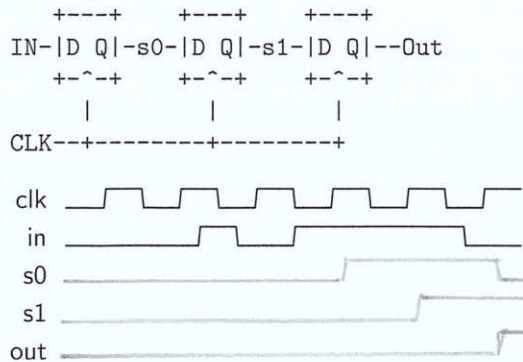
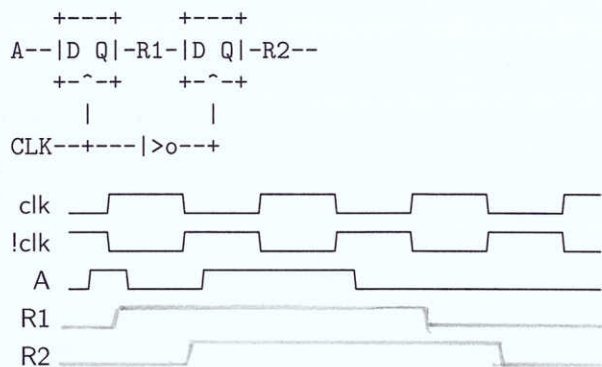


State

- Fill out the timing diagram for the circuit below:

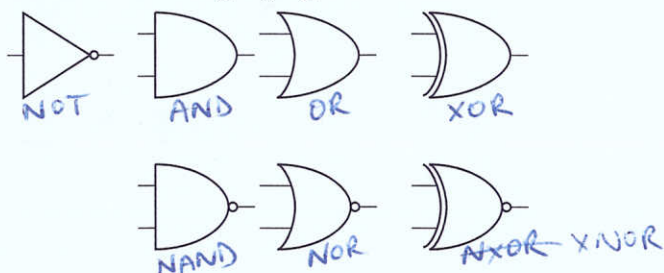


- Fill out the timing diagram for the circuit below:



Logic Gates

- Label the following logic gates:



- Convert the following to boolean expressions:

- NAND $Q = \overline{AB}$
- XOR $Q = \overline{A}B + A\overline{B}$
- XNOR $Q = AB + \overline{A}\overline{B}$

3. Create an AND gate using only NAND gates.



4. How many different two-input logic gates can there be? How many n-input logic gates?

1b. There are 2^n lines in an n-input truth table. If ~~the number~~ $x =$ number of lines there are 2^x possible outputs. Since $x = 2^n$, there are 2^{2^n} n-input logic gates.

Boolean Logic

$$\begin{array}{llll} 1 + A = 1 & A + \bar{A} = 1 & A + AB = A & (A + B)(A + C) = A + BC \\ 0B = 0 & B\bar{B} = 0 & A + \bar{A}B = A + B & \\ \text{DeMorgan's Law: } \overline{AB} = \bar{A} + \bar{B} & \overline{A + B} = \bar{A}\bar{B} & & \end{array}$$

1. Minimize the following boolean expressions:

(a) Standard: $(A + B)(A + \bar{B})C$

$$= (A + B\bar{B})C = (A + 0)C = AC$$

(b) Grouping & Extra Terms: $\bar{A}\bar{B}\bar{C} + \bar{A}B\bar{C} + A\bar{B}\bar{C} + A\bar{B}C + ABC + A\bar{B}C$

$$= (\bar{A} + A)\bar{B}\bar{C} + AB(\bar{C} + C) + \bar{A}B\bar{C} + A\bar{B}C = \bar{B}\bar{C} + AB + \bar{A}B\bar{C} + A\bar{B}C$$

$$= \bar{B}(\bar{C} + AC) + B(A + \bar{A}\bar{C})$$

$$= \bar{B}(\bar{C} + A) + B(A + \bar{C}) = (\bar{B} + B)(A + \bar{C})$$

$$= A + \bar{C}$$

(c) DeMorgan's: $\overline{A(\bar{B}C + BC)}$

$$= \bar{A} + (\bar{B}\bar{C} + \bar{B}C) \rightarrow \bar{A} + \bar{B}\bar{C}\bar{B}C \rightarrow \bar{A} + (B + C)(\bar{B} + \bar{C})$$

$$= \bar{A} + \bar{B}\bar{C}\bar{B}C \leftarrow \text{wrong!}$$

$$= (\bar{A} + \bar{B}\bar{C})(\bar{A} + \bar{B}C)$$

$$= \bar{A} + \bar{B}\bar{C} + \bar{B}C + \bar{C}\bar{B}C$$

$$= \bar{A} + 0 = \bar{A} + 1$$

$$= (\bar{A} + B + C)(\bar{A} + \bar{B} + \bar{C})$$

$$= \bar{A} + \bar{B}\bar{C} + \bar{B}C$$

$$= \bar{A}$$