

N^{th} Prime Number

- Only check odd numbers
- Only division by other odds
 - ↳ don't check 1

if $I_n = 1$ return 2

else

$j = 1$

LOOP: ~~while n > 0~~

$n = 1$

if $n == 0$

$out = j$

end

$j += 2$ // next odd int

~~loop~~

~~copy x~~

~~copy j~~

~~exit loop~~

~~divide by~~

~~x = 1~~ // $(1+2)$ ← (both already stored)

Div Loop

~~copy j = j~~ $\rightarrow x += 2$ share for overflow

if $x > j$ ~~exit~~

~~x / j~~

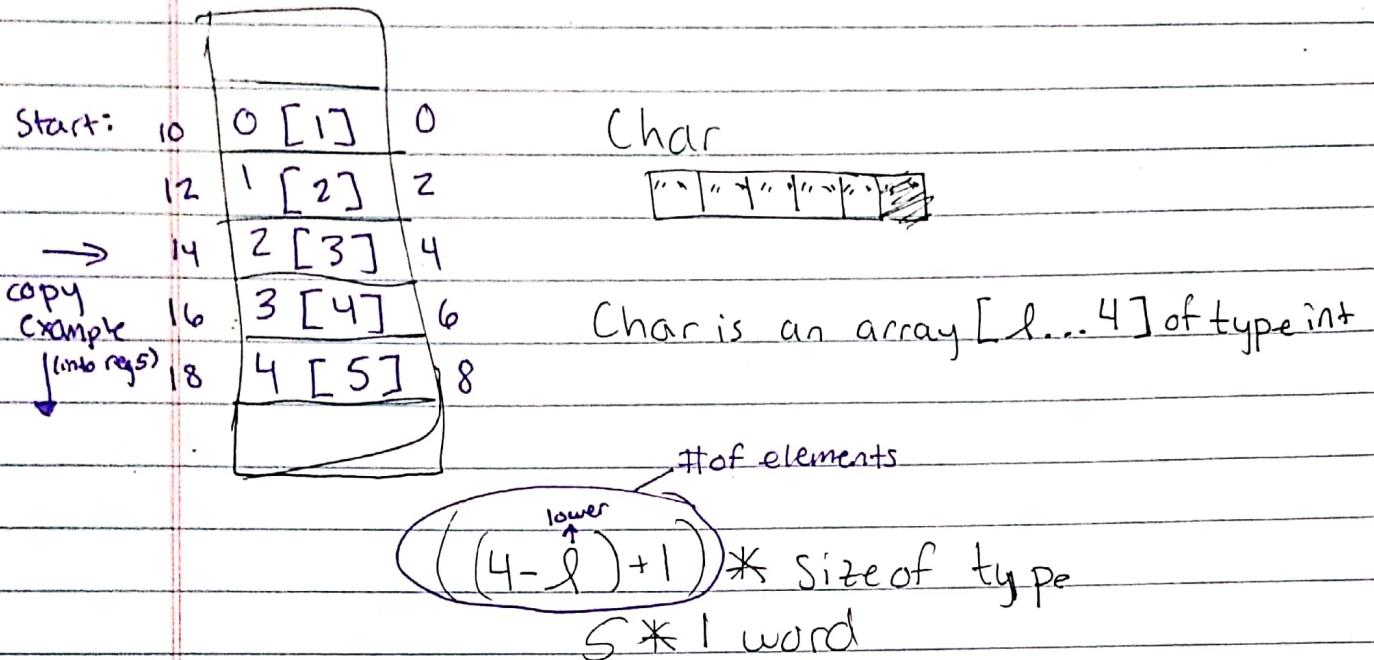
if remainder == 0 // not prime

exit div Loop

if

goto loop

Assembler (PDP-11) Arrays



address (char[i])

Start Location + $(i-l) \text{size of type}$

Addressing Mode

Dynamic

{Start} + offset

↳ put in registers for the sake of speed

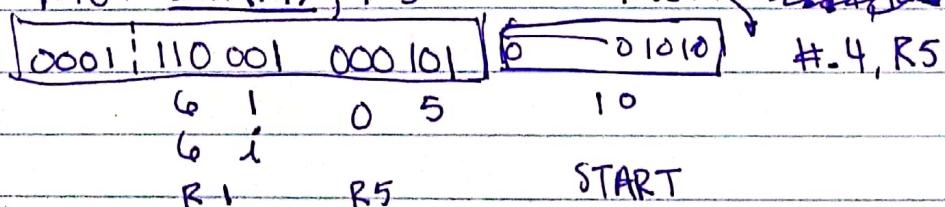
"Indexed Mode Addressing"

(l, i)

MOV start(R1), R5

→ MOV

~~#-4,R5~~



A is an array [1...100] of INTEGER
B is an array [10...110] of INTEGER

200. A: BLKW 100.
1000. B: BLKW 100.

200 A	$\begin{bmatrix} 1 \\ 2 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 2\% \end{bmatrix}$
		$\begin{array}{l} \vdots \\ \vdots \\ [100] 198 \end{array}$

COPY: MOV #198, R1
LOOP MOV A(R1), B(R1)

$$1000 \quad B \quad \begin{array}{c} 9 \\ 3 \\ 3 \end{array} \quad [10] \quad 0$$

$[11]$

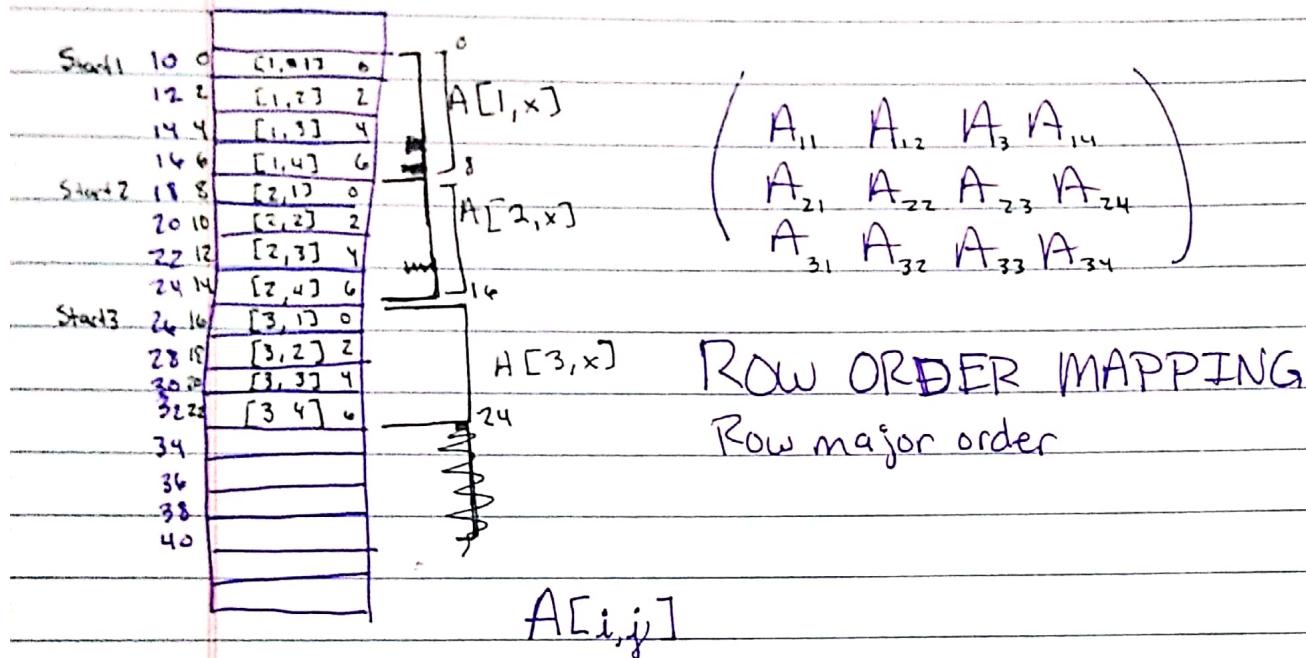
2

$[110] \quad 198$

SUB #2, R1

A is an array $[l_1 \dots u_1, l_2 \dots u_2]$ of type
similar shape

A is an array $[l_1 \dots u_1, l_2 \dots u_2]$ of type array $[l_3 \dots u_3]$



Total Size: $[u_1 - l_1 + 1] * [u_2 - l_2 + 1] * \text{size of type (bytes)}$
 $3 * 4 * 2$

