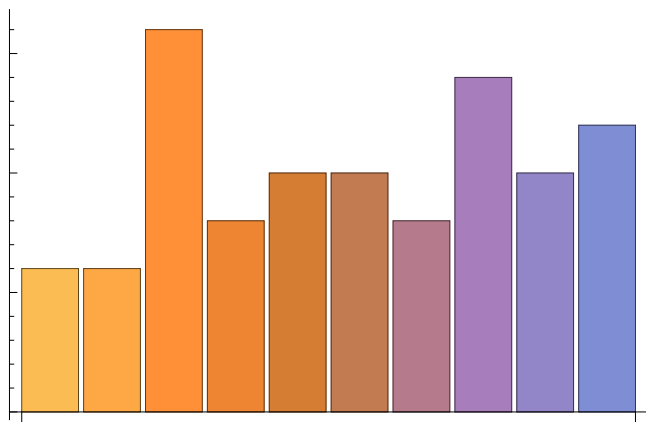


```
(* Simulate equipartition for the number e at levels 1 and 2 *)

(* Decimal expansion of e, small, level 1 *)
e = RealDigits[E, 10, 50]; (* number, base, length of digits *)
smallE = e[[1]];
f[n_] := N[ $\sum_{k=1}^{\text{Length}[\text{smallE}]} \text{If}[\{\text{smallE}[[k]]\} == \{n\}, 1, 0] / (\text{Length}[\text{smallE}])]$ 
equipartition = {};
For[i = 0, i < 10, i++, AppendTo[equipartition, f[i]]];
equipartition
{0.06, 0.06, 0.16, 0.08, 0.1, 0.1, 0.08, 0.14, 0.1, 0.12}

BarChart[equipartition]
```

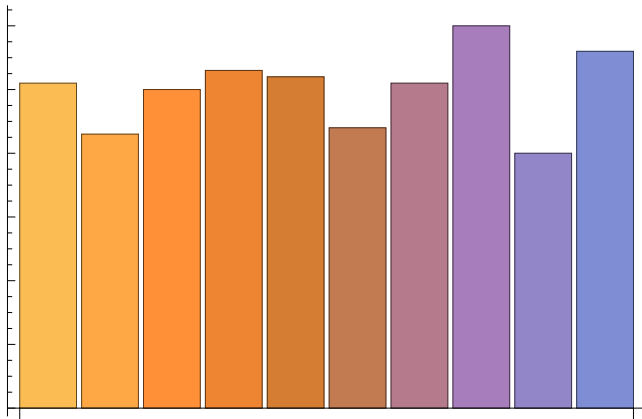


```
(* Decimal expansion of e, medium, level 1 *)
e = RealDigits[E, 10, 500];
mediumE = e[[1]];
f[n_] := N[ $\sum_{k=1}^{\text{Length}[\text{mediumE}]} \text{If}[\{\text{mediumE}[[k]]\} == \{n\}, 1, 0] / (\text{Length}[\text{mediumE}])]$ 
equipartitionMedium = {}
For[i = 0, i < 10, i++, AppendTo[equipartitionMedium, f[i]]];
equipartitionMedium

{}

{0.102, 0.086, 0.1, 0.106, 0.104, 0.088, 0.102, 0.12, 0.08, 0.112}
```

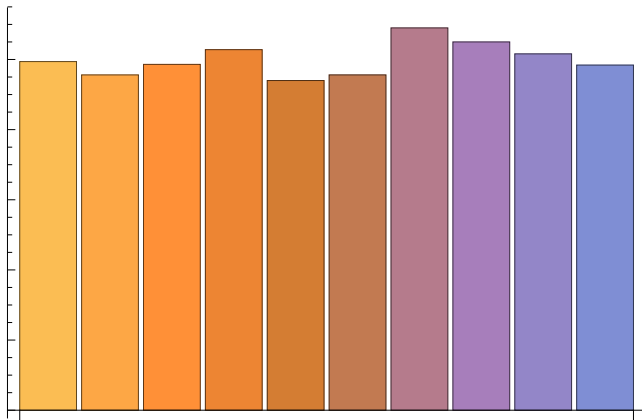
BarChart[{equipartitionMedium}]



```
(* Decimal expansion of e, large, level 1*)
e = RealDigits[E, 10, 5000];
largeE = e[[1]];
f[n_] := N[ $\sum_{k=1}^{\text{Length}[\text{largeE}]} \text{If}[\{\text{largeE}[[k]]\} = \{n\}, 1, 0] / (\text{Length}[\text{largeE}])]$ 
equipartitionLarge = {}
For[i = 0, i < 10, i++, AppendTo[equipartitionLarge, f[i]]];
equipartitionLarge
{}
```

