

# Marriage and Divorce Dynamics in Denmark

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2023

# Plan for today

- Bruze, Svarer and Weiss (2015): "The Dynamics of Marriage and Divorce"
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Danish data for cohorts 1960 (men), 1962 (women).

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- **Reading guide:**
  1. What are the main *research questions*?
  2. What is the (*empirical*) *motivation*?
  3. What are the central *mechanisms in the model*?
  4. What is the *simplest model* in which we could capture these?

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Danish data for cohorts 1960 (men), 1962 (women).
- **Reading guide:**
  1. What are the main *research questions*?
    - How does marriage and divorce behavior vary across age and educational groups?
    - How does educational differences influence intra-household inequality?
  2. What is the (*empirical*) *motivation*?
  3. What are the central *mechanisms in the model*?
  4. What is the *simplest model* in which we could capture these?

# Empirical Motivation: I

## ● Marriage and divorce

Age of female cohort = age of male cohort-2



FIG. 1.—Fraction married or in partnerships (marriage plus cohabitation) by age. A color version of this figure is available online.

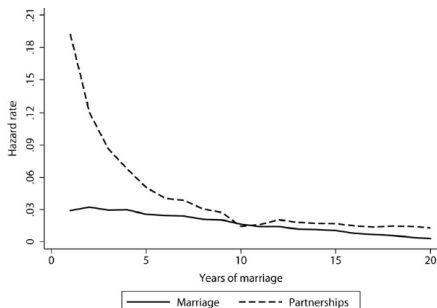


FIG. 3.—Divorce hazard for first marriage or partnership (marriage plus cohabitation). A color version of this figure is available online.

# Empirical Motivation: II

- **Highly educated** people partner later but more “stable”.  
Especially if both highly educated

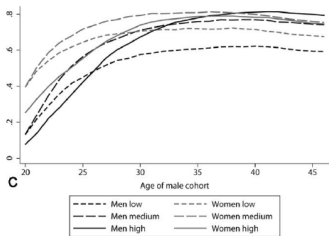


FIG. 4.—*A*, Fraction married men and women by age and education; *B*, fraction cohabiting men and women by age and education; *C*, fraction men and women in partnerships by age and education. A color version of this figure is available online.

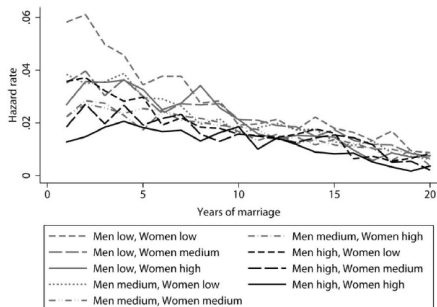


FIG. 6.—Divorce hazards for first marriages by education of the husband and wife. A color version of this figure is available online.

# Empirical Motivation: III

- **Highly educated** people re-marry faster.  
And stay in second marriage longer.



FIG. 7.—Hazard rate into second marriage for men and women by education. A color version of this figure is available online.



FIG. 8.—Divorce hazards when at least one spouse is in second marriage, by education of the husband and wife. A color version of this figure is available online.

# Empirical Motivation: IV

## ● Assortative matching:

people more likely to marry one with same education

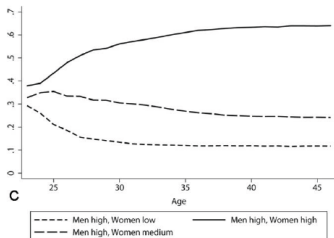


FIG. 9.—Distribution of marriages for men with low (top), medium (middle), or high (bottom) education. A color version of this figure is available online.

$$(a) P(\text{educ}_w | \text{educ}_m = \text{high})$$

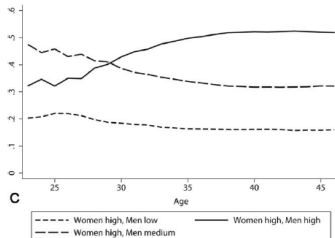


FIG. 10.—Distribution of marriages for women with low (top), medium (middle), or high (bottom) education. A color version of this figure is available online.

$$(b) P(\text{educ}_m | \text{educ}_w = \text{high})$$



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- **From Abstract:**

*Education raises the share of the marital surplus for men but not for women. As men and women get older, husbands receive a larger share of the marital surplus*

# Outline

## 1 Model and Mechanisms

## 2 Estimation

# Model Overview

- **Full commitment:**

Transferable utility

Perfect foresight wrt bargaining power.

