Topic: Limits at infinity and horizontal asymptotes

Question: Evaluate the limit.

$$\lim_{x \to \infty} \frac{6}{4x^2}$$

Answer choices:

- $A = \frac{3}{2}$
- B 0
- C ∞
- D 1



Solution: B

To find the limit as $x \to \infty$, we'll look at the highest-degree terms in both the numerator and denominator.

The highest-degree term in the numerator is 6, which has a degree of 0. The highest-degree term in the denominator is $4x^2$, which has a degree of 2. Therefore,

When the degree of the numerator is less that the degree of the denominator, the function has a horizontal asymptote at y = 0.

So, as $x \to \infty$, the limit is 0.



Topic: Limits at infinity and horizontal asymptotes

Question: Evaluate the limit.

$$\lim_{x \to \infty} \frac{6x^3 + 2x^2 - x + 1}{8x^3 - 1}$$

Answer choices:

A - 1

B ∞

 $c \qquad \frac{3}{4}$

D 1

Solution: C

To find the limit as $x \to \infty$, we'll look at the highest-degree terms in both the numerator and denominator.

The highest-degree term in the numerator is $6x^3$, which has a degree of 3. The highest-degree term in the denominator is $8x^3$, which has a degree of 3. Therefore,

$$N = D: 3 = 3$$

When the degree of the numerator is equal to the degree of the denominator, the function has a horizontal asymptote given by the ratio of the coefficients on those highest-degree terms.

$$\frac{6x^3 + 2x^2 - x + 1}{8x^3 - 1}$$

$$\frac{6x^3}{8x^3}$$

$$\frac{6}{8}$$

$$\frac{3}{4}$$

So, as $x \to \infty$, the limit is 3/4.

Topic: Limits at infinity and horizontal asymptotes

Question: Evaluate the limit.

$$\lim_{x \to \infty} \frac{x^2 + 1}{5x^4 + 2x^2}$$

Answer choices:

A $\sqrt{5}$

 $B \qquad \frac{\sqrt{5}}{5}$

C ∞

D 0

Solution: D

To find the limit as $x \to \infty$, we'll look at the highest-degree terms in both the numerator and denominator.

The highest-degree term in the numerator is x^2 , which has a degree of 2. The highest-degree term in the denominator is $5x^4$, which has a degree of 4. Therefore,

When the degree of the numerator is less that the degree of the denominator, the function has a horizontal asymptote at y = 0.

So, as $x \to \infty$, the limit is 0.

