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In[19]:= (* Adam Beck *)
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In[20]:= (* Calculate the fractional dimension of the Sierpinski carpet and "sponge" *)
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(* Sierpinski carpet *)
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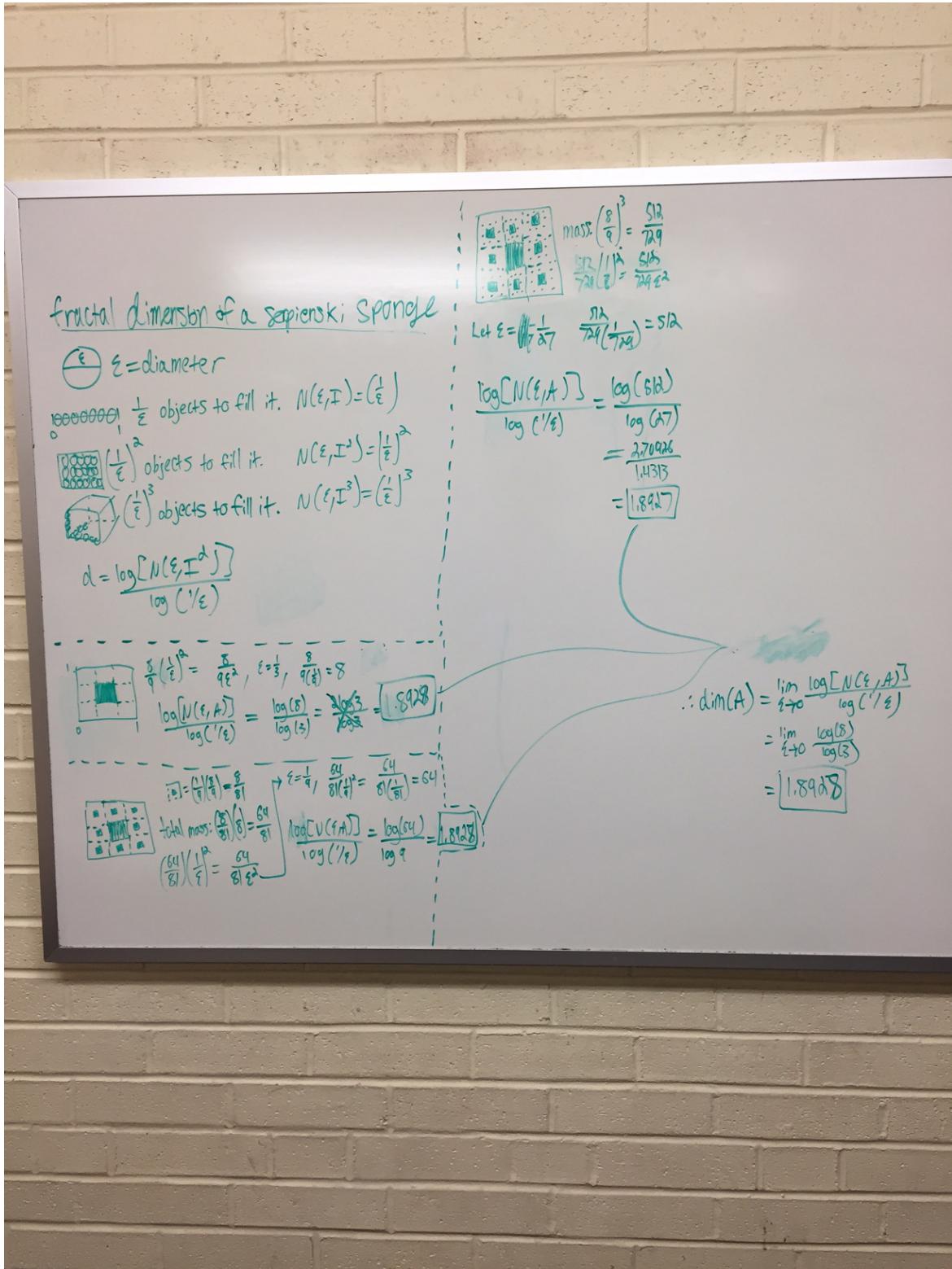
```
(* consider a 2D square. As discussed in class, we need  $(1/\text{epsilon})^2$  objects  
to "fill" the square, where epsilon is the diameter. Let E refer to epsilon. *)
```