Particular timing/expectation assumptions (get back)

- **Choices:**

Marriage: which type  $IJ$

Divorce

- **States:**

$d_t$ : duration of marriage

“TYPES”:

$e \in E = \{l, m, h\}$ : Educational type of both members

$p_t \in P = \{nm, pm\}$ : never/previously married

$u \in U = \{1, 2\}$  (unobserved type)

$\rightarrow I \in E \times P \times U$  (men) and  $J \in E \times P \times U$  (women)

(love-shock,  $\theta_t \sim iid \mathcal{N}(0, 1)$ )

# Bellman Equation: Married

- **Bellman equation** for type  $I$  being single is

$$\underbrace{W_t^{IJ}(d_t)}_{V_t^{m \rightarrow m}} + \underbrace{\theta_t}_{U^{IJ}} = \underbrace{\zeta^{IJ} + \theta_t + R \mathbb{E}_t[\max\{\underbrace{W_{t+1}^{IJ}(d_{t+1}) + \theta_{t+1}}_{V_{t+1}^{m \rightarrow m}}, \underbrace{V_{t+1}^I + V_{t+1}^J - s(d_{t+1})}_{V_{t+1}^{m \rightarrow s}}\}]}_{V_{t+1}^m}$$

where

$\zeta^{IJ}$ : type-specific utility

$R$ : discount factor

$s(d_{t+1})$ : divorce cost

$V_{t+1}^I + V_{t+1}^J$ : sum of value of singlehood (TU)

(I would think that  $d_{t+1} = d_t + 1$ , but they never write)

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- **Probability** of observing divorce,  $P_D(I, J, t, d_t)$ :

$$\Pr(W_t^{IJ}(d_t) < V_t^I + V_t^J - s(d_t)) = \Phi(V_t^I + V_t^J - s(d_t) - W_t^{IJ}(d_t))$$

# Bellman Equation: Single

- **Bellman equation** for type  $I$  man being single is

$$V_t^I = \varphi^I + R\mathbb{E}_t[V_{t+1}^I + \max_{J \in E \times P \times U} \{\varepsilon_{t+1}^0, \gamma_{t+1}^{IJ}[W_{t+1}(\underbrace{1}_{d_{t+1}}) - V_{t+1}^I - V_{t+1}^J] + \varepsilon_{t+1}^J\}]$$

where

$\varepsilon_{t+1}^0$ : EV taste-shock wrt value of singlehood

$\varepsilon_{t+1}^J$ : EV taste-shock wrt value of marriage with type  $J$

$\gamma_{t+1}^{IJ}$ : share of (new) marital surplus to man. Focus in a bit.

$\mathbb{E}_t[\cdot]$  is wrt. Extreme Value taste shocks over type of female match,  $J$ .  
(See discussion on following slides.)

- **Value of marriage next period** is thus the value of being single + the share of the marital surplus he gets.
- **Symmetric** for women with share  $1 - \gamma_{t+1}^{IJ}$ .



# Bellman Equation: Single, Marital Surplus!

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- **Marital surplus** is special:

$$W_{t+1}(1) - V_{t+1}^I - V_{t+1}^J = \mathbb{E}_t[W_{t+1}(1) + \theta_{t+1} - V_{t+1}^I - V_{t+1}^J]$$

since  $\mathbb{E}_t[\theta_{t+1}] = 0$ .

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since  $\mathbb{E}_t[\theta_{t+1}] = 0$ .

