

2)

a) Smoke \Rightarrow Fire

~~Satisfiable~~
Neither

S	T	T	F	F
F	T	F	T	F
a	T	F	F	F

b) Fire \Rightarrow Fire

Valid

F	T	T	F	F
b	T	T	F	F

c) $(\neg \text{Smoke} \Rightarrow \neg \text{Fire}) \Rightarrow (\text{Smoke} \Rightarrow \text{Fire})$ ~~Satisfiable~~
 $(\text{Smoke} \vee \neg \text{Fire}) \Rightarrow (\neg \text{Smoke} \vee \text{Fire})$ IE Neither
 $\neg(\text{Smoke} \vee \neg \text{Fire}) \vee (\neg \text{Smoke} \vee \text{Fire})$ IE

S	T	T	F	F
F	T	F	T	F
C	T	F	T	T

d) $\neg \text{Smoke} \vee \neg \text{Fire} \vee \text{Fire}$ Valid

$\neg \text{Smoke} \vee \text{True}$
True

e) $\text{Smoke} \vee \text{Fire} \vee (\text{Smoke} \Rightarrow \text{Fire})$ Valid

$\text{Smoke} \vee \text{Fire} \vee (\neg \text{Smoke} \vee \text{Fire})$ Implication elimination

S	T	T	F	F
F	T	F	T	F
e	T	T	T	T

$$f) ((\text{Smoke} \wedge \text{Heat}) \Rightarrow \text{Fire}) \Rightarrow (\text{Smoke} \Rightarrow \text{Fire})$$

$$(\neg(\text{Smoke} \wedge \text{Heat}) \vee \text{Fire}) \Rightarrow (\neg \text{Smoke} \vee \text{Fire})$$

$$\neg(\neg(\text{Smoke} \wedge \text{Heat}) \vee \text{Fire}) \vee (\neg \text{Smoke} \vee \text{Fire})$$

S	T	T	T	T	F	F	F
H	T	T	F	F	T	T	F
F	T	F	T	F	T	F	T
F	T	T	T	F	T	T	T

~~Satisfiable~~
Neither

$$g) (\text{Smoke} \Rightarrow \text{Fire}) \Rightarrow ((\text{Smoke} \wedge \text{Heat}) \Rightarrow \text{Fire})$$

$$(\neg \text{Smoke} \vee \text{Fire}) \Rightarrow (\neg(\text{Smoke} \wedge \text{Heat}) \vee \text{Fire})$$

$$\neg(\neg \text{Smoke} \vee \text{Fire}) \vee (\neg(\text{Smoke} \wedge \text{Heat}) \vee \text{Fire})$$

S	T	T	T	T	F	F	F
H	T	T	F	F	T	T	F
F	T	F	T	F	T	F	T
F	T	T	T	T	T	T	T

Valid

$$h) ((\text{Smoke} \wedge \text{Heat}) \Rightarrow \text{Fire}) \Leftrightarrow ((\text{Smoke} \Rightarrow \text{Fire}) \vee (\text{Heat} \Rightarrow \text{Fire}))$$

$$(\neg(\text{Smoke} \wedge \text{Heat}) \vee \text{Fire}) \Leftrightarrow ((\neg \text{Smoke} \vee \text{Fire}) \vee (\neg \text{Heat} \vee \text{Fire}))$$

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$$h) ((\text{Smoke} \wedge \text{Heat}) \Rightarrow \text{Fire}) \Leftrightarrow ((\text{Smoke} \Rightarrow \text{Fire}) \vee (\text{Heat} \Rightarrow \text{Fire}))$$

~~+~~ ~~(\neg Smoke)~~

$$(\neg(\text{Smoke} \wedge \text{Heat}) \vee \text{Fire}) \Leftrightarrow ((\neg \text{Smoke} \vee \text{Fire}) \vee (\neg \text{Heat} \vee \text{Fire}))$$

$$(\neg(\text{Smoke} \wedge \text{Heat}) \vee \text{Fire}) \Rightarrow ((\neg \text{Smoke} \vee \text{Fire}) \vee (\neg \text{Heat} \vee \text{Fire}))$$

$$((\neg \text{Smoke} \vee \text{Fire}) \vee (\neg \text{Heat} \vee \text{Fire})) \Rightarrow (\neg(\text{Smoke} \wedge \text{Heat}) \vee \text{Fire})$$

$$\neg(\neg(\text{Smoke} \wedge \text{Heat}) \vee \text{Fire}) \vee ((\neg \text{Smoke} \vee \text{Fire}) \vee (\neg \text{Heat} \vee \text{Fire}))$$

$$\neg((\neg \text{Smoke} \vee \text{Fire}) \vee (\neg \text{Heat} \vee \text{Fire})) \vee (\neg(\text{Smoke} \wedge \text{Heat}) \vee \text{Fire})$$

S	T	T	T	F	F	F	F
H	T	T	F	F	T	T	F
F	T	F	T	F	T	F	T
h	F	F	F	F	F	F	F

~~Invalid~~ Unsatisfiable