$\rm MA3505~Multivariate~Statistics~Project~1$

April 28, 2016

- 1 Introduction and exploratory data analysis for the variables.
- 2 Analysis to answer each research question
- 2.1 Question 1

2.2 Question 2

Using the above code I created the necessary multivariate regression model. I was able to use this model to get the following table of coefficients:

	chol	thaldur	thaltime	met	thalach
(Intercept)	2.182e+02	2.964e+00	1.941e+00	4.167e+00	1.216e+02
proto	5.933e - 01	7.621e-02	7.395e-02	1.284e-02	1.241e-01
restecg	$-1.965\mathrm{e}{+01}$	1.506e-01	4.325e-01	1.305e-01	-2.202e-01
dig	6.033e+00	$3.130\mathrm{e}{+00}$	2.889e+00	1.519e+00	$-8.249\mathrm{e}{+00}$
prop	$1.800\mathrm{e}{+01}$	$3.734e\!-\!01$	6.787e - 01	4.875e-02	$-6.759\mathrm{e}{+00}$
nitr	$-1.390\mathrm{e}{+01}$	-3.582e - 01	-3.903e-01	3.416e-02	-5.949e+00
pro	-6.872e+01	1.142e+00	9.582e - 01	$4.637\mathrm{e}\!-\!01$	1.990e-02
diuretic	-4.914e+01	1.516e+00	6.732e-01	$3.744e\!-\!01$	1.610e+01
	thalrest	$_{ m tpeakbps}$	$_{ m tpeakbpd}$	trestbpd	oldpeak
(Intercept)	$7.475\mathrm{e}{+01}$	1.607e+02	9.326e+01	8.488e+01	1.937e+00
proto	4.602e-02	$2.114\mathrm{e}\!-\!01$	3.306e-02	1.262e-02	-3.094e-03
restecg	1.481e+00	3.762e+00	-1.245e+00	1.159e+00	-2.081e-01
dig	2.175e+00	-7.984e+00	-1.854e+01	-4.949e+00	4.202e-01
prop	-2.692e-01	$5.788\mathrm{e}\!-\!02$	-1.988e+00	5.123e-01	-1.674e-02
nitr	-8.676e+00	-9.099e+00	-3.690e+00	$-3.270\mathrm{e}{+00}$	2.621e-01
pro	2.958e+00	4.851e+00	7.011e+00	2.962e-01	$-8.122e\!-\!01$
diuretic	-8.346e-01	6.602e+00	2.153e+00	1.116e+00	-2.439e-02
	rldv5	rldv5e			
(Intercept)	1.487e + 01	1.497e+01			
proto	-6.571e-04	-6.529e-03			
restecg	1.703e-01	$2.203\mathrm{e}\!-\!01$			
dig	-2.153e+00	-2.219e+00			
prop	1.272e+00	$1.175\mathrm{e}{+00}$			
nitr	$6.343e\!-\!01$	-6.043e-01			
pro	-1.583e+00	$7.800\mathrm{e}\!-\!01$			
diuretic	-1.303e-01	3.239e+00			

However this is not very useful, so I used the **summary()** function to enable me to achieve a more detailed view of my analysis. Below I have tried my best to explain the detailed view for each response variable.

```
Response chol:
Call:
lm(formula = chol ~ proto + restecg + dig + prop + nitr + pro +
    diuretic, data = datall)
Residuals:
                     Median
     Min
                1Q
                                   3Q
                                            Max
-221.153
           -37.934
                      -0.852
                               55.190
                                        310.650
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) 218.1866
                          16.6717
                                    13.087
                                            < 2e-16 ***
                                            0.00207 **
               0.5933
                           0.1884
                                     3.149
proto
restecg
             -19.6467
                          15.5463
                                    -1.264
                                            0.20877
                          42.3211
               6.0327
                                     0.143
                                            0.88689
dig
              17.9968
                          25.2562
                                     0.713
                                            0.47750
prop
nitr
             -13.8953
                          24.8506
                                    -0.559
                                            0.57710
pro
             -68.7201
                          27.9126
                                    -2.462
                                            0.01524 *
diuretic
             -49.1356
                          33.0596
                                    -1.486
                                            0.13983
                                                                                        1
Signif. codes:
                              0.001
                                              0.01
                                                             0.05
                                                                           0.1
                 0
Residual standard error: 85.12 on 120 degrees of freedom
  (771 observations deleted due to missingness)
Multiple R-squared:
                      0.2402,
                                  Adjusted R-squared:
F-statistic: 5.418 on 7 and 120 DF,
                                       p-value: 2.026e-05
```

From the table above we can see that the predictor that had the most affect in the value of the **chol** response was **proto**. As *chol* refers to the amount of cholesterol in a person's system and *proto* refers to the type of exercise that they do, it is not a major surprise that this is the most important as in theory the higher the intensity of the your exercise program the lower your cholesterol will be. The second most important variable is **pro**; this is an indicator variable that tells us if someone uses *calcium channel blocker used during exercise* (it is used in cholesteryl ester hydrolysis which helps reduce cholesterol) during their exercise routine.

```
Response thaldur:
Call:
lm(formula = thaldur ~\tilde{\ } proto + restecg + dig + prop + nitr +
    pro + diuretic, data = datall)
Residuals:
            1Q Median
                                   Max
   Min
                            3Q
-4.312 \quad -1.681 \quad -0.310
                         1.422
                                 6.440
Coefficients:
               Estimate Std. Error t value Pr(>|t|)
(Intercept)
               2.964440
                           0.443361
                                        6.686 \quad 7.65 \,\mathrm{e}{-10} \ ***
                                               < 2e-16 ***
proto
               0.076214
                           0.005011
                                       15.209
restecg
               0.150581
                           0.413433
                                        0.364
                                                 0.7163
                                                 0.0063 **
               3.129630
                           1.125473
                                        2.781
dig
               0.373380
                           0.671654
                                        0.556
                                                 0.5793
prop
nitr
              -0.358181
                           0.660868
                                       -0.542
                                                 0.5888
pro
               1.141536
                           0.742300
                                        1.538
                                                 0.1267
diuretic
               1.516199
                           0.879177
                                        1.725
                                                 0.0872
                                                                                            1
Signif. codes:
                                0.001
                                                 0.01
                                                                0.05
                                                                              0.1
                  0
                        ***
                                          **
Residual standard error: 2.264 on 120 degrees of freedom
  (771 observations deleted due to missingness)
Multiple R-squared:
                        0.6909,
                                    Adjusted R-squared:
F-statistic: 38.31 on 7 and 120 DF,
                                         p-value: < 2.2e-16
```

The predictor variable in this instance is **thaldur** which represents the length of time a person spends on an exercise test, it is therefore no surprise that **proto** is the most important predictor as the harder the exercise test the less time you will be able to do it for. The second most significant predictor **dig** refers to whether or not the person is taking a drug called *digitails* during exercise. Studies have shown that the use of this drug during exercise increases blood flow which could allow someone to exercise for longer (experts are not sure if it is a performance enhancing drug as trial results vary).

```
Response thaltime :
lm(formula = thaltime ~ proto + restecg + dig + prop + nitr +
    pro + diuretic, data = datall)
Residuals:
   Min
            1Q Median
                           3Q
                                  Max
-4.469 \quad -1.639 \quad -0.139
                        1.053
                                7.352
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)
                                      4.322 \ 3.21e-05 ***
              1.941466
                          0.449229
proto
              0.073951
                          0.005077
                                     14.565
                                              < 2e-16 ***
                                      1.032
                                               0.3039
restecg
              0.432490
                          0.418906
                                      2.533
dig
              2.888715
                          1.140370
                                               0.0126 *
                          0.680544
                                      0.997
                                               0.3206
prop
              0.678710
nitr
             -0.390289
                          0.669615
                                      -0.583
                                               0.5611
              0.958162
                          0.752125
                                      1.274
                                               0.2051
pro
              0.673187
                          0.890814
diuretic
                                      0.756
                                               0.4513
Signif. codes:
                               0.001
                                               0.01
                                                             0.05
                                                                            0.1
                                                                                         1
Residual standard error: 2.294 on 120 degrees of freedom
  (771 observations deleted due to missingness)
                       0.6704,
                                   Adjusted R-squared:
Multiple R-squared:
F-statistic: 34.86 on 7 and 120 DF,
                                        p-value: < 2.2e-16
```

thaltime refers to the time at which a person's ST depression was measured. It is therefore no surprise that **proto** has the highest effect as different exercises will take different amount of times to complete meaning that if *thaltime* is always measured at the end of the exercise test people who do different tests will have different times but those who take the same test should have very similar times. **dig** is the next significant variable which sort of makes sense as you most likely have to wait for the drug to leave your system before your ST depression can be measured.

```
Response met :
Call:
lm(formula = met ~ proto + restecg + dig + prop + nitr + pro +
    diuretic, data = datall)
Residuals:
              1Q Median
    Min
                               3Q
                                       Max
-3.7325 \quad -1.0919 \quad -0.1298
                           0.8792
                                    5.8206
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) 4.166578
                         0.336945
                                    12.366
                                              <2e-16 ***
proto
             0.012843
                         0.003808
                                     3.372
                                              0.0010 **
restecg
             0.130481
                         0.314201
                                     0.415
                                              0.6787
dig
             1.518904
                         0.855338
                                     1.776
                                              0.0783 .
prop
             0.048745
                         0.510444
                                     0.095
                                              0.9241
nitr
             0.034160
                         0.502247
                                     0.068
                                              0.9459
pro
             0.463725
                         0.564133
                                     0.822
                                              0.4127
diuretic
             0.374352
                         0.668158
                                     0.560
                                              0.5763
                                                             0.05
                                                                           0.1
                                                                                        1
Signif. codes:
                              0.001
                                               0.01
                 0
                       ***
Residual standard error: 1.72 on 120 degrees of freedom
  (771 observations deleted due to missingness)
Multiple R-squared:
                       0.1108,
                                   Adjusted R-squared:
F-statistic: 2.136 on 7 and 120 DF,
                                        p-value: 0.04484
```

The predictor **met** refers to the *metabolic equivalent of resting oxygen consumption while sitting* and therefore it is not much of a surprise that the response **proto** is the most significant. It is also not that surprising that it is as significant as before, as the trial that produced these results most likely used people of varying athletic abilities for each test in order to make the results more accurate.

```
Response thalach:
lm(formula = thalach ~\tilde{\ } proto + restecg + dig + prop + nitr +
    pro + diuretic, data = datall)
Residuals:
    Min
                  Median
                                3Q
                                       Max
              1Q
-42.497 -10.060
                  -0.925
                           13.735
                                    53.075
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) 121.6141
                           3.6895
                                    32.962
                                             < 2e-16 ***
               0.1241
                           0.0417
                                     2.977
                                             0.00352 **
proto
              -0.2202
restecg
                           3.4405
                                    -0.064
                                             0.94908
              -8.2489
                           9.3659
                                    -0.881
                                             0.38022
dig
prop
              -6.7587
                           5.5893
                                    -1.209
                                             0.22896
nitr
              -5.9491
                           5.4996
                                    -1.082
                                             0.28154
               0.0199
                           6.1772
                                     0.003
                                             0.99743
pro
                                     2.200
              16.0994
                           7.3163
                                             0.02969
diuretic
Signif. codes:
                               0.001
                                               0.01
                                                              0.05
                                                                            0.1
                                                                                         1
Residual standard error: 18.84 on 120 degrees of freedom
  (771 observations deleted due to missingness)
Multiple R-squared:
                       0.1867,
                                   Adjusted R-squared:
F-statistic: 3.934 on 7 and 120 DF,
                                        p-value: 0.0006723
```