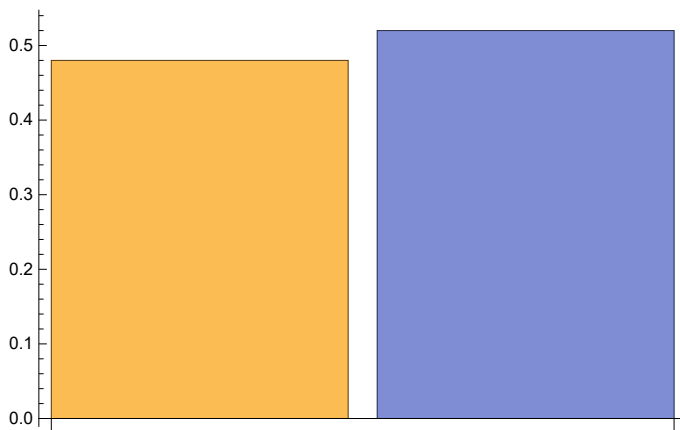
{0.0994, 0.0956, 0.0986, 0.1028, 0.094, 0.0956, 0.109, 0.105, 0.1016, 0.0984}

BarChart[{equipartitionLarge}]



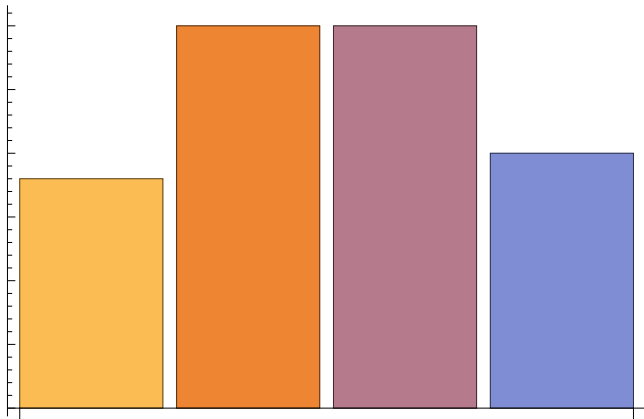
```
(* Binary expansion of the number e, small, level 1 *)
e = RealDigits[E, 2, 50];
smallE = e[[1]];
equipartitionSmall = {}
f[n_] := N[ $\sum_{k=1}^{\text{Length}[smallE]} \text{If}[\{smallE[[k]]\} == \{n\}, 1, 0] / (\text{Length}[smallE])]$ 
For[i = 0, i < 2, i++, AppendTo[equipartitionSmall, f[i]]];
equipartitionSmall
{0.48, 0.52}
```

```
BarChart[{equipartitionSmall}]
```



```
(* Binary expansion of the number e, small, level 2 *)
e = RealDigits[E, 2, 50]
smallE = e[[1]];
equipartitionSmall = {};
f[n_, m_] :=
N[ $\sum_{k=1}^{\text{Length}[smallE]-1} \text{If}[\{smallE[[k]], smallE[[k+1]]\} == \{n, m\}, 1, 0] / (\text{Length}[smallE] - 1)]$ ;
AppendTo[equipartitionSmall, f[0, 0]];
AppendTo[equipartitionSmall, f[0, 1]];
AppendTo[equipartitionSmall, f[1, 0]];
AppendTo[equipartitionSmall, f[1, 1]];
equipartitionSmall
{0.18, 0.3, 0.3, 0.2}
```

BarChart[{equipartitionSmall}]