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(* dimension =  $\log[N\{E,A\}] / \log[1/E]$  *)
```

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(*  $\log[N\{E,A\}]$  is calculated by taking the mass of the current iteration of the carpet,  
and plugging E into that mass equation. *)
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(* For the first iteration, the mass of the carpet is  $8/9$ , the next is  $8/9$  squared,  
then cubed, and so on. These are all multiplied by  $(1/E)$  squared. A
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For loop can be used to iterate through a few iterations of the carpet,  
and converge on an answer. Let epsilon be raised to the 1,  
2nd, 3rd, etc. power for every iteration *)
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epsilon = 1/3;
mass = 8/9;

```

For[i = 1, i < 5, i++, (
  epsilonTemp = (epsilon^i)^2;
  massTemp = mass^i;
  massEquation = massTemp / epsilonTemp;
  Print[N[Log[massEquation] / Log[1/(epsilon^i)]]])
];

```

1.89279

1.89279

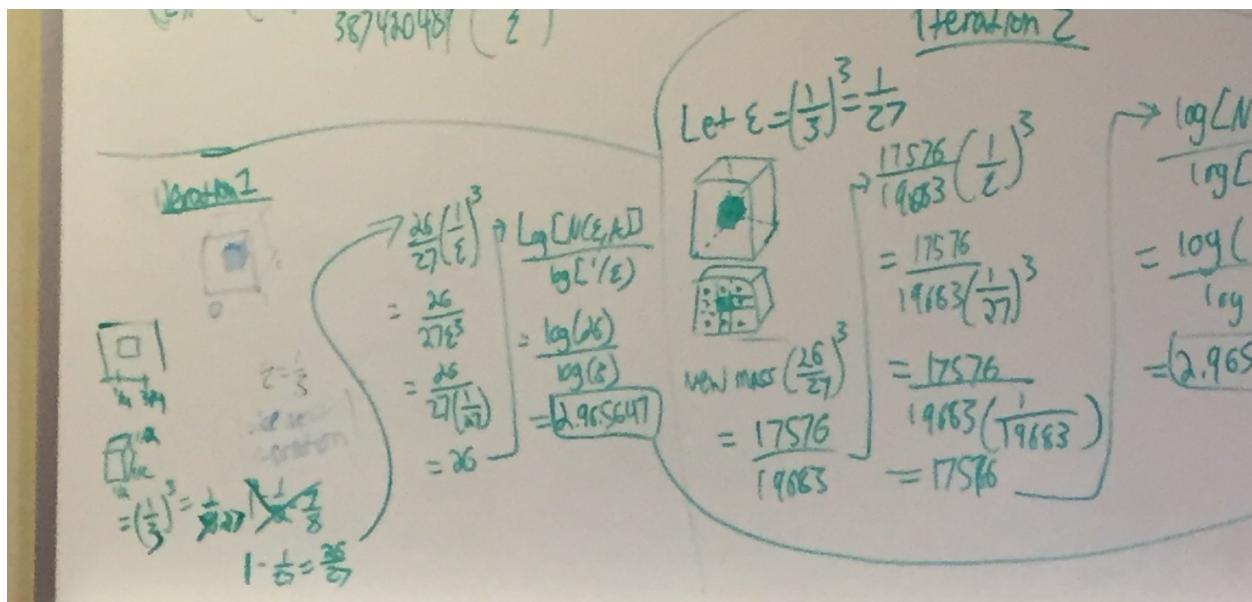
1.89279

1.89279

(* Therefore the dimension(A) =
limit as E approaches infinity of Log[N{E,A}] / log(1/E) = 1.89279 *)

(* Sierpinski sponge *)

(* This is relatively the same procedure. The "filling" is now $(1/E)^3$,
and the mass starts off at 26/27 for iteration 1, and cubes for every next iteration *)



epsilon = 1/3;
mass = 26/27;

In[26]:=

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In[35]:= For[i = 1, i < 4, i ++, (
  epsilonTemp = epsilon^(3^(i - 1));
  massTemp = mass^(3^(i - 1));
  massEquation = massTemp * ((1/epsilonTemp)^3);
  Print[N[Log[massEquation] / Log[1/(epsilonTemp)]]]]
];
2.96565
2.96565
2.96565
```