

# Chapter 1

(A)

① Blackbody radiation

- perfect absorber  
& emitter of light  
at all frequencies

② photoelectric effect

③ Hydrogen line spectra.

1800s

Rayleigh - Jeans law  
depends on Temperature

Square of frequency.

$$\rho_\nu(T) d\nu = \frac{8\pi k_B T}{c^3} \nu^2 d\nu$$

↑  
frequency

as heat increase in frequency  
the radiant energy density  
keeps on increasing & increasing.

Amount of light

⇒ This failure is known as ultraviolet  
catastrophe.

\* Classically, energy is  
a continuous range of  
values  
Quantum

Max. Planck solved this 1900s by coming up with Quantum

Assumption

$E = nh\nu$  → energy can only take integer values

↑  
integer

i.e. the space in between energy level.

\* Quantum assumption is  
that we have discrete  
energy levels with  
spacing.

Now the new Equation

frequency version {  $\rho_\nu(T) d\nu = \frac{8\pi h}{c^3} \frac{\nu^3}{e^{\frac{h\nu}{k_B T}} - 1} d\nu$

$$\rho_\lambda(T) d\lambda = \frac{8\pi hc}{\lambda^5} \times \frac{d\lambda}{e^{\frac{hc}{\lambda k_B T}} - 1}$$

$$h \approx 6.626 \times 10^{-34} \text{ J.s}$$

$$\lambda_{\max} T = \frac{hc}{4.965 k_B} \quad \lambda_{\max} T = 2.90 \times 10^{-3} \text{ m.K}$$

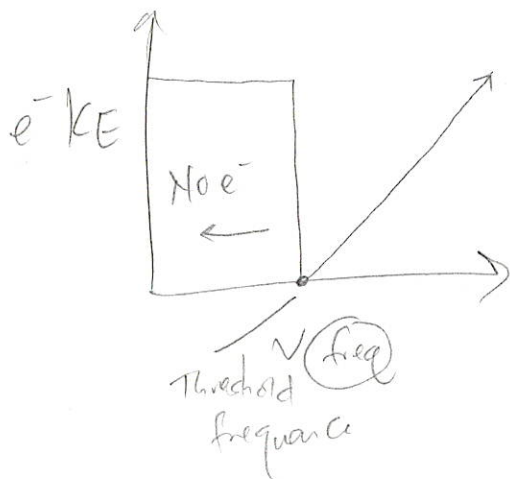
## ③ Photoelectric Effect.

Light — EM radiation, that's why it reacts with  $e^-$

- ① piece of metal
- ② shine the light on it
- ③ under the right conditions photon can be emitted.

\* Experimentally speaking

\* frequency determines the colour of the light.



Albert Einstein → Nobel Prize in Photoelectric Effect.

\* Light comes in quanta → called photons.

$$E = h\nu$$

By Conservation of Energy

$$KE = h\nu - \phi - eV$$

photon energy — work function of the metal  
— Amount of light required to remove an electron from the metal.

Quantum — discrete amount of Energy.

eV — amount of energy an electron gains when moving in 1V potential.

$$1\text{eV} = (1.602 \times 10^{-19} \text{ C}) \times (1\text{V})$$

$$= 1.602 \times 10^{-19} \text{ Joules}$$

\* To get any  $e^-$   $h\nu > \phi$

Same values of  $h$  for both Black Body radiation

# 1c) Hydrogen Atomic Spectra

- place hydrogen in a tube and pass electricity
- Excitation
- Emission of light.

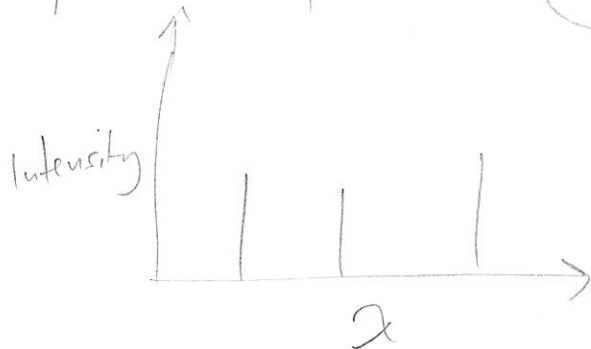
$$\lambda = \frac{h}{p} \quad \frac{\text{kg} \cdot \text{m}^2}{\text{s}^2} \div \frac{\text{kg} \cdot \text{m}}{\text{s}} = \frac{\text{m}}{\text{s}} \quad \text{page 2}$$

$$\lambda = \frac{h}{p} \quad \begin{matrix} \text{Planck's} \\ \text{constant} \end{matrix}$$

p - momentum

$$CV = \text{joules}$$

Hydrogen atomic spectrum



=> Hydrogen only emits light at very specific frequencies

Rydberg formula:  $\tilde{\nu} = R_H \left( \frac{1}{n_1^2} - \frac{1}{n_2^2} \right)$  where  $n_2 > n_1$