24 bytes \rightarrow 12 words of storage

$i \rightarrow (u_1 - l_1 + 1) * \text{size of type} * i$
 $j \rightarrow \cancel{(u_2 - l_2 + 1)} * \text{size of type} * j$

$\rightarrow (u_1 - l_1 + 1) * \text{size of type} * i + \text{size of type} * j$

$\rightarrow \text{size of type} * ((u_1 - l_1 + 1) * i + j)$

$A[2, 3]$

$\rightarrow \text{offset } 12$

$\rightarrow \text{Addr } 22$

$\rightarrow (i - l_1)(u_2 - l_2 + 1) \text{ size of basetype}$
 $+ (j - 1) * 2$

Ch 8 1abc, Ch 11 1, 6abc, Ch 12 1abc

1. a) $a^i b^j : i, j \geq 0$ and $i+j=5$

Regular strings $a^* b^*$ with length of 5

- only 5 possible strings so regular

b) $\{a^i b^j : i, j \geq 0 \text{ and } i-j=5\}$

so let's look at $a^k b^k$, where $y = a^p$, $|xy| \leq k$

pump up such that $w = a^{k+p} b^k$. Since $p \geq 1$

at the smallest $w = a^{k+1} b^k$ which no longer fits
the rule of $i-j=5$. Not Regular.

$w = a^k b^k a^k$ since $|xy| \leq k$ we know that

$y \neq$ must fall under a^k so $y = a^p$ $p \geq 1$

so let's pump up $w = a^{k+p} b^k a^k \rightarrow w = a^{k+1} b^k a^k$

this is no longer a palindrome ↗

$$a^i b^j : 2i = 3j + 1$$

~~Saa~~

bb, ~~aaabbabbabb~~, ~~aaaabbbbabbabb~~

~~S → aaabbabb~~

~~S → b~~

~~aaabbabb~~

~~aaabbabb~~

~~aaabbabb~~

~~aaabbabb~~

~~aaabbabb~~

$j=0 \quad x$

1 $2 = 3j + 1 \times$

2 $4 = 3j + 1 \quad j=1 \quad aabb \checkmark$

3 $6 = 3j + 1 \times$

4 $8 = 3j + 1 \times$

5 $10 = 3j + 1 \quad j=3 \quad aaaaabbabb$

6 $12 = 3j + 1 \quad aaaaabbabb aabb$

$a^i b^j : 2i \neq 3j + 1$

- 0 \rightarrow ~~any~~ ✓ any
- 1 \rightarrow ✓ any
- 2 \rightarrow any except 1
- 3 \rightarrow ✓ any
- 4 \rightarrow ✓ any
- 5 \rightarrow any except 3
- 6 \rightarrow ✓ any
- 7 \rightarrow ✓ any
- 8 \rightarrow any except 5
- 9 \rightarrow ✓ any
- 10 \rightarrow ✓ any

