^3}$$

$$f(x) = g(x) \pm h(x)$$

$$\frac{d}{dx} f(x) = \frac{d}{dx} g(x) \pm \frac{d}{dx} h(x)$$

$$\textcircled{5} \quad y = x^2 + x^5$$

$$\frac{dy}{dx} = 2x + 5x^4$$

$$\textcircled{7} \quad y = x^7 + x^8$$

$$\frac{dy}{dx} = 7x^6 + 8x^7$$

$$\textcircled{6} \quad y = x^3 - x^4$$

$$\frac{dy}{dx} = 3x^2 - 4x^3$$

$$\textcircled{8} \quad y = x^9 + \frac{1}{x^5}$$

$$\frac{dy}{dx} = 9x^8 - \frac{5}{x^6}$$

$y = x^6$

$\frac{dy}{dx} = 6x^5$

$$y = x^8$$

$$y' = \frac{dy}{dx} = 8x^7$$

$y = u \pm v$
$y' = u' \pm v'$

Q $y = x^3 + x^8$

$$\frac{dy}{dx} = 3x^2 + 8x^7$$

diff of y wrt x

Q $y = t^3 + t^8$

$$\frac{dy}{dt} = 3t^2 + 8t^7$$

diff of y wrt t

$$\text{Q} \quad y = 5x^3$$

$$\frac{dy}{dx} = 5 \times 3x^2 = 15x^2$$

$$\text{Q} \quad y = 4x^2$$

$$y' = 8x$$

$$\text{Q} \quad y = 3x^7$$

$$y' = \frac{dy}{dx} = 21x^6$$

$$\text{Q} \quad y = 2x^2 + 4x^3 + 6x^7$$

$$y' = 4x + 12x^2 + 42x^6$$

$$\text{Q} \quad y = x = x^1$$

$$\frac{dy}{dx} = 1 \cdot x^{1-1} = 1$$

$$y = x$$

$$\frac{dy}{dx} = 1$$

$$\text{Q} \quad y = 4x$$

$$\frac{dy}{dx} = 4 \cdot 1 = 4$$

#. $y = 5$

$$\frac{dy}{dx} = 0$$

$$y = C \text{ const}$$

$$\frac{dy}{dx} = 0, \quad \frac{d(\text{const})}{dx} = 0$$

. 8. $y = x^3 + 2x^5 + 7$

$$\frac{dy}{dx} = 3x^2 + 10x^4$$

. 9. $y = x^5 - x^4 + 2$

$$\frac{dy}{dx} = 5x^4 - 4x^3 + 0$$

All differentiation formulae Notes + (एक अलग पार्श्व)

P
W

* $\frac{d}{dx}(x^n) = n x^{n-1}$

* $\frac{d}{dx} \tan x = \sec^2 x$

* $\frac{d}{dx}(\ln x) = \frac{1}{x}$

* $\frac{d}{dx}(\text{const}) = 0$

* $\frac{d}{dx} \sec x = \sec x \tan x$

$\ln x = \log_e x$

* $\frac{d}{dx}(\sin x) = \cos x$

* $\frac{d}{dx} \cot x = -\operatorname{cosec}^2 x$

* $\frac{d}{dx}(\cos x) = -\sin x$

* $\frac{d}{dx} \operatorname{cosec} x = -\operatorname{cosec} x \cdot \cot x$

(*) $\frac{d}{dx} e^x = e^x$

$$Q \quad y = x^3 + \sin x$$

$$\frac{dy}{dx} = 3x^2 + \cos x$$

$$Q \quad y = x^7 + \tan x + 10$$

$$\frac{dy}{dx} = 7x^6 + \sec^2 x + 0$$

$$Q \quad y = \sin 30 = \frac{1}{2} = \text{const}$$

~~$$\frac{dy}{dx} = \cos 30 = \frac{\sqrt{3}}{2}$$~~

$$\frac{dy}{dx} = 0$$

$$Q \quad y = 3x^3 + \sin x + \tan x$$

$$\frac{dy}{dx} = 9x^2 + \cos x + \sec^2 x$$

$$Q \quad y = 2x^2 + \cos x + 5$$

$$\frac{dy}{dx} = 4x - \sin x + 0$$

$$y = \tan 45^\circ = 1$$

$$\frac{dy}{dx} = 0$$

$$Q \quad y = 3x^2 + \cos x + e^x - \sin x + 10$$

$$\frac{dy}{dx} = 6x - \sin x + e^x - \cos x + 0$$

$$\text{Q} \quad y = x^3 + \sin x$$

$$\frac{dy}{dx} = 3x^2 + \cos x$$

$$y = u \cdot v \\ y' = uv' + vu'$$

$$\text{Q} \quad y = x^3 \cdot \sin x$$

$$\frac{dy}{dx} = x^3 \left(\frac{d}{dx} \sin x \right) + \sin x \left(\frac{d}{dx} x^3 \right)$$

$$\frac{dy}{dx} = x^3 \cos x + [\sin x] \cdot 3x^2$$

$$\text{Q} \quad y = x^5 \tan x$$

$$\frac{dy}{dx} = x^5 \sec^2 x + [\tan x] (5x^4)$$

$$Q \quad y = x^3 e^x$$

$$\frac{dy}{dx} = x^3 e^x + e^x \cdot 3x^2$$

$$Q \quad y = e^x \cdot \sin x$$

$$\frac{dy}{dx} = e^x \cos x + \sin x \cdot e^x$$

$$Q \quad y = x^4 \ln x$$

$$\frac{dy}{dx} = x^4 \cdot \frac{1}{x} + (\ln x) (4x^3)$$

$$Q \quad y = e^x \cdot \cos x$$

$$\frac{dy}{dx} = e^x (-\sin x) + (\cos x) (e^x)$$

imp नहीं है phy के point of view से (skip) may ✓

$$\frac{10}{2} = 10 \times \left(\frac{1}{2}\right)$$



$$y = \frac{u}{v}$$

$$y' = \frac{vu' - uv'}{v^2}$$

Q $y = \frac{x^5}{\sin x}$

$$y' = \frac{(\sin x) \cdot 5x^4 - x^5 \cdot \cos x}{(\sin x)^2}$$

Q(m-z) product के form में ले जाकर diff कर दो

$$y = x^5 \cdot \csc x$$

$$y' = x^5 \cdot (-\csc x \cdot \cot x) + \csc x \cdot 5x^4$$

$$= \frac{\sin x}{\sin x} \frac{5x^4}{\sin x} - \frac{x^5}{\sin x} \frac{\cos x}{\sin x} = \frac{\sin x 5x^4 - x^5 \cos x}{\sin^2 x}$$

same

Chain rule

$$Q \quad y = \sin(x^2 + x^7)$$

$$\frac{dy}{dx} = \cos(x^2 + x^7) \times (2x + 7x^6)$$

$$Q \quad y = \cos(x^3)$$

$$\frac{dy}{dx} = -\sin(x^3) \cdot 3x^2$$

Book

$$y = f(g(x))$$

$$y' = f'(g(x)) \cdot g'(x)$$

$$y = f(\sqrt{x})$$

$$y' = f'(\sqrt{x}) \cdot (\sqrt{x})'$$

$$\text{Q} \quad y = \ln x^5$$

$$\frac{dy}{dx} = \frac{1}{x^5} \cdot 5x^4$$

$$\text{B} \quad y = \ln x^4$$

$$\frac{dy}{dx} = \frac{1}{x^4} \cdot 4x^3$$

$$\alpha \quad y = \ln(\sin x)$$

$$\frac{dy}{dx} = \frac{1}{\sin x} \cdot \cos x$$

$$\text{Q} \quad y = \tan^2 x = (\tan x)^2$$

$$y = (2 \tan x) \cdot \sec^2 x$$

$$\text{Q} \quad y = \cos^5 x$$

$$\frac{dy}{dx} = 5 \cos^4 x \times (-\sin x)$$

$$\textcircled{1} \quad y = \sin^3 x = (\sin x)^3$$

$$\frac{dy}{dx} = 3(\sin x)^2 \cdot \cos x.$$

$$\textcircled{2} \quad y = \sin^4 x = (\sin x)^4$$

$$\frac{dy}{dx} = 4(\sin x)^3 \cdot \cos x$$

$$\textcircled{3} \quad y = \ln(\sqrt{x})$$

$$\frac{dy}{dx} = \frac{1}{\sqrt{x}} \cdot \left(\text{कदर का differentiation} \right)$$

$$y = x^3$$

$$\frac{dy}{dx} = 3x^2$$

$$y = f(g(x)) \Rightarrow y' = f'(g(x)) \cdot (g(x))'$$

पहले अंदर का वाले को कादू मानकर बाहर का वाले का differentiation करो।

Q $y = \ln(x^2 + x^3)$

$$\frac{dy}{dx} = \frac{1}{x^2 + x^3} \times [2x + 3x^2]$$

Q $y = \sin(x^2 + x^3)$

$$\frac{dy}{dx} = \cos(x^2 + x^3) (2x + 3x^2)$$

Q $y = \tan x^3$

$$\frac{dy}{dx} = \sec^2(x^3) \times 3x^2$$

$$\text{Q } y = \ln(\sin x^3)$$

$$\frac{dy}{dx} = \frac{1}{\sin x^3} \times \cos(x^3) \times [3x^2]$$

$$\text{Q } y = e^{x^3}$$

$$y = e^{x^3} \times 3x^2$$

$$\text{Q } y = \sin(e^x)$$

$$y = \cos(e^x) \cdot e^x$$

Q Imp. for physio

$$y = \sin\left(5x + \frac{\pi}{3}\right)$$

$$\frac{dy}{dx} = \cos\left(5x + \frac{\pi}{3}\right) (5 + 0)$$



SHM \Rightarrow (5-6) month waves

$y = A \cdot \sin(\omega t + \phi)$

$(A, \omega, \phi \rightarrow \text{const})$

$\frac{dy}{dx} = A [\cos(\omega t + \phi)] [\omega + 0]$

P
W

$$\textcircled{Q} \quad y = 5 + x \quad ; \quad y = 5x$$

$$\frac{dy}{dx} = 0+1 \quad ; \quad \frac{dy}{dx} = 5 \times 1$$

$$\textcircled{Q} \quad y = \underbrace{k+x}_{\text{const}} \quad ; \quad y = \underbrace{kx}_{\text{const}}$$
$$y' = 0+1 \quad ; \quad y' = k$$

Kinematik

$$\text{Q2} \quad y = x^2 + 4x + 10$$

$$\frac{dy}{dx} = 2x + 4 + 0$$

$$\text{Q3} \quad y = t^2 - 2t + 10$$

$$\frac{dy}{dt} = 2t - 2 + 0$$

$$\text{Q4} \quad y = x^2 - 6x + 5$$

$$\frac{dy}{dx} = 2x - 6 + 0$$

$$\text{Q5} \quad y = t^3 - t^2 + 10t + 5$$

$$\frac{dy}{dt} = 3t^2 - 2t + 10$$

$$Q \quad y = x^6$$

$$\frac{dy}{dx} = 6x^5$$

और differentiable करो

double differentiation $\equiv \frac{d^2y}{dx^2} = y''$
of y wrt x

diff of $(\frac{dy}{dx})$ wrt x

$$y = x^6 \quad \text{diff}$$

$$\frac{dy}{dx} = y' = 6x^5 \quad \text{diff}$$

$$\frac{d^2y}{dx^2} = y'' = 30x^4$$

$$Q \quad y = x^3 + x^5 + x^4$$

$$y' = 3x^2 + 5x^4 + 4x^3$$

$$\frac{d^2y}{dx^2} = y'' = 6x + 20x^3 + 12x^2$$

Homework

$$\underline{Q} \quad y = \pi x^2$$

$$\frac{dy}{dx} =$$

$$\underline{Q} \quad A = \pi r^2$$

$$\frac{dA}{dr} =$$

$$\underline{Q} \quad y = \pi x^3$$

$$\frac{dy}{dx} =$$

$$\underline{Q} \quad V = \frac{4}{3}\pi r^3$$

$$\frac{dV}{dr} =$$

$$\underline{\text{Q}} \quad y = t^2 - 4t + 10$$

$$\frac{dy}{dt} =$$

$$\frac{d^2y}{dt^2} =$$

$$\underline{\text{Q}} \quad y = t^3 - 4t^2 + 10$$

$$\frac{dy}{dt} =$$

$$\frac{d^2y}{dt^2} =$$

$$\underline{\text{Q}} \quad x = t^2 - 4t + 10$$

$$\frac{dx}{dt} =$$

$$\frac{d^2x}{dt^2} =$$

$$\underline{\text{Q}} \quad x = t^3 - 4t^2 + 10$$

$$\frac{dx}{dt} =$$

$$\frac{d^2x}{dt^2} =$$

$$\text{Q } y = \sin x$$

$$\frac{dy}{dx} =$$

$$\frac{d^2y}{dx^2} =$$

$$\text{Q } P = \ln t$$

find $\frac{dP}{dt}$ at $t = 10 \text{ sec}$

$$\text{Q} \quad y = x^3$$

find $\frac{dy}{dx}$, at $x=2$

$$\text{Sol} \quad y = x^3$$

$$\frac{dy}{dx} = 3x^2$$

$$\text{at } x=2, \quad \frac{dy}{dx} = 3x^2$$

$$= 12 \quad \text{Ans}$$

Similarly
find \Rightarrow

$$\text{Q} \quad y = t^2$$

find $\frac{dy}{dt}$ at $t=10 \text{ sec}$

$$\text{Q} \quad x = t^2 + 2t$$

find $\frac{dx}{dt}$ at $t=3 \text{ sec}$

$$\text{Q} \quad x = t^3 - 2t^2 + 5$$

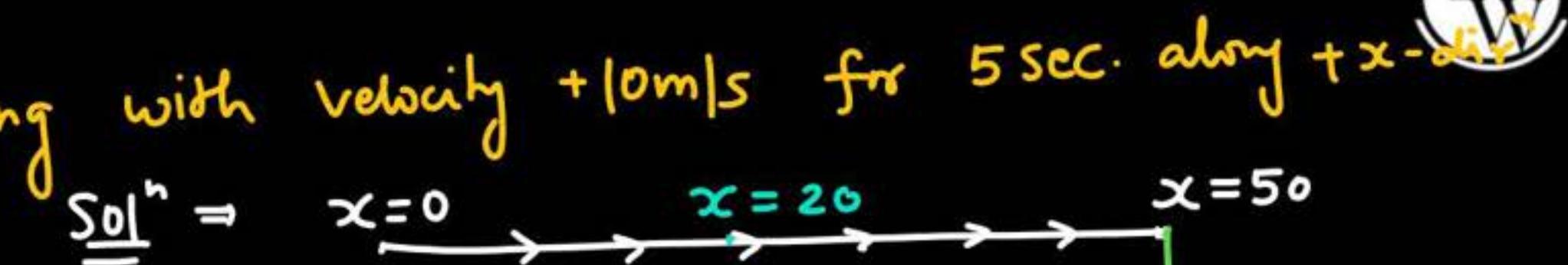
find $\frac{dx}{dt}$ and $\frac{d^2x}{dt^2}$ at $t=2 \text{ sec}$

Q

A particle is moving with velocity $+10 \text{ m/s}$ for 5 sec. along $+x$ -dir. than it reversed its direction and move with velocity -10 m/s for three second.

find ① displacement

② Distance



$$\text{Displacement} = 20 - 0 \\ = 20$$

$$\text{Distance} = 50 + 30 = 80$$

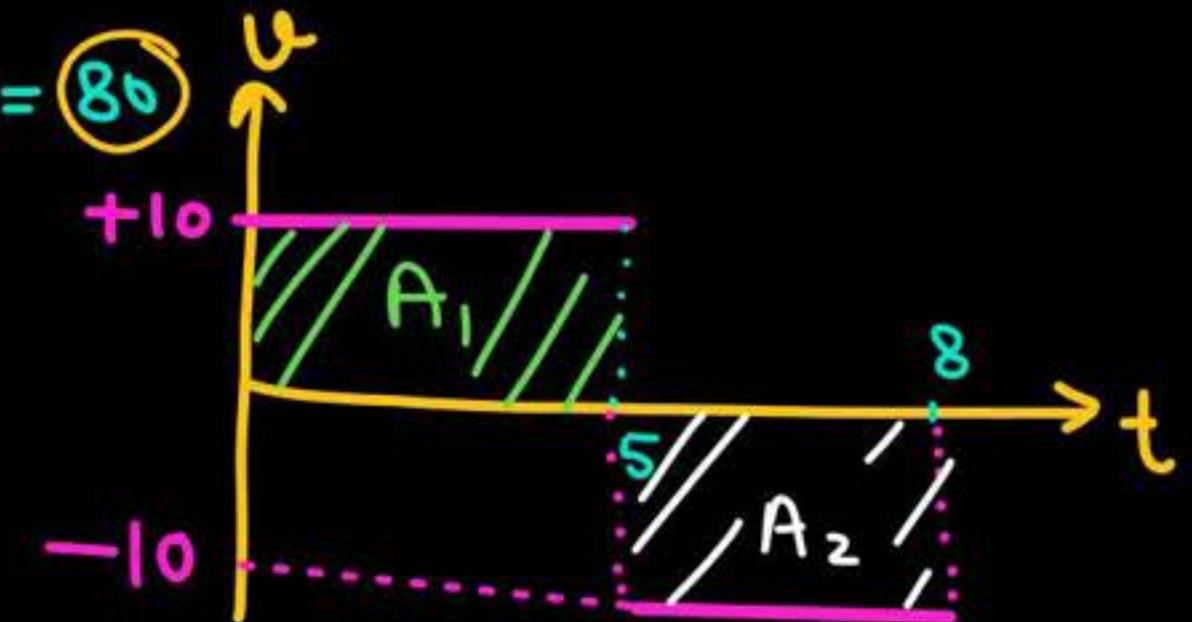
$$A_1 = 5 \times 10 = 50$$

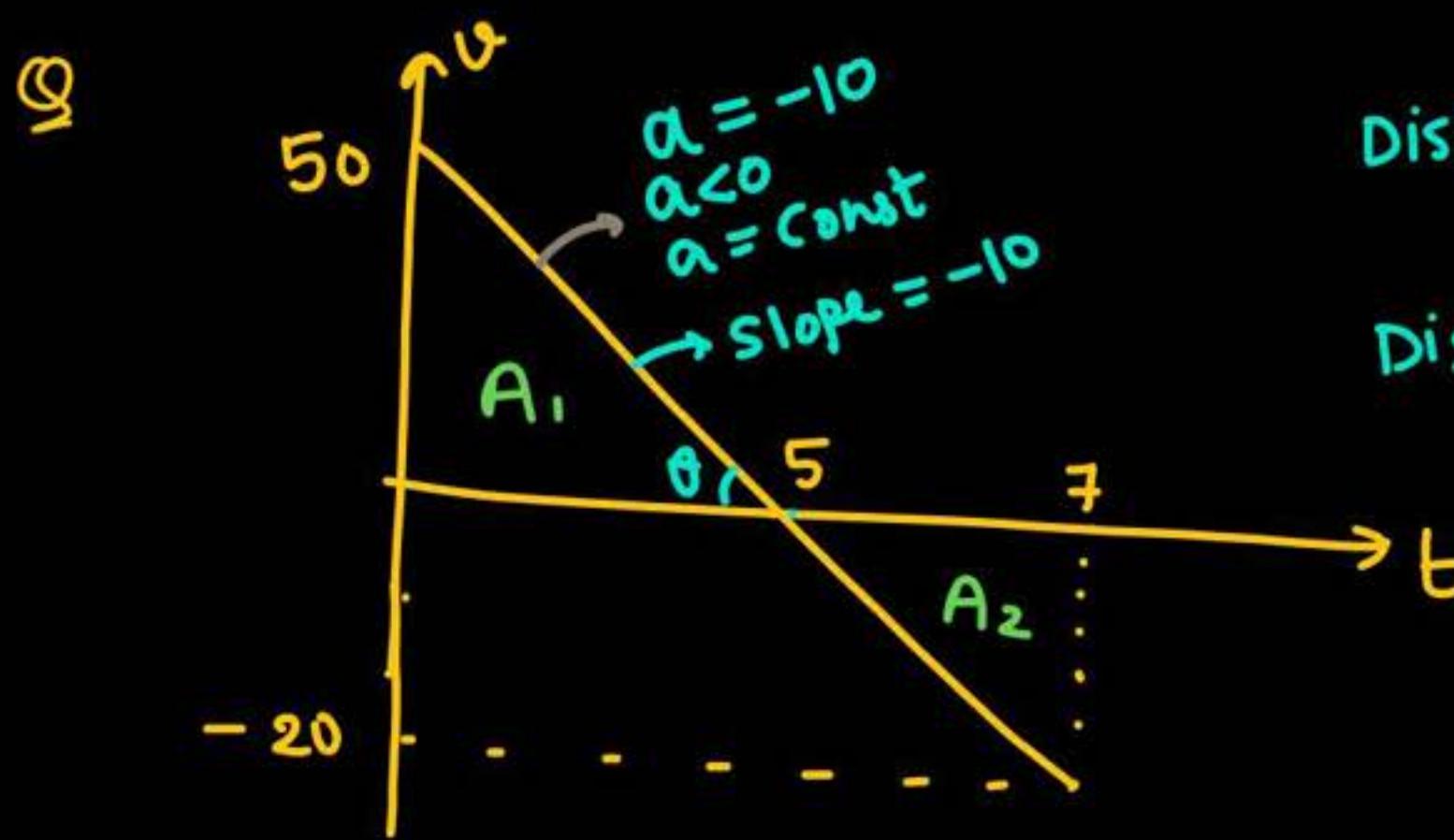
$$A_2 = 3 \times 10 = 30$$

$$\text{Displacement} = A_1 - A_2$$

$$= 50 - 30 = 20$$

$$\text{Distance} = A_1 + A_2 = 50 + 30 = 80$$





$$\text{Displacement} = 125 - 20 = 105$$

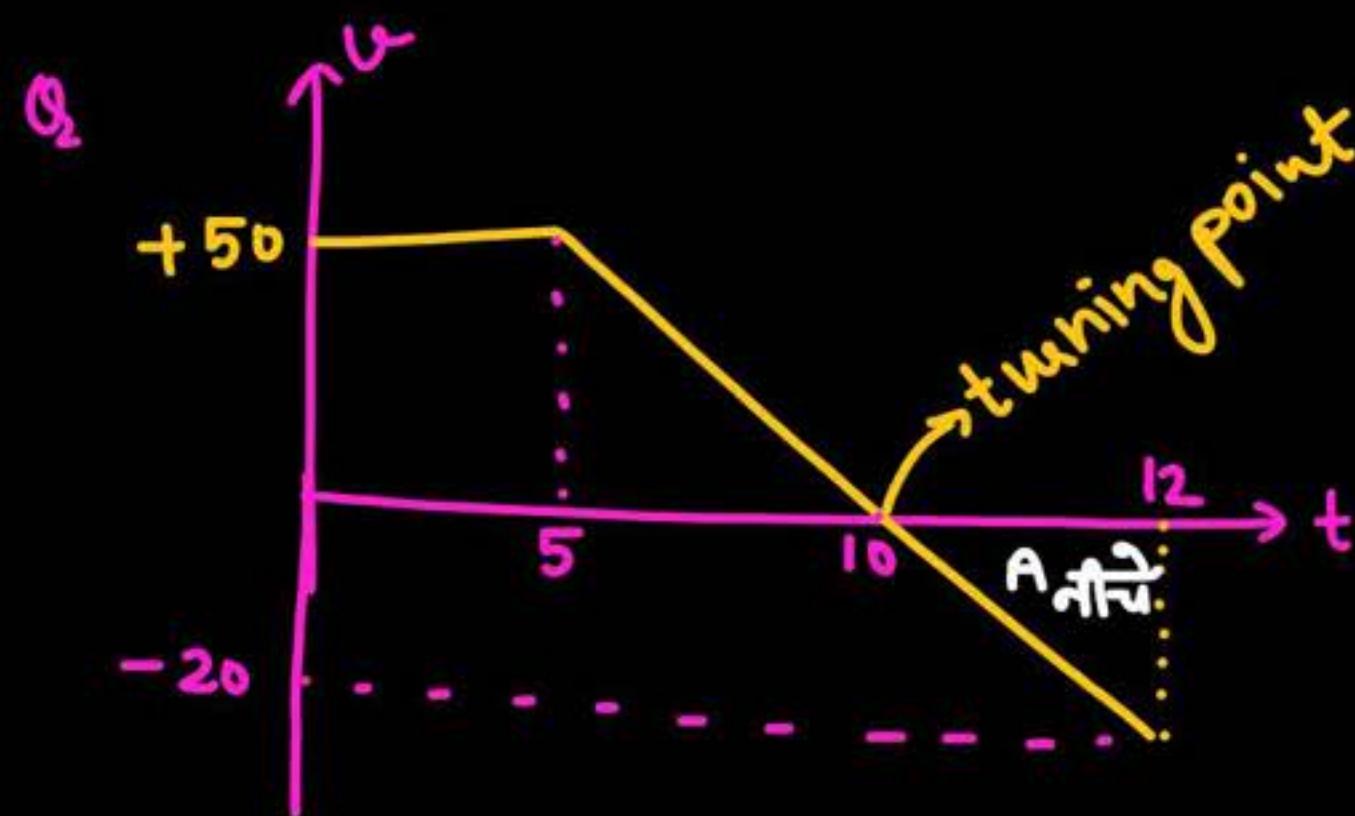
$$\text{Distance} = 125 + 20 = 145$$

$$\text{Average velocity} = \frac{105}{7}$$

$$\text{Avg. Speed} = \frac{145}{7}$$

$$A_1 = \frac{1}{2} \times 5 \times 50 = 125$$

$$A_2 = \frac{1}{2} \times 2 \times 20 = 20$$



Displacement = $A_{\text{upper}} - A_{\text{नीचे वाला}}$

$$= \frac{1}{2} (5+10) \times 50 - \frac{1}{2} \times 2 \times 20$$

$$= \frac{750}{2} - \frac{40}{2} = 375 - 20 = 355$$

Distance = $375 + 20 = 395$

Q2

$$v = 10t + 20$$

Slope = 10 = const

$$a = 10$$

$$\rightarrow a = \frac{dv}{dt} = 10 + 0$$

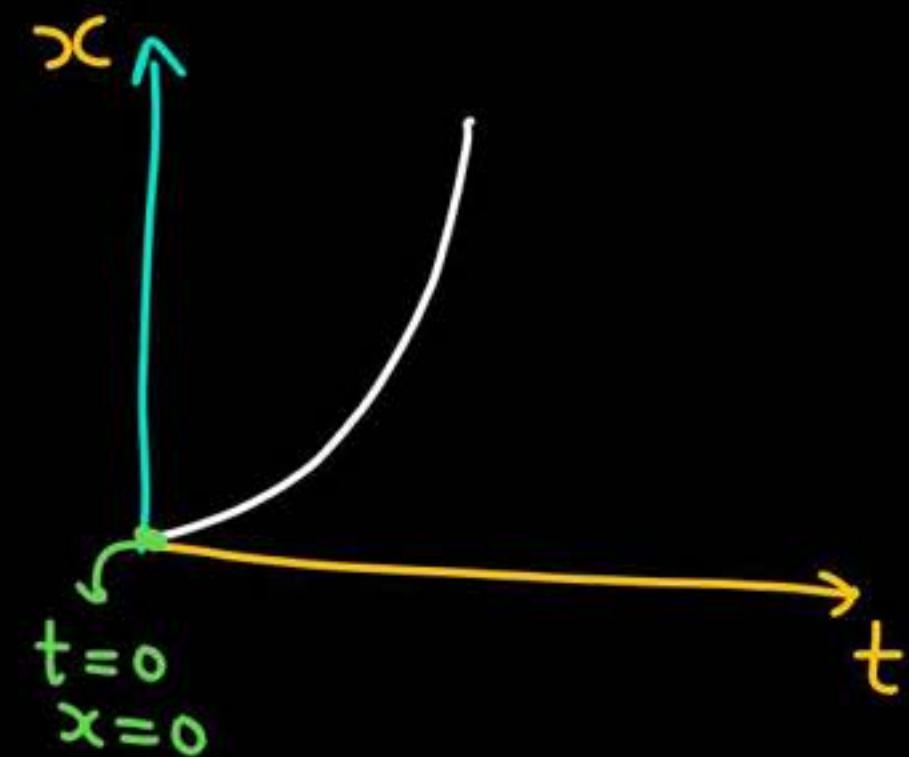
Q

Draw $x-t$ graph if at $t=0$ particle is at origin ($x=0$)

$$V = 10t + 20$$

$$a = +10 > 0$$

सुरक्षा



CET 92 note करना

P
W

Q A particle start motion from rest from origin such that its acc is +10. Draw v-t, x-t graph

$$a = +10$$

$$\frac{dv}{dt} = 10$$

$$\int dv = \int 10 dt$$

$$v = 10t + C$$

$$\text{at } t=0, 0 = 0 + C$$

$$\boxed{C=0}$$

$$t = 0, x = 0 \\ v = 0$$

$$v = 10t$$

$$\frac{dx}{dt} = 10t$$

$$\int dx = \int 10t dt$$

$$x = 10 \frac{t^2}{2} + C$$

$$x = 5t^2 + C$$

$$t = 0, x = 0 \Rightarrow 0 = 0 + C$$

given

$$x = 5t^2$$

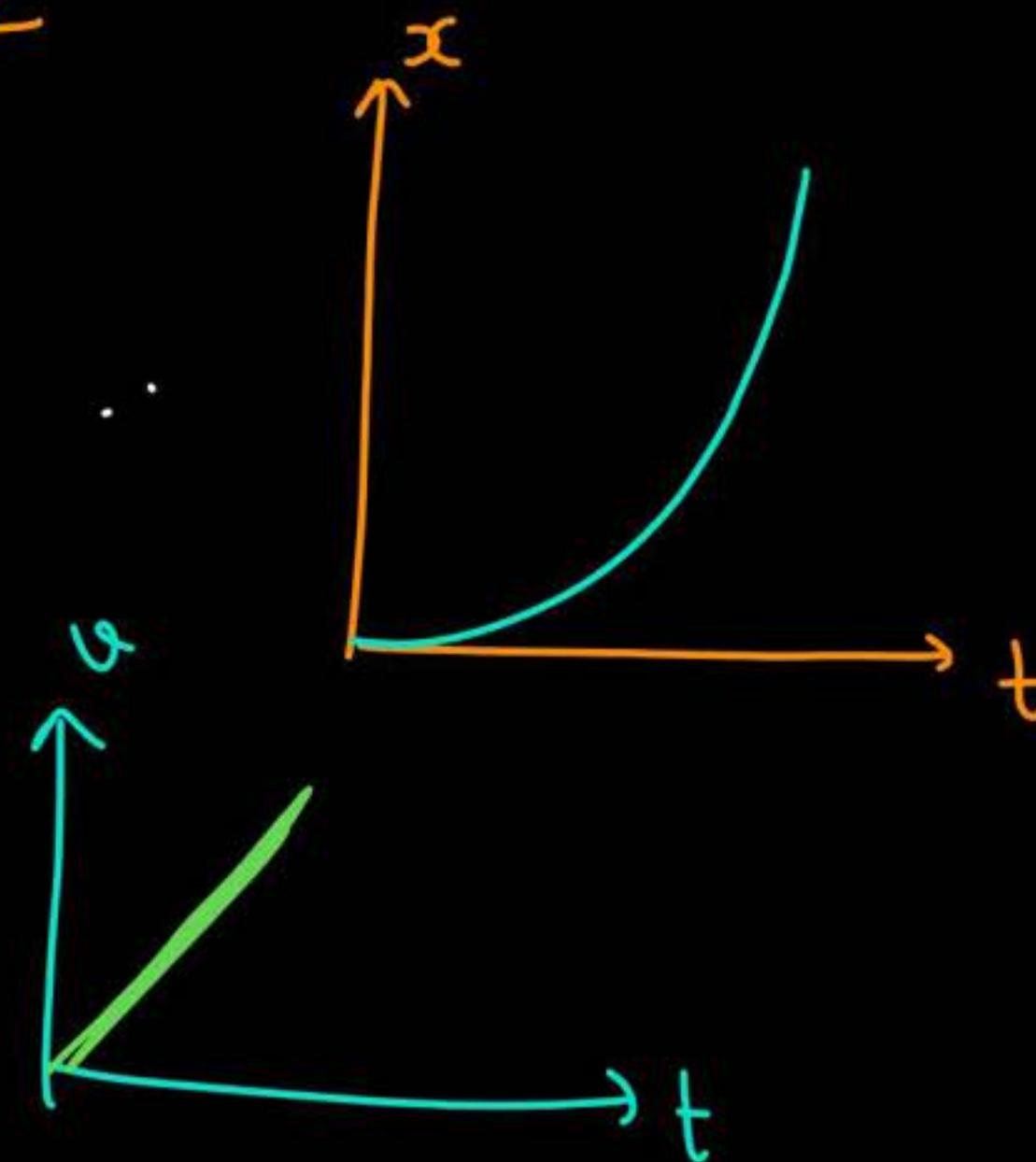
111
(Parabola)

$$\boxed{C=0}$$

~~Q&W~~

$$x = 5t^2$$

$$v = 10t$$

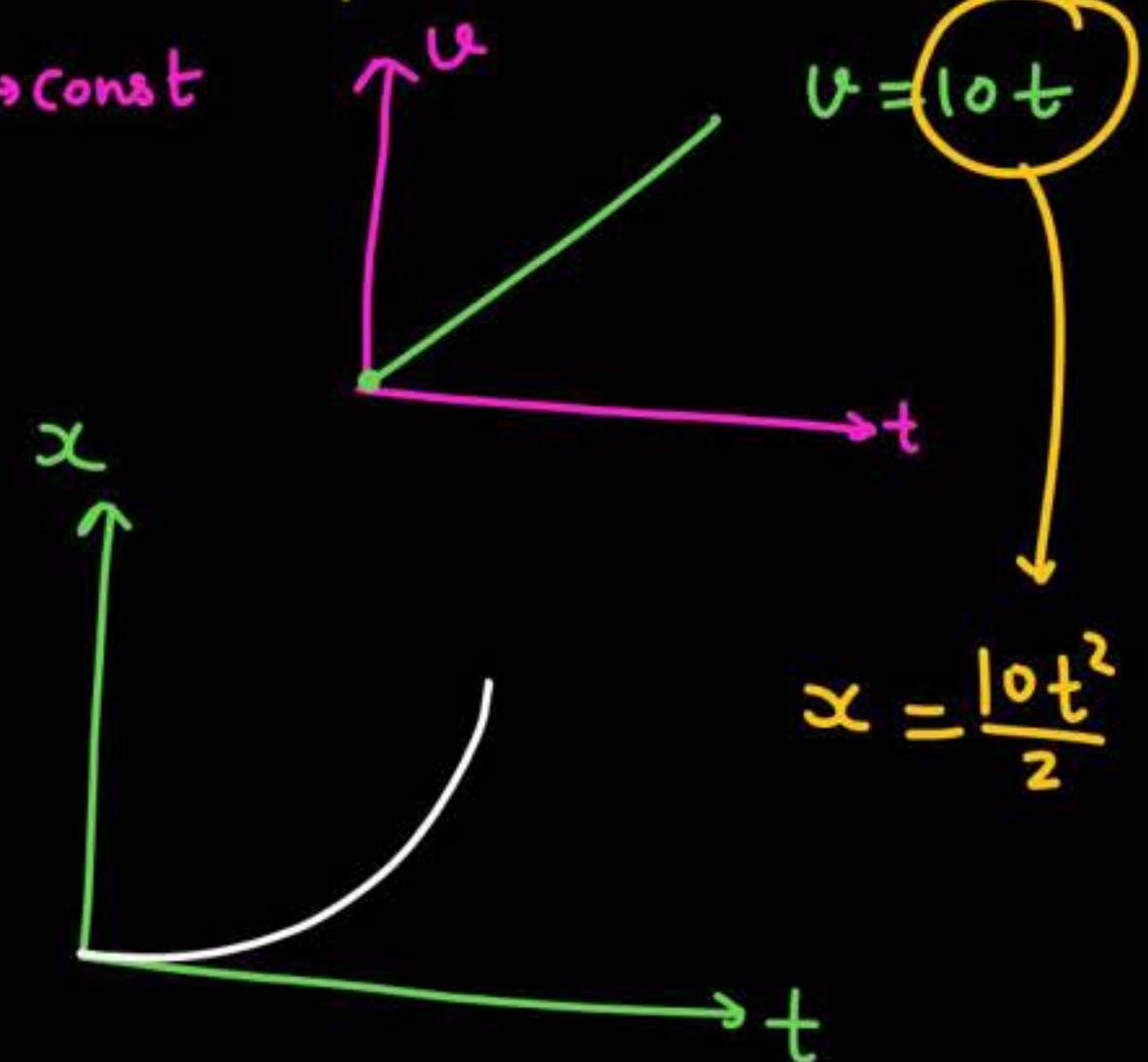


Q

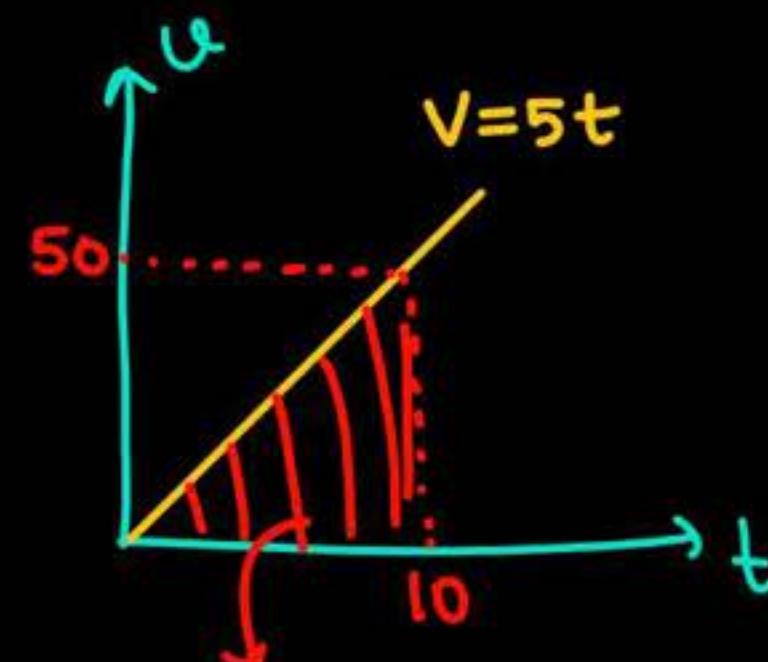
particle start from rest
from origin at $t=0$, having
acc $+10 \text{ m/s}^2$.

