Topic: Position, velocity, and acceleration

Question: Find the velocity function.

$$x(t) = 4t^2 - 6t + 2$$

Answer choices:

A
$$v(t) = 8t - 4$$

B
$$v(t) = 8t + 6$$

$$C v(t) = 4t - 6$$

$$D v(t) = 8t - 6$$

Solution: D

Take the derivative of the position function.

$$x(t) = 4t^2 - 6t + 2$$

$$x'(t) = 8t - 6$$

Velocity is the derivative of position.

$$v(t) = 8t - 6$$



Topic: Position, velocity, and acceleration

Question: Find the position of a car when its velocity is zero.

$$x(t) = 4t^2 - 8t + 10$$

Answer choices:

$$A \qquad x = 6$$

B
$$x = 7$$

C
$$x = 10$$

$$D \qquad x = 0$$

Solution: A

Take the derivative of the position function.

$$x(t) = 4t^2 - 8t + 10$$

$$x'(t) = 8t - 8$$

Velocity is the derivative of position.

$$v(t) = 8t - 8$$

We need to find time when velocity is 0.

$$8t - 8 = 0$$

$$8t = 8$$

$$t = 1$$

Velocity is 0 when t=1. To find position at the same time, substitute t=1 into the position function.

$$x(1) = 4(1)^2 - 8(1) + 10$$

$$x(1) = 4 - 8 + 10$$

$$x(1) = 6$$

Topic: Position, velocity, and acceleration

Question: Use the position function to find the velocity of a rocket at t = 4.

$$x(t) = 6t^3 - t^2 + 3t - 9$$

Answer choices:

A
$$v(4) = 238$$

B
$$v(4) = 371$$

C
$$v(4) = 283$$

D
$$v(4) = 317$$

Solution: C

Take the derivative of the position function.

$$x(t) = 6t^3 - t^2 + 3t - 9$$

$$x'(t) = 18t^2 - 2t + 3$$

Velocity is the derivative of position.

$$v(t) = 18t^2 - 2t + 3$$

We need to find velocity when t=4, so we'll plug t=4 into the velocity function we just found.

$$v(4) = 18(4)^2 - 2(4) + 3$$

$$v(4) = 288 - 8 + 3$$

$$v(4) = 283$$