The predictor **thalach** refers to the maximum heart rate that a person achieves during their exercise test and as such it is no surprise that the response variable that is the most significant when calculating it is **proto**. This is because the more intense the exercise test is the more oxygen your body is going to need thus you will have a higher heart rate. Again it is not surprising that *proto* is only a 2* rather than a 3* significance level as your maximum heart rate will depend on how athletic you are, the more athletic the lower your max heart rate will be. **diuretic** is the other significant response variable and it refers to whether or not the subject uses diuretic used during exercise. Diuretic is considered to be a performance enhancing drug so it is therefore no surprise that it only has a 1* significance level due to the fact that the analysis up to now has shown that there is a high probability that athletes are involved in this trial and would be band by WADA if they were caught using it.

```
Response thalrest:
lm(formula = thalrest ~ proto + restecg + dig + prop + nitr +
    pro + diuretic, data = datall)
Residuals:
                               3Q
    Min
              1Q
                  Median
                                      Max
-28.204
                  -1.909
         -8.542
                            8.172
                                   55.796
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) 74.75201
                                             <2e-16 ***
                          2.60040
                                    28.746
                                              0.120
proto
              0.04602
                          0.02939
                                     1.566
                                    0.611
                                              0.542
restecg
              1.48140
                          2.42487
                          6.60112
                                              0.742
dig
              2.17533
                                    0.330
                                    -0.068
                                              0.946
prop
             -0.26923
                          3.93939
nitr
             -8.67576
                          3.87612
                                    -2.238
                                              0.027 *
              2.95844
                          4.35374
                                    0.680
                                              0.498
pro
             -0.83465
                                              0.872
diuretic
                          5.15655
                                    -0.162
Signif. codes:
                              0.001
                                              0.01
                                                            0.05
                                                                          0.1
                                                                                       1
Residual standard error: 13.28 on 120 degrees of freedom
  (771 observations deleted due to missingness)
                      0.09876,
                                  Adjusted R-squared:
Multiple R-squared:
F-statistic: 1.879 on 7 and 120 DF,
                                       p-value: 0.07885
```

The **thalrest** variable refers to the subjects resting heart rate and the only variable that has any significant effect on the outcome of this result is **nitr** which tells us whether or not the subject uses nitrates used during their exercise. I am not quite sure what the use of nitrates has to do with the resting heart rates but I do know that they are added to 'unhealthy foods' such as *bacon*, *sandwich meats and salami* which could indicate that they are not very athletic but a high resting heart does not mean that someone is less athletic.

In this trial the subjects the measuring of their peak blood pressure was split into two different variables: **tpeakbps** and **tpeakbpd**, google wasn't able to explain why this is the case.

```
Response tpeakbps:
lm(formula = tpeakbps ~ proto + restecg + dig + prop + nitr +
    pro + diuretic, data = datall)
Residuals:
   Min
           1Q Median
                           3Q
                                 Max
-46.56 -15.18
               -2.97
                        13.36
                               58.73
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) 160.70295
                           4.33227
                                    37.094
                                            < 2e-16 ***
                                      4.317 \ \ 3.27e - 05 \ ***
proto
               0.21138
                           0.04897
                           4.03984
                                               0.354
restecg
               3.76224
                                      0.931
              -7.98425
                          10.99749
                                     -0.726
                                               0.469
dig
prop
               0.05788
                           6.56303
                                     0.009
                                               0.993
nitr
              -9.09857
                           6.45763
                                     -1.409
                                               0.161
pro
                                      0.669
               4.85054
                           7.25334
                                               0.505
               6.60213
                           8.59083
                                      0.769
diuretic
                                               0.444
Signif. codes:
                              0.001
                                              0.01
                                                            0.05
                                                                          0.1
                                                                                       1
Residual standard error: 22.12 on 120 degrees of freedom
  (771 observations deleted due to missingness)
Multiple R-squared:
                      0.1992,
                                  Adjusted R-squared:
F-statistic: 4.266 on 7 and 120 DF,
                                       p-value: 0.0003059
```

For the variable that had the most significant affect on **tpeakbps** was (as normal it seems in this trial) **proto**. This is most likely because of the fact that exercise can lower your blood pressure and therefore the subjects that are able to take the more intensive exercise tests were likely to have a lower peak blood pressure.

```
Response tpeakbpd :
lm(formula = tpeakbpd ~\tilde{}~ proto + restecg + dig + prop + nitr +
    pro + diuretic, data = datall)
Residuals:
    Min
                                3Q
                                       Max
              1Q
                  Median
-60.687
                   -0.023
                                    36.329
          -7.517
                             8.638
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)
                            2.68207
              93.26322
                                     34.773
                                              <\ 2\,{\rm e}\!-\!16\ ***
                                              0.27768
proto
               0.03306
                            0.03031
                                       1.091
                                      -0.498
restecg
              -1.24519
                            2.50103
                                              0.61948
dig
             -18.54131
                            6.80844
                                      -2.723
                                              0.00743 **
                            4.06311
prop
              -1.98759
                                      -0.489
                                              0.62561
nitr
              -3.69032
                            3.99786
                                      -0.923
                                              0.35782
               7.01102
                            4.49047
                                       1.561
                                              0.12108
pro
               2.15344
                            5.31850
                                       0.405
                                              0.68627
diuretic
Signif. codes:
                               0.001
                                                0.01
                                                              0.05
                                                                            0.1
                                                                                          1
Residual standard error: 13.69 on 120 degrees of freedom
  (771 observations deleted due to missingness)
Multiple R-squared:
                       0.1321,
                                   Adjusted R-squared:
F-statistic:
               2.61 on 7 and 120 DF,
                                        p-value: 0.01525
```

The response variable that was most significant when working out the predictor **tpeakbpd** was **dig**. This makes sense as studies have shown that the use of the drug digitalis during exercise lowers a person's blood pressure.

```
Response trestbpd:
Call:
lm(formula = trestbpd ~ proto + restecg + dig + prop + nitr +
    pro + diuretic, data = datall)
Residuals:
              1Q Median
    Min
                               3Q
                                      Max
-35.510
                  -1.298
                            5.543
                                   24.175
         -6.141
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) 84.87854
                          1.88379
                                   45.057
                                             <2e-16 ***
              0.01262
                          0.02129
                                    0.593
                                              0.554
proto
restecg
              1.15852
                          1.75663
                                    0.660
                                              0.511
                                              0.303
             -4.94866
                          4.78200
                                    -1.035
dig
              0.51233
                          2.85378
                                    0.180
                                              0.858
prop
                                              0.246
nitr
             -3.27042
                          2.80795
                                    -1.165
pro
              0.29623
                          3.15394
                                    0.094
                                              0.925
diuretic
              1.11644
                          3.73552
                                     0.299
                                              0.766
                                                                                       1
Signif. codes:
                 0
                              0.001
                                              0.01
                                                            0.05
                                                                          0.1
Residual standard error: 9.618 on 120 degrees of freedom
  (771 observations deleted due to missingness)
Multiple R-squared:
                      0.0366,
                                  Adjusted R-squared:
F-statistic: 0.6514 on 7 and 120 DF,
                                        p-value: 0.7126
```

The predictor variable **trestbpd** refers to the subjects resting blood pressure. As this must be taken before any exercise is started it makes sense that none of the responses are significant in determining what this value shall be due to them being manly related to the exercise test the subject takes.

```
Response oldpeak :
lm(formula = oldpeak ~ proto + restecg + dig + prop + nitr +
    pro + diuretic, data = datall)
Residuals:
    Min
              1Q
                 Median
                                3Q
                                       Max
-1.9343 \quad -0.6280 \quad -0.0506
                           0.3642
                                    3.5801
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)
              1.937386
                          0.169250
                                     11.447
                                              <\ 2\,{\rm e}\!-\!16\ ***
proto
             -0.003094
                          0.001913
                                      -1.617
                                              0.10841
                                      -1.319
restecg
             -0.208133
                          0.157825
                                              0.18976
dig
              0.420187
                          0.429642
                                      0.978
                                              0.33004
                          0.256399
prop
             -0.016737
                                      -0.065
                                              0.94806
nitr
              0.262057
                          0.252282
                                      1.039
                                              0.30101
             -0.812187
                          0.283368
                                      -2.866
                                              0.00491
pro
             -0.024390
                          0.335620
diuretic
                                      -0.073
                                              0.94219
Signif. codes:
                               0.001
                                               0.01
                                                              0.05
                                                                            0.1
Residual standard error: 0.8642 on 120 degrees of freedom
  (771 observations deleted due to missingness)
                       0.1081,
                                   Adjusted R-squared:
Multiple R-squared:
F-statistic: 2.077 on 7 and 120 DF,
                                        p-value: 0.0511
```

The predictor variable **oldpeak** refers to *ST depression induced by exercise relative to rest* (which I understand from google to be a fancy way of saying that the subject gets a small heart attack during exercise). It makes sense then that the most significant variable in deciding what the value of which if it is high can cause heart attacks. *oldpeak* is going to be is **pro** as helps to lower cholesterol

The next two predictors, **rldv5** and **rldv5e**, refer to height at rest and height at peak exercise. I don't know what height they are referring to (I am assuming it is not just how tall they are as that would be dull to measure at rest and during peak exercise as it would not change) and luckily none of the response variables are significant in working out what the values of the variables will be.

Response rldv5 :

```
lm(formula = rldv5 ~ proto + restecg + dig + prop + nitr + pro +
    diuretic, data = datall)
Residuals:
     Min
                1Q
                     Median
                                   3Q
                                           Max
-10.7927
          -3.3161
                    -0.7927
                               3.0914
                                       16.1580
Coefficients:
               Estimate Std. Error t value Pr(>|t|)
(Intercept) 14.8748145
                                     14.108
                                               <2e-16 ***
                         1.0543301
             -0.0006571
                         0.0119165
                                     -0.055
                                                0.956
proto
restecg
              0.1703404
                         0.9831619
                                      0.173
                                                0.863
dig
             -2.1530704
                         2.6764216
                                     -0.804
                                                0.423
prop
              1.2718279
                          1.5972216
                                      0.796
                                                0.427
              0.6342939
                                      0.404
                                                0.687
nitr
                          1.5715709
             -1.5831511
                          1.7652196
                                     -0.897
                                                0.372
pro
             -0.1302669
                         2.0907202
diuretic
                                     -0.062
                                                0.950
Signif. codes:
                              0.001
                                              0.01
                                                            0.05
                                                                          0.1
Residual standard error: 5.383 on 120 degrees of freedom
  (771 observations deleted due to missingness)
Multiple R-squared:
                      0.016,
                                  Adjusted R-squared: -0.0414
F-statistic: 0.2787 on 7 and 120 DF,
                                        p-value: 0.9612
Response rldv5e :
lm(formula = rldv5e ~ proto + restecg + dig + prop + nitr + pro +
    diuretic, data = datall)
Residuals:
                     Median
     Min
                1Q
                                   3Q
                                            Max
-11.1533
          -3.5409
                    -0.4798
                               2.7664
                                       14.0371
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                                    14.284
                                              <2e-16 ***
(Intercept) 14.969428
                          1.048021
             -0.006529
                          0.011845
                                    -0.551
                                               0.583
proto
              0.220336
                         0.977279
                                     0.225
                                               0.822
restecg
dig
             -2.219224
                          2.660406
                                    -0.834
                                               0.406
              1.174742
                          1.587664
                                     0.740
                                               0.461
prop
             -0.604272
                          1.562167
                                     -0.387
                                               0.700
nitr
pro
              0.779970
                          1.754657
                                     0.445
                                               0.657
              3.238914
                          2.078210
diuretic
                                     1.559
                                               0.122
Signif. codes:
                              0.001
                                              0.01
                                                            0.05
                                                                          0.1
Residual standard error: 5.351 on 120 degrees of freedom
  (771 observations deleted due to missingness)
Multiple R-squared:
                      0.03959,
                                  Adjusted R-squared: -0.01643
F-statistic: 0.7067 on 7 and 120 DF,
                                        p-value: 0.6663
```

2.3 Question 3

Due to that each dataset is missing different variables from the data, we have decided that in order to maximise the amount of variables we have, we are going to be using each dataset independent of the others.

