Ex vivo Magnetic Resonance Diffusion Weighted Imaging in Congenital Heart Disease, an Insight into the Microstructures of Tetralogy of Fallot, Biventricular and Univentricular Systemic Right Ventricle

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Ex vivo Magnetic Resonance Diffusion Weighted Imaging in Congenital Heart Disease,
an Insight into the Microstructures of Tetralogy of Fallot,
Biventricular and Univentricular Systemic Right Ventricle (Tous et al, 2020)
from the Journal of Cardiovascular Magnetic Resonance Imaging. This sequence
was part of a comparison between SE monopolar, SE bipolar, STEAM monopolar,
TRSE and TRSE adjusted to scan long term (~40 years) formalin fixed specimens
with low T2 (~20 ms). The scans were performed on a 3 T Skyra bought in
the early 2010 (43 mT / m gradient amplitude, 180 mT / m / ms slew rate).

SE bipolar :

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(* modified mathematica from (Mattiello et al, 1995) and (Zubkov et al, 2014) *)
Date : 22/09/2017;
Input :
Known sequence diagram of the diffusion sequence with the timing and gradients' amplitude;
Output : B matrix [ndir, 6] with ndir the number of diffusion directions,
and Bmatrix[1, :] = [Bxx, Byy, Bzz, 2 Bxy, 2 Bxz, 2 Byz];
Goal :
= > Generating the B matrix from the known sequence diagram;
= > determining M0 = F = Integral (g (t)), M1 = Integral (t*g (t)),
M2 = Integral (t^2*g (t)) for the zeroth moment, first moment, second moment;
= > Calculating velocity shift Kv = γ*M1, d = Integral (F^2),
Maxwell gradient moment = Integral (g (t)^2);

method : References :
–' Spin Diffusion Measurements : Spin Echoes in the Presence of a Time – Dependent Field Gradient' (STEjskal and Tanner, 1965);
–' Tissue Perfusion in Humans Studied by Fourier Velocity Distribution, Line Scan, and Echo Planar Imaging' (Feinberg, 1990);
– ' Analytical expressions for the b matrix in NMR diffusion Imaging and Spectroscopy' (Mattiello et al, 1993);
– ' Estimation of the Effective Self Diffusion TEnsor from the NMR Spin Echo' (Basser et al, 1993);
– ' Part II Analytical Calculation of the b Matrix in Diffusion Imaging' (Mattiello et al, 1995); = > (Mathematica);
– ' Pusled – Field Gradient Nuclear Magnetic Resonance as a tool for studying translational diffusion : Part 1 Basic Theory' (Price 1997);
– ' The b matrix in diffusion TEnsor echo planar imaging' (Mattiello et al, 1997);
–' Reduction of eddy – current – induced distortion in diffusion MRI using a twice – refocused spin echo' (Reese, 2003);
–' Handbook of MRI Pulse Sequences (Bernstein, King, Zhou, 2004)'
–' Double spin echo diffusion weighting with a modified eddy current adjustment' (FinsTErbusch, 2010);
– ' Efficient and precise calculation of the b matrix elements in diffusion weigthed imaging pulse sequences' (Zubkov et al, 2014);
= > (Mathematica);
–' Orthogonalizing crusher and diffusion – encoding gradients to suppress undesired echo pathways in the twice – refocused spin echo diffusion sequence' (Nagy, 2014);

```
(*
      90          δ               180              δ                  echo

      _        ______          _             _______
     ||       |      |         ||            |      |                 ||||
    -----------------------------------------------------------------
*)
"Pulsed Field Gradient Nuclear Magnetic resonance as a Tool
   for Studying Translational Diffusion: Part 1. Basic Theory(Price, 1996)";
ClearAll["Global`*"]
F[g_, ti_] = ∫_ti^t g ⅆtd;
g1 = 0;
l1 = 0;
F1 = F[g1, l1];

l2 = t1;
g2 = g;
F2 = Replace[F1, t → l2, All] + F[g2, l2];

l3 = t1 + δ;
g3 = 0;
F3 = Replace[F2, t → l3, All] + F[g3, l3];

l4 = t1 + Δ;
g4 = g;
F4 = Replace[F3, t → l4, All] + F[g4, l4] ;

l5 = t1 + Δ + δ ;
g5 = 0;
F5 = Replace[F4, t → l5, All] + F[g5, l5];

l6 = 2 * τ;

(* Define the function "f" [=F(tau)] *)
f = Replace[F3, t → τ, All];

(* Define the integral of F between τ and 2τ *)
(* FINT = Simplify[∫_τ^l4 F3 ⅆt+ ∫_l4^l5 F4ⅆt+ ∫_l5^l6 F5ⅆt ] *)
FINT = Simplify[
   Integrate[F3, {t, τ, l4}] + Integrate[F4, {t, l4, l5}] + Integrate[F5, {t, l5, l6}]];

(* Define the integral of F^2 between 0 and 2τ *)
FSQINT = Simplify[Integrate[F1^2, {t, l1, l2}] + Integrate[F2^2, {t, l2, l3}] +
    Integrate[F3^2, {t, l3, l4}] + Integrate[F4^2, {t, l4, l5}]
            + Integrate[F5^2, {t, l5, l6}]];

(* Define the function to give the STEjskal
 and Tanner relationaship and simplify the result *)
logE = Simplify[-γ^2 * D * (FSQINT - 4 * f * FINT + 4 * f^2 * τ )]
(* D g² γ² δ² (δ/3-Δ)*)
```

In[373]:=

Defining the bipolar gradient pulse and its integral;

