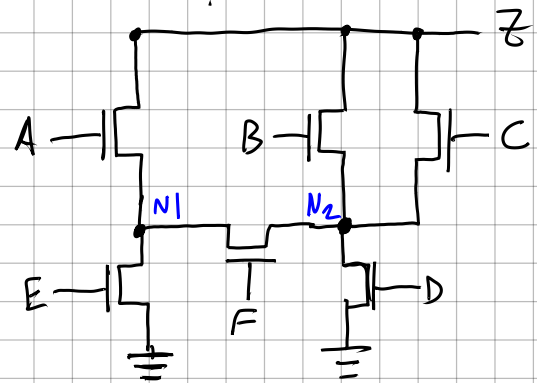
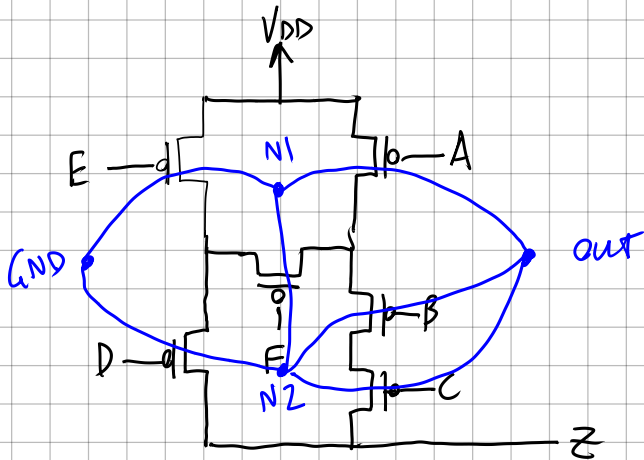
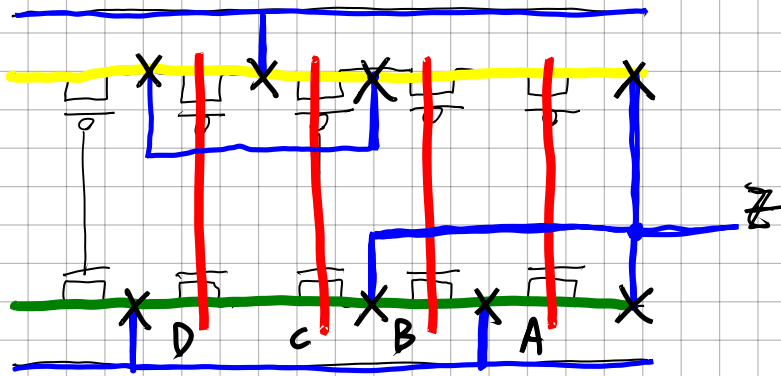


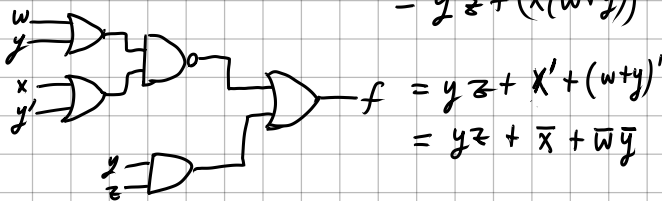
①



②

$$f(w, x, y, z) = (yz)' \cdot ((w+y)' + (x+y'))'$$

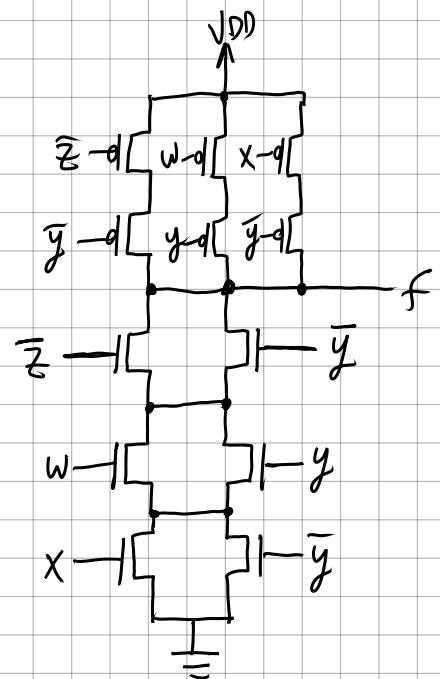
$$f = yz + ((w+y)(x+y'))' = yz + (wx + xy)' = yz + (x(w+y))'$$