$S \rightarrow aaasbb$

$S \rightarrow aaaX$ / extra a's

$S \rightarrow T$ / Terminate

$X \rightarrow A | Ab$ / arb. more a's

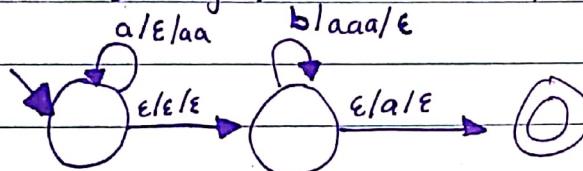
$T \rightarrow A | B | aB | aabbB$

$A \rightarrow aA | \epsilon$

$B \rightarrow bB | \epsilon$

$a^i b^j : 2i = 3j + 1$

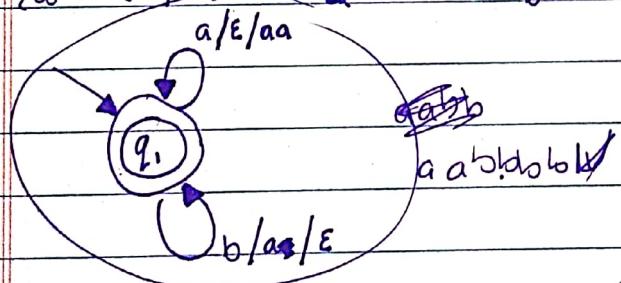
aab, aaaaa bbb



aab, aaaaa

aaaab

$\{w \in \{a,b\}^*: \#_a(w) = 2\#_b(w)\}$

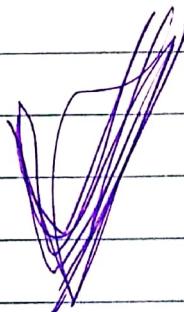


aaaab

aabbabbabb

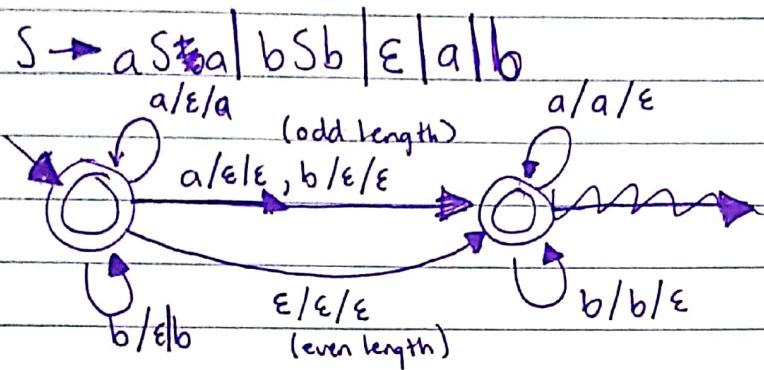
aaaa

aaaa



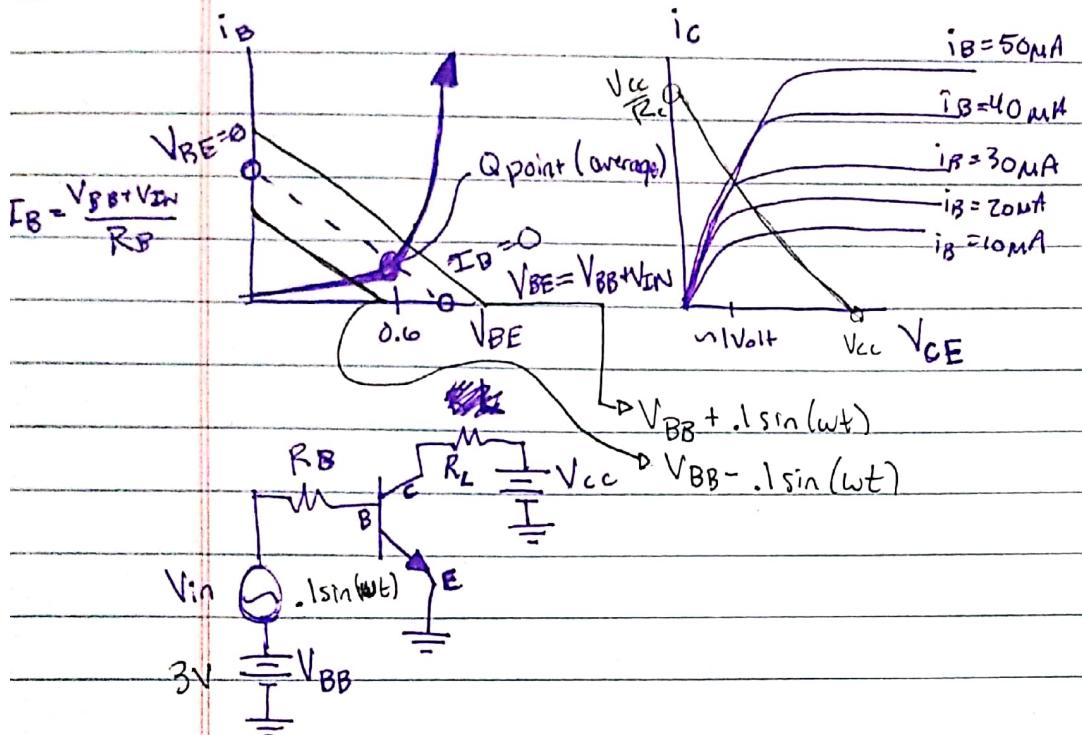
$$\{ w \in \{a, b\}^*: w = w^R \}$$

all palindromes, both even and odd



~~$w = a^k b^k$~~ even length palindrome
 \rightarrow no longer palindrome

~~$w = a^k b^k$~~
 \rightarrow ~~$a^{k+1} b^k$~~



$$\text{Loop \#1: } 0 + V_{BB} + V_{in} - V_{RB} - V_D = 0$$

$$V_{BB} + V_{in} - I_B R_B - V_{BE} = 0$$

$$I_B = \frac{V_{BB} + V_{in} - .25 \sin(2000\pi t)}{R_B} = \frac{8V + 0.25 \sin(2000\pi t)}{40k\Omega} = 0.00052 \text{ Amps}$$

$$V_{BE} = V_{BB} + V_{IN} = .8V + 0.25 \sin(2000\pi t) = 0.825 \text{ Volts} = .8$$

$$V_{BB} + .25 = 1 \text{ Volt}$$

$$\text{Loop 2: } V_{CC} - I_C R_C - V_{CE} = 0$$

$$V_{BB} - .25 = .6 \text{ Volt}$$

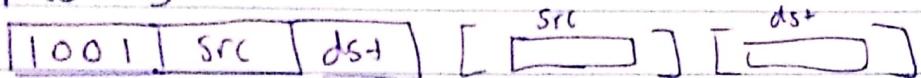
$$I_C = 0 \quad V_{CE} = V_{CC}$$

$$V_{CE} = 0$$

$$I_C = \frac{V_{CC}}{R_C}$$

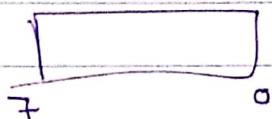
MOV src, dst

MOV B



N-HOB (7.)

CLRB



INCB

2's
comp.

MAXINT $\rightarrow 0111111(2^8-1)-1$

$\hookrightarrow +127$

DEC B

MININT $\rightarrow 10000000-(2^8-1)$

NEG B

$\hookrightarrow -127$

TST B

HSRB

CARDINAL

MAXINT $\rightarrow 1111111 \rightarrow 255$

ASLB

ADCB

SBCB

Strings

MOVB

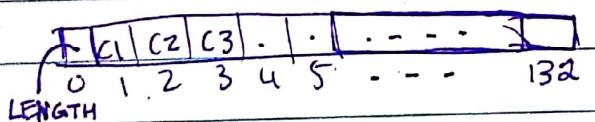
Linked lists? Arrays?

CMPB

\hookrightarrow overhead

\hookrightarrow extra empty space

132 characters SI: .BLKW 133.



[A|B|C]

COPY: MOV #132, R0

LOOP: MOVB SI(R0), S2(R0)

DEC R0

BGE LOOP

COPY: MOVB SI, R0 → sign exchange causes this
to break when length
is > 127.

LOOP: MOVB SI(R0), S2(R0)

DEC R0

BGE LOOP

TMP := BLKW 1

MOVB SI, TMP

~~MOVBL~~

~~MOVB #0, TMP~~

CLRB TMP+1

Mov TMP, R0

BR DST

[OP CODE] offset

BRANCHES to 2^*offset
can't reach very far

JMP DST

[OP CODE] DST

ANY ADDRESSING MODES ARE ALLOWED
so any address is reachable

BEQ X // too far so

BNE NEXT

JMP X

NEXT: ↗

Addressing Mode Review

MOV —, R0

MOV Ie., R0 → Relative Mode Addressing

Indirect Addressing

(4 of them)

Example (Post Office Box with mail forwarding)

MOV @4, R0

7,7

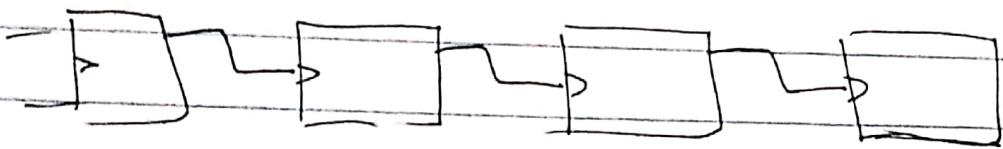
111 111

use the contents of 4 as the address
and store the contents of this address
in register 0

MOV @#28, R0

Absolute Mode Addressing

1.



~~111
011
001
000~~

~~111
110
101
000
011
010~~

$$11_{10} \rightarrow 1011_2$$

$$111 \rightarrow 7$$

$$110 \rightarrow 6$$

$$101 \rightarrow 5$$

$$100 \rightarrow 4$$

$$011 \rightarrow 3$$

$$010 \rightarrow 2$$

$$001 \rightarrow 1$$

$$000 \rightarrow 0$$

↓ ↓ ↓

25Hz .5Hz 1Hz

Switch case is not fair. It takes longer to get to the 4th case than the 1st, since it is ~~essentially~~ pretty much a big if else if...

I: .BLKW 1

TABLE: .WORD L10 (1 | 6)
 .WORD L20 2 | 2
 .WORD L30 3 | 4
 .WORD L40 4 | 0

; Table is an array [1 4] of type address
 Table(I)

Mov I, R0

Dec R0 ; bring down one
 ASL R0 ; times 2 because addresses occupy words
 -

Turn
Index
into
offset

JMP @TABLE(R0)

0 Register

1 Ind. Register

2, 7 Immediate

3, 7 Absolute

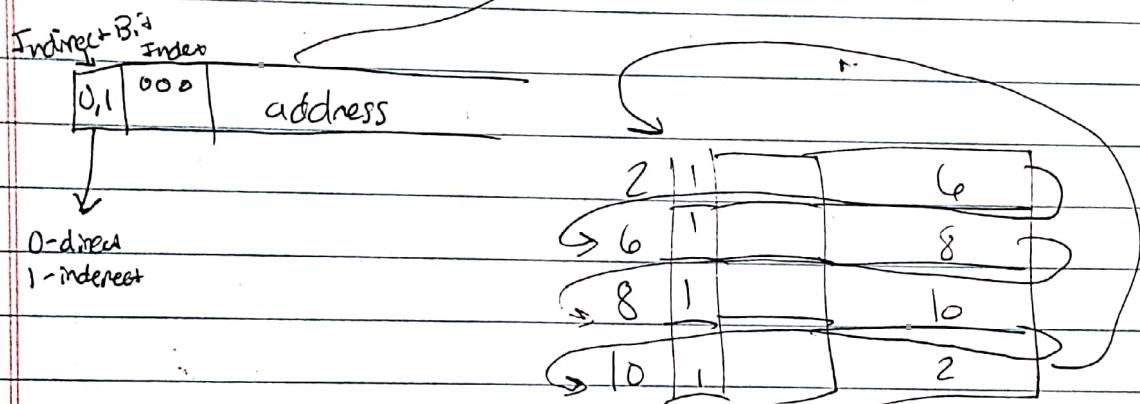
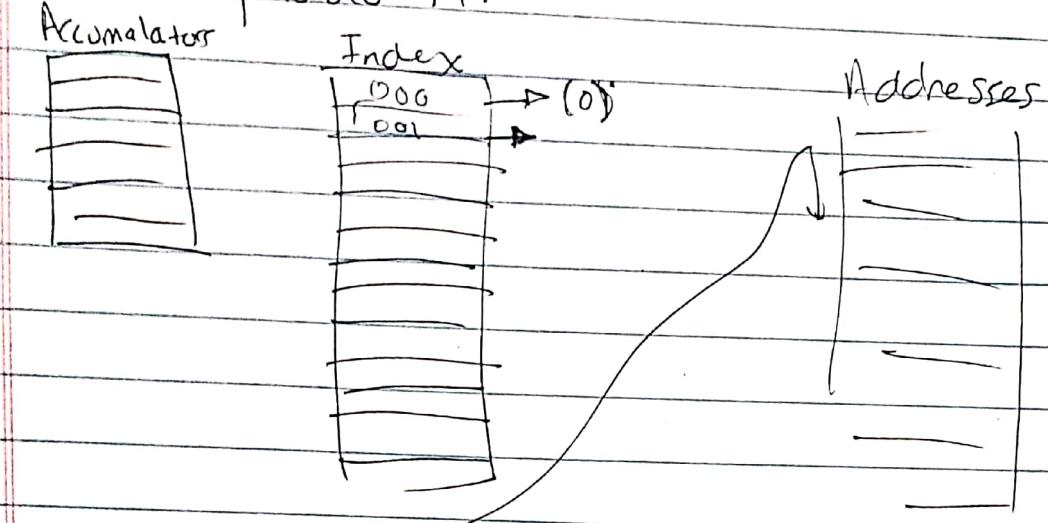
6, 7 Relative

