



NATIONAL OPEN UNIVERSITY OF NIGERIA

SCHOOL OF SCIENCE AND TECHNOLOGY

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COURSE TITLE: ELEMENTARY MATHEMATICS III

COURSE GUIDE

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Course Guide

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Course Title: ELEMENTARY MATHEMATICS III

Introduction

MTH 103 - Elementary Mathematics III is designed to teach you how mathematics could be used in solving problems in the contemporary Scientific world. Therefore, the course is structured to expose you to the skills required in order to attain a level of proficiency in Sciences, technology and Engineering Professions.

What you will learn in this Course

You will be taught the basis of mathematics required in solving scientific problems.

Course Aim

There are eleven study units in the course and each unit has its objectives. You should read the objectives of each unit and bear them in mind as you go through the unit. In addition to the objectives of each unit, the overall aims of this course include:

- (i) To introduce you to the words and concepts in Elementary mathematics
- (ii) To familiarize you with the peculiar characteristics in Elementary mathematics.
- (iii) To expose you to the need for and the demands of mathematics in the Science world.
- (iv) To prepare you for the contemporary Science world.

Course Objectives

The objectives of this course are:

- * To inculcate appropriate mathematical skills required in Science and Engineering.

- * Educate learners on how to use mathematical Techniques in solving real life problems.

- * Educate the learners on how to integrate mathematical models in Sciences, technology and Engineering.

Working through this Course

{ You have to work through all the study units in the course. There are two modules and ten study units in all.

Course Materials

Major components of the course are:

1. Course Guide

2. Study Units

3. Textbooks

4. CDs

5. Assignments File

6. Presentation Schedule

Study Units

The breakdown of the four modules and eleven study units are as follows:

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Recommended Texts

- Larson Edwards Calculus: An Applied Approach. Sixth Edition.
- Blitzer. Algebra and Trigonometry Custom. 4th Edition
- K.A Stroud. Engineering Mathematics. 5th Edition
- Pure Mathematics for Advanced Level By B.D Bunday H Mulholland 1970.
- Godman and J.F Talbert. Additional Mathematics

Assignment File

{ In this file, you will find all the details of the work you must submit to your tutor for marking. The marks you obtain from these assignments will count towards the final mark you obtain for this course. Further information on assignments will be found in the Assignment File itself and later in this *Course Guide* in the section on assessment.

Presentation Schedule

The Presentation Schedule included in your course materials gives you the important dates for the completion of tutor-marked assignments and attending tutorials. Remember, you are required to submit all your assignments by the due date. You should guard against falling behind in your work.

Assessment

Your assessment will be based on tutor-marked assignments (TMAs) and a final examination which you will write at the end of the course.

Exercises TMA

{ Every unit contains at least one or two assignments. You are advised to work through all the assignments and submit them for assessment. Your tutor will assess the assignments and select four which will constitute the 30% of your final grade. The tutor-marked assignments may be presented to you in a separate file. Just know that for every unit there are some tutor-marked assignments for you. It is important you do them and submit for assessment. }

Final Examination and Grading

{ At the end of the course, you will write a final examination which will constitute 70% of your final grade. In the examination which shall last for two hours, you will be requested to answer three questions out of at least five questions.

Course marking Scheme

This table shows how the actual course marking as it is broken down.

Assessment	Marks
Assignments	Four assignments, Best three marks of the four count at 30% of course marks
Final Examination	70% of overall course marks
<i>Total</i>	100% of course marks

How to Get the Most from This Course

In distance learning, the study units replace the university lecture. This is one of the great advantages of distance learning; you can read and work through specially designed study materials at your own pace, and at a time and place that suits you best. Think of it as reading the lecture instead of listening to the lecturer. In the same way a lecturer might give you some reading to do, the study units tell you when to read, and which are your text materials or set books. You are provided exercises to do at appropriate points, just as a lecturer might give you an in-class exercise. Each of the study units follows a common format. The first item is an introduction to the subject matter of the unit, and how a particular unit is integrated with the other units and the course as a whole. Next to this is a set of learning objectives. These objectives let you know what you should be able to do by the time you have completed the unit. These learning objectives are meant to guide your study. The moment a unit is finished, you must go back and check whether you have achieved the objectives. If this is made a habit, then you will significantly improve your chances of passing the course. The main body of the unit guides you through the required reading from other sources. This will usually be either from your set books or from a Reading section. The following is a practical strategy for working through the course. If you run into any trouble, telephone your tutor. Remember that your tutor's job is to help you. When you need assistance, do not hesitate to call and ask your tutor to provide it.

In addition do the following:

1. Read this Course Guide thoroughly, it is your first assignment.
2. Organise a Study Schedule. Design a Course Overview “to guide you through the Course”. Note the time you are expected to spend on each unit and how the assignments relate to the units. Important information, e.g. details of your tutorials, and the date of the first day of the Semester is available from the study centre. You need to gather all the information into one place, such as your diary or a wall calendar. Whatever method you choose to use, you should decide on and write in your own dates and schedule of work for each unit.
3. Once you have created your own study schedule, do everything to stay faithful to it. The major reason that students fail is that they get behind with their course work. If you get into difficulties with your schedule, please, let your tutor know before it is too late for help.
4. Turn to Unit 1, and read the introduction and the objectives for the unit.
5. Assemble the study materials. You will need your set books and the unit you are studying at any point in time.
6. Work through the unit. As you work through the unit, you will know what sources to consult for further information.
7. Keep in touch with your study centre. Up-to-date course information will be continuously available there.
8. Well before the relevant due dates (about 4 weeks before due dates), keep in mind that you will learn a lot by doing the assignment carefully. They have been designed to help you meet the objectives of the course and, therefore, will help you pass the examination. Submit all assignments not later than the due date.
9. Review the objectives for each study unit to confirm that you have achieved them. If you feel unsure about any of the objectives, review the study materials or consult your tutor.

10. When you are confident that you have achieved a unit's objectives, you can start on the next unit. Proceed unit by unit through the course and try to pace your study so that you keep yourself on schedule.

11. When you have submitted an assignment to your tutor for marking, do not wait for its return before starting on the next unit. Keep to your schedule. When the Assignment is returned, pay particular attention to your tutor's comments, both on the tutor-marked assignment form and also the written comments on the ordinary assignments.

12. After completing the last unit, review the course and prepare yourself for the final examination. Check that you have achieved the unit objectives (listed at the beginning of each unit) and the course objectives (listed in the Course Guide).

Tutors and Tutorials

The dates, times and locations of these tutorials will be made available to you, together with the name, telephone number and the address of your tutor. Each assignment will be marked by your tutor. Pay close attention to the comments

your tutor might make on your assignments as these will help in your progress.

Make sure that assignments reach your tutor on or before the due date.

Your tutorials are important therefore try not to skip any. It is an opportunity to meet your tutor and your fellow students. It is also an opportunity to get the help of your tutor and discuss any difficulties encountered on your reading.

Summary

This course would train you on the concept of multimedia, production and utilization of it.

Wish you the best of luck as you read through this course

MAT 103
ELEMENTARY MATHEMATICS III
(VECTORS, GEOMETRY AND DYNAMICS)

Edited By

Prof. U. A. Osiogu

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