P
W

$a \rightarrow \text{const}$



Q particle start from rest from origin having acc $a = +5 = \text{const}$



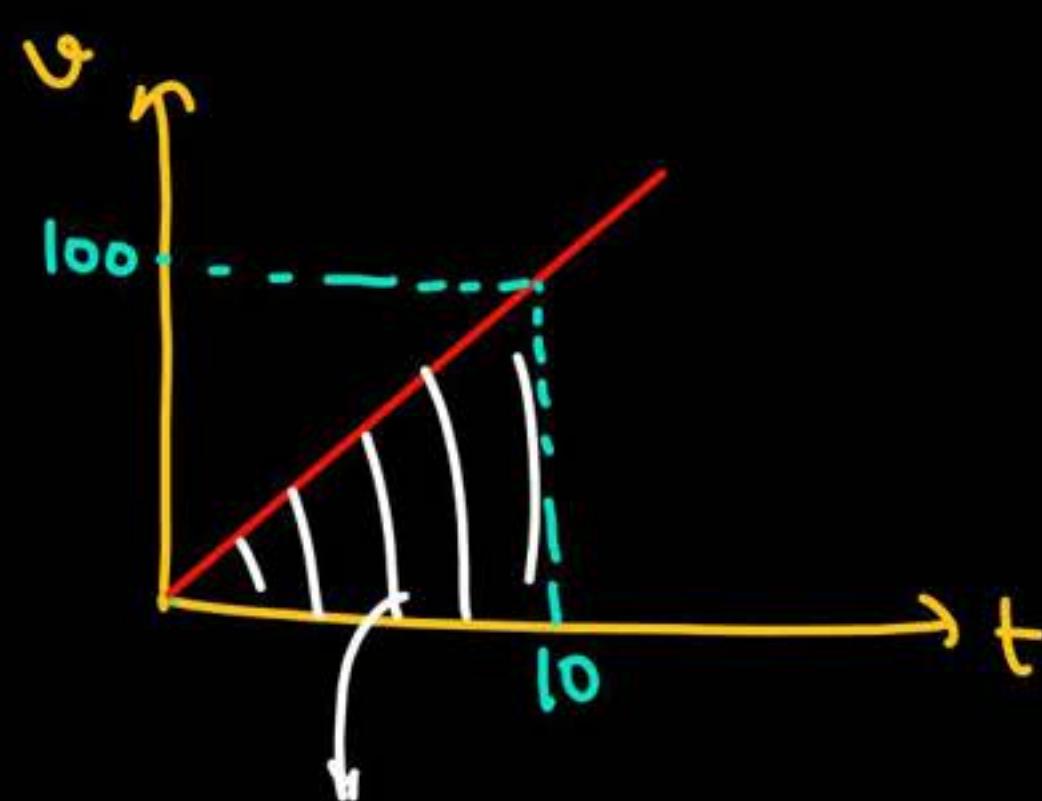
$$\text{Area} = \frac{1}{2} \times 50 \times 10 = 250$$

$$\begin{aligned} * & V = u + at \\ & = 0 + 5 \times 10 \\ & V = 50 \end{aligned}$$

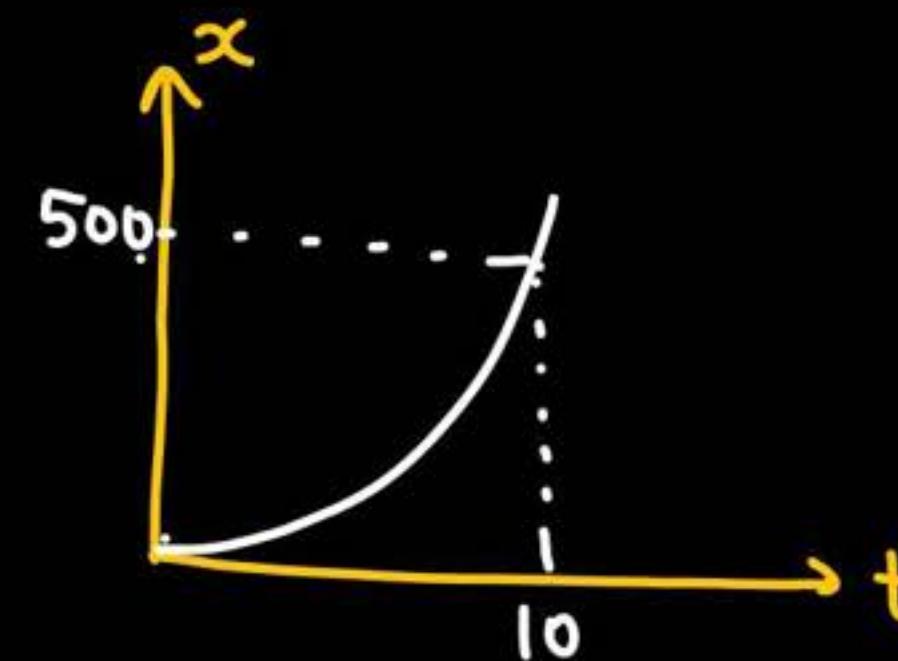
$$\begin{aligned} S &= ut + \frac{1}{2}at^2 \\ &= 0 + \frac{1}{2} \times 5 \times 10^2 \\ &= 250 \end{aligned}$$

Q. particle start from rest from origin having acc = +10m/s.

$t=0 \longrightarrow t=10$ तक $(v-t), (x-t)$ draw



$$\text{Area} = \frac{1}{2} \times 10 \times 100 = 500$$



$$u=0 \\ a=+10 \\ t=10$$

$$v=u+at$$

$$v=0+10 \times 10$$

$$v=100$$

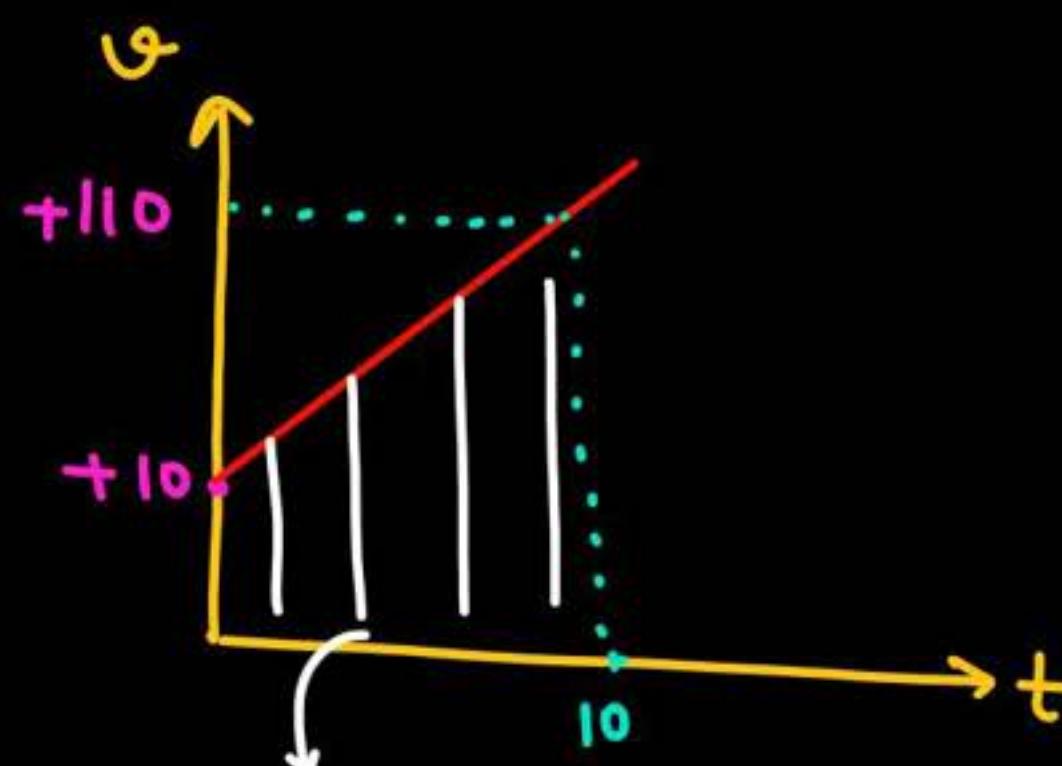
$$s=ut+\frac{1}{2}at^2$$

$$= 0 + \frac{1}{2} \times 10 \times 10^2$$

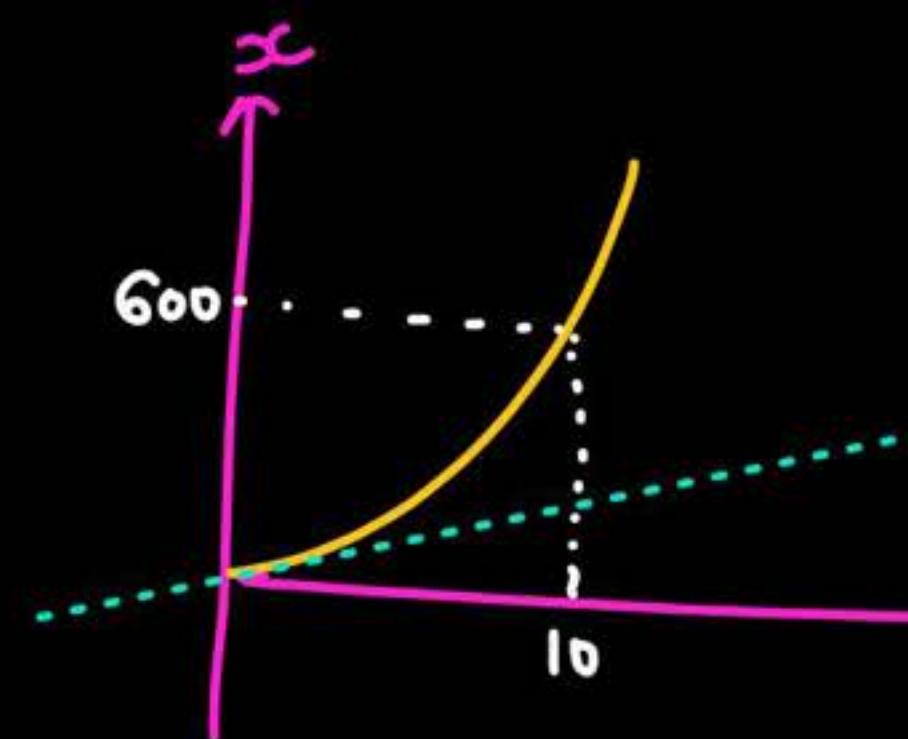
$$= 500$$

Q A particle starts motion having initial velocity +10m/s

and acc = +10m/s².



$$\text{Area} = \frac{1}{2} \times (10 + 110) \times 10 \\ = 600$$



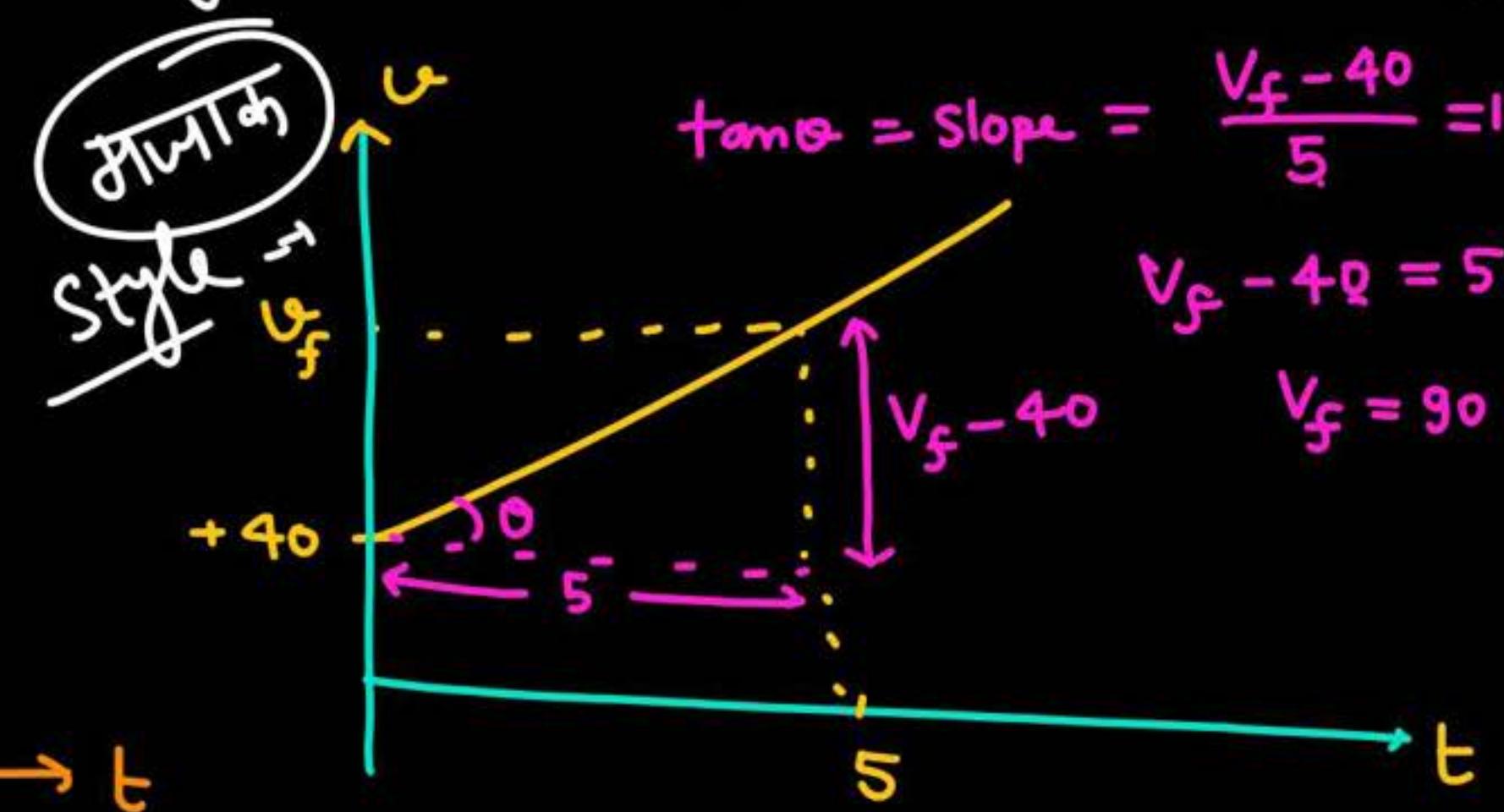
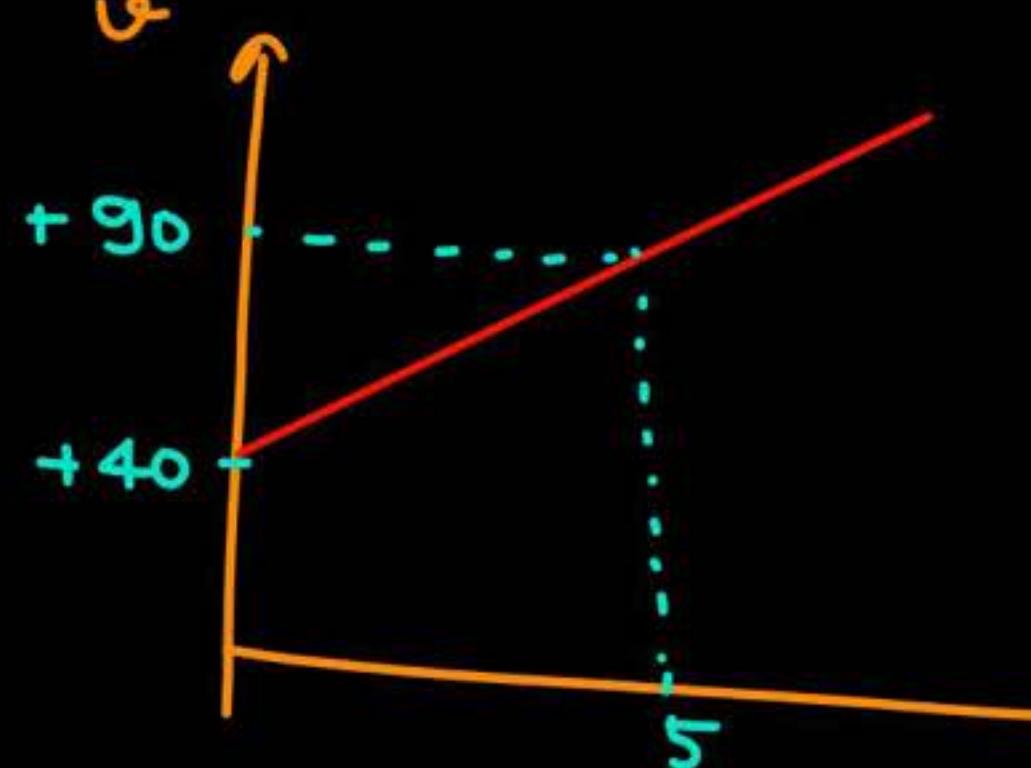
$$\begin{aligned} u &= +10 \\ a &= +10 \\ t &= 10 \text{ sec} \\ v &= u + at \\ &= 10 + 10 \times 10 \\ &= 10 + 100 \\ &\underline{\underline{v = 110}} \end{aligned}$$

$$\begin{aligned} S &= ut + \frac{1}{2}at^2 \\ &= 10 \times 10 + \frac{1}{2} \times 10 \times 10^2 \\ &= 100 + 500 = 600 \end{aligned}$$

Q A particle starts motion having initial velocity $+40 \text{ m/s}^2$

and $\text{acc} = +10 \text{ m/s}^2$.

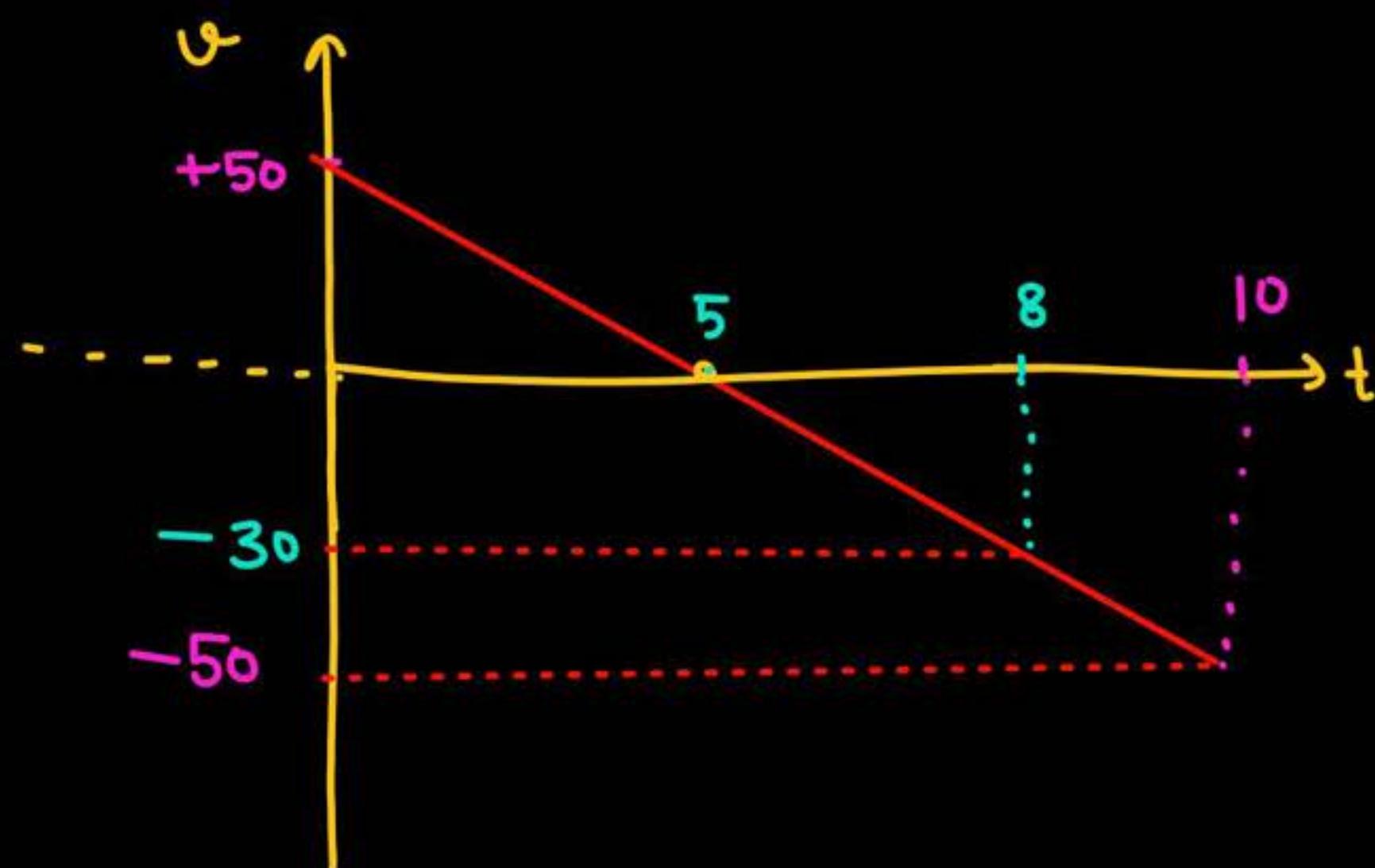
★



Q A particle starts motion having initial velocity +50 m/s and acc = -10 m/s². $a < 0$

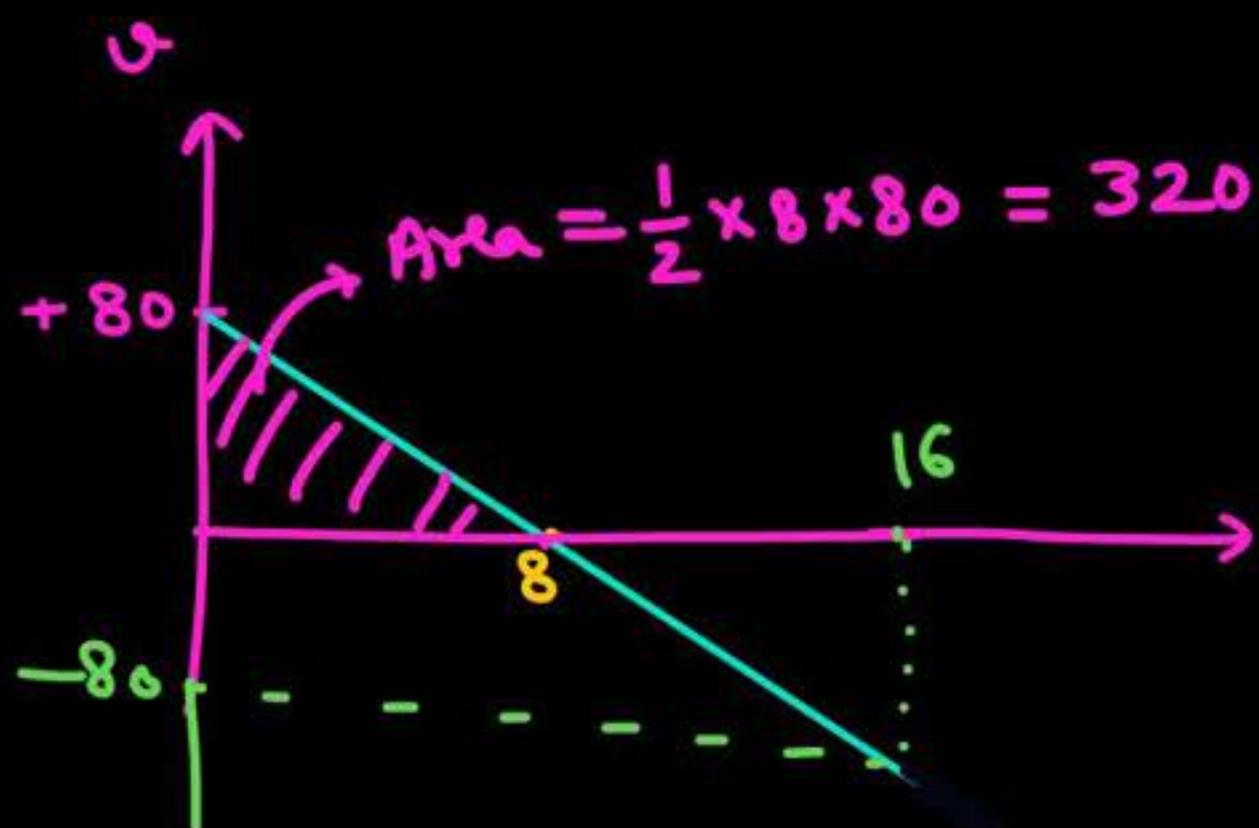
$$50 - 80 = -30$$

10



Q A particle starts motion having initial velocity $+80 \text{ m/s}$

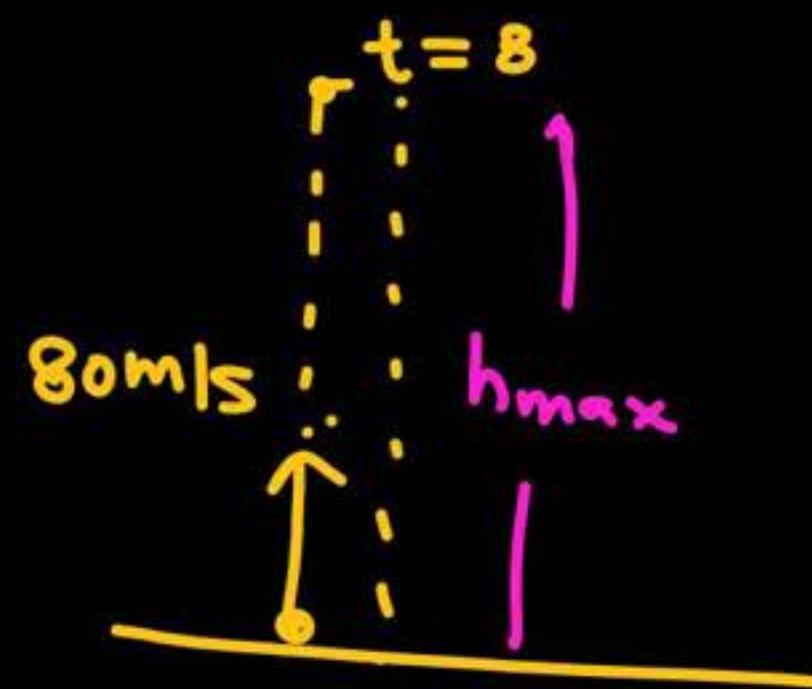
and $\text{acc} = -10 \text{ m/s}^2$



$$t = 10 \text{ sec}$$

$$v = 80 - 100 = -20 \text{ m/s}$$

$$\begin{aligned} v &= u + at = 80 + (-10) 10 \\ &= -20 \end{aligned}$$

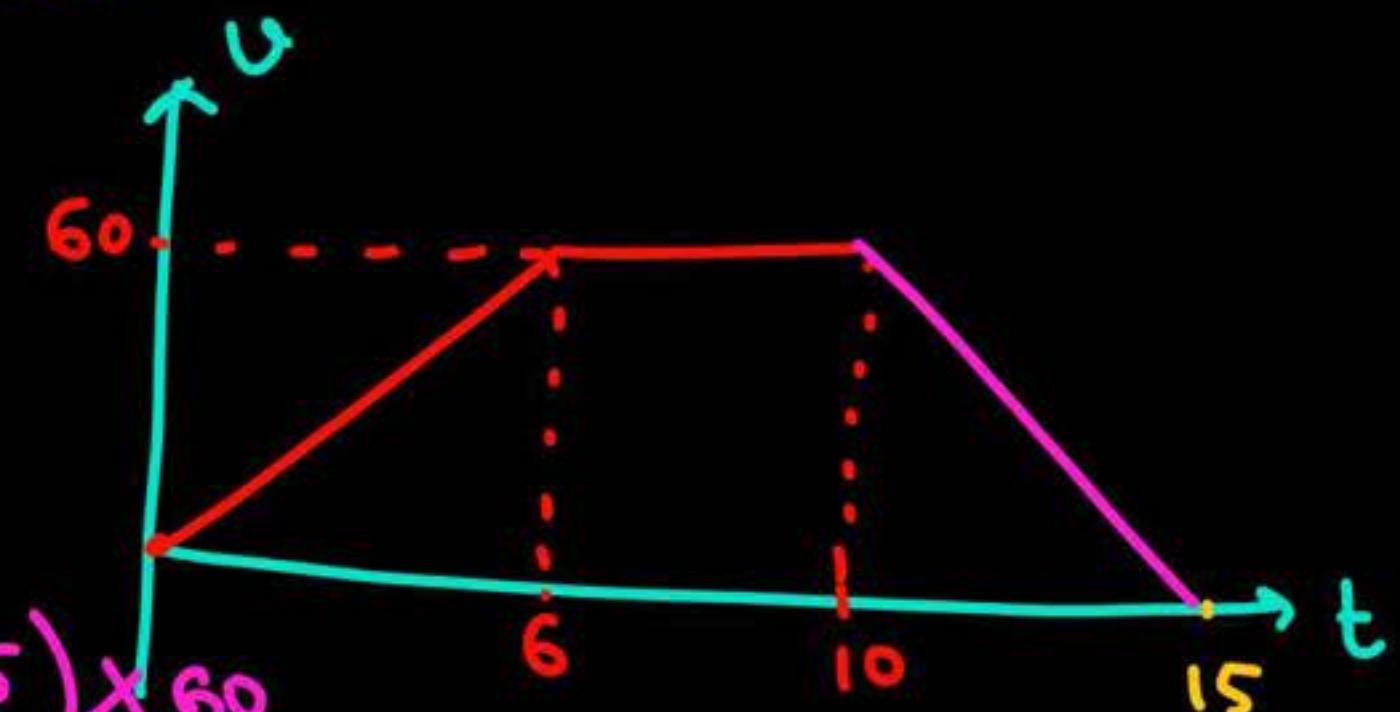


Q A particle starts motion from rest, having acc + 10 m/s^2 for 6 sec. after that it moves with constant velocity for next 4 sec. In last part of journey particle comes to rest & took 5 sec. having const acc.

① find acc in last part of journey

② Distance travelled, Displacement

$$\therefore \text{Displ.} = \text{Area} = \frac{1}{2} \times (4 + 15) \times 60$$

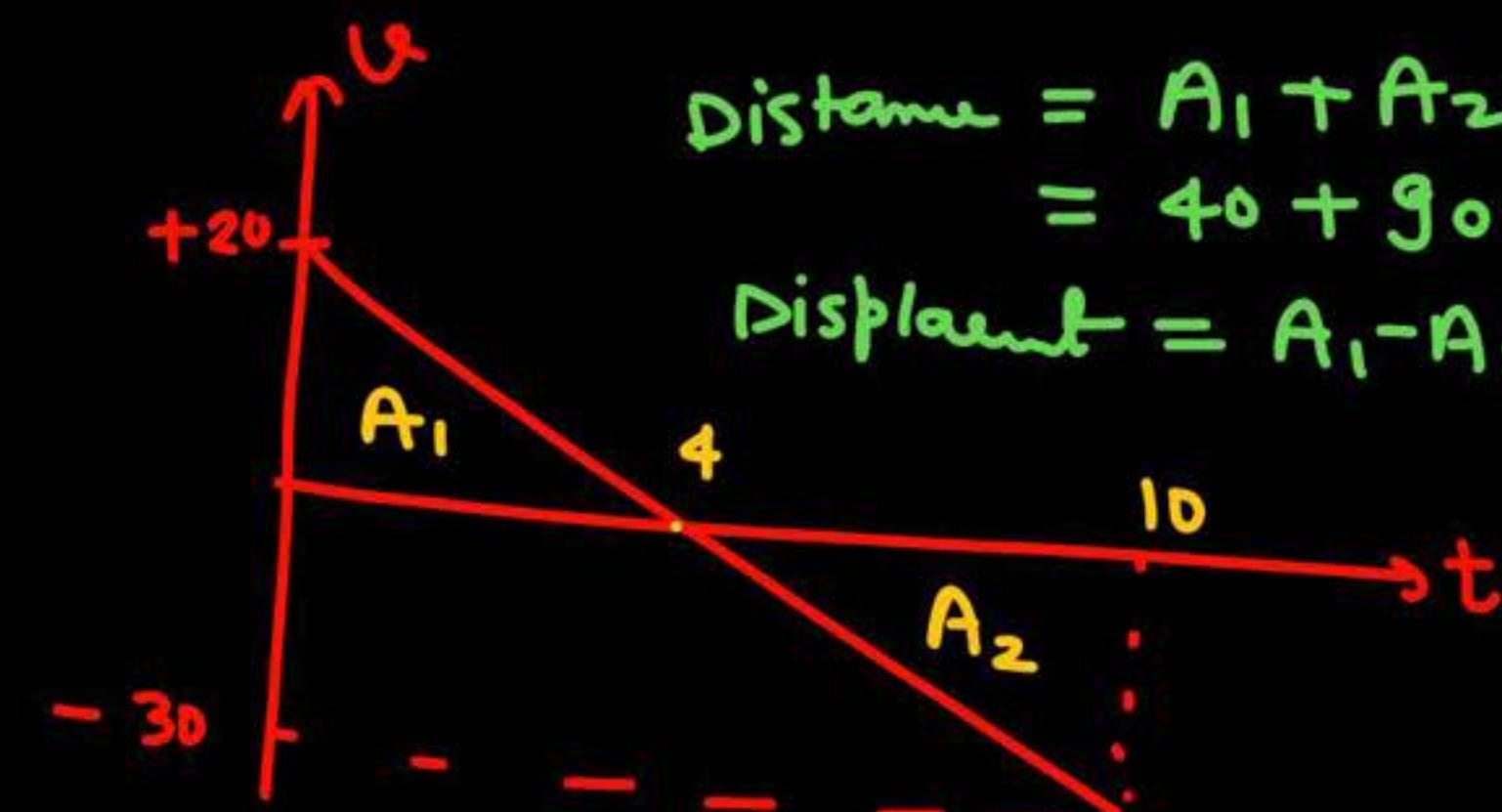


Question

Q.

particle is moving with initial velocity +20 m/s having acceleration -5 m/s². find distance travelled by particle in 10 sec.

~~$u = +20$
 $a = -5$
 $s = ut + \frac{1}{2}at^2$
 $\text{Displ} = 20 \times 10 - \frac{1}{2} \times 5 \times 10^2$
 $= 200 - 250$
 $= -50$~~



$$\text{Distance} = A_1 + A_2$$

$$= 40 + 90 = 130$$

$$\text{Displacement} = A_1 - A_2 = 40 - 90$$

$$= -50$$

~~H/W~~

P
W

Q A particle starts motion from rest, having acc + 10 m/s^2 for 6 sec. after that it moves with constant velocity for next four second. After that particle moves with const acc of -20 m/s^2 for five second. find

Distance travelled.

$$\int \sin(ax+b) dx = -\frac{1}{a} \cos(ax+b) + C$$

$$\int e^x dx = e^x + C$$

$$\int e^{ax+b} dx = \frac{1}{a} e^{ax+b} + C$$

$$* \int \frac{1}{x} dx = \ln x + C$$

$$\begin{aligned} * \int \frac{1}{3x} dx &= \frac{1}{3} \int \frac{1}{x} dx \\ &= \frac{1}{3} \ln x + C \end{aligned}$$

$$* \int \frac{1}{3x+4} dx = \frac{1}{3} \ln(3x+4) + C$$

मनकेर लिए करता प्रश्नलिखि



प्रश्न लिखि

$$\int \frac{1}{ax+b} dx = \frac{1}{a} \ln(ax+b) + C$$

क

$$\int \frac{1}{4x+5} dx = \frac{1}{4} \ln(4x+5) + C$$

$$\int \frac{1}{4x+5} dx = ?$$

$$4x+5 = t \quad (\text{let})$$

differentiate

$$4 dx = 1 dt$$

$$dx = \frac{1}{4} dt$$

$$\int \frac{1}{4x+5} dx = \int \frac{1}{t} \frac{1}{4} dt$$

$$= \frac{1}{4} \int \frac{1}{t} dt = \frac{1}{4} \ln t$$

$$= \frac{1}{4} \ln(4x+5)$$

Definite Integration

$$\int f(x) \cdot dx = g(x) \Big|_{x_i=a}^{x_f=b} = g(b) - g(a)$$

upper limit of x
 $x_f = b$
 $x_i = a$
 lower limit of x

$$Q \quad \int_{x_i=0}^{x_f=3} x^2 dx = \int_0^3 x^2 dx = \frac{x^3}{3} \Big|_0^3 = \left(\frac{3^3}{3} \right) - \left(\frac{0^3}{3} \right)$$

$$= 9 \quad \text{Ans}$$

P
W

$$Q \int_2^3 9x^3 dx = 4 \cdot \frac{x^4}{4} \Big|_{x=2}^{x=3} = x^4 \Big|_{x=2}^{x=3} = 3^4 - 2^4 = 81 - 16 = \checkmark$$

$$Q \int_0^{\pi/2} \cos x dx = \sin x \Big|_0^{\pi/2} = (\sin \pi/2) - \sin 0 = 1 - 0 = 1$$

Q

$$\int_{x=1}^{x=4} 2x \, dx = 2 \cdot \frac{x^2}{2} \Big|_1^4 = x^2 \Big|_{x=1}^{x=4} = 4^2 - 1^2 = 15$$

Q

$$\int_0^1 7x^6 \, dx = x^7 \Big|_0^1 = 1^7 - 0^7 = 1$$

Q

$$\int_2^3 e^x \, dx = e^x \Big|_2^3 = e^3 - e^2$$

X

$$\int_0^{10} 2x \, dx = x^2 \Big|_{x=0}^{x=10} = 100 - 0 = 100$$

$$Q \quad \int_0^1 (3x^2 + 2x) \, dx = \left(3 \frac{x^3}{3} + 2 \frac{x^2}{2} \right) \Big|_{x=0}^{x=1} = (x^3 + x^2) \Big|_{x=0}^{x=1} = (1^3 + 1^2) - (0^3 + 0^2) = 2$$

not imp
12th class math

Q $y = x^3$

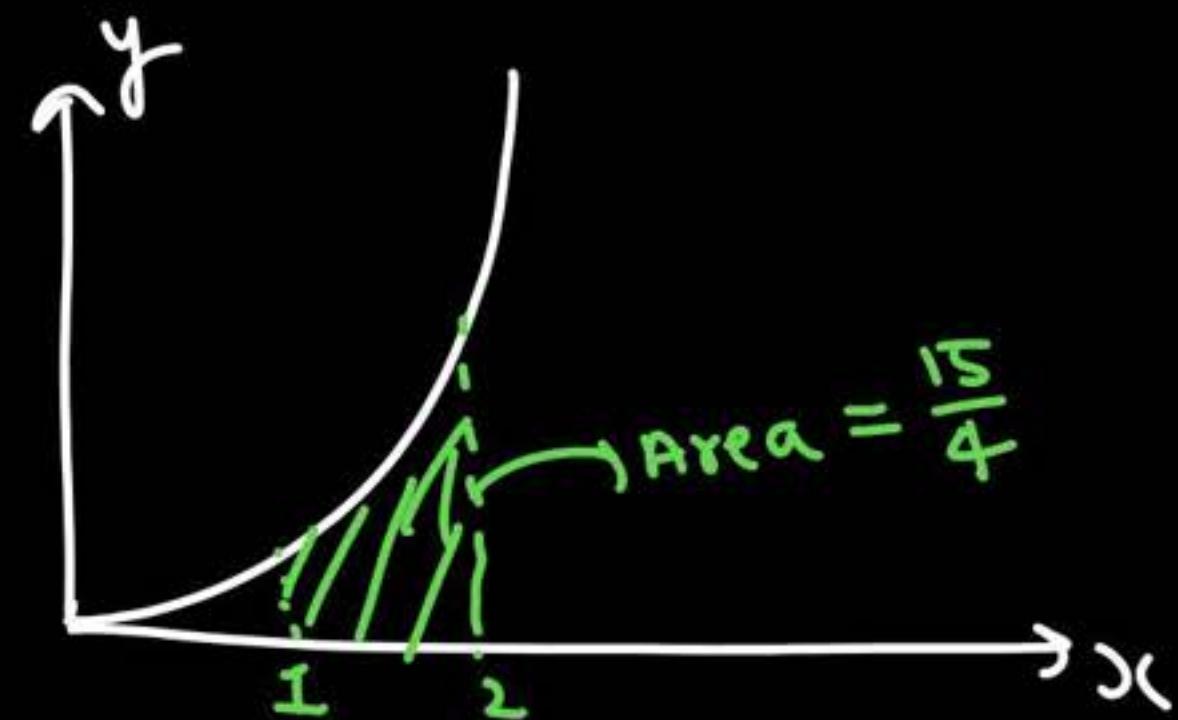
find area under curve (b/w curve & x-axis)
from $x = 1$ to $x = 2$

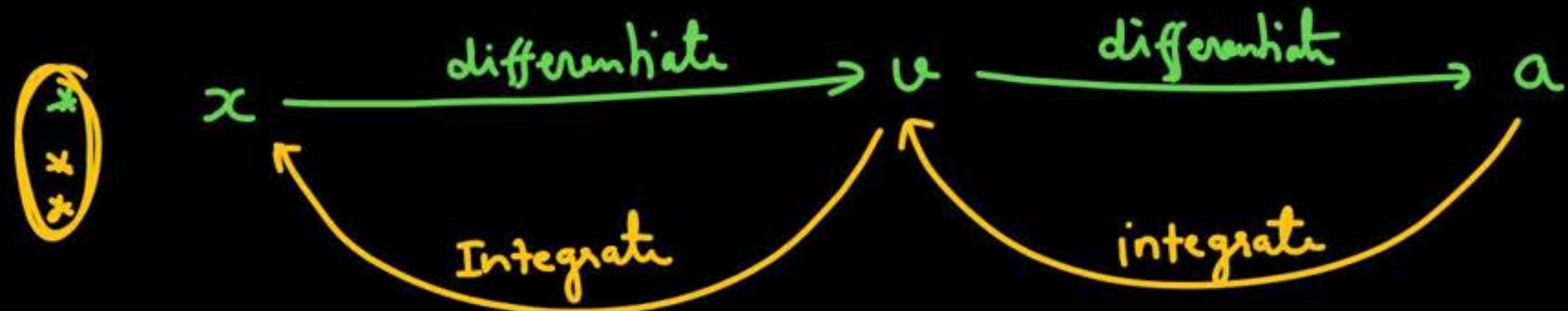
Sol

$$\text{Area} = \int y \, dx = \int x^3 \, dx$$

$$\text{Area} = \frac{x^4}{4} \Big|_{x=1}^{x=2}$$

$$= \frac{1}{4} [2^4 - 1] = \frac{15}{4}$$





Q at $t=0$, particle is at $x=10$
 particle is moving such that its - v vs time relation is given as

$$v = 3t^2 + 2t$$

find ① location of particle at $t = 1$ sec

$$\textcircled{2} \quad x = f(t)$$

$$x = \int v dt = \int (3t^2 + 2t) dt = t^3 + t^2 + C$$

$$\text{at } t=0, x=10$$

$$10 = 0 + 0 + C \Rightarrow \textcircled{C=10}$$

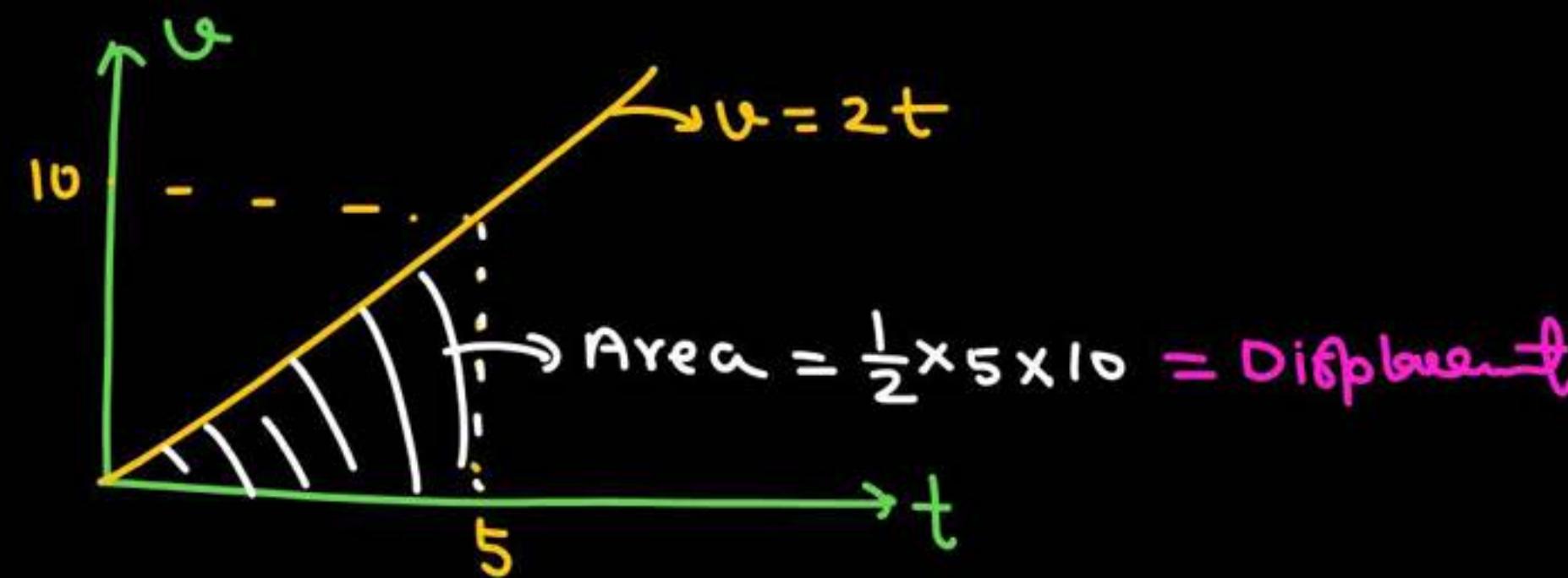
$$x = t^3 + t^2 + C$$

$$x = t^3 + t^2 + 10$$

Q A particle is moving along x-axis s.t its velocity vs time relation is given as

Displacement
from $t=0 \rightarrow t=5$

Solⁿ Area = $\frac{1}{2} \times 5 \times 10$
= 25



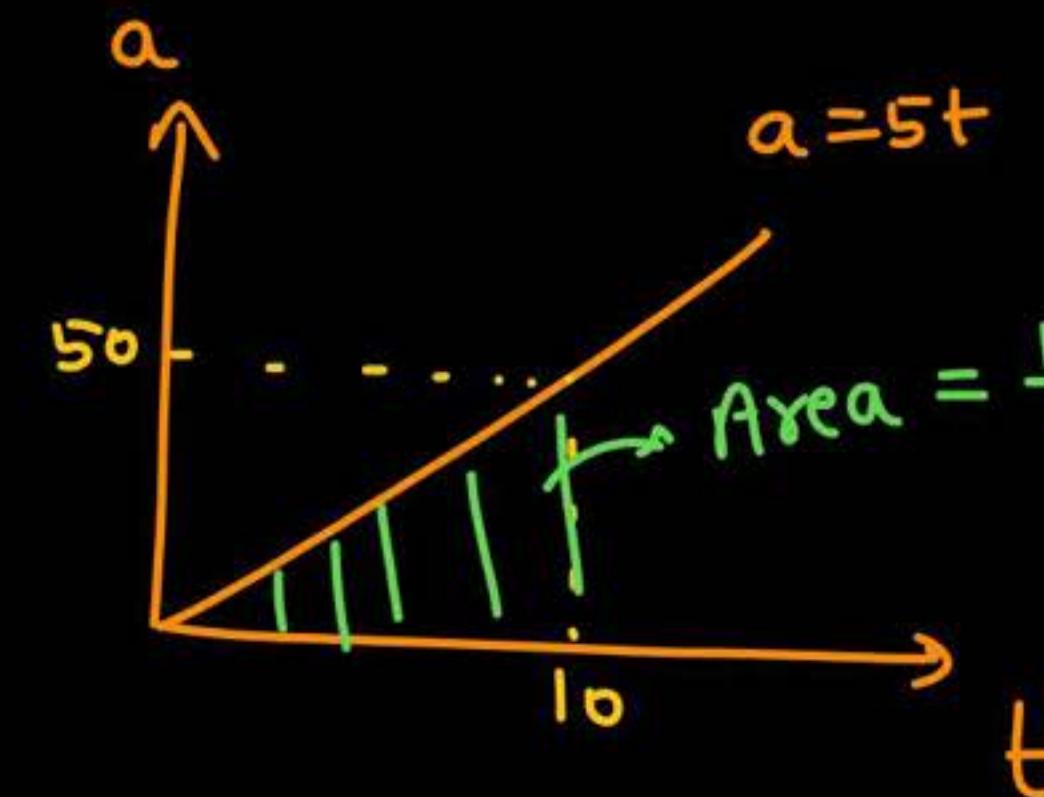
Q A particle starts motion from rest such that its a-t graph is given as

