

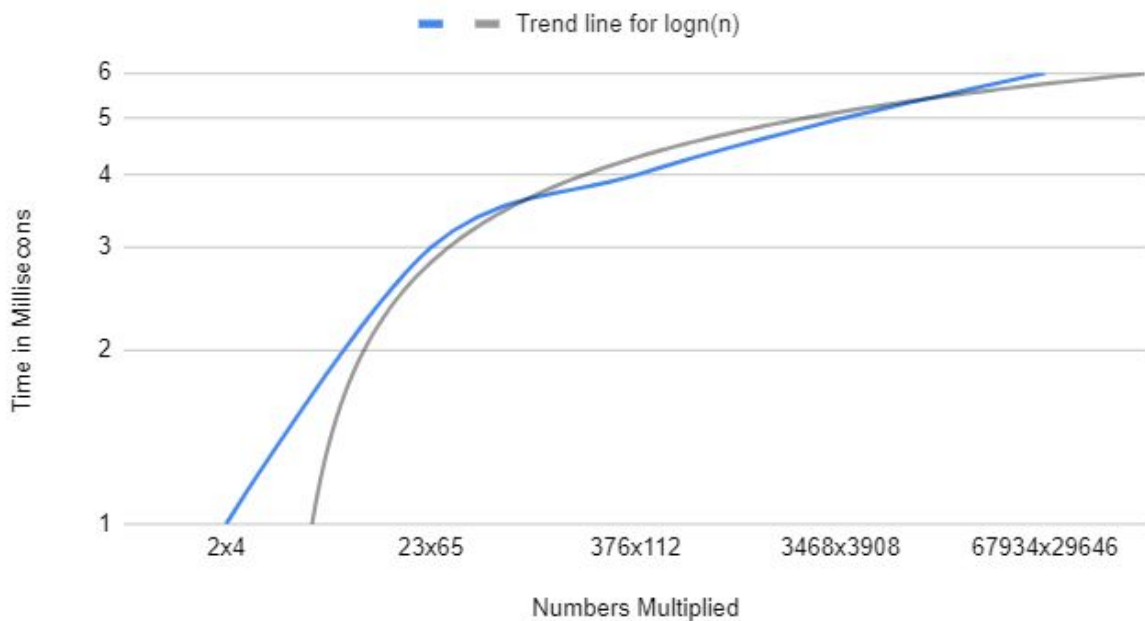
Algorithm Analysis - Adam Russell (18328861)

Link to Google Sheets:

<https://docs.google.com/spreadsheets/d/1okFcOSyPnkcgeKQZLfD30bILTSamzbztGlgX-IN5hO8/edit?usp=sharing>

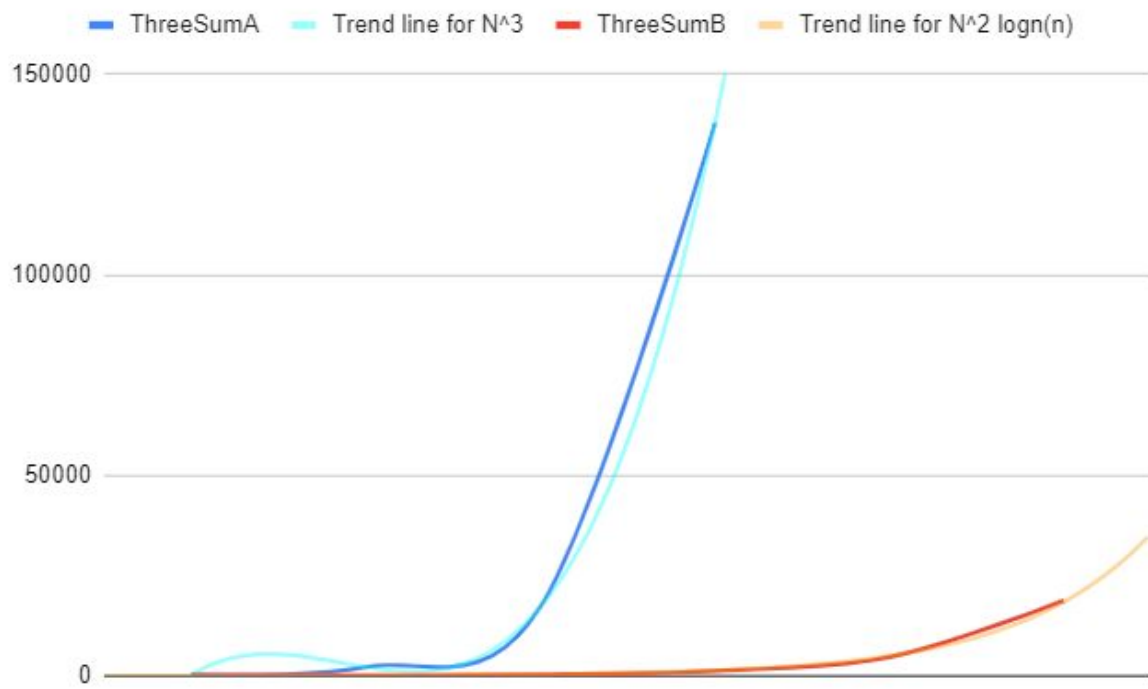
Russian Peasant Multiplication Algorithm:

Russian Peasant Algorithm Performance



The time complexity of the R.P algorithm is roughly $O(\log n)$. The blue line above represents the time's I got through testing alongside a trendline for the $\log(n)$. We can see that my times roughly follow the trendline for $\log(n)$.

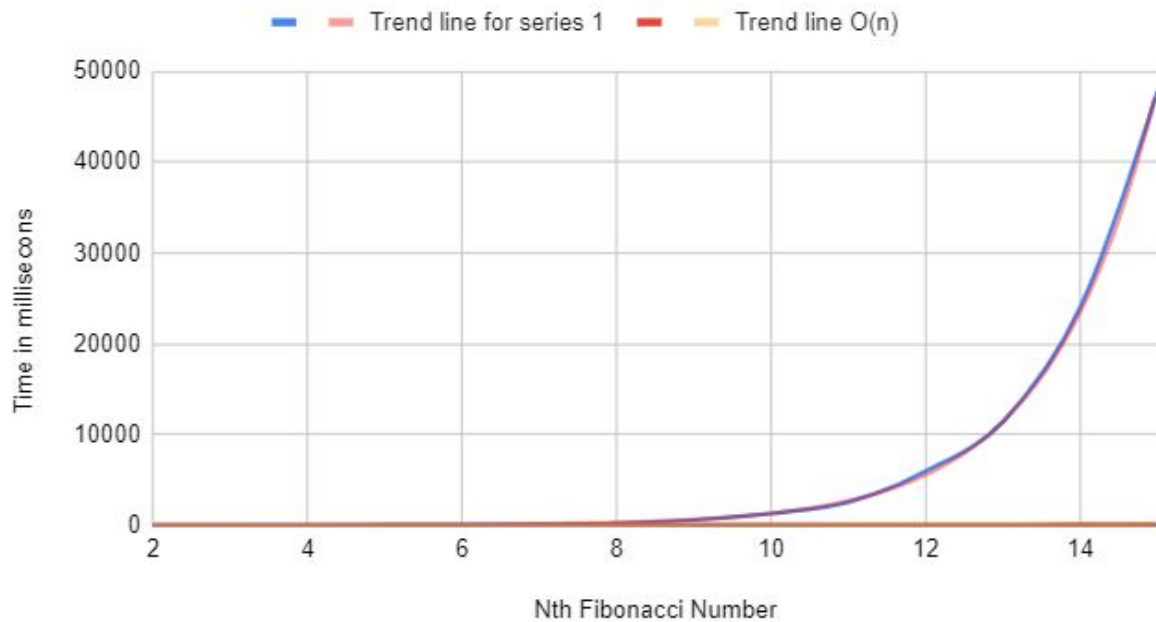
ThreeSumA & ThreeSumB:



Above is ThreeSumA ($O(n^3)$) and ThreeSumB ($O(n^2 \log n)$) plotted with the data I got through testing, alongside trendlines for expected outcomes, which match extremely well with the experimental data I received.

Recursion:

Fibonacci Recursion



A line graph based on my testing of a recursive and iterative implementation of finding the nth fibonacci number, alongside a trendline for 2^n , showing a good correlation for the recursive implementation, and n (linear) for the iterative implementation. After a certain n (roughly $n = 7$) the iterative approach begins to outpace the recursive implementation immensely.

