

Calculus 2 Workbook

Other approximation methods



OVER AND UNDERESTIMATION

■ 1. Use a Riemann sum to estimate the maximum and minimum area under the curve on $[0,\pi]$. Use rectangular approximation methods with 4 equal subintervals. Round the answer to 2 decimal places.

$$f(x) = 5\sin\frac{x}{2} + 3$$

■ 2. Use a Riemann sum to estimate the maximum and minimum area under the curve on [0,4]. Use rectangular approximation methods with 4 equal subintervals.

$$g(x) = \frac{1}{4}(x-4)^2 + 1$$

■ 3. Use a Riemann sum to estimate the maximum and minimum area under the curve on [0,9]. Use rectangular approximation methods with 3 equal subintervals. Round the answer to 2 decimal places.

$$h\left(x\right) = \frac{1}{2}\sqrt{7x} + 2$$



LIMIT PROCESS TO FIND AREA ON [A,B]

■ 1. Use the limit process to find the area of the region between the graph of f(x) and the x-axis on the interval [3,7].

$$f(x) = x^2 + 2$$

■ 2. Use the limit process to find the area of the region between the graph of g(x) and the x-axis on the interval [2,6].

$$f(x) = x^2 - x + 3$$

■ 3. Use the limit process to find the area of the region between the graph of h(x) and the x-axis on the interval [2,5].

$$h(x) = x^2 - 3x + 7$$



LIMIT PROCESS TO FIND AREA ON [-A,A]

■ 1. Use the limit process to find the area of the region between the graph of f(x) and the x-axis on the interval [-5,5].

$$f(x) = x^2 + 1$$

■ 2. Use the limit process to find the area of the region between the graph of g(x) and the x-axis on the interval [-3,3].

$$g(x) = 3x^2 - 4$$

■ 3. Use the limit process to find the area of the region between the graph of h(x) and the x-axis on the interval [-1,1].

$$h(x) = 4x^2 - x + 1$$



TRAPEZOIDAL RULE

■ 1. Using n = 6 and the Trapezoidal rule, approximate the value of the integral. Round the answer to 2 decimal places.

$$\int_{4}^{16} 2\sqrt[3]{x} + 3 \ dx$$

 \blacksquare 2. Using n=6 and the Trapezoidal rule, approximate the value of the integral.

$$\int_0^6 \frac{1}{4} x^4 - \frac{1}{2} x^3 + 2x^2 - 5x + 8 \ dx$$

 \blacksquare 3. Using n=4 and the Trapezoidal rule, approximate the value of the integral.

$$\int_0^8 \frac{1}{2} x^2 - 3x + 6 \ dx$$

■ 4. Using n = 4 and the Trapezoidal rule, approximate the value of the integral.

$$\int_0^{16} \frac{1}{16} x^4 - \frac{1}{2} x^3 - x^2 - x + 1 \ dx$$



SIMPSON'S RULE

■ 1. Use Simpson's Rule with n = 6 to approximate the value of the integral. Round the answer to 2 decimal places.

$$\int_2^8 6\sqrt{3x} + 5 \ dx$$

■ 2. Use Simpson's Rule with n = 8 to approximate the value of the integral. Round the answer to 2 decimal places.

$$\int_{4}^{28} 120(0.95)^x \ dx$$

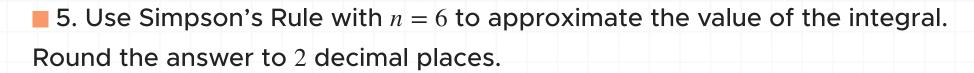
■ 3. Use Simpson's Rule with n = 4 to approximate the value of the integral. Round the answer to 2 decimal places.

$$\int_{5}^{7} 3\ln(x+5) - 2 \ dx$$

 \blacksquare 4. Use Simpson's Rule with n=4 to approximate the value of the integral.

$$\int_{-3}^{9} x^2 + 3x + 2 \ dx$$





$$\int_{0.4}^{1.6} \frac{1}{3} x^3 - x^2 + 5x + 4 \ dx$$





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