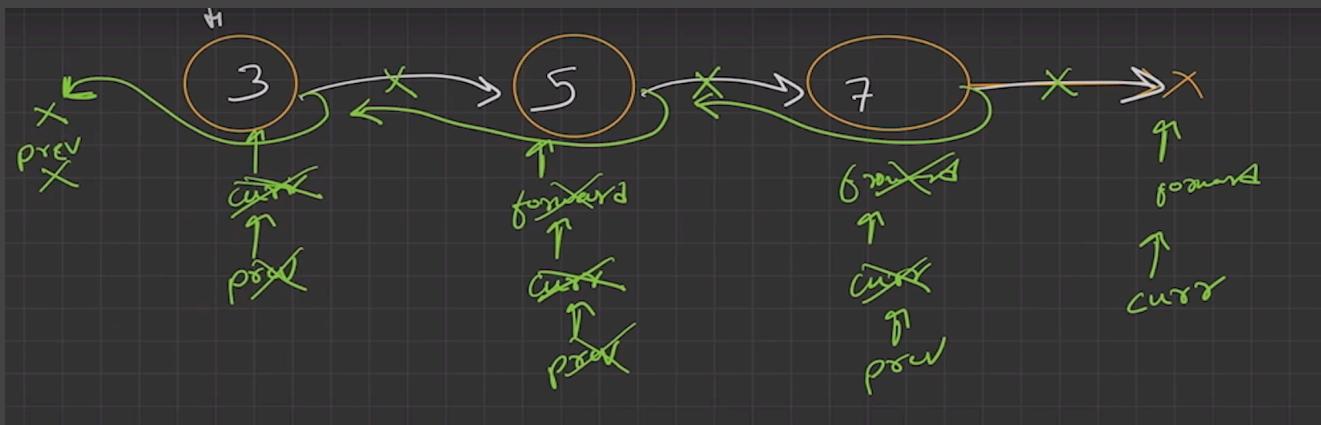
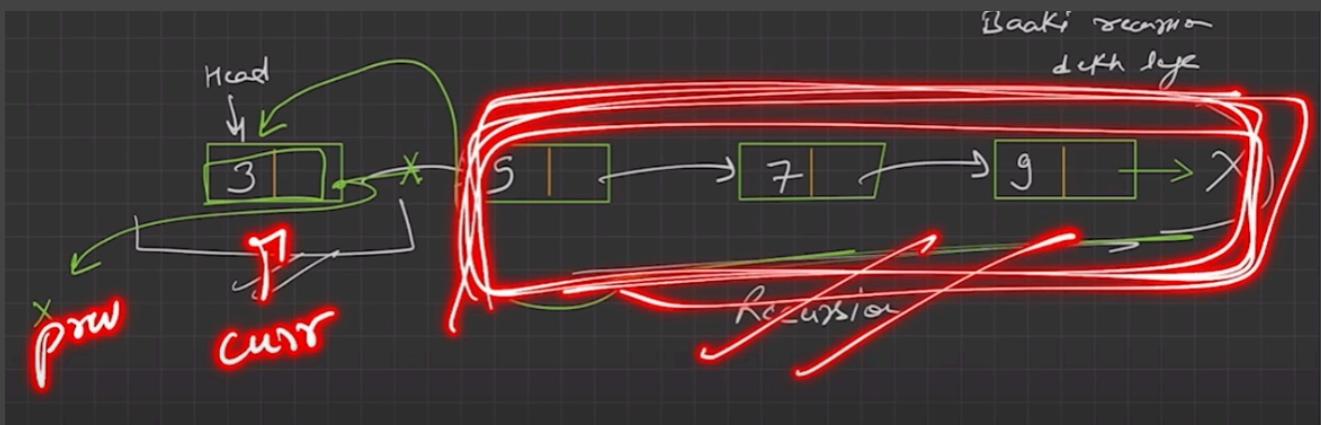


Linked-List

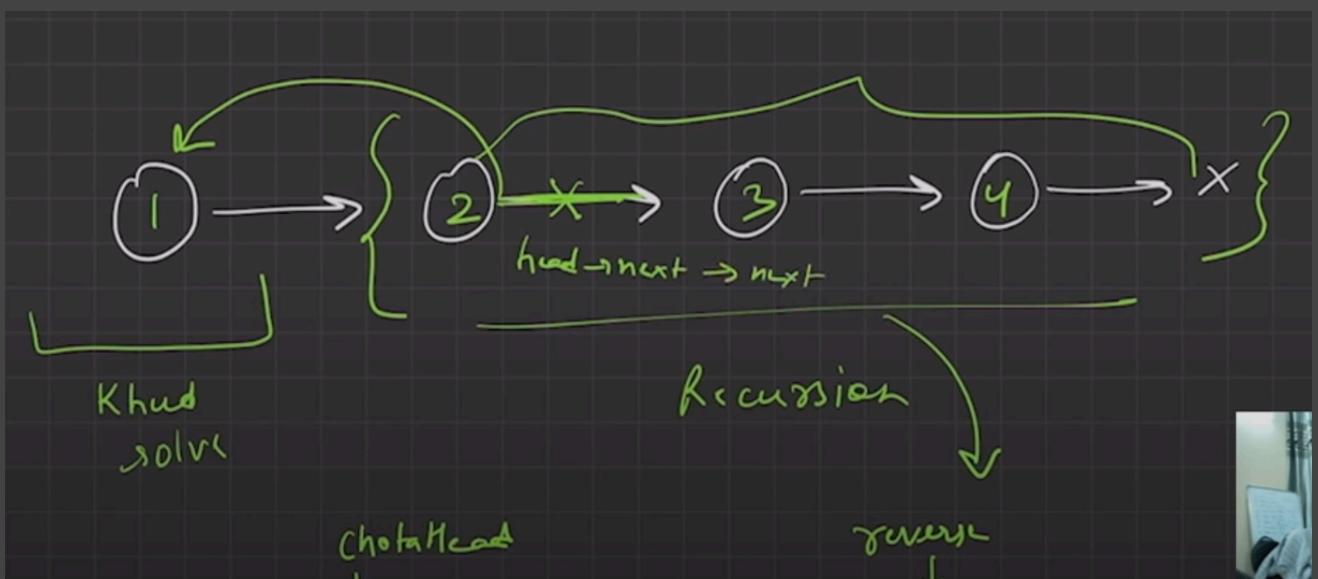
Reverse A Singly Linked List Approach-I:



Reverse A Singly Linked List Approach-II:

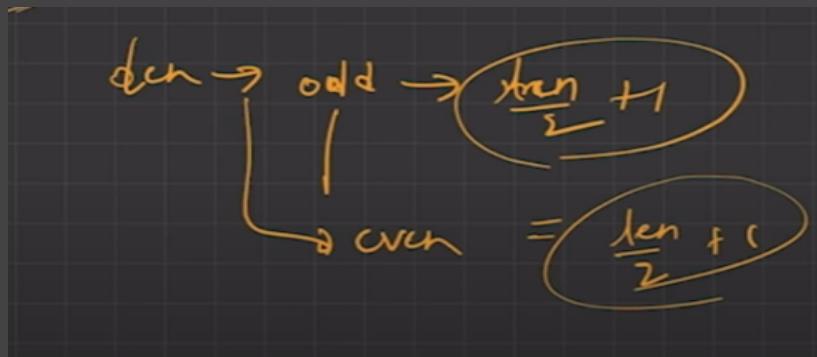
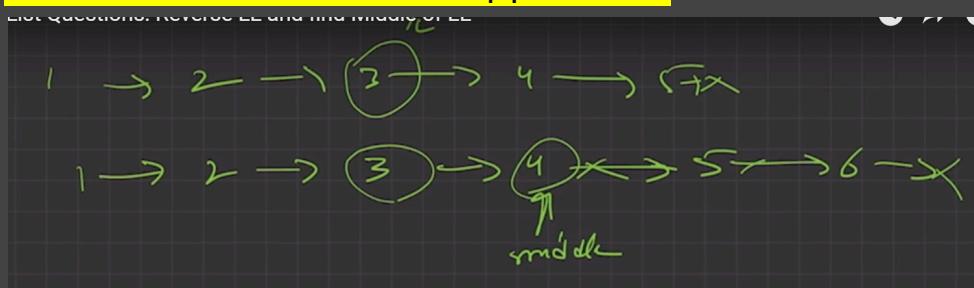