7, 7

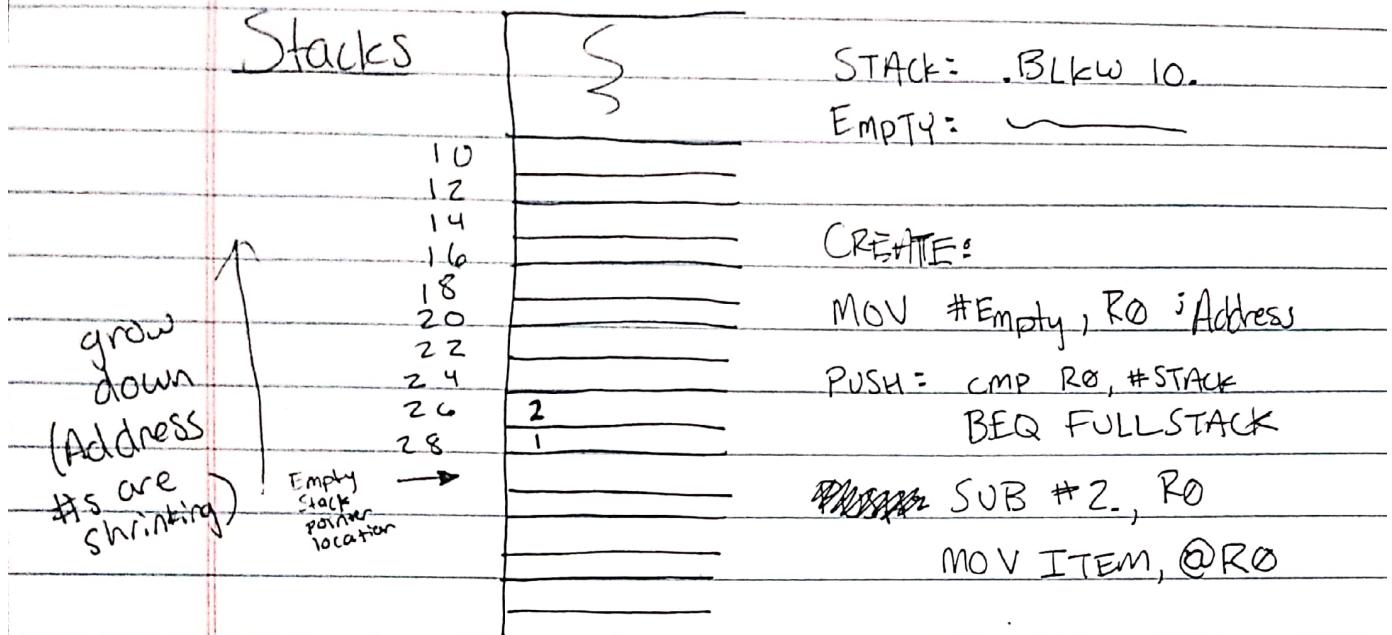
6, i Index

7, i Ind. Index

Other way to do it.



↗ Indirect address Loop



Stack pointer

STACK + 10. * 2 bytes

$$10 + 20 = 30$$

POP: CMP R0, EMPTY

BEQ EMPTY STACK

MOV @R0, wherever

ITEM	R0	ADD #2, R0
1	30	
2	28	
	26	

POP → 2 stays in memory, the stack just
goes wherever 28 doesn't care about it.

Addressing Mode 4 - Auto decrement mode addressing
4,0 → Register 0

use the address inside
the register and decrement
by 2 if word instruction
or 1 if byte instruction.

Registers 6 and 7
only decrement by 2

PC must be even. Register 6 is Stack Pointer (Special Stack)

PUSH: MOV ITEM, -(R0)

POP: MOV ITEM, *(R0) +

Auto Dec

4,0 $-(R0)$ decrement then use indirectly
MOV ITEM, $-(R0)$

Auto Inc

2,0 $+(R0)$ use ^{indirectly}, then increment
MOV $+(R0)$, whatever

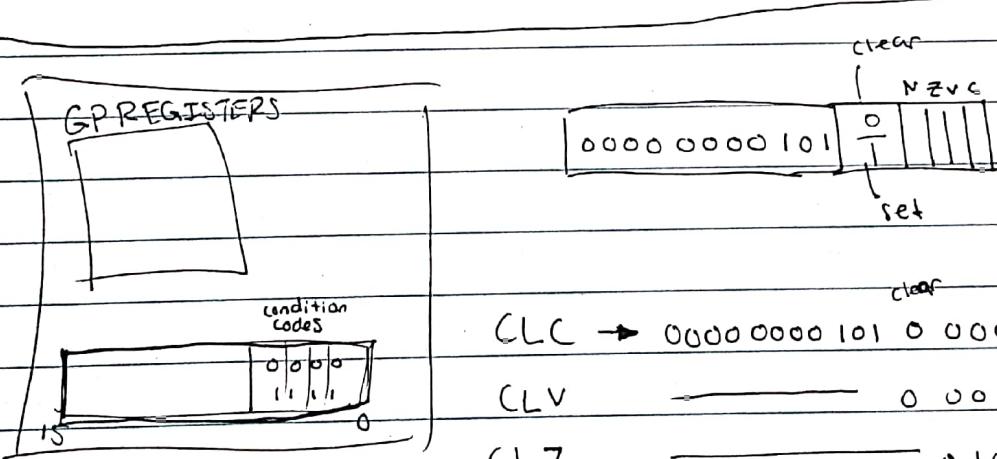
MOV #2, R0



PC

~~80.~~

22.



CLC \rightarrow 0000 0000 101 0 0001

CLV 0 0010

CLZ 0 100

NOP 0000 0000 101 0 0000 CLN 1000

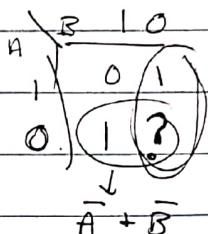
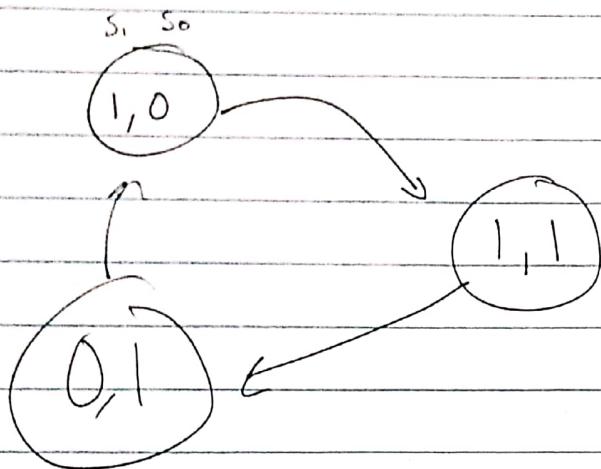
No op clear Nothing CCC 1111

Time Delay SEZ 10100

or SEN 1

Padding SEC 1

SCC 1111



A B

<u>OLD</u>	<u>NEW</u>
1 0	1 1

<u>OLD</u>	<u>NEW</u>
1 1	0 1

<u>OLD</u>	<u>NEW</u>
0 1	1 0

<u>OLD</u>	<u>NEW</u>
1 1	0 ?