$$\begin{aligned} (w+y)x + (w+y)y' \\ wx + xy + w \\ w(x+1) + xy \end{aligned}$$

$$\begin{aligned} f_n &= (zy)' \cdot ((w+y)' + (x+y'))' \\ &= (zy)' \cdot (\overline{w}y + \overline{x}y)' \\ &= (zy)' \cdot (\overline{w}y)' \cdot (\overline{x}y)' \\ &= (\overline{z} + \overline{y}) \cdot (w+y) \cdot (x+y) \end{aligned}$$

$$f_p = \overline{z}\overline{y} + wy + xy$$



③

A	B	X	Y
0	0	0	1
1	0	1	0
0	1	1	0
1	1	0	1

$$X = A \oplus B$$

$$Y = \overline{A \oplus B}$$

④

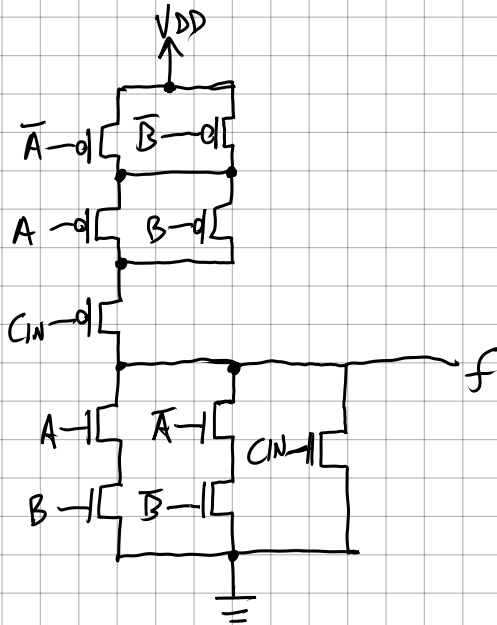
$$f(A, B, C_{IN}) = (\overline{A \oplus B}) \cdot C_{IN} = (AB + \bar{A} \cdot \bar{B}) C_{IN}$$

$$= (AB + (A+B)') C_{IN}$$

$$f_n = \overline{(A \oplus B) \cdot C_{IN}} = A \oplus B + \bar{C}_{IN}$$

$$f_n = AB + \bar{A} \bar{B} + C_{IN}$$

$$f_p = (A+B)(\bar{A} + \bar{B})(C_{IN})$$



⑤

$$1) ab + bdc + ca'$$

no further simplification

$$2) (x+y)(x+z)$$

$$(x+y)x + (x+y)z$$

$$yx + xz + yz$$

$$y(1+z) + xz$$

$$yz + xz$$

$$z(y+x)$$

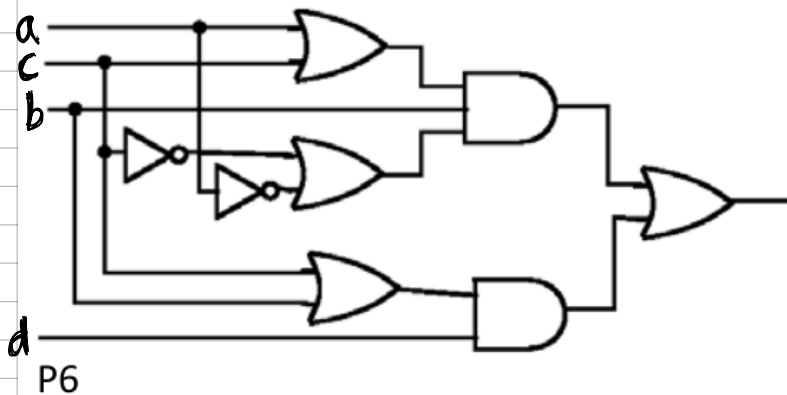
$$3) a(b+c+d) + b(c+d+a) + c(d+a+b) + d(a+b+c)$$