For each dataset we removed the dummy variables and variables that were missing at least a percentage of data. This percent was different for each data set and we were aiming for approximate at least double the number of observations to the number of variables.

2.3.1 Cleveland

After removing dummy variables and variables with at least 90% NA data, we are left with 45 variables and 201 observations.

Cloveland	l variance	inflation	factor
Слеуегалс	i variance	пппаллоп	Tactor

age	sex	$_{\mathrm{cp}}$	trestbps	htn	chol	cigs	years	
2.070591	2.379469	1.683710	2.935706	1.734144	1.326342	2.346224	2.315459	
fbs	famhist	restecg	$_{ m ekgmo}$	ekgday	ekgyr	dig	prop	
1.281244	1.291443	1.338021	14.903816	3.357399	78.992867	1.296383	1.679766	
nitr	pro	diuretic	thaldur	thaltime	met	thalach	thalrest	
1.546570	1.415979	1.480903	9.549788	1.422540	10.328475	2.868773	1.713892	
tpeakbps	$_{ m tpeakbpd}$	trestbpd	exang	xhypo	oldpeak	slope	${\tt rldv5e}$	
2.829387	2.173463	2.785971	1.734917	1.870852	2.831028	2.291928	1.557587	
ca	thal	cmo	cday	cyr	$_{ m lmt}$	ladprox	laddist	
1.841289	2.051953	15.389866	3.413846	80.511913	1.401270	1.496650	1.526869	
cxmain	om1	rcaprox	rcadist					
1.543251	1.789705	1.764053	1.835745					

From the variance inflation factor we see the variables **ekgmo**, **ekgyr**, **cmo** and **cyr** are highly collinear with other variables in the model.

Scree plot - Cleveland

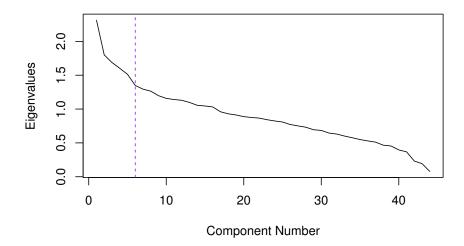


Figure 1: Scree plot for PCA of Cleveland

From the scree plot in Figure 1 we see that we keep 6 components.

We have the loadings of each components as follows.

Cleveland PCA loadings

Loadings:

Comp.1 Comp.2 Comp.3 Comp.4 Comp.5 Comp.6 Comp.7 Comp.8 Comp.9 Comp.10

age 0.192 -0.196 0.167 -0.122 0.1	
$-0.195 0.306 0.193 \qquad -0.33 $	
cp 0.208 0.384	-0.116
trestbps $0.133 - 0.144 - 0.297 \ 0.222 \ 0.107 \ 0.119 \ -0.149$	
htn $0.222 -0.189 0.390 0.117$	
-0.184 0.184 0.2	
cigs $-0.200 0.181 0.231 -0.292 -0.128 -0.28$	
-0.189 0.145 0.223 -0.330 0.138 -0.138	56
fbs $-0.128 0.143 -0.214 0.132$	0.129
	62 -0.136
restecg $-0.103 -0.132$ $-0.128 0.238$	
ekgmo -0.244 -0.433 -0.109 0.220 -0.161 -0.109	44
0.384 0.326 0.255 0.298 -0.1384 0.326 0.255 0.298 -0.1384 0.326 0.255 0.298 -0.1384 0.326 0.255 0.298 -0.1384 0.326 0.255 0.298 -0.1384 0.326 0.255 0.298 -0.1384 0.326 0.255 0.298 -0.1384 0.326 0.255 0.298 -0.1384 0.326 0.255 0.298 -0.1384 0.326 0.255 0.298 -0.1384 0.326 0.255 0.298 -0.1384 0.326 0.255 0.298 -0.1384 0.255 0.298 -0.2884 -0.1384 0.2884 -0.1384 -	.09
	29 - 0.212
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	
prop $0.102 0.107 0.162 -0.263 -0.247 0.105$	0.173
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	
pro 0.236 -0.115 0.154 -0.2	
diuretic $0.128 - 0.417$ -0.1	
thaldur -0.301 -0.109 0.237 0.125 0.184 -0.149	0.200
	59 - 0.189
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0.100
	06 - 0.141
	94 - 0.113
the lattest 0.225 0.297 0.221 0.145 0.145 0.145 0.145 0.145	0.110
tpeakbpd $-0.167 -0.330 \ 0.142$ $-0.128 \ 0.161 \ -0.1$	48 _0 150
	67 - 0.194
	0.154 0.154 0.157
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	
•	-0.169 -0.263
	-0.205
	11 0 051
$\begin{bmatrix} ca & 0.213 & 0.113 & -0.124 & 0.283 & 0.2\\ ca & 0.211 & 0.162 & 0.167 & 0.102 & 0.283 & 0.$	
thal $0.231 - 0.163 \ 0.167 \ 0.102 \ -0.163 \ 0.167 \ 0.102$	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	
	30 -0.218
lmt 0.130 -0.106 0.132	-0.126
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	32
laddist 0.206 0.107 -0.114 0.254	
cxmain 0.189 0.150 0.104 0.1	11 0.201
om1 0.249 -0.108 0.202	
<u>-</u>	81 - 0.291
rcadist 0.196 0.103 0.183 -0.130	0.250

We see that the first principle component is mostly formed of thaldur, thalach, met and oldpeak variables.

The second principle component is mostly formed of cyr and ekgyr variables.

The third principle component is mostly formed of $\mathbf{tpeakbpd}$, $\mathbf{trestbpd}$, \mathbf{sex} and $\mathbf{trestbps}$ variables.

The fourth principle component is mostly formed of **ekgmo** and **cmo** variables.

The fifth principle component is mostly formed of cday, ekgday, years and cigs variables.

The sixth principle component is mostly formed of diuretic, htn, ekgday

2.3.2 Hungary

After removing dummy variables and variables with at least 79% NA data, we are left with 36 variables and 88 observations.

Hungary variance inflation factor

age	sex	painloc	painexer	relrest	ср	trestbps	
2.434590	2.080449	2.654746	10.046548	6.565678	19.690793	4.275217	
htn	chol	$_{ m fbs}$	restecg	$_{ m ekgmo}$	ekgday	ekgyr	
1.861599	2.510843	2.038199	1.494730	26.201141	3.202566	179.069024	
prop	$\operatorname{nit} \mathbf{r}$	pro	diuretic	proto	thaldur	thaltime	
4.687494	8.190981	9.216954	3.508473	40.100317	160.858151	159.083733	
met	thalach	thalrest	$_{ m tpeakbps}$	$_{ m tpeakbpd}$	${ m trestbpd}$	exang	
8.256667	3.592979	1.974234	3.419070	3.548859	3.556353	3.194635	
oldpeak	slope	rldv5	rldv5e	cmo	cday	cyr	
2.059364	2.928694	9.159900	8.276601	26.609872	2.619470	173.894964	

From the variance inflation factor we see that the variables **painexer**, **cp**, **ekgmo**, **ekgyr**, **proto**, **thaldur**, **thaltime**, **cmo** and cyr are highly collinear with other variables in the model.

Scree plot - Hungary

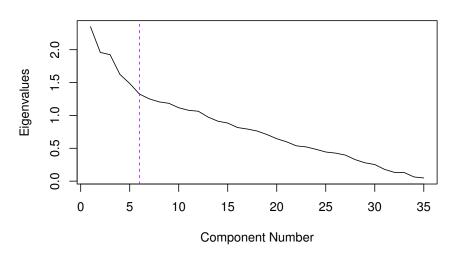


Figure 2: Scree plot for PCA of Hungary

From the scree plot in Figure 2 we see that we keep 6 components.

We have the loadings of each components as follows.

Hungary PCA loadings

					8017 1 017					
Loadings:										
	Comp.1	Comp.2	Comp.3	Comp.4	Comp.5	Comp.6	Comp.7	Comp.8	Comp.9	Comp.10
age	0.162		0.184		-0.253		-0.105	-0.185	-0.114	0.137
sex		-0.144	-0.164	-0.236					0.232	
painloc	0.143		-0.261	-0.112	0.116					0.214
painexer	0.212		-0.335			-0.146				
relrest	0.228		-0.332					-0.159		-0.108
ср	0.229		-0.357			-0.163		-0.115		
trestbps	0.213		0.179	-0.290	0.113			-0.214		0.198
htn		-0.160	0.101			0.247		0.125	0.230	0.214
chol				-0.139	-0.207	-0.105		0.186	-0.529	
fbs		-0.170		-0.127	-0.193	0.168		0.265	-0.304	-0.195
restecg									-0.135	0.304
ekgmo	-0.191		-0.177		-0.276		0.344	-0.380		
ekgday			-0.108		-0.254	0.479	-0.110		0.255	
ekgyr	0.126	-0.312	0.189			-0.181	0.237		0.101	-0.326
prop	0.132	-0.253		0.301	0.117		0.112			0.194
nitr		-0.286		0.402						0.163

pro		-0.309		0.355					-0.105	0.119	
diuretic			0.129	-0.101	0.149		0.275	0.123	0.377	0.281	
proto	-0.312	-0.277	-0.136	-0.121							
thaldur	-0.305	-0.277	-0.135	-0.130							
thaltime	-0.303	-0.270	-0.138	-0.128			-0.111			0.113	
met	-0.306	-0.227					-0.192				
thalach	-0.259			-0.135	0.126		0.376	0.177	-0.142		
thalrest				-0.126			0.539	0.233	-0.141	0.269	
tpeakbps		-0.225		-0.292		0.170		-0.264			
tpeakbpd		-0.191	0.271	-0.231		0.134		-0.199			
trestbpd	0.157		0.155	-0.301	0.137			-0.207	-0.150	0.256	
exang	0.237		-0.216	-0.140						-0.175	
oldpeak		0.113		-0.168	0.217	0.146			0.259	-0.200	
slope	0.156		-0.245			0.280		0.287			
rldv5	-0.147	0.126			0.439	0.283		-0.130	-0.232	-0.109	
rldv5e	-0.128			0.116	0.444	0.289		-0.179	-0.172	-0.129	
cmo	-0.175		-0.194		-0.284	0.103	0.297	-0.395			
cday		-0.123			-0.229	0.387	0.133	0.142		-0.211	
cyr	0.130	-0.316	0.179			-0.181	0.222			-0.331	

We see that the first principle component is mostly formed of proto, met, thaldur and thaltime variables.

The second principle component is mostly formed of cyr, ekgyr and pro variables.

The third principle component is mostly formed of cp, painexer and relrest variables.

The fourth principle component is mostly formed of **nitr** and **pro** variables.

The fifth principle component is mostly formed of ${\bf rldv5e}$ and ${\bf rldv5}$ variables.

The sixth principle component is mostly formed of ekgday and cday variables.

2.3.3 Longbeach

After removing dummy variables and variables with at least 50% NA data, we are left with 50 variables and 94 observations.

