



# Robótica Móvel e Inteligente

## Path Planning and Obstacle Avoidance

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## Outline

- ① Navigation
- ② Path planning concepts
- ③ Environment representation
- ④ Search algorithms
- ⑤ Potential field path planning
- ⑥ Obstacle avoidance
- ⑦ Bibliography

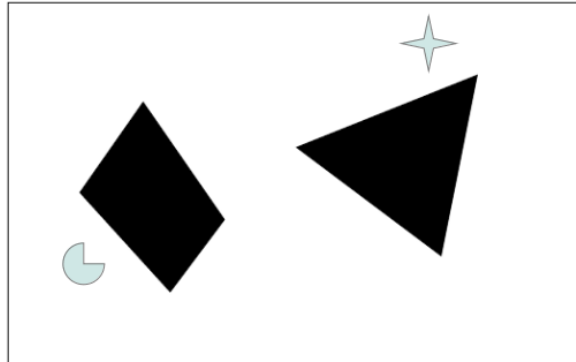
# Navigation

## Definition

- “Given partial knowledge about its environment and a goal position or series of positions, **navigation** encompasses the ability of the robot to act based on its knowledge and sensor values so as to reach its goal positions as efficiently and as reliably as possible.”

[Siegwart, <http://www.cs.cmu.edu/~rasc/Download/AMRobots6.pdf>]

- In mobile robotics the knowledge about the **environment** and **situation** is usually only **partially** and **uncertain**



# Navigation

## Issues in navigation

- Where am I?
  - localization
- Where have I been?
  - mapping
- Where should I go?
  - decision
- **What's the best way to get there?**
  - **Path planning**
- How do I get there?
  - Path following and obstacle avoidance (Motion)

# Path planning

## Definition

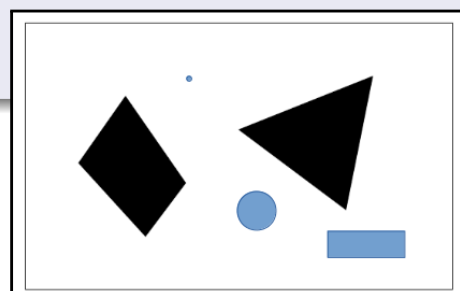
- **Path planning** – the task of computing a **path** for the robot such that it can reach the desired goal without colliding with **known** obstacles
  - Optimal paths can be hard to compute, specially for robots that can not move in arbitrary directions (i.e. non-holonomic robots)
- 
- Path and trajectory are often used with the same meaning
    - But one can distinguish them
  - **Path** – only geometric considerations
    - a way from a start position/pose/configuration to a goal one
  - **Trajectory** – includes geometric and time considerations
    - the dynamics is also considered
  - Another term is **motion**, applied to mobile robots or manipulators
    - considers other constraints, like collision avoidance (of dynamic obstacles)

[2] Peter Corke, <https://robotacademy.net.au/masterclass/paths-and-trajectories/>

# Path planning

## Some concepts

- **Configuration space (C-Space)** – set of possible valid configurations (poses) of the robot
  - Defines the search space and the set of allowable paths
- **Free space (F-Space)** – set of valid configurations that do not intercept obstacles in the environment
  - Depends on the robot shape
- Cases to be considered:
  - Point robot .
  - Symmetric robot ●
  - Non-symmetric robot ■



# Path planning

## Some assumptions

- **Assumption 1:**
  - Often, path planning methods assume that the robot is symmetric and holonomic, and treat it simply as a point
  - If the robot is treated as a point, the obstacles must be “inflated” in order to compensate the robot radius
  - This approach greatly simplifies path planning
- **Assumption 2:**
  - there exists a good enough estimation of the robot’s pose
- **Assumption 3:**
  - there exists a good enough representation (map) of the environment that can be used to compute a path

# Environment representation

## Possible representations

- There are different ways to represent the environment
- Two common ones are geometric maps and topological maps
- Geometric maps may represent a continuous geometric description
- Topological representations are formally graphs where:
  - nodes denote areas/points/sections in the environment
  - arcs denote adjacency between nodes