In[374]:=

"code adapted from: 'Efficient and precise calculation of the b matrix elements in diffusion weigthed imaging pulse sequences' (Zubkov et al, 2014); (Mathematica)";

```
ClearAll["Global`*"]
trap[δ_, ϵ_, β_, t_] = β * Clip[UnitTriangle[2 t / (δ + ϵ) - 1] * (ϵ + δ) / (2 ϵ)];
(*defining the trapezoidal gradient pulse*)

ScaleDiagram = 50.;

ndir = 32;
bvalueInput = 800;

(*our values (2017);*)
γ = 2. * Pi * 42.5756 * 1000000;
ϵ = 400. * 10^-6; (*[s]*)
shiftADC = 500. * 10^-6; (*[s]*)
tReadout = 7700. * 10^-6; (*[s]*)
rampReadout = 10. * 10^-6; (*[s]*)
GmaxDiff = 36. * 10^-2; (*[G/mm]*)
GmaxCrush = 19.79 * 10^-2; (*[G/mm]*)
RampGrdp = 60. * 10^-6; (*[s]*)
RampGpe = 50. * 10^-6; (*[s]*)
RampGsrf = 120. * 10^-6; (*[s]*)
RampCrushers = 240. * 10^-6; (*[s]*)
PhaseDispersionCrushers = 6.;
SliceThickness = 4.; (*[mm]*)

(* Bernstein et al, handbook of MRI pusle sequences *)
(* Duration of the crushers' gradients according to the phase dispersion input. *)
AreaCrushers = PhaseDispersionCrushers * Pi / (γ * 0.000001 * SliceThickness * 0.001);
DurationCrushers = N[Round[AreaCrushers / (GmaxCrush * 10^2 * 0.001)]];

(* For the graph's plot and kvslice ;*)
(*SignDelta={1.,1.};*)

(*For the bmatrix calculation;*)
SignDelta = {1., -1.};

(* " Optimal strategies for measuring diffusion in
   anisotropic systems by magnetic resonance imaging" (Jones, 1999)*)
(* we have sorted the gradient encoding scheme to alternate between
 the gradient axis at each new direction*)
(* 6dir Electrostatic Repulsions *)
GradDiff6 = {{-0.887689, -0.101313, -0.449159},
{0.152552, 0.851204, 0.502175},
```

```
{-0.006226, 0.064447, -0.997902},
{0.789559, -0.384929, -0.47794},
{-0.399917, 0.82842, -0.392157},
{0.636679, 0.653135, -0.409945}} // MatrixForm;

(* 32dir:Electrostatic Repulsion scheme *)
GradDiff32 = {{0.978177, -0.099085, -0.182624},
{0.004364, -0.977355, 0.211562},
{0.058008, -0.049572, -0.997085},
{-0.951171, 0.161172, -0.263244},
{0.117967, -0.96576, -0.231065},
{-0.20677, 0.303548, -0.93011},
{-0.944892, -0.293928, -0.144174},
{-0.353468, -0.934011, -0.05181},
{-0.435353, -0.090815, -0.895667},
{0.890215, 0.360105, -0.279001},
{0.519013, -0.854199, -0.031151},
{-0.102942, -0.448113, -0.88803},
{0.841861, -0.525064, -0.124811},
{0.378146, 0.845537, -0.376926},
{0.478308, 0.041353, -0.877218},
{0.801211, 0.063809, -0.59497},
{-0.281684, -0.832306, -0.477411},
{0.231306, 0.428135, -0.873612},
{-0.80002, -0.223072, -0.556963},
{-0.348364, -0.817823, 0.458049},
{0.37987, -0.40282, -0.832727},
{-0.760744, 0.566441, -0.316879},
{0.11871, -0.750307, -0.650344},
{-0.49852, -0.514078, -0.697998},
{0.74759, -0.362889, -0.556256},
{0.029535, -0.733272, 0.679294},
{-0.467151 , 0.549242, -0.692895},
{0.716315, -0.197382, 0.669278},
{0.514837, -0.726299, -0.455448},
{-0.697256, -0.653755, -0.294005},
{-0.680714, -0.715159, 0.15867},
{0.599777, 0.492419, -0.630707}} // MatrixForm;

(* 64dir Electrostatic Repulsions *)
GradDiff64 = {{-0.997625, -0.026724, 0.063488},
{-0.154722, 0.987867, 0.013398},
{-0.015834, -0.014472, -0.99977},
{0.963101, -0.267540, 0, .029315},
{-0.12564, -0.9854060, 0.114845},
{0.065038, 0.29541300, -0.953153},
{-0.959665, -0.2166720, -0.179153},
{0.006778, -0.955284, -0.295611},
{0.30751, 0.090828, -0.9472},
{0.949992, -0.0861430, 0.300156},
{-0.27859, -0.9485760, -0.150306},
```

```
{-0.055576, -0.316879, -0.946836},
{0.927325, -0.21633400, -0.305397},
{-0.132838, 0.93592300, -0.326194},
{-0.3284670, -0.0346480, -0.94388},
{0.926285, 0.117378, -0.358076},
{-0.419397, 0.89762, 0.135587},
{0.2760480, -0.2176970, -0.936165},
{0.923215, 0.3629970, -0.126124},
{0.208215, 0.891081, -0.403263},
{-0.239236, 0.2854840, -0.928044},
{0.83921, -0.379789, 0.389213},
{0.446139, 0.883423, -0.143262},
{-0.370819, -0.344175, -0.862576},
{-0.837437, 0.5327130, -0.12213},
{-0.423944, 0.882753, -0.202533},
{0.218118, -0.5048100, -0.835219},
{-0.835774, -0.104423, -0.539052},
{0.291451, -0.8639870, -0.410588},
{0.304862, 0.464001, -0.831722},
{-0.834875, 0.510044, 0.206975},
{-0.141862, -0.824696, -0.547496},
{-0.020026, 0.576391, -0.816928},
{-0.830952, -0.381428, -0.405009},
{-0.407192, -0.82266700, -0.396753},
{-0.522214, 0.248724, -0.815738},
{0.827364, 0.548564, 0.12061},
{-0.063469 , 0.795508, -0.60261},
{0.580539, -0.068549, -0.811342},
{0.797023, -0.136705, -0.588273},
{0.601245, 0.789791, 0.121382},
{0.539573, 0.252383, -0.803221},
{0.792823, 0.455369, -0.405057},
{-0.378698, 0.766359, -0.518923},
{-0.122014, -0.589755, -0.798312},
{0.768559 , 0.1941, -0.609624},
{0.66151, -0.749911, -0.006173},
{-0.607712, -0.077141, -0.790402},
{-0.762479 , 0.1863260, -0.619604},
{0.137929, -0.7466040, -0.650813},
{0.532848, -0.37023500, -0.760920},
{0.734088, -0.4443650, -0.513473},
{-0.524955, -0.74215100, 0.416694},
{-0.332668 , 0.55742500, -0.760663},
{0.726209, 0.66617000, -0.169821},
{0.611904, -0.7124550, -0.343485},
{-0.637493, -0.37653400, -0.672179},
{0.269452, 0.7119370, -0.648492},
{-0.413285, -0.619494, -0.6674},
{-0.651714, -0.630831, -0.421095},
{-0.645004 , 0.682074, -0.344595},
{0.456964, -0.642255, -0.61538},
```

```
{0.576347, 0.522314, -0.6285},
{-0.611822 , 0.50219, -0.611129}} // MatrixForm;

Switch[ndir, 4, GradDiff = GradDiff4, 6, GradDiff = GradDiff6,
  32, GradDiff = GradDiff32, 64, GradDiff = GradDiff64];

(*"Orthogonalizing crusher and diffusion-encoding gradients to suppress undesired echo
  pathways in the twice-refocused spin echo diffusion sequence(Nagy, 2014)"*)
dir = 1;
While[dir < ndir + 1,
  if [((Abs[GradDiff[[1, dir, 1]]] + Abs[GradDiff[[1, dir, 3]]]) ≠ 0.),
   CoordCrusherX[dir] = -Sign[GradDiff[[1, dir, 1]] * GmaxDiff * 10^2] *
     Sign[GradDiff[[1, dir, 3]] * GmaxDiff * 10^2] *
     (1 - Abs[GradDiff[[1, dir, 1]]] /
        (Abs[GradDiff[[1, dir, 1]]] + Abs[GradDiff[[1, dir, 3]]]));
   CoordCrusherY[dir] = 0.;
   CoordCrusherZ[dir] = 1. - Abs[CoordCrusherX[dir]];
   ,
   CoordCrusherX[dir] = GradDiff[[1, dir, 1]];
   CoordCrusherY[dir] = 0.;
   CoordCrusherZ[dir] = 1. - Abs[CoordCrusherX[dir]]
  ];

  (* (our values, 2017) *)
  subamp[dir] =
   {Gsl90 → 0.075 * 10^2 * 10^-6, Gsl180 → 0.06 * 10^2 * 10^-6, Gsrf → -0.1982 * 10^2 * 10^-6,
    Gpe → 0. * 10^2 * 10^-6, Grdp → 0.1071 * 10^2 * 10^-6, Gro → 0.0153 * 10^2 * 10^-6,
    Gcr → GmaxCrush * CoordCrusherX[dir] * 10^2 * 10^-6,
    Gcp → GmaxCrush * CoordCrusherY[dir] * 10^2 * 10^-6,
    Gcs → GmaxCrush * CoordCrusherZ[dir] * 10^2 * 10^-6,
    Gdr → GmaxDiff * GradDiff[[1, dir, 1]] * 10^2 * 10^-6,
    Gdp → GmaxDiff * GradDiff[[1, dir, 2]] * 10^2 * 10^-6,
    Gds → GmaxDiff * GradDiff[[1, dir, 3]] * 10^2 * 10^-6};
  dir++];

(* (our values, 2017) *)
time1 = N[{TE → 90100 * 10^-6, Gsl90t → 2960 * 10^-6, Gsl180t → 3840 * 10^-6, Grdpt →
     560 * 10^-6 + RampGrdp, Gpet → 580 * 10^-6 + RampGpe, Gsrft → 440 * 10^-6 + RampGsrf,
    Grot → tReadout + shiftADC + rampReadout, Crut → DurationCrushers * 10^-6}];
```