- **“Wrong”**: This means that the expected value is inserted in the max, rather than taking the expected value of the max...:

$$\max_{J \in E \times P \times U} \{\varepsilon_{t+1}^0, \gamma_{t+1}^{IJ} \mathbb{E}_t[W_{t+1}(1) + \theta_{t+1} - V_{t+1}^I - V_{t+1}^J] + \varepsilon_{t+1}^J\}$$

VS

$$\mathbb{E}_t[\max_{J \in E \times P \times U} \{\varepsilon_{t+1}^0, \gamma_{t+1}^{IJ} [W_{t+1}(1) + \theta_{t+1} - V_{t+1}^I - V_{t+1}^J] + \varepsilon_{t+1}^J\}]$$

# Bellman Equation: Single, Marital Surplus!

- **Their formulation removes a numerical integral wrt.  $\theta_{t+1}$**
- The expectation in

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- **Known in closed-form:** The log-sum!

$$\mathbb{E}_t[V_{t+1}^I + \max_{J \in E \times P \times U} \{\varepsilon_{t+1}^0, \gamma_{t+1}^{IJ}[W_{t+1}(1) - V_{t+1}^I - V_{t+1}^J] + \varepsilon_{t+1}^J\}]$$

=

$$\log\{\exp(V_{t+1}^I) + \sum_{J \in E \times P \times U} \exp(V_{t+1}^I + \gamma_{t+1}^{IJ}[W_{t+1}(1) - V_{t+1}^I - V_{t+1}^J])\}$$

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- **Probability** of entering marriage with type  $j$ , ( $j = 0 \rightarrow \text{single}$ )

$$P_M^I(j, t) = \frac{\exp(V_t^I + \gamma_t^{Ij}[W_t(1) - V_t^I - V_t^j])}{\exp(V_t^I) + \sum_{J \in E \times P \times U} \exp(V_t^I + \gamma_t^{IJ}[W_t(1) - V_t^I - V_t^J])}$$

# Commitment

- **Full commitment:**

$$\gamma_t^U$$

is known, and fixed throughout.

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$$\gamma_t^{IJ}$$

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- **Assume** the functional form

$$\gamma_t^{IJ} = \frac{\exp\{\rho^{IJ} + \kappa^{IJ}t + \lambda^{IJ}t^2\}}{1 + \exp\{\rho^{IJ} + \kappa^{IJ}t + \lambda^{IJ}t^2\}}$$

which has 108 estimated parameters.  
(not reported)

# Outline

1 Model and Mechanisms

2 Estimation



# Remaining Parameters

- **Cost of divorce** “non-parametric” (10)

$$s(d_t) = \sum_{k=1}^9 \beta_k \mathbf{1}(d_t = k) + \beta_{10} \mathbf{1}(d_t \geq 10)$$

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- **Utility** for singles are  $u \in \{1, 2\}$

$$\varphi_t^I = \mu_t^I + \eta_u^I$$

$$\varphi_t^J = \mu_t^J + \eta_u^J$$

and estimated parameters are

$\zeta^{IJ}$  :13 (education mix (9) or marital order mix (4))

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- **Unobserved types** (4):

estimate  $u_2^I, u_2^J$  (relative to type 1) and the share of type 2.

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Dynamic logit due to EV taste-shocks wrt discrete types.

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- Let  $S_{i,0}$  and  $S_{j,0}$  be initial states. These states are taken as given.

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- The (conditional) likelihood function of the observed data is

$$L = \prod_{i=1}^{N^m} \Pr(O_i | S_{i,0}) \times \prod_{j=1}^{N^f} \Pr(O_j | S_{j,0})$$

assuming independence.

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assuming independence.

- The EV assumption makes  $\Pr(\bullet)$  conditional multinomial logit (MNL)  
Can be found in closed form.

# Estimation

- **Likelihood of *sequence*** of choices given  $S_{i,0}$ ,  $u_i$

$$\Pr(O_i | S_{i,0}, u_i) = \prod_{t=2}^T \Pr(O_{i,t} | O_{i,t-1}, u_i) \Pr(O_{i,1} | S_{i,0}, u_i)$$



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- **Do not observe  $u$**  we “integrate that out”:

$$\begin{aligned} \Pr(O_i | S_{i,0}) &= \mathbb{E}[\Pr(O_i | S_{i,0}, u_i)] \\ &= q^m \Pr(O_i | S_{i,0}, u_i = 1) + (1 - q^m) \Pr(O_i | S_{i,0}, u_i = 2) \end{aligned}$$

where  $q^m$  and  $q^f$  are the shares of type 1 ( $u = 1$ )