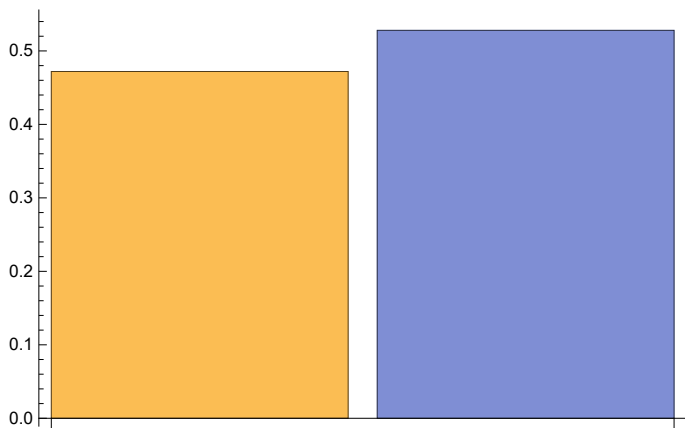


```
(* Binary expansion of the number e, medium, level 1 *)
e = RealDigits[E, 2, 500];
smallE = e[[1]]; (* should have been named mediumE *)
equipartitionSmall = {}
f[n_] := N[ $\sum_{k=1}^{\text{Length}[smallE]} \text{If}[\{smallE[[k]]\} == \{n\}, 1, 0] / (\text{Length}[smallE])]$ ]
For[i = 0, i < 2, i++, AppendTo[equipartitionSmall, f[i]]];
equipartitionSmall
```

```
{}
```

```
{0.472, 0.528}
```

BarChart[{equipartitionSmall}]



```
(* Binary expansion of the number e, medium, level 2 *)
e = RealDigits[E, 2, 500];
mediumE = e[[1]];
equipartitionMedium = {}
```

```
{}
```

```
f[n_, m_] := N[
  Sum[If[{mediumE[[k]], mediumE[[k + 1]]} == {n, m}, 1, 0] / (Length[mediumE] - 1),
  {k, 1, Length[mediumE] - 1}];
```

```
equipartitionMedium = {}
```

```
{}
```

```
AppendTo[equipartitionMedium, f[0, 0]];
AppendTo[equipartitionMedium, f[0, 1]];
AppendTo[equipartitionMedium, f[1, 0]];
AppendTo[equipartitionMedium, f[1, 1]];
equipartitionMedium
```

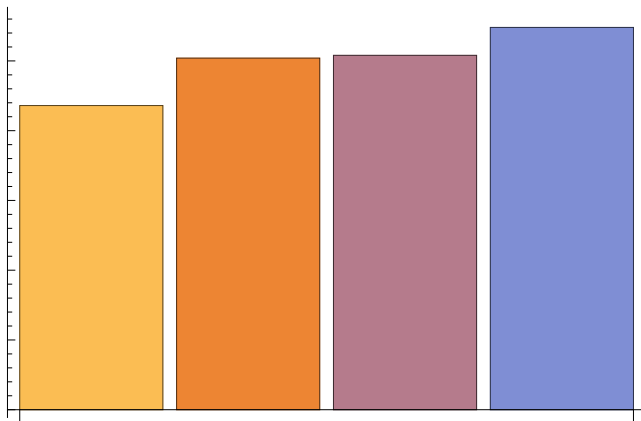
```
{0.218, 0.252, 0.254, 0.274}
```

```
{0.218, 0.252, 0.254, 0.274}
```

```
equipartitionMedium
```

```
{0.218, 0.252, 0.254, 0.274}
```

```
BarChart[{equipartitionMedium}]
```



```
In[43]:= (* Binary expansion of the number e, large, level 1 *)
equipartitionLarge = {}
```

```
Out[43]= {}
```

```
In[37]:= largeEDigits = RealDigits[E, 2, 5000];
```

```
In[38]:= largeE = largeEDigits[[1]];

```

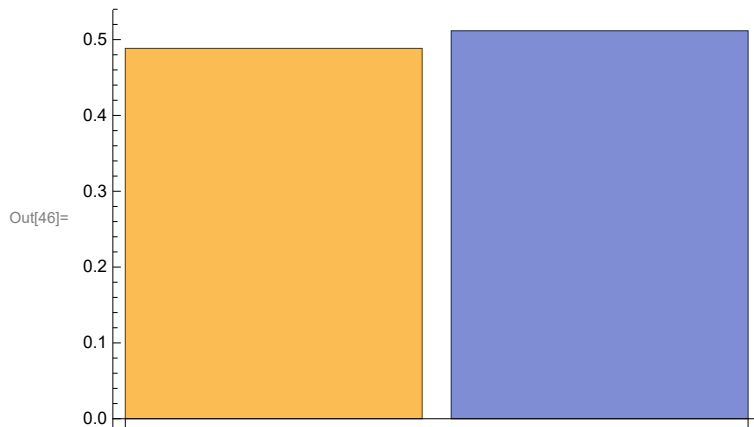
```
In[40]:= f[n_] := N[Sum[If[{largeE[[k]]} == {n}, 1, 0] / (Length[largeE]),
  {k, 1, Length[largeE]}];
```

```
In[44]:= For[i = 0, i < 2, i++, AppendTo[equipartitionLarge, f[i]]];
```

```
In[45]:= equipartitionLarge
```

```
Out[45]= {0.4884, 0.5116}
```