Calculation of δ1 according to the inputs;

```
bvalue =
  2 (γ^2 * G^2 * (δ^2 * (Δ - δ/3) + ϵ^3/30 - δ * ϵ^2/6)) /. G → (GmaxDiff * 10^2 * 10^-6) /. Δ → (δ + ϵ) /. time1 /.
   subamp[1];
deltas = ComplexExpand[Re[Solve[bvalue == bvalueInput, δ]]];
deltas = Select[deltas[[All, 1, 2]], # > 0 &];
delta = Ceiling[deltas[[1]] * 10^6, 10] * 10^-6;
time1 = N[Append[time1, δ → delta]];
```

```
Interduration =
  N[Max[(Gsl90t - ϵ) / 2 + ϵ + Max[Grdpt + RampGrdp, Gpet + RampGpe, Gsrft + RampGsrf],
     tReadout / 2 + shiftADC + rampReadout] /. time1];

time2 = N[{t2 → (Gsl90t + ϵ) / 2.,
     t21 → (Gsl90t + ϵ) / 2. + Max[Grdpt + RampGrdp, Gpet + RampGpe, Gsrft + RampGsrf],
     t31a → Interduration,
     t31b → Interduration + (δ + ϵ),
     t41 → Interduration + 2 (δ + ϵ),
     t5 → Interduration + 2 (δ + ϵ) + Crut,
     t42 → Interduration + 2 (δ + ϵ) + Crut + (Gsl180t + ϵ) - RampCrushers,
     t32a → Interduration + 2 (δ + ϵ) + 2 Crut + (Gsl180t + ϵ),
     t32b → Interduration + 3 (δ + ϵ) + 2 Crut + (Gsl180t + ϵ),
     t6 → Interduration + 4 (δ + ϵ) + 2 Crut + (Gsl180t + ϵ),
     t7 → Interduration + 4 (δ + ϵ) + 2 Crut +
       (Gsl180t + ϵ) + tReadout / 2. + shiftADC + rampReadout} /. time1];

Δ = t31b - t31a;

time3 = time2 /. time1;
subs[g_] := g /. time1;

(* Stejkal and Tanner formula. *)
bvaluecalculation =
 subs[2 (γ^2 * G^2 * (δ^2 * (Δ - δ/3) + ϵ^3/30 - δ * ϵ^2/6)) /. G → (GmaxDiff * 10^2 * 10^-6)] /. time3 /.
  subamp[1]
(* 800.50 *)
```

In[415]:=

Defining the SE bipolar gradient pulse and its integral;

In[416]:=

```
FiInt[f_, ll_, ul_] :=
  Integrate[f, {t, ll, ul}, Assumptions → {ll > 0, ul > 0, offs > 0, wid > ϵ, wid > 0, ϵ > 0}] ;
```

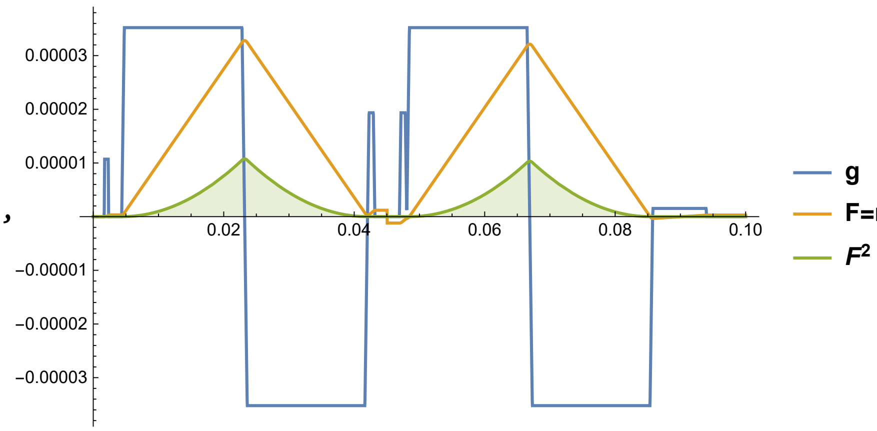
integral;

```
idtrap[δ_, ϵ_, β_, ll_, ul_] = Simplify[Refine[FiInt[trap[wid, ϵ, amp, t - ll], ll, ul],
      Assumptions → {wid > 0, ϵ > 0, ul > 0, wid > ϵ}]] /. wid → δ /. amp → β;
```

```
In[419]:= READ;
dir = 1;
While[dir < ndir + 1,
  AmpIntReadAtTEHalf[dir] =
   subs[ idtrap[Grdpt, RampGrdp, Grdp, t2, TE/2] + idtrap[δ, ϵ, SignDelta[[1]] * Gdr,
        t31a, TE/2] + idtrap[δ, ϵ, -SignDelta[[1]] * Gdr, t31b, TE/2] +
       idtrap[Crut, RampCrushers, Gcr, t41, TE/2]] /. time3 /. subamp[dir];

  Gread[t_, dir] =
   subs[trap[Grdpt, RampGrdp, Grdp, t - t2] + trap[δ, ϵ, SignDelta[[1]] * Gdr, t - t31a] +
       trap[δ, ϵ, -SignDelta[[1]] * Gdr, t - t31b] + trap[Crut, RampCrushers, Gcr, t - t41] +
       trap[Crut, RampCrushers, Gcr, t - t42] + trap[δ, ϵ, SignDelta[[2]] * Gdr, t - t32a] +
       trap[δ, ϵ, -SignDelta[[2]] * Gdr, t - t32b] +
       trap[Grot, RampGrdp, Gro, t - t6]] /. time3 /. subamp[dir];

  Fread[t_, dir] =
   Simplify[subs[(1 - UnitStep[t - TE / 2.]) * (idtrap[Grdpt, RampGrdp, Grdp, t2, t] +
           idtrap[δ, ϵ, SignDelta[[1]] * Gdr, t31a, t] + idtrap[δ, ϵ,
            -SignDelta[[1]] * Gdr, t31b, t] + idtrap[Crut, RampCrushers, Gcr, t41, t]) +
        UnitStep[t - TE / 2.] * (-AmpIntReadAtTEHalf[dir] +
           idtrap[Crut, RampCrushers, Gcr, t42, t] +
           idtrap[δ, ϵ, SignDelta[[2]] * Gdr, t32a, t] + idtrap[δ, ϵ, -SignDelta[[2]] * Gdr,
            t32b, t] + idtrap[Grot, RampGrdp, Gro, t6, t])] /. time3 /. subamp[dir]];
  dir++];
dir = 1;

{subs[Gread[t, 1] /. t → TE] /. time3 /. subamp[1],
   subs[(γ * Fread[t, 1] /. t → TE)] /. time3 /. subamp[1],
   subs[(γ * Fread[t, 1] /. t → TE)^2] /. time3 /. subamp[1]} // AbsoluteTiming;
```

In[424]:=
```
dirPlot = 1;
(*Plot[{subs[Gread[t,dirPlot]]/.time3/.subamp[dirPlot],
   ScaleDiagram*subs[Fread[t,dirPlot]]/.time3/.subamp[dirPlot],
   (100ScaleDiagram)^2*subs[(Fread[t,dirPlot])^2]/.time3/.subamp[dirPlot]},
  {t,0*10^-6,100000.*10^-6},PlotRange→All,Filling→{3->Axis},
  PlotLegends→{"g","F=m0","F^2"}]//AbsoluteTiming*)
```