# Environment representation

## Example of metric and topological maps

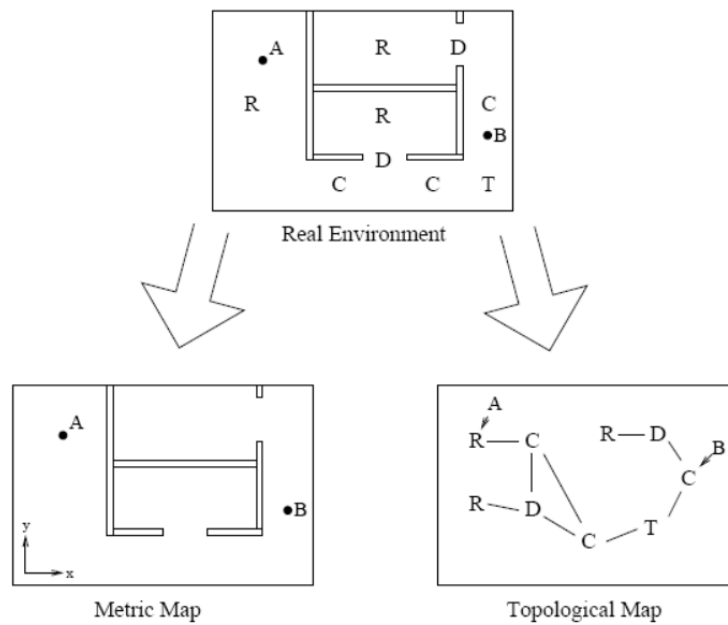
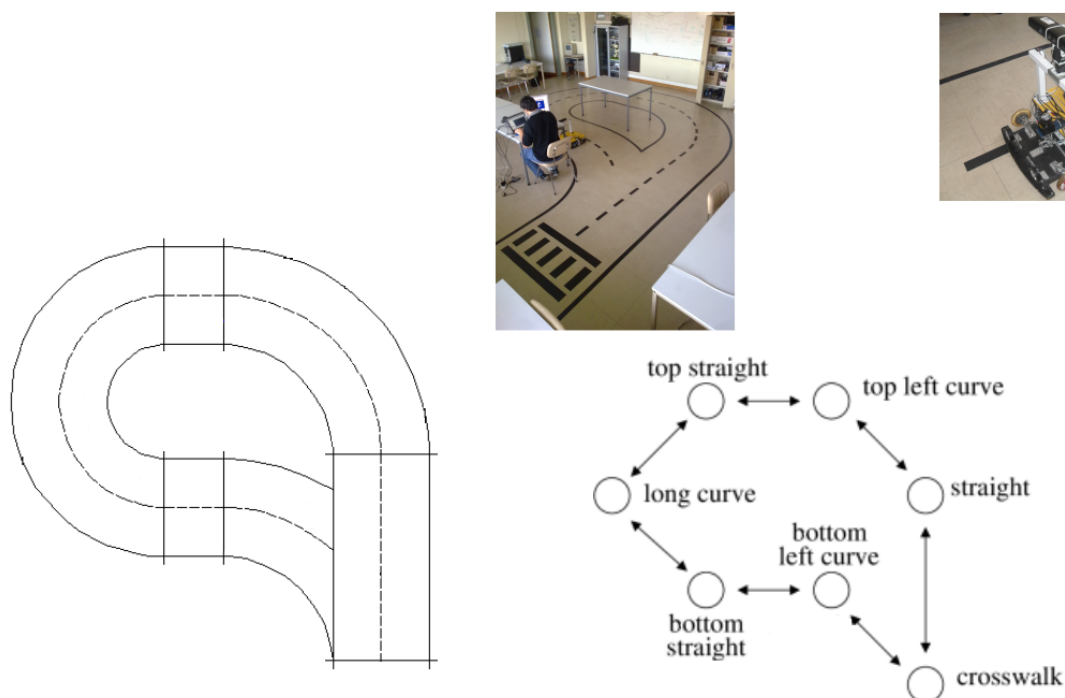


Figure from Meyer, "Map-based navigation in mobile robotics". 2003

# Environment representation

## Another example of metric and topological maps



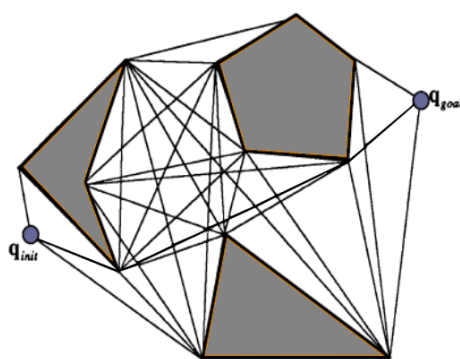
# Environment representation

## Mapping approaches

- Path-planning algorithms often are only applicable to **discrete maps**
  - Transforming a possibly continuous environment into a discrete representation suitable for the chosen path-planning algorithm is a must
  - Path planner approaches differ in how they perform this decomposition
- 
- General strategies for decomposition:
    - **Road map** – identify routes within the free space
      - Transforming the free space into a network of 1-D curves or lines, called road-map
    - **Cell decomposition** – divide space into cells that are discriminated between free and occupied cells
      - Transforming the free space into a connectivity graph of free cells, based on adjacency
    - **Potential field** – apply a mathematical function over the space
      - Transforming the free space into a field, or gradient, that directs the robot to the goal position

# Path planning approaches

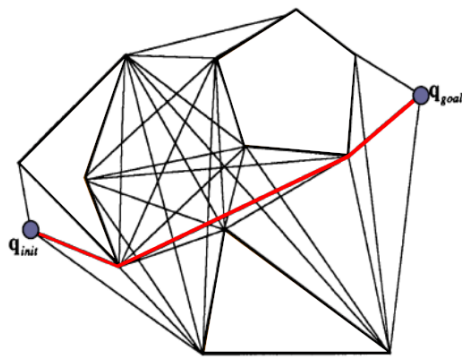
## Visibility graph



- Obstacles are treated as polygons
    - for every obstacle, a polygon including it is defined
  - Then, a graph is defined, where:
    - $q_{init}$ ,  $q_{goal}$ , and all polygons' vertices are the **nodes**
    - for every pair of nodes which can be connected by a line segment, not passing through an obstacle, there is an **edge**
      - such pair of nodes can “see” each other)
- 
- With the detected nodes and edges, a connectivity graph (visibility graph) is then generated
    - every edge can be labelled with some cost function value (for example, the Euclidian distance)