Reverse A Singly Linked List Approach-III:

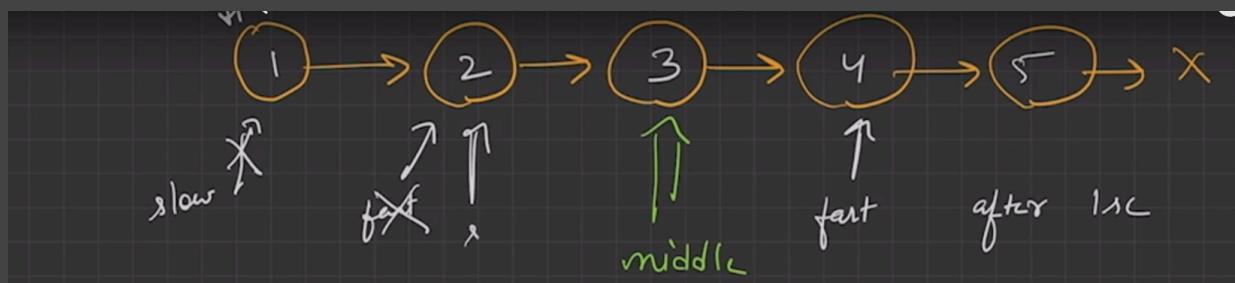


Reverse A Doubly Linked List

Find Middle In A Linked List Approach-I:



Find Middle In A Linked List Approach-II:



① if \rightarrow empty list \rightarrow return `NULL`



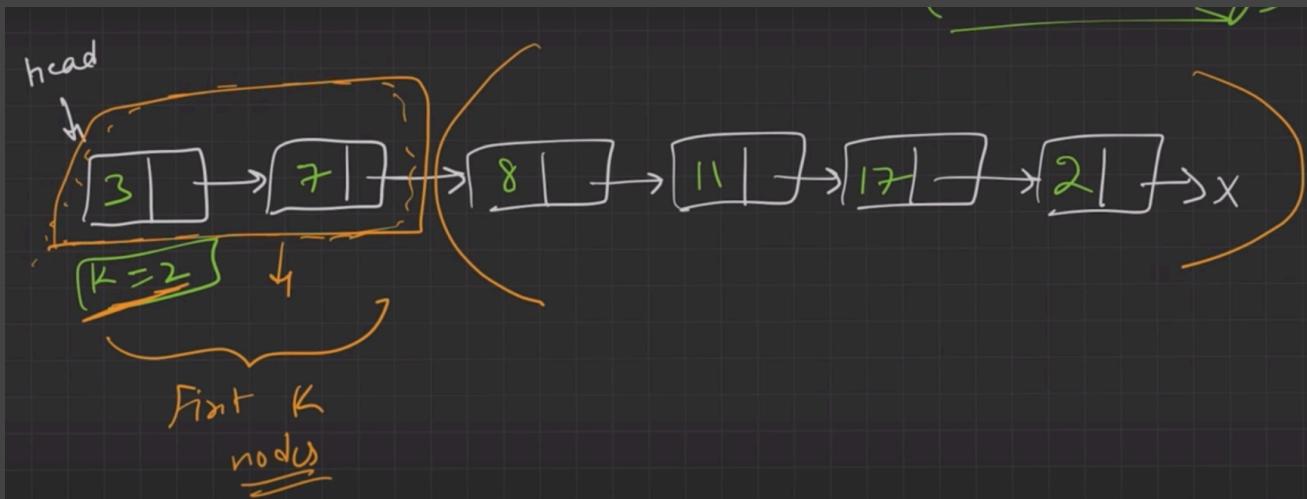
② 1 node \rightarrow head

③ 2 nodes \rightarrow head \rightarrow next

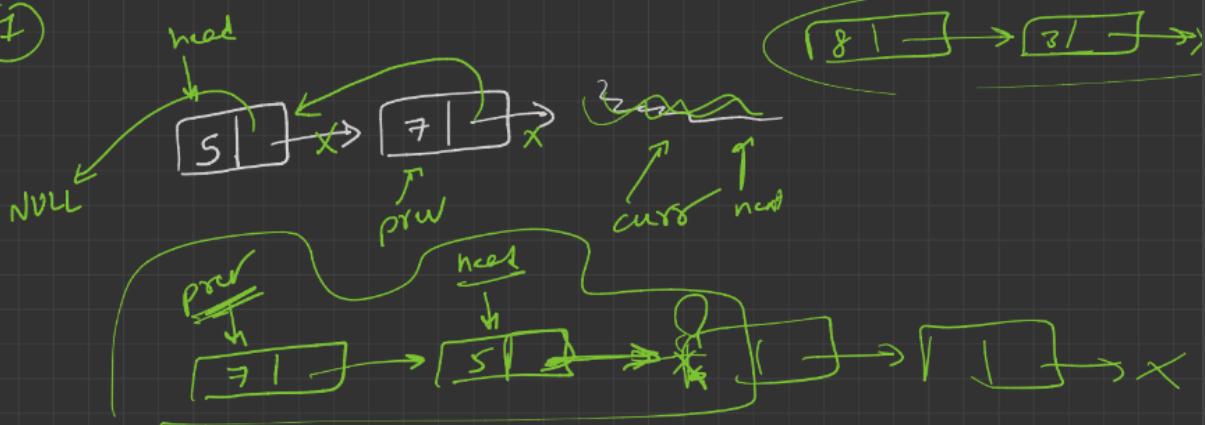
④ Algo



Reverse Linked List In 'K' groups:



(i)



(ii)

$head \rightarrow next \rightarrow$ Recursion call

(iii)

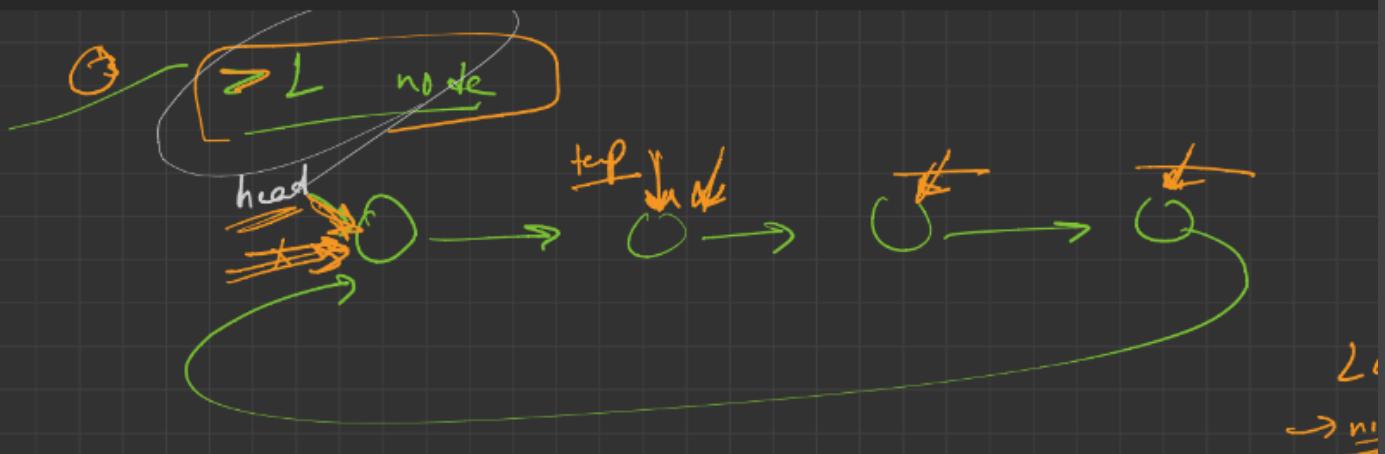
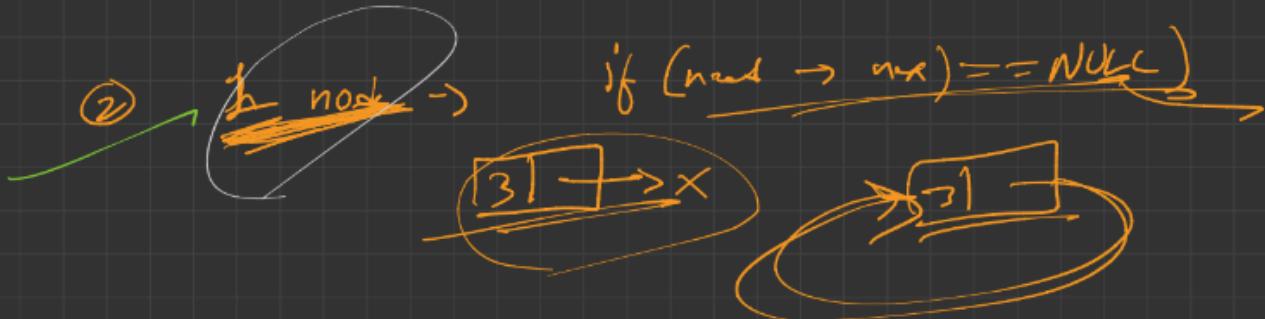
return prev

