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In[19]:= (* Adam Beck *)
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In[20]:= (* Calculate the fractional dimension of the Sierpinski carpet and "sponge" *)
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        (* Sierpinski carpet *)
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In[21]:= (* consider a 2D square. As discussed in class, we need  $(1/\epsilon)^2$  objects  
        to "fill" the square, where epsilon is the diameter. Let E refer to epsilon. *)  
        (* dimension =  $\log[N\{E,A\}] / \log[1/E]$  *)  
        (*  $\log[N\{E,A\}]$  is calculated by taking the mass of the current iteration of the carpet,  
        and plugging E into that mass equation. *)
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        (* For the first iteration, the mass of the carpet is  $8/9$ , the next is  $8/9$  squared,  
        then cubed, and so on. These are all multiplied by  $(1/E)$  squared. A  
        For loop can be used to iterate through a few iterations of the carpet,  
        and converge on an answer. Let epsilon be raised to the 1,  
        2nd, 3rd, etc. power for every iteration *)
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epsilon = 1/3;
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mass = 8/9;
```

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For[i = 1, i < 5, i++, (  
    epsilonTemp = (epsilon ^ i) ^ 2;  
    massTemp = mass ^ i;  
    massEquation = massTemp / epsilonTemp;  
    Print[N[Log[massEquation] / Log[1 / (epsilon ^ i)]] ]]  
);
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1.89279
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1.89279
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1.89279
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1.89279
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In[24]:=
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        (* Therefore the dimension(A) =  
        limit as E approaches infinity of  $\log[N\{E,A\}] / \log(1/E) = 1.89279$  *)
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        (* Sierpinski sponge *)
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        (* This is relatively the same procedure. The "filling" is now  $(1/E)^3$ ,  
        and the mass starts off at  $26/27$  for iteration 1, and cubes for every next iteration *)  
        epsilon = 1/3;  
        mass = 26/27;
```

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In[26]:=
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In[35]:= For[i = 1, i < 4, i ++, (  
    epsilonTemp = epsilon ^ (3 ^ (i - 1));  
    massTemp = mass ^ (3 ^ (i - 1));  
    massEquation = massTemp * ((1 / epsilonTemp) ^ 3);  
    Print[N[Log[massEquation] / Log[1 / (epsilonTemp)]] ]]  
);  
2.96565  
2.96565  
2.96565
```