# Path planning approaches

## Visibility graph (2)

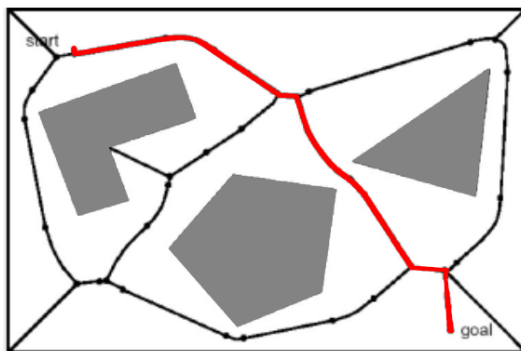


- A **graph search** algorithm can be used to find the shortest path along the “roads” defined by the visibility graph
- Efficient method for sparse environments

- **Problem** – may cause the robot to move too close to obstacles
  - little margin for errors in motion
- **Solution** – grow obstacles (even more), giving more clear space between robot and obstacles

# Path planning approaches

## Voronoi diagrams



- For each point in free space its **distance to the nearest obstacle** is computed
- Then, the **set of points equidistant** from the nearest two or more obstacle boundaries are selected

- The Voronoi diagram is obtained by linking these points, from where the shortest path can be computed
- The result is a **path of maximum distance from obstacles**
  - usually far from optimal, in the sense of total path length

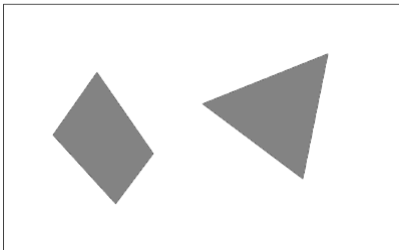
# Path planning approaches

## Cell decomposition

- Divide space into simple, connected regions called **cells**
  - cells can be either free, occupied or partially occupied
- Discretize the space by constructing an **adjacency graph** of the free cells
- Adjacency graph
  - **Nodes** – free cells
  - **Edges** – there is an edge between every pair of nodes whose corresponding cells are adjacent
- Locate “goal” and “start” cells and search for the **shortest path** in the adjacency graph that join them
- Typically paths are assumed to pass through the **mid-points** of the cells

# Path planning approaches

## Cell decomposition (2)



- Given an environment, how to decompose it?

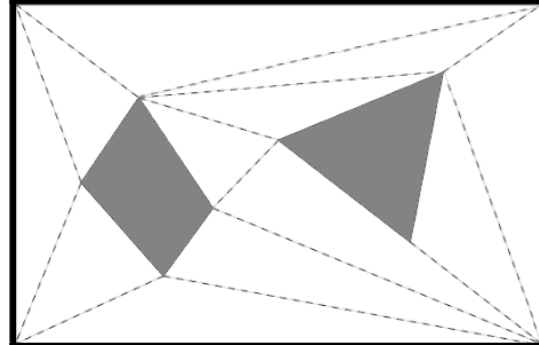
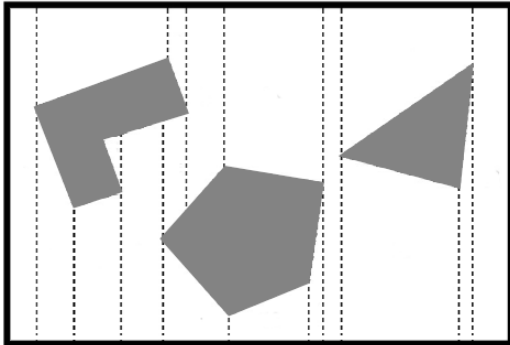
- Two possible cell decomposition methods
  - **Exact cell decomposition** and **approximate cell decomposition**
- Exact cell decomposition
  - Free cells correspond exactly to free space
    - There is no partially occupied cells
- Approximate cell decomposition
  - Some free space is included in partially occupied cells
    - the partially occupied cells are considered as occupied
- Cells may or may not differ on size or shape



# Path planning approaches

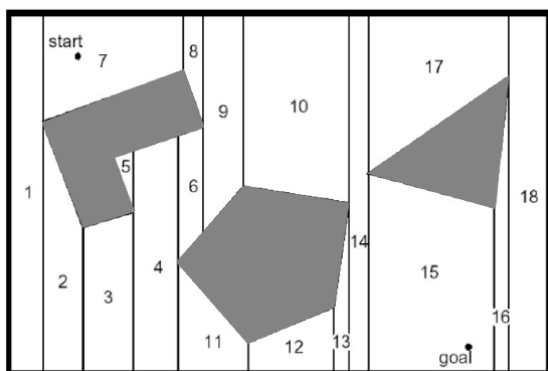
## Exact cell decomposition

- The free space  $F$  is divided into a set of non-overlapping **convex** cells whose union is **exactly**  $F$
- Examples of convex shapes: **trapezoids**, **triangles**
- The basic abstraction behind this method is that the position of the robot within each cell does not matter, only the ability to travel to another free cell