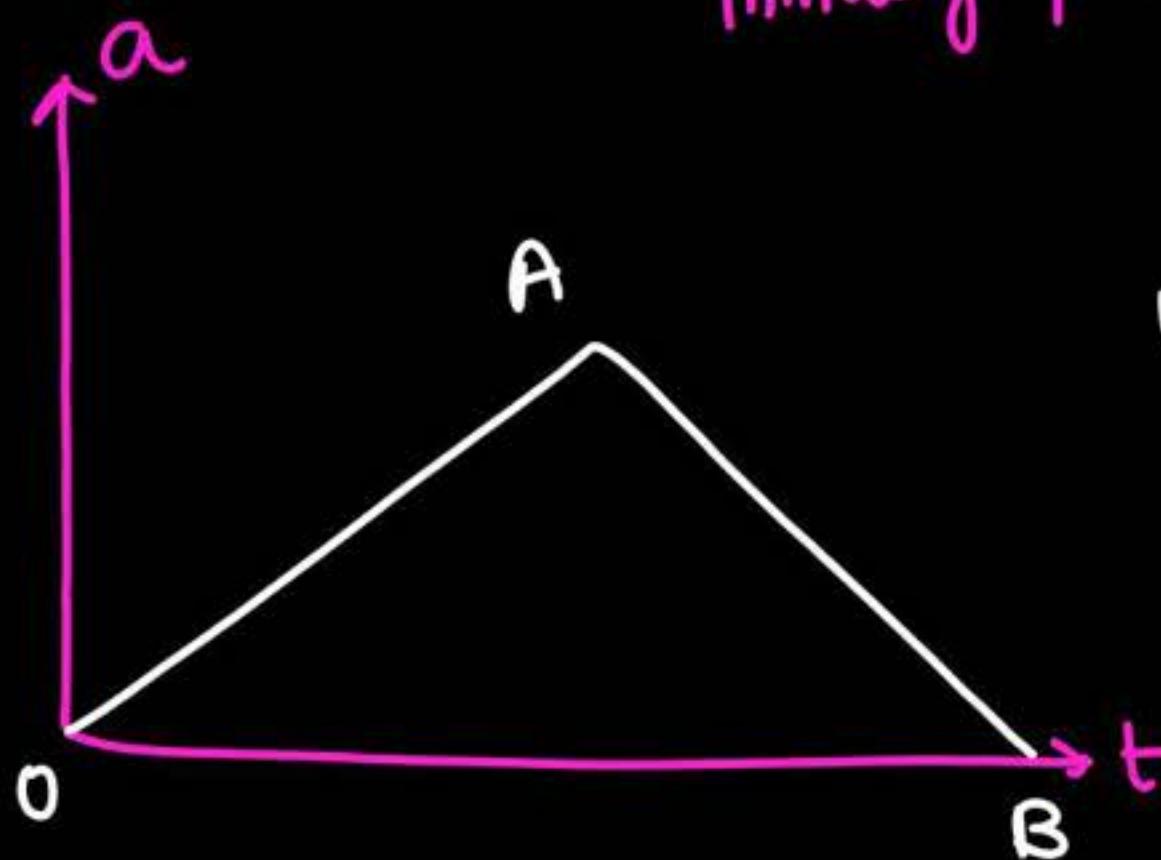
find velocity at $t=10\text{ sec}$,

$$\text{Area} = \vec{V}_f - \vec{V}_i$$

$$\frac{1}{2} \times 10 \times 50 = V_f - 0$$

$$V_f = 250$$





initially particle is at rest

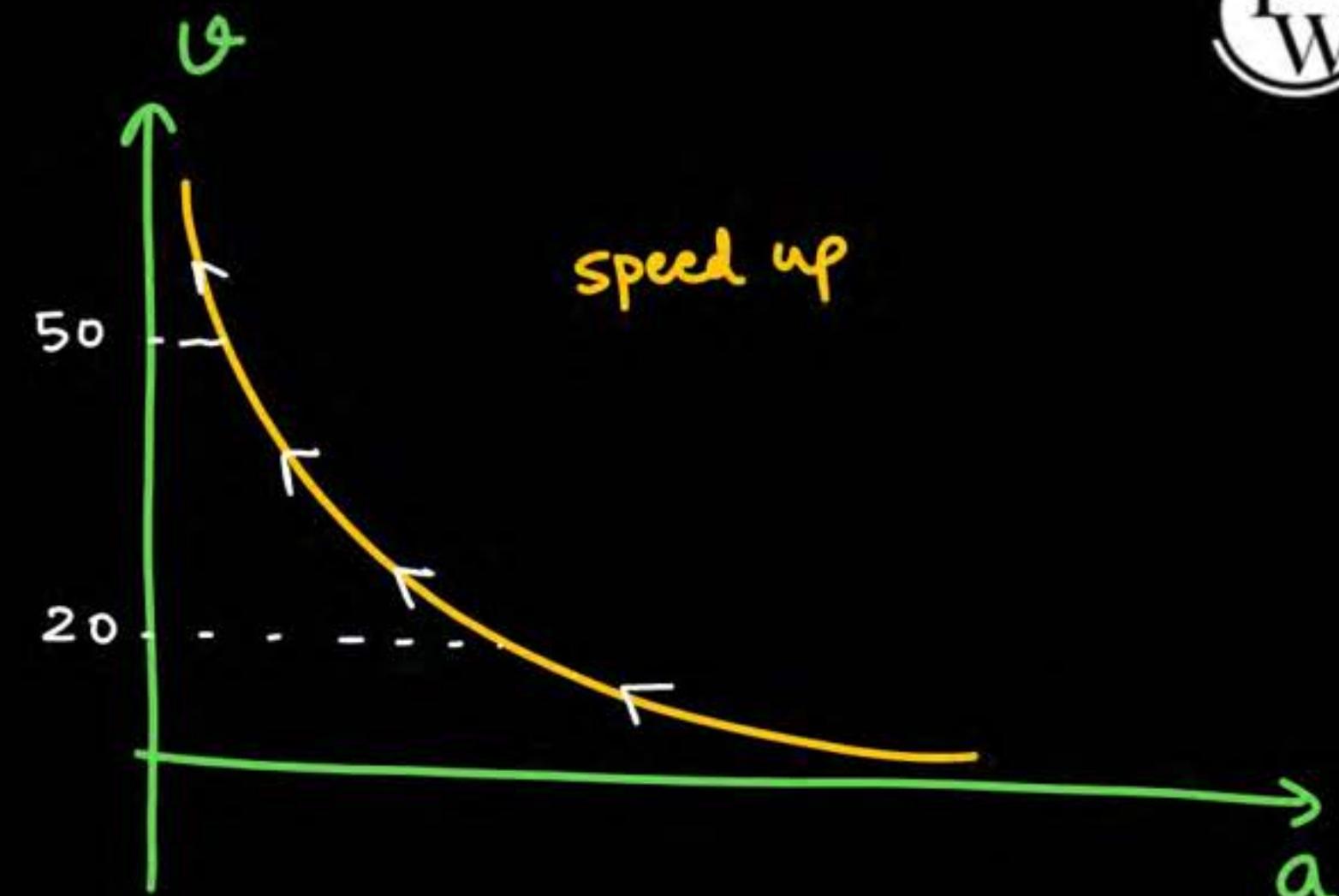
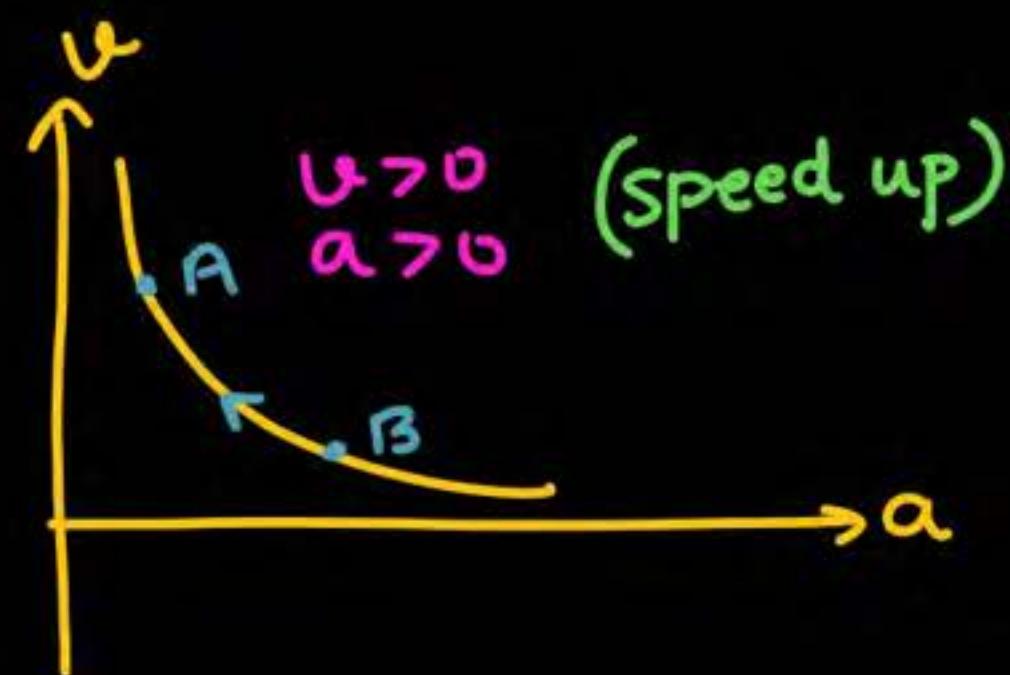
v_{max} ~~on ET~~ ~~ET~~

~~A~~ $\approx 35\%$

~~B~~ $\approx 45\%$

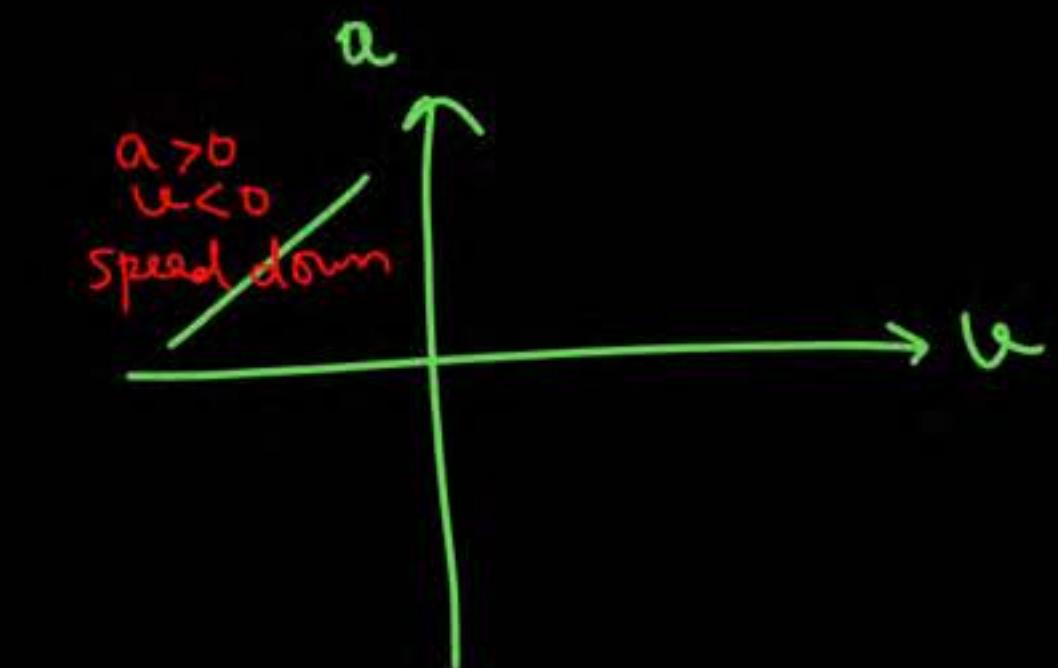
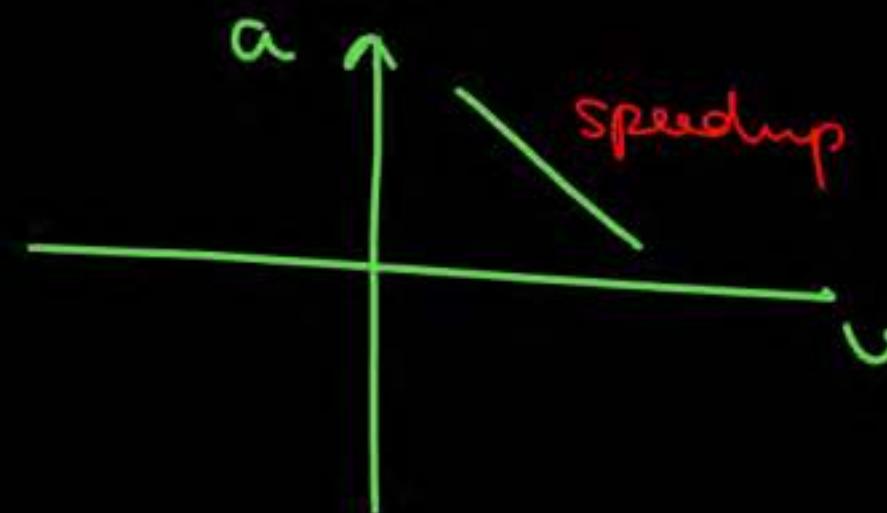
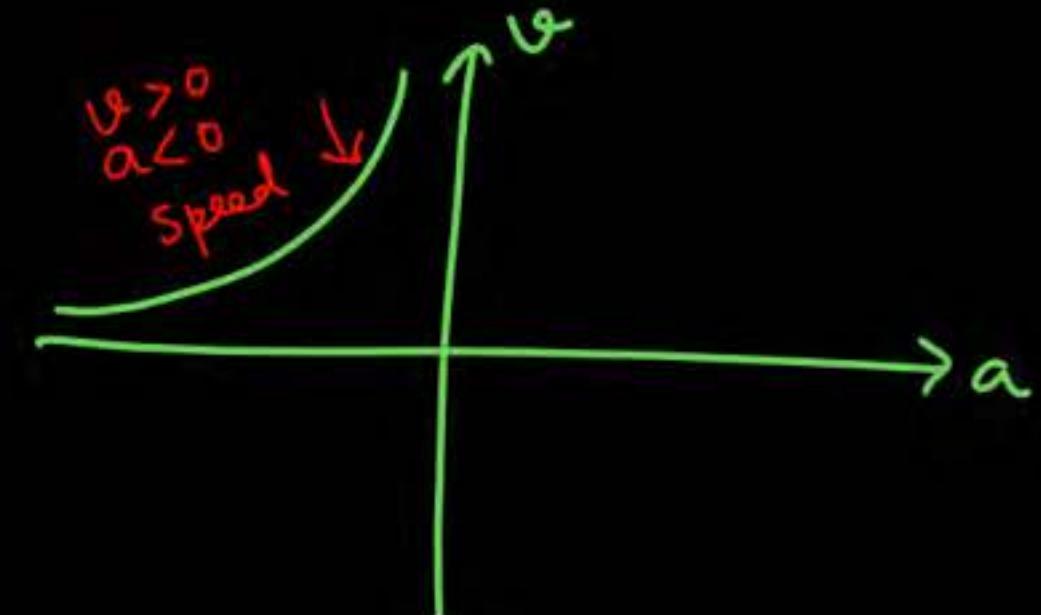
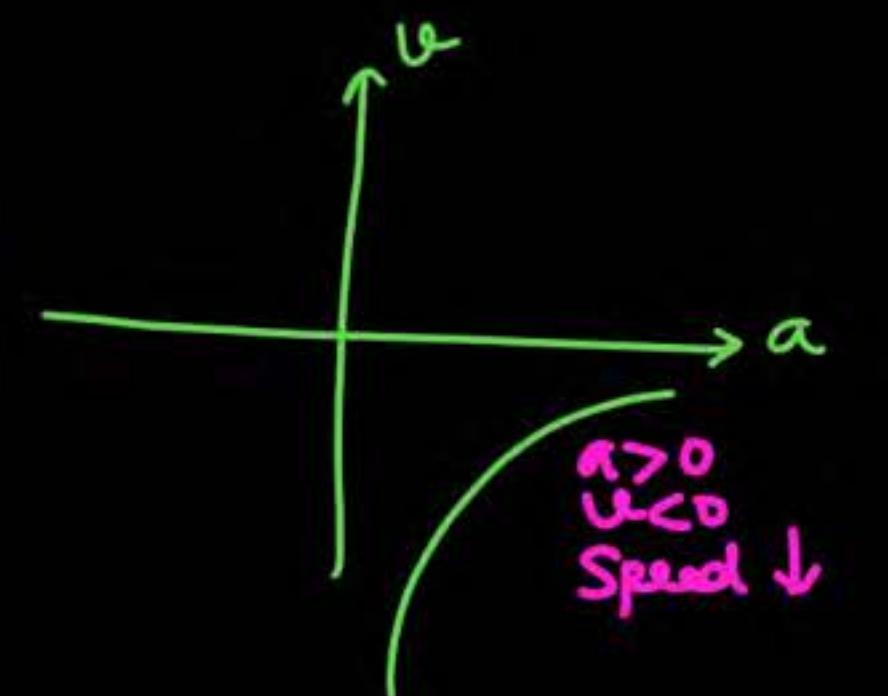
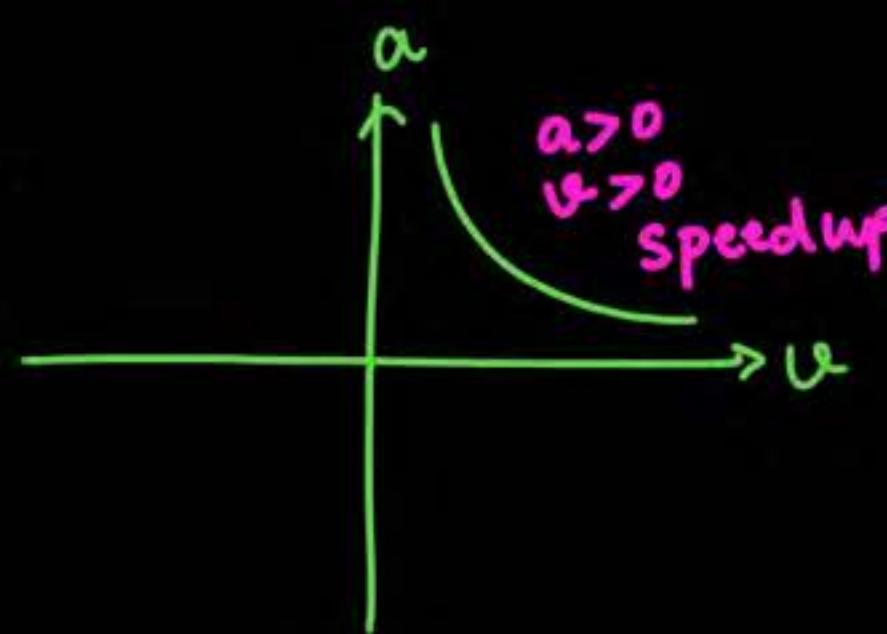
~~C~~ $\approx 0\%$

~~D~~ \approx ~~ET~~ ~~ET~~ \approx ~~ET~~ \approx 7%



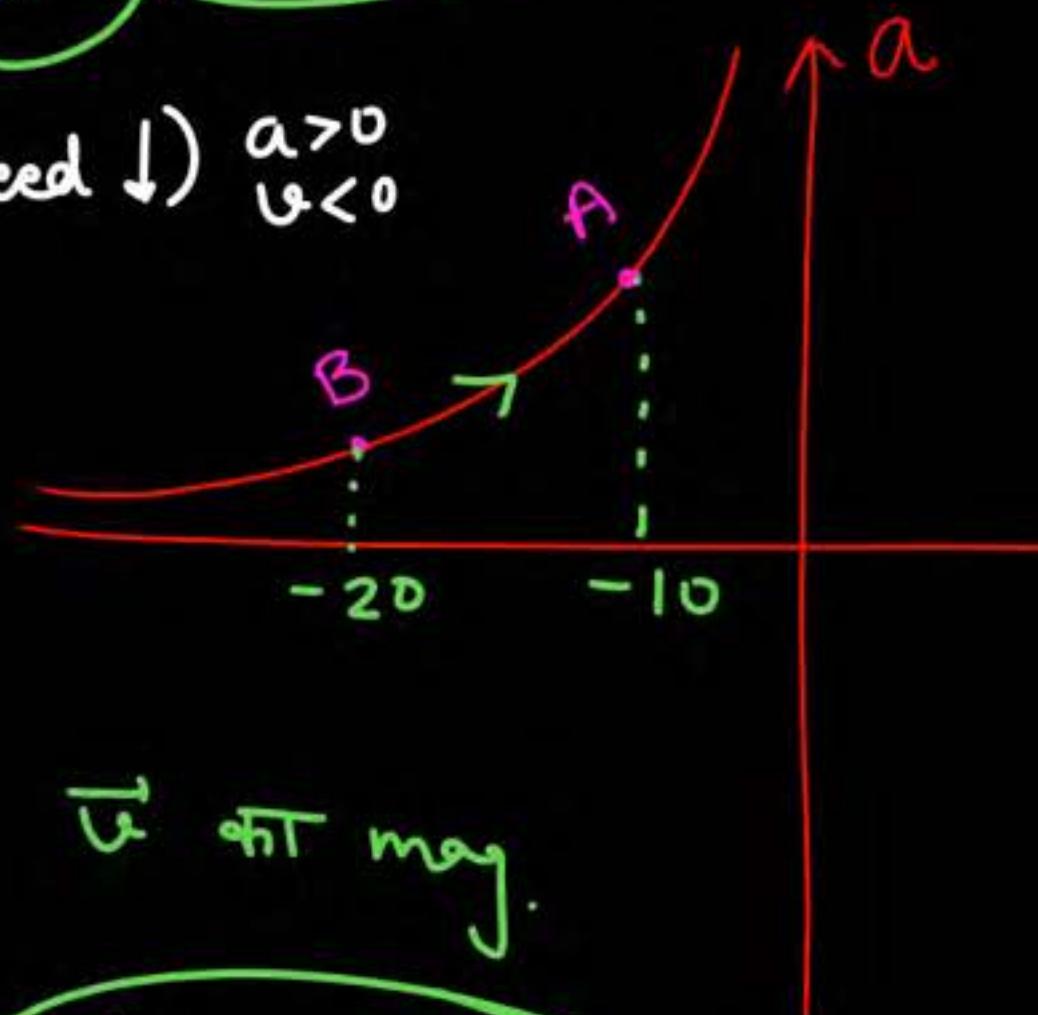
- ① Velocity is decreasing X
- ② " " increasing ✓
- ③ acc is increasing X
- * ④ acc is decreasing ✓

Q



Q HW next dn = Dis

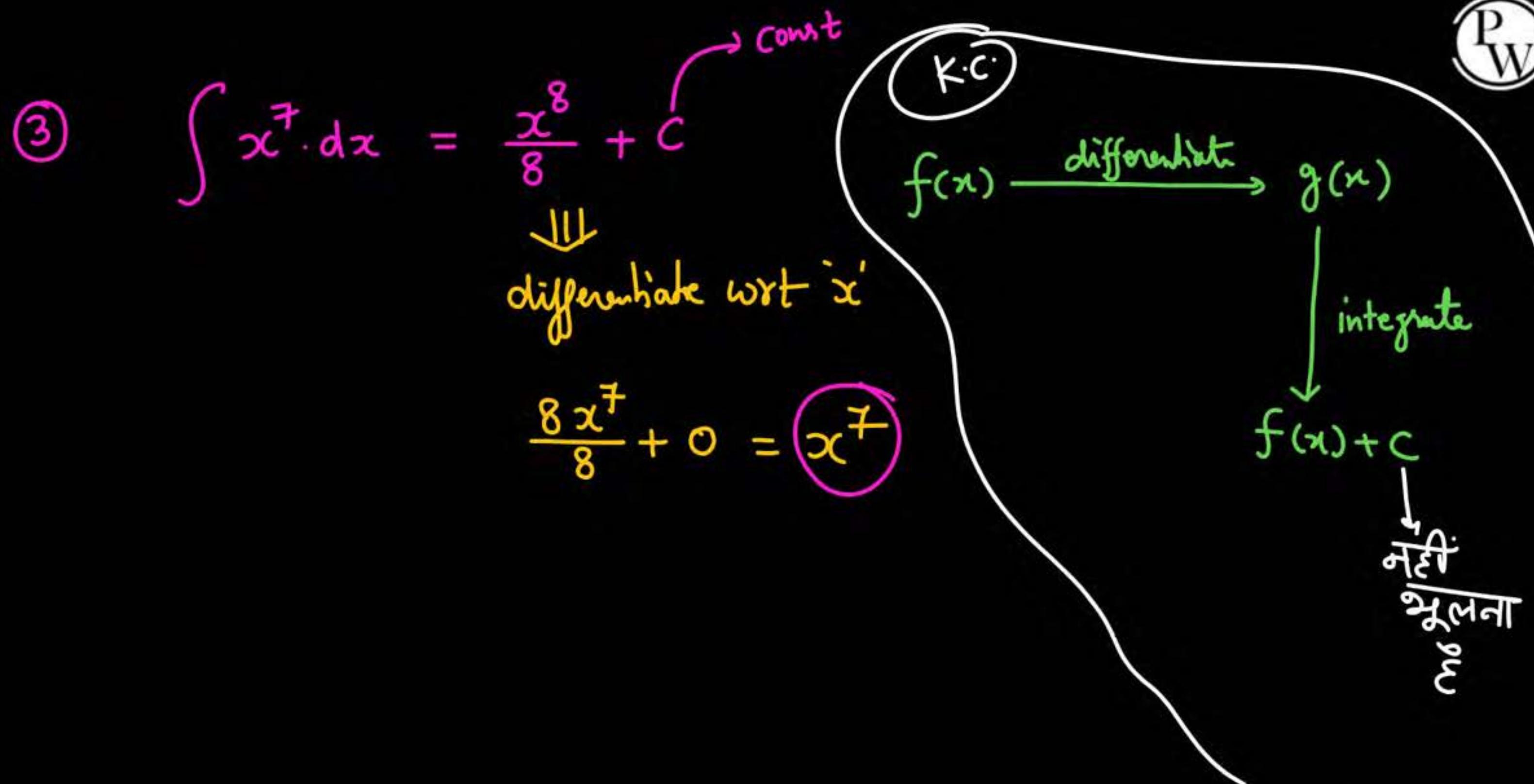
(Speed ↓) $a > 0$
 $v < 0$



\vec{v} ~~at~~ mag.

B → A

- ① acc is increasing
- ② " " decreasing = ?
- ③ v " increasing
- ④ v is decreasing



Q

$$\textcircled{1} \quad x^3 \text{ का diff. wrt } x \Rightarrow 3x^2 \Rightarrow \int 3x^2 dx = 3 \int x^2 dx \\ = 3 \frac{x^3}{3} + C \\ = x^3 + C$$

$$\textcircled{2} \quad (x^3 + 5) \text{ का differentiation wrt } x \Rightarrow 3x^2 + 0$$

$$\int 3x^2 \cdot dx = x^3 + C$$

$$\textcircled{3} \quad (x^3 + 25) \text{ का diff. बताओ wrt } x \Rightarrow 3x^2 + 0$$

$$\int 3x^2 dx = x^3 + C$$

④

$$\int x^{10} dx = \frac{x^{11}}{11} + C$$

⑤

$$\int x^{50} dx = \frac{x^{51}}{51} + C$$

⑥

$$\int x^{25} dx = \frac{x^{26}}{26} + C$$

⑦

$$\int x^{-5} dx = \frac{x^{-5+1}}{-5+1} + C$$

$$\textcircled{8} \quad \int x^2 dx = \frac{x^3}{3} + C$$

$$\textcircled{9} \quad \int x^7 dx = \frac{x^8}{8} + C$$

$$\textcircled{10} \quad \int (x^2 + x^3) dx = \frac{x^3}{3} + \frac{x^4}{4} + C$$

$$= \int x^2 dx + \int x^3 dx$$

$$\textcircled{11} \quad \begin{aligned} \int 5x^4 dx &= 5 \int x^4 dx \\ &= 5 \frac{x^5}{5} + C \\ &= x^5 + C \end{aligned}$$

$$\textcircled{12} \quad \int 6x^5 dx = x^6 + C$$

P
W

$$\textcircled{13} \quad \int (3x^2 + 7x^6) dx$$

$$= 3\frac{x^3}{3} + 7\frac{x^7}{7} + C = x^3 + x^7 + C$$

$$\textcircled{14} \quad \int x^{-3} dx = \frac{x^{-3+1}}{-3+1} + C$$

$$= -\frac{1}{2x^2} + C$$

देखाया गया
लिएगा।।।

$$\textcircled{15} \quad \int \frac{1}{x^3} dx = \int x^{-3} dx$$

$$= -\frac{1}{2x^2} + C$$

$$\textcircled{16} \quad \int \left(\frac{1}{x^2} + \frac{1}{x^3} \right) dx = \int (x^{-2} + x^{-3}) dx$$

$$= -\frac{1}{x} - \frac{1}{2x^2} + C$$

$$\textcircled{17} \quad \int \left(\frac{1}{x^9} + \frac{1}{x^{10}} \right) dx = \int (x^{-9} + x^{-10}) dx$$

$$= \frac{x^{-9+1}}{-9+1} + \frac{x^{-10+1}}{-10+1} + C = \boxed{-\frac{x^{-8}}{8} - \frac{x^9}{9} + C}$$

$$\textcircled{18} \quad \int (3x^2 - 4x^3) dx = x^3 - x^4 + C$$

$$\textcircled{19} \quad \int dx = \int 1 dx = \int x^0 dx = \frac{x^{0+1}}{0+1} + C$$

$$= x$$

$$\boxed{\int dx = x + C}$$

$$\int 5dx = 5\int dx = 5x + C$$

$$\int 7dx = 7x + C$$

$$\begin{aligned} & \int (3x^2 + 4x^3 + 5)dx \\ &= 3 \cdot \frac{x^3}{3} + 4 \cdot \frac{x^4}{4} + 5x + C \\ &= x^3 + x^4 + 5x + C \end{aligned}$$

सही तरीका ✓

Q

$$\int (2x + 7x^6 + 10) dx = x^2 + x^7 + 10x + C$$

III

differentiate wrt x

same

$$2x + 7x^6 + 10 + 0$$

$$\int (2t + 7t^6 + 10) dt = t^2 + t^7 + 10t + C$$

** very very imp

$$\text{Q} \quad \frac{d}{dx} \sin(2x+3) = \cos(2x+3) \cdot [2+0] = 2\cos(2x+3)$$

$$\frac{d}{dx} \sin(ax+b) = a\cos(ax+b)$$

$$\frac{d}{dx} e^{2x+3} = e^{2x+3} \cdot (2+0) = 2e^{2x+3}$$

$$\frac{d}{dx} \sin(2x+3) = 2\cos(2x+3)$$

$$\int 2\cos(2x+3) dx = \sin(2x+3) + C$$

$$\int \cos(2x+3) dx = \frac{1}{2} \sin(2x+3) + C'$$

$$\int \cos x dx = \sin x + C$$

$$\int \cos(ax+b) dx = \frac{1}{a} \sin(ax+b) + C$$

$$\int e^{2x} dx = \frac{1}{2} e^{2x} + C$$

$$\frac{d}{dx} \sin(2x) = 2 \cdot \cos 2x$$

diff →
integ.

$$\int 2 \cos 2x \cdot dx = \sin 2x + C$$

$$\int \cos 2x \cdot dx = \frac{1}{2} \sin 2x + \frac{C}{2}$$

$$\sin x \xrightarrow{\text{diff}} \cos x$$

$$\int \cos x \cdot dx = \sin x + C$$

$$\int \boxed{\cos 2x} \cdot dx = \sin 2x + C \times$$

III
differentielle

$$\boxed{2(\cos 2x)} + 0$$

$$\int \cos 2x \cdot dx = \boxed{\frac{1}{2} \sin 2x + C}$$

III
differentielle

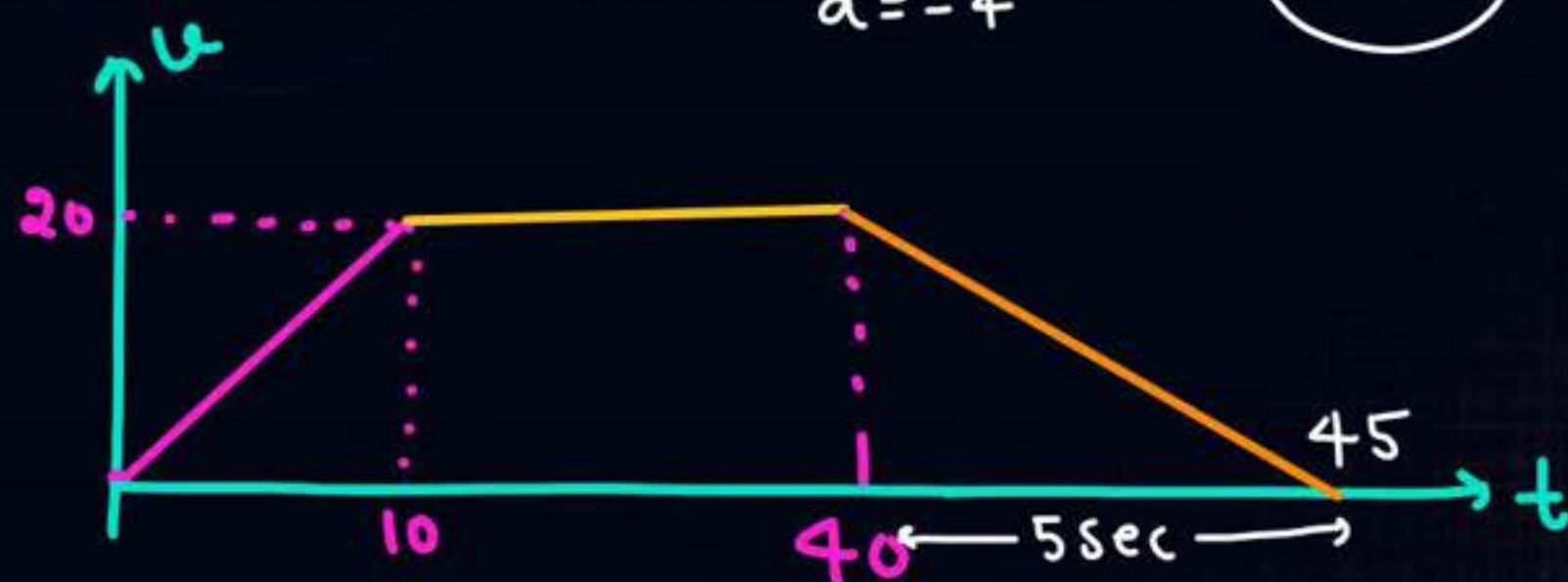
$$\cos 2x = \frac{1}{2} (\cos 2x) \times 2$$

Question

Note ✓

A particle starts from rest, accelerates at 2 m/s^2 for 10 s and then goes at constant speed for 30 s and then decelerates at 4 m/s^2 till it stops. What is the distance travelled by it:

- A 750 m
- B 800 m
- C 700 m
- D 850 m



$$\text{Area} = \frac{1}{2} \times (30 + 45) \times 20 = \underline{\underline{750}}$$

Ans : (A)

Question

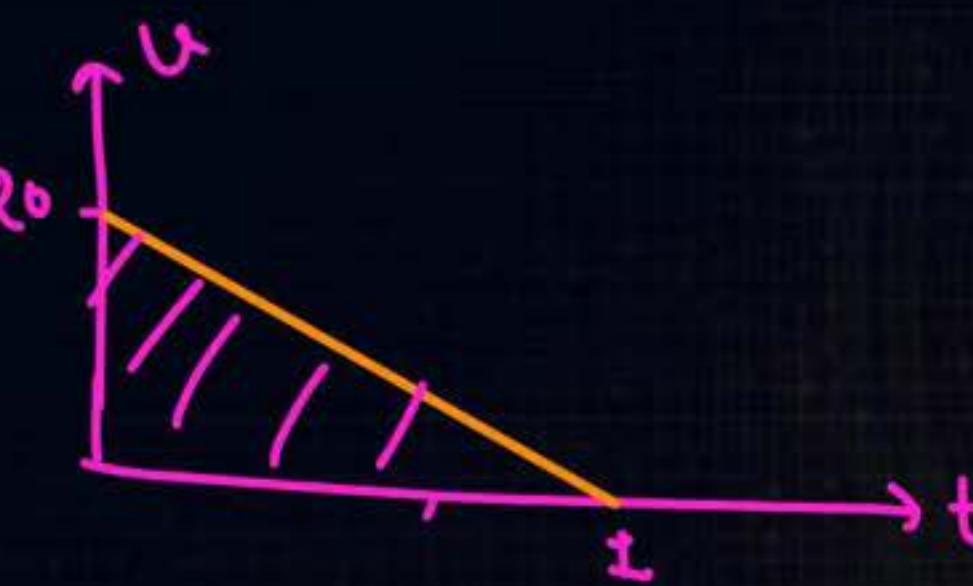
note X

The driver of a car which is moving on a straight horizontal road with a speed of 72 kmh^{-1} applies brakes. If the retardation produced is 20 ms^{-2} , the distance moved by the car before coming to rest will be

- A 10 m
- B 8 m
- C 6 m
- D 2 m

$$u = 72 \frac{\text{km}}{\text{hr}} = 72 \times \frac{5}{18} \text{ m/s} = 20 \text{ m/s}$$

$$\text{Area} = \frac{1}{2} \times 20 \times 1 \\ = 10$$



Ans : (A)

Q A particle starts motion having initial velocity 20 m/s and it moves with const acc of 10 m/s².

① find velocity at t = 4 sec

② find displacement of particle from t = 0 \longrightarrow t = 4 sec

③ find displacement in 4th sec

$$S_n = u + \frac{1}{2}(2n-1)a$$

$$S_n = 20 + \frac{1}{2} \cdot (2 \times 4 - 1) \times 10$$

$$= 20 + 35 = 55$$

$$u = 20$$

$$a = 10$$

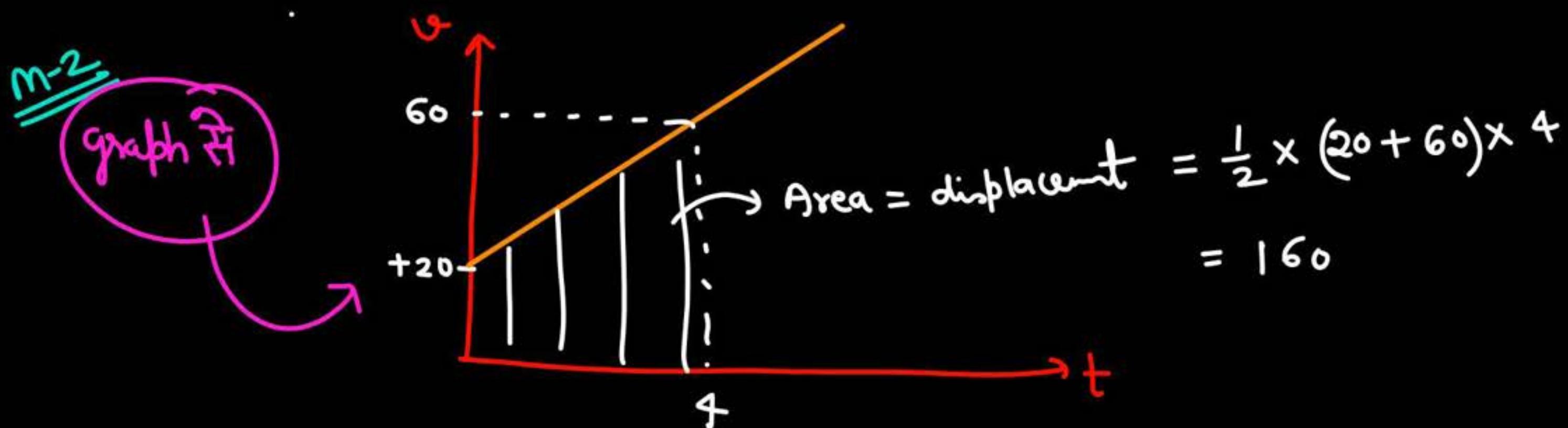
$$\textcircled{1} \quad t = 4, \Rightarrow v = u + at \\ = 20 + 10 \times 4$$

$$v = 60$$

$$\textcircled{2} \quad S = ut + \frac{1}{2}at^2$$

$$= 20 \times 4 + \frac{1}{2} \times 10 \times 4^2 = 160$$

Q A particle starts motion having initial velocity 20 m/s and it moves with const acc of 10 m/s^2 .