In[46]:= **BarChart[{equipartitionLarge}]**



In[47]:= **(* Binary expansion for the number E, large, level 2 *)**
equipartitionLarge = {}

Out[47]= {}

In[48]:= **largeE = RealDigits[E, 2, 5000];**

In[49]:= **e = largeE[[1]];**

In[60]:= **f[n_, m_] := N[$\sum_{k=1}^{\text{Length}[e]-1} \text{If}[\{e[[k]], e[[k+1]]\} = \{n, m\}, 1, 0] / (\text{Length}[e] - 1)$];**

AppendTo[equipartitionLarge, f[0, 0]];

In[62]:= **AppendTo[equipartitionLarge, f[0, 1]];**

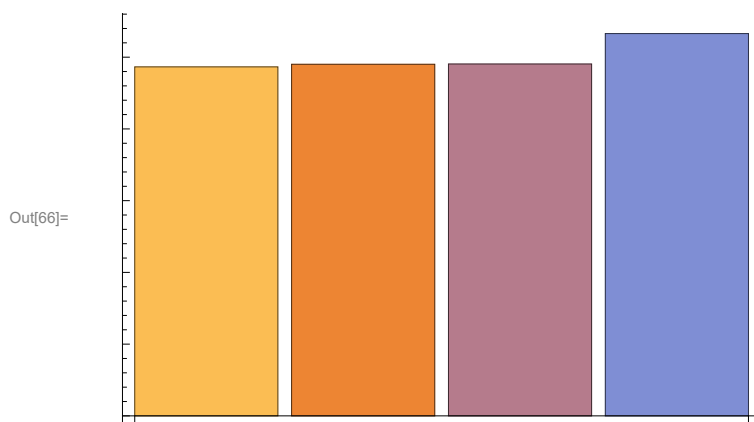
In[63]:= **AppendTo[equipartitionLarge, f[1, 0]];**

AppendTo[equipartitionLarge, f[1, 1]];

In[65]:= **equipartitionLarge**

Out[65]= {0.243249, 0.245049, 0.245249, 0.266453}

In[66]:= **BarChart[{equipartitionLarge}]**



(* Decimal expansion for the number e, small, level 2 *)

```
In[67]:= e = RealDigits[E, 10, 50];
```

```
In[68]:= smallE = e[[1]];
```

```
In[70]:= equipartitionSmall = {}
```

```
Out[70]= {}
```

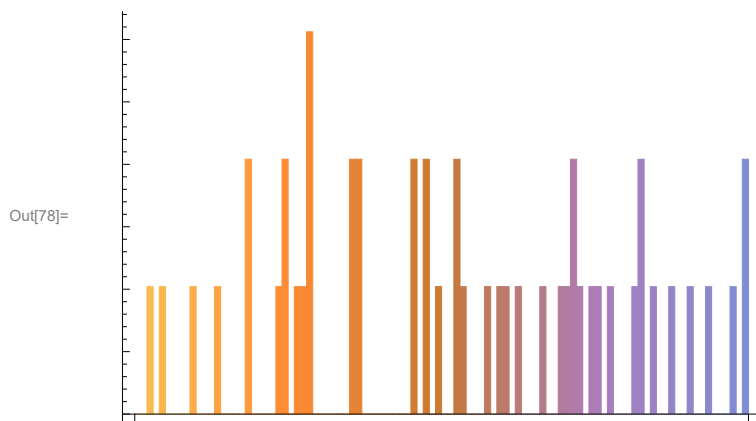
```
In[71]:= f[n_, m_] :=
  N[
$$\sum_{k=1}^{\text{Length}[smallE]-1} \text{If}[\{smallE[[k]], smallE[[k+1]]\} = \{n, m\}, 1, 0] / (\text{Length}[smallE] - 1)];$$