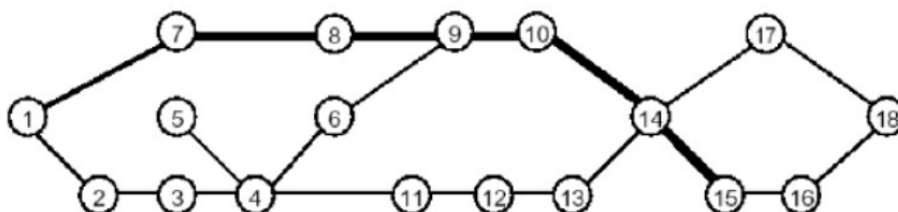


# Path planning approaches

## Exact cell decomposition (2)

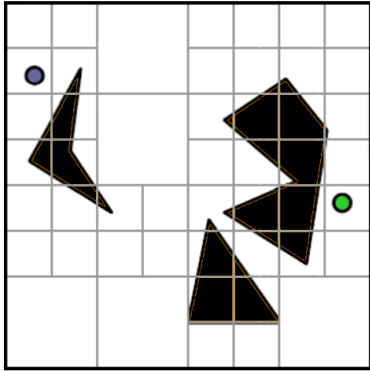


- A **connectivity graph** can be constructed, where:
  - nodes represent the free cells
  - every adjacent pair of cells is connected by an edge
- Result can be complex if the world is complex
  - Good for sparse environments



# Path planning approaches

## Approximate cell decomposition



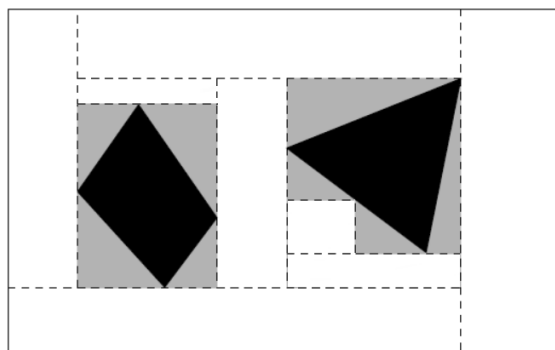
- Free space  $F$  is represented by a set of non-overlapping cells whose union is contained in  $F$
- Cells usually have simple, regular shapes, like rectangles, squares, hexagons

- Two approaches:
  - Variable-size cell decomposition
  - Fixed-size cell decomposition

# Path planning approaches

## Variable-size cell decomposition

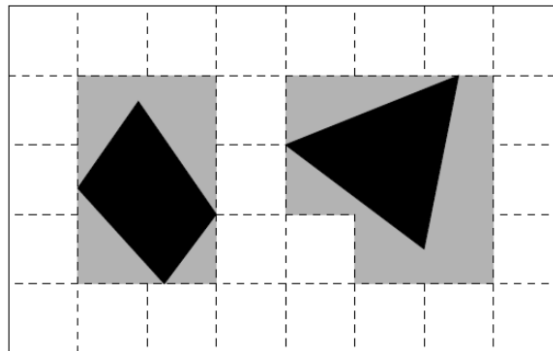
- Decomposing using variable-size cells
  - with a rectangular shape
- Grey areas are free space considered as occupied



# Path planning approaches

## Fixed-size cell decomposition

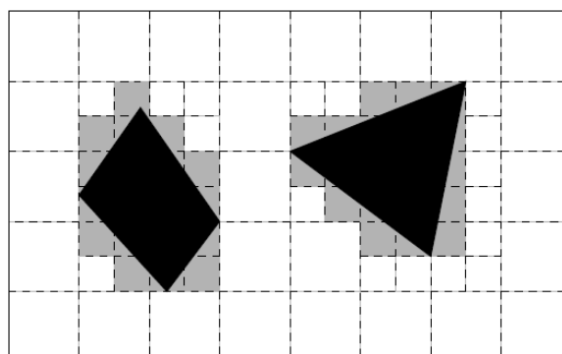
- Decomposing using fixed-size cells
  - with a square shape
- Grey areas are free space considered as occupied
- Cell size is not dependent on the obstacle size in the environment
  - narrow passage ways can be lost
- Low computational complexity of path planning



# Path planning approaches

## Quad-tree cell decomposition

- Decomposing using variable-size cells
  - with a square shape
- Partially occupied cells are subdivided until a given granularity
- At each level of resolution only the cells whose interiors lie entirely in the free space are used to construct the connectivity graph
- Efficient representation, [adapted to the complexity of the environment](#)
  - sparse environments contain fewer cells thus consuming less memory