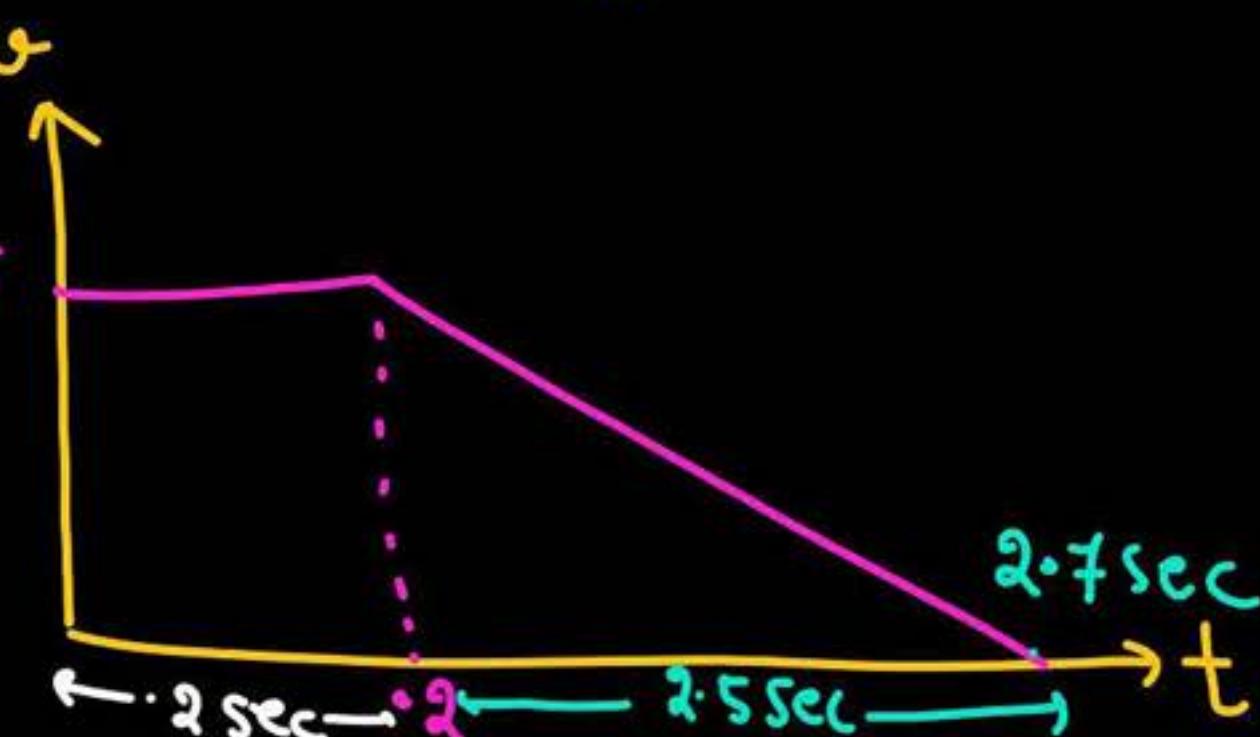
19. A driver takes 0·20 s to apply the brakes after he sees a need for it. This is called the reaction time of the driver. If he is driving a car at a speed of 54 km/h and the brakes cause a deceleration of 6 m/s^2 , find the distance travelled by the car after he sees the need to put the brakes on.

HCV
note
find stopping distance.

$$54 \text{ km/hr} = 54 \times \frac{5}{18} = 15 \text{ m/s}$$

$$\text{Area} = \frac{1}{2} \times (2 + 2.7) \times 15$$

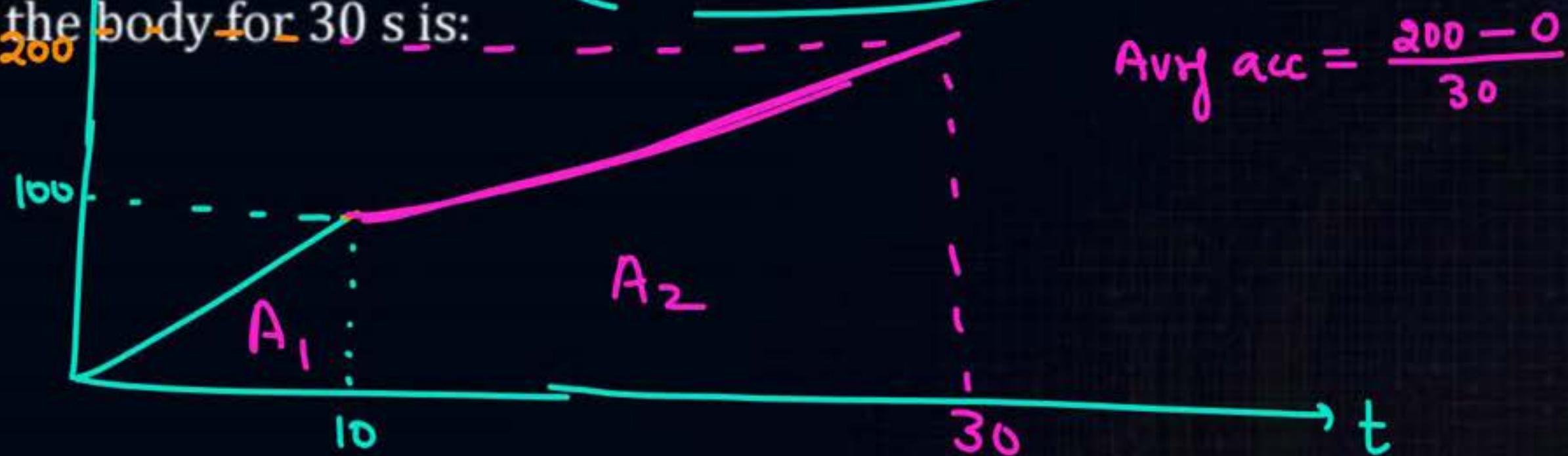
$$= 21.75$$



Question

Note X

If a body starting from the rest travels with a uniform acceleration of 10 ms^{-2} for first 10 second and with uniform acceleration 5 ms^{-2} for next 20 seconds, then average acceleration of the body for 30 s is:



- A 15 ms^{-2}
- B 10 ms^{-2}
- C 20 ms^{-2}
- D $20/3 \text{ ms}^{-2}$

$$\text{Displac} = A_1 + A_2$$

Ans : (D)

Question

notex

Rough copy

P
W

A car is moving with a velocity of 30 m/s. The driver applied brake for 5 seconds to bring it down to zero. What is the average acceleration? $= \frac{v_f - v_i}{\text{total time}} = \frac{0 - 30}{5}$

$$= -6 \checkmark$$

- A -5 m/s^2
- B 6 m/s^2
- C -6 m/s^2
- D ZERO

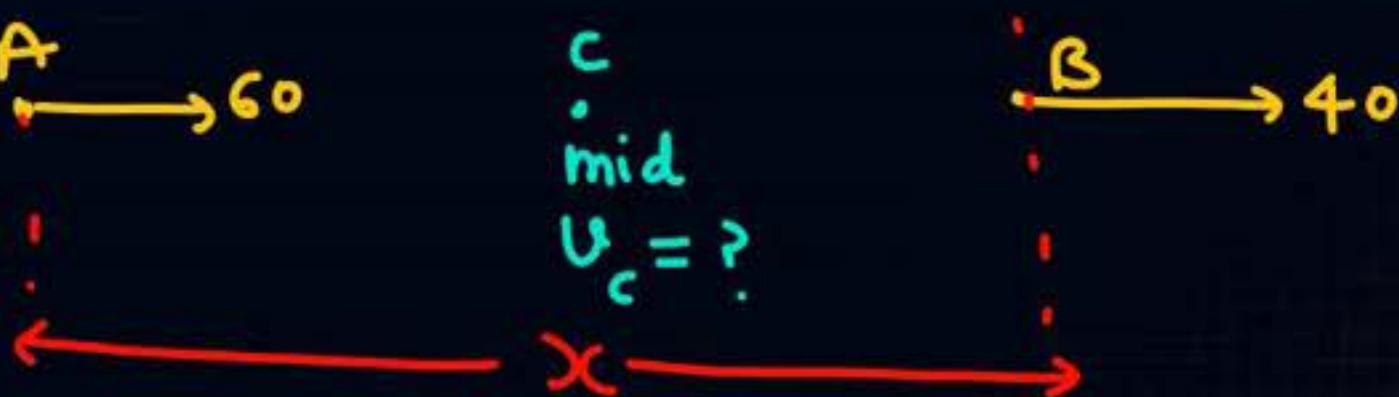
Ans : (C)

Question

Notes ✓

A truck travelling with uniform acceleration crosses two points A and B with velocities 60 m/s and 40 m/s respectively. The speed of the body at the midpoint of A and B is nearest to:

- A 17 m/s
- B 20 m/s
- C 19.49 m/s
- D 50.9 m/s



$\text{A} \rightarrow \text{B}$

$(\text{A} \rightarrow \text{C})$

$$40^2 = 60^2 + 2ax \Rightarrow 2ax = -2000$$

$$U_c^2 = 60^2 + \cancel{2ax} \frac{x}{2}$$

$$U_c^2 = 3600 - 1000 = 2600$$

$$U_c = 10\sqrt{26}$$

$$\begin{aligned} 40^2 &= 1600 \\ 60^2 &= \underline{3600} \\ &\quad -2000 \end{aligned}$$

Ans : **(A)**

Question

Notes ✓

Both

P
W

A particle having initial velocity 10 m/s moves with a constant acceleration 5 ms^{-2} , for a time 15 second along a straight line, what is the displacement of the particle in the last 2 second?

A 160 m

$t = 0 \rightarrow t = 15$

B 200 m

$$S_{15} = 10 \times 15 + \frac{1}{2} 5 (15)^2$$

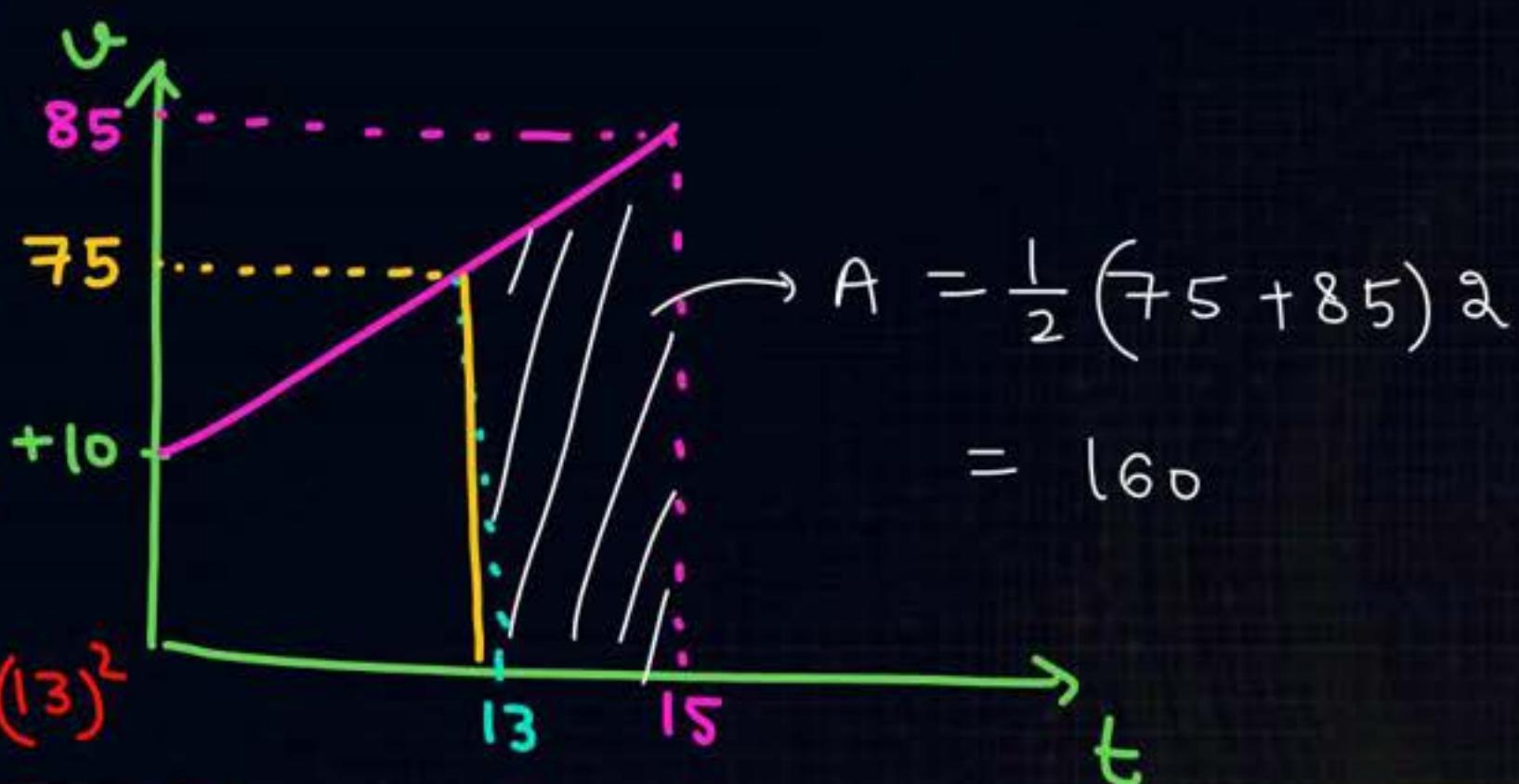
C 210 m

$$S_{13} = 10 \times 13 + \frac{1}{2} \times 5 \times (13)^2$$

D 230 m

$$\text{Ans } S_{15} - S_{13} = 20 + \frac{5}{2} [15^2 - 13^2]$$

$$= 20 + \frac{5}{2} \times 28 \times 2 = 20 + 140 = 160$$



Ans : (A)

Question

Class notes ✓

2 m/s

A bullet moving with a velocity of 200 cm/s penetrates a wooden block and comes to rest after travelling 4 cm inside it. What velocity is needed for travelling distance of 9 cm in same block?

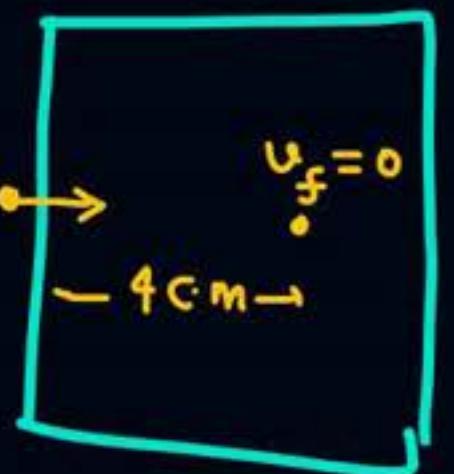
A 100 cm/s

B 136.2 cm/s

C 300 cm/s

D 250 cm/s

$u = 2$



$0^2 = 2^2 + 2a \times \frac{4}{100}$

$-4 = \frac{8}{100} a$

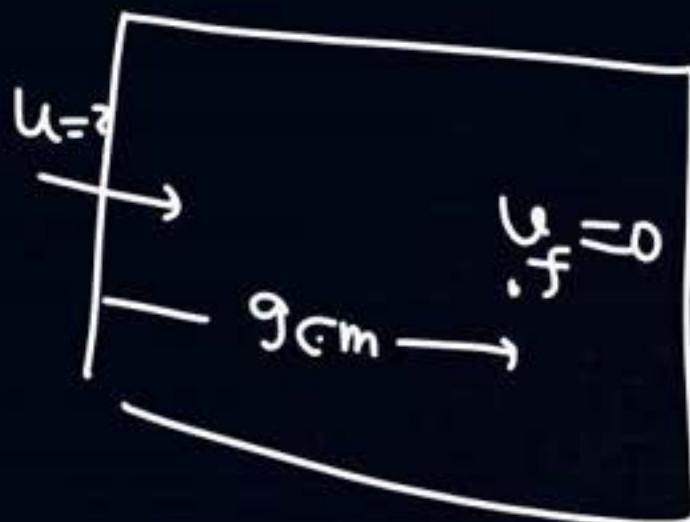
$a = -50$

$0^2 = u^2 + 2as$

$0 = u^2 + 2 \times (-50) \left(\frac{9}{100} \right)$

$u^2 = 9$

$u = 3$



Ans : (C)

Question

note X

$F=ma$

$u = 10$

$v_f = 0$

A car moving with a velocity of 10 m/s can be stopped by the application of a constant force F in a distance of 20m. If the velocity of the car is 30 m/s. It can be stopped by this force in $\alpha = \text{const}$ $S = 20$.

A $20/3$ m

B 20 m

C 60 m

D 180 m

$$\begin{aligned}v^2 &= u^2 + 2as \\0 &= 10^2 + 2a \cdot 20 \\a &= -\frac{100}{40} = -\frac{5}{2}\end{aligned}$$

$0^2 = 30^2 + 2 \times a \times x$

$0 = 900 + 2 \left(-\frac{5}{2}\right) x$

$5x = 900$

$x = 180$

Ans : (D)

Note ✓

17. A bullet going with speed 350 m/s enters a concrete wall and penetrates a distance of 5.0 cm before coming to rest. Find the deceleration.

μ_{kN}

Rough

$$v_f = 0 \quad a = ?$$

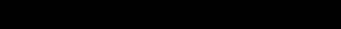
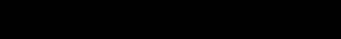
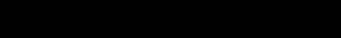
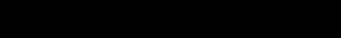
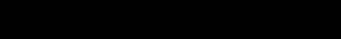
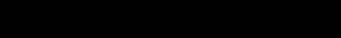
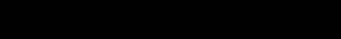
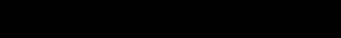
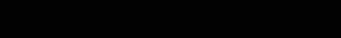
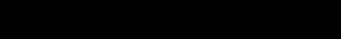
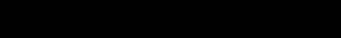
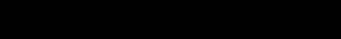
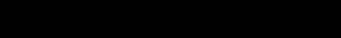
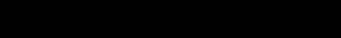
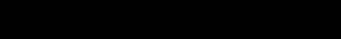
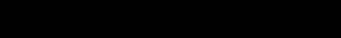
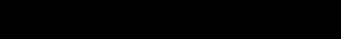
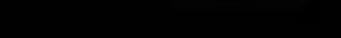
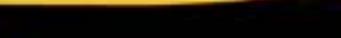
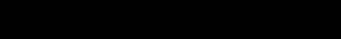
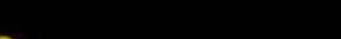
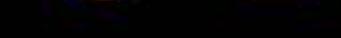
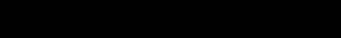
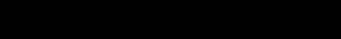
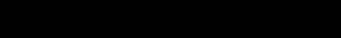
1 min

$$\begin{array}{r} 35 \\ 35 \\ \hline 1225 \end{array}$$

$u =$

350 m/s

5.0 cm



Q A particle covered 100m distance in first 10 sec. and in next 10 sec it travel 200m. find distance travel in next 10 sec. (acc is const)

300 X
400 X



$$t=0 \rightarrow t=10 \Rightarrow 100 = u \times 10 + \frac{1}{2} a \cdot 10^2$$

$$100 = 10u + 50a \quad \text{--- (1)}$$

$$\textcircled{1} - \textcircled{2}$$

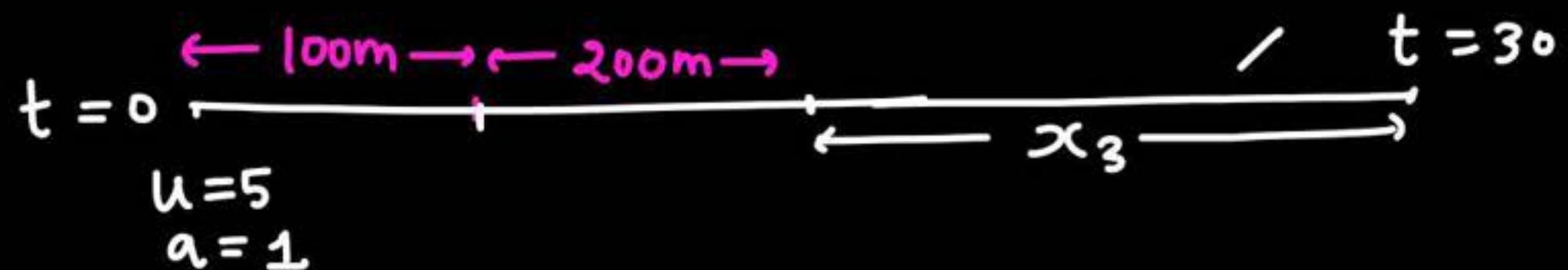
$$-50 = -50a$$

$$t=0 \rightarrow t=20 \Rightarrow 300 = u \cdot 20 + \frac{1}{2} \cdot a \cdot (20)^2$$

$$300 = 20u + 200a$$

$$150 = 10u + 100a \quad \text{--- (2)}$$

$a = 1$
$u = 5$



$$u=5$$

$$a=1$$

$$\boxed{t=0 \longrightarrow t=30}$$

$$300 + x_3 = ut + \frac{1}{2}at^2$$

$$300 + x_3 = 5 \times 30 + \frac{1}{2} \times 1 \times (30)^2$$

$$300 + x_3 = 150 + 450$$

$$\boxed{x_3 = 300}$$

A particle, after starting from rest experiences, constant acceleration for 20 seconds. If it covers a distance of S_1 , in first 10 seconds and distance S_2 in next 10 sec, then

(a) $S_2 = S_1/2$

(c) $S_2 = 2S_1$

(b) $S_2 = S_1$

~~(d)~~ $S_2 = 3S_1$

$$S_1 = 0 + \frac{1}{2} \cdot a \cdot 10^2$$

$$S_1 + S_2 = 0 + \frac{1}{2} \cdot a \cdot (20)^2$$

$$\frac{S_1 + S_2}{S_1} = \frac{400}{100}$$

$$1 + \frac{S_2}{S_1} = 4$$

$$\frac{S_2}{S_1} = 3$$

$S_2 = 3S_1$

Q A particle travels x_1 in 1st 10 sec & x_2 in next 10 sec
find distance travelled in next 10 sec. ($a \rightarrow \text{const}$)

$$x_1 = u \times 10 + \frac{1}{2} \cdot a \cdot 10^2$$

$$x_1 + x_2 = u \times 20 + \frac{1}{2} \cdot a \cdot 20^2$$

$$x_1 + x_2 + x_3 = u \times 30 + \frac{1}{2} \cdot a \cdot 30^2$$

$$\begin{aligned} a &= \checkmark \\ u &= \checkmark \end{aligned}$$

Q A particle starts motion from origin towards $+x$ -axis with initial velocity 60 m/s and const acc = -10 m/s^2

① When particle will come to rest

$$t = 6$$

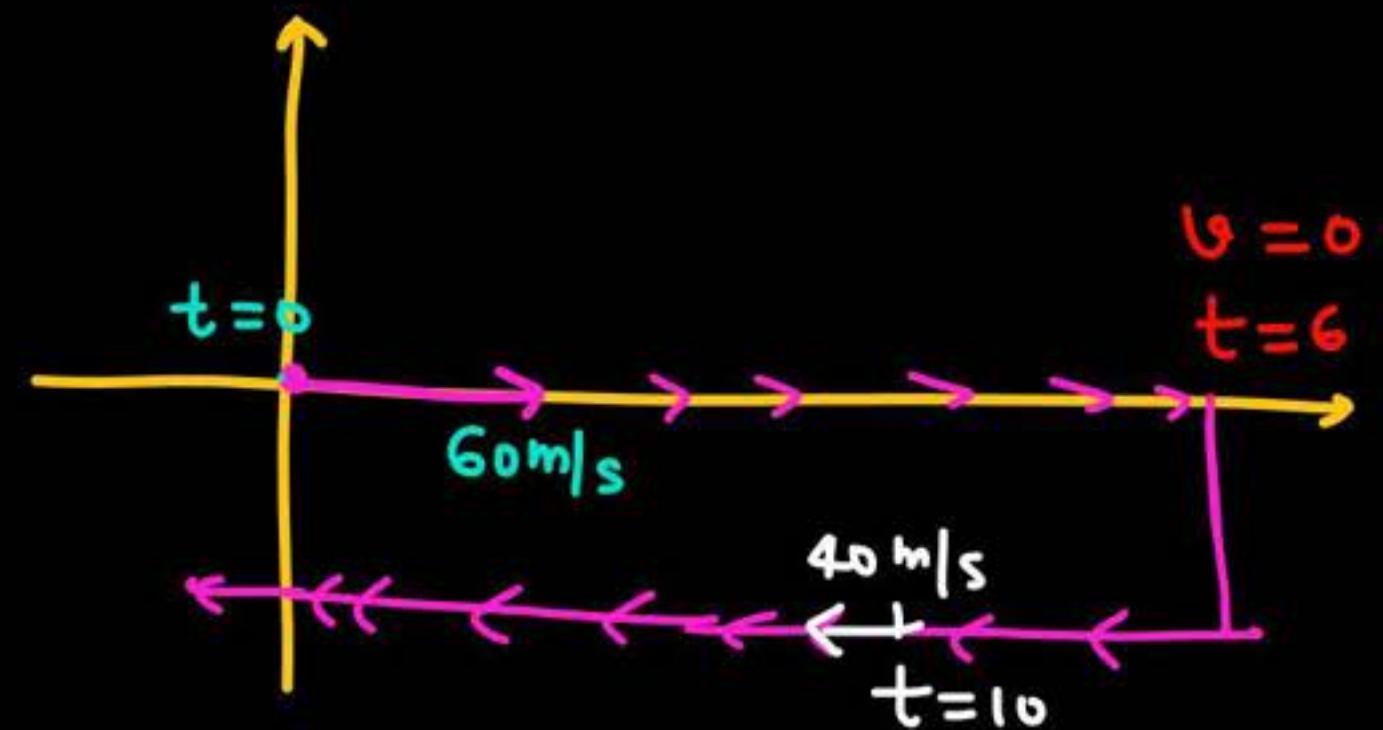
② find v at $t = 2$, $v = 40$

" v at $t = 10\text{ sec}$

$$v = -40$$

③ Displacement in 10 sec

$$S = 60 \times 10 + \frac{1}{2} \times (-10) \times 10^2 = 600 - 500 = 100$$



A particle starts from rest at $t = 0$ and $x = 0$ to move with a constant acceleration $= +2 \text{ m/s}^2$, for 20 seconds. After that, it moves with -4 m/s^2 for the next 20 seconds. Finally, it moves with positive acceleration for 10 seconds until its velocity becomes zero.

- (a) What is the value of the acceleration in the last phase of motion?
- (b) What is the final x-coordinate of the particle?
- (c) Find the total distance covered by the particle during the whole motion.



Ans

- (a) 4 m/s^2
- (b) 200 m
- (c) 1000 m

A car accelerates with uniform rate from rest on a straight road. The distance travelled in the last second of a three second interval from the start is 15 m then find the distance travelled in first second in m.

Hlw

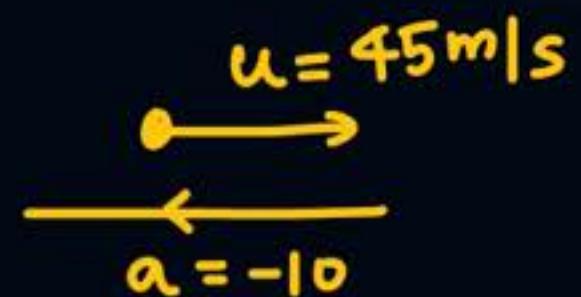
Ans → 3

A particle moving in one-dimension with constant acceleration of 10 m/s^2 is observed to cover a distance of 100 m during a 4s interval. How far will the particle move in the next 4s?

110

Ans 260

Q2



distance travelled in 5th sec.

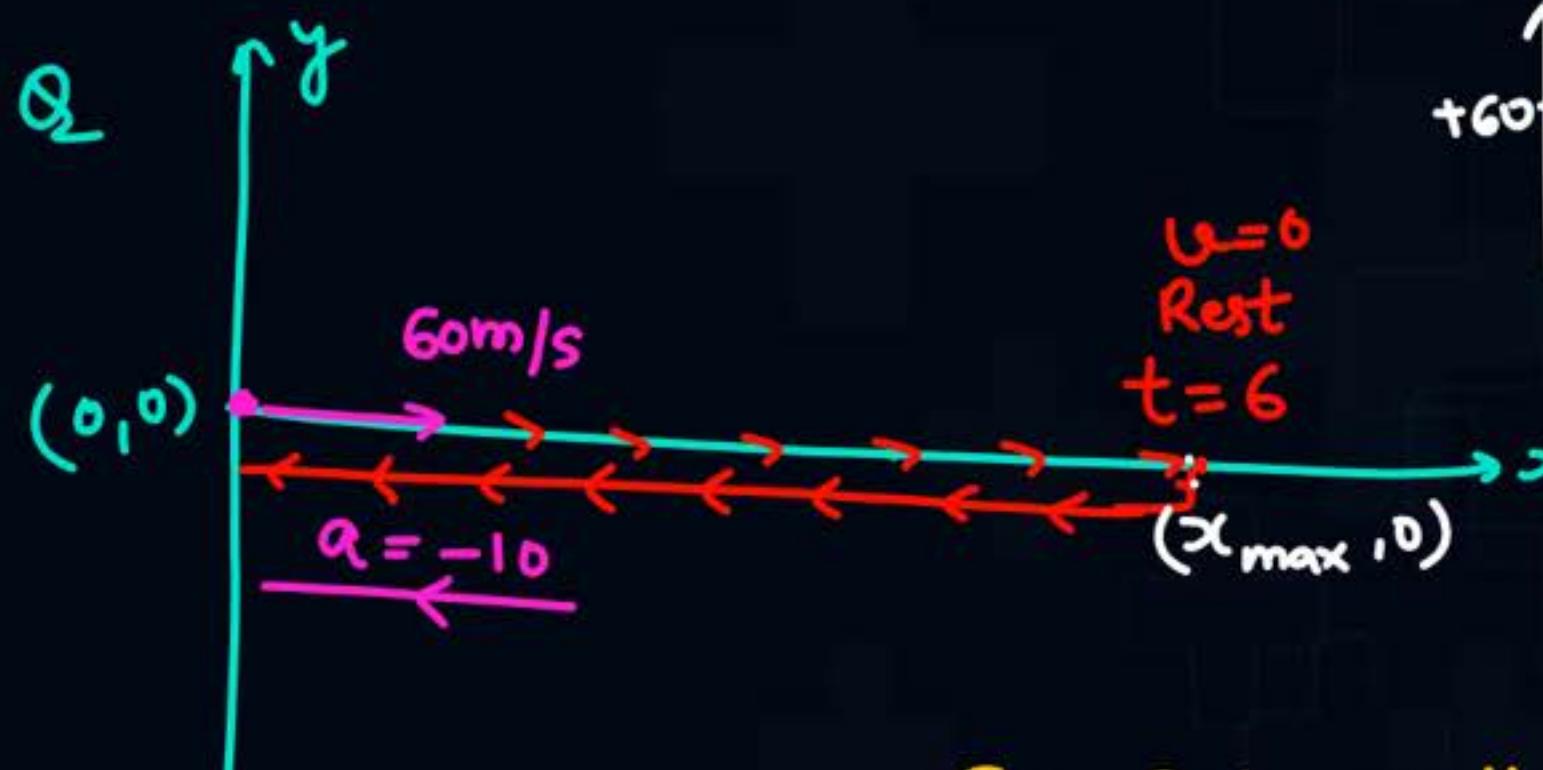
$$\text{Displacement} = A_{\text{अपर}} - A_{\text{तीसरी}} = 0$$

$$\begin{aligned}\text{Distance} &= A_{\text{अपर}} + A_{\text{तीसरी}} \\ &= \frac{25}{20} + \frac{25}{20} = \frac{50}{20} = \underline{2.5}\end{aligned}$$



$$A_{\text{अपर}} = \frac{1}{2} \times 5 \times 5 = \frac{25}{20}$$

$$A_{\text{तीसरी}} = \frac{1}{2} \times 5 \times 5 = \frac{25}{20}$$



$$\textcircled{1} \quad t = 4, v = 20$$

$$\textcircled{2} \quad t = 6, v = 0$$

$$\textcircled{3} \quad t = 8, v = -20$$

$$\textcircled{4} \quad t = 10, v = -40$$

$$\textcircled{5} \quad t = 12, v = -60$$

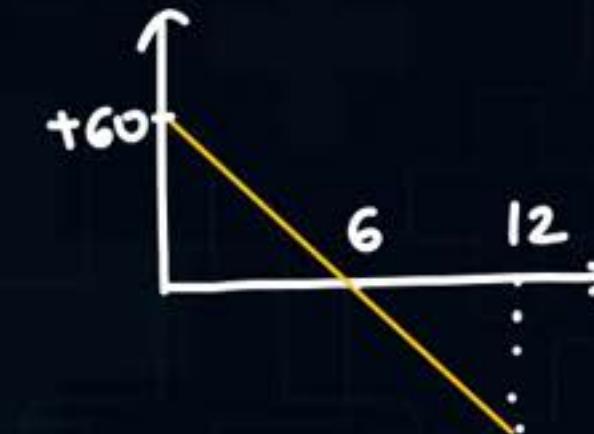
⑥ find location of particle at $t = 4$ sec

$$u = +60, a = -10$$

$$S = ut + \frac{1}{2}at^2$$

$$x = 60 \times 4 - \frac{1}{2} \times 10 \times 4^2$$

$$x = 240 - 80 = \underline{\underline{160}}$$



⑦ find location of particle at $t = 8$ sec

$$x = 60 \times 8 - \frac{1}{2} \times 10 \times 8^2$$

$$x = 480 - 320 = 160$$

③ find where particle comes to rest

$$x_{\max} = ?$$

$$v_f = 0$$

$$v^2 = u^2 + 2as$$

$$0 = (60)^2 + 2(-10)x_{\max}$$

$$\boxed{x_{\max} = 180}$$

Q A particle is projected from ground vertically upward with Velocity 60 m/s. find

① find velocity at $t = 10$

Sign Convention

Consider Upward dir^h (+ve)

$$u = 60 \text{ ऊपर} = +60$$

$$a = 10 \text{ नीचे} = -10$$

$$\textcircled{1} \quad t = 10, \quad v = u + at = 60 + (-10)(10)$$

$$v = -40$$

location

$$t = 10$$

$$y = 60 \times 10 + \frac{1}{2}(-10)(10)^2 = +100$$



$$\downarrow a = g = 10$$

Q

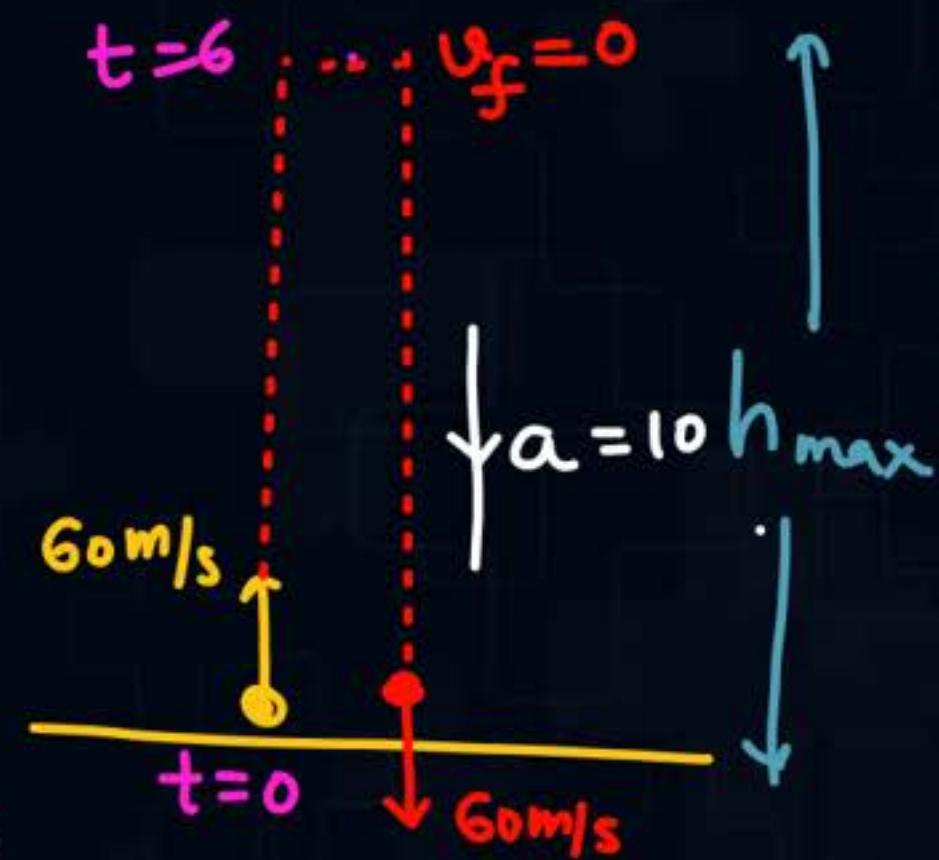
① find v at

$$t=4, v = 20$$

$$t=11, v = -50$$

② when particle will comes to at rest $t=6$

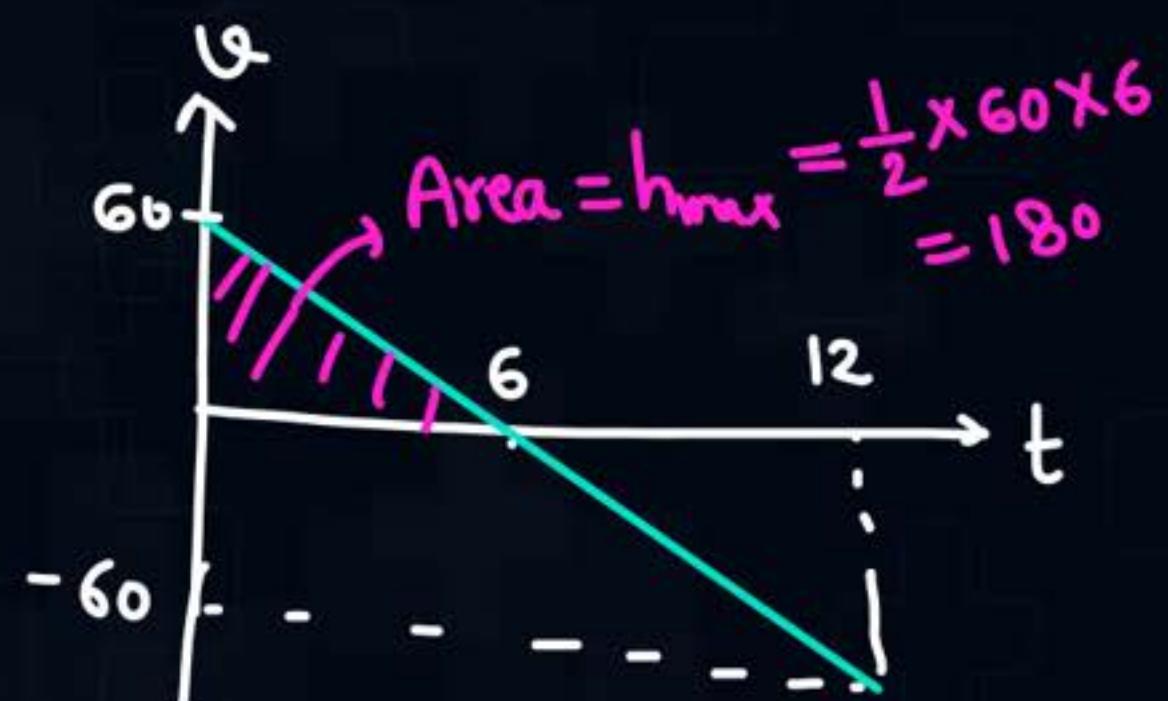
③ find time of flight $\Rightarrow 6+6 = 12 \text{ sec}$

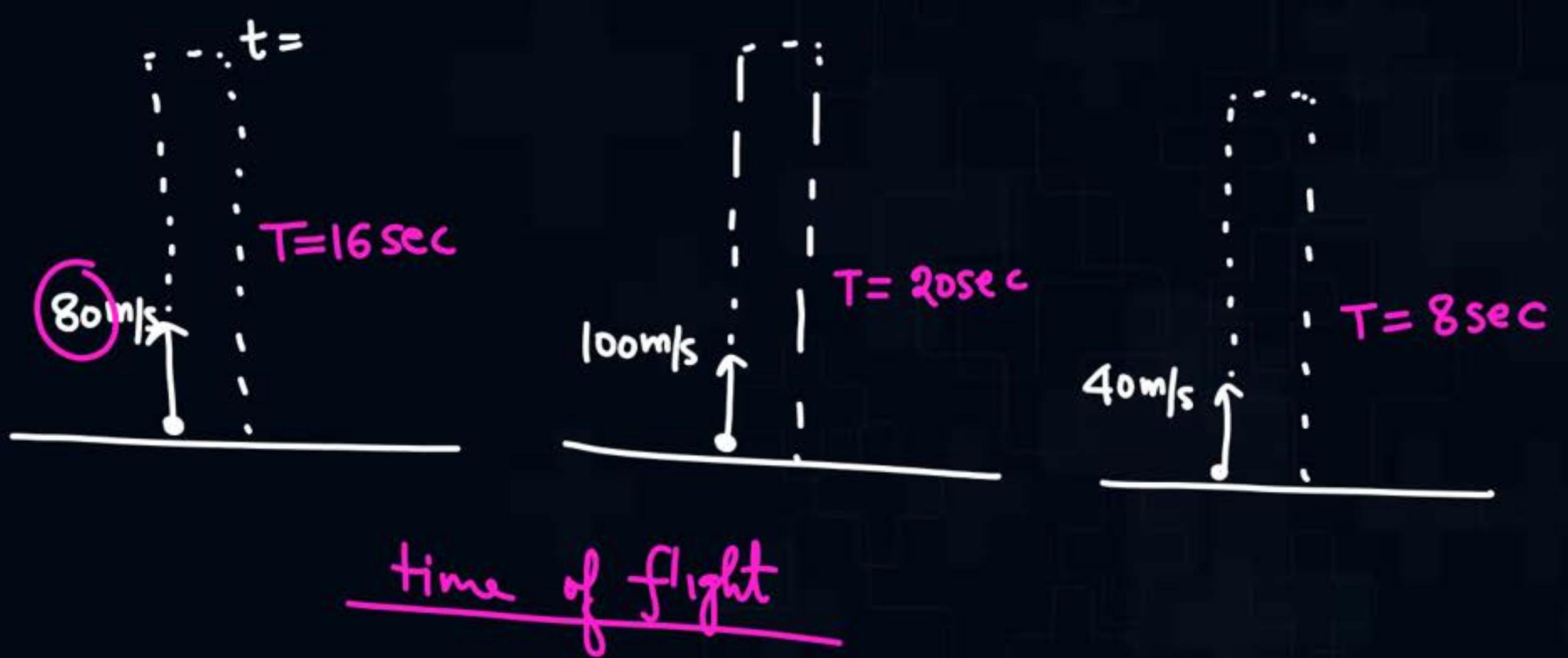


④ max height

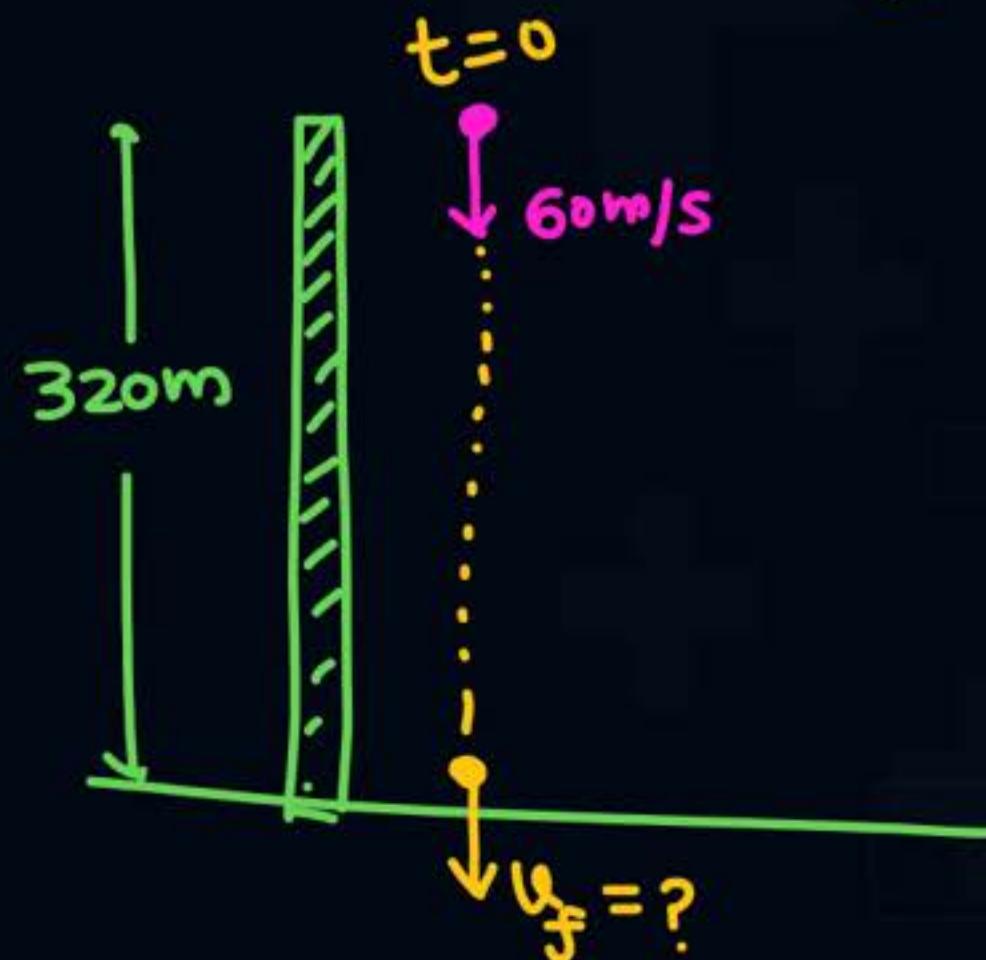
$$0^2 = 60^2 + 2 \times (-10) h_{\max}$$

$$h_{\max} = 180$$





Q



Q when particle will hit the ground
& with what velocity.