Longbeach variance inflation factor

			ongocach van					
age	sex	painloc	painexer	$\operatorname{relrest}$	$_{\mathrm{cp}}$	trestbps	htn	
3.228090	1.931427	2.577184	7.718893	6.621863	14.044802	3.617851	2.921354	
chol	smoke	cigs	years	$_{ m fbs}$	famhist	restecg	$_{ m ekgmo}$	
2.045184	4.098390	3.361309	4.794619	3.248168	2.369061	2.192354	3.658305	
ekgday	ekgyr	dig	prop	$\operatorname{nit} \mathbf{r}$	pro	diuretic	proto	
2.449554	39.950248	2.509731	2.528256	1.901292	1.732049	2.476101	4.533802	
thaldur	met	thalach	thalrest	$_{ m tpeakbps}$	$_{ m tpeakbpd}$	${\tt trestbpd}$	exang	
18.058001	16.434757	3.931213	2.659439	3.784661	2.735284	3.161172	2.222555	
xhypo	oldpeak	rldv5	rldv5e	cmo	cday	cyr	$_{ m lmt}$	
2.096734	4.015243	7.661567	6.930116	4.934749	2.272059	43.093455	1.678378	
ladprox	laddist	diag	$_{\rm cxmain}$	ramus	om1	om2	rcaprox	
2.126046	1.837113	1.766507	1.847673	2.269851	2.527439	2.913807	2.246981	
rcadist								
2.142703								

From the variance inflation factor we see that the variables **cp**, **ekgyr**, **thaldur**, **met** and **cyr** are highly collinear with other variables in the model.

Scree plot - Longbeach

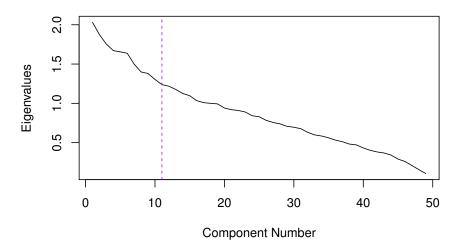


Figure 3: Scree plot for PCA of Longbeach

From the scree plot in Figure 3 we see that we keep 11 components.

We have the loadings of each components as follows.

Longbeach PCA loadings

Loadings: Comp.1 Comp.2 Comp.3 Comp.4 Comp.5 Comp.6 Comp.7 Comp.8 Comp.9 Co	1.0
Comp.1 Comp.2 Comp.3 Comp.4 Comp.5 Comp.6 Comp.7 Comp.8 Comp.9 Co	1.0
	omp.10
age -0.204 0.197 -0.182 -0.205	
	0.146
painloc $-0.133 0.209 \qquad 0.255 \qquad 0.136 -0.105$	
painexer $-0.192 -0.223$ $0.288 0.188 -0.162$	
relrest $-0.181 -0.203$ $0.114 0.314$ 0.197	
cp $-0.181 -0.276$ $0.216 0.288 -0.128 0.184$	
trestbps -0.196 $0.310 -0.133$ -0.202	
htn $0.313 - 0.134 - 0.219$	0.106
	-0.194
smoke 0.160 -0.191 -0.334	-0.186
-0.250 -0.320	0.240
years $0.155 -0.117 -0.133 -0.344$ 0.103	
fbs $0.111 0.196 -0.168 -0.154$	0.315
	-0.316
8	0.229
ekgmo $-0.189 -0.134$ 0.178 -0.289	
	0.166
ekgyr -0.357 0.130 -0.161 -0.127 -0.195	
dig 0.166 $-0.111 -0.241$ $0.111 0.227 -0.111$	
prop $0.137 -0.106$ $0.115 0.179 -0.179 0.135 -0.135$	-0.116
nitr 0.123 -0.215 0.181 -0.255 -0.139	
pro $-0.177 -0.253$ $0.170 -0.112$	
diuretic -0.140 0.162 -0.221 0.106 0.187 -0.187	-0.109
proto $-0.288 0.135 -0.240 \qquad \qquad -0.102 \qquad \qquad -0.171$	
thaldur 0.402 0.102 0.153 -0.190 $-$	-0.113
met 0.353 0.126 0.131 0.237 -0.172	
thalach 0.151 -0.129 0.323 0.279 0.172	
thalrest 0.349 0.169 0.119	
1 1	0.158
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	
trestbpd $0.200 -0.181 -0.154 0.135$	

1	0 405	0.000				0.44			0.440	0.4-4
exang	-0.105	-0.260				-0.14)	-0.110	-0.174
xhypo	-0.128				0.153				-0.148	
oldpeak	-0.250					-0.208				-0.274
rldv5	-0.238				-0.118		0.280		0.249	-0.137
rldv5e	-0.238				-0.191		0.255		0.224	-0.153
cmo		-0.244 -	-0.131 (0.117		-0.12	4 0.210)	-0.291	
cday					0.135	0.129	9 0.160	-0.310		0.299
cyr	-0.352	0.156 -	-0.160 $-$	0.134			-0.185	õ		
lmt	-0.104						-0.149	0.166		
ladprox		-0.103	_	0.127	0.229	-0.22	0			0.140
laddist						0.123		2	-0.233	
diag	-0.105				-0.109			0.384		0.174
cxmain	0.200	-0.126			0.200	-0.23	3	0.00-	-0.118	
ramus		0.103	0.113 -	0.139	0.140	0.20	-0.114	4 - 0.232	0.110	-0.116
om1		-0.105		0.144	0.110		0.11	0.202	-0.347	-0.161
om2		0.105		0.144 0.217	0.100	0.13	Q	-0.310	0.041	-0.142
rcaprox		-0.139		0.217 0.118	0.100	-0.34		-0.310 -0.113		-0.142
1 *	0.106	-0.139	_		-0.192				0.177	0.170
rcadist	-0.196	C 10	C 10				0.131		-0.177	0.172
	Comp.11	Comp. 12	Comp.13			mp.15		Comp.17		
age	-0.163		-0.136	0.11			0.110		0.185	-0.230
sex		-0.264		0.12				-0.206	-0.150	-0.363
painloc				0.21	10 0	.397			-0.138	-0.199
painexer							-0.246			
relrest	-0.147							0.229	0.114	
ср							-0.138			
trestbps	0.112		-0.129	-0.10	01					
htn	-0.123		0.241	-0.19	96 0	.100	0.102			
chol		0.180	-0.233					0.113	-0.105	-0.178
smoke	-0.107	0.100	0.200					0.203	0.100	0.1.0
cigs	0.101		-0.160		0	.131		0.200	-0.118	0.198
years			-0.264		U	.101		0.156	0.211	0.130
1 "	0.100	0.022	-0.204	0.16	20 0	176		0.130		0.050
fbs	-0.182	0.233		0.13		.176		0.110	0.135	0.250
famhist	0.400	0.269		0.19	99 0	.119	0.04.0	-0.113		0.209
restecg	-0.169						-0.216	-0.139		-0.238
ekgmo	-0.384	0.110	-0.184	-0.20		0.258				
ekgday	0.168	0.147		0.17	72 0	.161				
ekgyr		0.133					0.168	-0.111		
dig			0.121	-0.14			-0.255	-0.247		-0.129
prop		0.242	-0.265	-0.25	55 - 0	0.141	-0.265		-0.185	-0.188
nitr				0.32	-(22 - (0.116			-0.135	
pro		0.168	0.127	0.20			-0.188	-0.190		
diuretic	-0.194		0.170	-0.13		.170	0.322	0.248	0.107	-0.126
proto	-				ŭ			-0.156		-
thaldur	-0.152				0	.114	-0.138	0.111	-0.183	-0.152
met	-0.132						-0.230	0.215	-0.143	-0.166
thalach	3.100			0.13			0.230 0.102	5.210	0.140	0.111
thalrest		0.183		0.10		0.220	0.102 0.151	-0.344	0.430	-0.102
tpeakbps	-0.110			0.16		0.240	0.101	0.044	0.162	
		-0.145					0.252	0.155	0.102	-0.112
tpeakbpd	0.102	-0.105	0.145	0.14		0.169	0.353	-0.157	0.104	0.114
trestbpd	0.371	0.130	-0.147	-0.21		0.110	0.10-	-0.134	-0.124	0.114
exang	0.206	-0.116	-0.215	0.20			-0.106			
xhypo		0.349		-0.15		.253	0.155		0.123	
oldpeak		-0.159	0.101		0	.100			0.143	0.175
rldv5		-0.105								0.119
rldv5e					-(0.108		0.104		
cmo	-0.337		-0.142					-0.116		
cday	0.209	0.127			0	.122		0.258	-0.119	
cyr		0.146			· ·		0.164			
lmt		-0.226	-0.455	-0.24	45		0.126			
ladprox		-0.220 -0.137	0.224	0.2	10		0.120	0.117	-0.310	0.236
ladbrox		-0.137	0.224					0.111	-0.510	0.230

laddist	0.331	-0.207		-0.191	0.182	-0.167	-0.168	0.349	-0.174	
diag		-0.262						-0.327	0.139	
cxmain	0.104	0.130		0.137	-0.356	-0.184	0.350	0.191	-0.105	
ramus	-0.196	-0.260		0.165	0.104	-0.133	-0.169	0.115	0.279	
om1			0.313	-0.280		0.122		-0.129		
om2						-0.257	-0.104		0.209	
rcaprox				0.184	0.156			-0.297		
rcadist		0.124	0.214				-0.106			

We see that the first principle component is mostly formed of **ekgyr**, **cyr** and **proto** variables.

The second principle component is mostly formed of thaldur, met variables.

The third principle component is mostly formed of htn, trestbps and cigs variables.

The fourth principle component is mostly formed of years, smoke and cigs variables.

The fifth principle component is mostly formed of thalrest, thalach and painexer variables.

The sixth principle component is mostly formed of **rcaprox**, **relrest** and **cp** variables.

The seventh principle component is mostly formed of ekgday, rldv5 and thalach variables.

The eight principle component is mostly formed of diag, cday and om2 variables.

The ninth principle component is mostly formed of **om1**, **cmo** and **ekgmo** variables.

The tenth principle component is mostly formed of famhist, fbs and cday variables.

The eleventh principle component is mostly formed of ekgmo, trestbpd, cmo and laddist variables.

2.3.4 Switzerland

After removing dummy variables and variables with at least 13% NA data, we are left with 39 variables and 101 observations.

Switzerland	variance	inflation	factor
D W I UZCI I ali a	variance	111111111111111111111111111111111111111	Ideooi

age	sex	painloc	painexer	relrest	$_{\mathrm{cp}}$	trestbps	restecg
2.369562	1.738028	3.014841	5.301607	5.348634	5.703978	3.512376	2.391685
$_{ m ekgmo}$	ekgday	ekgyr	dig	prop	\mathtt{nitr}	pro	diuretic
15.412883	4.698930	11.069307	1.660195	2.140460	2.363016	2.250616	1.810968
thaldur	thalach	thalrest	$_{ m tpeakbps}$	$_{ m tpeakbpd}$	${ m trestbpd}$	exang	xhypo
4.680438	4.923162	3.031050	4.382267	2.124042	2.928830	1.982196	2.170784
oldpeak	cmo	cday	cyr	lmt	ladprox	laddist	diag
2.282318	17.422769	4.254917	6.008334	1.696866	2.296964	1.815151	1.777471
$_{ m cxmain}$	ramus	om1	om2	rcaprox	rcadist		
2.269139	2.183169	2.849526	1.660434	1.868517	1.905493		

From the variance inflation factor we see that the variables **ekgmo**, **ekgyr** and **cmo** are highly collinear with other variables in the model.

Scree plot - Switzerland

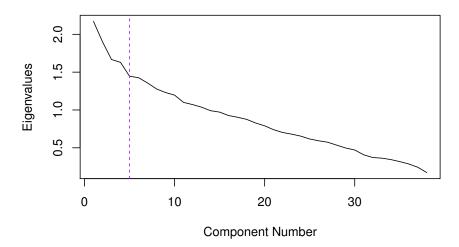


Figure 4: Scree plot for PCA of Switzerland

From the scree plot in Figure 4 we see that we keep 5 components.

We have the loadings of each components as follows.