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where  $q^m$  and  $q^f$  are the shares of type 1 ( $u = 1$ )

- **The likelihood** of observing the outcomes is then

$$\begin{aligned} L &= \prod_{i=1}^{N^m} [q^m \Pr(O_i | S_{i,0}, u_i = 1) + (1 - q^m) \Pr(O_i | S_{i,0}, u_i = 2)] \\ &\quad \times \prod_{j=1}^{N^f} [q^f \Pr(O_j | S_{j,0}, u_j = 1) + (1 - q^f) \Pr(O_j | S_{j,0}, u_j = 1)] \end{aligned}$$

# Identification (idea)

- **Identification** arguments in paper  
Only without unobserved types
  
- **Talk about some here**  
To give idea of arguments  
Ignores unobserved types,  $u \in \{1, 2\}$

# Identification: Weights

- **From probability of marriage** of  $I$  with  $J$  relative to remaining single

$$\log \left( \frac{P_M^I(J, t)}{P_M^I(0, t)} \right) = \gamma_t^{IJ} [W_t^{IJ}(1) - V_t^I - V_t^J]$$

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- similarly for women marrying type  $I$ :

$$\log \left( \frac{P_M^J(I, t)}{P_M^J(0, t)} \right) = (1 - \gamma_t^{IJ}) [W_t^{IJ}(1) - V_t^I - V_t^J]$$

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- such that taking ratios **identifies weights**,

$$\frac{\gamma_t^{IJ}}{1 - \gamma_t^{IJ}} = \underbrace{\log \left( \frac{P_M^I(J, t)}{P_M^I(0, t)} \right) / \log \left( \frac{P_M^J(I, t)}{P_M^J(0, t)} \right)}_{\text{data}}$$

# Identification: Divorce costs

- From probability of divorce:

$$V_t^I + V_t^J - s(d_t) - \underbrace{W_t^{IJ}(d_t)}_{\text{data}} = \underbrace{\Phi^{-1}(P_D(I, J, t, d_t))}_{\text{data}}$$

We can then insert to get  $s(1)$

$$\begin{aligned} \log \left( \frac{P_M^I(J, t)}{P_M^I(0, t)} \right) &= \gamma_t^{IJ} [W_t^{IJ}(1) - V_t^I - V_t^J] \\ &= \gamma_t^{IJ} [s(1) - \Phi^{-1}(P_D(I, J, t, 1))] \\ &\quad \Updownarrow \\ s(1) &= \underbrace{\log \left( \frac{P_M^I(J, t)}{P_M^I(0, t)} \right)}_{\text{data}} / \underbrace{\gamma_t^{IJ}}_{\text{"known"}} + \underbrace{\Phi^{-1}(P_D(I, J, t, d_t))}_{\text{data}} \end{aligned}$$

- Remaining  $s(d)$ : Noting that  $W_t^{IJ}(d_t)$  depends on  $d_t$  through  $s(d)$  and  $\underbrace{\Phi^{-1}(P_D(I, J, t, d_t)) - \Phi^{-1}(P_D(I, J, t, d'_t))}_{\text{data}} = s(d'_t) - s(d_t) + W_t^{IJ}(d'_t) - W_t^{IJ}(d_t)$

# Identification: Utility Flow

- **Assume** that flow-utility in couple are constant
- **“Normalize”** value of singlehood for men over age 40 to zero (but more than normalization since several periods,  $T = 71$ ?)
- **“Normalize”** value of singlehood for women over age 38 to zero (but more than normalization since several periods,  $T = 71$ ?)



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- **Couples:** For  $t > 39$ :

$$V_t^I + V_t^J - s(d_t) - W_t^{IJ}(d_t) = s(d_t) - W_t^{IJ}(d_t)$$

and thus gets  $\zeta^{IJ}$ :

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- **Singles:** time-differences in likelihood gives  $\varphi_t^I$  and  $\varphi_t^J$ .