# Search algorithms

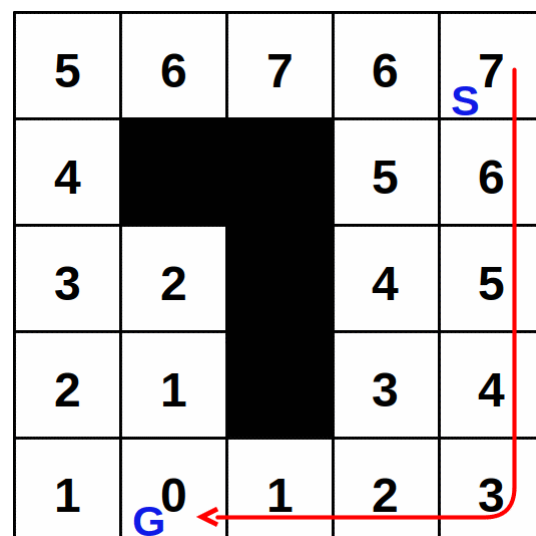
## Methods

- Once a graph is obtained, finding the shortest path between start node and goal node can be done using [graph search algorithms](#)
- Many graph search algorithms require visiting each node in the graph to determine the shortest path
  - Computationally tractable for sparsely connected graphs
  - Computationally expensive for highly connected graphs (e.g., regular grid)
- Covered methods:
  - [Wavefront expansion](#)
  - [Dijkstra's algorithm](#)
  - [A\\* algorithm](#)

# Search algorithms

## Wavefront expansion

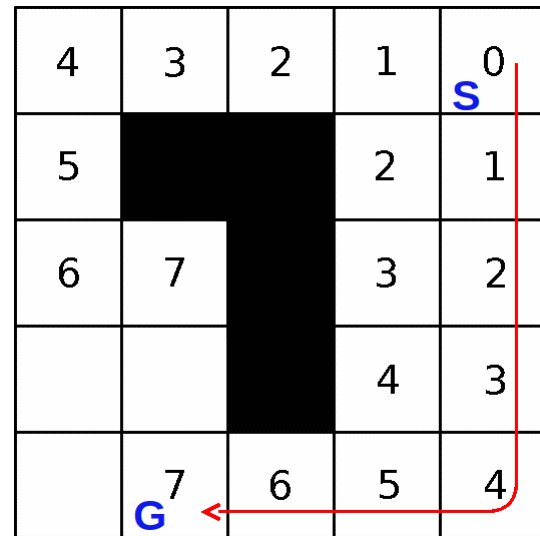
- Wavefront expansion (aka NF1 or grassfire), useful to find paths in fixed-size cell arrays
- Starting at the goal, [mark in each adjacent cell its distance to the goal](#) (here using Manhattan distance)
- This process continues until the cell corresponding to the [start position is reached](#)
- The planner calculate a path to reach the goal by [linking together cells that are adjacent and closer to the goal](#)



# Search algorithms

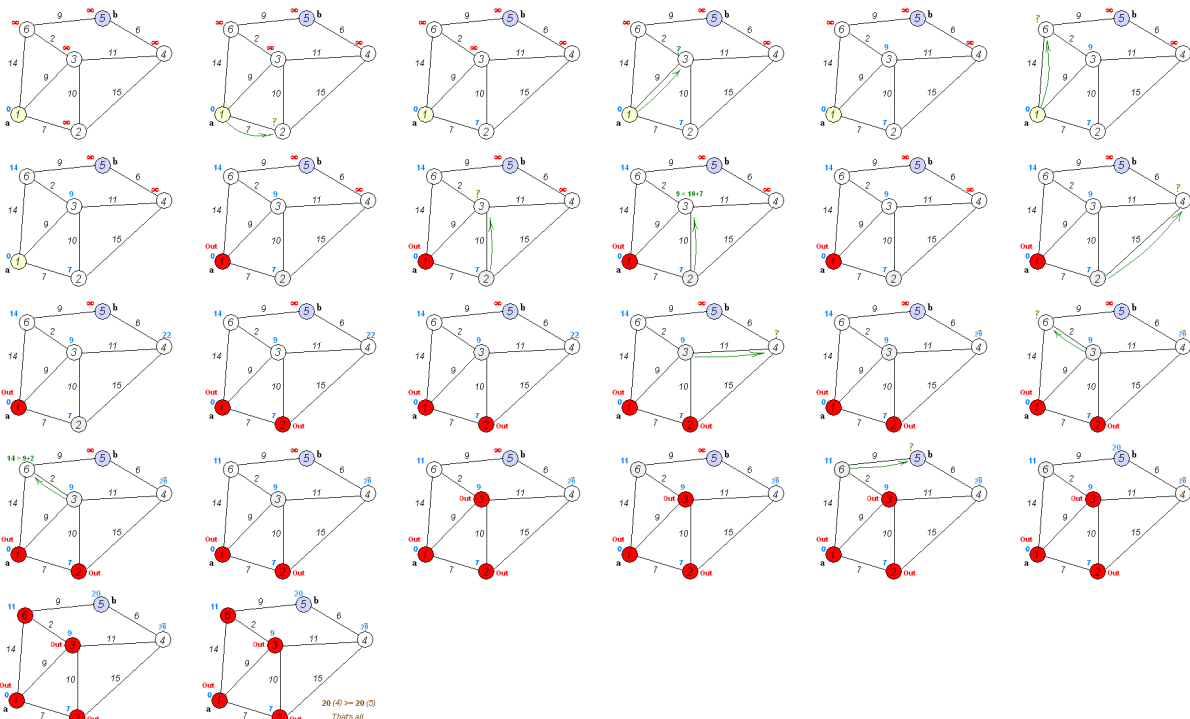
## Dijkstra's algorithm – cell environment