Switzerland PCA loadings

						A loading				
Loadings:										
	Comp. 1	Comp. 2								Comp. 10
age			0.366		0.115		-0.106	0.158		-0.138
sex		-0.107			-0.238			-0.326	0.118	
painloc			-0.145							0.160
painexer							0.160			
relrest			-0.187				0.147	0.144		
$^{\mathrm{cp}}$			-0.203							
trestbps	-0.154							0.169	0.116	
restecg		0			-0.182			0.101	0.202	-0.451
ekgmo	-0.337	0.199				-0.168				
ekgday			-0.219		-0.172	0.420	-0.178	0.222		
ekgyr	0.316	-0.219	0.142	-0.179			0.171			
dig				0.140		0.167	0.281	0.187		0.342
prop		-0.227		0.129		-0.201	-0.174		0.204	0.143
nitr	0.137	-0.214				-0.307		0.181	0.332	
pro		-0.111	0.106		-0.198	-0.331	-0.201	0.325		0.104
diuretic	-0.105	-0.119	0.133	0.113	-0.114	-0.201	-0.162	0.173	-0.162	
thaldur	0.231			-0.107	-0.355	-0.161	0.192	-0.166		0.214
thalach	0.184	0.172	-0.191	-0.187	-0.242		0.247	0.232	-0.236	
thalrest		0.269	-0.156				0.222	0.411	-0.151	-0.160
tpeakbps		0.215	0.117	-0.372	-0.176			0.197		
tpeakbpd	-0.116	0.125	0.148	-0.352		0.100			0.189	
trestbpd	-0.206	0.106	0.199	-0.179		0.214	-0.123		0.163	0.152
exang	-0.188					0.153	-0.315		-0.251	-0.117
xhypo			0.114	0.170	0.226	0.229	0.290	0.269		0.182
oldpeak		-0.110		-0.298			0.151		-0.205	-0.187
cmo	-0.345	0.185			-0.128	-0.128		-0.109		
cday			-0.189							
	0.275							-0.138		
lmt			-0.142				0.135		0.166	-0.333
ladprox	-0.150							0.122		-0.195
laddist		-0.150			-0.348					0.198

diag		-0.187	0.196		-0.179			-0.32	23	
cxmain	-0.102	-0.128			-0.190	0.219		-0.208	-0.366	
ramus	-0.139	-0.107	0.237	0.129			0.108	-0.31	11	
om1		-0.186	0.154	0.153	-0.247		0.315	0.12	24 - 0.149	
om2		-0.161	0.212					-0.33	38	
rcaprox	-0.189		0.119		0.159		0.133	0.11	6 0.156	
rcadist	-0.106			0.137	-0.255		0.277	0.22	20	

We see that the first principle component is mostly formed of cmo, ekgmo, ekgyr and cyr variables.

The second principle component is mostly formed of **cp**, **thalrest**, **painloc**, and **painexer** variables.

The third principle component is mostly formed of **trestbps** and **age** variables.

The fourth principle component is mostly formed of **tpeakbps**, **tpeakbpd** and **oldpeak** variables.

The fifth principle component is mostly formed of ${f thaldur}$ and ${f laddist}$ variables.

2.4 Question 4

In order to distinguish patients based on their disease through discriminant analysis, I had to create four models, one for each of the datasets.

2.4.1 Cleveland

```
Call:
lda(num ~~ ., ~ data = clevdata)
Prior probabilities of groups:
0.50248756 \ \ 0.18407960 \ \ 0.12935323 \ \ 0.12935323 \ \ 0.05472637
Group means:
                                cp trestbps
        age
                                                     htn
                                                              chol
                                                                         cigs
                                                                                  vears
                    sex
0 \ 53.52475 \ 0.5247525 \ 2.841584 \ 128.7921 \ 0.5544554 \ 249.3465 \ 14.52475 \ 13.77228
1 \ 55.86486 \ 0.8918919 \ 3.459459 \ 132.7838 \ 0.7027027 \ 252.4324 \ 21.67568 \ 17.27027
2\ 58.00000\ 0.8076923\ 3.692308\ 133.0385\ 0.7307692\ 274.0000\ 15.30769\ 15.15385
3 \ 56.03846 \ 0.8076923 \ 3.807692 \ 136.7308 \ 0.4230769 \ 252.1923 \ 15.88462 \ 12.73077
4\ 59.54545\ 0.9090909\ 3.636364\ 140.0000\ 0.6363636\ 233.5455\ 26.27273\ 22.63636
                             restecg
          fbs
                 famhist
                                          ekgmo
                                                    ekgday
                                                               ekgvr
0\ 0.14851485
               0.5445545 1.0000000 5.900990 14.89109 82.30693 0.06930693
1 \quad 0.08108108 \quad 0.6756757 \quad 1.1351351 \quad 6.756757 \quad 13.29730 \quad 82.02703 \quad 0.000000000
2\ 0.19230769\ 0.8076923\ 0.9230769\ 5.192308\ 12.34615\ 82.38462\ 0.00000000
3\ 0.23076923\ 0.5384615\ 1.1538462\ 5.692308\ 16.80769\ 82.03846\ 0.00000000
4\ 0.09090909\ 0.5454545\ 1.6363636\ 7.636364\ 14.18182\ 82.09091\ 0.00000000
                    nitr
                                        diuretic
                                                    thaldur thaltime
        prop
                                  pro
                                                                              met
                                                                                    thalach
0\ \ 0.2772277\ \ 0.2079208\ \ 0.11881188\ \ 0.1386139\ \ 8.836634\ \ 4.271287
                                                                       10.227723 \ 157.2376
  0.3783784 \ 0.3513514 \ 0.10810811 \ 0.1081081 \ 8.294595
                                                             6.027027
                                                                         9.837838 145.3784
2\ 0.5769231\ 0.3076923\ 0.15384615\ 0.1153846\ 7.873077
                                                             6.215385
                                                                         8.807692 132.3846
3\ 0.3846154\ 0.4230769\ 0.03846154\ 0.1923077\ 6.707692\ 4.642308
                                                                         8.076923 132.9231
4\ 0.3636364\ 0.2727273\ 0.000000000\ 0.00000000\ 6.027273\ 4.863636
                                                                         7.363636 139.4545
  thalrest tpeakbps tpeakbpd trestbpd
                                                 exang
                                                              xhypo
                                                                       oldpeak
0\ 77.28713\ 170.0891\ 78.96040\ 84.23762\ 0.1782178\ 0.00990099\ 0.7435644\ 1.504950
1 \ 72.37838 \ 172.3243 \ 77.59459 \ 85.05405 \ 0.5405405 \ 0.02702703 \ 1.2864865 \ 1.702703
2\ 69.76923\ 158.4615\ 81.69231\ 85.26923\ 0.5769231\ 0.07692308\ 1.7653846\ 1.961538
3\ 75.11538\ 160.2692\ 79.26923\ 87.65385\ 0.6538462\ 0.07692308\ 2.2884615
4 \quad 74.63636 \quad 165.4545 \quad 84.09091 \quad 86.63636 \quad 0.5454545
                                                        0.000000000 2.0272727
                                                                                 2.000000
     rldv5e
                             thal
                                         cmo
                                                  cday
                                                              cyr
                                                                    ladprox
                                                                              laddist
                     ca
0\ 122.9010\ 0.3267327\ 3.792079\ 5.811881\ 15.22772\ 82.30693\ 1.000000\ 1.000000
1 \ 131.3243 \ 0.8648649 \ 5.432432 \ 6.756757 \ 14.67568 \ 82.02703 \ 1.270270 \ 1.324324
2\ 127.0000\ 1.3076923\ 6.115385\ 5.153846\ 13.61538\ 82.42308\ 1.423077\ 1.384615
3\ 138.9231\ 1.4230769\ 6.538462\ 5.923077\ 16.50000\ 82.07692\ 1.461538\ 1.730769
  107.8182 \ 1.4545455 \ 6.181818 \ 7.636364 \ 15.36364 \ 82.00000 \ 1.272727 \ 1.545455
    cxmain
                  om1
                        rcaprox
                                   rcadist
0 \ 1.000000 \ 1.000000 \ 1.000000 \ 1.000000
1 \quad 1.135135 \quad 1.081081 \quad 1.216216 \quad 1.108108
2\ 1.384615\ 1.346154\ 1.576923\ 1.230769
3 \ 1.500000 \ 1.730769 \ 1.461538 \ 1.576923
4 \quad 1.545455 \quad 1.545455 \quad 1.454545 \quad 1.272727
Coefficients of linear discriminants:
                      LD1
                                      LD2
                                                      LD3
                                                                      LD4
          -0.0064021152 \quad -0.0425071101
                                             0.017806402
                                                           -1.388222e-02
age
                                                           -1.080167e-01
           0.2188951081 - 0.8385787717
                                             0.966289676
sex
           0.0836865201 - 0.0684255751
                                             0.213747047
                                                           -2.619771e-01
ср
trestbps
           0.0086722361 - 0.0110214859
                                             0.009667569
                                                            7.267368e-03
htn
            0.1339883778 -0.5852997536
                                           -0.309526408
                                                            3.116354e-01
           -0.0001853615 \quad -0.0026943630
                                           -0.007365030
chol
                                                            1.378357e-03
```

```
0.0014297509
                         -0.0040736758
                                         0.023693179
                                                       -5.710203e-03
cigs
years
          -0.0058677471
                          0.0064698922
                                         -0.010415602
                                                       2.424284e-02
fbs
                                                       1.160757e - 01
          -0.0677560105
                          0.4462514441
                                        -0.809205331
famhist
                                                       -7.834152e-03
          -0.1536120593
                         -0.6331094392
                                        -0.046988498
restecg
          0.0020724640
                          0.0306173919
                                                       1.242487e-01
                                         0.343424560
ekgmo
          -0.0333931677
                         -0.1894708072
                                         0.003215433
                                                       1.790893e-01
                                                       -1.967420e-02
ekgday
           0.0307768259
                          0.0202459475
                                         0.004269374
ekgyr
           0.2849909378
                         -0.1910807911
                                         3.244719860
                                                       3.043414e+00
                                                       4.891422e-01
dig
          -0.5880796669
                          1.2356661900
                                         -0.935588867
prop
          -0.2044468618
                         -0.4228151708
                                         0.314419800
                                                       2.952549e-01
nitr
          -0.0500314492
                         -0.1132297678
                                        -0.008236496
                                                       -6.704832e-01
pro
          -0.0422771375
                                                       -7.934840e-02
                         -0.3051736743
                                        -0.212490269
diuretic
          0.0903449725
                         -0.1880557316
                                                       -3.147873e-01
                                        -0.424110167
thaldur
           0.0123720933
                         -0.0940568662
                                        -0.296638460
                                                       2.257168e-01
thaltime
          0.0352787900
                         -0.1062383655
                                         0.033833393
                                                       2.174663e-03
          -0.0227104963
                          0.0333032838
                                         0.052992717
                                                       -2.510038e-01
met
thalach
          0.0004083536
                          0.0016079361
                                         0.014067133
                                                       -2.553563e-05
thalrest
         -0.0143560702
                          0.0142803750
                                         0.001611765
                                                       -7.030841e-03
tpeakbps
          -0.0071065254
                         -0.0069409621
                                         0.008450720
                                                       -1.586376e-02
          0.0126391705
                          0.0036640956
tpeakbpd
                                        -0.017755491
                                                       4.596684e-02
trestbpd
                                                      -3.778290e-02
         -0.0092676913
                          0.0131619284
                                        -0.014903990
exang
                                        -0.162847360
                                                       -3.792109e-01
           0.3742483643
                         -0.6846868868
xhypo
          -0.3070163922
                         -0.9550240951
                                        -0.837879117
                                                       -9.084565e-01
oldpeak
                                                       7.428472\,\mathrm{e}\!-\!02
          -0.0507070406
                          0.3552810935
                                        -0.016595052
slope
           0.2158763397
                         -0.3990518860
                                         0.152776941
                                                       1.517427e-01
rldv5e
          -0.0016341882
                         -0.0009474799
                                         -0.004657443
                                                       -6.008307e-03
ca
           0.0604185429
                         -0.1322843859
                                         0.044212892
                                                       3.194839e-02
thal
                                                       -1.153858e-01
           0.1790094224
                         -0.0163313489
                                        -0.036193049
cmo
           0.0652759054
                          0.1570432167
                                         0.099289729
                                                       -1.540472e-01
          -0.0202700434
                                                       1.056202e-02
cdav
                          0.0109527280
                                         0.006883157
          -0.2318889441
                          0.0552735975
                                        -3.287530952
                                                       -2.820889e+00
cyr
ladprox
           2.1449671081
                         -0.7520705684
                                                       -3.504782e-01
                                        -0.456454141
laddist
           2.2474742138
                          0.3244757867
                                         0.480884470
                                                       -6.849638e-01
cxmain
           2.4577588717
                          0.6761926661
                                         0.110008133
                                                       9.377253e-01
om1
                                                       6.720648e - 01
           2.3487229073
                          1.7069044343
                                        -0.588196080
rcaprox
                         -0.9443404888
                                        -0.769549935
                                                       8.529602e-01
           2.5240275251
rcadist
           1.8594484941
                          0.6017481881 - 0.073459411
                                                      -4.100481e-01
Proportion of trace:
```

