## Assignment 13

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The link to the solution is

https://github.com/Adarsh1310/EE5609

Abstract—This documents solves a problem based on invertible matrix.

## 1 Problem

Suppose **A** is a  $2\times1$  matrix and **B** is  $1\times2$  matrix. Prove that **C**=**AB** is non invertible.

## 2 Solution

Let's assume,

$$\mathbf{A} = \begin{pmatrix} a \\ b \end{pmatrix} \tag{2.0.1}$$

$$\mathbf{B} = \begin{pmatrix} c & d \end{pmatrix} \tag{2.0.2}$$

Now,

$$\mathbf{C} = \mathbf{AB} \tag{2.0.3}$$

$$= \begin{pmatrix} a \\ b \end{pmatrix} \begin{pmatrix} c & d \end{pmatrix} \tag{2.0.4}$$

$$= \begin{pmatrix} ac & ad \\ bc & bd \end{pmatrix} \tag{2.0.5}$$

Let,

$$\mathbf{U} = \begin{pmatrix} ac \\ bc \end{pmatrix} \tag{2.0.6}$$

$$\mathbf{V} = \begin{pmatrix} ad \\ bd \end{pmatrix} \tag{2.0.7}$$

For (2.0.5) to be non invertible

$$\mathbf{C}\mathbf{x} = 0 \tag{2.0.8}$$

Should have a non zero solution.

$$\left( \mathbf{U} \quad \mathbf{V} \right) \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} = 0$$
 (2.0.9)

$$x_1 \mathbf{U} = -x_2 \mathbf{V} \tag{2.0.10}$$

This shows that the two columns are a scalar multiple of each other and hence they will have a non trivial solution. So, we can say that C is non invertible.