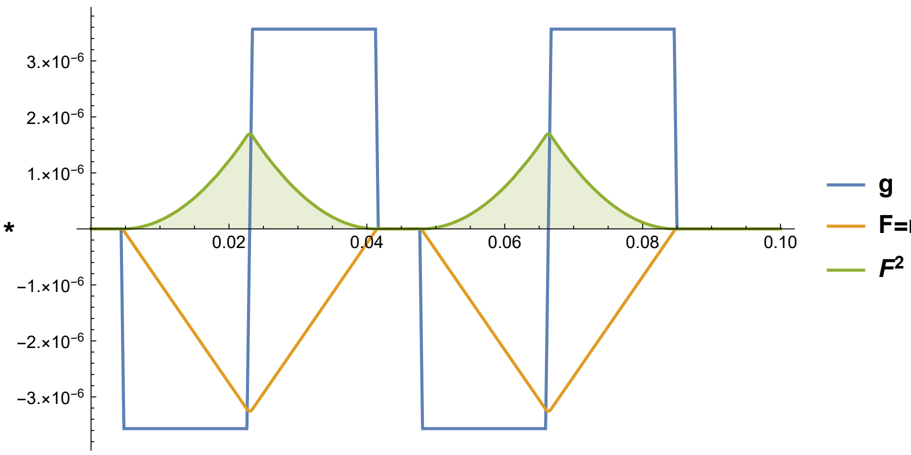
(*{0.0999385`,



}*)

```
In[425]:= PHASE;
dir = 1;
While[dir < ndir + 1,
  AmpIntPhaseAtTEHalf[dir] =
   subs[ idtrap[Gpet, RampGpe, Gpe, t2, TE/2] + idtrap[δ, ϵ, SignDelta[[1]] * Gdp, t31a, TE/2] +
       idtrap[δ, ϵ, -SignDelta[[1]] * Gdp, t31b, TE/2] +
       idtrap[Crut, RampCrushers, Gcp, t41, TE/2]] /. time3 /. subamp[dir];

  Gphase[t_, dir] =
   subs[trap[Gpet, RampGpe, Gpe, t - t2] + trap[δ, ϵ, SignDelta[[1]] * Gdp, t - t31a] +
       trap[δ, ϵ, -SignDelta[[1]] * Gdp, t - t31b] + trap[Crut, RampCrushers, Gcp, t - t41] +
       trap[Crut, RampCrushers, Gcp, t - t42] + trap[δ, ϵ, SignDelta[[2]] * Gdp, t - t32a] +
       trap[δ, ϵ, -SignDelta[[2]] * Gdp, t - t32b]] /. time3 /. subamp[dir];

  Fphase[t_, dir] =
   Simplify[subs[ (1 - UnitStep[t - TE / 2]) * (idtrap[Gpet, RampGpe, Gpe, t2, t] +
          idtrap[δ, ϵ, SignDelta[[1]] * Gdp, t31a, t] + idtrap[δ, ϵ,
           -SignDelta[[1]] * Gdp, t31b, t] + idtrap[Crut, RampCrushers, Gcp, t41, t]) +
        UnitStep[t - TE / 2] * (-AmpIntPhaseAtTEHalf[dir] +
          idtrap[Crut, RampCrushers, Gcp, t42, t] +
          idtrap[δ, ϵ, SignDelta[[2]] * Gdp, t32a, t] + idtrap[δ, ϵ,
           -SignDelta[[2]] * Gdp, t32b, t])] /. time3 /. subamp[dir]];
  dir++];
dir = 1;
{subs[Gphase[t, 1] /. t → TE] /. time3 /. subamp[1],
   subs[ (γ * Fphase[t, 1] /. t → TE)] /. time3 /. subamp[1],
   subs[ (γ * Fphase[t, 1] /. t → TE)^2] /. time3 /. subamp[1]} // AbsoluteTiming;
```

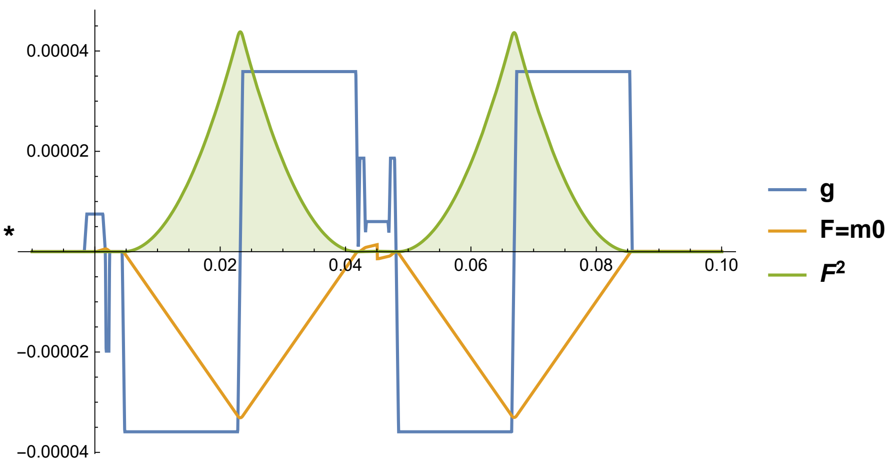
In[430]:=
```
dirPlot = 1;
(*Plot[{subs[Gphase[t,dirPlot]]/.time3/.subamp[dirPlot],
   ScaleDiagram*subs[Fphase[t,dirPlot]]/.time3/.subamp[dirPlot],
   (400ScaleDiagram)^2*subs[(Fphase[t,dirPlot])^2]/.time3/.subamp[dirPlot]},
  {t,0.*10^-6,100000.*10^-6},PlotRange→Full,Filling→{3->Axis},
  PlotLegends→{"g","F=m0","F^2"}]//AbsoluteTiming*)
```

(*  *)

In[431]:=
```
SLICE;
dir = 1;
While[dir < ndir + 1,
  AmpIntSliceAtt2[dir] =
   subs[idtrap[Gsl90t, ϵ, Gsl90, t2, TE / 2] / 2] /. time3 /. subamp[dir];

  AmpIntSliceAtTEHalf[dir] =
   subs[idtrap[Gsl90t, ϵ, Gsl90, t2, TE / 2] / 2 + idtrap[Gsrft, RampGsrf, Gsrf, t2, TE / 2] +
       idtrap[δ, ϵ, SignDelta[[1]] * Gds, t31a, TE / 2] + idtrap[δ, ϵ,
        -SignDelta[[1]] * Gds, t31b, TE / 2] + idtrap[Crut, RampCrushers, Gcs, t41, TE / 2] +
       idtrap[(Gsl180t + ϵ) / 2, ϵ, Gsl180, t5, TE / 2]] /. time3 /. subamp[dir];

  Gslice[t_, dir] =
   subs[trap[Gsl90t, ϵ, Gsl90, t + t2] + trap[Gsrft, RampGsrf, Gsrf, t - t2] + trap[δ, ϵ,
        SignDelta[[1]] * Gds, t - t31a] + trap[δ, ϵ, -SignDelta[[1]] * Gds, t - t31b] +
       trap[Crut, RampCrushers, Gcs, t - t41] + trap[Gsl180t, ϵ, Gsl180, t - t5] +
       trap[Crut, RampCrushers, Gcs, t - t42] + trap[δ, ϵ, SignDelta[[2]] * Gds, t - t32a] +
       trap[δ, ϵ, -SignDelta[[2]] * Gds, t - t32b]] /. time3 /. subamp[dir];

  Fslice[t_, dir] =
   Simplify[subs[((1 - UnitStep[t - t2]) * idtrap[Gsl90t, ϵ, Gsl90, t2, t + t2] +
          UnitStep[t - t2] * (AmpIntSliceAtt2[dir] + idtrap[Gsrft, RampGsrf, Gsrf, t2, t])) +
        (1 - UnitStep[t - TE / 2]) * (idtrap[δ, ϵ, SignDelta[[1]] * Gds, t31a, t] +
           idtrap[δ, ϵ, -SignDelta[[1]] * Gds, t31b, t] + idtrap[Crut, RampCrushers, Gcs,
            t41, t] + idtrap[(Gsl180t + ϵ) / 2, ϵ, Gsl180, t5, t]) + UnitStep[t - TE / 2] *
         (-AmpIntSliceAtTEHalf[dir] + idtrap[(Gsl180t + ϵ) / 2, ϵ, Gsl180, TE / 2, t] +
           idtrap[δ, ϵ, SignDelta[[2]] * Gds, t32a, t] + idtrap[δ, ϵ, -SignDelta[[2]] * Gds,
            t32b, t] + idtrap[Crut, RampCrushers, Gcs, t42, t])] /. time3 /. subamp[dir]];
  dir++];
dir = 1;
```

```
In[435]:= dirPlot = 3;
          {subs[Gslice[t, dirPlot] /. t → TE] /. time3 /. subamp[dirPlot],
            subs[(γ * Fslice[t, dirPlot] /. t → TE)] /. time3 /. subamp[dirPlot],
            subs[(γ * Fslice[t, dirPlot] /. t → TE)^2] /. time3 /. subamp[dirPlot]} // AbsoluteTiming;

          (*Plot[{subs[Gslice[t,dirPlot]]/.time3/.subamp[dirPlot],
             ScaleDiagram*subs[Fslice[t,dirPlot]]/.time3/.subamp[dirPlot],
             (200ScaleDiagram)^2*subs[(Fslice[t,dirPlot])^2]/.time3/.subamp[dirPlot]},
           {t,-10000.*10^-6,100000.*10^-6},PlotRange→Full,Filling→{3->Axis},
           PlotLegends→{"g","F=m0","F^2"}]//AbsoluteTiming*)
```