तीक्ष्णे \Rightarrow +ve (downward)

$$u = +60 \quad a = +10$$

$$\text{displacement} = s = \text{तीक्ष्णे } 320 \\ s = +320$$

$$s = ut + \frac{1}{2}at^2$$

$$+320 = 60t + \frac{1}{2} \times 10 \times t^2$$

$$t^2 + 12t - 64 = 0$$

$$(t+16)(t-4) = 0$$

$$t = 4 \text{ sec}$$

$$v^2 = u^2 + 2as$$

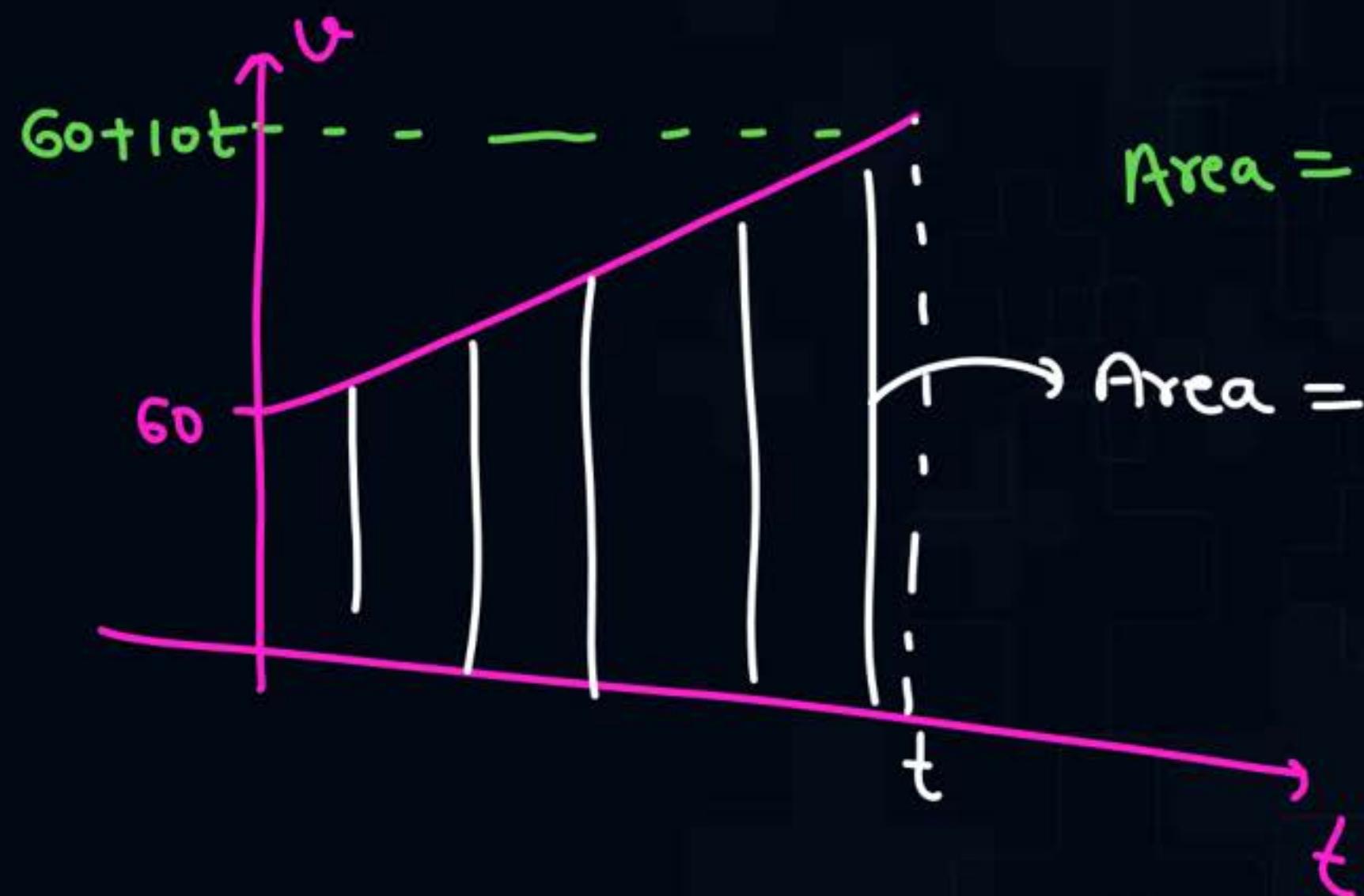
$$v^2 = 60^2 + 2 \times 10 \times 320$$

$$v^2 = 3600 + 6400$$

$$v^2 = 10000$$

$$v = 100 \text{ (तीक्ष्णे)}$$

III
(Common Sense)



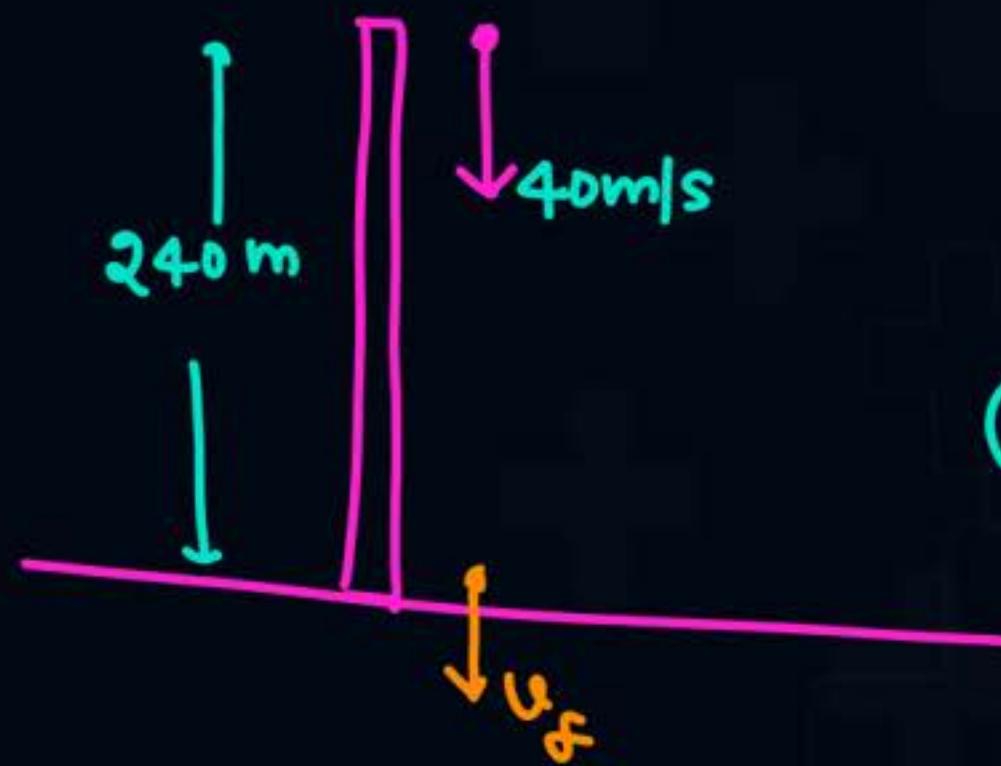
$$\text{Area} = \frac{1}{2}(60+60+10t) \times t = 320$$

$$(120+10t)t = 640$$

$$10t^2 + 120t = 640$$

$$t^2 + 12t - 64 = 0$$

Q



downward = +ve

$$u = +40$$

$$a = +10$$

$$s = +240$$

- ① velocity of particle before it hit the ground

$$u^2 = (40)^2 + 2 \times 10 \times 240$$

$$u = 80 \text{ (Ans)}$$

- ② when particle will hit the ground.

$$s = ut + \frac{1}{2}at^2$$

$$240 = 40t + \frac{1}{2} \times 10 \times t^2$$

$$5t^2 + 40t - 240 = 0$$

$$t^2 + 8t - 48 = 0$$

$$(t+12)(t-4) = 0$$

$$\boxed{t=4}$$

:

Q note ✓



when it will hit the ground

$$u = 0$$

$$a = +10$$

$$S = +500$$

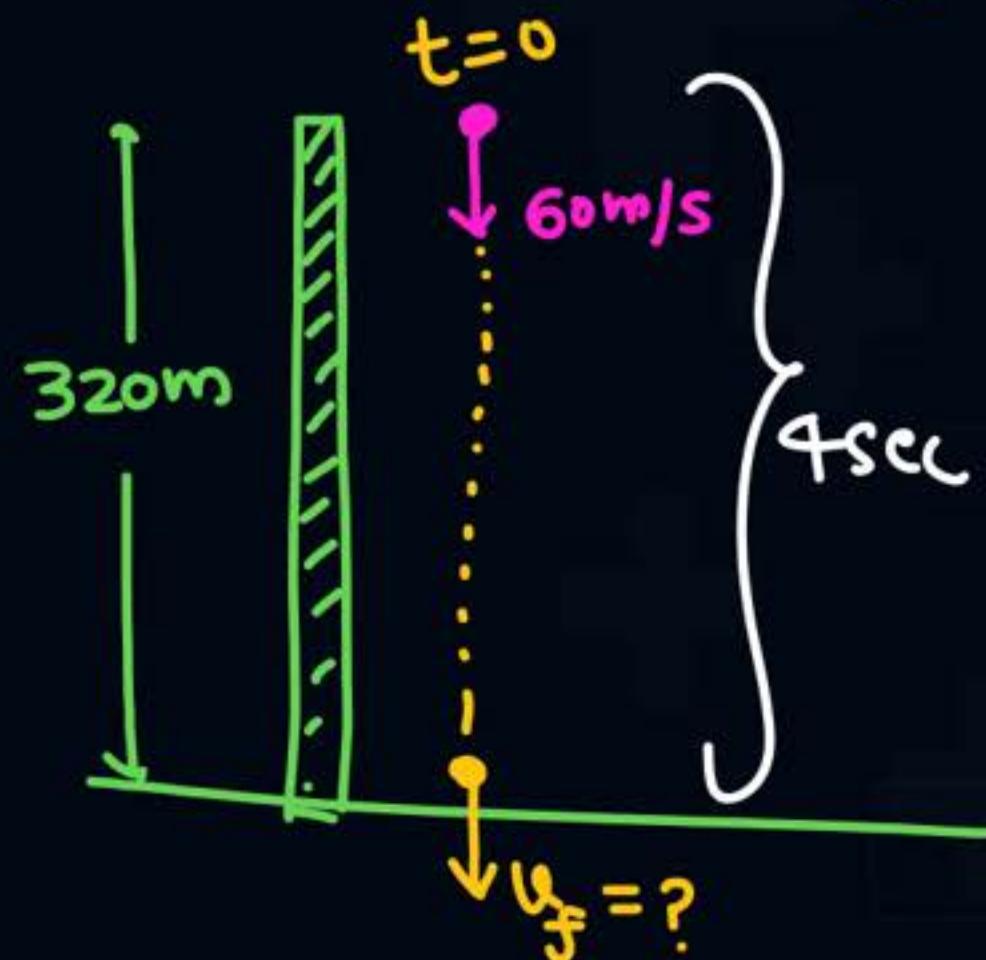
$$500 = 0 + \frac{1}{2} \times 10 \times t^2$$

$$t = \sqrt{\frac{1000}{10}} = 10 \text{ sec}$$

$$v_f^2 = 0^2 + 2 \times 10 \times 500$$

$$\boxed{v_f = 100}$$

Q



Q when particle will hit the ground
& with what velocity.

तीव्रे \Rightarrow +ve (downward)

$$u = +60 \quad a = +10$$

$$\text{displacement} = s = \text{तीव्रे } 320 \\ s = +320$$

$$s = ut + \frac{1}{2}at^2$$

$$+320 = 60t + \frac{1}{2} \times 10 \times t^2$$

$$t^2 + 12t - 64 = 0$$

$$(t+16)(t-4) = 0$$

$$t = 4 \text{ sec}$$

$$v^2 = u^2 + 2as$$

$$v^2 = 60^2 + 2 \times 10 \times 320$$

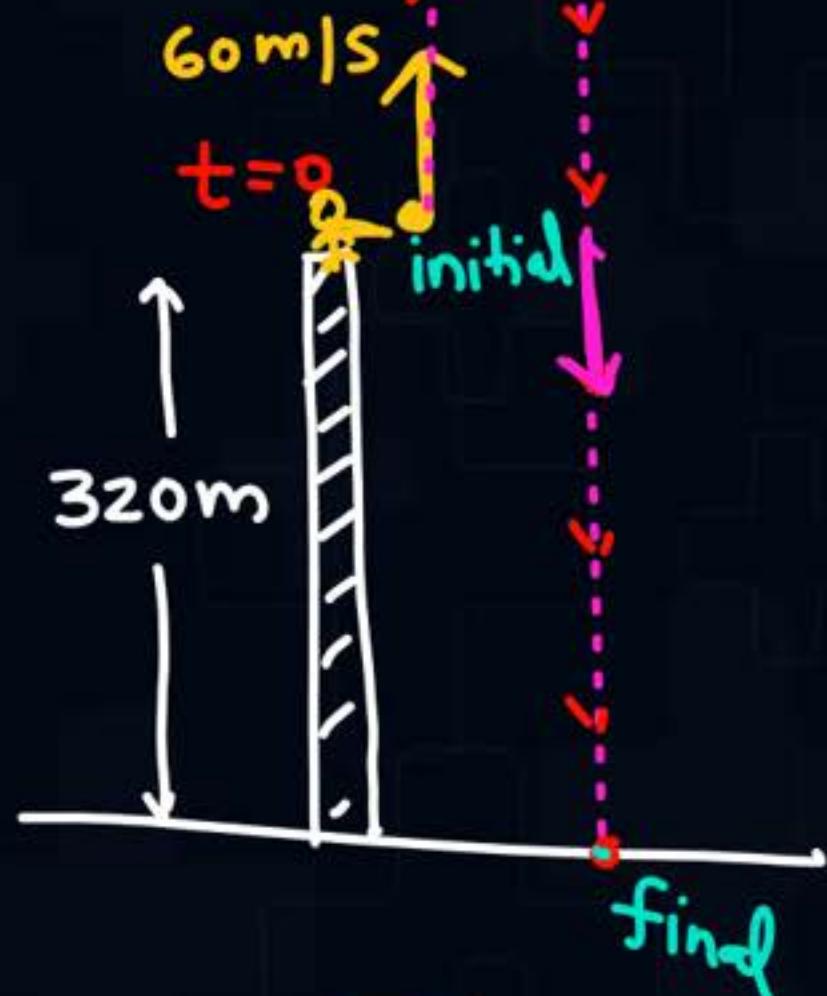
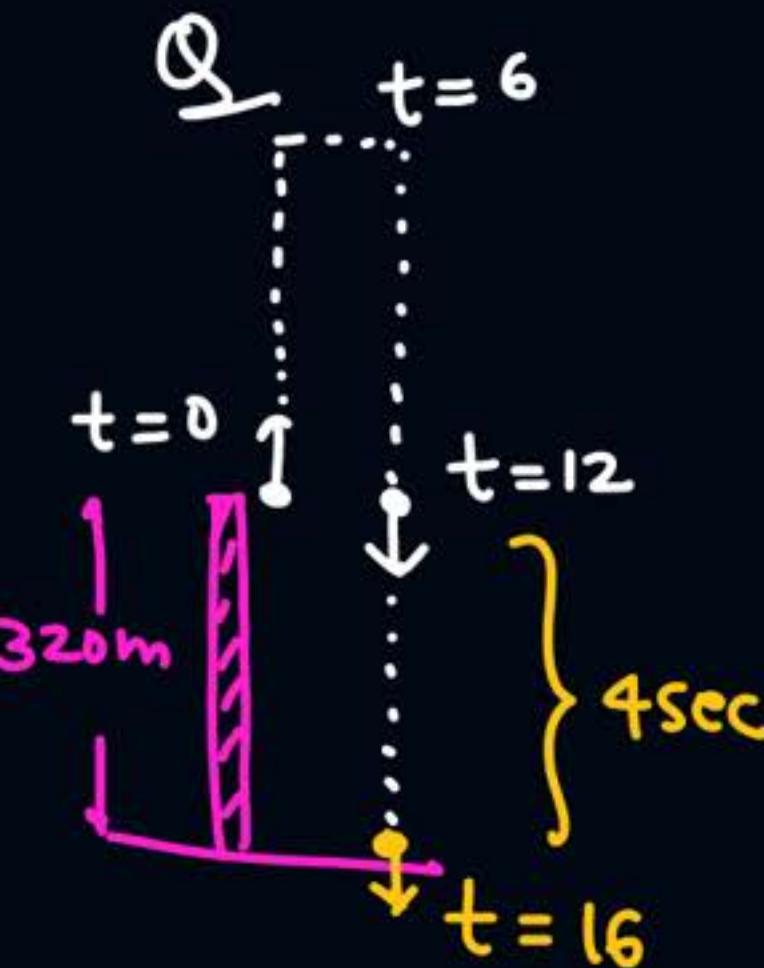
$$v^2 = 3600 + 6400$$

$$v^2 = 10000$$

$$v = 100 \text{ (तीव्रे)}$$

III
(Common Sense)

$t = 6 \text{ sec}$ $\rightarrow u_f = 0$



$$t = 16 \text{ sec}$$

when it will hit the ground.

उपर $\rightarrow +ve$

$$u = \text{उपर } 60 = +60$$

$$a = \text{नीचे } g = -10$$

$$S = \text{नीचे } 320 = -320$$

$$S = ut + \frac{1}{2}at^2$$

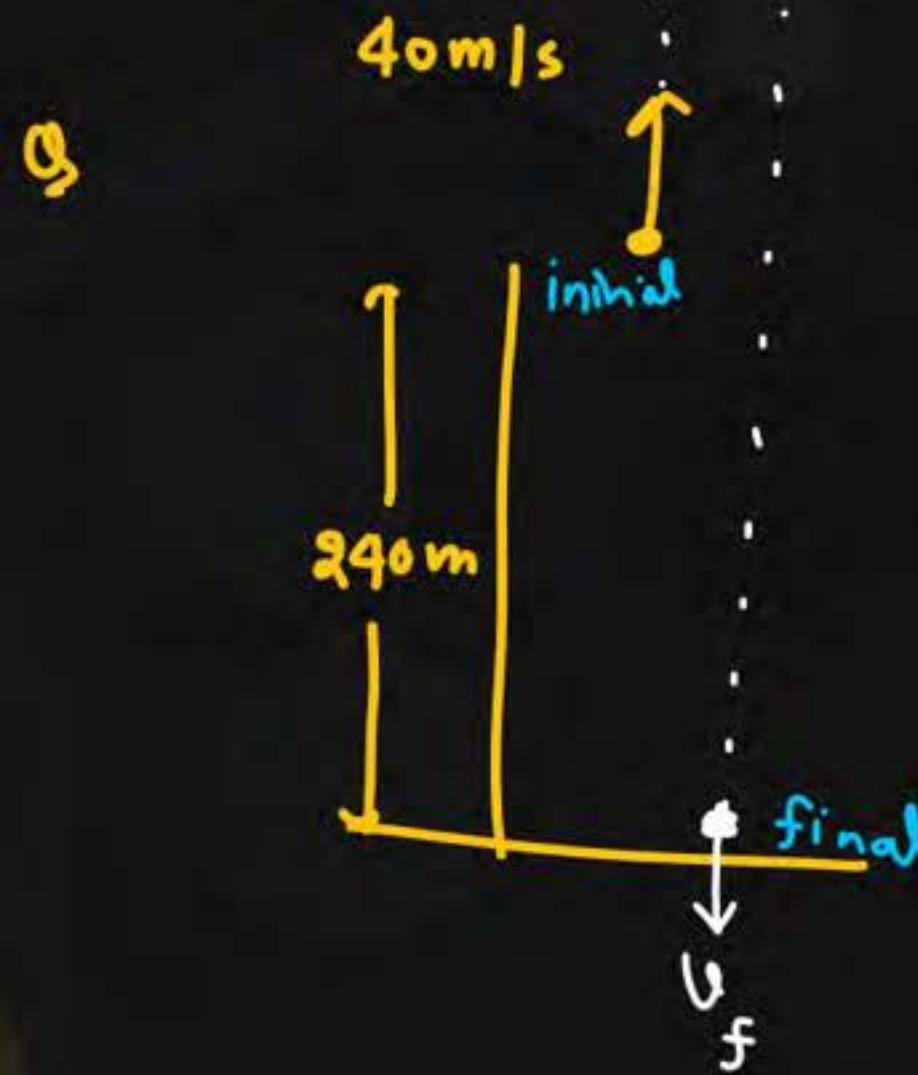
$$-320 = 60t - \frac{1}{2} \times 10 \times t^2$$

$$5t^2 - 60t - 320 = 0$$

$$t^2 - 12t - 64 = 0$$

$$(t-16)(t+4) = 0$$

on M practice



- ① find the time when particle will hit the ground
- ② " " velocity just before particle hit the ground

$$u = +40$$

$$a = -10$$

$$s = -240$$

$$s = ut + \frac{1}{2}at^2$$

$$-240 = 40t + \frac{1}{2}(-10)t^2$$

$$5t^2 - 40t - 240 = 0$$

$$t^2 - 8t - 48 = 0$$

$$(t-12)(t+4) = 0$$

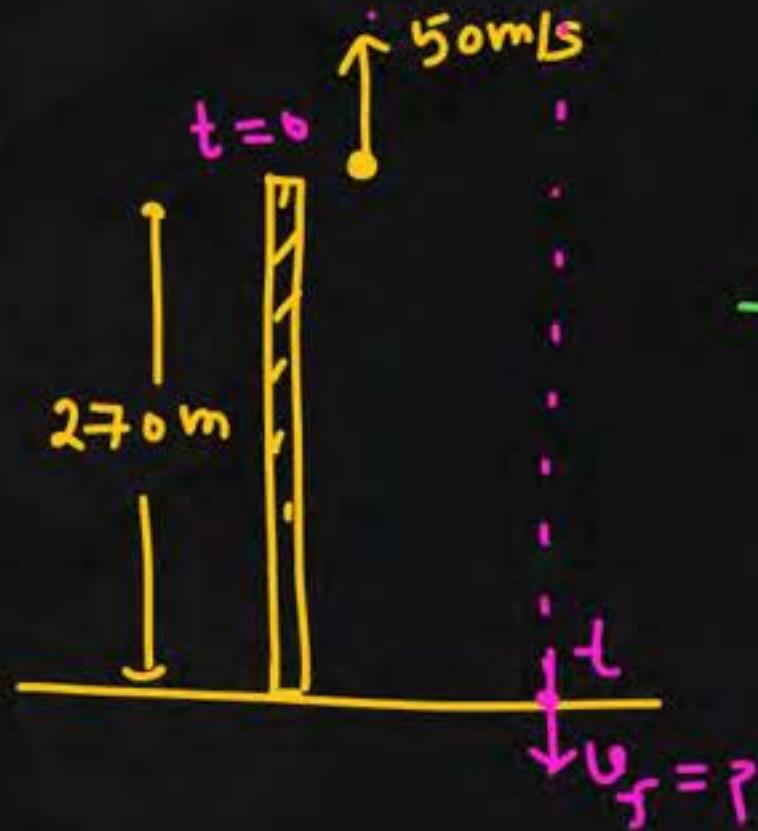
$$\boxed{t=12 \text{ Ans}}$$

$$v^2 = u^2 + 2as$$

$$= (40)^2 + 2 \times (-10)(-240)$$

$$\boxed{v = 80}$$

Q2

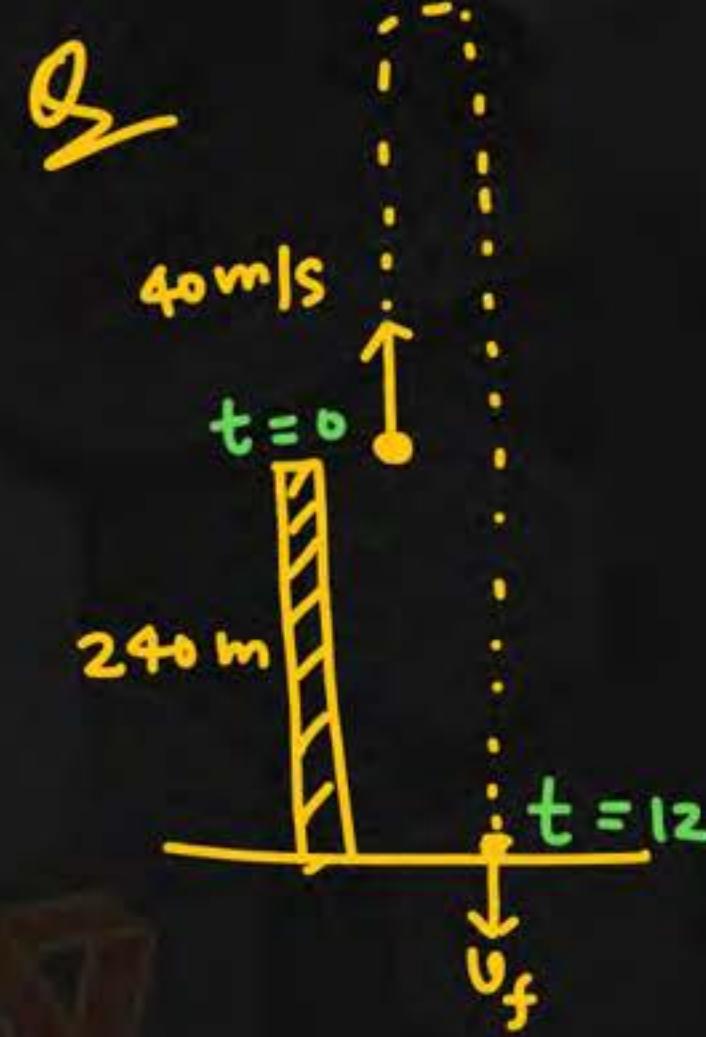


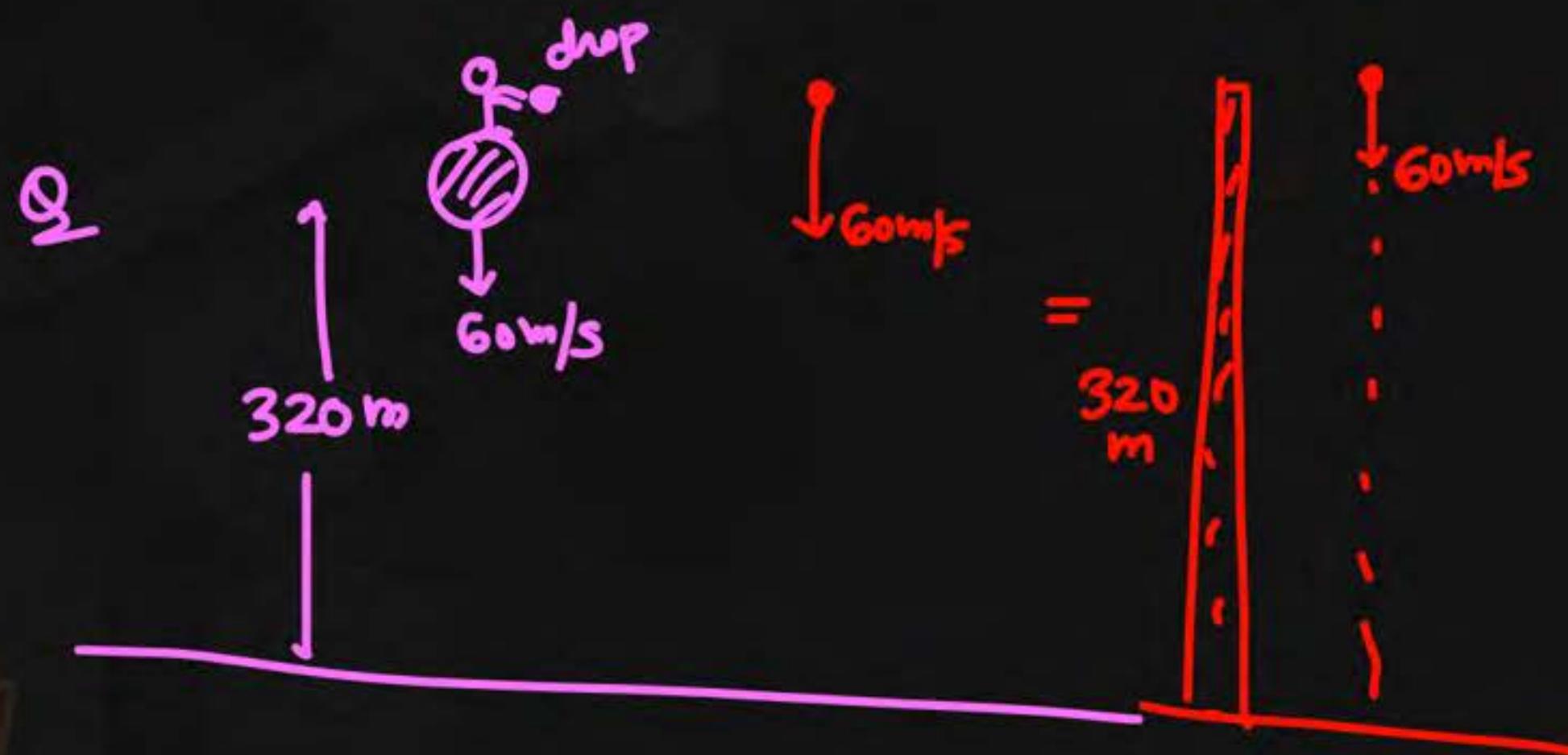
$$S = ut + \frac{1}{2}at^2$$

$$-270 = 50t - \frac{1}{2} \times 10 \times t^2$$

Solve quadratic ✓

$$v_f^2 = (50)^2 + 2(-10)(-270)$$





Q A particle is projected with velocity 100m/s at angle of 53° with the horizontal.

(a) Find initial velocity

$$\vec{u} = 60\hat{i} + 80\hat{j}$$

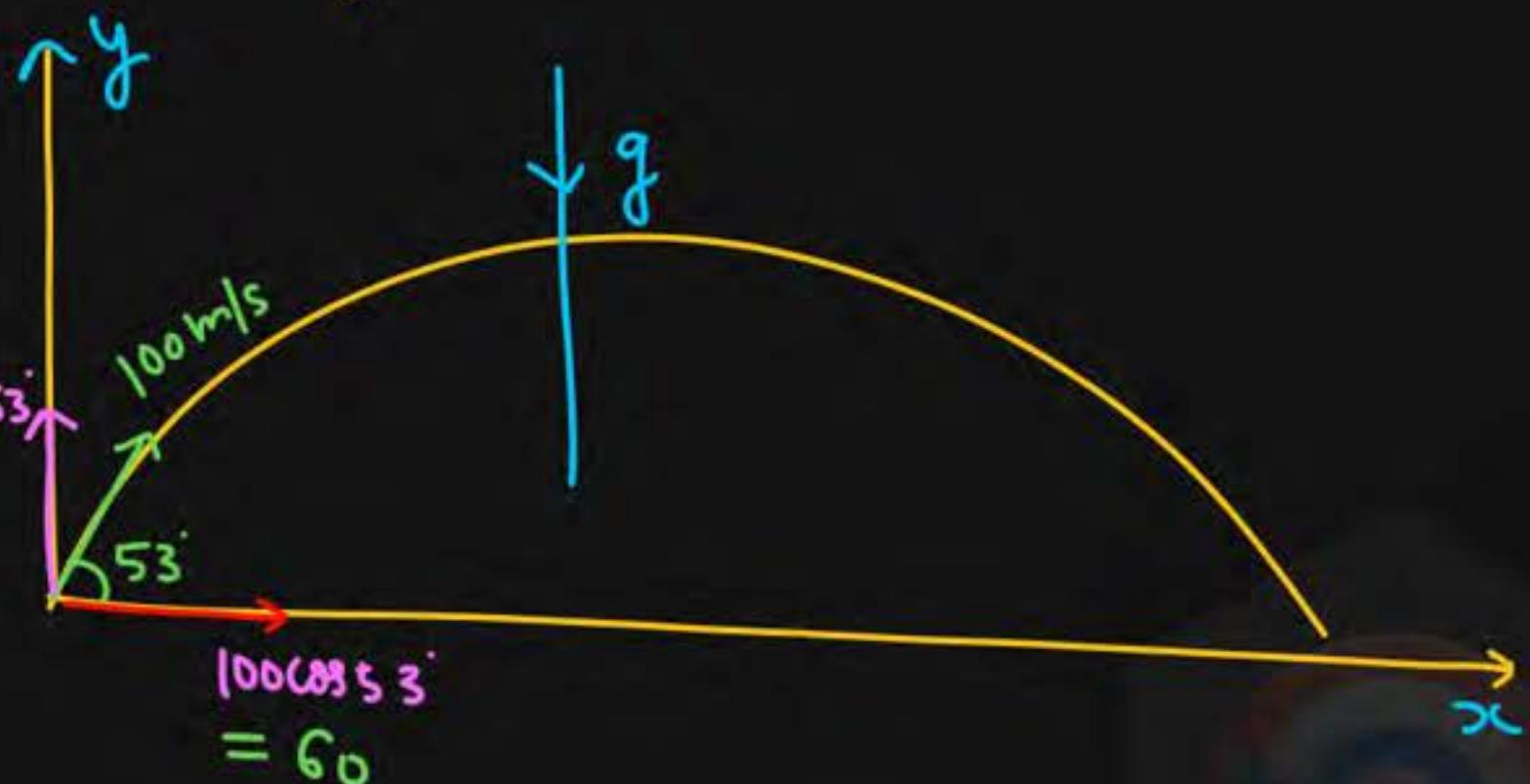
$$v_0 = 100 \sin 53^\circ$$

(b) $\vec{a} = g \text{ नीचे}$

$$\vec{a} = -g\hat{j} = -10\hat{j}$$

$$\vec{a} = 0\hat{i} - 10\hat{j}$$

$$\vec{a}_x = 0$$



(c) Find time of flight

$$T = 8 + 8 = 16 \text{ sec}$$

(d) Range = $60 \times 16 = 960$

(e) find velocity at

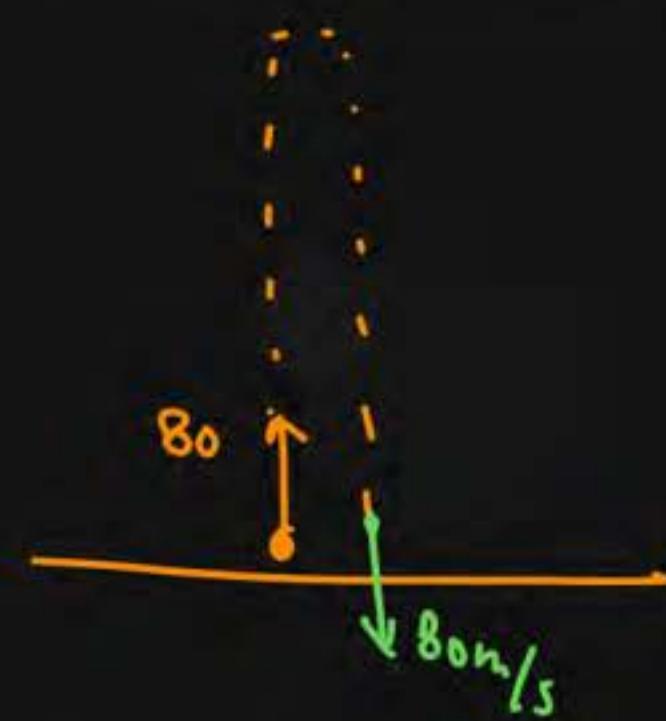
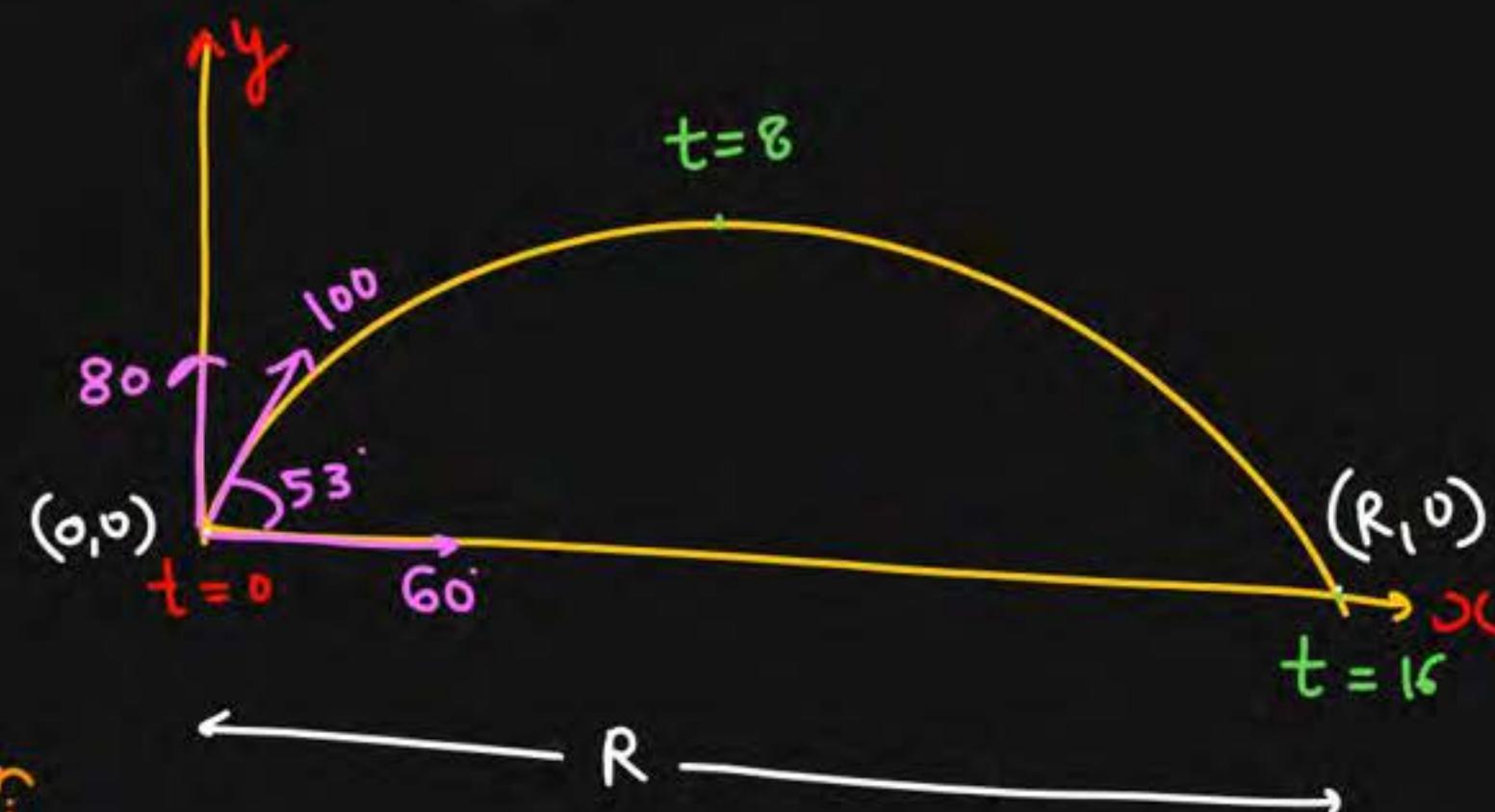
$$t = 2 \quad \vec{v} = 60\hat{i} + 60\hat{j}$$

$$t = 8 \quad \vec{v} = 60\hat{i} + 0\hat{j}$$

$$t = 10 \quad \vec{v} = 60\hat{i} - 20\hat{j}$$

$$\textcircled{X} \quad t = 16 \quad \vec{v} = 60\hat{i} - 80\hat{j}$$

just before it hit the ground



$$\vec{P} = \text{momentum} = m \vec{v}$$

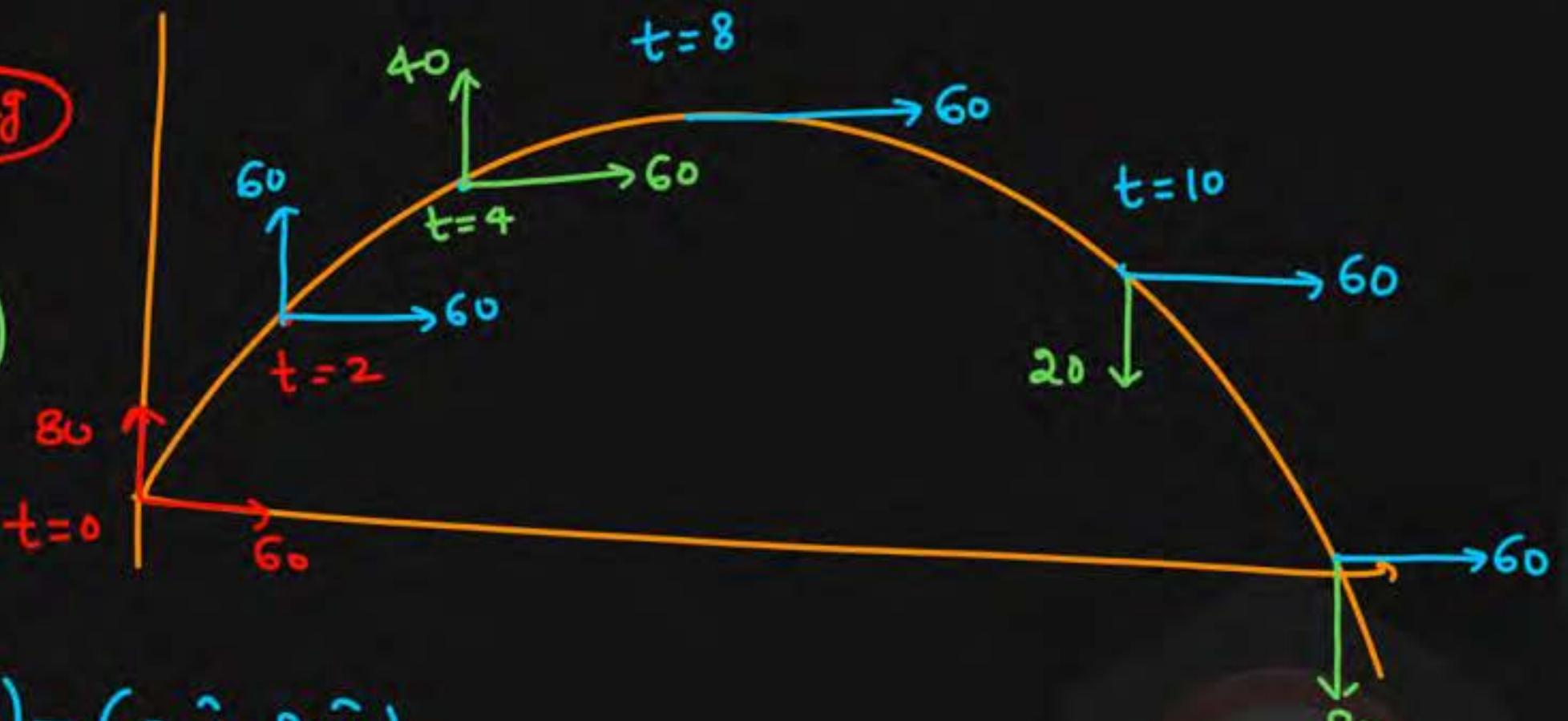
f) find change in momentum
for entire motion $m = 1 \text{ kg}$

$$\Delta \vec{P} = \vec{P}_f - \vec{P}_i$$

$$\begin{aligned}\vec{P}_i &= m \vec{v}_i = 1(60\hat{i} + 80\hat{j}) \\ &= 60\hat{i} + 80\hat{j}\end{aligned}$$

$$\vec{P}_f = 60\hat{i} - 80\hat{j}$$

$$\begin{aligned}\Delta \vec{P} &= \vec{P}_f - \vec{P}_i = (60\hat{i} - 80\hat{j}) - (60\hat{i} + 80\hat{j}) \\ &= -160\hat{j}\end{aligned}$$

