

- Fourier transform
- Laplace transform
- Fundamental theorem of algebra
- Riemann hypothesis
- Green's function

- * Zeros are significant when not as placeholders.
- * More precise measurement more sigfigs
- * Less precise measurement less sigfigs

Mcquarrie Chapter III: Experimental Error

Significant figures → minimum # of digits needed to write a number in scientific notation.
→ writing it without losing precision.

Types of Errors:

① Systematic Error → Flaw in experiment equipment or design.
→ Reproducible
→ can be corrected
→ Always one away from actual value
* Miscalibrated sensor

② Random Error → Comes from things you can't control
→ Not reproducible
→ Example of things we can't control: Temp & Pressure
→ Electrical noise * When measuring voltage; the last number keeps on changing.

Accuracy & Precision

→ How reproducible is the result; related to standard deviation.
→ How close is result close to true value.

Expressing Uncertainty

① Absolute Uncertainty: $97.54 \text{ cm} \pm 0.02 \text{ cm} \rightarrow$ b/w $97.52 - 97.56$ → have units

② Relative Uncertainty: $\frac{\text{absolute uncertainty}}{|\text{Value of measurement}|} = \frac{0.02}{97.54} = 0.0002$
[no units]

③ % relative = Relative Uncertainty $\times 100$
 $= 0.0002 \times 100 = 0.02\%$

Propagation of Uncertainty

$$\begin{aligned} & \text{e}_1 \qquad \qquad \qquad \text{e}_2 \\ & 0.154 \text{ g} \pm 0.002 \text{ g} - 0.105 \text{ g} \pm 0.002 \text{ g} \\ & \hline & 0.253 \text{ L} \pm 0.005 \text{ L} \end{aligned}$$

$$\text{SE}_{\text{L}} = \frac{0.154 \text{ g} - 0.105 \text{ g}}{0.253 \text{ L}} = 0.1937 \text{ g/L} \pm ?$$

$$? = e_3 = \sqrt{e_1^2 + e_2^2}$$

$$\begin{aligned} e_3 &= \sqrt{0.002^2 + 0.002^2} \\ &= 0.0028 \text{ g} \end{aligned}$$

$\times 0.049 \text{ g}$

$$\frac{0.049 \text{ g} \pm 0.0028 \text{ g}}{0.253 \text{ L} \pm 0.005 \text{ L}} = C$$

$$\left(\frac{e_c}{0.1937} \right)^2 = \left(\frac{0.0028}{0.049} \right)^2 + \left(\frac{0.005}{0.253} \right)^2$$

$$\begin{aligned} e_c &= C \sqrt{\left(\frac{0.0028}{0.049} \right)^2 + \left(\frac{0.005}{0.253} \right)^2} \\ &= 0.01 \end{aligned}$$

Ans: $0.19 \pm 0.01 \text{ g/L}$

for addition & subtraction

$$e_3 = \sqrt{e_1^2 + e_2^2}$$

for multiplication & division

$$\left(\frac{e_c}{\text{value}} \right)^2 = \left(\frac{e_a}{a} \right)^2 + \left(\frac{e_b}{b} \right)^2$$

e_1, e_2 relative uncertainties