(*

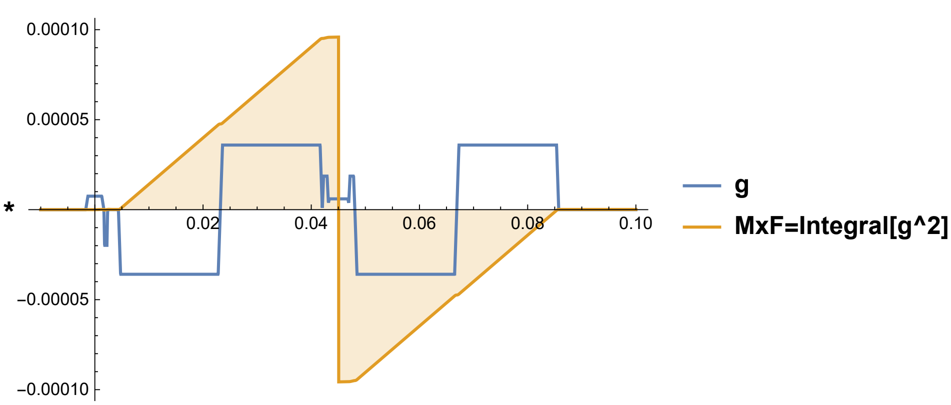


*)

"Maxwell gradient moment= integral(g^2)";

```
dir = 1;
While[dir < ndir + 1,
  AmpIntSliceAtt2[dir] =
   subs[idtrap[Gsl90t, ϵ, Gsl90^2, t2, TE / 2]] /. time3 /. subamp[dir];
  AmpMxIntSliceAtTEHalf[dir] = idtrap[δ, ϵ, Gds^2, t31a, TE/2] + idtrap[δ, ϵ, Gds^2, t31b, TE/2] +
    idtrap[Crut, RampCrushers, Gcs^2, t41, TE/2] + idtrap[Gsl180t, ϵ, Gsl180^2, t5, TE/2];

  MxFslice[t_, dir] =
   (1 - UnitStep[t - t2]) * idtrap[Gsl90t, ϵ, Gsl90^2, t2, t + t2] + UnitStep[t - t2] *
     (-idtrap[Gsl90t, ϵ, Gsl90^2, t2, t + t2] + idtrap[Gsrft, RampGsrf, Gsrf^2, t2, t]) +
    (1 - UnitStep[t - TE / 2]) * (idtrap[δ, ϵ, Gds^2, t31a, t] +
       idtrap[δ, ϵ, Gds^2, t31b, t] + idtrap[Crut, RampCrushers, Gcs^2, t41, t] +
       idtrap[Gsl180t, RampGsl180, Gsl180^2, t5, t]) + UnitStep[t - TE / 2] *
     (-AmpMxIntSliceAtTEHalf[dir] + idtrap[Gsl180t, RampGsl180, Gsl180^2, t5, t] -
       idtrap[Gsl180t, ϵ, Gsl180^2, t5, TE/2] + idtrap[Crut, RampCrushers, Gcs^2, t42, t] +
       idtrap[δ, ϵ, Gds^2, t32a, t] + idtrap[δ, ϵ, Gds^2, t32b, t]);
  dir++];
dir = 1;

dirPlot = 3;
{subs[Gslice[t, dirPlot] /. t → TE] /. time3 /. subamp[dirPlot],
  subs[(MxFslice[t, dirPlot] /. t → TE)] /. time3 /. subamp[dirPlot]};
(*Plot[{subs[Gslice[t,dirPlot]]/.time3/.subamp[dirPlot],
   200^2ScaleDiagram*subs[MxFslice[t,dirPlot]]/.time3/.subamp[dirPlot]},
  {t,-10000.*10^-6,100000.*10^-6},PlotRange→Full,Filling→{2->Axis},
  PlotLegends→{"g","MxF=Integral[g^2]"}]//AbsoluteTiming*)
```

(*



*)

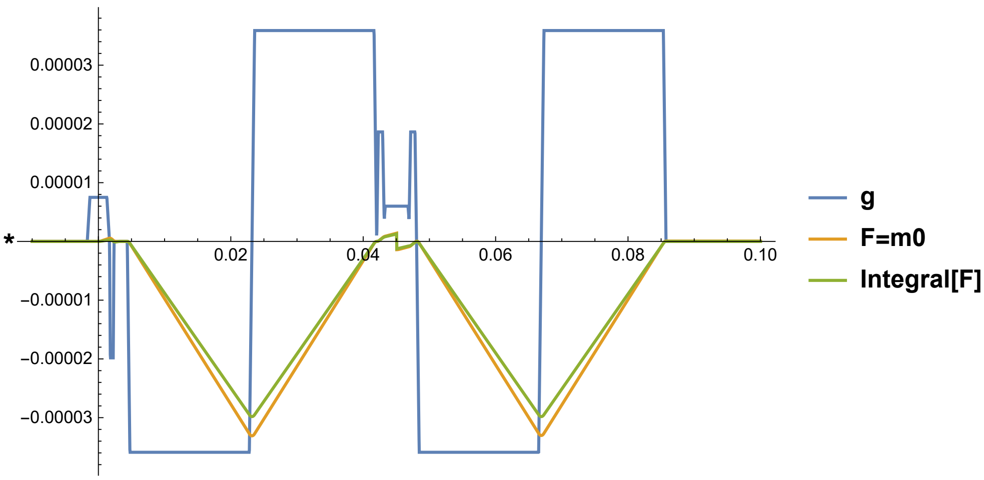
In[444]:=

integral (integral);

```
i2dtrap[δ_, ϵ_, β_, ll_, ul_, a_, b_] =
  Simplify[Refine[FiInt[idtrap[δ, ϵ, amp, ll, ul], a, b],
      Assumptions → {wid > 0., a ≥ 0., b > a, b > 0., a < ul < b, ll ≥ 0.,
        ϵ > 0., ul > 0., β ≥ 0., wid > ϵ}]] /. wid → δ /. amp → β;
dir = 1;
While[dir < ndir + 1,
  Amp2IntSliceAtTEHalf[dir] =
   subs[ i2dtrap[Gsl90t, ϵ, Gsl90, t2, TE / 2, 0, TE] / 2. + i2dtrap[Gsrft, RampGsrf, Gsrf,
        t2, TE / 2, 0, TE] + i2dtrap[δ, ϵ, SignDelta[[1]] * Gds, t31a, TE / 2, 0, TE] +
       i2dtrap[δ, ϵ, -SignDelta[[1]] * Gds, t31b, TE / 2, 0, TE] +
       i2dtrap[Crut, RampCrushers, Gcs, t41, TE / 2, 0, TE] +
       i2dtrap[Gsl180t, RampGsl180, Gsl180, t5, TE, 0, TE] / 2.] /. time3 /. subamp[dir];

  IntFslice[t_, dir] =
   (1 - UnitStep[t - t2]) * i2dtrap[Gsl90t, ϵ, Gsl90, t2, t + t2, 0, TE] / 2. +
    UnitStep[t - t2] * (i2dtrap[Gsl90t, ϵ, Gsl90, t2, t + t2, 0, TE] / 2. +
       i2dtrap[Gsrft, RampGsrf, Gsrf, t2, t, 0, TE]) +
    (1 - UnitStep[t - TE / 2]) * (i2dtrap[δ, ϵ, SignDelta[[1]] * Gds, t31a, t, 0, TE] +
       i2dtrap[δ, ϵ, -SignDelta[[1]] * Gds, t31b, t, 0, TE] + i2dtrap[Crut, RampCrushers,
        Gcs, t41, t, 0, TE] + i2dtrap[Gsl180t, RampGsl180, Gsl180, t5, t, 0, TE]) +
    UnitStep[t - TE / 2] * (-Amp2IntSliceAtTEHalf[dir] + i2dtrap[Gsl180t, RampGsl180,
        Gsl180, t5, t, 0, TE] - i2dtrap[Gsl180t, ϵ, Gsl180, t5, TE/2, 0, TE] +
       i2dtrap[Crut, RampCrushers, Gcs, t42, t, 0, TE] + i2dtrap[δ, ϵ, SignDelta[[2]] * Gds,
        t32a, t, 0, TE] + i2dtrap[δ, ϵ, -SignDelta[[2]] * Gds, t32b, t, 0, TE]);

  dir++];
dir = 1;
```