Check Whether A Linked List is Circular or Not Approach-I:

Approach 1 :-

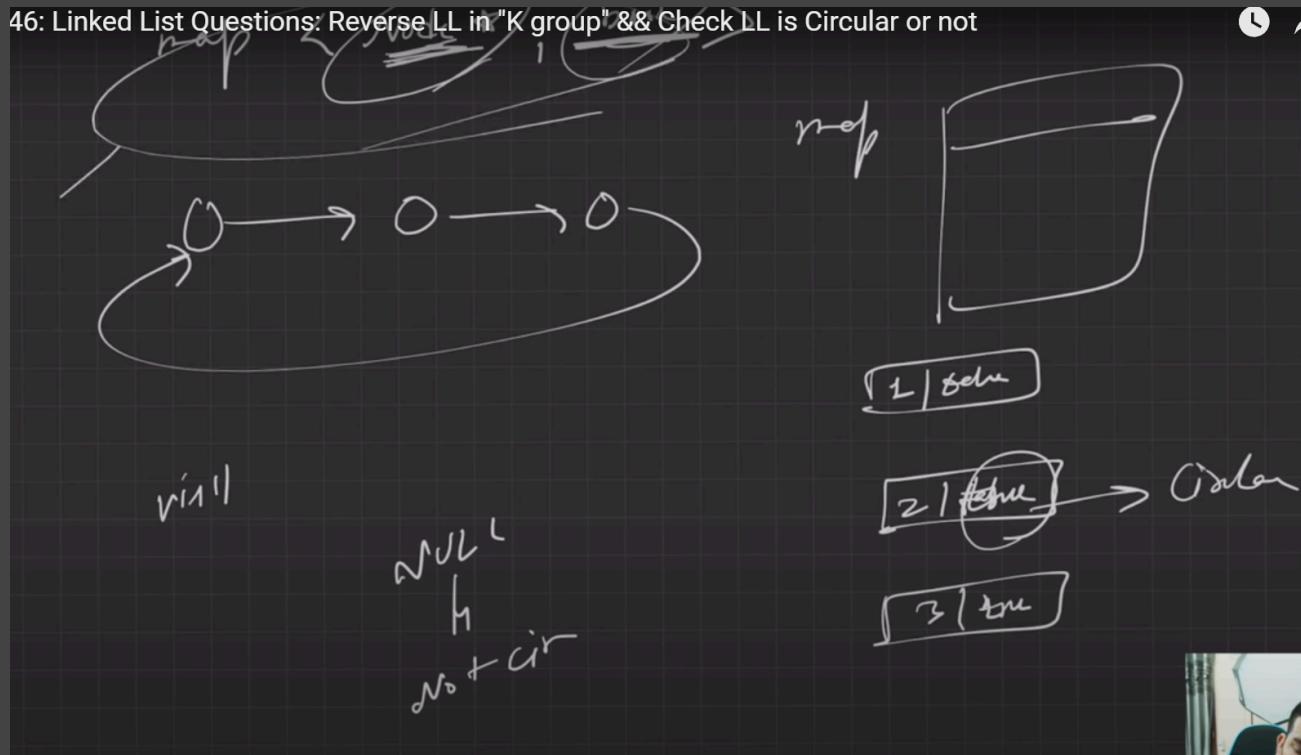


(1) Empty List \rightarrow if (head == NULL)
return True

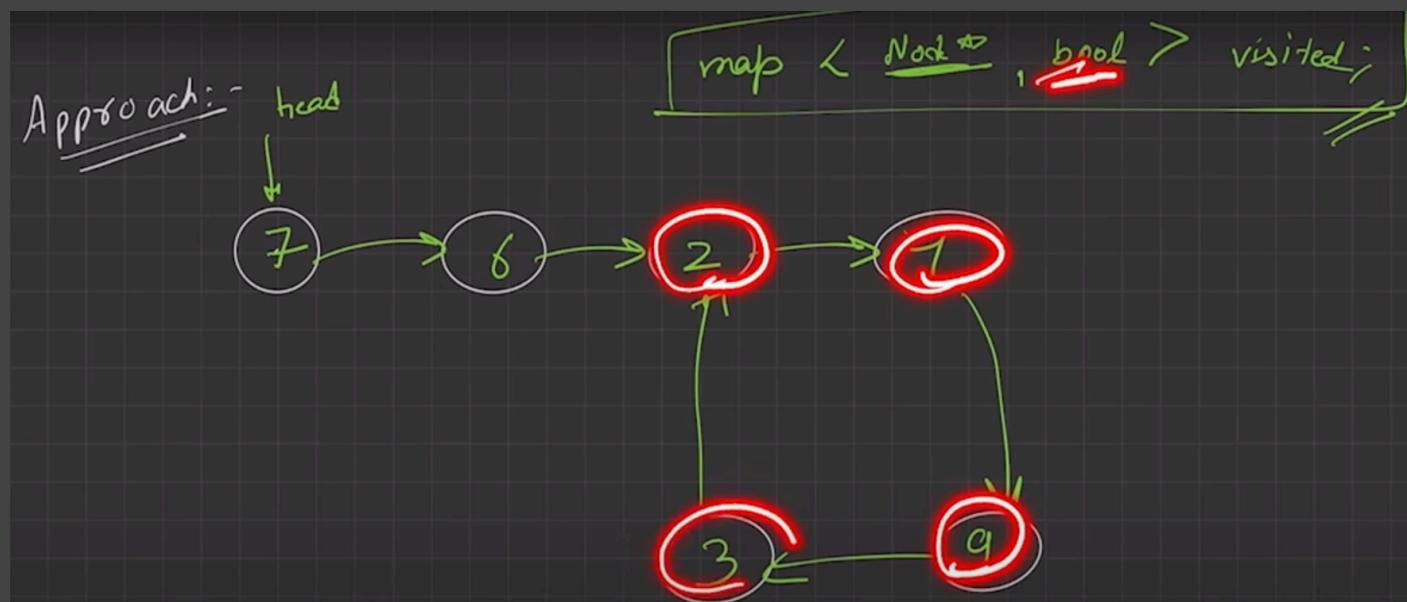


Check Whether A Linked List is Circular or Not Approach-II:

46: Linked List Questions: Reverse LL in "K group" && Check LL is Circular or not