LD1

LD2

 $0.9090 \ 0.0477 \ 0.0268 \ 0.0164$

LD3

LD4

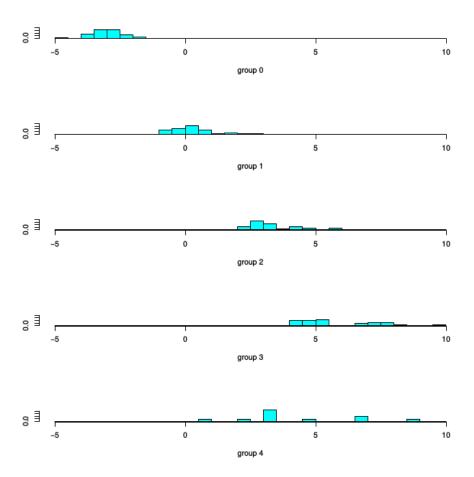


Figure 5: Histergram for discriminant analysis of Cleveland

scatterplot for Clevland model

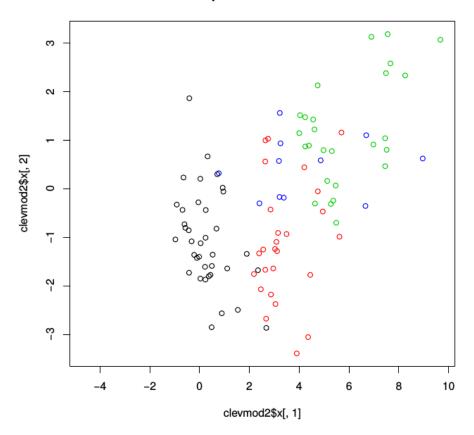


Figure 6: Scatter plot for discriminant analysis of Cleveland

2.4.2 Hungary

```
Call:
lda(num ~~.,~data = ex3dathun)
Prior probabilities of groups:
                               2
                    1
0.2954545 \ \ 0.2045455 \ \ 0.1590909 \ \ 0.2272727 \ \ 0.1136364
Group means:
                         painloc painexer
                                                relrest
                                                                cp trestbps
        age
                   sex
0\ 51.53846\ 0.4615385\ 0.8461538\ 0.4230769\ 0.4230769\ 2.884615\ 131.6923\ 0.3076923
1\ \ 47.72222\ \ 0.8333333\ \ 1.0000000\ \ 0.8333333\ \ 0.8888889\ \ 3.722222\ \ 130.9444\ \ 0.5000000
2\ 51.07143\ 0.9285714\ 1.0000000\ 1.00000000\ 0.9285714\ 4.000000\ 145.8571\ 0.7142857
3 \ 51.15000 \ 0.9000000 \ 0.9500000 \ 0.7000000 \ 0.7000000 \ 3.400000 \ 140.8000 \ 0.4000000
4 \ 50.40000 \ 0.8000000 \ 1.0000000 \ 0.9000000 \ 1.0000000 \ 3.900000 \ 138.5000 \ 0.5000000
       chol
                   fbs
                          restecg
                                      ekgmo
                                               ekgdav
                                                          ekgvr
                                                                        prop
0\ 246.9615\ 0.00000000\ 0.2307692\ 6.192308\ 14.96154\ 85.03846\ 0.07692308\ 0.11538462
2\ 288.4286\ 0.2142857\ 0.1428571\ 4.642857\ 16.07143\ 85.57143\ 0.14285714\ 0.07142857
3\ 250.4500\ 0.1500000\ 0.3000000\ 5.750000\ 17.60000\ 85.35000\ 0.05000000\ 0.25000000
4\ \ 275.0000\ \ 0.1000000\ \ 0.4000000\ \ 7.200000\ \ 16.80000\ \ 84.90000\ \ 0.20000000\ \ 0.20000000
                              proto thaldur thaltime
                 diuretic
                                                              met thalach thalrest
          pro
0\ 0.03846154\ 0.000000000\ 83.65385\ 9.038462\ 8.038462\ 5.269231\ 136.1923\ 81.26923
1 \quad 0.22222222 \quad 0.00000000 \quad 81.94444 \quad 9.055556 \quad 7.972222 \quad 5.111111 \quad 129.8333 \quad 76.77778
2\ 0.07142857\ 0.07142857\ 75.00000\ 8.428571\ 7.285714\ 4.235714\ 119.0714\ 82.57143
3\ 0.200000000\ 0.050000000\ 76.25000\ 7.975000\ 6.800000\ 4.820000\ 121.5000\ 71.95000
4\ 0.20000000\ 0.00000000\ 60.00000\ 5.900000\ 4.950000\ 3.800000\ 127.0000\ 82.30000
  tpeakbps
            tpeakbpd trestbpd
                                     exang oldpeak
                                                          slope
                                                                    rldv5
                                                                             rldv5e
             95.15385 \  \, 84.96154 \  \, 0.5000000 \  \, 1.242308 \  \, 1.653846 \  \, 15.53846 \  \, 15.46154
0.176.1538
             96.94444 83.55556 0.8333333 1.6111111 2.000000 15.00000 14.94444
1 171.4444
2\ 181.1429\ 100.35714\ 90.71429\ 0.9285714\ 1.785714\ 2.071429\ 14.00000\ 13.57143
3 182.0000
             98.95000 \ \ 89.05000 \ \ 0.7500000 \ \ 1.750000 \ \ \ 2.000000 \ \ 12.90000 \ \ 13.55000
             94.20000 \ \ 89.40000 \ \ 0.9000000 \ \ 2.300000 \ \ 2.000000 \ \ 17.80000 \ \ 16.50000
4 171.0000
       cmo
                 cdav
0 \ 6.307692 \ 15.30769 \ 85.03846
1 \ 5.722222 \ 16.11111 \ 85.55556
2\ \ 4.642857\ \ 20.28571\ \ 85.57143
3 \quad 6.300000 \quad 18.10000 \quad 85.30000
4 \quad 7.200000 \quad 21.60000 \quad 85.00000
Coefficients of linear discriminants:
                     LD1
                                     LD2
                                                   LD3
                                                                  LD4
          -0.0319039718
                          0.0949747891
                                          0.013319391
                                                         0.025531882
age
sex
           1.0915165611 -1.0511591741
                                         -0.128089043
                                                        -0.217640165
painloc
           0.1592508146 -0.5982393519
                                           0.751516162
                                                        -1.356165886
painexer
           1.0443921480 - 1.8274651017
                                           0.423915039
                                                        -0.129822932
relrest
          -0.5353907890
                          0.3080857927
                                           1.366855699
                                                        -1.292874896
           0.2051091438
                           1.0860954298 -0.347952792
                                                         0.582142933
^{\mathrm{cp}}
trestbps -0.0291801216 -0.0210943388 -0.005915740
                                                         0.010631108
htn
           0.7977232482
                           0.7125540372
                                           0.687763392
                                                         0.090163649
chol
           0.0059740613
                           0.0003533943
                                         -0.008706924
                                                         0.001824229
fbs
           0.3020817737 \quad -1.2745529471
                                           0.340669290
                                                        -0.124606147
                                                        -0.477512401
restecg
          -0.0034817198
                           0.0287925187
                                          -0.860566466
                                                        -0.163174965
ekgmo
           0.1766896834
                           0.2064361753 - 0.235624384
          -0.0008617825 -0.0371982064 -0.025145255
                                                        -0.019070970
ekgday
ekgyr
          -2.1415512648 -2.4433469890
                                          1.742048061
                                                         0.200436115
          -1.7298024975 2.4134058221
prop
                                           0.644332191
                                                         0.279975382
nitr
          -1.3114932699 -1.8866584974 -1.084697545
                                                        0.526330742
           2.2930978213 -0.2622377510 -0.638507586 -1.800873718
pro
```

```
diuretic
                                        -3.921468835
                                                       0.528639304
          4.0807841243 -1.4825164759
proto
          -0.0268455617
                          0.0109964005
                                        -0.052095246
                                                       -0.002381793
thaldur
                                         0.116598448
          -0.1915704888
                         -0.2807526053
                                                       0.766573761
thaltime
                          0.3449238438
                                         0.509998503
                                                       -0.660418467
          0.2397031414
met
          0.1538161967
                        -0.1558001805
                                        -0.188012336
                                                       0.045169327
thalach
          -0.0113911821
                         -0.0075009574
                                         0.012289493
                                                       -0.030730660
thalrest
          -0.0148107903
                          0.0404184418
                                         0.014743907
                                                       0.032907539
                                        -0.014276027
                                                       0.015577249
tpeakbps
           0.0055246183
                         -0.0024652818
tpeakbpd
           0.0147301260
                          0.0121621412
                                         0.034171915
                                                       -0.027803617
trestbpd
           0.0447580846
                         -0.0017554695
                                        -0.059802256
                                                       0.041413630
                                         0.081711393
exang
           0.3026614220
                         -0.0396448017
                                                       -0.223888568
oldpeak
           0.5557096564
                          0.6919891057
                                        -0.374908659
                                                      -0.319812279
slope
           1.5871575130
                        -0.1881557988
                                         0.947157542
                                                       0.617202485
rldv5
           0.0870335285
                          0.232222300
                                         0.056690032
                                                       -0.001700644
rldv5e
          -0.0568400417
                         -0.1650279852
                                        -0.053695184
                                                       -0.020264457
          -0.1012481889
                         -0.1914088336
                                         0.070107909
cmo
                                                       0.059942757
           0.0266986647
                          0.0502210848
cday
                                        -0.025879692
                                                       0.029755031
cyr
           2.4408858944
                          2.4327046963
                                        -1.459350228
                                                       -0.307030741
Proportion of trace:
          LD2
                          LD4
   LD1
                  LD3
0.5086 \ \ 0.2406 \ \ 0.1662 \ \ 0.0846
```

