

# Assignment 13

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The link to the solution is

<https://github.com/Adarsh1310/EE5609>

**Abstract**—This documents solves a problem based on invertible matrix.

## 1 PROBLEM

Suppose  $\mathbf{A}$  is a  $2 \times 1$  matrix and  $\mathbf{B}$  is  $1 \times 2$  matrix. Prove that  $\mathbf{C} = \mathbf{AB}$  is non invertible.

## 2 SOLUTION

Let's take,

$$\mathbf{A} = \begin{pmatrix} a \\ b \end{pmatrix} \quad (2.0.1)$$

$$\mathbf{B} = \begin{pmatrix} c & d \end{pmatrix} \quad (2.0.2)$$

assuming  $\mathbf{A}$  and  $\mathbf{B}$  to be non zero vectors. Now, we know that for  $\mathbf{C}$  to be non invertible  $\mathbf{Cx} = 0$  should have a non trivial solution. So,

$$\mathbf{Cx} = 0 \quad (2.0.3)$$

$$\implies \mathbf{ABx} = 0 \quad (2.0.4)$$

Here, we know that  $\mathbf{B}$  is  $1 \times 2$  matrix and  $\mathbf{x}$  is  $2 \times 1$  matrix then  $\mathbf{Bx}$  will result to a scalar constant  $k$ .

$$\implies \mathbf{Ak} = 0 \quad (2.0.5)$$

For (2.0.5) to be true  $k$  should be zero. We also know that  $\mathbf{B}$  is  $1 \times 2$  matrix i.e. rows are less than column hence,

$$\mathbf{Bx} = 0 \quad (2.0.6)$$

will have a non trivial solution. Hence, using (2.0.5) and (2.0.6) we can say,

$$\mathbf{ABx} = 0 \quad (2.0.7)$$

will have a non trivial solution so,  $\mathbf{C}$  is non invertible.