

(a) Prove that $T(n) = 3n^3 + 4n + 8 \in \Omega(n)$

(i) $3n^3 + 4n + 8 \geq Cn \quad \forall n \geq n_0$ //Find C and n_0

(ii) $3(1)^3 + 4(1) + 8 \geq C(1) \quad \forall n \geq 1$

(iii) $15 \geq 15$

(iv) $\Rightarrow C=15$ and $n_0=1$

(b) $O(n^2)$ is not a tight upper bound for $T(n)$. The tight upper bound for $T(n)$ is $O(n^3)$

(c) $T(n)$ is NOT $\in \Theta(n^4)$.