$$ab + ac + ad + bc + bd + ba + cd + ca + cb + da + db + dc$$

$$ab + ac + ad + bc + bd + cd$$

$$a(b+c+d) + b(c+d) + cd$$

⑥



$$((w+x) \cdot y \cdot (w'+x')) + (z(x+y))$$

$$((wy+xy) \cdot (w'+x')) + (zx+yz)$$

$$(w'(wy+xy) + x'(wy+xy)) + xz + yz$$

$$w'xy + x'wy + xz + yz$$

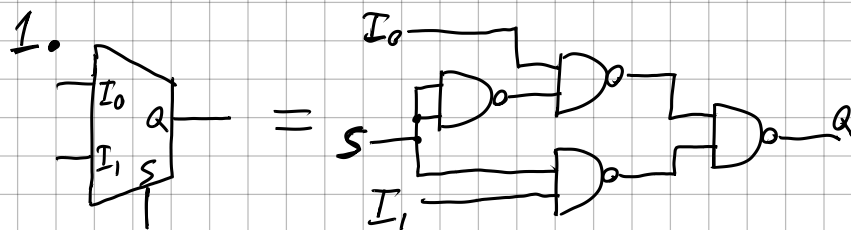
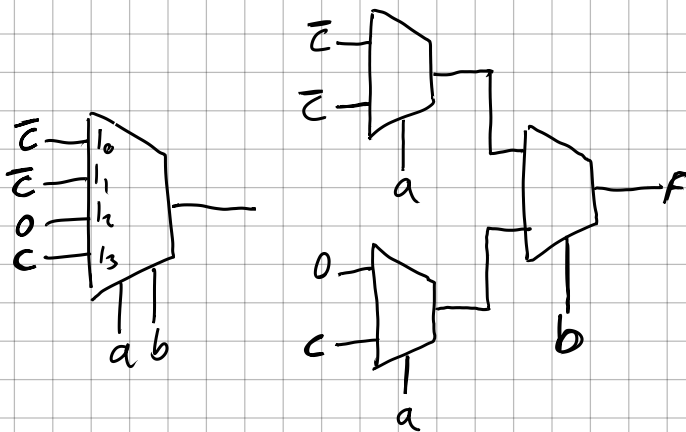
$$y(w'x + x'w) + xz + yz$$

$$db + db'c + abc' + a'bc$$

$$db'c + db + b(ac' + a'c)$$

⑦

a	b	c	F
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1



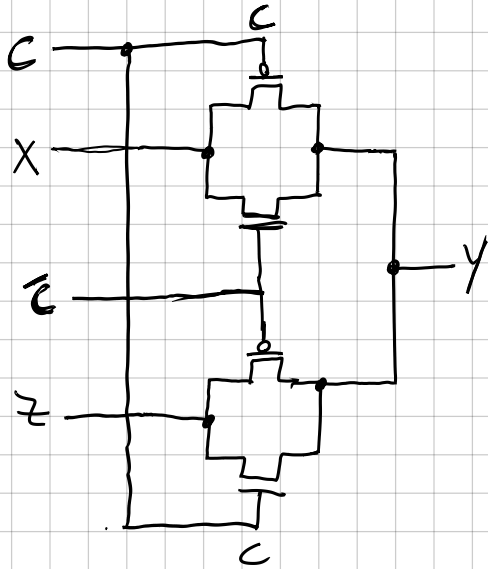
2. 16 transistors per 2-to-1 mux.

48 transistors total.

3. 4 per mux

16 transistors total.

⑧



2-to-1 mux