Integer n shows up

$$\frac{1}{\lambda}$$

5 6 \*

## Chapter 1: De Broglie Postulate - matter can also behave like wave.

\* Light as both light & particle.

Particle -> photoelectric effect

wave -> light diffraction.

$$\lambda = \frac{h}{mv}$$

\* ① and ② have to balance each other.

## ② Electron Diffraction ->

Coulomb's law = ①  $f = \frac{e^2}{4\pi\epsilon_0 r^2}$

force of attraction

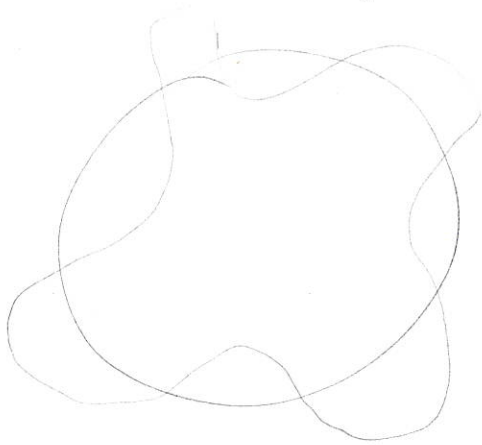
distance between charges

- force that keeps  $e^-$  from collapsing is centrifugal force

$$\textcircled{2} f = \frac{mv^2}{r}$$

velocity squared

$$\therefore \frac{e^2}{4\pi\epsilon_0 r^2} = \frac{M_e v^2}{r} \quad \text{Bohr assumes radius is fixed}$$



Circumference =  $2\pi r$

$$2\pi r = n\lambda \quad n=1,2,3$$

$$\lambda = \frac{h}{mv} \quad 2\pi r = n \left( \frac{h}{mv} \right) \quad \text{mass of } e^-$$

$$mv \cdot 2\pi r = nh \quad m = m_e$$

$$M_e v 2\pi r = nh$$

$$M_e v r = \frac{nh}{2\pi} = n\hbar \rightarrow \text{Angular momentum}$$

angular momentum comes in integer  $\hbar$

You can't have a fraction.

$\therefore$  Angular momentum is also Quantised.

$\rightarrow$  So what is the velocity of the electron?

$$v = \frac{n\hbar}{M_e r}$$

$$\frac{e^2}{4\pi\epsilon_0 r^2} = M_e v^2 = \frac{M_e \left( \frac{n\hbar}{M_e r} \right)^2}{r}$$

$$\text{Solve for } r; \underline{r = \frac{4\pi\epsilon_0 \hbar^2 n^2}{M_e e^2}}$$

this shows that  
orbits are Quantised.

$$n=1 \\ r = a_0 = 5.29 \times 10^{-11} \text{ m}$$

Energy  
 $= KE + PE$  / Potential energy is Coulomb potential  
 $\frac{1}{2} MeV^2$

$$KE + PE = \frac{1}{2} MeV^2 - \frac{e^2}{4\pi\epsilon_0 r}$$

because  $e^-$  going away from nucleus.

$$E = - \frac{Me^4}{8\epsilon_0^2 h^2 n^2}$$

Energy is also Quantized.

$$\Delta E = h\nu = \frac{Me^4}{8\epsilon_0^2 h^2} \left( \frac{1}{n_1^2} - \frac{1}{n_2^2} \right)$$

Rydberg Constant  
 $R_H = 109680 \text{ cm}^{-1}$

Bohr's Model doesn't predict the — That's why Bohr Model is not correct but right for H.

- Atom in a magnetic field
- Fails for He
- Violates uncertainty principle

$$\Delta x \Delta p \geq \frac{h}{2}$$