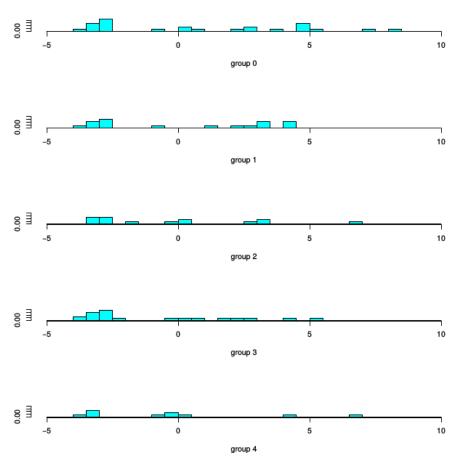


Figure 7: Histergram for discriminant analysis of Hungary

scatterplot for Hungary model

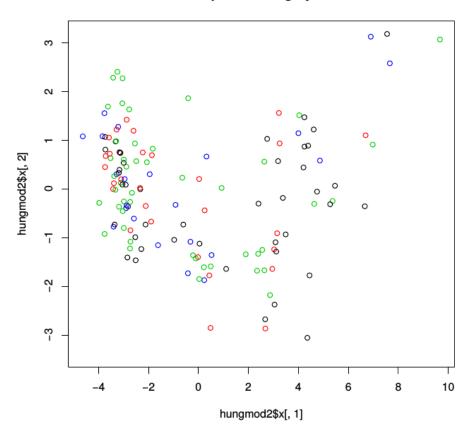


Figure 8: Scatter plot for discriminant analysis of Hungary

2.4.3 Longbeach

```
Call:
lda(num ~~.,~data = ex3datlon)
Prior probabilities of groups:
                   1
                                2
0.1808511 0.3191489 0.2553191 0.2234043 0.0212766
Group means:
                          painloc painexer
                                                 relrest
                                                                 cp trestbps
        age
                   sex
0\ 58.88235\ 0.8823529\ 1.0000000\ 0.5882353\ 0.8235294\ 3.470588\ 124.5882\ 0.5294118
1 \ 56.63333 \ 0.9333333 \ 0.9666667 \ 0.8666667 \ 0.9333333 \ 3.833333 \ 131.4667 \ 0.5333333
2\ 60.58333\ 1.0000000\ 0.9583333\ 0.7916667\ 0.8333333\ 3.625000\ 136.6250\ 0.6666667
3\ 62.95238\ 1.00000000\ 0.9047619\ 0.8571429\ 0.9047619\ 3.714286\ 140.9048\ 0.7142857
4\ 63.50000\ 1.0000000\ 1.0000000\ 1.0000000\ 1.0000000\ 4.000000\ 148.0000\ 0.5000000
                                      years
                                                          famhist
       chol
                 smoke
                                                   fbs
                                                                     restecg
                            cigs
0\ 198.9412\ 0.5294118\ 24.70588\ 27.23529\ 0.4117647\ 0.7058824\ 0.7647059\ 5.647059
1 \ 194.0000 \ 0.4333333 \ 19.90000 \ 17.00000 \ 0.3666667 \ 0.4666667 \ 0.7000000 \ 6.700000
2\ 174.0417\ 0.5833333\ 18.33333\ 24.41667\ 0.2500000\ 0.4166667\ 0.7083333\ 6.208333
3\ 217.4286\ 0.5714286\ 23.80952\ 27.76190\ 0.3333333\ 0.3809524\ 0.6666667\ 7.000000
4\ 251.0000\ 1.0000000\ 30.00000\ 38.50000\ 0.5000000\ 1.0000000\ 0.5000000\ 6.000000
                                                                       diuretic
                ekgyr
                               dig
                                         prop
                                                    nitr
                                                                 pro
0 \ 15.05882 \ 84.58824 \ 0.11764706 \ 0.4117647 \ 0.7058824 \ 0.1764706 \ 0.3529412 \ 3.588235
1 \ 16.13333 \ 84.40000 \ 0.06666667 \ 1.0666667 \ 0.5666667 \ 0.2000000 \ 0.1666667 \ 3.566667
2\ 13.33333\ 84.83333\ 0.12500000\ 0.4583333\ 0.5416667\ 0.2916667\ 0.3750000\ 4.000000
3\ 15.28571\ 84.42857\ 0.09523810\ 0.4285714\ 0.6190476\ 0.2380952\ 0.3809524\ 3.904762
4\ 26.50000\ 86.50000\ 0.50000000\ 0.0000000\ 1.0000000\ 0.5000000\ 0.5000000\ 5.000000
                  met thalach thalrest tpeakbps tpeakbpd trestbpd
   thaldur
0\ 5.858824\ 5.876471\ 115.3529\ 63.94118\ 159.7059\ 88.35294\ 78.23529\ 0.4705882
1 \ 6.758333 \ 6.740000 \ 121.9667 \ 69.70000 \ 162.9667 \ 91.66667 \ 80.63333 \ 0.6000000
2\ 6.504167\ 6.375000\ 122.0000\ 69.62500\ 172.0417\ 90.62500\ 83.29167\ 0.7083333
3 \ 5.730952 \ 5.619048 \ 116.8571 \ 67.04762 \ 159.4286 \ 83.66667 \ 83.47619 \ 0.9047619
4\ \ 4.250000\ \ 3.500000\ \ 124.0000\ \ 76.50000\ \ 170.0000\ \ 84.00000\ \ 79.00000\ \ 1.0000000
        xhypo
                 oldpeak
                             rldv5
                                      rldv5e
                                                    cmo
                                                              cdav
                                                                         cyr
                                                                                   lmt
0 \ 0.000000000 \ 0.7529412 \ 15.88235 \ 17.52941 \ 6.000000 \ 10.52941 \ 84.64706 \ 10.47059
1 \ 0.00000000 \ 0.9166667 \ 16.70000 \ 16.06667 \ 6.333333 \ 16.13333 \ 84.53333
                                                                              1.00000
2\ 0.04166667\ 1.3791667\ 14.75000\ 14.83333\ 6.791667\ 14.58333\ 84.91667
                                                                               1.00000
3 \ 0.04761905 \ 1.7142857 \ 15.42857 \ 15.47619 \ 7.952381 \ 14.09524 \ 84.52381
                                                                               1.00000
                                                                               2.00000
4\ 0.000000000\ 3.5000000\ 24.00000\ 19.50000\ 7.000000\ 6.50000\ 86.50000
            laddist
   ladprox
                           diag
                                   cxmain ramus
                                                       om1
                                                                  om2
                                                                       rcaprox
 1.000000 \ 1.000000 \ 1.117647 \ 1.000000 \ 1.000 \ 1.000000 \ 1.000000 \ 1.000000 \ 1.000000
1 \ \ 1.166667 \ \ 1.133333 \ \ 1.133333 \ \ 1.333333 \ \ 1.000 \ \ 1.100000 \ \ 1.033333 \ \ 1.233333 \ \ 1.100000
2\ \ 1.458333\ \ 1.166667\ \ 1.125000\ \ 1.458333\ \ 1.125\ \ 1.291667\ \ 1.083333\ \ 1.708333\ \ 1.083333
3\ 1.761905\ 1.238095\ 1.238095\ 1.857143\ 1.000\ 1.285714\ 1.095238\ 1.857143\ 1.238095
4 \ 1.500000 \ 1.000000 \ 1.000000 \ 2.000000 \ 1.000 \ 1.000000 \ 1.000000 \ 2.000000 \ 1.000000
Coefficients of linear discriminants:
                     LD1
                                    LD2
                                                   LD3
                                                                  LD4
           0.0990101557
                           0.035457144 - 0.029404453 - 0.037368451
age
          -0.7001377631 -1.223212780
                                         2.472604131 - 0.385002333
sex
           1.3527943877
                           2.689379586 -1.442324304
                                                         0.925270543
painloc
painexer
           1.6779571229
                           1.095644137
                                          1.132485802
                                                         0.132422919
relrest
           1.0061607957
                           2.683724569
                                          1.044784632 -0.315270284
          -1.3452114777 -2.179502234 -0.074000882
                                                         0.276431196
^{\mathrm{cp}}
           0.0152057624
                           0.043147540
                                         0.019492777
                                                         0.004725401
trestbps
_{
m htn}
           0.2007845282 - 0.213314404 - 0.049905568
                                                         0.516879641
chol
           0.0022668552
                          0.003074371
                                          0.000609473 -0.004283149
           1.3848919525 \quad 0.579322247
                                          0.717647892 -0.203604359
smoke
```

```
-0.0021092781
                          0.040230996 - 0.017470605
                                                     -0.046310142
cigs
years
          -0.0189346337
                         -0.009935330
                                       -0.025142432
                                                      0.020697154
fbs
          -0.5602845218
                         -0.600564294
                                        0.917260811
                                                     -0.583766088
famhist
           0.2368404852
                          0.633387492
                                        0.062625332
                                                     -0.435654580
restecg
           0.3148426505
                                        0.230598184
                                                     -0.620653987
                          0.054613753
ekgmo
           0.1066755233
                          0.146072767
                                        0.174751517
                                                      0.051019305
ekgday
           0.0302154060
                          0.042708813
                                        0.006610623
                                                      0.007431638
          -0.6058539073
ekgyr
                          1.011772666
                                       -0.482944430
                                                      1.028674481
dig
           0.1934068922
                                        0.420059417
                                                      1.532752361
                          1.829523966
prop
          -0.0258580607
                         -0.128530397
                                       -0.013717278
                                                     -0.004001685
nitr
          -0.2979245919
                          0.890522089
                                        0.221162357
                                                     -0.115880411
pro
           0.2277745757
                          0.495507245
                                       -0.293334921
                                                      0.886596619
diuretic
          -0.5265872971
                         -1.108015873
                                       -0.622279383
                                                     -0.614113919
           0.0389888030
                         -0.304394784
                                       -0.045447788
                                                      0.044131177
proto
thaldur
           0.0974633776
                          0.347965964
                                        0.471833171
                                                      -0.506561997
           0.0520777936
                         -0.547177132
                                       -0.234459599
                                                      0.387387794
met
thalach
           0.0012019440
                         -0.009656180
                                        0.001428743
                                                      0.009332465
thalrest
           0.0349744126
                          0.037022030
                                        0.013999657
                                                      0.005532030
tpeakbps
          -0.0005518933
                          0.012532493
                                       -0.016658042
                                                      0.026948500
tpeakbpd
          0.0110131580
                          0.013873221
                                        0.019296564
                                                      0.018578019
trestbpd
         -0.0101443057
                         -0.111258996
                                        0.003785584
                                                      0.004558456
                                                      -0.290403026
exang
          -0.2885342130
                         -0.491316817
                                        0.711632300
                                       -2.533162072
xhypo
          -2.0890734776
                         -1.546304470
                                                      2.585953825
oldpeak
           0.0562423983
                          0.729631495
                                       -0.150881175
                                                      -0.454416331
rldv5
           0.1212482697
                          0.141480974
                                        0.244757211
                                                      0.074758659
rldv5e
          -0.1098458488
                         -0.119370257
                                       -0.225942614
                                                      0.008272690
cmo
          -0.0044982969
                        -0.215097791
                                       -0.184654932
                                                      0.011105799
cday
           0.0154098050 \;\; -0.018575403
                                        0.045237609
                                                      0.014481709
cyr
           0.7728103647
                         -0.622781492
                                        0.438416369
                                                     -0.517516020
lmt
                                       -0.011799002
          -0.0076644410
                          0.016199837
                                                     -0.006409811
                         -0.236848734
                                       -0.756165644
                                                     -0.403482082
ladprox
           5.1429956452
laddist
                         -0.538647061
                                       -0.111674357
           5.4700303913
                                                     -0.040224894
diag
           0.1674878034
                         -0.867356837
                                       -0.233108173
                                                     -0.424424671
cxmain
           4.9690488611
                          0.288788245
                                        0.491785610
                                                     -0.752048882
ramus
           2.2794956046
                        -2.518189778
                                       -1.110123699
                                                      4.143654026
                         -0.569683759
                                        0.382398821
om1
           2.7419747798
                                                      0.098133650
om2
           1.3014833954
                          0.573435941
                                       -1.109721994
                                                     -1.917714264
rcaprox
           4.3481392232
                          0.005190937
                                       -0.578608990
                                                      1.523789635
           1.9383005198
rcadist
                          0.312683826
                                        0.793005347 - 2.408552088
Proportion of trace:
          LD2
   LD1
                  LD3
                          LD4
0.9072\  \, 0.0418\  \, 0.0262\  \, 0.0248
```

