Fundamental Algorithmic Techniques.

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Outline

The greedy algorithm paradigm

Characteristics of greedy algorithms

Correctness proof techniques



The greedy algorithm paradigm

Best possible (greedy) choice right now, for immediate best outcome!

Requirements:

- 1 greedy-choice property: globally optimal solution ⇔ local optimal (greedy) choices
- 2 optimal substructure

Examples where Greedy Algorithm is suboptimal

- life!?
- road...
- 0-1 knapsack problem



Examples where Greedy is optimal

Course allocation, Cache, Huffman coding and Shannon Entropy



Characteristics of greedy algorithms

Greedy stays ahead!

- $A = \{a_0, a_1, \dots, a_n\}$ algo. sequence and $O = \{o_0, o_1, \dots, o_n\}$ optimal sequence
- \blacksquare choose a measure $\mu(\dot{)}$
- show stay ahead: $\mu(a_0, a_1, \dots, a_n) \leq \mu(o_0, o_1, \dots, o_n)$ by induction!
- Prove optimality: use greedy stays ahead to generate contradiction

Correctness proof techniques

Induction example: classes Scheduling