A

1 0

INPUTS
NEW STATES

J₁ K₁ J₂ K₂

1 0 1 0

1 1

0 1 1 0

0 1

1 0 0 1

A ⊕ B AB A $\bar{A}B$

$$L = \{a^n b^{2n} a^{4n} : n \geq 0\}$$

Not
Context
Free

push a's on to stack

pop b's \rightarrow stack is empty, can't keep track
of $4n$ for the second a

$$\omega = a^k | b^{2k} | a^{4k}$$

(1) (2) (3)

at least k symbols, is accepted by L

v, y

(1,1) pump up once

$$a^{k+p} b^{2k} a^{4k}$$

$$1 \leq p \leq k$$

not accepted

(2,2) —————

$$a^k b^{2k+p} a^{4k}$$

$$—$$

not accepted

(3,3) —————

$$a^k b^{2k} a^{4k+p}$$

$$—$$

not accepted

(1,2) —————

$$a^{k+p} b^{2k+q} a^{4k}$$

$$not enough$$

—

(1,3) —————

$$a^{k+p} b^{2k} a^{4k+p}$$

$$—$$

v and y are more than k apart

(2,3) —————

$$a^k b^{2k+p} a^{4k+q}$$

$$not enough$$

not accepted

Span regions

pumping up will get them out of order

$$L = \{a^{n^2} : n \geq 0\}$$

NCF

can't keep track of n^2 with just a stack

$$a^{k^2}$$

(1)

since we only have one region, v and y must fall under

$$a^{k^2} \text{ so } \omega = a^{k^2+p} \quad 1 \leq p \leq k$$

if we pump up once

$$\omega = a^{k^2+1}$$

$$yy = a^p$$

The next string after a^{k^2} is $a^{(k+1)^2}$
 so $k^2 + 2k + 1$

$$p = 2k + 1 \text{ and } p >$$

$$so too big |y| \leq k$$

$$L = \{ w \in \{a, b, c\}^*: \#_a(w) = \#_b(w) = \#_c(w) \}$$

$$L' = L \cap a^* b^* c^*$$

$$= \underbrace{a^n b^n c^n : n \geq 0}$$

Context Free \cap regular = context free
 so w must also be context free

$\frac{1}{2} w = aabbcc$ not k length

$$w = a^k | b^k | c^k$$

(1) (2) (3)

(1,1) : $a^{k+p} \leq p \leq k$ ~~is~~ $a^{k+p} b^k c^k$ not accepted

~~(1,2)~~ :

(2,2) : $a^k b^{k+p} c^k \quad 1 \leq p \leq k$

(3,3) : $a^k b^k c^{k+p}$

(1,2) : $a^{k+p} b^{k+q} c^k$

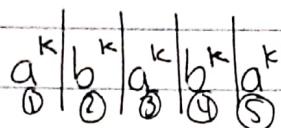
(2,3) : $a^k b^{k+p} c^{k+q}$

(1,3) : too far apart v y

cross : if crossed regions, pump would take letters
 Regions out of order

$$L = \{a^n b^m a^n b^m a^n : n, m \geq 0\}$$

can't keep track of n or m more than once
or at the same time in this order



$$(1,1) : a^{k+p} b^k a^k b^k a^k$$

$$(2,2) : a^k b^{k+p} a^k b^k a^k$$

$$(3,3) : a^k b^k a^{k+p} b^k a^k$$

$$(4,4) : a^k b^k a^k b^{k+p} a^k$$

$$(5,5) : a^k b^k a^k b^k a^{k+p}$$

$$(1,2) :$$

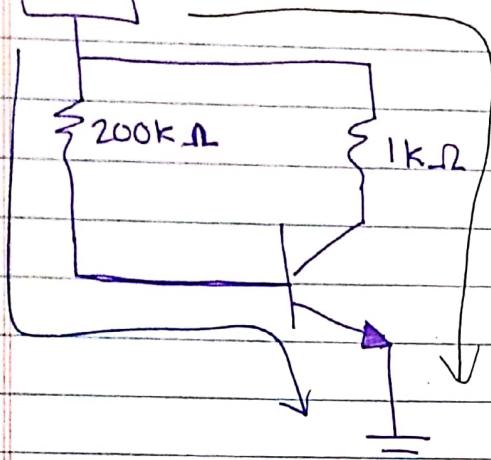
$$(2,3) :$$

$$(3,4) :$$

$$(4,5) :$$

span
regions:

$$V_{cc} = 15V$$



Or assume saturation

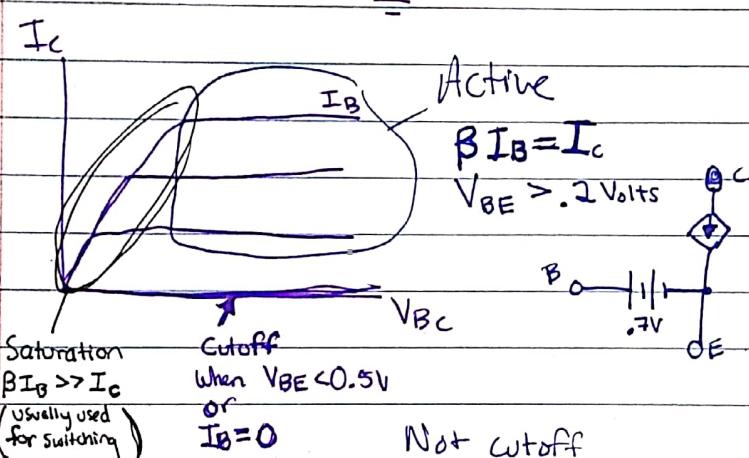
$$15 - I_c(100) - 2 = 0$$

$$I_c \approx 14.8 \text{ mA}$$

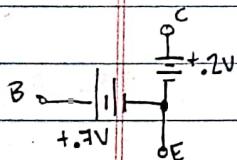
$$\beta = \frac{14.8 \text{ mA}}{72 \mu\text{A}} \approx 200$$

not to spec

"proved" wrong



V_{BC} is small



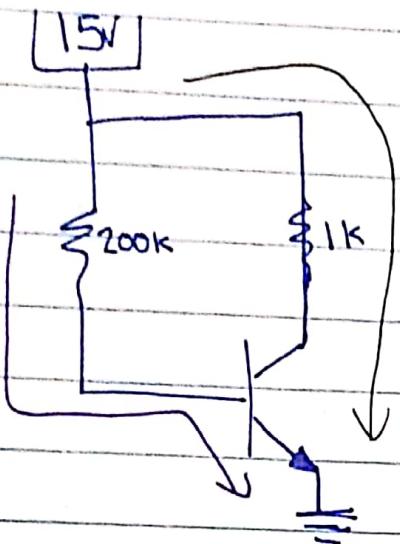
$$I_B = \frac{15 - 0.7}{200k} \approx 72 \mu\text{A}$$

$$\begin{aligned} \text{Assume Active} \rightarrow I_C &= 100(72 \mu\text{A}) \\ &= 7.2 \text{ mA} \end{aligned}$$