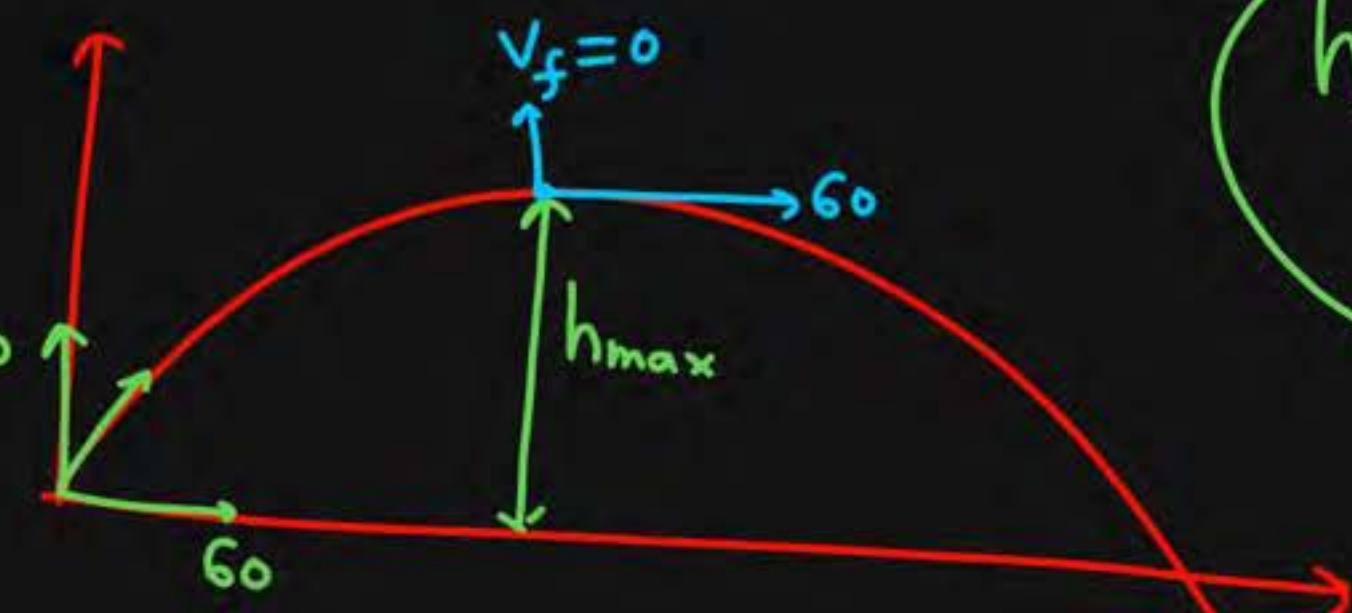


(g) find h_{\max}

$$(y) v^2 = u^2 + 2as$$

$$0^2 = (80)^2 + 2(-10)(h_{\max})$$

$$h_{\max} = 320$$



h_{\max} का तरीका
3rd eqn of motion
y में

(h) find \vec{v} at any time t

$$\vec{v} = 60\hat{i} + (80 - 10t)\hat{j}$$

(i) find when \vec{v} become perpendicular to \vec{a}

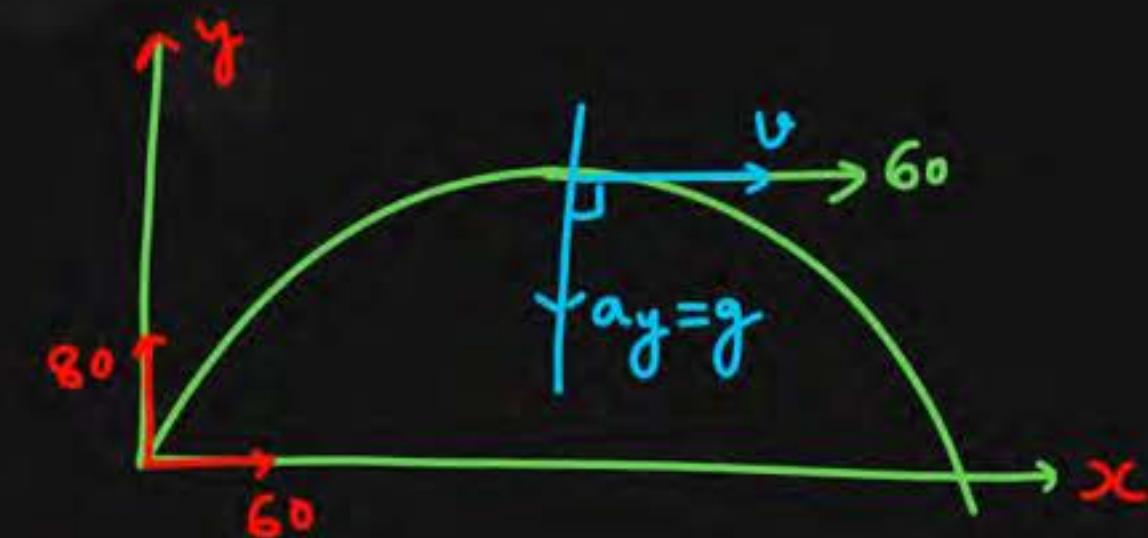
$$\vec{v} \cdot \vec{a} = 0$$

$$\vec{v} = 60\hat{i} + (80 - 10t)\hat{j}$$

$$\vec{a} = -10\hat{j}$$

$$\vec{v} \cdot \vec{a} = -10(80 - 10t) = 0$$

$$t = 8 \text{ sec}$$



(j) $v = u + at$
 $\vec{v}_y = 80 - 10t$

(j) find the time when velocity of particle become perpendicular to initial velocity.

$$\vec{u} = 60\hat{i} + 80\hat{j}$$

$$\vec{v}_f = 60\hat{i} + (80 - 10t)\hat{j}$$

$$\underline{\vec{v} \cdot \vec{u} = 0}$$

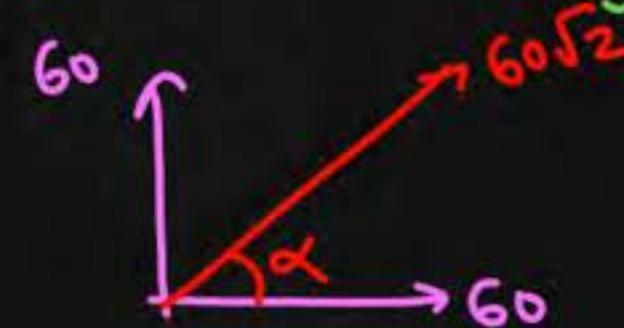
$$60 \times 60 + 80(80 - 10t) = 0$$

$$3600 + 6400 - 800t = 0$$

$$t = \frac{10000}{800} = \frac{100}{8} = 12.5$$

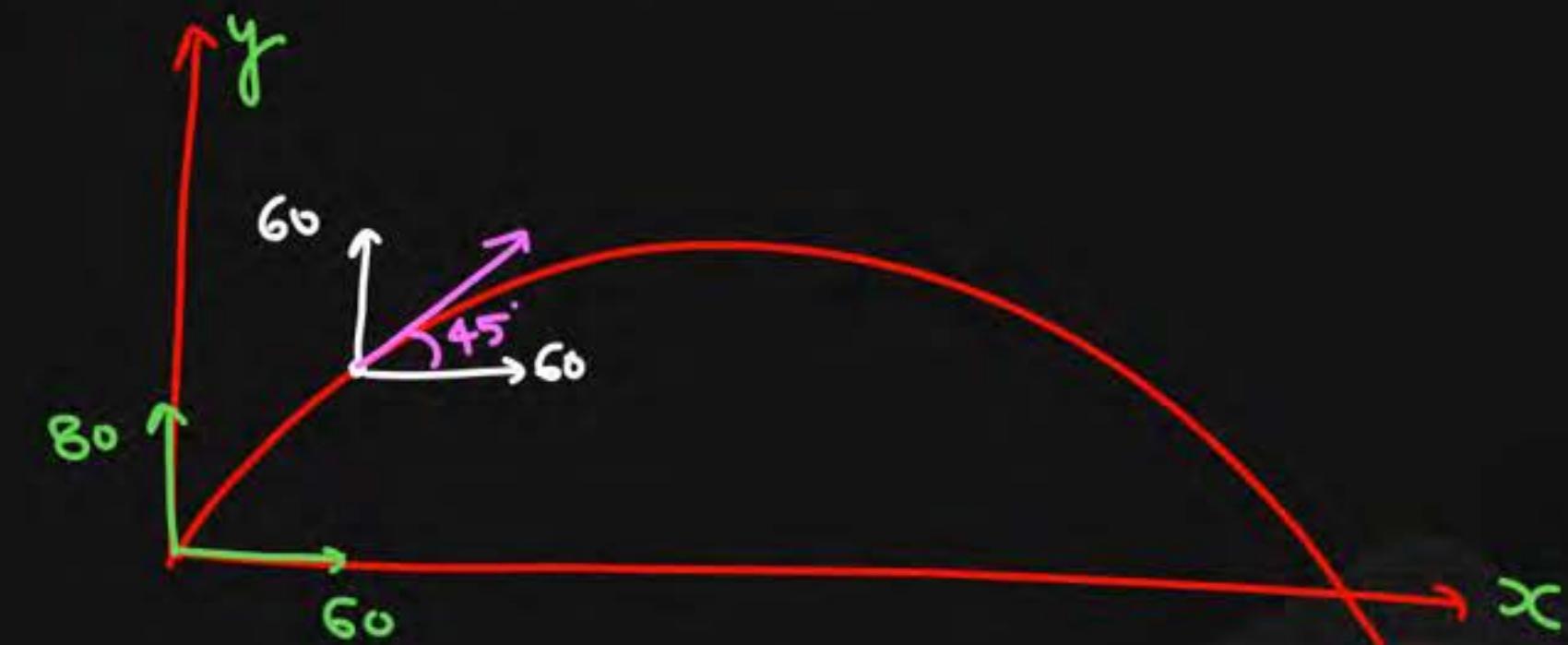
*^k find the angle made by velocity with horizontal at $t=2\text{ sec}$

$$t=2, \vec{v} = 60\hat{i} + 60\hat{j}$$



$$\tan \alpha = \frac{60}{60} = 1$$

$$\alpha = 45^\circ$$



Direction Cosine $\cos \alpha = \frac{Ax}{A} = \frac{60}{60\sqrt{2}} = \frac{1}{\sqrt{2}}$

$$\alpha = 45^\circ$$

(Q) find location of particle at $t=2$, $t=8$ sec

$$x = 60 \times 2 = 120$$

$$y = 80 \times 2 - \frac{1}{2} \times 10 \times 2^2 \\ = 160 - 20 = 140$$

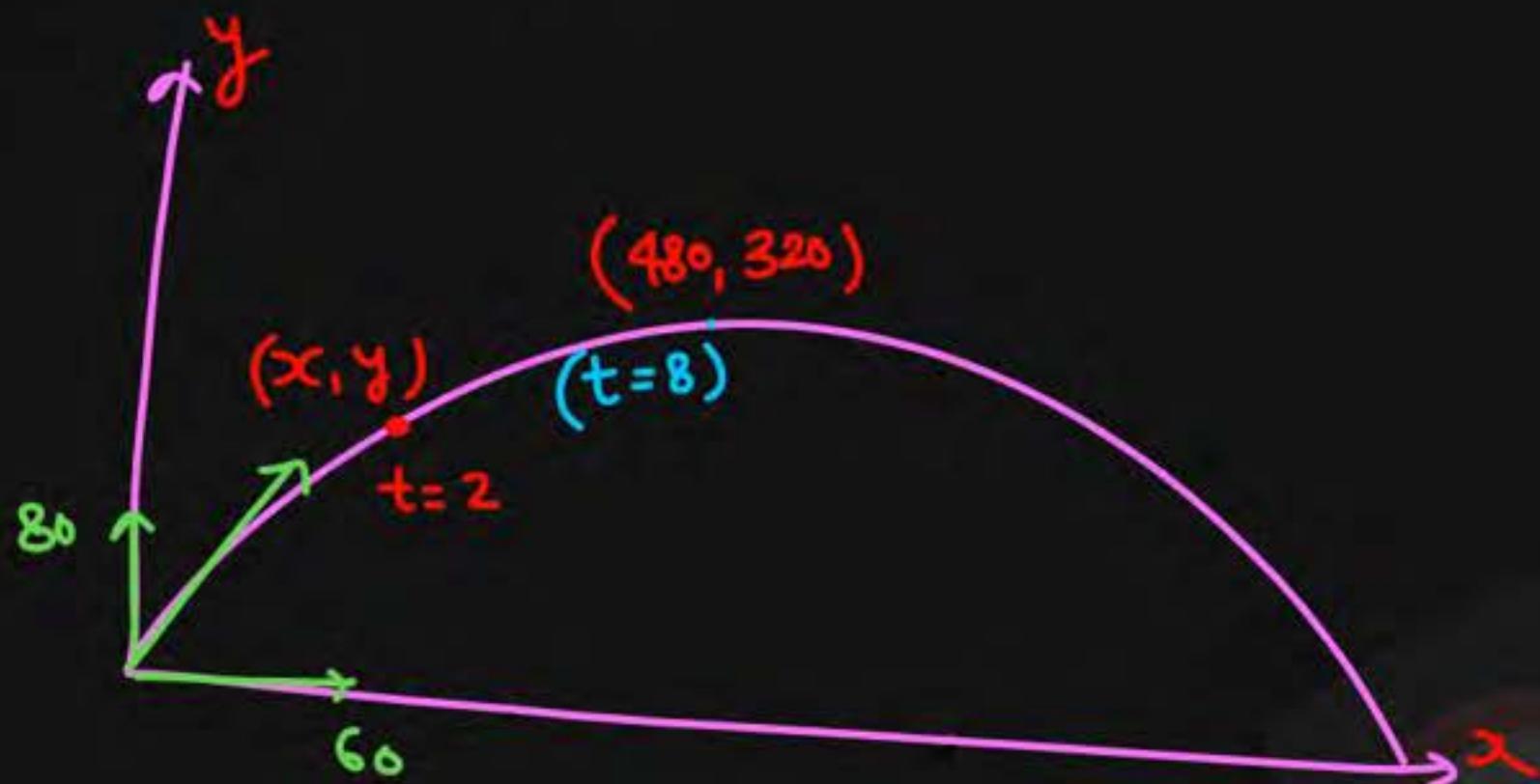
$$(x, y) \Rightarrow (120, 140)$$

$$t = 8, \quad x = 60 \times 8 = 480$$

$$y = 80 \times 8 - \frac{1}{2} \times 10 \times 8^2$$

$$= 640 - 320 = 320$$

$$(480, 320)$$



(m) If air start flowing such that it given horizontal acc of $+5 \text{ m/s}^2$ to the particle (No air resistance) find

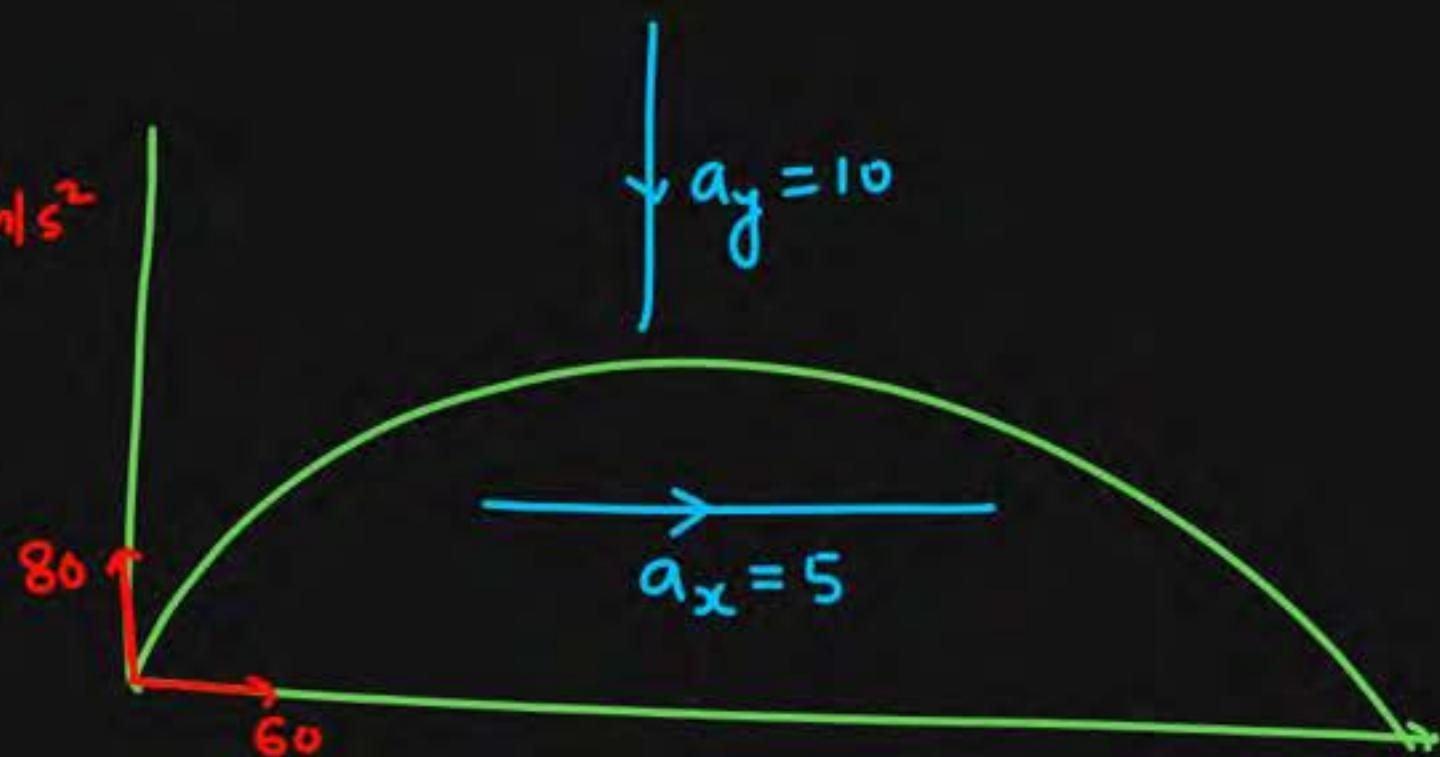
$$\textcircled{1} \quad T = 8 + 8 = 16 \text{ (Same)}$$

T, H_{\max} \longrightarrow Same.

$$\text{Range} = R = ut + \frac{1}{2}at^2 \quad (\text{x dir } \vec{i})$$

$$R = 60 \times 16 + \frac{1}{2} \times 5 \times (16)^2$$

$$\begin{aligned} t &= 2, \vec{v} = (60 + 5 \times 2)\hat{i} + (80 - 10 \times 2)\hat{j} \\ &= 70\hat{i} + 60\hat{j} \end{aligned}$$



Q

$$\vec{u}_i = 40\hat{i} + 60\hat{j}$$

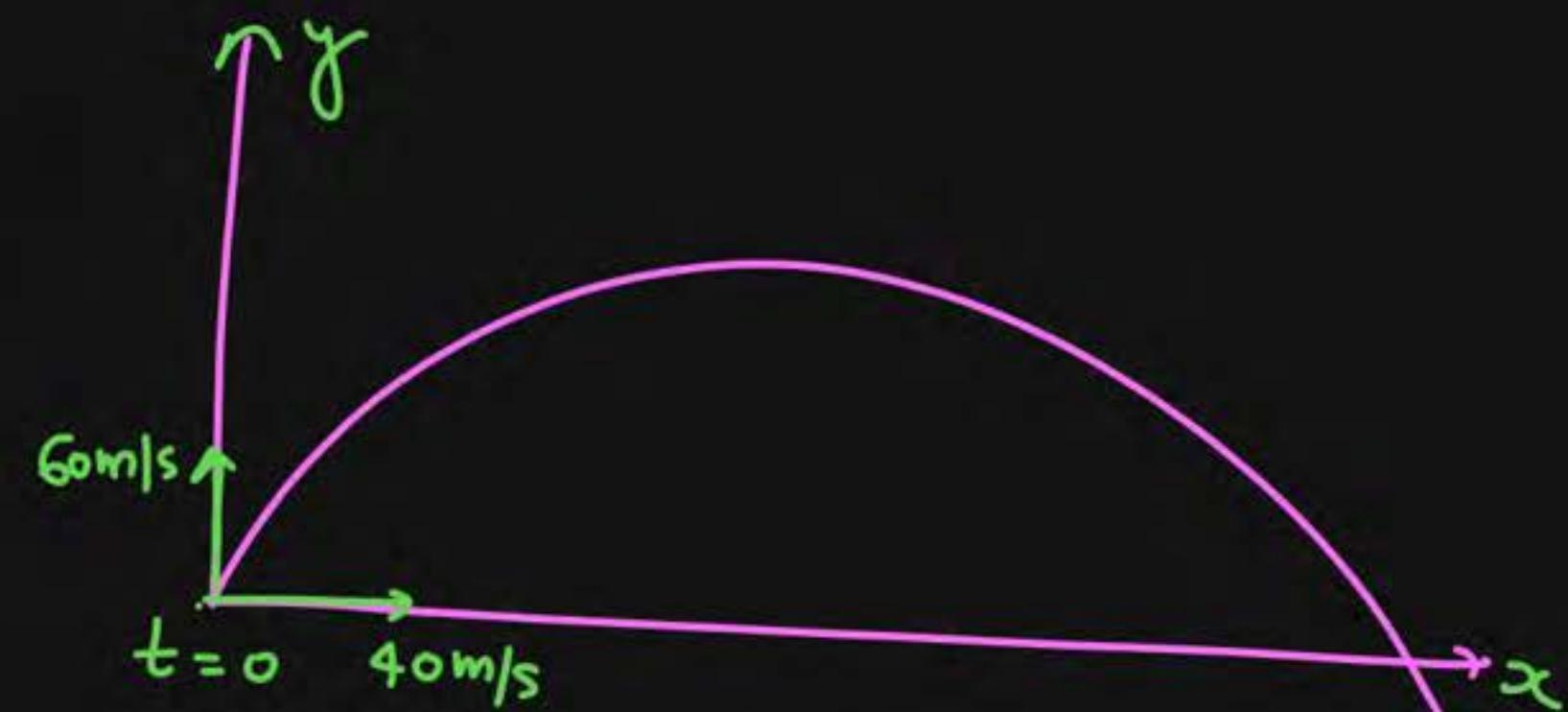
find

$$\textcircled{1} \quad T = 6 + 6 = 12$$

$$\textcircled{2} \quad R = 40 \times 12 = 480$$

$$\textcircled{3} \quad h_{max} = 180$$

$$\textcircled{4} \quad t=2, \vec{v} = 40\hat{i} + 40\hat{j}$$



$$\textcircled{3} \quad 0^2 = C_0^2 + 2 \times (-10) h_{max}$$

$$h_{max} = \frac{3600}{20}$$

Q2 find equation of trajectory

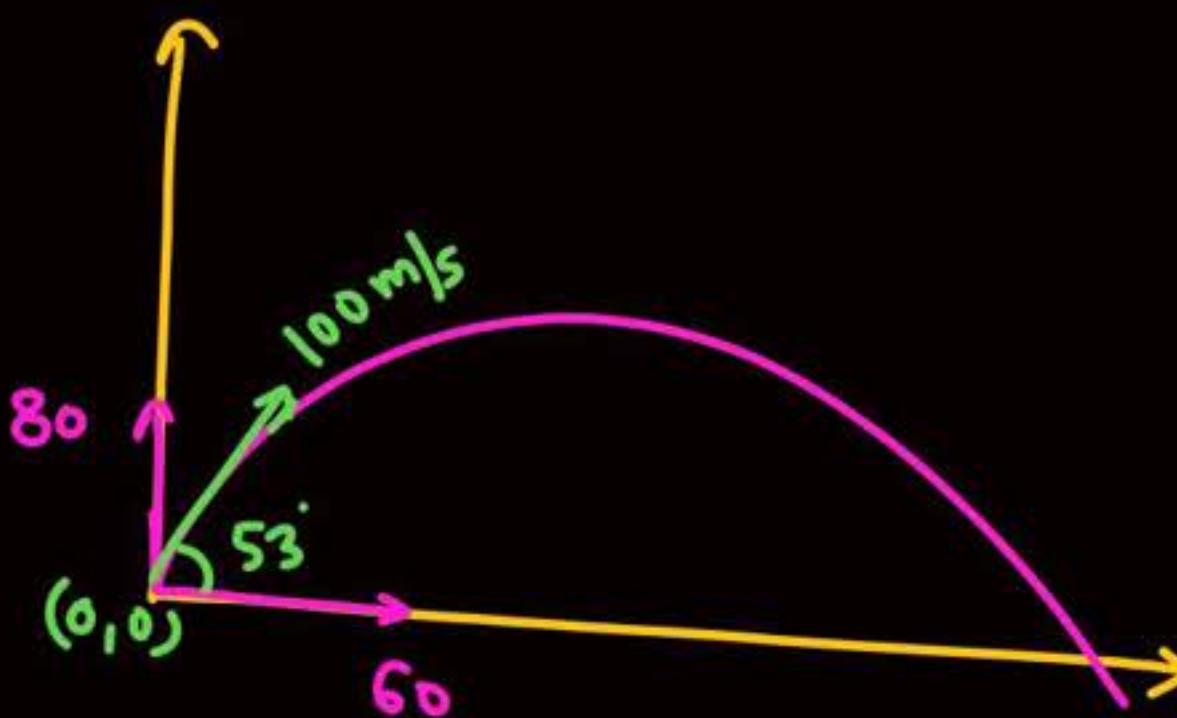
$$x = 60t \Rightarrow t = \frac{x}{60}$$

$$y = 80t - \frac{1}{2} \times 10 \times t^2$$

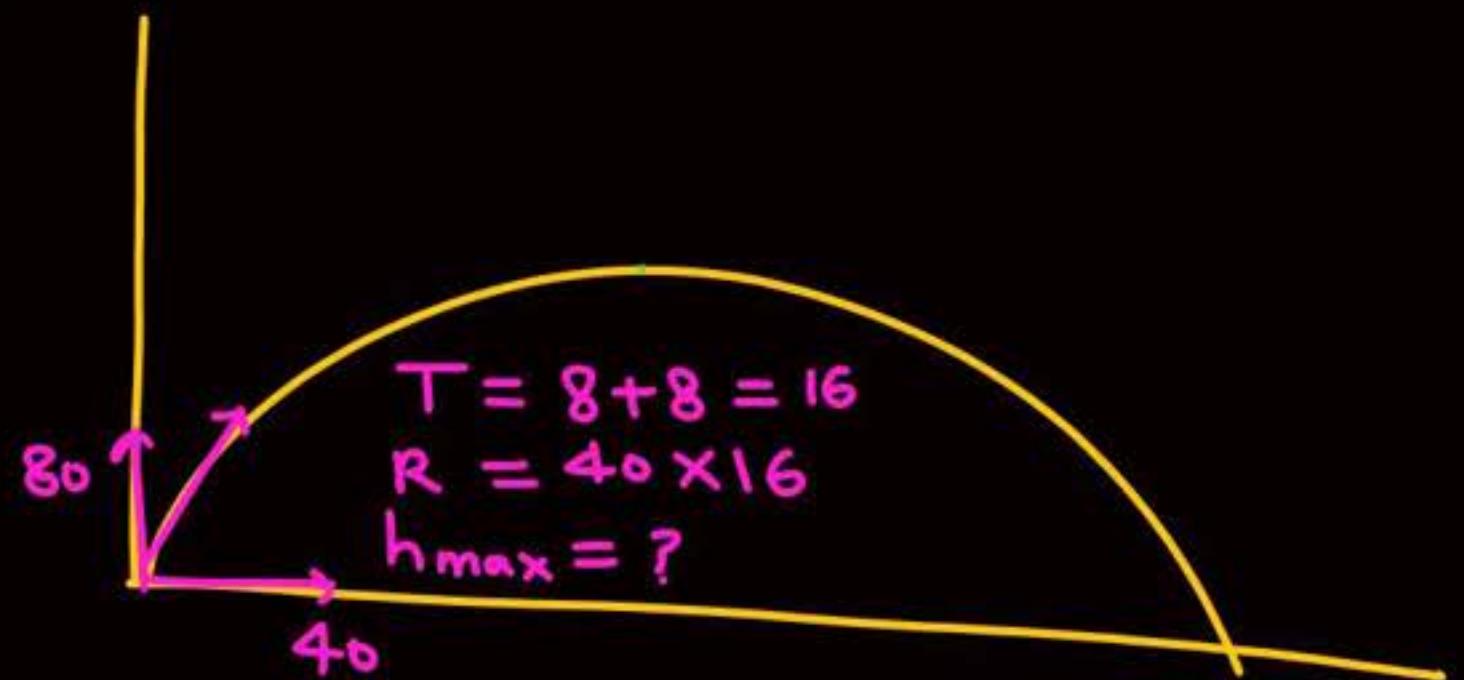
$$y = 80 \frac{x}{60} - \frac{1}{2} \times 10 \times \left(\frac{x}{60}\right)^2$$

$$\boxed{y = \frac{4x}{3} - \frac{x^2}{720}}$$

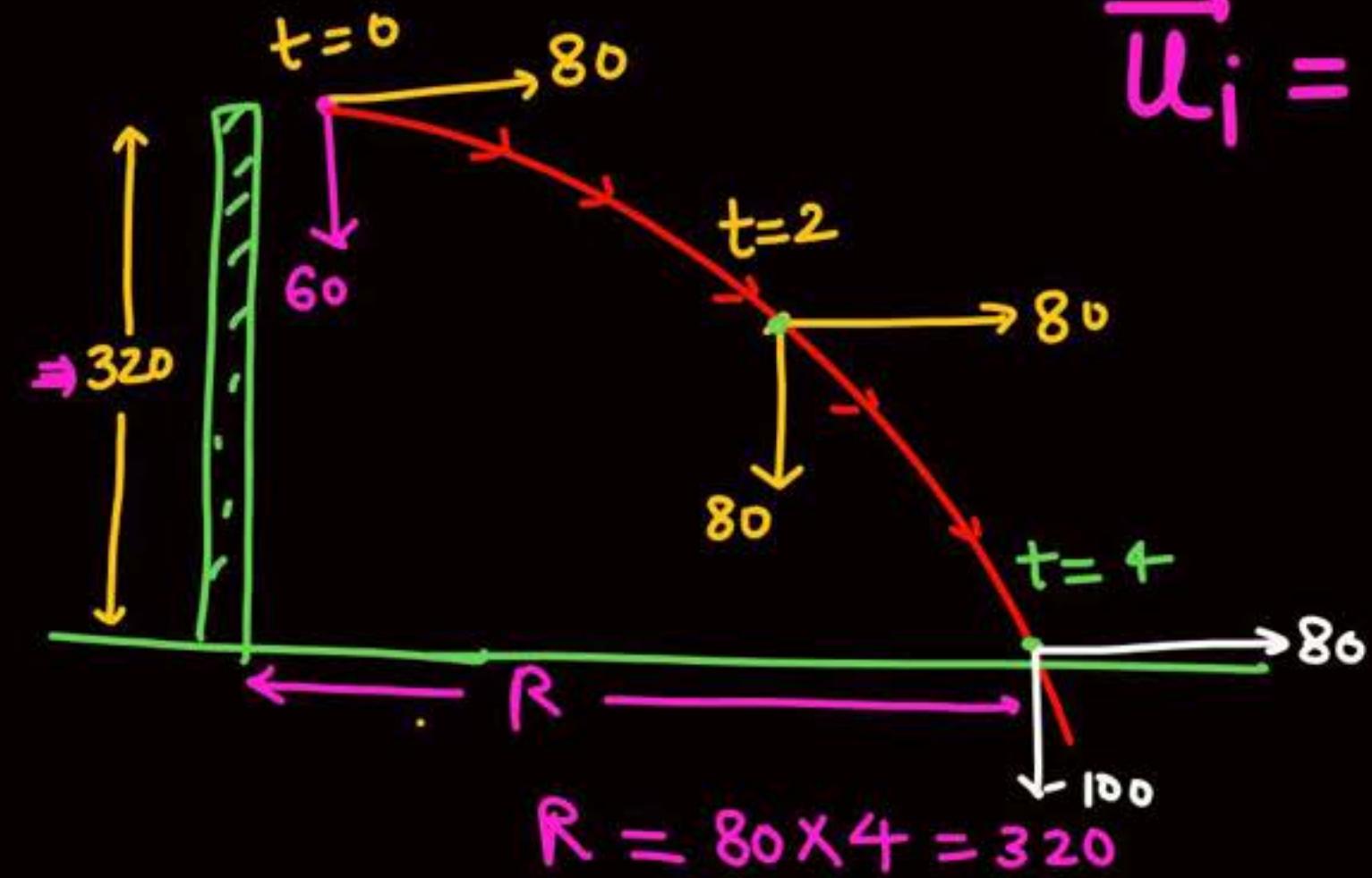
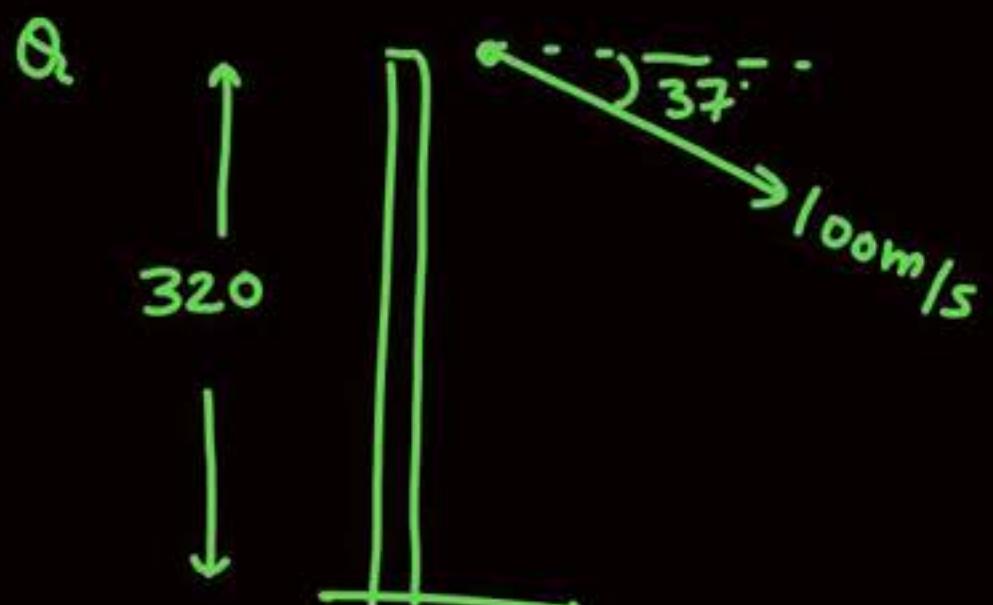
parabola



Q



$$0^2 = 80^2 - 2 \times 10 \times h_{\max}$$



$$\vec{U}_i = 80\hat{i} - 60\hat{j}$$

① When & where particle will strike the ground.