- Beginning at the start node, the algorithm marks all adjacent neighbors with the **cost to get there**
- It then **proceeds to the node with the lowest cost** marking all of its adjacent nodes with the lowest cost to reach them
- Once all adjacent neighbors of a node have been marked, the algorithm **proceeds to the node with the next lowest cost not visited yet**
- Once the algorithm visits the goal node, it terminates
- The **path to goal** may be obtained starting from the goal node and following the **edges pointing towards the lowest node cost**



# Search algorithms

## Dijkstra's algorithm – graph example



Taken from [https://en.wikipedia.org/wiki/Dijkstra's\\_algorithm](https://en.wikipedia.org/wiki/Dijkstra's_algorithm)

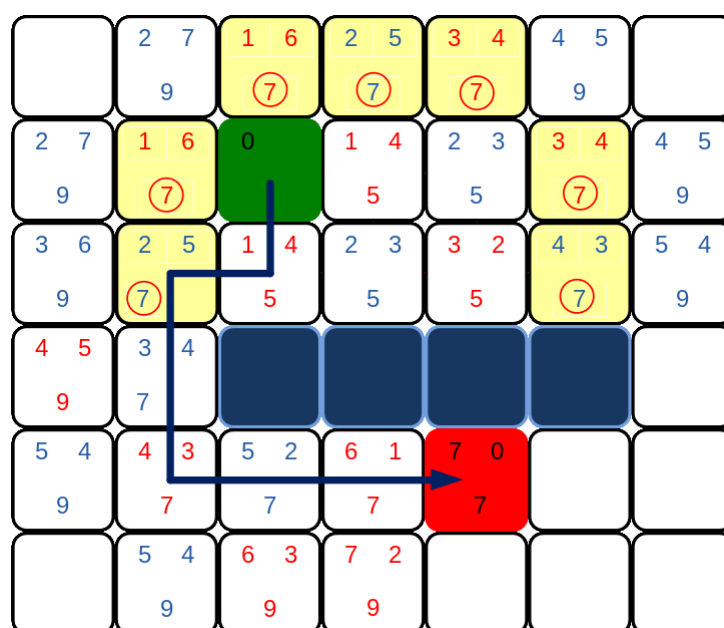
# Search algorithms

## A\* search algorithm

- The idea is to use a **cost function to rank** the choices, choose the best one first, and try it
- Cost function:
  - $f^*(n) = g(n) + h^*(n)$  – ('\*' means they are estimates)
  - where:
    - $g(n)$  is the cost of going from the start to node  $n$
    - $h^*(n)$  is an estimated cost of going from node  $n$  to the goal
- $h^*$  is a “heuristic function” – (a way of **guessing** the cost of going from node  $n$  to **goal**)
  - the robot can't “see” the path between node  $n$  and the goal
  - $h^*(n)$  should never be greater than  $h(n)$ :  $h^*(n) \leq h(n)$
  - Must always underestimate remaining cost to reach goal
  - The Euclidian (straight line) distance is often a good choice

# Search algorithms

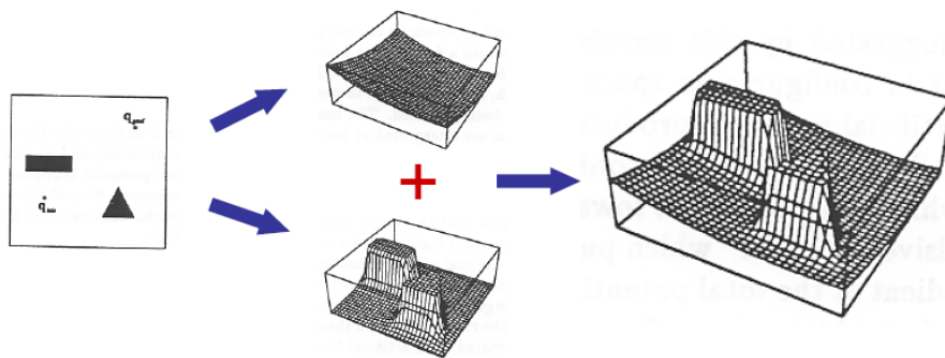
## A\* search algorithm (2)