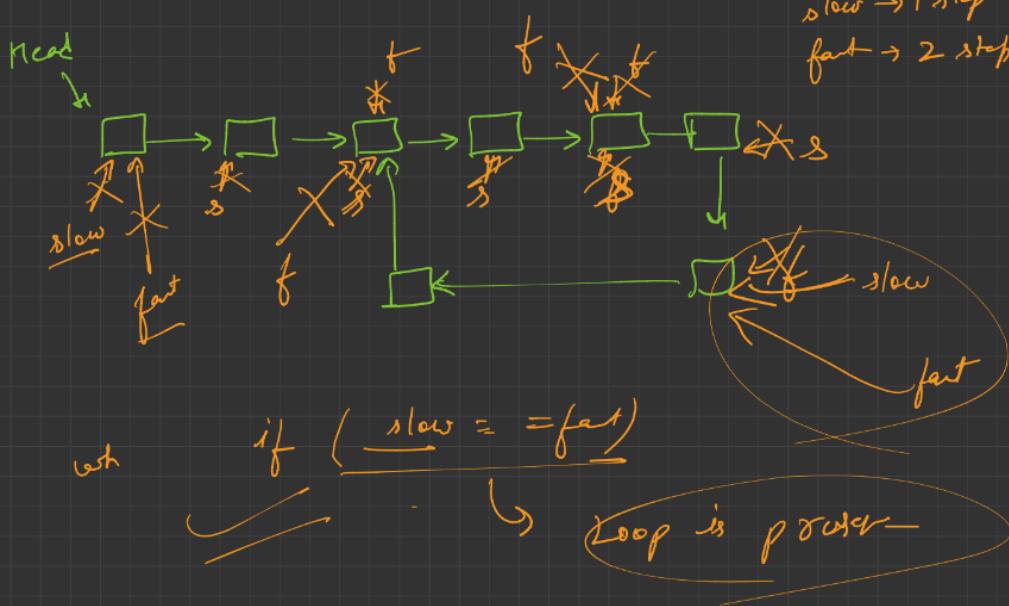


Detect Whether A Linked List Forms a Loop or Not:

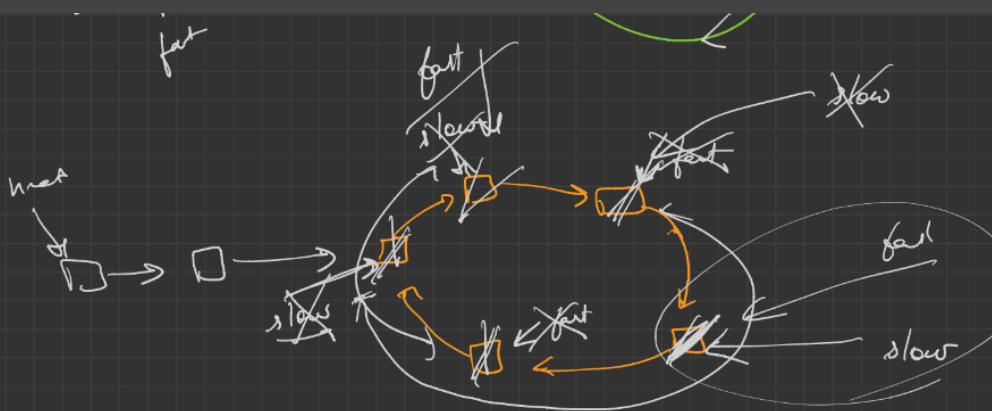


Floyd's Cycle Detection:

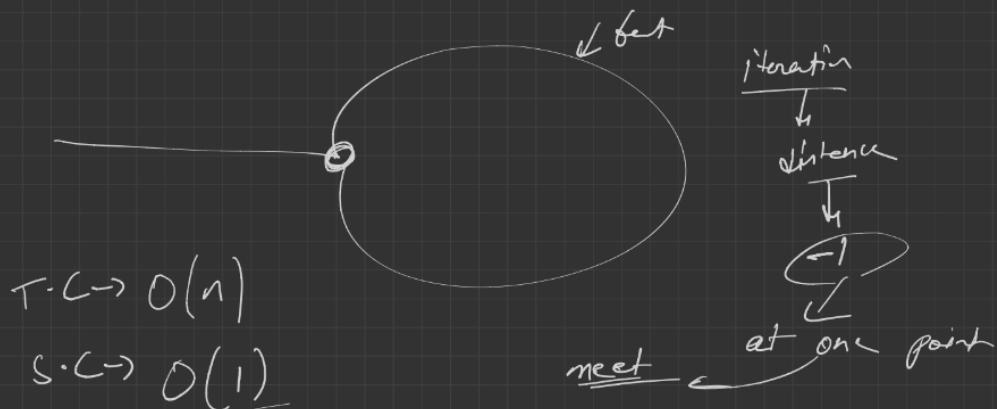
① Floyd's cycle detection algo.



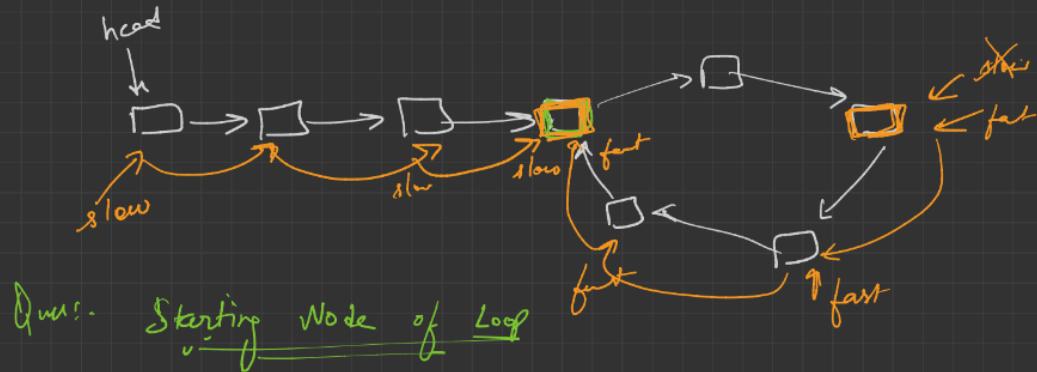
② fast = NULL → No loop



Distance: 4, 3, 2 1



Find The Starting Node Of The Loop:



Approach:-

I \rightarrow FCD Algo \rightarrow Point of Intersection

II \rightarrow $slow = head$
 $slow, fast \rightarrow$ same pace
 / / /

when ($slow == fast$)

\hookrightarrow [start of point of Loop]

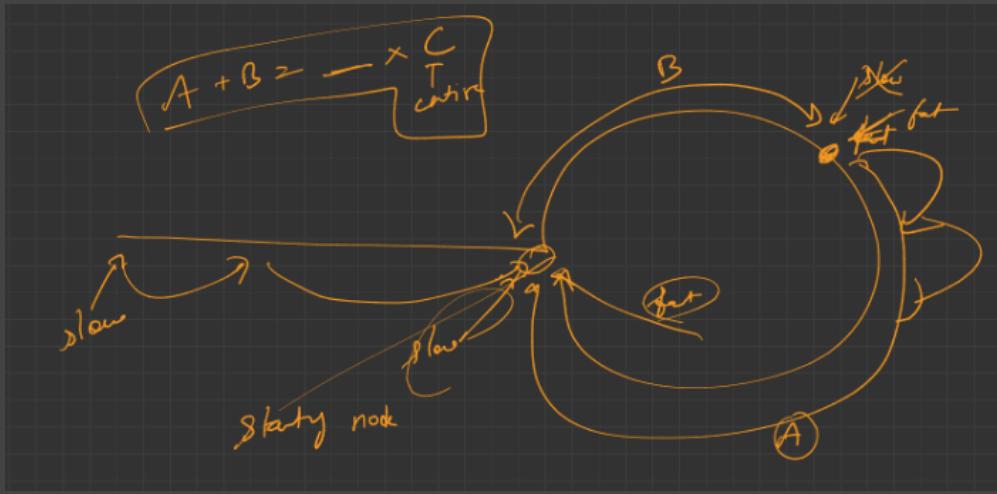
Distance by $= 2 \star$ Distance by slow pointed
 fast pointer