$$y = \downarrow +ve \quad s = ut + \frac{1}{2}at^2$$

$$+320 = +60t + \frac{1}{2} \times 10 \times t^2$$

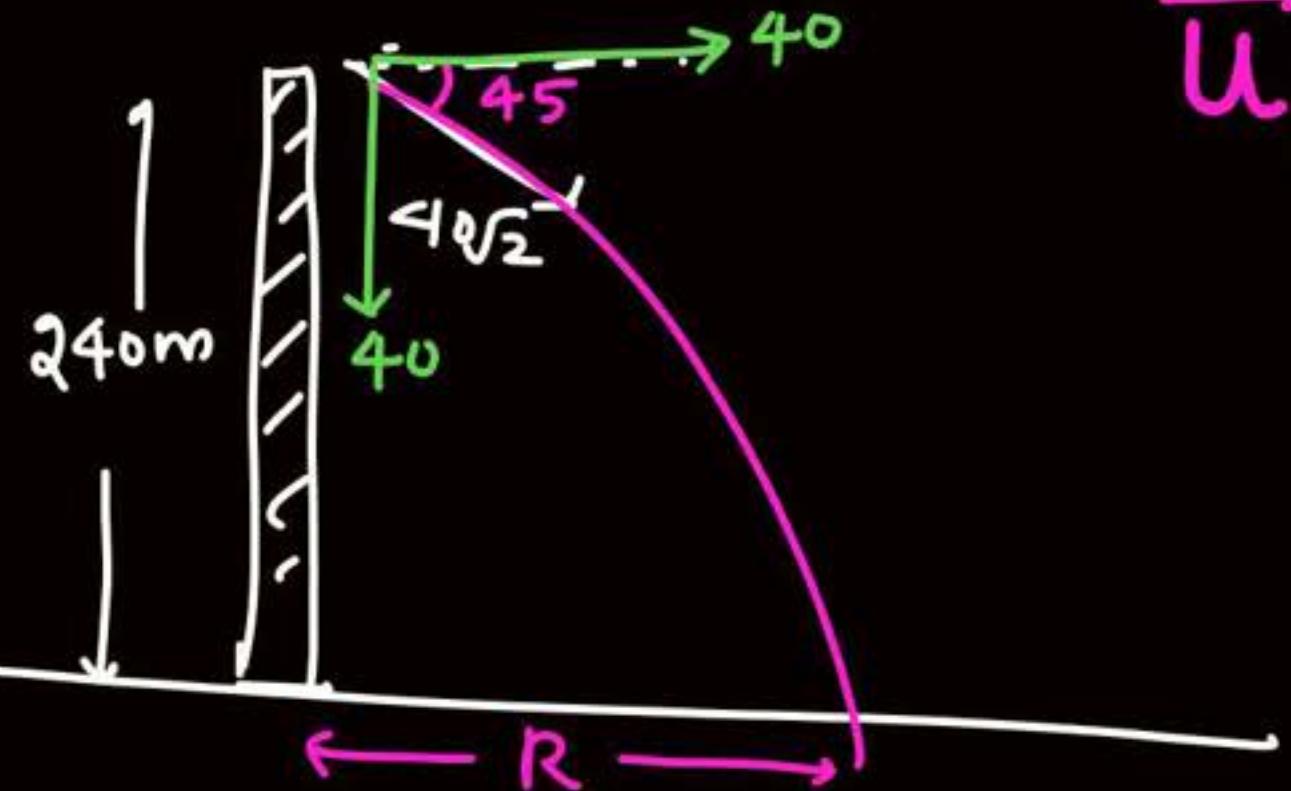
$$\boxed{t = 4 \text{ sec}}$$

Q2

When particle will strike the ground & where

(y)

$$S = ut + \frac{1}{2}at^2$$

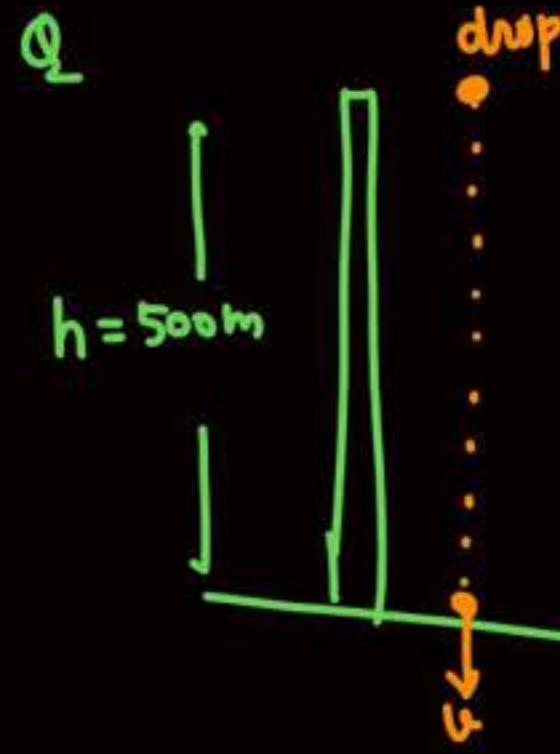


$$240 = 40t + \frac{1}{2} \times 10 \times t^2$$

$$t = 4$$

$$R = 40 \times 4 = 160$$

$$\vec{u}_i = 40\hat{i} - 40\hat{j}$$



$$h = 0 + \frac{1}{2}gt^2$$

$$500 = \frac{1}{2} \times 10 \times t^2$$

$$t^2 = 100$$

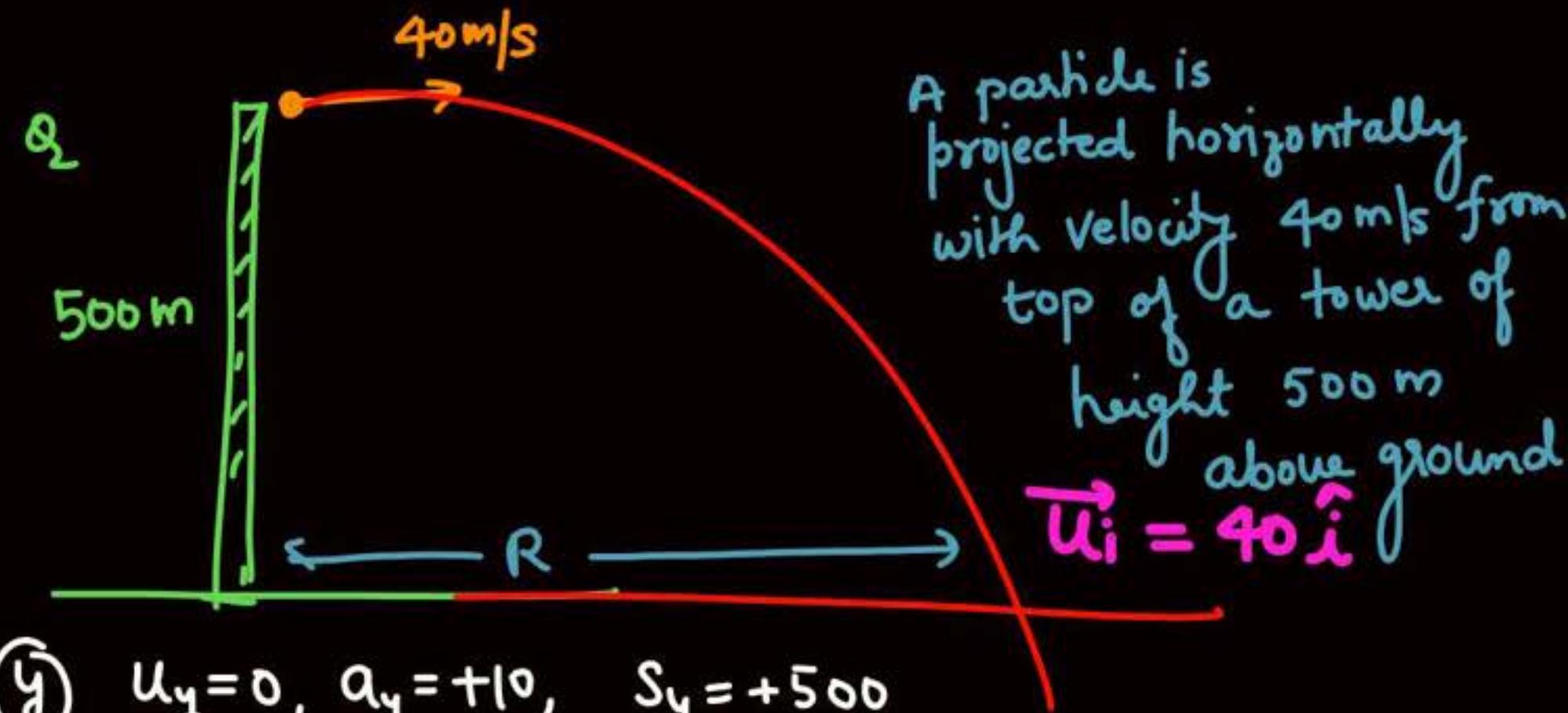
$$\boxed{t = 10 \text{ sec}}$$

$$v^2 = 0^2 + 2gh$$

$$v = \sqrt{2gh}$$

$$= \sqrt{2 \times 10 \times 500}$$

$$= 100$$

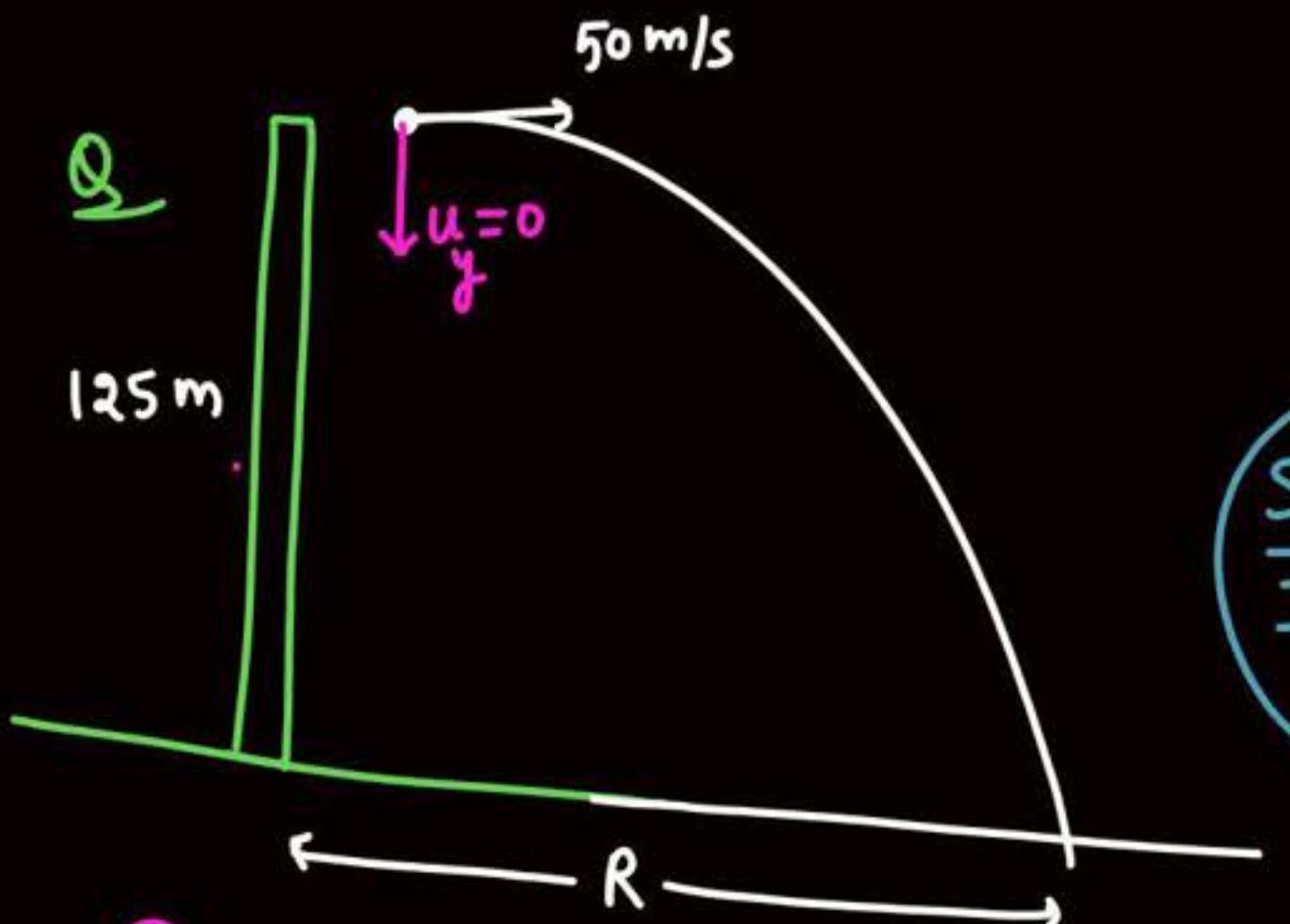


④ $U_y = 0, a_y = +10, S_y = +500$

$$500 = 0 + \frac{1}{2} \times 10 \times t^2$$

$$\boxed{t = 10 \text{ sec}}$$

$$R = 40 \times 10 = 400 \text{ m}$$



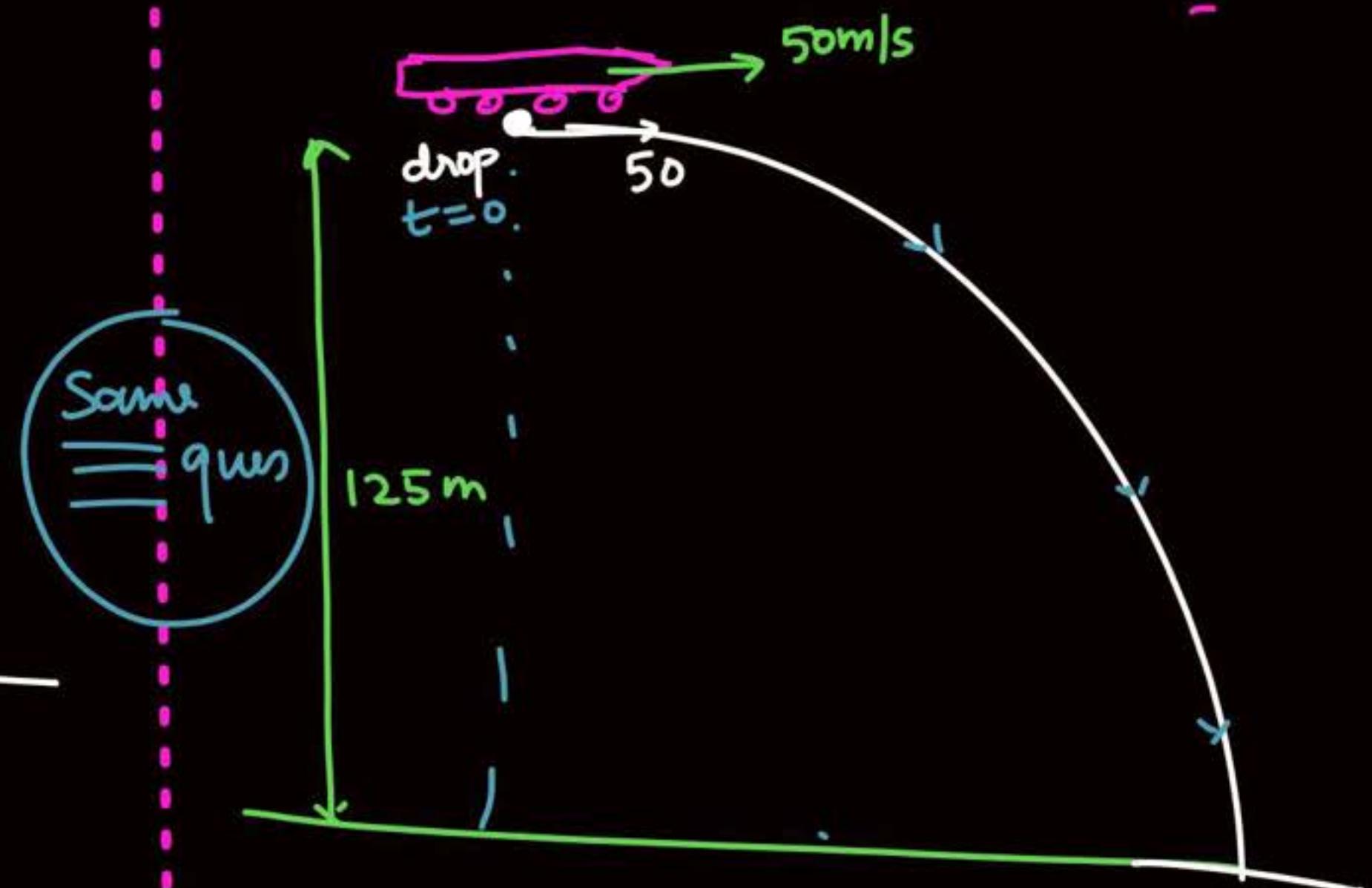
(y)

$$125 = 0 + \frac{1}{2} \times 10 \times t^2$$

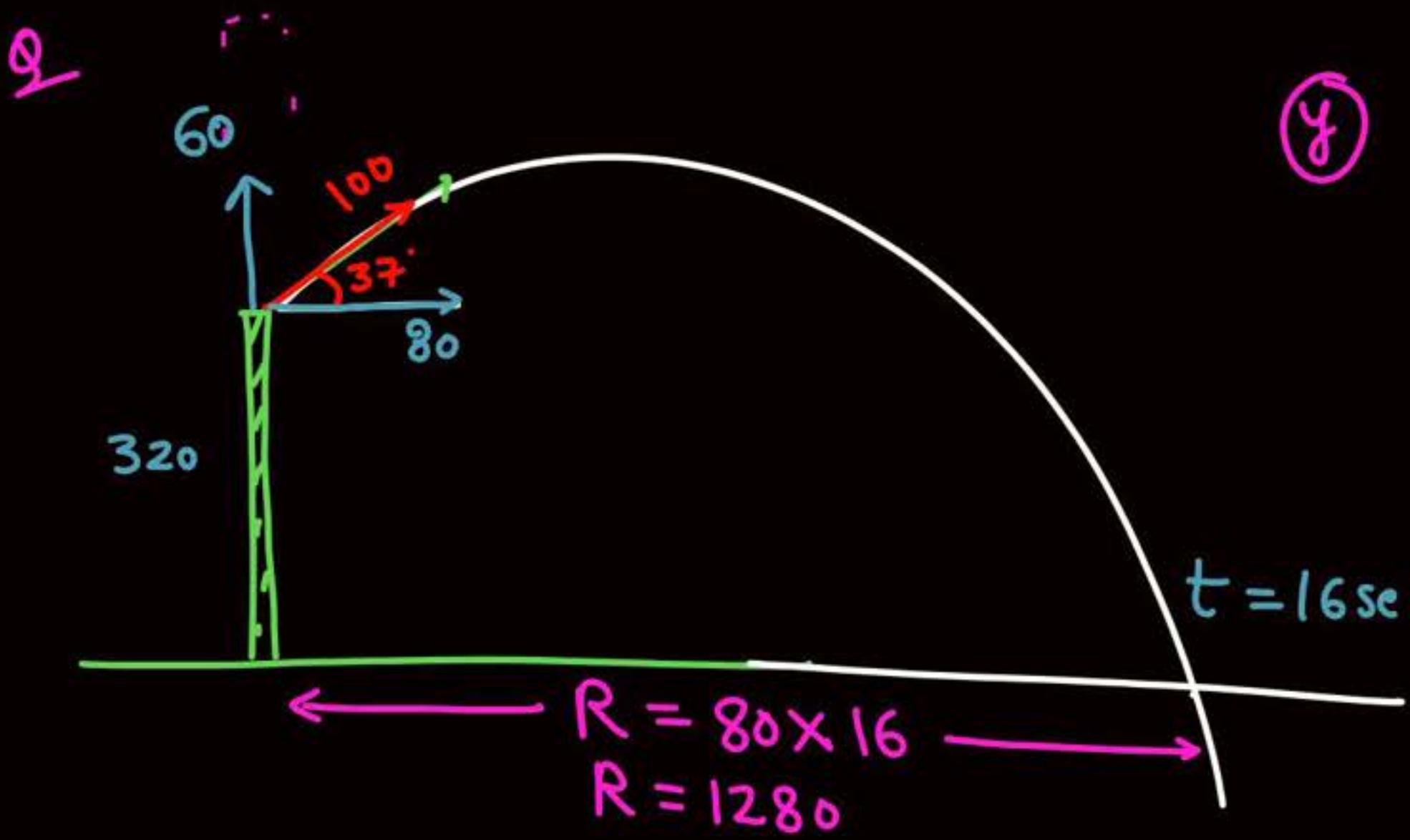
$$t = \sqrt{\frac{250}{10}} = 5$$

(x)

$$R = 50 \times 5 = 250 \text{ m}$$



$$t = 5 \\ R = 250 \text{ m}$$



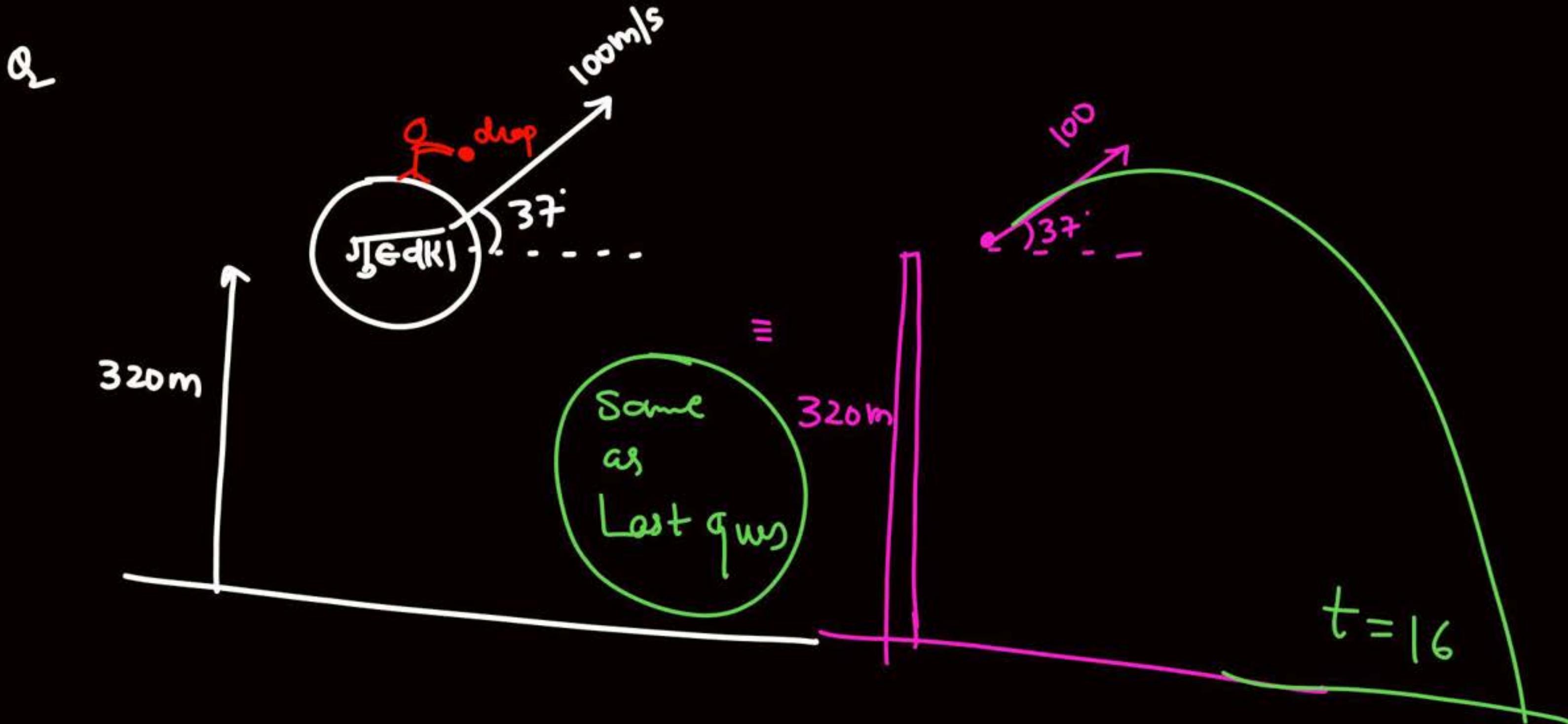
④ ↑ +ve
 $U_y = +60$
 $a_y = -10$
 $S_y = -320$

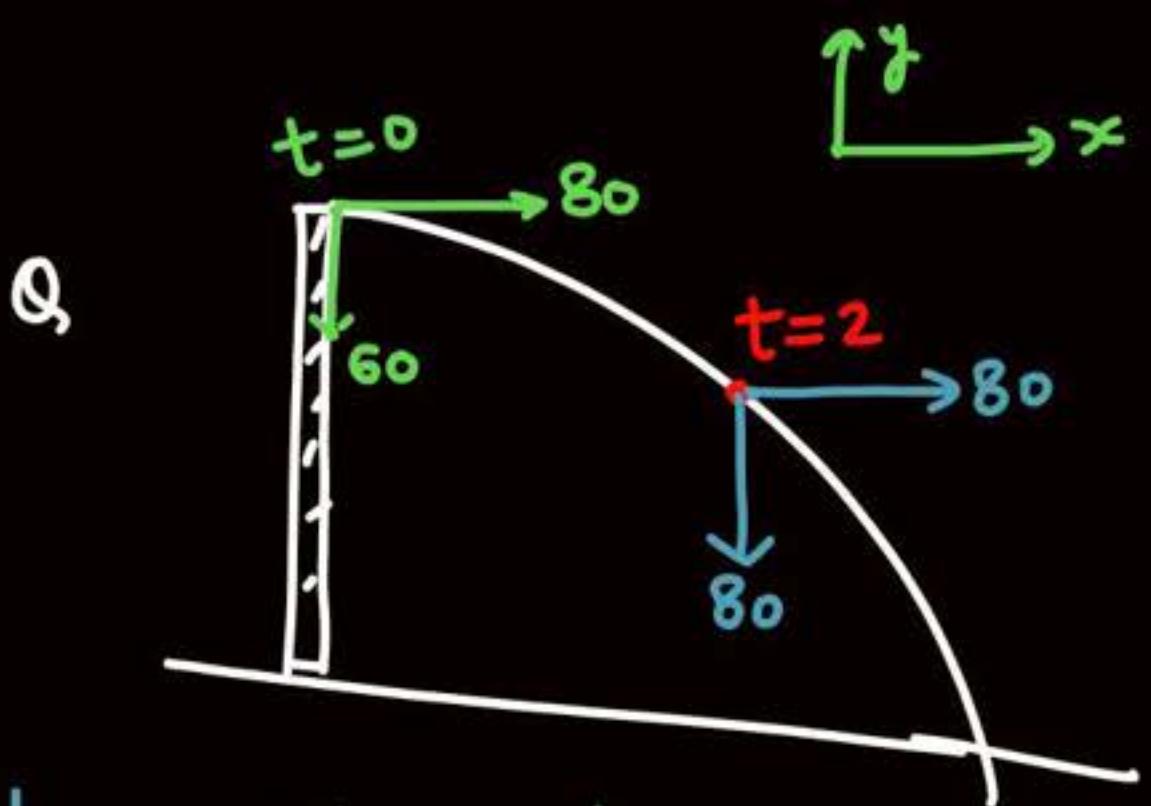
Alreadys ✓

$$-320 = 60t - \frac{1}{2} \times 10 \times t^2$$

$t = 16 \text{ sec}$

w find T & R





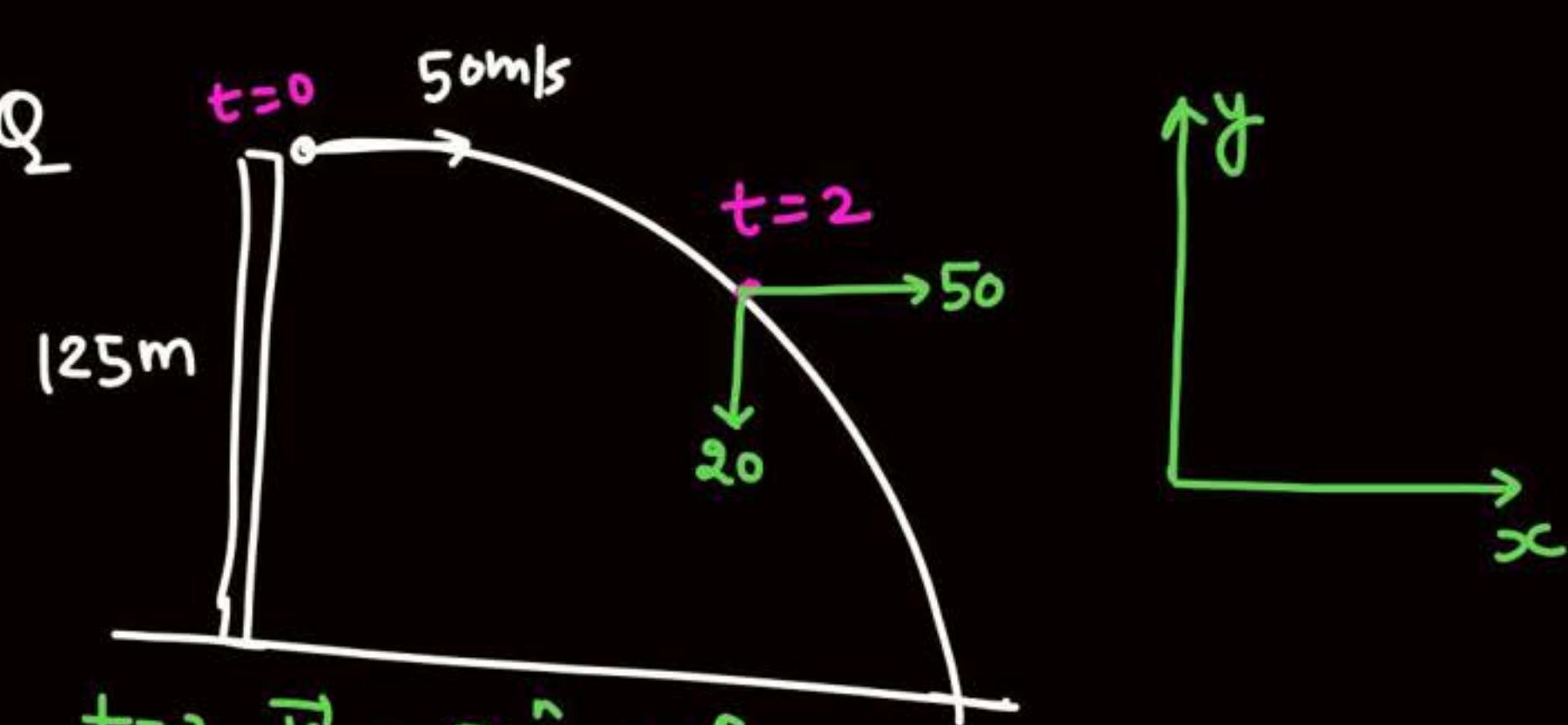
$$t=2, \vec{v} = 80\hat{i} - 80\hat{j}$$

$$t=4, \vec{v} = 80\hat{i} - 100\hat{j}$$

$$\rightarrow v_y = u_y + a_y t$$

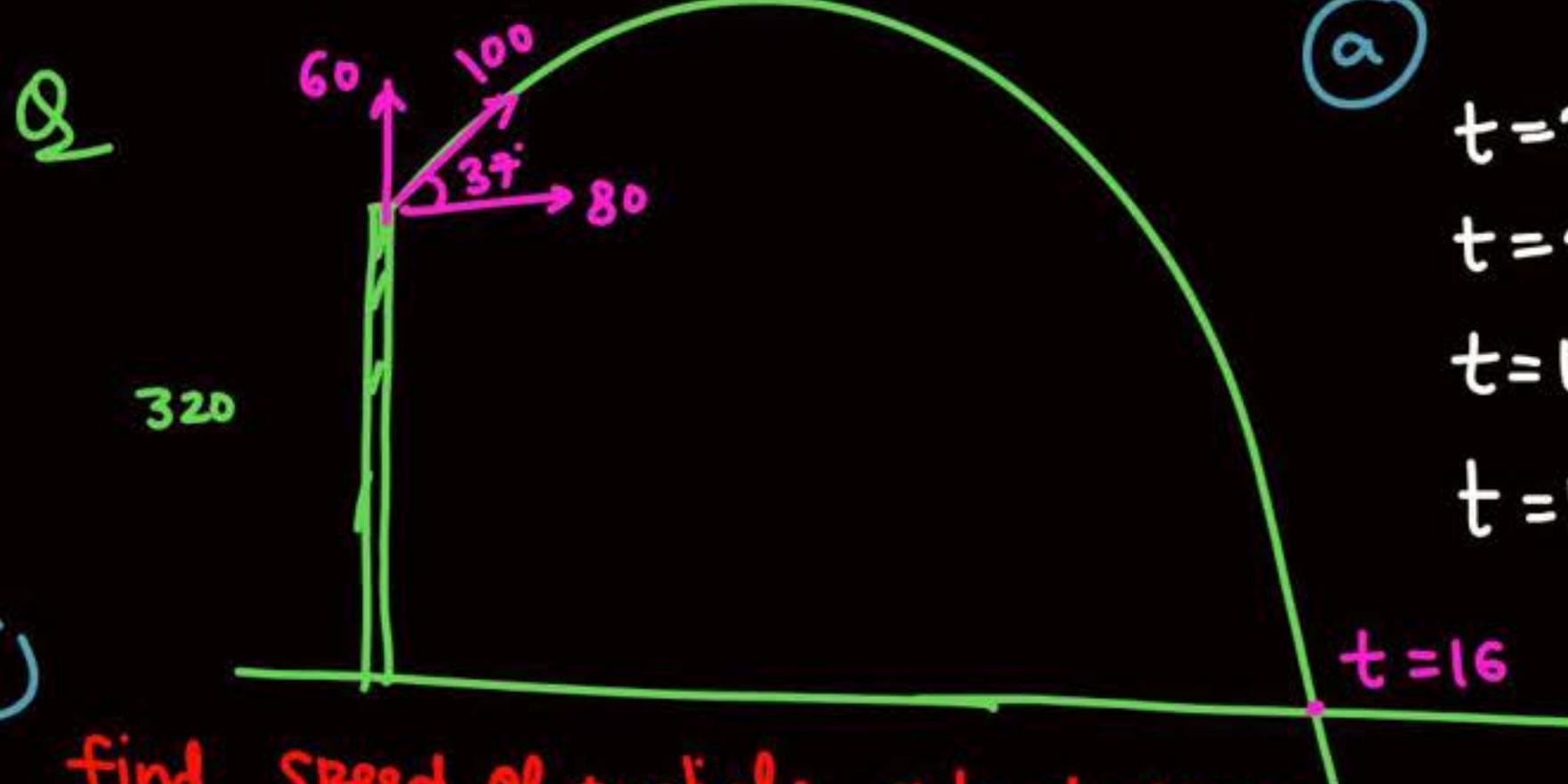
$$= +60 + 10 \times 4$$

$$= 100 \text{ m/s}$$



$$t=2, \vec{v} = 50\hat{i} - 20\hat{j}$$

$$\textcircled{y} \quad \begin{aligned} v &= u + at \\ v &= 0 - 10 \times 2 \\ v &= -20 \end{aligned}$$



(b) find speed of particle at $t=16 \text{ sec}$

$$\vec{V} = 80\hat{i} - 100\hat{j} \quad (\text{just before hit the ground})$$

$$|\vec{V}| = \sqrt{(80)^2 + (100)^2}$$

(a)

$t=2, \vec{V} = 80\hat{i} + 40\hat{j}$

$t=4, \vec{V} = 80\hat{i} + 20\hat{j}$

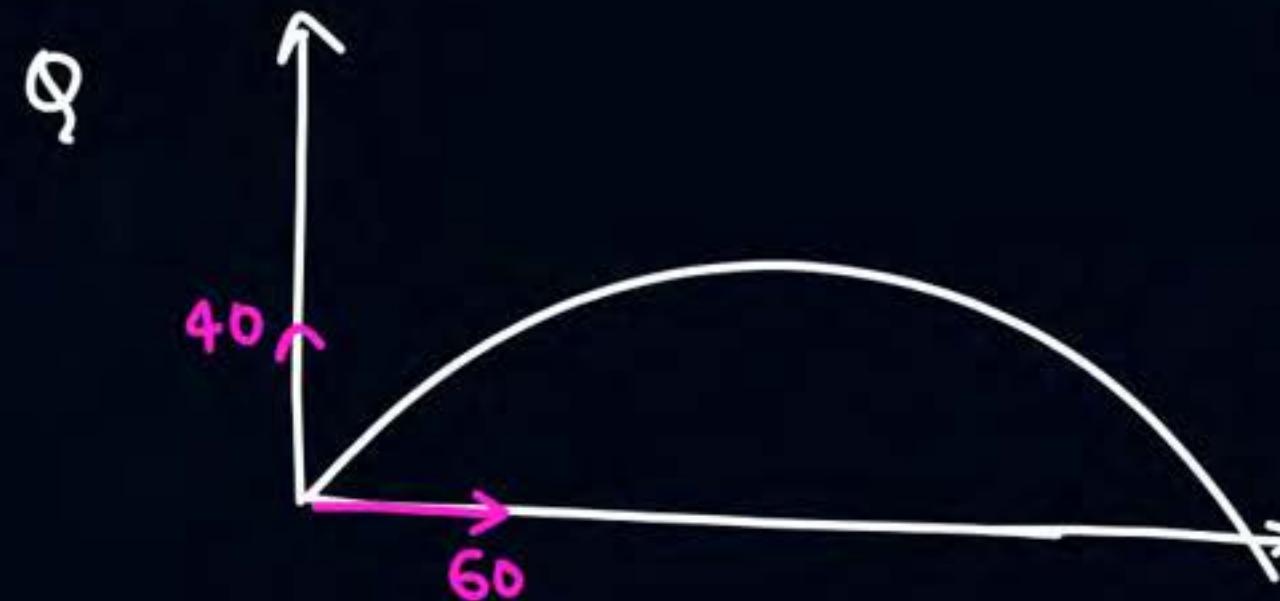
$t=10, \vec{V} = 80\hat{i} - 40\hat{j}$

$t=16, \vec{V} = 80\hat{i} - 100\hat{j}$

(c) find angle made by \vec{V} with horizontal at $t=16 \text{ sec}$

$$\vec{V} = 80\hat{i} - 100\hat{j}$$

$$\tan \alpha = \frac{100}{80}$$



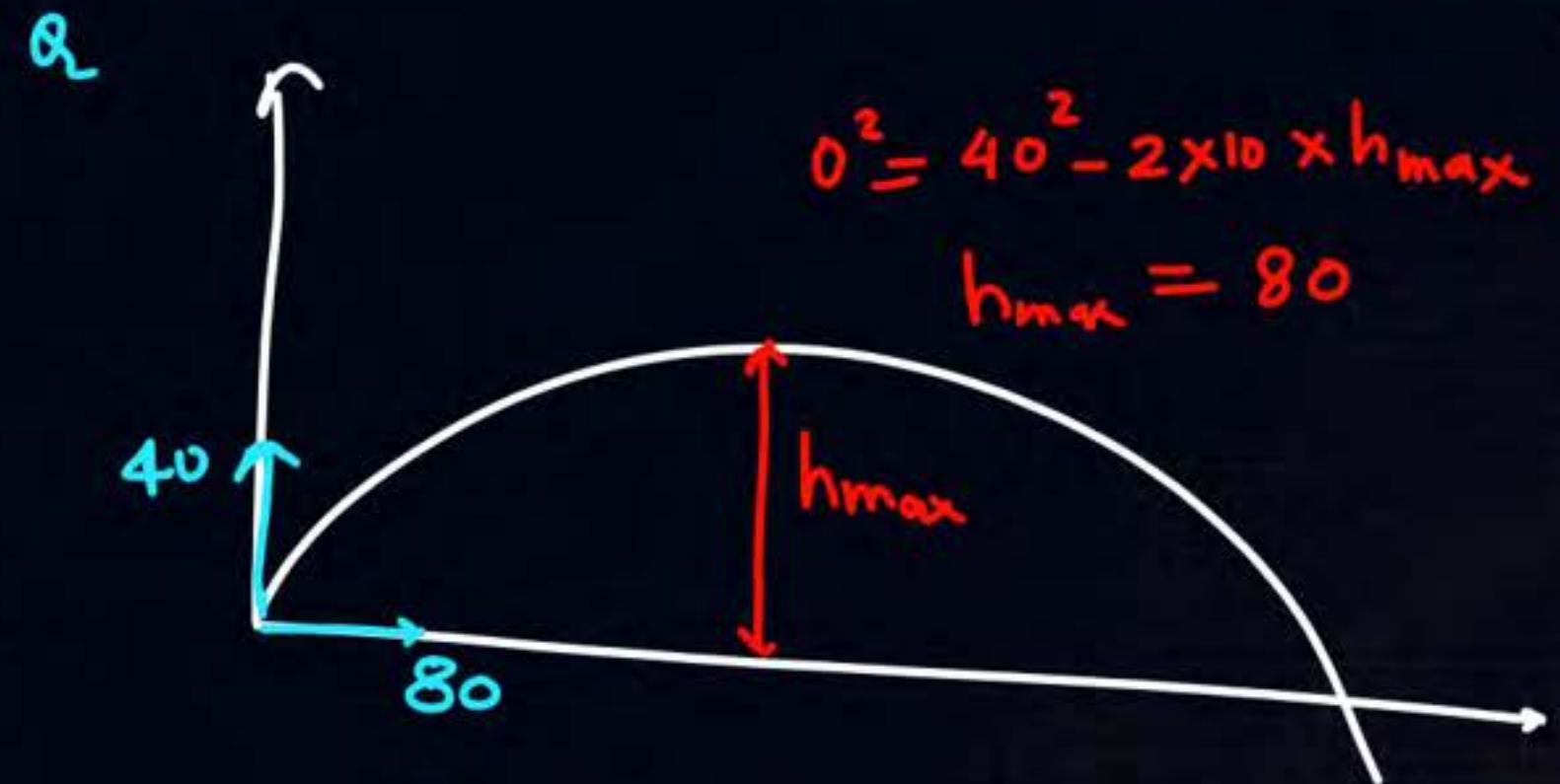
$$0^2 = 40^2 - 2 \times 10 \times h_{\max}$$

$$T = 4 + 4 = 8$$

$$h_{\max} = 80$$

$$R = 60 \times 8 = \underline{480}$$

V0



$$0^2 = 40^2 - 2 \times 10 \times h_{\max}$$

$$h_{\max} = 80$$

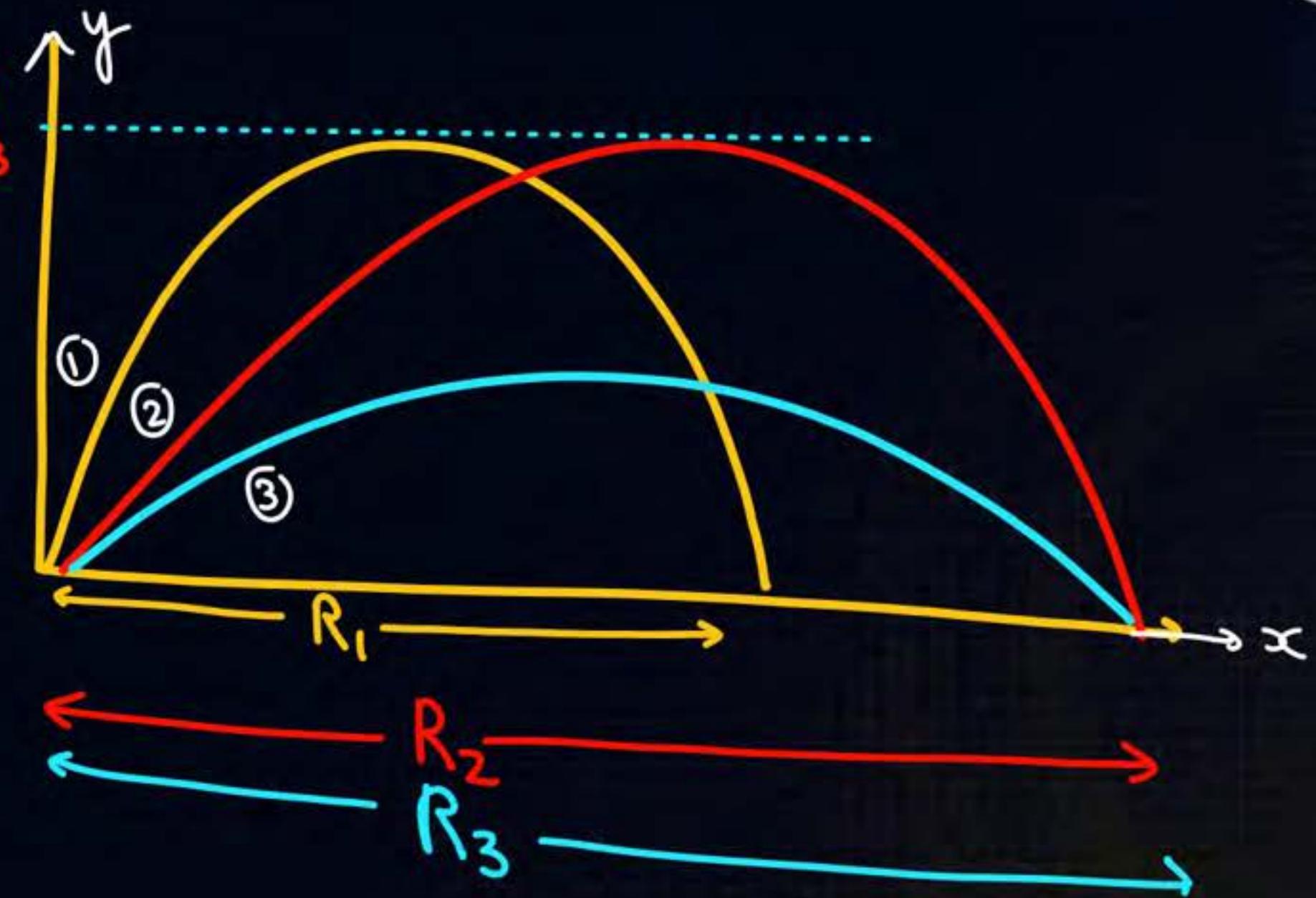
$$T = 4 + 4 = 8$$

$$h_{\max} = 80$$

$$R = 80 \times 8 = \underline{640}$$

Q

- * $(H_{max})_1 = (H_{max})_2 > (H_{max})_3$
- * $T_1 = T_2 > T_3$
- $(u_y)_1 = (u_y)_2 > (u_y)_3$
- $R_1 < R_2 = R_3$



Q

A particle is projected from ground with speed u at an angle θ with horizontal such that its maximum height is half of range. find θ

$$h_{\max} = \frac{1}{2} R$$

$$\frac{u^2 \sin^2 \theta}{2g} = \frac{1}{2} \frac{u^2 \sin 2\theta}{g}$$

$$\sin^2 \theta = \sin 2\theta$$

$$\sin^2 \theta = 2 \sin \theta \cos \theta$$

$$\tan \theta = 2$$

$$\boxed{\theta = \tan^{-1} 2}$$

Q. Two particle are projected with same speed u at angle 30° & 60° respectively. find ① Ratio of their max height ② " " " Range ③ " " " time of flight

$$\textcircled{1} \frac{(h_{\max})_1}{(h_{\max})_2} = \frac{\frac{u^2 \sin^2 30}{2g}}{\frac{u^2 \sin^2 60}{2g}} = \frac{\left(\frac{1}{2}\right)^2}{\left(\frac{\sqrt{3}}{2}\right)^2} = \frac{1}{3}$$

$$\textcircled{2} \frac{R_1}{R_2} = \frac{\frac{u^2 \sin(2 \times 30)}{g}}{\frac{u^2 \sin(2 \times 60)}{g}} = \frac{\sin 60}{\sin 120} = \frac{\sqrt{3}/2}{\sqrt{3}/2} = 1$$

M-Z

$$\theta = 30^\circ$$

$$90 - \theta = 60^\circ \rightarrow R_1 = R_2$$

$$\textcircled{3} T = \frac{2u \sin \theta}{g}$$

$$\frac{T_1}{T_2} = \frac{\sin 30}{\sin 60} = \frac{1/2}{\sqrt{3}/2} = \frac{1}{\sqrt{3}}$$