# Potential field path planning

## Main idea

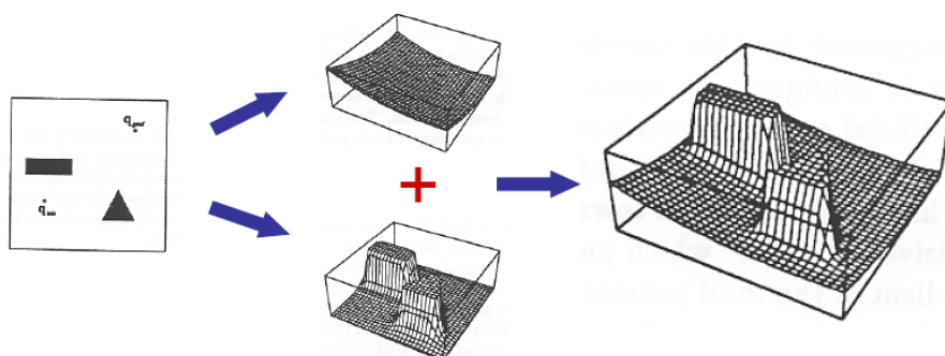
- Think the robot as a **particle in a potential field**
- Define a potential function over the free space that has a **global minimum at the goal**
- Define high potentials for the obstacles
- The robot follow the steepest descent of the potential function



# Potential field path planning

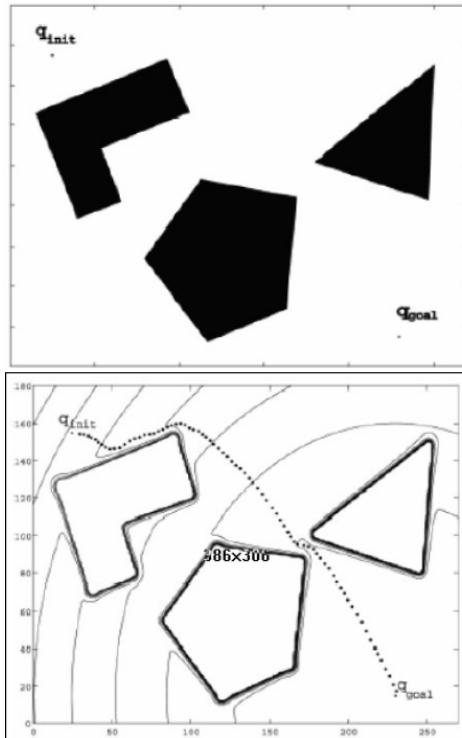
## Rolling down the hill

- The **goal** location generates an **attractive potential**, pulling the robot towards the goal
- The **obstacles** generate a **repulsive potential**, pushing the robot far away from the obstacles
- The negative gradient of the total potential is treated as an artificial force applied to the robot
- Generated robot movement is similar to a ball rolling down the hill

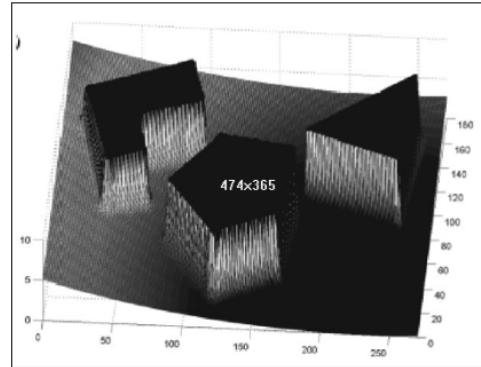


# Potential field path planning

## Problems



- Often leads to oscillating motion
- Trapped in local minima in the potential field
- Parameter tuning problems



# Navigation

## Issues in navigation

- Where am I?
  - localization
- Where have I been?
  - mapping
- Where should I going?
  - decision
- What's the best way to get there?
  - Path planning
- **How do I get there?**
  - Path following and **obstacle avoidance** (Motion)



# Obstacle avoidance

## Purpose

- In general, the environment is **not fully modeled**
    - Some obstacles (chairs, for example) may not be represented
  - The environment might also **change dynamically**
    - for example, people moving around
  - In such cases, to navigate, the robot may need to modify the planned path
    - **reacting, re-planning**
- 
- The purpose of the obstacle avoidance algorithms is to avoid collisions with obstacles, while pursuing the goal/plan
  - Obstacle avoidance relies on
    - Information about the goal (position, plan)
    - current pose (on the map)
    - Recent sensory information (a local map)

# Obstacle avoidance

## Methods

- Efficient obstacle avoidance should be optimal with respect to
    - The overall goal
    - The actual speed and kinematics of the robot
    - The on-board sensors
    - The current and future risk of collision
- 
- Covered methods:
    - **Bug1**
    - **Bug2**
    - **Vector field histogram**