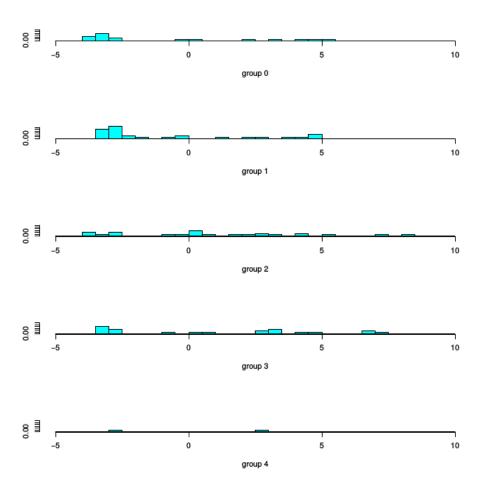


Figure 9: Histergram for discriminant analysis of Longbeach

scatterplot for Longbeach model

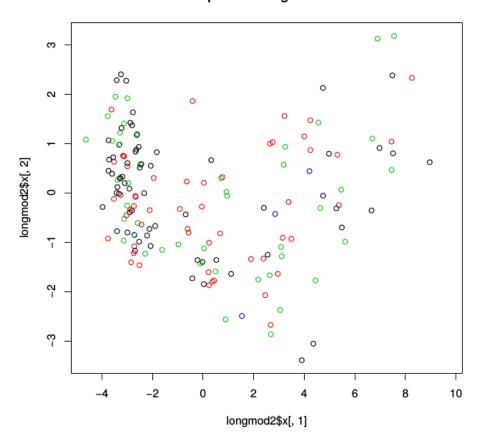


Figure 10: Scatter plot for discriminant analysis of Longbeach

2.4.4 Switzerland

```
Call:
lda(num ~~.,~data = swidata)
Prior probabilities of groups:
                                  2
                                              3
                      1
0.05940594 \ \ 0.39603960 \ \ 0.26732673 \ \ 0.22772277 \ \ 0.04950495
Group means:
                         painloc painexer
                                               relrest
                                                               cp trestbps
        age
                   sex
0\ 52.00000\ 1.0000000\ 0.6666667\ 0.3333333\ 0.3333333\ 3.166667\ 117.5000\ 0.1666667
1 \ 56.80000 \ 0.8750000 \ 0.9500000 \ 0.8500000 \ 0.8000000 \ 3.675000 \ 129.3750 \ 0.3250000
2\ 53.59259\ 0.9259259\ 0.8888889\ 0.8888889\ 0.8888889\ 3.740741\ 132.5926\ 0.4074074
3 \ 58.65217 \ 0.9565217 \ 1.0000000 \ 0.9130435 \ 0.7826087 \ 3.782609 \ 140.6522 \ 0.3478261
4 \ 52.00000 \ 1.0000000 \ 1.0000000 \ 1.0000000 \ 1.0000000 \ 4.000000 \ 120.0000 \ 0.4000000
     ekgmo
              ekgdav
                         ekgvr
                                       dig
                                                 prop
                                                             nitr
                                                                         pro
                                                                              diuretic
0\ 2.500000\ 21.33333\ 84.83333\ 0.000000000\ 0.33333333\ 0.3333333\ 0.5000000\ 0.0000000
1\ \ 4.100000\ \ 16.27500\ \ 84.65000\ \ 0.000000000\ \ 0.4250000\ \ 0.4000000\ \ 0.4000000\ \ 0.1000000
3 \ 5.695652 \ 13.95652 \ 84.52174 \ 0.000000000 \ 0.3913043 \ 0.2608696 \ 0.4347826 \ 0.4347826
4\ 5.800000\ 18.60000\ 84.60000\ 0.000000000\ 0.6000000\ 1.00000000\ 0.4000000\ 0.2000000
    thaldur thalach thalrest tpeakbps tpeakbpd trestbpd
                                                                   exang
                                                                               xhypo
0 \ 10.000000 \ 143.1667 \ 68.00000 \ 175.8333 \ 82.50000 \ 75.00000 \ 0.1666667 \ 0.00000000
   7.557500 \ 123.7500 \ 69.52500 \ 171.7500 \ 86.37500 \ 81.62500 \ 0.4750000 \ 0.00000000
   7.518519 \ 125.3333 \ 72.11111 \ 169.8148 \ 88.14815 \ 83.51852 \ 0.4074074 \ 0.03703704
   6.947826 \ 104.2174 \ 64.52174 \ 160.0000 \ 86.08696 \ 87.17391 \ 0.6086957 \ 0.13043478
   6.900000\ 109.8000\ 74.20000\ 138.0000\ 78.00000\ 76.00000\ 0.4000000\ 0.20000000
                                                                   diag
    oldpeak
                           cdav
                                      cyr
                                           ladprox laddist
                  cmo
                                                                           cxmain
0\ 0.3333333\ 2.333333\ 21.33333\ 84.83333\ 1.000000\ 1.000000\ 1.166667\ 1.000000
1 \ \ 0.3675000 \ \ 4.075000 \ \ 17.12500 \ \ 84.70000 \ \ 1.300000 \ \ 1.175000 \ \ 1.075000 \ \ 1.100000
2\ 0.7555556\ 5.814815\ 13.77778\ 84.37037\ 1.592593\ 1.481481\ 1.259259\ 1.333333
3\ 0.8608696\ 5.739130\ 14.21739\ 84.52174\ 1.782609\ 1.521739\ 1.478261\ 1.521739
4\ 0.9600000\ 6.000000\ 14.20000\ 84.60000\ 1.800000\ 1.200000\ 1.000000\ 1.400000
                 om1
                           om2 reaprox readist
0 \ 1.000000 \ 1.000000 \ 1.000000 \ 1.000000 \ 1.000000
1 \ 1.025000 \ 1.000000 \ 1.000000 \ 1.275000 \ 1.125000
2\ 1.185185\ 1.000000\ 1.148148\ 1.518519\ 1.222222
3\ 1.521739\ 1.347826\ 1.130435\ 1.739130\ 1.521739
4 \quad 1.200000 \quad 1.200000 \quad 1.000000 \quad 1.400000 \quad 1.200000
Coefficients of linear discriminants:
                    LD1
                                    LD2
                                                  LD3
                                                                  LD4
          -0.0007858366
                          0.0628048943 -0.071526268
                                                       -0.0417811598
age
          0.8186870033
                          0.2412555376
                                          0.363652833
                                                        0.3287857513
sex
painloc
          -0.3837830485
                          2.2727914494
                                        -1.184109094
                                                       -3.4202311632
painexer 0.9118113566
                        -1.4374997954
                                          0.056616312
                                                       -2.5683124594
relrest
          -1.2647469151 -1.2871470954
                                          0.420021842
                                                       -0.3980500354
           0.3521125467
                          0.6077931365
                                          0.237965504
                                                        1.4684042267
ср
         0.0052216770 -0.0003397642
                                          0.022936687
                                                       -0.0002354636
trestbps
          -0.2637513280 -0.3449011590
                                          0.449630173
                                                       -0.2538746008
restecg
          0.0417657735 -0.0734676135
                                          0.099042462
                                                        0.2295703277
ekgmo
ekgday
          -0.0056874619
                          0.0230409744
                                          0.050349943
                                                        0.0416943072
ekgyr
          0.5069361444
                          0.5686400550
                                          0.296652266
                                                        0.3918472529
          -2.5341631270 \quad -2.9792700230
dig
                                         -1.502320680
                                                        0.4888530492
          -0.2807770793 -0.0863581677
prop
                                          0.267336756
                                                       -0.1333181334
          0.4315496561
                         0.2855985294
                                          1.759176079
                                                       -0.4000743686
nitr
          -0.0005018530 -0.7611546405
pro
                                        -0.194037649
                                                        0.5060712017
diuretic 0.7636514352 0.7979700757 -0.147302771
                                                        0.0096484846
thaldur
        -0.0033692288 -0.0929494992 0.081758599
                                                       0.0702982571
```

```
thalach
          -0.0087387451 \quad -0.0094572112
                                        -0.009259432
                                                      -0.0050115022
thalrest
          0.0504091039
                          0.0242042236
                                         0.022939061
                                                       -0.0254912923
                                                       0.0032913902
tpeakbps
          -0.0081181662
                         -0.0013325295
                                        -0.020142259
                                        -0.002362359
tpeakbpd
         -0.0111369375
                         -0.0140911285
                                                       0.0210386963
trestbpd
          0.0361591182
                         -0.0007605452
                                        -0.024619507
                                                       -0.0320079275
exang
          -0.1520069720
                          0.6009664626
                                        -0.429942733
                                                       -0.4604614290
xhypo
          -0.3341779201
                          1.5596277090
                                         1.378414692
                                                       1.2645700698
oldpeak
          0.1908935156
                        -0.0967478433
                                         0.388405128
                                                       0.2164803514
cmo
           0.0277780256
                          0.2412607985
                                         0.073061630
                                                       -0.1960612646
cday
          -0.0151970362
                         -0.0148062415
                                         -0.026759876
                                                       -0.0152737194
cyr
           0.2318645756
                          0.6265312268
                                         0.095369608
                                                       -0.6515047003
ladprox
           1.7277441803
                        -1.2217191986
                                         0.314767813
                                                      -0.1033884127
laddist
           1.1672585854
                         -0.8125308678
                                        -0.278617954
                                                       -0.6830410921
diag
           0.2504224578
                         -0.3244353820
                                        -0.673472037
                                                       0.3895221999
cxmain
           1.7362037233
                         -0.3507318707
                                        -0.017925974
                                                       0.4765159079
           1.1291841912
                          0.2856883362
                                         0.286684835
                                                       1.0561701368
ramus
          -0.1893535303
                          3.8891176666
                                        -0.704398542
om1
                                                       0.5598622966
om2
           0.4071110870
                         -2.5992153764
                                        -0.676202349
                                                       -0.4854881569
rcaprox
           1.4316751371
                         -0.7666014034
                                        -0.317212280
                                                       -0.2971793102
           1.0688251201 \quad -0.2259274588 \quad -0.629453212
rcadist
                                                       0.1276147609
Proportion of trace:
   LD1
          LD2
                  LD3
                          LD4
0.6579 \ 0.1599 \ 0.1086 \ 0.0736
```

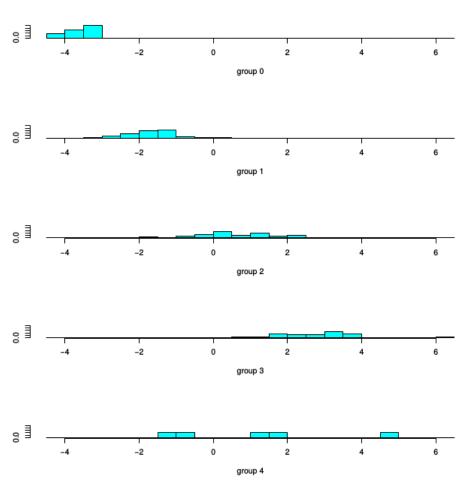


Figure 11: Histergram for discriminant analysis of Switzerland

scatterplot for Switzerland model

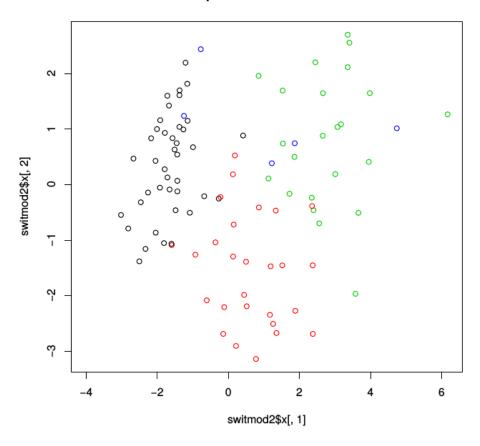


Figure 12: Scatter plot for discriminant analysis of Switzerland

3 Summary