Q An arrow is projected such that its range is 400m and time of flight is 5 sec.
find

$$\textcircled{1} h_{\max}$$

$$\textcircled{2} \text{ inclination of arrow at } t=0 \\ \theta = ?$$

$$R = 400 = \frac{u^2 \sin 2\theta}{g}$$

$$5 = \frac{2usin\theta}{g}$$

$$u = \frac{25}{\sin\theta}$$

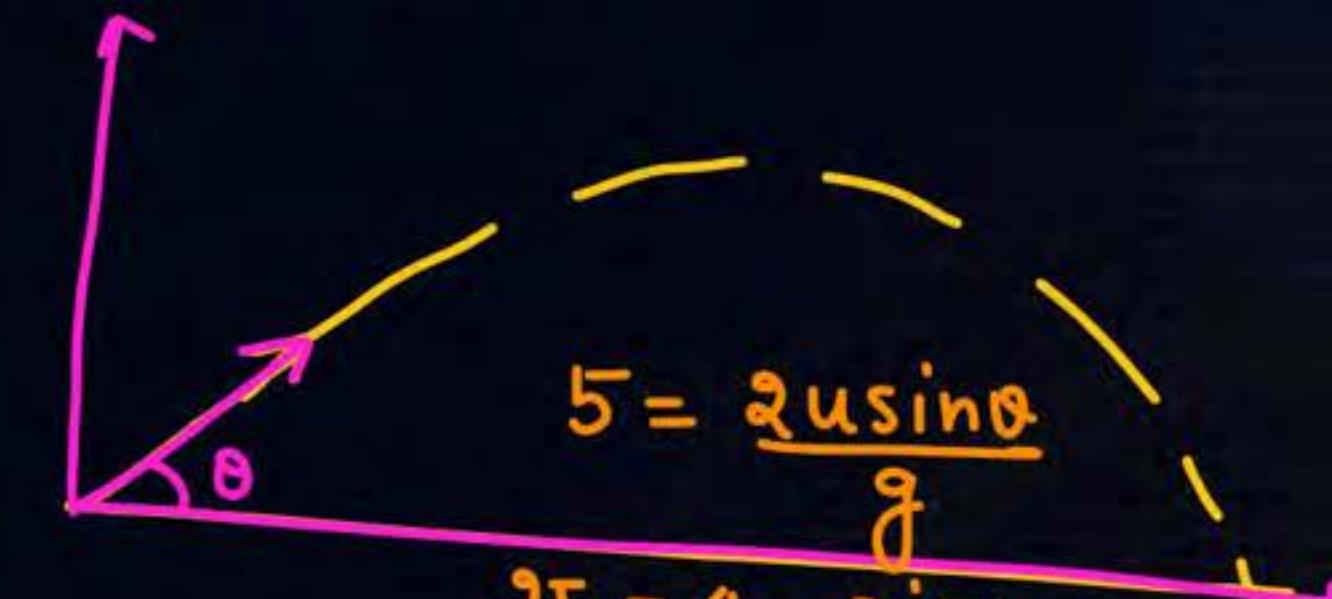
$$400 = \left(\frac{25}{\sin\theta}\right)^2 \cdot \frac{\sin 2\theta}{10}$$

$$400 = \frac{625}{\sin^2\theta} \cdot \frac{2 \sin\theta \cos\theta}{10}$$

$$400 = 125 \frac{\cos\theta}{\sin\theta} = 125 \cot\theta$$

$$\cot\theta = \frac{400}{125}$$

$$\tan\theta = 125/400 = \frac{5}{16}$$



$$5 = \frac{2usin\theta}{g}$$

$$25 = \frac{4}{100} u^2 \sin^2\theta$$

$$u^2 \sin^2\theta = 625$$

$$H_{\max} = \frac{u^2 \sin^2\theta}{2g} = \frac{625}{20}$$

Q An arrow is projected such that its range is 400m and time of flight is 5 sec.
find

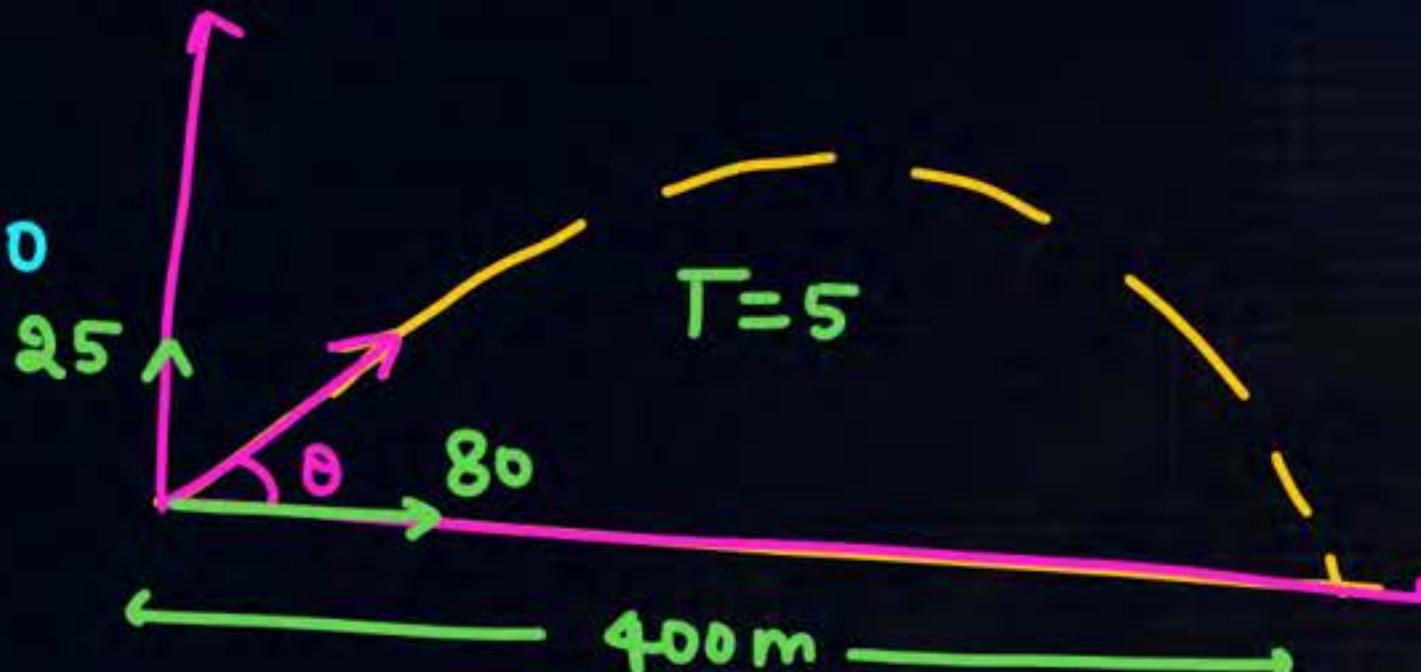
- ① h_{\max}
- ② inclination of arrow at $t=0$

$$\tan \theta = \frac{25}{80} = \frac{5}{16}$$

$$\vec{u} = 2.5\hat{i} + 80\hat{j}$$

$$0^2 = (25)^2 - 2 \times g \times h_{\max}$$

$$h_{\max} = \frac{(25)^2}{20} = \frac{625}{20}$$



Q2 A particle is projected at angle θ such that its range is 1200 m and time of flight is 20 sec
find ① angle at which particle is projected.

$$\tan \theta = \frac{100}{60} = \frac{5}{3}$$



Q. Find equation of trajectory.

$$x = 60t \quad t = \frac{x}{60}$$

$$y = 80t - \frac{1}{2} g t^2$$

$$y = 80 \frac{x}{60} - \frac{1}{2} g \left(\frac{x}{60}\right)^2$$

$$y = \frac{4}{3}x - \frac{5}{3600}x^2$$



KC
किसी time t पर x, y
मिकालों और
 t को eliminate करते

Q

find eqⁿ of trajectory

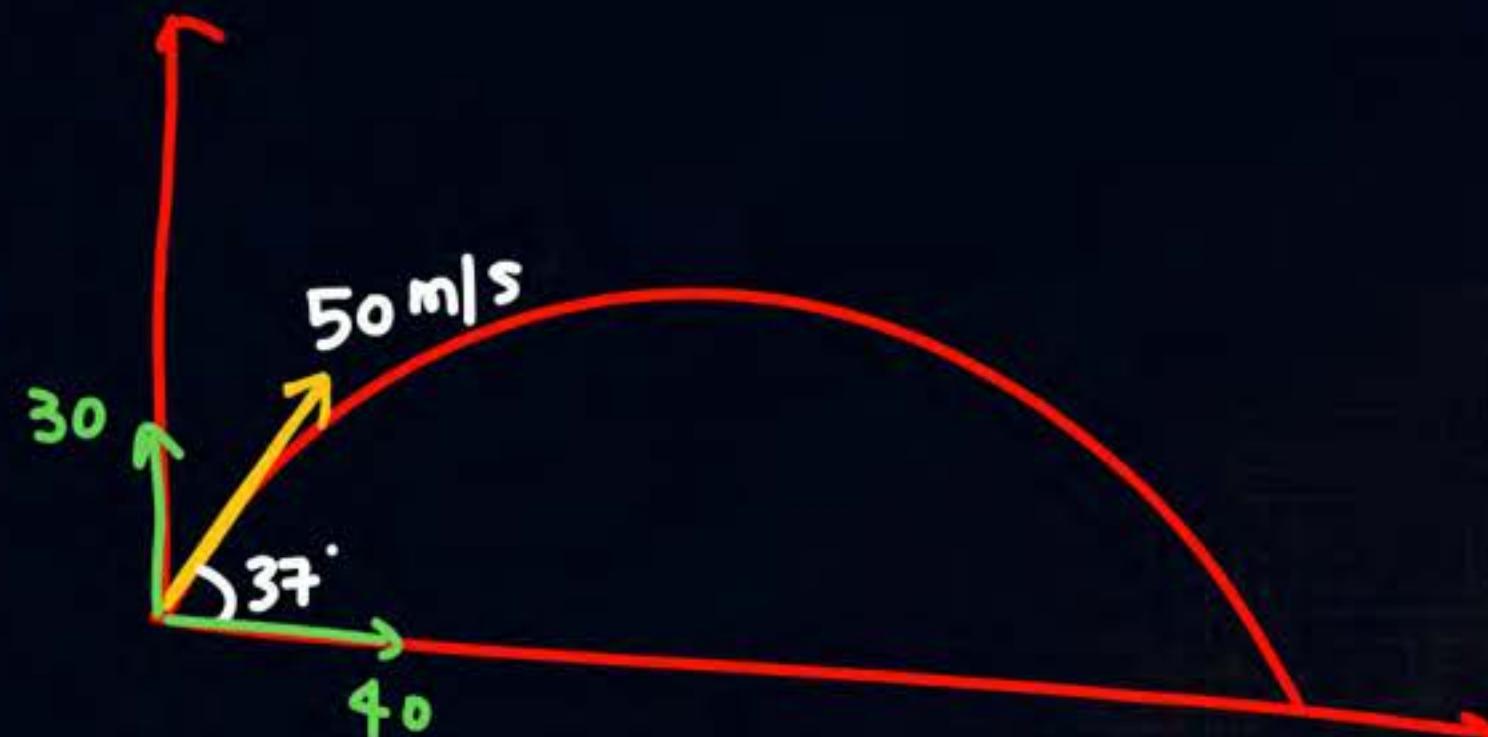
$$x = 40t$$

$$t = x/40$$

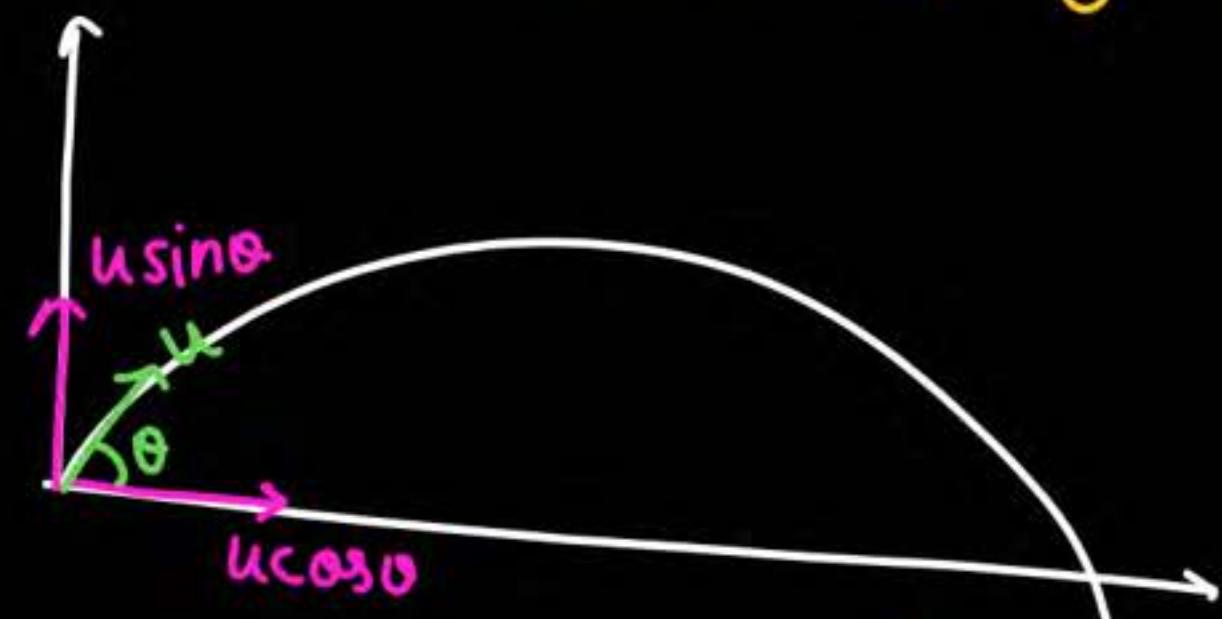
$$y = 30t - \frac{1}{2} g t^2$$

$$y = 30 \cdot \frac{x}{40} - \frac{1}{2} g \frac{x^2}{(40)^2}$$

$$y = \frac{3}{4}x - \frac{5}{1600}x^2$$



Equation of trajectory



Rough copy $\frac{2\pi}{T}$
 2π calculation
 $\frac{T}{\pi}$

$$x = u \cos \theta \cdot t \quad t = \frac{x}{u \cos \theta}$$

$$y = u \sin \theta \cdot t - \frac{1}{2} g t^2$$

$$y = u \sin \theta \cdot \frac{x}{u \cos \theta} - \frac{1}{2} g \frac{x^2}{u^2 \cos^2 \theta}$$

$$y = x \tan \theta - \frac{1}{2} g \frac{x^2}{u^2 \cos^2 \theta}$$

$$y = x \tan \theta - \frac{1}{2} g \left(\frac{x}{u \cos \theta} \right)^2$$

Q If eqn of trajectory is given by

$$y = x \sqrt{3} - \frac{x^2}{20}$$

Find ① u, Q, T, R, θ

$$y = x \tan \theta - \frac{1}{2} g \frac{x^2}{u^2 \cos^2 \theta} \quad (\text{Compare})$$

$$\sqrt{3} = \tan \theta$$

$$\boxed{\theta = 60^\circ}$$

$$\frac{1}{20} = \frac{g}{2 u^2 \cos^2 \theta}$$

$$\frac{1}{20} = \frac{10}{2 u^2 \cos^2 60^\circ}$$

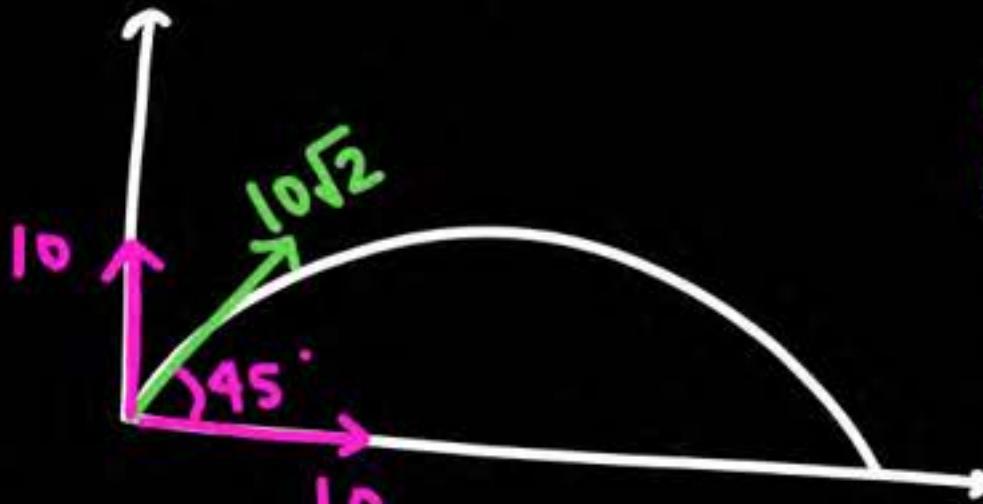
$$2u^2 \frac{1}{4} = 20 \times 10$$

$$\begin{cases} u^2 = 400 \\ u = 20 \end{cases}$$



Q If eqn of trajectory is given by

$$y = x - \frac{x^2}{20}$$



① find u, θ, T, R, \dots

$$T = l + l = 2$$

$$R = 10 \times 2 = 20$$

$$y = x - \frac{x^2}{20}$$

$$y = x \tan \theta - \frac{1}{2} g \frac{x^2}{u^2 \cos^2 \theta}$$

$$\tan \theta = 1$$

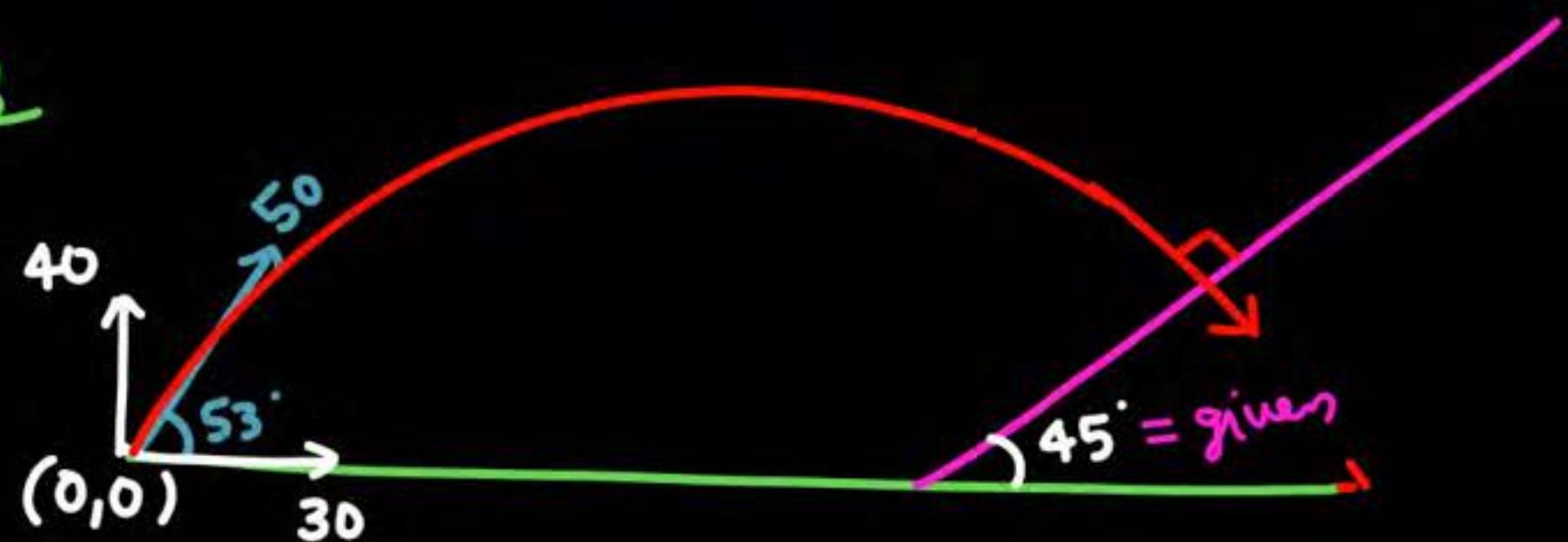
$$\theta = 45^\circ$$

$$\frac{1}{20} = \frac{g}{2 u^2 \cos^2 45^\circ}$$

$$2u^2 \frac{1}{2} = 200$$

$$u = 10\sqrt{2}$$

Q



particle strike the plane
perpendicularly.

find T .

Co-ordinate of point where
particle strike at plane



$$u \cos 45 = 30$$

$$u = 30\sqrt{2}$$

$$t = 7 \Rightarrow$$

$$x = 30 \times 7 = 210$$

$$y = 40 \times 7 - \frac{1}{2} \times 10 \times 7^2$$

JA find distance of striking point from projection point

Distance formula = $\sqrt{(x-0)^2 + (y-0)^2} = \checkmark$

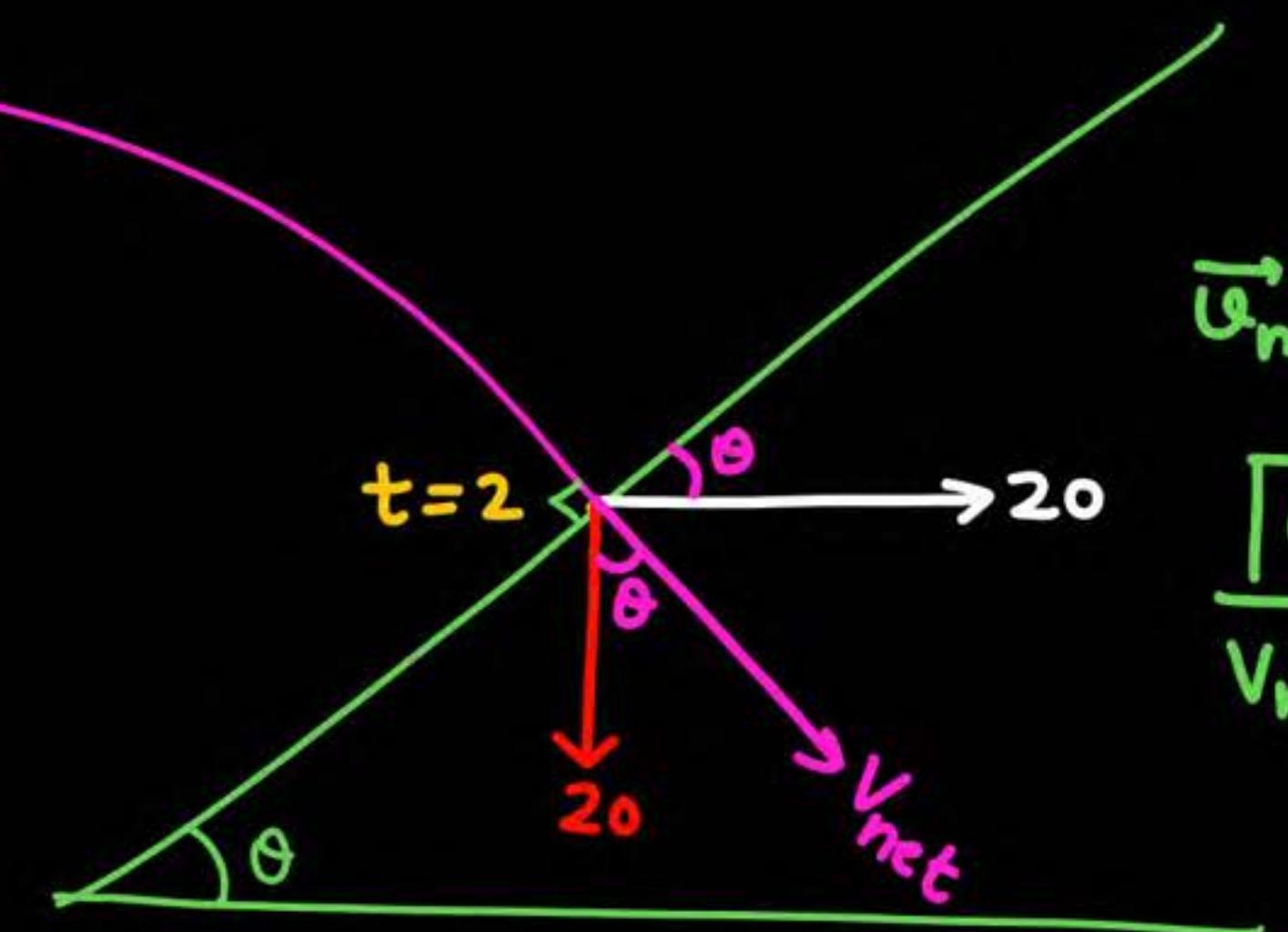
Q

particle strike the
plane perpendicularly
find α

$$\textcircled{y} \quad v = u + at$$

$$v = -10 \times 2$$

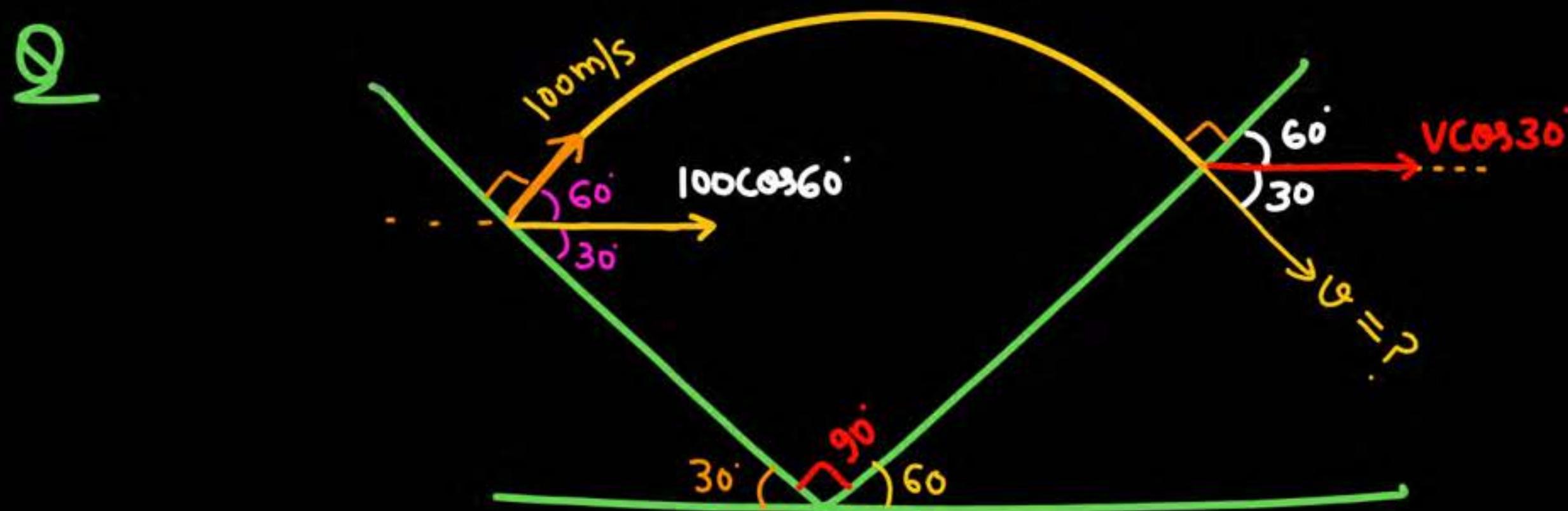
$$v = \theta_{20} = u_f$$



$$\vec{v}_{net} = 20\hat{i} - 20\hat{j}$$

$$\boxed{\alpha = 45^\circ}$$

$$V_{net} = 20\sqrt{2}$$



$$100 \cos 60 = V \cos 30$$

$$100 \times \frac{1}{2} = V \frac{\sqrt{3}}{2}$$

$$V = \frac{100}{\sqrt{3}}$$

$$\vec{r} = 4t^2 \hat{i} + 2t^3 \hat{j} + 4t^4 \hat{k}$$

P
W

Q A particle is moving such that

$$x = 4t^2$$

$$y = 2t^3$$

$$z = 4t^4$$

① find velocity at $t = 1 \text{ sec}$

$$\vec{v} = 8\hat{i} + 6\hat{j} + 16\hat{k}$$

② find acc at $t = 2 \text{ sec}$

$$\vec{a} = 8\hat{i} + 24\hat{j} + 192\hat{k}$$

$$v_x = \frac{dx}{dt} = 8t \longrightarrow a_x = 8$$

$$v_y = \frac{dy}{dt} = 6t^2 \longrightarrow a_y = 12t$$

$$v_z = \frac{dz}{dt} = 16t^3 \longrightarrow a_z = 48t^2$$

$$\vec{v} = 8t\hat{i} + 6t^2\hat{j} + 16t^3\hat{k}$$

$$\vec{a} = 8\hat{i} + 12t\hat{j} + 48t^2\hat{k}$$

Q A particle is moving such that

Q

$$\vec{r} = 2t^2 \hat{i} + 4t^3 \hat{j} + 6t^2 \hat{k}$$

$$\vec{v} = \frac{d\vec{r}}{dt} = 4t \hat{i} + 12t^2 \hat{j} + 12t \hat{k}$$

$$\boxed{\vec{a} = 4 \hat{i} + 24t \hat{j} + 12 \hat{k}}$$

Q A particle is moving such that

$$\vec{r} = 3t^2 \hat{i} + 2t^3 \hat{j} + 10t \hat{k}$$

find ① find \vec{v} & \vec{a} at $t = 1\text{ sec}$

$$\vec{v} = 6t \hat{i} + 6t^2 \hat{j} + 10 \hat{k}$$

$$\vec{a} = 6 \hat{i} + 12t \hat{j} + 0 \hat{k}$$

$$t = 1 \quad \vec{v} = 6 \hat{i} + 6 \hat{j} + 10 \hat{k}$$
$$\vec{a} = 6 \hat{i} + 12 \hat{j}$$

vector

② find angle b/w \vec{v} & \vec{a}
at $t = 1\text{ sec}$

$$\vec{a} \cdot \vec{v} = a v \cos \theta$$

$$\cos \theta = \frac{\vec{a} \cdot \vec{v}}{av} = \frac{36 + 72 + 0}{\sqrt{6^2 + 12^2} \sqrt{6^2 + 6^2 + 10^2}}$$

= ✓

प्र० कानूनी

$$Q \quad y = 2x - \frac{x^2}{6}$$

Range = ?

$$y = 2x \left(1 - \frac{x}{12} \right)$$

$$\boxed{R=12}$$

$$y = x \tan \theta \left(1 - \frac{x}{R} \right).$$

$$y = x \tan \theta - \frac{x^2 \tan \theta}{u \cos \theta \cdot 2u \sin \theta g}$$

$$y = x \tan \theta - \frac{1}{2} \frac{x^2}{u^2} \frac{\sin \theta}{\cos \theta} g$$

$$y = x \tan \theta - \frac{1}{2} g \frac{x^2}{u^2 \cos^2 \theta}$$

$$\Omega \quad y = ax - bx^2$$

find θ , & Range

$$R = \frac{a}{b}$$

$$y = ax \left(1 - \frac{bx^2}{ax}\right)$$

$$\tan \theta = a$$

$$y = ax \left(1 - \frac{x}{a/b}\right)$$

$$\theta = \tan^{-1} a$$

$$y = x \tan \theta \left(1 - \frac{x}{R}\right)$$

(Ques practice on diff & integration based ques)

Q $\vec{r} = 3t^2 \hat{i} + 4t \hat{j} - 6t^3 \hat{k}$

find \vec{v} , \vec{a} at $t=1$ sec

$\vec{v} = \frac{d\vec{r}}{dt} = 6t \hat{i} + 4 \hat{j} - 18t^2 \hat{k} \Rightarrow t=1 \quad \vec{v} = 6\hat{i} + 4\hat{j} - 18\hat{k}$

$\vec{a} = 6\hat{i} + 0\hat{j} - 36\hat{k}$

1D

A particle is moving on x -axis such that

Q find \vec{v}, \vec{a} , at $t=2 \text{ sec}$

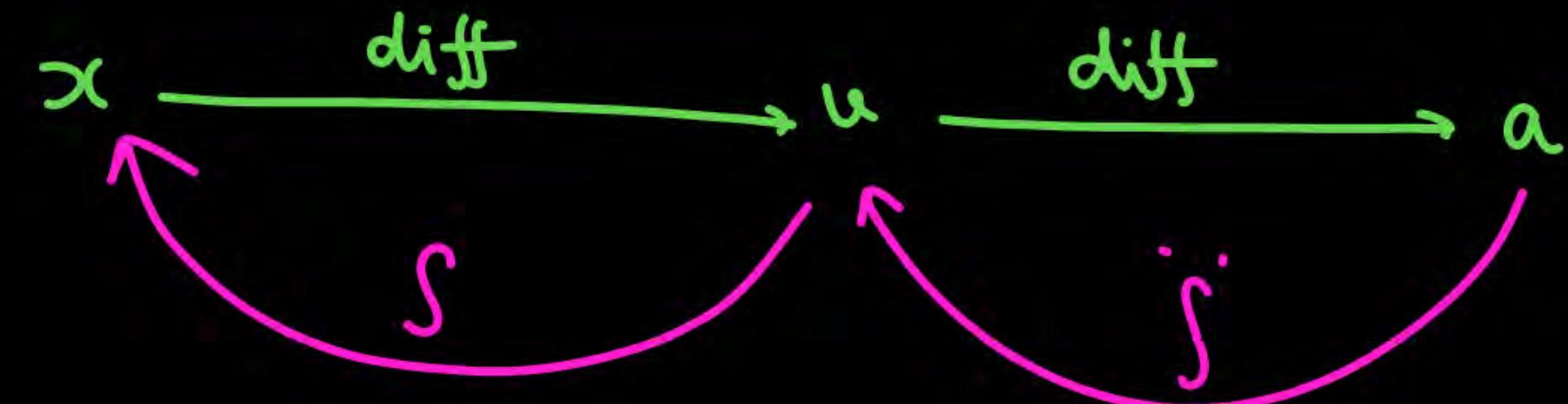
$$x = t^3 + 2t^2 + 6t$$

$$v = 3t^2 + 4t + 6$$

$$a = 6t + 4$$

$$t=2, v = 12+8+6$$

$$a = 16$$



at $t=0$

Q A particle start motion[^] from $x=0$
such that its v vs t relation
is given as

$$v = 4t^3 + 3t^2 + 2t$$

find location of particle $t=1 \text{ sec}$

$$x = \int v dt \text{ (indefinite)} \checkmark$$

$$x = \int (4t^3 + 3t^2 + 2t) dt$$

$$x = 4\frac{t^4}{4} + 3\frac{t^3}{3} + 2\frac{t^2}{2} + C$$

$$x = t^4 + t^3 + t^2 + C$$

$$(t=0, x=0) 0=0+0+0+C$$

$$\boxed{C=0}$$

$$x = t^4 + t^3 + t^2 + 0$$

$$t=1, x = 1+1+1 = 3$$

Q A particle start motion at $t=0$

from $x=+10$, such that - - - - .

$$v = 4t^3 + 3t^2 + 2t$$

find location of particle at $t=1 \text{ sec}$

$$x = \int v dt$$

$$x = t^4 + t^3 + t^2 + C$$

$$t=0, x=10 \text{ (put)}$$

$$10 = 0+0+0+C \Rightarrow \boxed{C=10}$$

$$x = t^4 + t^3 + t^2 + 10$$

$$t=1, x = 13 \text{ Ans}$$

Q A particle starts motion from $x=5$ at $t=0$, such that

$$v = t^2 + t$$

find location of particle at $t=6$ sec

$$x = \frac{t^3}{3} + \frac{t^2}{2} + C$$

$$t=0, x=5$$

$$5 = 0 + 0 + C$$

$$\boxed{C=5}$$

$$x = \frac{t^3}{3} + \frac{t^2}{2} + 5$$

$$t=6 \quad x = \frac{6^3}{3} + \frac{6^2}{2} + 5$$

$$x = 72 + 18 + 5 = 95$$

(M-2) Definite Integration

$$v = \frac{dx}{dt}$$

$$dx = v dt$$

$$\int_{x=5}^{x_f} dx = \int_{t=0}^{t=6} (t^2 + t) dt$$

$$\int_{5}^{x_f} dx = \int_{0}^{6} (t^2 + t) dt$$

$$x \Big|_5^{x_f} = \left(\frac{t^3}{3} + \frac{t^2}{2} \right) \Big|_0^6$$

$$x_f - 5 = \left(\frac{6^3}{3} + \frac{6^2}{2} \right)$$

$$- \left(\frac{0^3}{3} + \frac{0^2}{2} \right)$$

$$x_f - 5 = 72 + 18 - 0$$

$$x_f = 90 + 5$$

$$\boxed{x_f = 95}$$

Q A particle starts motion from rest from origin at $t=0$
such that $a = 6t$

find v, x (location) at $t = 2 \text{ sec}$

$$a = 6t$$

$$v = \int a dt = \int 6t dt$$

$$v = 6 \frac{t^2}{2} + C$$

$$v = 3t^2 + C$$

$$t=0, v=0$$

$$0=0+C$$

$$C=0$$

$$v = 3t^2$$

$$t=2, v=12$$

$$x = \int 3t^2 dt = 3 \frac{t^3}{3} + C'$$

$$x = t^3 + C'$$

$$t=0, x=0, 0=0+C' \Rightarrow C'=0$$

$$x = t^3$$

$$t=2, x=8$$

Q A particle starts motion at $t=0$ having initial velocity $v=+10$ and initial location at $x=20$
such that $a=24t^2$



find v, x (location) at $t=2$ sec

$$a = 24t^2$$

$$v = \int 24t^2 dt = 24 \frac{t^3}{3} + C$$

$$v = 8t^3 + C$$

$$\text{put } t=0, v=10$$

$$10 = 0 + C \Rightarrow C = 10$$

$$v = 8t^3 + 10$$

$$v = 8t^3 + 10$$

$$x = \int (8t^3 + 10) dt =$$

$$x = 8 \frac{t^4}{4} + 10t + C'$$

$$t=0, x=20 \Rightarrow C' = 20$$

$$x = 2t^4 + 10t + 20$$

$$t=2, v = 8 \times 8 + 10 = 74$$

$$x = 2 \times 16 + 10 \times 2 + 20 = 72$$

Q A particle is moving on x-axis such that its acc is given by $a = \frac{3}{v}$. at $t=0$ its velocity is 1 m/s find Velocity at $t=40$ sec

P
W

Sol

$$a = \frac{3}{v}$$

$$\text{at } t=0, v=1$$

$$\frac{dv}{dt} = \frac{3}{v}$$

$$\frac{1}{2} = 0 + C$$

$$\int v dv = \int 3 dt$$

$$\frac{v^2}{2} = 3t + \frac{1}{2}$$

$$\frac{v^2}{2} = 3t + C$$

$$v^2 = 6t + 1$$

$$t=40, v = \sqrt{6 \times 40 + 1} = \sqrt{241}$$

(सबसे पहले थे दरवा
given acc ए
पूछा क्या है)

$$\begin{aligned} v &= \frac{dx}{dt} \\ a &= \frac{dv}{dt} \\ a &= v \frac{dv}{dx} \end{aligned}$$

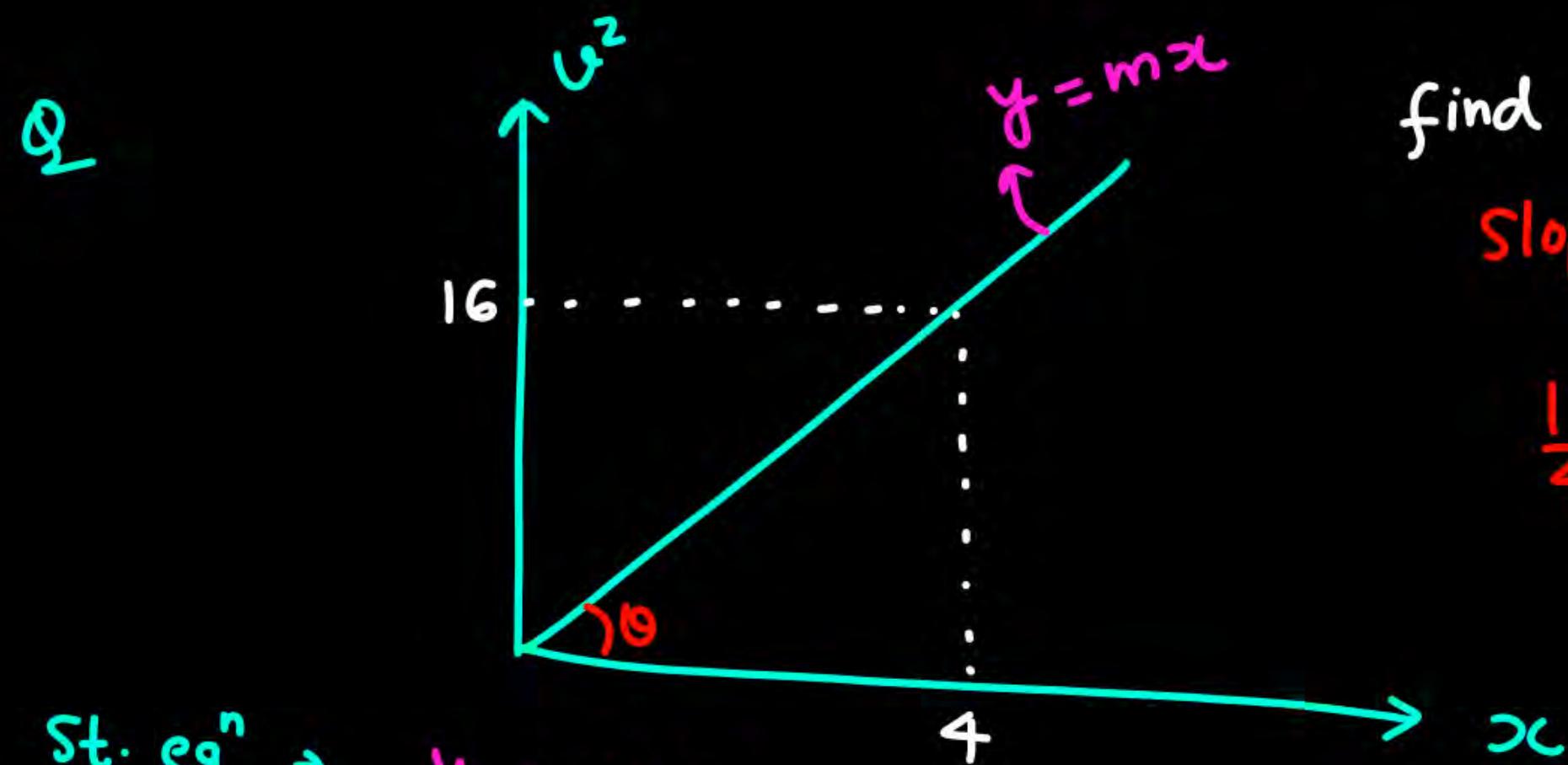
Q If $v = x^2 + 3x$
find acc at $x = 2$

$$a = v \frac{dv}{dx} \quad \frac{dv}{dx} = 2x + 3$$

$$a = (x^2 + 3x)(2x + 3)$$

$$\text{put } x = 2, a = (4+6)(4+3)$$

$$\boxed{a = 70}$$



find acc at $x=4$

$$\text{Slope} = \frac{dy}{dx} = \frac{d(v^2)}{dx}$$

$$\frac{16}{4} = 2v \frac{dv}{dx}$$

$$4 = 2a \Rightarrow \boxed{a=2}$$

St. eqⁿ $\Rightarrow y = mx$

$$v^2 = 4x$$

$$2v \frac{dv}{dx} = 4$$

$$\underline{\underline{a = 2}}$$

Q

find acc

at $x = 4$

$$\text{Slope} = \frac{dy}{dx} = \frac{dv}{dx} = \frac{16}{4}$$

$$a = g \frac{dv}{dx}$$

$$a = 16 \times \frac{16}{4} = 64$$