In[449]:=
```
dirPlot = 3;
(*Plot[{subs[Gslice[t,dirPlot]]/.time3/.subamp[dirPlot],
  ScaleDiagram*subs[Fslice[t,dirPlot]]/.time3/.subamp[dirPlot],
  10ScaleDiagram*subs[IntFslice[t,dirPlot]]/.time3/.subamp[dirPlot]},
 {t,-10000*10^-6,100000*10^-6},PlotRange→Full,
 PlotLegends→{"g","F=m0","Integral[F]"}]*)
```

(*



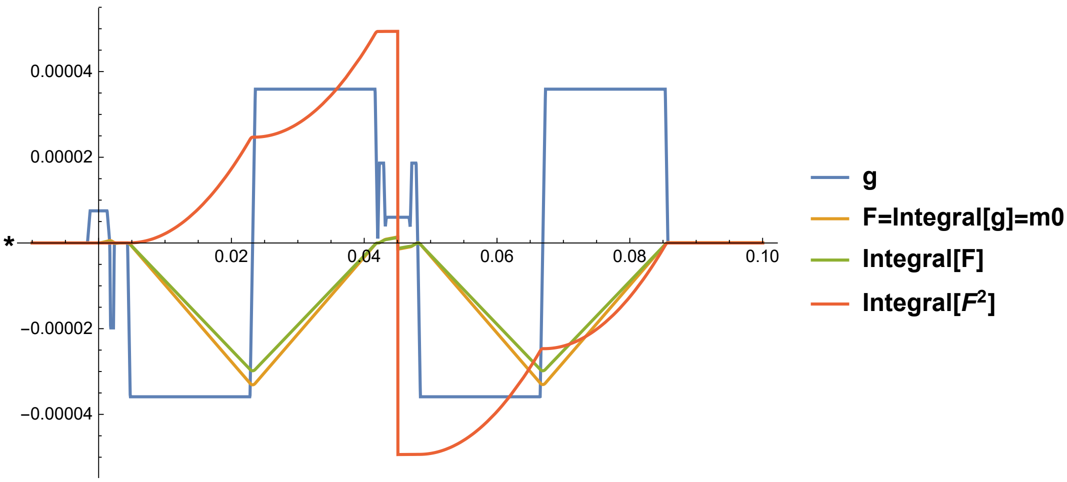
*)

In[450]:= **d = integral[integral^2];**

```
iSqidtrap[δ_, ϵ_, β_, ll_, ul_, a_, b_] =
  Simplify[Refine[FiInt[(idtrap[δ, ϵ, amp, ll, ul])^2, a, b],
      Assumptions → {wid > 0., a ≥ 0., b > a, b > 0., a < ul < b, ll ≥ 0.,
        ϵ > 0., ul > 0., β ≥ 0., wid > ϵ}]] /. wid → δ /. amp → β;
dir = 1;
While[dir < ndir + 1,
  AmpIntSqIntSliceAtTEHalf[dir] =
   subs[ iSqidtrap[Gsl90t, ϵ, Gsl90, t2, TE/2, 0, TE] / 2. + iSqidtrap[Gsrft, RampGsrf, Gsrf,
        t2, TE/2, 0, TE] + iSqidtrap[δ, ϵ, SignDelta[[1]] * Gds, t31a, TE/2, 0, TE] +
       iSqidtrap[δ, ϵ, -SignDelta[[1]] * Gds, t31b, TE/2, 0, TE] +
       iSqidtrap[Crut, RampCrushers, Gcs, t41, TE/2, 0, TE] +
       iSqidtrap[Gsl180t, RampGsl180, Gsl180, t5, TE, 0, TE] / 2.] /. time3 /. subamp[dir];

  IntSqFslice[t_, dir] =
   (1 - UnitStep[t - t2]) * iSqidtrap[Gsl90t, ϵ, Gsl90, t2, t + t2, 0, TE] / 2. +
    UnitStep[t - t2] * (iSqidtrap[Gsl90t, ϵ, Gsl90, t2, t + t2, 0, TE] / 2. +
       iSqidtrap[Gsrft, RampGsrf, Gsrf, t2, t, 0, TE]) +
     (1 - UnitStep[t - TE/2]) * (iSqidtrap[δ, ϵ, SignDelta[[1]] * Gds, t31a, t, 0, TE] +
       iSqidtrap[δ, ϵ, -SignDelta[[1]] * Gds, t31b, t, 0, TE] + iSqidtrap[Crut, RampCrushers,
        Gcs, t41, t, 0, TE] + iSqidtrap[Gsl180t, RampGsl180, Gsl180, t5, t, 0, TE]) +
    UnitStep[t - TE/2] * (-AmpIntSqIntSliceAtTEHalf[dir] + iSqidtrap[Gsl180t,
        RampGsl180, Gsl180, t5, t, 0, TE] - iSqidtrap[Gsl180t, ϵ, Gsl180, t5, TE/2, 0, TE] +
       iSqidtrap[Crut, RampCrushers, Gcs, t42, t, 0, TE] +
       iSqidtrap[δ, ϵ, SignDelta[[2]] * Gds, t32a, t, 0, TE] +
       iSqidtrap[δ, ϵ, -SignDelta[[2]] * Gds, t32b, t, 0, TE]);

  dir++];
dir = 1;
```

In[455]:=
```
dirPlot = 3;
(*Plot[{subs[Gslice[t,dirPlot]]/.time3/.subamp[dirPlot],
  ScaleDiagram*subs[Fslice[t,dirPlot]]/.time3/.subamp[dirPlot],
  10ScaleDiagram*subs[IntFslice[t,dirPlot]]/.time3/.subamp[dirPlot],
  500^2ScaleDiagram^2*subs[IntSqFslice[t,dirPlot]]/.time3/.subamp[dirPlot]},
 {t,-10000*10^-6,100000*10^-6},PlotRange→Full,
 PlotLegends→{"g","F=Integral[g]=m0","Integral[F]","Integral[F^2]"}]*)
```

(*



*)

