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## Homework 2

1.)  $(\mathbb{Z}_5, +, \cdot)$ 

$$\mathbb{Z} = \{0, 1, 2, 3, 4\}$$

$\begin{matrix} 0 & 1 & 2 & 3 & 4 \\ \uparrow & \uparrow & \uparrow & \uparrow & \uparrow \\ 0 & 1 & 2 & 3 & 4 \end{matrix}$

additive inverse

$1 \rightarrow 4$   
 $2 \rightarrow 3$   
 $3 \rightarrow 2$   
 $4 \rightarrow 1$

Multiplicative Inverse

	0	1	2	3	4
0	0	0	0	0	0
1	0	1	2	3	4
2	0	2	4	6	1
3	0	3	6	2	5
4	0	4	1	5	2

2.)

	0	1	2	3
0	0	0	0	0
1	0	1	2	3
2	0	2	4	6
3	0	3	6	2

does not have  
 multiplicity  
 for all  
 non-zero  
 elements  
 hence  
 not a  
 field