

# MQE: Economic Inference from Data:

## Module 2: Fixed Effects

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## Module 2: Fixed Effects

- ▶ Data Structures

- ▶ Fixed Effects

- A simulation

- Fixed effects as demeaned data

- Thinking about variation

- Example: Crime and Unemployment

## Controlling for unobservables

We saw with AGG(2006) that even with many covariates, unobservables are a problem.

Certain types of data allow us to control for more of these unobservables by using fixed effects.

## Example:

$$Income_i = \beta_0 + \beta_1 Schooling_i + \epsilon$$

$\beta_1$  cannot be interpreted as causal: big OVB problems, even with lots of control variables. Unlikely to have good measures of 'ability', 'enthusiasm', 'grit'...

What if I can control for unchanging individual characteristics?

## Data Structures: Cross-Section

Individual	Income	Schooling	Female
1	22000	12	1
2	57000	16	1
...	...	...	...
N	15000	12	0

Each individual is observed once.

## Data Structures: Panel Data

Individual	Income	Schooling	Female	Year
1	22000	12	1	2001
1	23000	12	1	2002
2	57000	16	1	2001
2	63000	17	1	2002
...	...	...	...	...
N	15000	12	0	2001
N	13000	12	0	2002

Each individual is observed multiple times.

## Data Structures: Panel Data Subscripts

Unique observations must be identified by both the individual and time dimensions. . . notice the new subscripts:

$$Income_{it} = \beta_0 + \beta_1 Schooling_{it} + \epsilon.$$

# Data Structures: Panel Data

Panel Data can be

- balanced**: same number of observations for each unit
- unbalanced**: some units are observed more often than others (probably good to look into why)



## Review: Indicator (Dummy) Variables

If I have multiple Female observation and multiple non-female observations I can control for the effect of being female on wages:

$$Income_{it} = \beta_0 + \beta_1 Schooling_{it} + \beta_2 Female_i + \epsilon.$$

## Fixed Effects as Individual Indicator Variables

Indiv	Income	School	Female	Year	Indiv1	Indiv2	...	IndivN
1	22000	12	1	2007	1	0	0	0
1	23000	12	1	2008	1	0	0	0
2	57000	16	1	2007	0	1	0	0
2	63000	17	1	2008	0	1	0	0
...	...	...	...	...	...	...	...	...
N	15000	12	0	2007	0	0	0	1
N	13000	12	0	2008	0	0	0	1

# Fixed Effects as Individual Indicator Variables

I can estimate:

$$Inc_{it} = \beta_0 + \beta_1 School_{it} + \beta_2 Fem_i + \beta_{a1} Ind1_i + \beta_{a2} Ind2_i + \dots + \beta_{aN-1} Ind(N-1)_i + \epsilon.$$

What do the  $\beta_{ak}$  coefficients tell me?

Also:

- Why do the  $IndN$  indicators only have an  $i$  subscript?
- What is the implied assumption if  $Fem$  only has an  $i$  subscript?
- Why are there only  $(N-1)$  individual dummies?

# Fixed Effects as Individual Indicator Variables

## What will these individual controls control for?

- $\beta_{a1}$  will control for the effect of being individual 1 on income that is not explained by that person's gender or schooling.
- Any **time invariant** characteristic that affects individual 1's income, such as ability, grit, enthusiasm... will be controlled for by adding this individual dummy variable.
- These controls are known as individual **fixed effects**.

## For notational convenience:

$$Income_{it} = \beta_0 + \beta_1 Schooling_{it} + \beta_2 Female_i + \gamma_i + \epsilon.$$

# Fixed Effects

**With my panel data, what else can I control for?**

$$Income_{it} = \beta_0 + \beta_1 Schooling_{it} + \beta_2 Female_i + \gamma_i + \tau_t + \epsilon.$$

-What is  $\tau_t$ ?

-What is this estimation equivalent to?