$$15 - 1000(I_c) - V_{CE} = 0$$

$$15 - 7.2 = V_{CE} \approx 7.8 \text{ Volts}$$

Makes sense for active region



$$\beta = 300$$

$$15 - 200k(I_B) = V_{BE}$$

Not in cutoff

Assume Active

$$15 - I_B(200k) \approx .7$$

$$I_B \approx 72\text{mA} \quad I_C = 300(72\mu\text{A}) \approx 21.6\text{mA}$$

$$15 - 1k(I_C) = V_{CE} \rightarrow 1kI_C = 15 \quad I_C = \frac{15}{1000}$$

$$15 - 1000(21.6\text{mA}) = V_{CE} \quad 15 = V_{CE}$$

$$15 - 21.6 = V_{CE} = 6.6$$

So not active

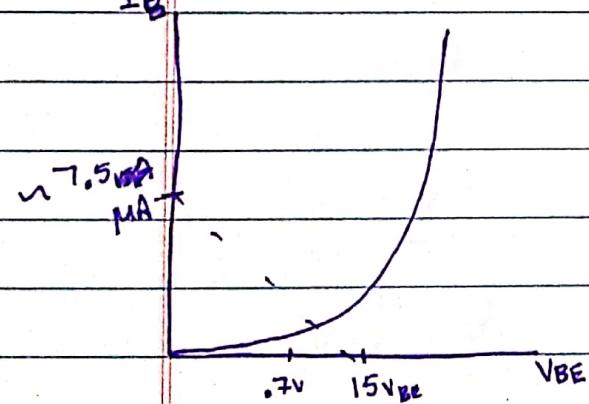
I_B

Saturation

$$15 - I_C(1000) = V_{CE}$$

$$15 - I_C(1000) = \cancel{6.6}.2$$

$$I_C = \frac{14.8}{1000} = 14.8\text{mA}$$



$$15 - I_B(200k) = V_{BE}$$

$$\beta = \frac{14.8}{72\text{mA}} \approx 200$$

$$I_B = \frac{15}{200k} \text{ when } V_{BE}=0$$

$$200 < 300 \quad \checkmark$$

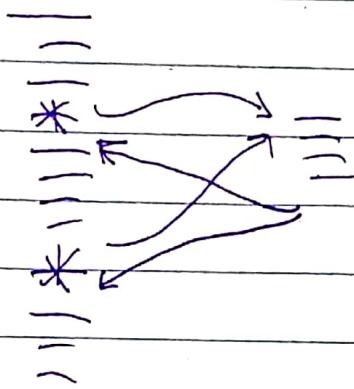
$$V_{BE} = 15 \text{ when } I_B=0$$

"Subroutine" - function, method, procedures, etc.

- Open (Macros)
- "Copy Paste"

- Closed

- goto sub and come back



Linkage Problem

1. Get to sub

2. Get back from sub

3. Share data

Newer higher level languages are "block structured"

Original higher — "non-block structured"

- Methods and Main Programs are compiled separately and Linked together by the Linker

MOV RAI, SUB

JMP SUB+2

RAI

RA2

SUB: RAI

use more
space here
for data
passing

JMP @ SUB

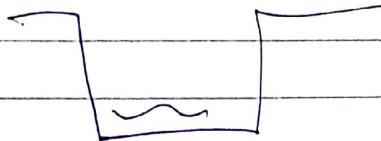
JSR R_i, dst

$\downarrow (SP) \leftarrow (R_i)$

$(R_i) \leftarrow (PC)$

$(PC) \leftarrow dst$

Assumes properly formed
stack at SP



RTS R_i

$(PC) \leftarrow (R_i)$

$(R_i) \leftarrow (SP)$

TABLE:

# of arguments	3
address A ₁	
address A ₂	
address A ₃	

MOV #ARGTBL, R5

JSR PC, ADDER

RA:

ITMP=S

I = ITMP+K

RETURN

ARGTBL WORD 3

WORD IA

ADDER: MOV @4(R5), ITMP

WORD IB

MOV ITMP, @2(R5)

WORD IC

ADD @6(R5), @2(R5)

IA: BLKW ~~BB~~ 1

RTS PC

IB: BLKW 1

IC: BLKW 1

2 more pages for block structure version

Non-Restoring Division Example (5 bit)

$$X = 15_{10} = 01111_2$$

$$N=5$$

$$Y = 4_{10} = 00100_2$$

1. Make X double precision $01111 \rightarrow 00000\ 01111$

$$\text{Loop Counter} = N-1 \rightarrow 5-1 = 4 \quad i=4$$

$$\text{Subtract } 00100 * 2^4 \quad 2^i * Y \quad (\text{shift left } 4 \text{ times})$$

$$\begin{array}{r} \rightarrow X & 00000\ 01111 \\ \rightarrow Y & 00010\ 00000 \\ & \hline & \text{Subtract} \\ & 11110\ 01111 \end{array}$$

3. if negative $q_i = 0$ else $q_i = 1$ $q_4 = 0$

$$i = -1 \rightarrow 3 \rightarrow 2 \quad q_3 = 0$$

$$q_2 = 0$$

$$q_1 = 1 \quad q_0 = 1$$

4. if neg add $2^i * Y$ to result else sub $2^i * Y$

$$\begin{array}{r} 11110\ 01111 \\ + 00001\ 00000 \\ \hline 11111\ 01111 \\ + 00000\ 10000 \\ \hline 11111\ 11111 \\ + 00000\ 01000 \\ \hline 11111\ 00111 \\ - 00000\ 00100 \\ \hline 00000\ 00011 \end{array}$$

↓

neg ~~00000~~ goto step 3

$q_3 = 0$

$q_2 = 0$

$q_1 = 1$

$q_0 = 1$

sub because last answer was non neg

quotient cause $i = -1$

00011

All double Precision Arithm.

QUESTION

Adder (I, J, K)

Var I, J, K : INT

I = TMP + J

I = I + K

Return

Driver

Build, use, deconstruct

SUB #2, SP

MOV #IA, -(SP)

MOV #IB, -(SP)

MOV #RA, -(SP)

JMP ADDER

RA: ADD #10, (SP)

ITMP	Arg IA	Arg IB	Arg IC	Ret. Addr
------	--------	--------	--------	-----------

"Activation Record"
"Stack Frame"

Pointer to
NORMALLY
BUT LEP ~~KEEP~~
IT'S SIMPLE

800	RA	200	0
802	IA	1004	2
804	IB	1002	4
806	JA	1000	6
808	ITMP		8

To Allow for nested calls let's put
our activation record on a stack

SUBROUTINES SUPPORT

① REUSABLE

② RECURSIVE

③ REENTRANT

↳ Multiprocessing

mm

CPU

P1

P2

P3

ADDER: MOV @4(SP), B(SP)

MOV B(SP), @6(SP)

COPY IB
TO ITMP

COPY ITMP
TO IC

ADD @6(SP), 2 @6(SP)

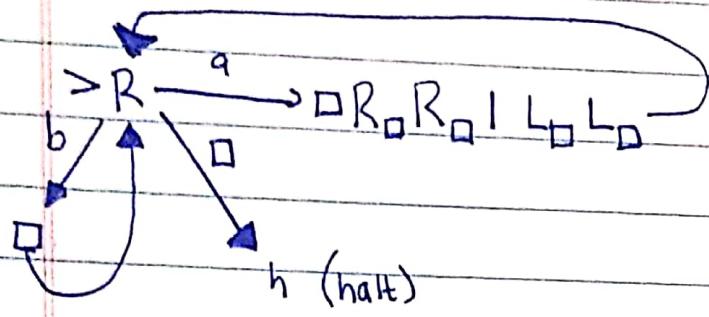
ADD IA
TO IC

JMP @ (SP)