## Results: Marriage Order

- **Estimates** suggest that second marriages are less “costly” for men

**Table 3**  
**Effects of Marriage Order on the Marital Output Flow**

	Wife's First Marriage	Wife's Second Marriage
Husband's first marriage	.5166	.3891
Husband's second marriage	.4709	.5364

## Results: Divorce Costs

- **Estimates** suggest that divorce costs are U-shaped  
Authors are surprised, but this could still be due to children.

**Table 4**  
**Costs of Divorce by Duration of Marriage**

Marital Duration	Cost of Divorce
1 year	14.3
2 years	14.1
3 years	12.4
4 years	11.5
5 years	11.6
6 years	11.6
7 years	11.5
8 years	12.7
9 years	12.7

## Results: Marital Surplus Shares

- Do not want to look at  $\gamma_t^{IJ}$  due to selection.

# Results: Marital Surplus Shares

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- Adjusted shares:** wants to add the Extreme Value taste shock and states

$$\mathbb{E}_t[V'_{t+1} + \varepsilon_{t+1}^0] = V'_{t+1}$$

is the *expected value of being forced to remain single*.

But I don't think that is correct... The mean of the taste shock is

$\mathbb{E}_t[\varepsilon_{t+1}^0] \approx 0.5772$  (the Euler–Mascheroni constant)

# Results: Marital Surplus Shares

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$$\mathbb{E}_t[V_{t+1}^I + \varepsilon_{t+1}^0] = V_{t+1}^I$$

is the *expected value of being forced to remain single*.

But I don't think that is correct... The mean of the taste shock is  $\mathbb{E}_t[\varepsilon_{t+1}^0] \approx 0.5772$  (the Euler–Mascheroni constant)

- If allowed on the marriage market**, the expected value is (log-sum):

$$C_{t+1}^I = \mathbb{E}_t[V_{t+1}^I + \max_{J \in E \times P \times U} \{\varepsilon_{t+1}^0, \gamma_{t+1}^{IJ}[W_{t+1}(1) - V_{t+1}^I - V_{t+1}^J] + \varepsilon_{t+1}^J\}]$$

- Expected gains** from entering the marriage market:

$$S_t^I = C_{t+1}^I - \mathbb{E}_t[V_{t+1}^I + \varepsilon_{t+1}^0]$$

and *similarly for women*.

## Results: Marital Surplus Shares

- They define the total share of surplus of the husband be

$$\Gamma_t^{IJ} = \frac{S_t^I}{S_t^I + S_t^J}$$

**Table 9**  
**Estimated Average Total Surplus Share  $\Gamma$  for Husband**  
**by Education of Husband and Wife**

Husband's Education	Wife's Education		
	Low	Medium	High
Low	.417	.387	.402
Medium	.496	.463	.490
High	.530	.493	.498



# Results: Marital Surplus Shares

**Table 11**

**Estimated Average Total Surplus Share  $\Gamma$  for Husband by Marital History of Husband and Wife**

	Wife's First Marriage	Wife's Second Marriage
Husband's first marriage	.464	.353
Husband's second marriage	.563	.455

**Table 12**

**Estimated Average Total Surplus Share  $\Gamma$  for Husband by Age of Husband**

Age of Husband	Share of Gains to Marriage
25	.425
30	.465
35	.486
40	.505
45	.541

# Next Time

- **Next time:**

Fertility and Labor Supply.

- **Literature:**

Jakobsen, Jørgensen and Low (2022): "Fertility and Family Labor Supply"  
[unitary]

- **Read** before lecture

- **Reading guide:**

Section 1: Introduction + overview. Read.

Section 2: Data. Skim.

Section 3: Empirical Motivation. Get the idea.

Section 4: Model. Key, get the idea.

Section 5: Calibrated parameters. skim fast.

Section 6: Estimation. Skim/read.

Section 7: Simulation Results. Key. Read.

Section 8: Sensitivity Analysis. Skim/skip.

# References I

BRUZE, G., M. SVARER AND Y. WEISS (2015): “The Dynamics of Marriage and Divorce,” *Journal of Labor Economics*, 33(1), 123–170.

JAKOBSEN, K., T. H. JØRGENSEN AND H. LOW (2022): “Fertility and Family Labor Supply,” Working paper, Centre for Economic Behavior and Inequality.