```

```
In[76]:= For[i = 0, i < 10, i++,
  AppendTo[equipartitionSmall, f[i, 0]];
  AppendTo[equipartitionSmall, f[i, 1]];
  AppendTo[equipartitionSmall, f[i, 2]];
  AppendTo[equipartitionSmall, f[i, 3]];
  AppendTo[equipartitionSmall, f[i, 4]];
  AppendTo[equipartitionSmall, f[i, 5]];
  AppendTo[equipartitionSmall, f[i, 6]];
  AppendTo[equipartitionSmall, f[i, 7]];
  AppendTo[equipartitionSmall, f[i, 8]];
  AppendTo[equipartitionSmall, f[i, 9]];
];
```

```
equipartitionSmall
```

```
In[78]:= BarChart[{equipartitionSmall}]
```



```
In[79]:= (* Decimal expansion for the number e, medium, level 2 *)
e = RealDigits[E, 10, 500];
mediumE = e[[1]];
```

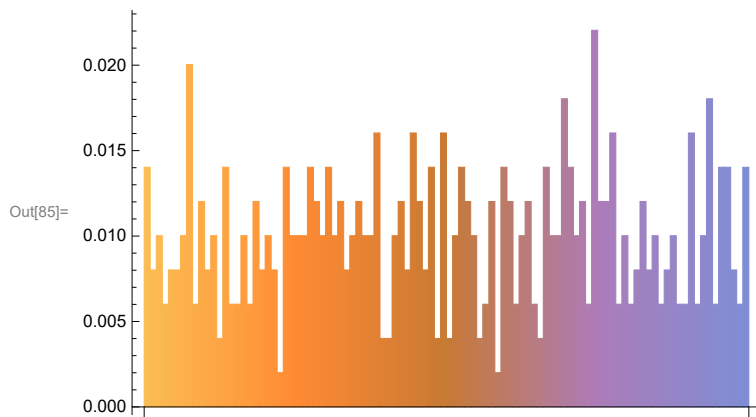
```
In[82]:= equipartitionMedium = {}
```

```
Out[82]= {}
```

```
In[83]:= f[n_, m_] := N[
  Sum[If[{mediumE[[k]], mediumE[[k + 1]]} == {n, m}, 1, 0] / (Length[mediumE] - 1),
  {k, 1, Length[mediumE] - 1}]
```

```
In[84]:= For[i = 0, i < 10, i++,
  AppendTo[equipartitionMedium, f[i, 0]];
  AppendTo[equipartitionMedium, f[i, 1]];
  AppendTo[equipartitionMedium, f[i, 2]];
  AppendTo[equipartitionMedium, f[i, 3]];
  AppendTo[equipartitionMedium, f[i, 4]];
  AppendTo[equipartitionMedium, f[i, 5]];
  AppendTo[equipartitionMedium, f[i, 6]];
  AppendTo[equipartitionMedium, f[i, 7]];
  AppendTo[equipartitionMedium, f[i, 8]];
  AppendTo[equipartitionMedium, f[i, 9]];
];
```

```
In[85]:= BarChart[ {equipartitionMedium} ]
```



```
In[87]:= (* Decimal expansion for the number e, large, level 2 *)
e = RealDigits[E, 10, 5000];
```

```
In[88]:= largeE = e[[1]];
```

```
In[89]:= equipartitionLarge = {}
```

```
Out[89]= {}
```

```
In[90]:= f[n_, m_] :=
  N[Sum[If[{largeE[[k]], largeE[[k + 1]]} == {n, m}, 1, 0] / (Length[largeE] - 1),
  {k, 1, Length[largeE] - 1}]
```



```
In[91]:= For[i = 0, i < 10, i++,  
  AppendTo[equipartitionLarge, f[i, 0]];  
  AppendTo[equipartitionLarge, f[i, 1]];  
  AppendTo[equipartitionLarge, f[i, 2]];  
  AppendTo[equipartitionLarge, f[i, 3]];  
  AppendTo[equipartitionLarge, f[i, 4]];  
  AppendTo[equipartitionLarge, f[i, 5]];  
  AppendTo[equipartitionLarge, f[i, 6]];  
  AppendTo[equipartitionLarge, f[i, 7]];  
  AppendTo[equipartitionLarge, f[i, 8]];  
  AppendTo[equipartitionLarge, f[i, 9]];  
];
```

```
In[92]:= BarChart[{equipartitionLarge}]
```