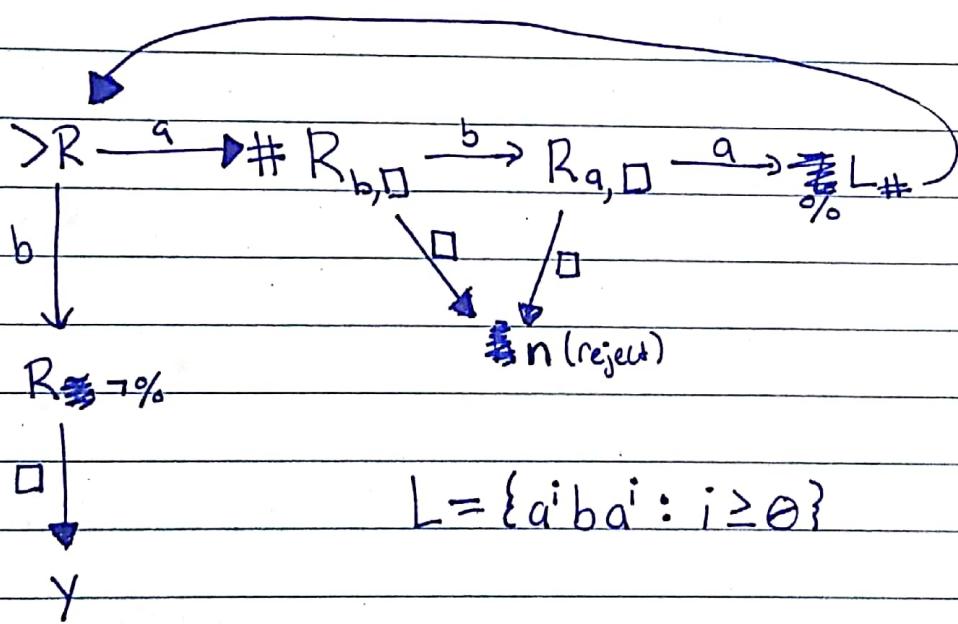
STATE INFORMATION

→ COPYING this to main
memory we call a
CONTEXT SWITCH

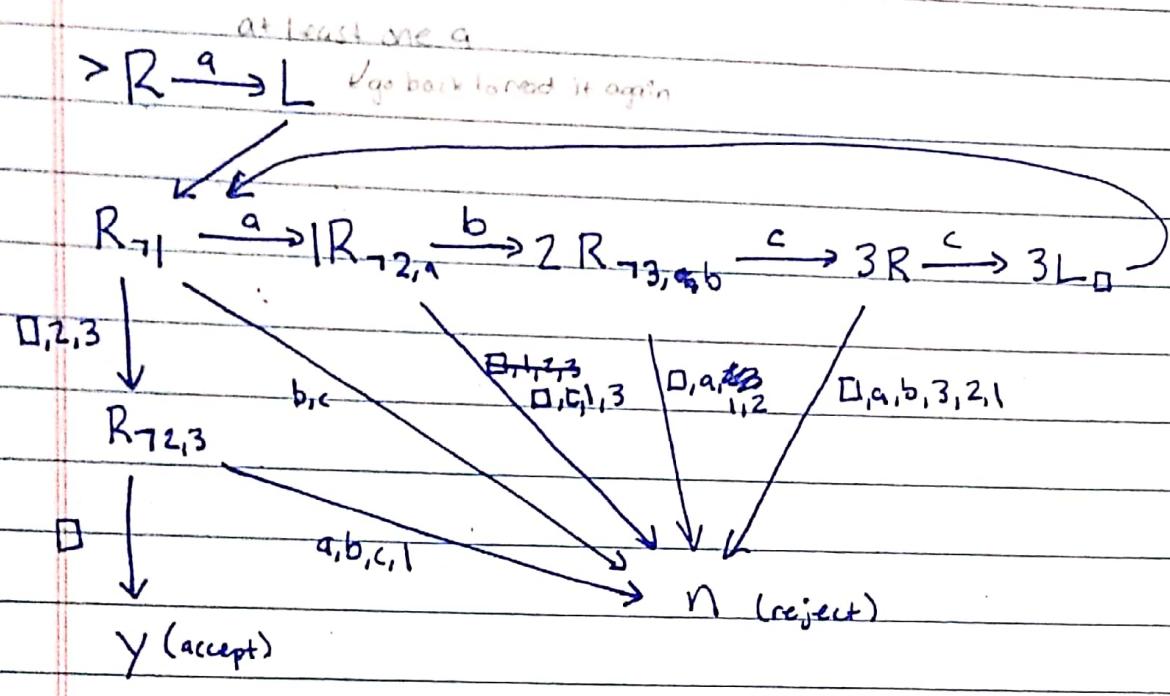
Turing Machines



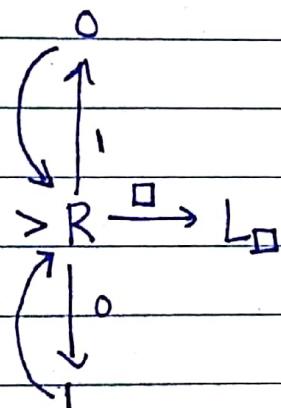
$\square a b a \square$
 \downarrow
 $\square \square b a \square$
 $\square \square \square a \square | \square \square$
 $\square \square \square \square | \square \square \square$
 $\square \square \square \square h | \square \square \square$



$$L = \{a^n b^n c^n : n \geq 1\}$$



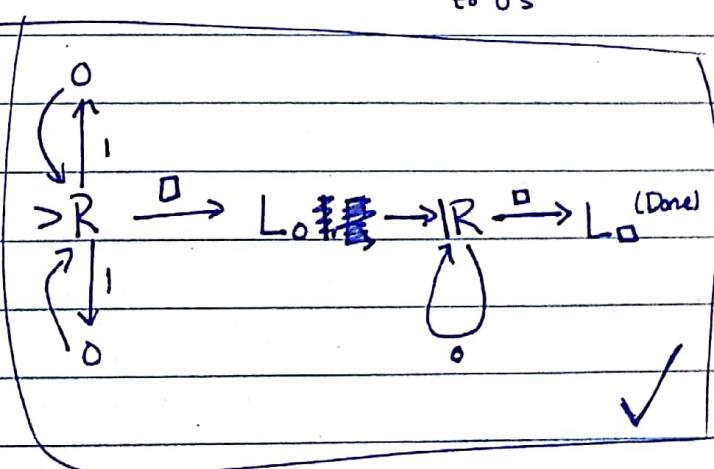
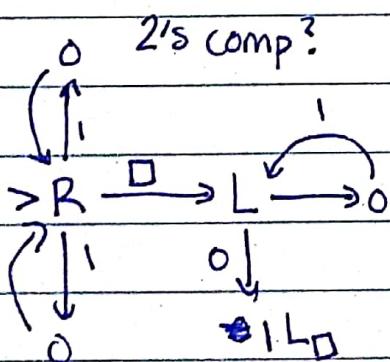
Compute the complement of a binary # on the tape



$\square 0xx0xx\square$
 $\square 1001000\square$

100011
100100

Find the first 0 from
the right and add
flip to 1, flip all
bits to the right
to 0s



Double Binary #

$> R_0 \square L_0$ (shift left 1)

Halve # (no leading zero)

$\begin{matrix} & \xrightarrow{\text{!}} & R & \xrightarrow{0,1} & R_0 L \square L_0 \\ 0 \downarrow & & \square \downarrow & & \\ L & & LOL & & \end{matrix}$

Russian Multiplication (2 binary #'s)
^{partant}

$$\begin{array}{l} axb \\ 2a \times \frac{b}{2} \quad b \text{ even} \\ 2a \times \frac{b-1}{2} + a \quad b \text{ odd} \end{array}$$

$A > B$

		B, B ₀		00		01		11		10	
A, A_0	\downarrow	0	1	0	0	1	1	1	1	0	0
00											
01											
11											
10											

A, \bar{B}_1

A_0, B, \bar{B}_0

\bar{B}_0, A, A_0

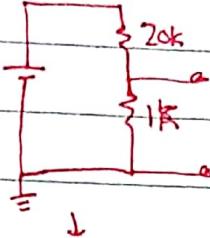
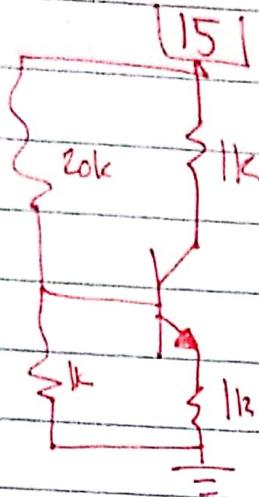
		B, B ₀		00 01 11 10			
A, A_0	\downarrow						
00		1 0 0 0					
01		0 1 0 0					
11		0 0 1 0					
10		0 0 0 1					