$$(A + x * C + B) = 2 \star (A + y * C + B)$$

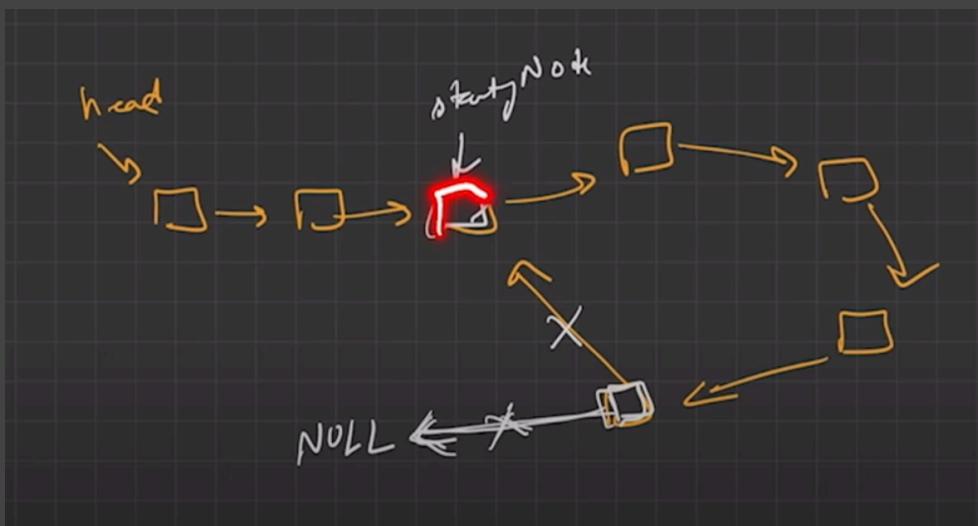
$$A + nC + B = 2A + 2yC + 2B$$

$$C(n - 2y) = A + B$$

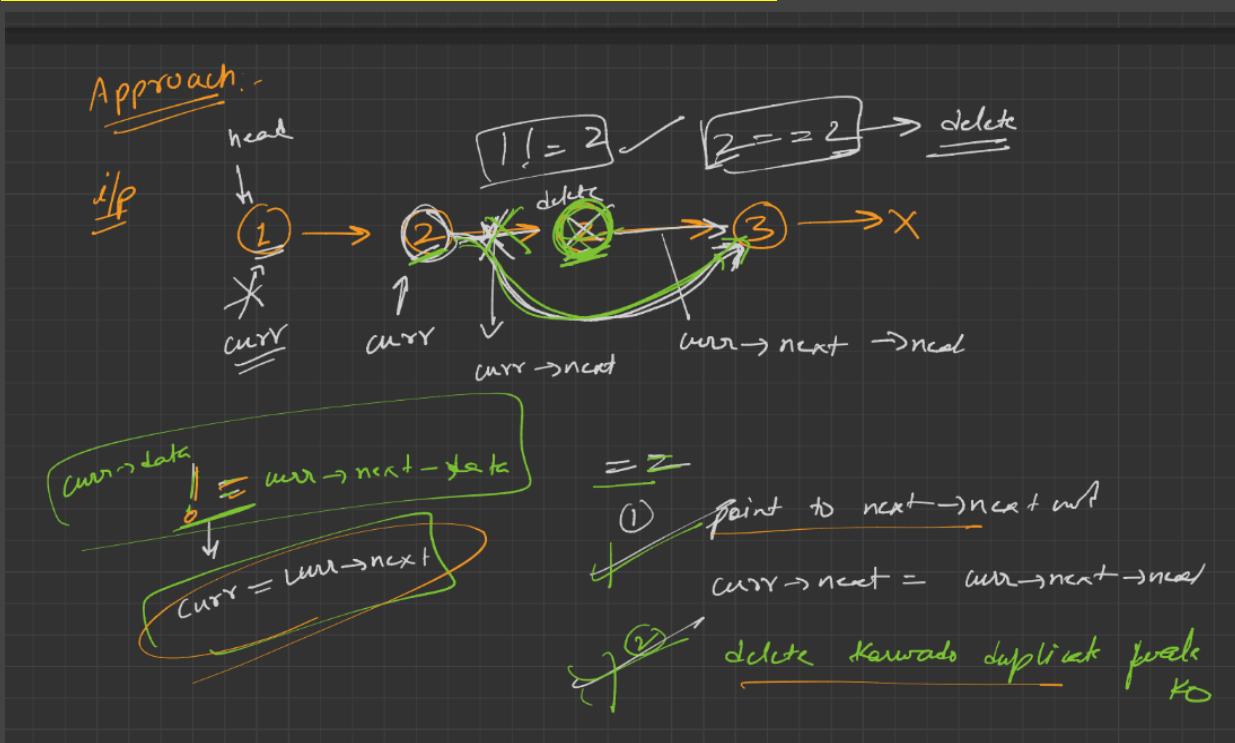
$$\frac{A + B}{K} = \frac{n - 2y}{C}$$



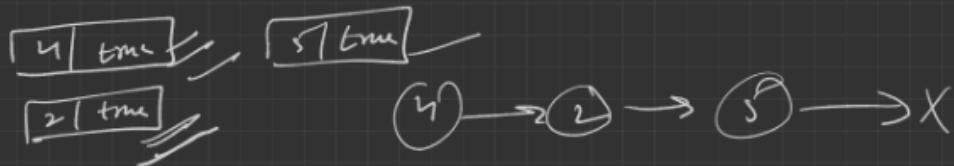
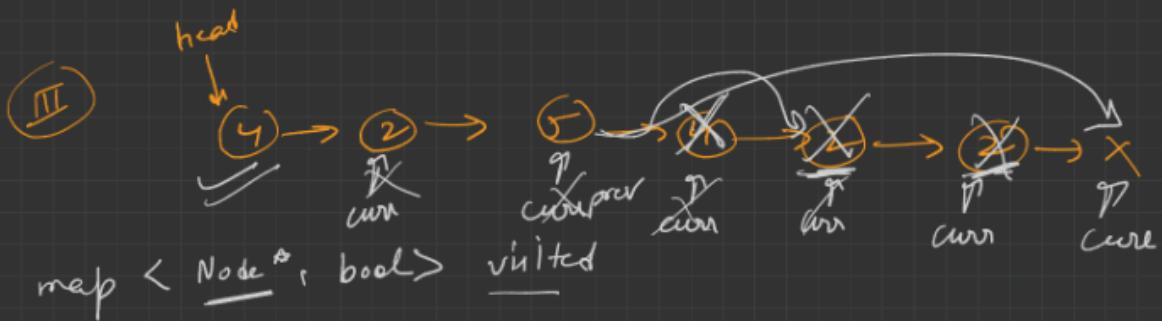
Remove The Loop:



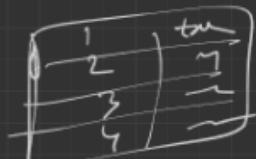
Remove Duplicates From A Sorted Linked List:



Remove Duplicates From A Unsorted Linked List:



$$\begin{array}{l} T \cdot C \rightarrow O(n) \\ S \cdot C \rightarrow O(n) \end{array}$$