In[456]:=

Bmatrix;

```
(*set SignDelta={1.,-1.};*)
dir = 1;
While[dir < ndir + 1,
  (F[t_, dir] = {{Fread[t, dir]}, {Fphase[t, dir]}, {Fslice[t, dir]}}) // MatrixForm;

  fread[dir] = Fread[t, dir] /. t → N[TE / 2 /. time1];
  fphase[dir] = Fphase[t, dir] /. t → N[TE / 2 /. time1];
  fslice[dir] = Fslice[t, dir] /. t → N[TE / 2 /. time1];
  (f[dir] = {{fread[dir]}, {fphase[dir]}, {fslice[dir]}}) // MatrixForm;

  b1v[dir] = NIntegrate[F[t, dir].Transpose[F[t, dir]], {t, 0, N[TE / 2 /. time1]}];
  b2v[dir] = NIntegrate[(F[t, dir] - 2 f[dir]).Transpose[F[t, dir] - 2 f[dir]],
    {t, N[TE / 2 /. time1], N[TE /. time1]}];
  dir++];
dir = 1;
```

```
In[460]:= bTensor = Reap[Do[Sow[γ^2 * (b1v[dir] + b2v[dir])], {dir, 1, ndir}]][[2]] // MatrixForm;
bTrace = Transpose[Reap[Do[Sow[Tr[bTensor[[1, 1, dir]]]], {dir, 1, ndir}]][[2]]];
Mean[bTrace]; (* 815.51 *)
StandardDeviation[bTrace]; (* 49.82 *)
Bmatrix =
  Reap[Do[Sow[ {bTensor[[1, 1, dir, 1, 1]], bTensor[[1, 1, dir, 2, 2]], bTensor[[1, 1,
        dir, 3, 3]], 2 bTensor[[1, 1, dir, 1, 2]], 2 bTensor[[1, 1, dir, 1, 3]],
       2 bTensor[[1, 1, dir, 2, 3]]}], {dir, 1, ndir}]][[2]];

(*Switch[ndir,4,Export["C:\\users\\Bmatrix_SEbp_4dir.xlsx",Bmatrix,"XLSX"],
  6,Export["C:\\users\\Bmatrix_SEbp_6dir.xlsx",Bmatrix,"XLSX"],
  32,Export["C:\\users\\Bmatrix_SEbp_32dir.xlsx",Bmatrix,"XLSX"],
  64,Export["C:\\users\\Bmatrix_SEbp_64dir.xlsx",Bmatrix,"XLSX"]];*)
```

Bmatrix display;

```
Bmatrix = Transpose[
   Reap[Do[Sow[ {{bTensor[[1, 1, dir, 1, 1]], bTensor[[1, 1, dir, 2, 2]], bTensor[[1, 1,
          dir, 3, 3]], 2 bTensor[[1, 1, dir, 1, 2]], 2 bTensor[[1, 1, dir, 1, 3]],
        2 bTensor[[1, 1, dir, 2, 3]]}}], {dir, 1, ndir}]][[2]]] // MatrixForm

(* ( (711.1568580500234`  7.859236670259006`  36.85427051116142`  -149.06285106573588`  -312.
     (0.31459038203272766`  764.6614885476494`  24.39026036174379`  -6.559657194111128`  3.659
     (2.8793326828206744`  1.96714974896834`  908.6647413401818`  -4.422505645696763`  -91.6
     (669.4972018206752`  20.794272457617392`  69.83791889077072`  -235.7720169360186 2`  425.
     (10.795571485249718`  746.6257555624701`  75.2049197753557`  -175.21602020350682`  -49.69
     (31.663129280752532`  73.75972540707633`  787.9364492275109`  -96.52925766499945`  315.04
     (660.6812804358967`  69.15864231280571`  25.564635140473115`  427.13700134061247`  249.
     (92.3591246598508`  698.3425779160345`  13.444179527587735`  507.7455857757415`  56.34
     (140.11469977643017`  6.602063760545031`  719.045787142942`  60.8055458726816 4`  631.82
     (589.1831180485815`  103.80609232456776`  78.8450398542407`  493.0240695858108`  -420.00
     (200.8045683463561`  584.0938816655282`  8.400877433782686`  -681.8382448726886`  -56.58
     (7.9876512637978205`  160.74579694578713`  729.8100393346249`  70.94539445435323`  152.1
     (527.0187748338415`  220.6932372659919 7`  21.934009569944298`  -679.824319263636`  -199.6
     (106.89395112209809`  572.3079425873527`  151.5465502370981`  491.7407399415225`  -244.5
     (170.64564361411806`  1.368921620004252`  688.6192957267541`  30.4199663315275`  -675.3
     (477.4408990920083`  3.259330620658113`  319.7203806349164`  78.6272170737925 6`  -771.0
     (58.672056160679546`  554.5370791483672`  232.48853379826875`  360.569732332226`  230.9
     (40.32018037851905`  146.7323947030436`  699.4511264271504`  152.304134865424 4`  -327.1
     (473.509523737577`  39.834068131594016`  282.5975747046772`  274.4668942972565 4`  725.9
     (89.71160039830642`  535.4059339776167`  136.2466503527205`  438.1639587025635`  -217.49
     (107.8654440009177`  129.8932520205085`  630.4552728926797`  -235.33693055072945`  -511.
     (428.1274372329679`  256.8466474515555`  102.27212539688348`  -662.7309904503486`  411.2
     (10.927103020126252`  450.65327982483205`  412.5082158613341`  -136.98416477163286`  -126
     (183.7463012992797`  211.55465064094358`  447.879034823352`  394.14467890495143`  569.8
     (415.7905732873876`  105.41736285414007`  284.13880897307985`  -417.2355936727353`  -676
     (0.9867211245424282`  430.42227959990566`  309.04000495902744`  -33.307814693674004`  30.7
     (161.33920926117312`  241.48603429836916`  443.4783066035182`  -394.6072731347523`  531.
     (381.80070355383566`  31.187433012274447`  321.2515369577747`  -217.4481182174588 7`  700
     (197.59742340296464`  422.27505984333646`  205.1111747202357`  -575.0813188269398`  -392.
     (359.6058390341094`  342.1327014742657`  91.39817058451955`  701.0537979035859`  355.03
     (342.7337310442434`  409.4206624091034`  14.037429134573602`  748.7060697558733`  -126.61
     (267.9164558222443`  194.1038472419002`  366.3368773206426`  454.2225303493532`  -616.1
```

In[467]:=
```
(* For the graph's plot and dslice, kvslice ;*)
(*set SignDelta={1.,1.};*)
dslice = γ^2 * NIntegrate[F[t, 1].Transpose[F[t, 1]], {t, 0, N[TE /. time1]}];
dsliceTrace = Tr[dslice];
dsliceExp =
  γ^2 * NIntegrate[F[t, 1].Transpose[F[t, 1]] * Exp[-t / 0.030], {t, 0, N[TE /. time1]}] //
   MatrixForm;
Kvslice = γ * NIntegrate[t * Gslice[t, 1], {t, 0, N[TE /. time1]}] // MatrixForm;
```

In[471]:=

M0 and M1 and M2;

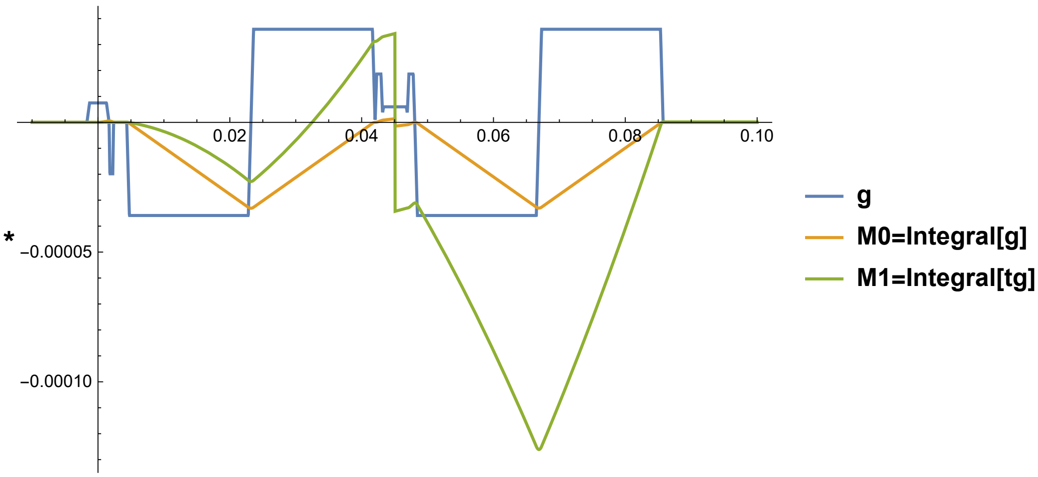
integral M1;

```
iM1dtrap[δ_, ϵ_, β_, ll_, ul_] =
  Simplify[Refine[FiInt[t * trap[wid, ϵ, amp, t - ll], ll, ul],
      Assumptions → {wid > 0., ϵ > 0., ul > 0., wid > ϵ}]] /. wid → δ /. amp → β;
```