		B, B ₀		00 01 11 10			
A, A_0	\downarrow						
00		0 1 1 1					
01		0 0 1 1					
11		0 0 0 0					
10		0 0 1 0					

\bar{A}, B_1

B_0, A, A_0

B, B_0, \bar{A}_0



$$\frac{2k}{2k+1k} \rightarrow \frac{2k}{3k} = 0.6667 \rightarrow 952.38\Omega$$

$$71428 \text{ Volt} \downarrow I = 750 \mu\text{A}$$

$$15 - 20k(I_B + I_C) - 1k(I_E) = 0$$

$$-20kI_B - 20kI_C - 1kI_E = -15$$

$$-20kI_B - 20kI_C = -15$$

$$\begin{array}{c|c} I_B & I_E \\ \hline -20k & 0 \\ 0 & 0 \\ 0 & 0 \end{array} \quad | -15$$

$$15 - 1kI_C - V_{CE} - 1kI_E = 0$$

$$-V_{CE} - 1kI_C - 1k(I_B + I_C) = -15$$

$$-1kI_B - V_{CE} - 2kI_C = -15 \rightarrow -1k \quad 0 \quad -1 \quad -2k \quad | -15$$

$$15 - 20k(I_C + I_B) - 1kI_E = 0$$

$$-20kI_B - 20kI_C - 1k(I_B + I_C) = 14.3$$

$$-20kI_B - 20kI_C - 1kI_B - 1kI_C = -14.3$$

$$-21kI_B - 20kI_C - 1kI_C = -14.3 \rightarrow -21k - 20k \quad 0 \quad -1k \quad | -14.3$$

Week from thursday
Today is Oct 21st, Tuesday

Nth Prime Number

Write a program to find the Nth prime number. For our purposes, the first three primes are 2,3 and 5.

Do not use arrays or indexed mode addressing. This eliminates a class of algorithms such as sieves.

While the restriction above limits your ability to write a real efficient program, you should try to be as efficient as possible given these limitations.

```
;  
;      Data Area  
;  
N:     .BLKW    1          ;IN - 2's complement > 0  
PRIME: .BLKW   1          ;OUT - 2's complement Nth prime or  
;                      ;-32768. As error msg.  
.END
```

- 4.15.** An *npn* transistor has $V_{BE} = 0.7\text{ V}$ for $I_E = 10\text{ mA}$. Find V_{BE} if $I_E = 1\text{ mA}$. Repeat for $I_E = 1\text{ }\mu\text{A}$. Assume a temperature of 300 K.

- D4.16. Beta meter.** Design a “ β -meter” for measurement of the β of small-signal *npn* silicon transistors at room temperature. Assume that $v_{BE} = 0.7$ for the transistors to be measured. The following parts are available:

1. A 1-mA-full-scale meter having a resistance of 150Ω .
2. Standard 5%-tolerance resistors. (See Appendix A.)
3. Potentiometers of 100Ω , $1\text{k}\Omega$, $10\text{k}\Omega$, $100\text{k}\Omega$, and $1\text{M}\Omega$.
4. A 4.7-V Zener diode.
5. Switches and mechanical components, as required.
6. A 9-V “transistor” battery.

The meter is to have switch-selectable full-scale values of $\beta_{FS} = 10, 100, \text{ and } 1000$. Adjustments are to be provided that allow calibration of the meter, which is to provide accurate readings for battery voltages ranging from 7 to 9 V. Under reasonable operating conditions (including short-circuited test terminals), the battery drain should not exceed 5 mA. Suggestions:

1. Use a Zener diode regulator to obtain a constant source voltage for delivering base current to the transistor.
2. Use a switch and resistor network to apply a suitable base current to the transistor under test for each range of β to be measured.
3. Use the meter to measure the collector current with full scale corresponding to $\beta = 10, 100, \text{ or } 1000$.

- 4.17.** Use SPICE to obtain output characteristics for an *npn* BJT having $I_s = 10^{-16}\text{ A}$, $\beta = 200$, and $V_A = 25\text{ V}$. Allow v_{CE} to range from 0 to 10 V, and let $i_B = 0, 10, 20, 30, 40, \text{ and } 50\text{ }\mu\text{A}$.

- 4.18.** Use SPICE to obtain input characteristics for an *npn* BJT having $I_s = 10^{-16}\text{ A}$, $\beta = 200$, and $V_A = 25\text{ V}$. Set $v_{CE} = 10\text{ V}$, and allow v_{BE} to range from 0 to 0.7 V.

Section 4.2: Load-Line Analysis of a Common-Emitter Amplifier

- 4.19.** What can cause distortion in BJT amplifiers?

- 4.20.** Consider the circuit of Figure 4.10. Assume that $V_{CC} = 20\text{ V}$, $V_{BB} = 0.8\text{ V}$, $R_B = 40\text{k}\Omega$, and $R_C = 2\text{k}\Omega$. The input signal is a 0.2-V-peak, 1-kHz sinusoid given by $v_{in}(t) = 0.2\sin(2000\pi t)$. The common-emitter characteristics for the transistor are shown in Figure P4.20. Find the maximum, minimum, and Q -point values for v_{CE} . What is the approximate voltage gain for this circuit?

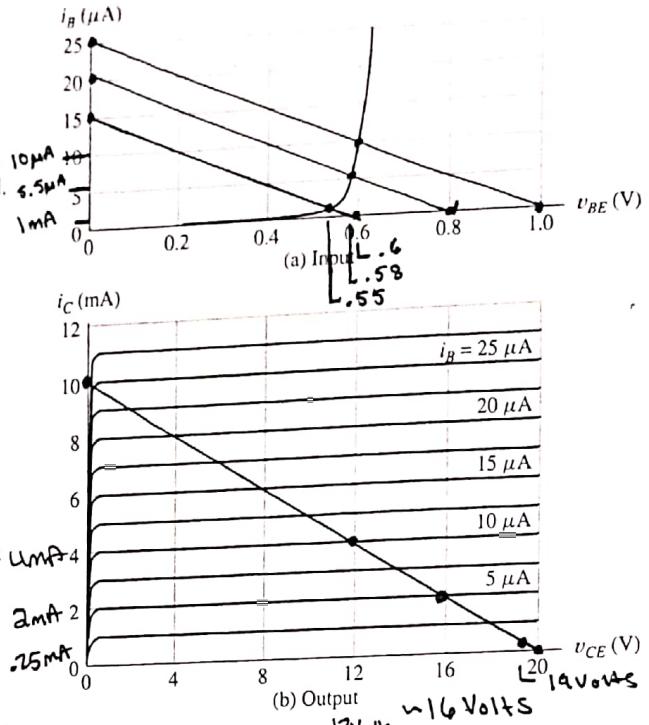


Figure P4.20

- 4.21.** Repeat Problem 4.20 for $R_C = 10\text{k}\Omega$. What can you say about the waveform for $v_{CE}(t)$?

- 4.22.** Repeat Problem 4.20 for $V_{BB} = 0.3\text{ V}$. Why is the gain so small in magnitude?

Section 4.3: The *pnp* Bipolar Junction Transistor

- 4.23.** Draw the circuit symbol for a *pnp* BJT. Label the terminals and the currents. Choose reference directions that agree with the true directions of the current for operation in the active region.

- 4.24.** A certain *pnp* silicon transistor has $\beta = 100$ and $i_B = 0.1\text{ mA}$. Sketch i_C against v_{CE} for v_{CE} ranging from 0 to -5 V . Repeat for $\beta = 300$. Ignore second-order effects.

- 4.25.** At a temperature of 30°C , a particular *pnp* transistor has $V_{BE} = -0.7\text{ V}$ for $I_E = 2\text{ mA}$. Estimate V_{BE} for $I_E = 0.1\text{ mA}$ at a temperature of 180°C .

Section 4.4: Large-Signal DC Circuit Models

- 4.26.** Draw the large-signal dc circuit model for a silicon *npn* transistor operating in the active region at room temperature. Include the constraints of any currents or voltages that guarantee