Sorting:

Elementary Sorting:

SelectionSort and InsertionSort



Above is a graph of my times for various arrays of length n using selection sort and insertion sort. The start of the graph is a bit wobbly as for small arrays times will be affected by system noise, but after that it is a straight line, which is what is to be expected. My arrays increased in size by a factor of n^2 , and since SelectionSort and InsertionSort both have $O(n^2)$, as straight line is to be expected when graphed using these input sizes. InsertionSort is faster than SelectionSort as seen by my testing. I believe this is because SelectionSorts best case is still $O(n^2)$, while InsertionSorts best case is $O(n)$, meaning InsertionSort can be done faster than $O(n^2)$, which is seen by my graph.

N.B. I did not include my third ridiculous sorting algorithm in the graph as Stalin Sort works in linear time and would have therefore just been a flat line at the bottom of my graph.

MergeSort:

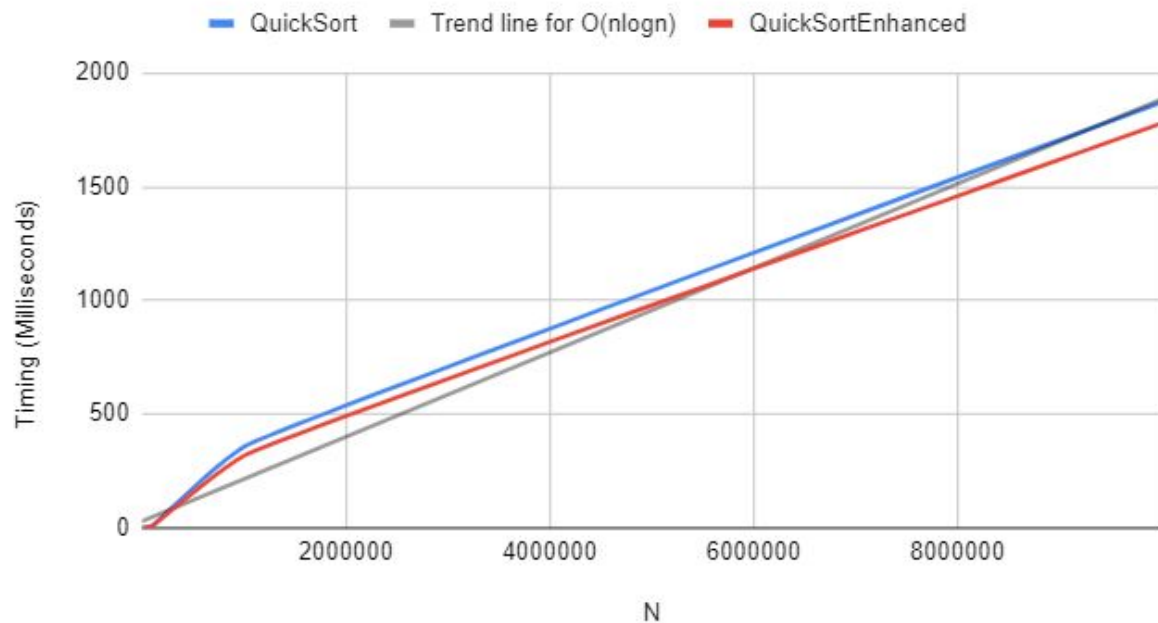
MergeSort Timings



These are my timings for MergeSort and MergeSortEnhanced alongside a trendline for $O(n \log n)$. MergeSortEnhanced is slightly faster than MergeSort (roughly 10%), but as the size of the array to sort gets larger, MergeSort and MergeSortEnhanced get closer timings as the enhancements are effective at the small array stage.

QuickSort:

QuickSort Timings



These are my timings for QuickSort and QuickSortEnhanced alongside a trendline for roughly $O(n \log n)$. QuickSortEnhanced is slightly faster than QuickSort, and they roughly follow the average expected time of $O(n \log n)$.

String Pattern Matching:

Brute Force and KMP



These are my timings for string pattern matching using a brute force approach vs. the KMP algorithm, which is also graphed against a trendline for $O(n)$ linear time.