In[474]:=
```
dir = 1;
While[dir < ndir + 1,
  AmpIntM1SliceAtTEHalf[dir] =
   subs[ iM1dtrap[Gsl90t, ϵ, Gsl90, t2, TE / 2] +
       iM1dtrap[Gsrft, RampGsrf, Gsrf, t2, t2 + Gsrft + RampGsrf] + iM1dtrap[δ, ϵ,
        SignDelta[[1]] * Gds, t31a, t41] + iM1dtrap[δ, ϵ, -SignDelta[[1]] * Gds, t31b, t41] +
       iM1dtrap[Crut, RampCrushers, Gcs, t5, t5 + Crut + RampCrushers] +
       iM1dtrap[Gsl180t, RampGsl180, Gsl180, t5, TE / 2]] /. time3 /. subamp[dir];

  M1slice[t_, dir] =
   (1 - UnitStep[t - t2]) * iM1dtrap[Gsl90t, ϵ, Gsl90, t2, t + t2] / 2. + UnitStep[t - t2] *
     (iM1dtrap[Gsl90t, ϵ, Gsl90, t2, t + t2] / 2. + iM1dtrap[Gsrft, RampGsrf, Gsrf, t2, t]) +
    (1 - UnitStep[t - TE / 2]) * (iM1dtrap[δ, ϵ, SignDelta[[1]] * Gds, t31a, t] +
       iM1dtrap[δ, ϵ, -SignDelta[[1]] * Gds, t31b, t] + iM1dtrap[Crut, RampCrushers, Gcs,
        t41, t] + iM1dtrap[Gsl180t, RampGsl180, Gsl180, t5, t]) + UnitStep[t - TE / 2] *
    (-AmpIntM1SliceAtTEHalf[dir] + iM1dtrap[Gsl180t, RampGsl180, Gsl180, t5, t] -
       iM1dtrap[Gsl180t, ϵ, Gsl180, t5, TE/2] + iM1dtrap[Crut, RampCrushers, Gcs, t42, t] +
       iM1dtrap[δ, ϵ, SignDelta[[2]] * Gds, t32a, t] +
       iM1dtrap[δ, ϵ, -SignDelta[[2]] * Gds, t32b, t]);

  dir++];
dir = 1;
```

In[477]:=
```
dirPlot = 3;
(*Plot[{subs[Gslice[t,dirPlot]]/.time3/.subamp[dirPlot],
  ScaleDiagram*subs[Fslice[t,dirPlot]]/.time3/.subamp[dirPlot],
  50ScaleDiagram*subs[M1slice[t,dirPlot]]/.time3/.subamp[dirPlot]},
 {t,-10000*10^-6,100000*10^-6},PlotRange→Full,
 PlotLegends→{"g","M0=Integral[g]","M1=Integral[tg]"}]*)
```

(*



*)

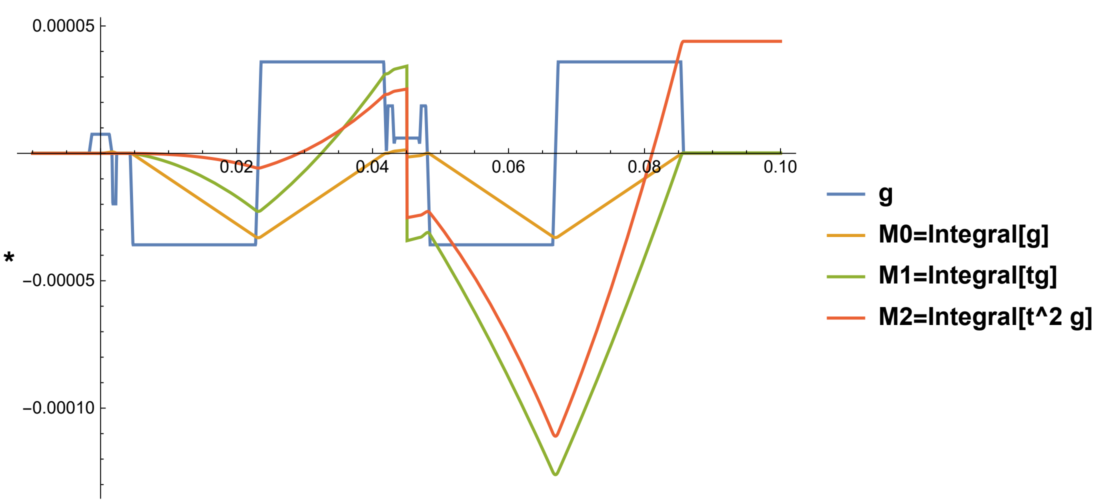
In[478]:=
integral M2;

```
iM2dtrap[δ_, ϵ_, β_, ll_, ul_] =
  Simplify[Refine[FiInt[t^2 * trap[wid, ϵ, amp, t - ll], ll, ul],
     Assumptions → {wid > 0., ϵ > 0., ul > 0., wid > ϵ}]] /. wid → δ /. amp → β;
```

In[480]:=
```
dir = 1;
While[dir < ndir + 1,
  AmpIntM2SliceAtT1[dir] =
   subs[ iM2dtrap[Gsl90t, ϵ, Gsl90, 0, t2] / 2. + iM2dtrap[Gsrft, RampGsrf, Gsrf, t2,
        t2 + Gsrft + RampGsrf] + iM2dtrap[δ, ϵ, SignDelta[[1]] * Gds, t31a, t41] +
       iM2dtrap[δ, ϵ, -SignDelta[[1]] * Gds, t31b, t41] +
       iM2dtrap[Crut, RampCrushers, Gcs, t5, t5 + Crut + RampCrushers] +
       iM2dtrap[Gsl180t, RampGsl180, Gsl180, t5, TE / 2]] /. time3 /. subamp[dir];

  M2slice[t_, dir] =
   (1 - UnitStep[t - t2]) * iM2dtrap[Gsl90t, ϵ, Gsl90, t2, t + t2] / 2. + UnitStep[t - t2] *
     (iM2dtrap[Gsl90t, ϵ, Gsl90, t2, t + t2] / 2. + iM2dtrap[Gsrft, RampGsrf, Gsrf, t2, t]) +
    (1 - UnitStep[t - TE / 2]) * (iM2dtrap[δ, ϵ, SignDelta[[1]] * Gds, t31a, t] +
       iM2dtrap[δ, ϵ, -SignDelta[[1]] * Gds, t31b, t] + iM2dtrap[Crut, RampCrushers, Gcs,
        t41, t] + iM2dtrap[Gsl180t, RampGsl180, Gsl180, t5, t]) + UnitStep[t - TE / 2] *
     (-AmpIntM2SliceAtT1[dir] + iM2dtrap[Gsl180t, RampGsl180, Gsl180, t5, t] -
       iM2dtrap[Gsl180t, ϵ, Gsl180, t5, TE/2] + iM2dtrap[Crut, RampCrushers, Gcs, t42, t] +
       iM2dtrap[δ, ϵ, SignDelta[[2]] * Gds, t32a, t] +
       iM2dtrap[δ, ϵ, -SignDelta[[2]] * Gds, t32b, t]);

  dir++];
dir = 1;
```

In[483]:=
```
dirPlot = 3;
(*Plot[{subs[Gslice[t,dirPlot]]/.time3/.subamp[dirPlot],
  ScaleDiagram*subs[Fslice[t,dirPlot]]/.time3/.subamp[dirPlot],
  50ScaleDiagram*subs[M1slice[t,dirPlot]]/.time3/.subamp[dirPlot],
  (4ScaleDiagram)^2*subs[M2slice[t,dirPlot]]/.time3/.subamp[dirPlot]},
 {t,-10000*10^-6,100000*10^-6},PlotRange→Full,
 PlotLegends→{"g","M0=Integral[g]","M1=Integral[tg]","M2=Integral[t^2 g]"}]*)
```

(*



*)