# Obstacle avoidance

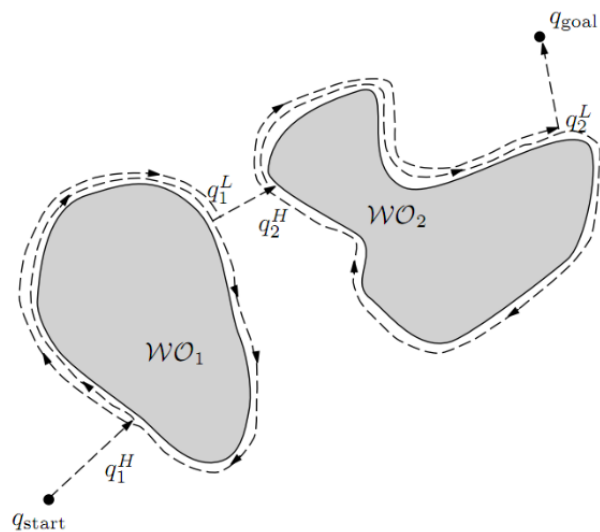
## Bug1 algorithm

- **Algorithm:**

- Go in direction to the goal until reach it or hit an obstacle
- If goal reached, finish
- Do a full tour around the obstacle, storing the closest point to the goal
- Go to that point
- Repeat

- **Comment:**

- Inefficient but does the job



# Obstacle avoidance

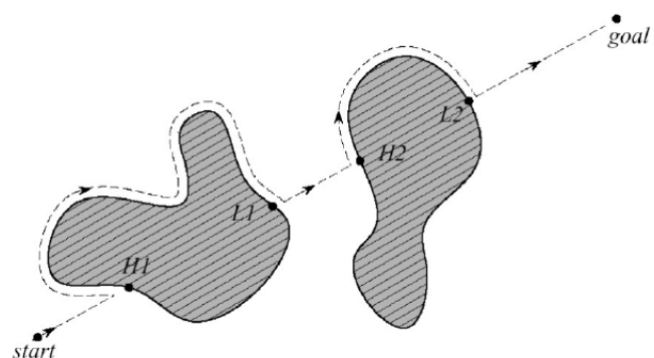
## Bug2 algorithm

- **Algorithm:**

- Go in direction to the goal until reach it or hit an obstacle
- If goal reached, finish
- Contour the obstacle, from left or right, until reach the line between start and goal
- Repeat, keeping the same side (left or right) as before

- **Comment:**

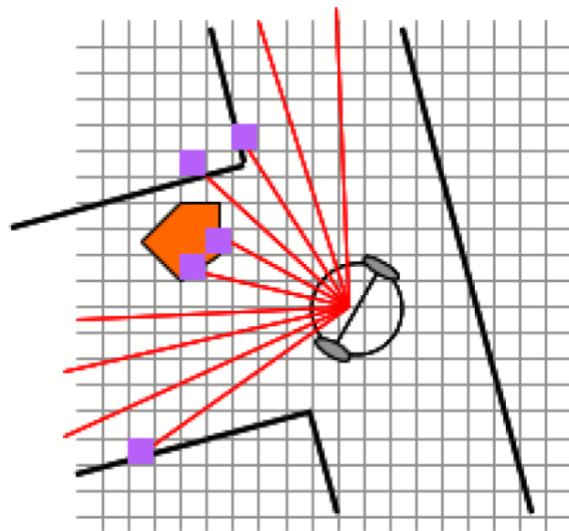
- More efficient but can fail



# Obstacle avoidance

## Vector field histogram (VFH)

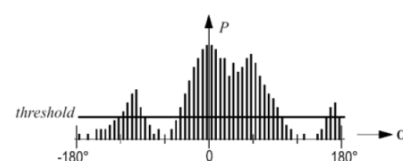
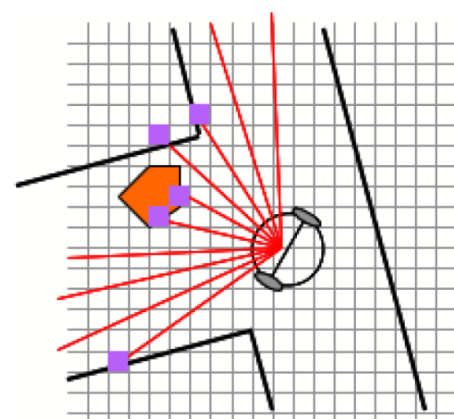
- Creates a **local map of the environment around the robot**
- Environment is represented as an **occupancy grid** (2D Cartesian grid called the **histogram grid**)
- Each **grid cell (i, j)** value holds the **confidence** that there is an **obstacle** at that location
- The grid is updated by relatively recent sensor data



# Obstacle avoidance

## Vector field histogram (VFH) – 2

- Information in the histogram grid is converted to a simpler representation, called the **polar histogram**
- The **polar histogram** retains the statistical information but reduces the amount of data that needs to be handled in real-time
- A **threshold** transforms the polar histogram in a **binary diagram** with passable regions
- A sector with low obstacle density (below threshold) is a candidate to travel away from obstacle
- The one chosen depends on the target point



## Bibliography

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- “Principles of Robot Motion: Theory, Algorithms, and Implementations”, Howie Choset et al., MIT Press, Boston, 2005
- “Artificial Intelligence: A Modern Approach”, 3rd edition, Russel and Norvig, Pearson, 2009
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- “The Vector Field Histogram - Fast Obstacle Avoidance for Mobile Robots”, J. Borenstein and Y. Koren
- “VFH+: Reliable Obstacle Avoidance for Fast Mobile Robots”, I. Ulrich and J. Borenstein