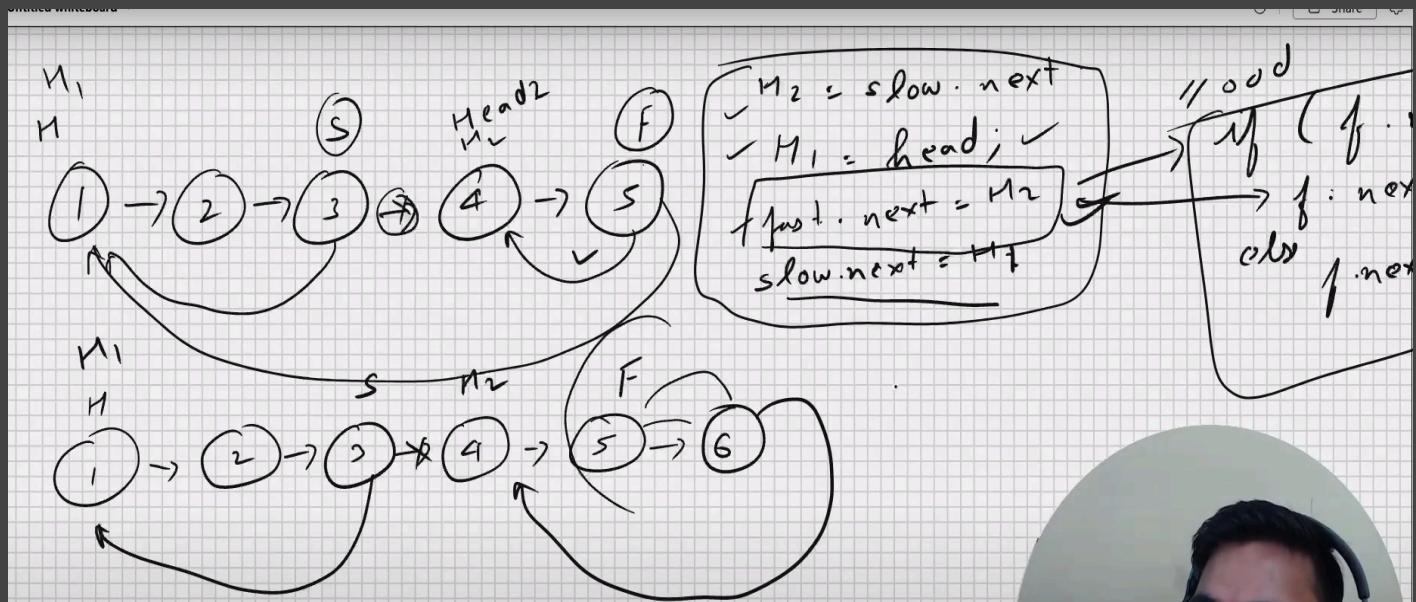
Remove Duplicate from Unsorted L

Homework

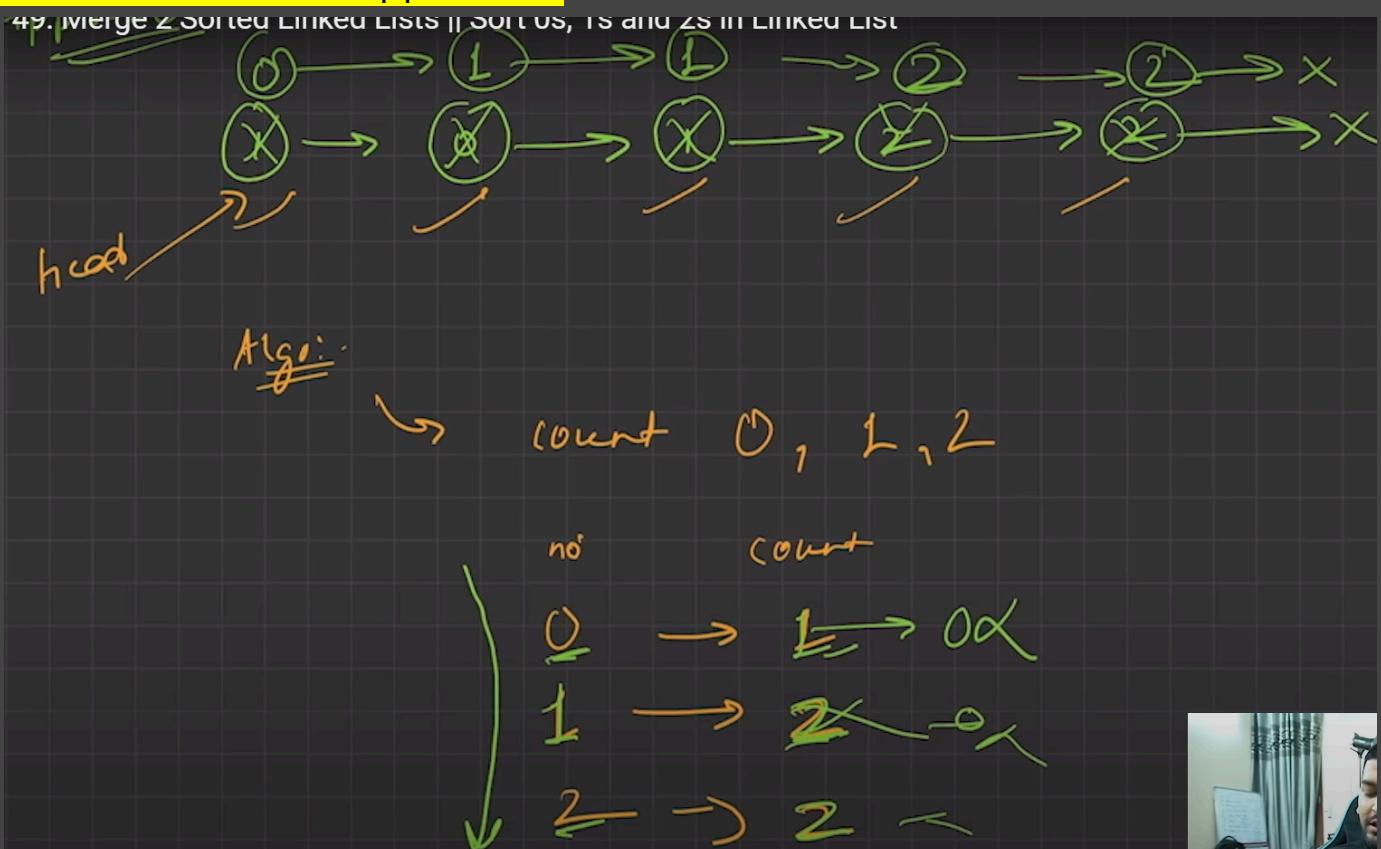
$\rightarrow O(n) \rightarrow 2\text{ Loops}$

$\Rightarrow O(n \log n) \rightarrow \text{sort} \rightarrow O(n)$ when
 $\Rightarrow \boxed{n \log n \rightarrow O(n)}$

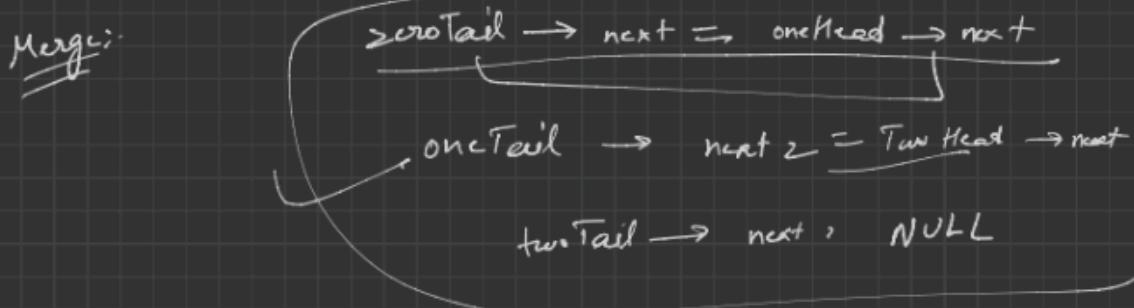
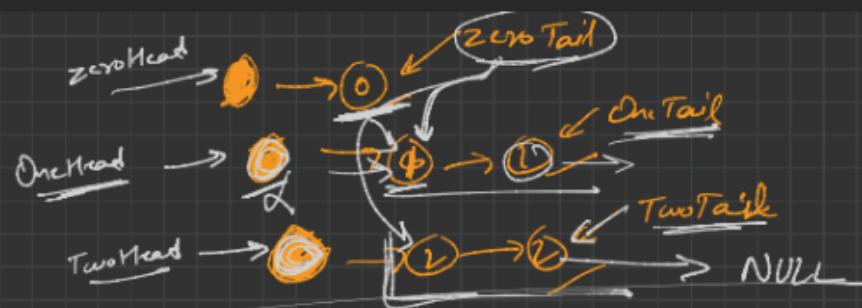
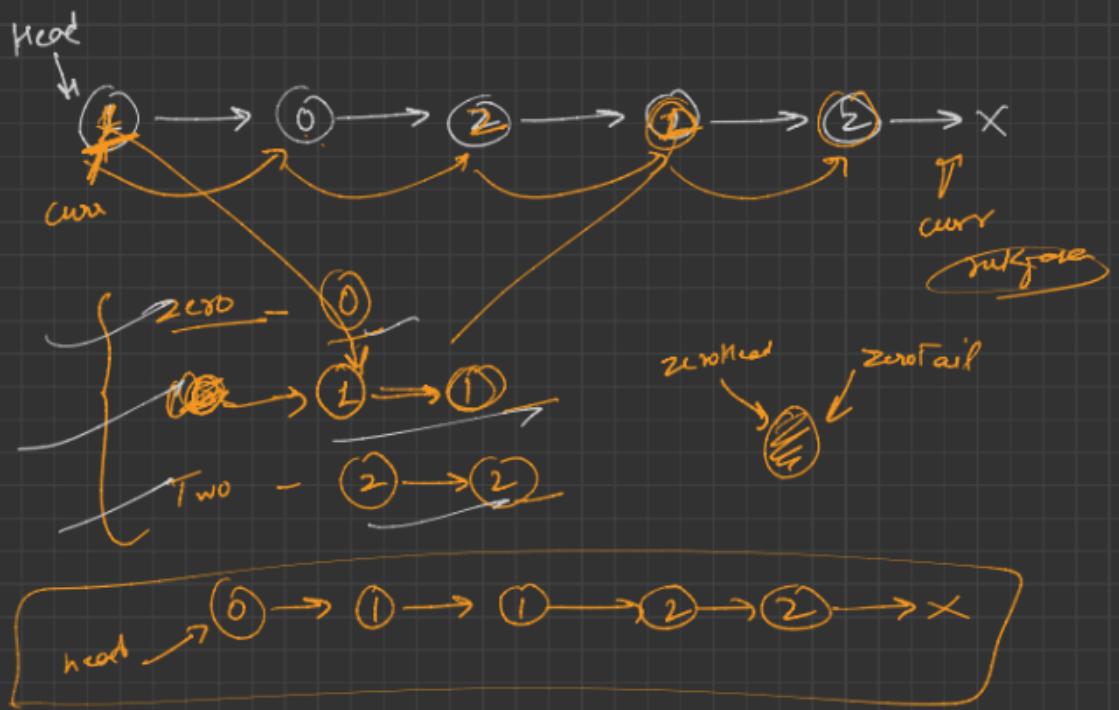
Split A Circular LL Into Two Halves:



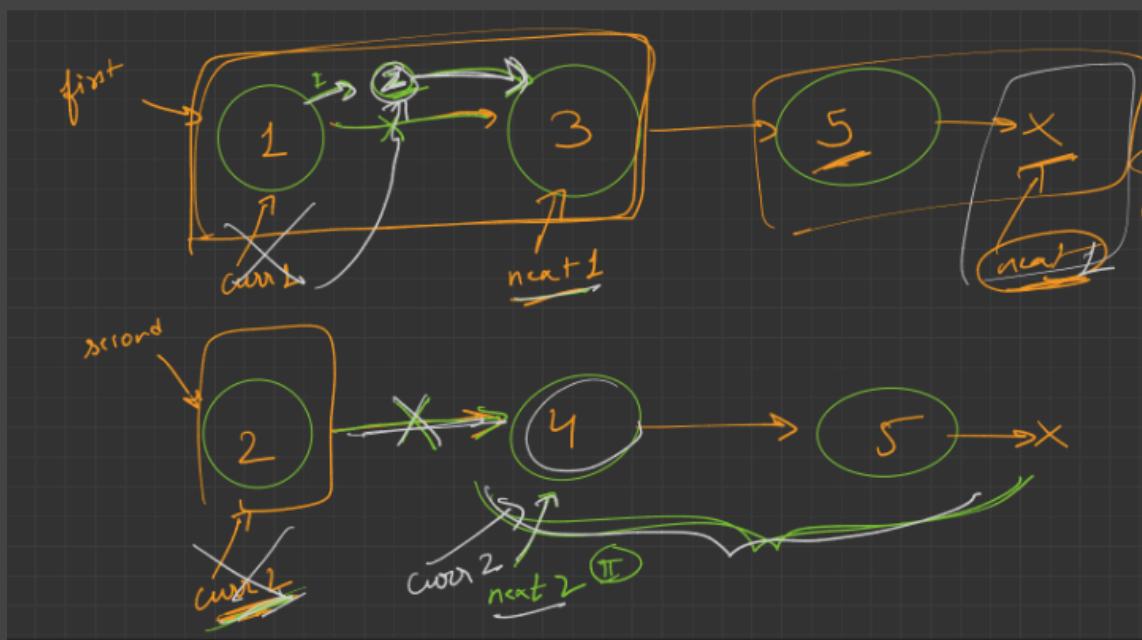
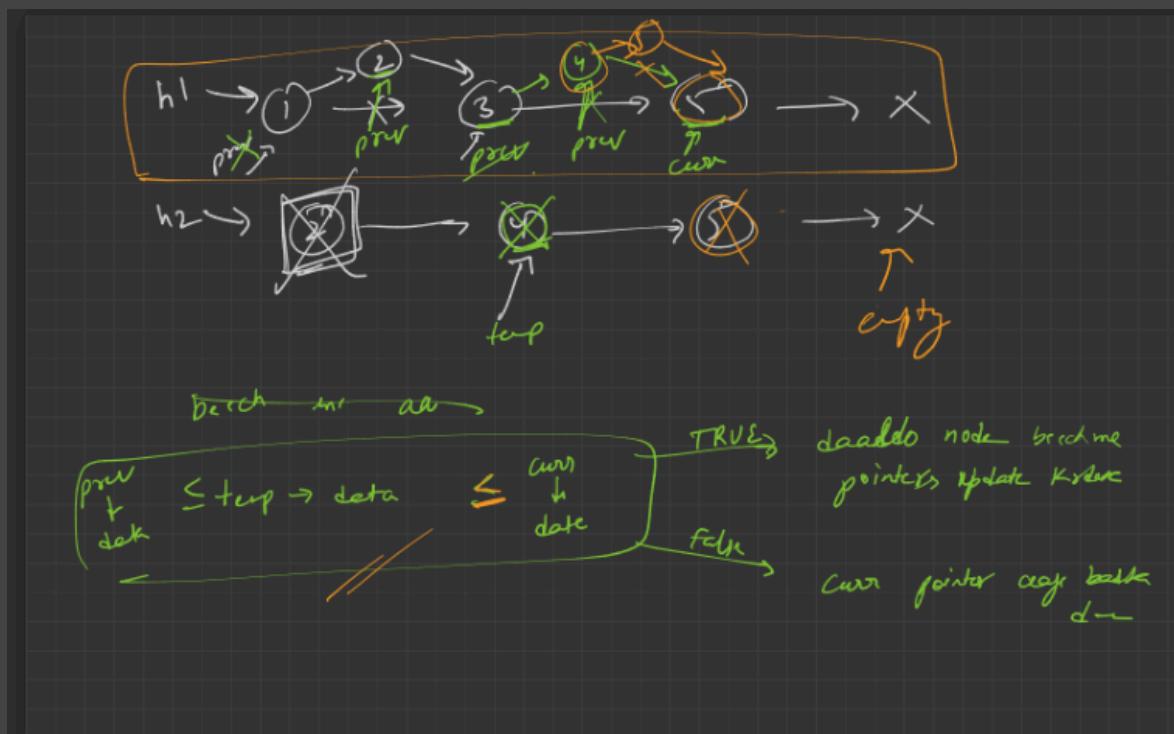
Sort 0s, 1s & 2s In A LL Approach-I:



Sort 0s, 1s & 2s In A LL Approach-II:



Merge Two Sorted LL:



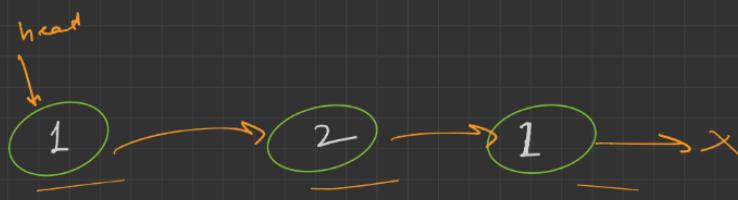
$$\left. \begin{array}{l}
 \text{I} \rightarrow curr1 \rightarrow next = curr2 \\
 \text{II} \quad next2 = curr2 \rightarrow next \\
 \text{III} \quad curr2 \rightarrow next = next - 1
 \end{array} \right\}$$

$$(N) \Rightarrow curr1 = curr2$$

$$(v) = curr2 = nc$$

Check Palindrome In LL Approach-I:

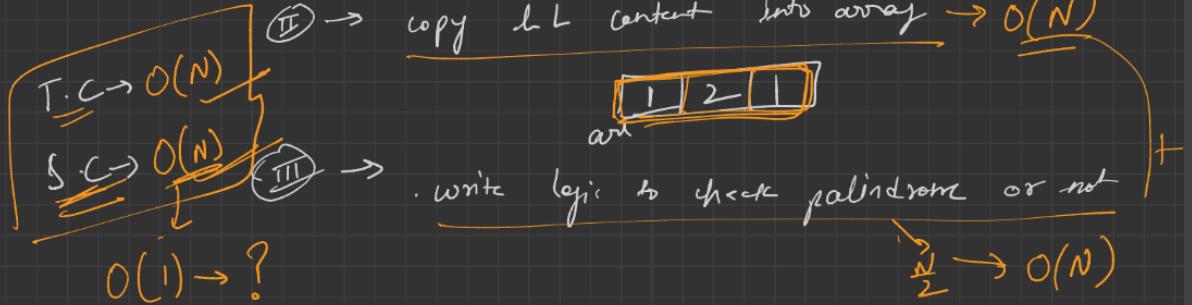
Approach #1



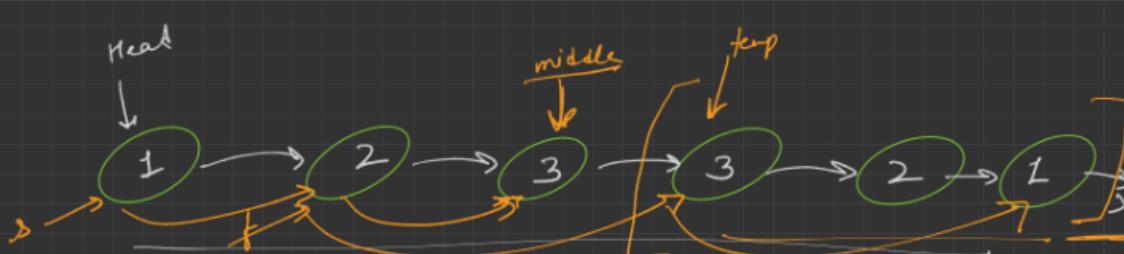
Algo:-

① → create an array

② → copy h L content into array $\rightarrow O(N)$



Check Palindrome In LL Approach-II:



Algo:-

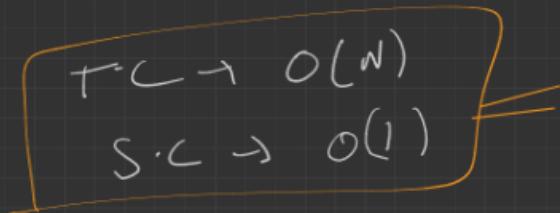
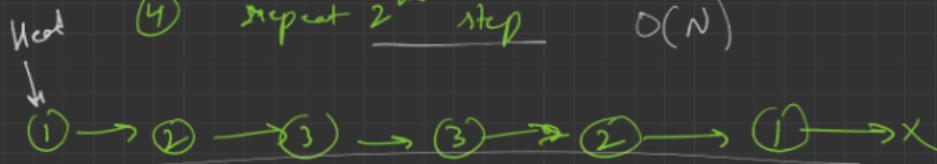
① middle (find) $\rightarrow O(N)$

head ② reverse LL after it $O(N)$

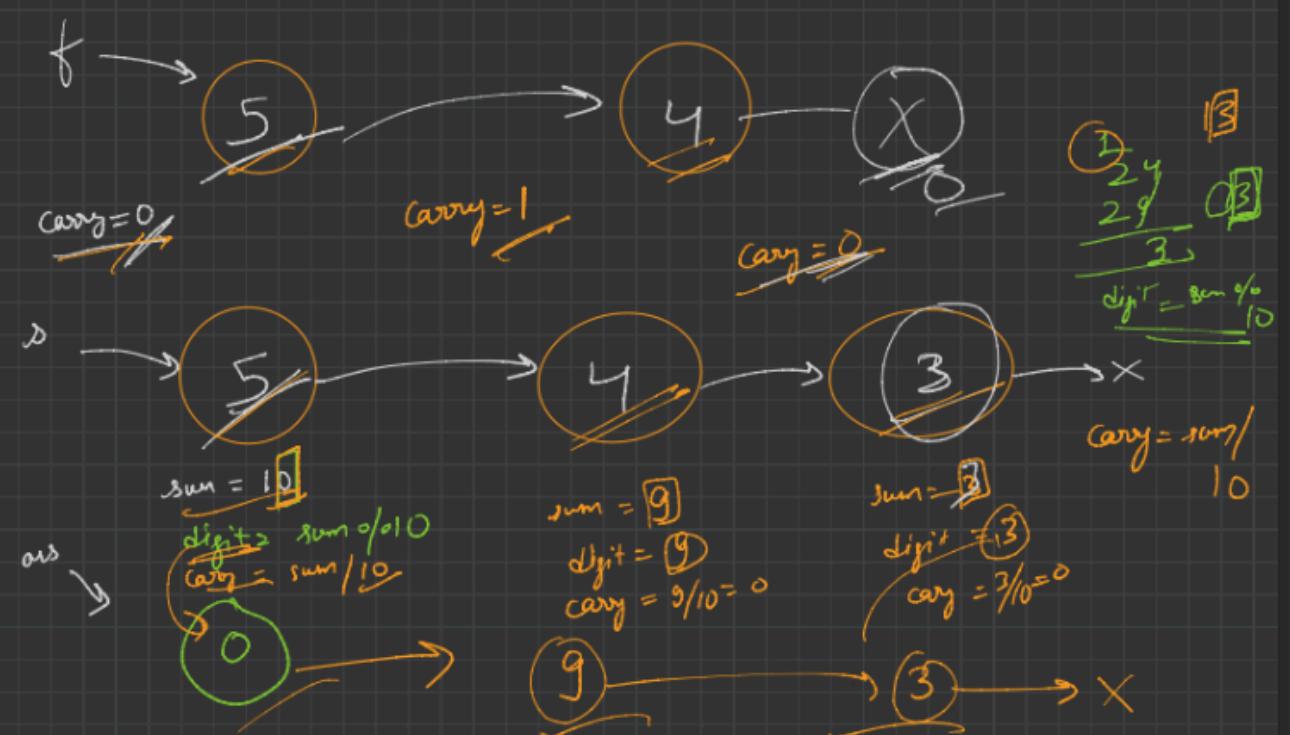


③ compare both halves PL or not $O(N)$

④ repeat 2ⁿ⁻¹ step $O(N)$



Add Two Numbers Represented By Linked List:

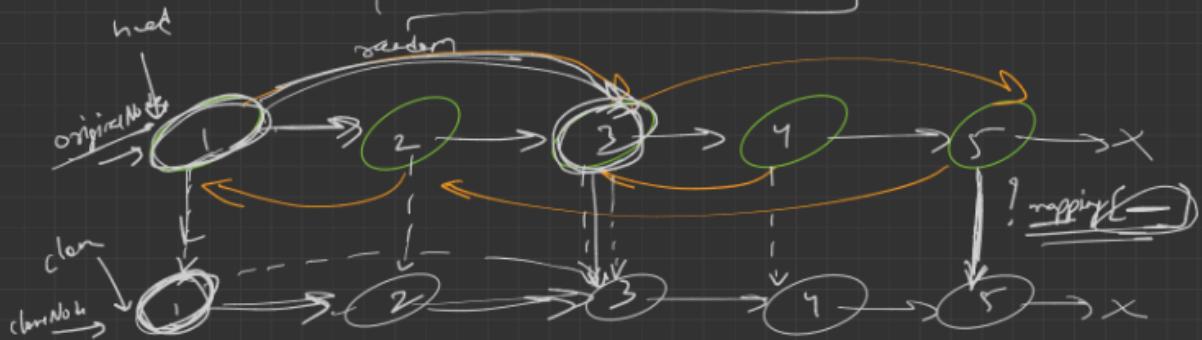


Clone A Linked List Approach-I:

Approach #2

↳ (I) → create a clone List (using next ptr of Original List)

↳ (II) Random ptr (copy) →



(II) $\text{clone Node} \rightarrow \text{random} = ?$

mapping [original Node \rightarrow random]

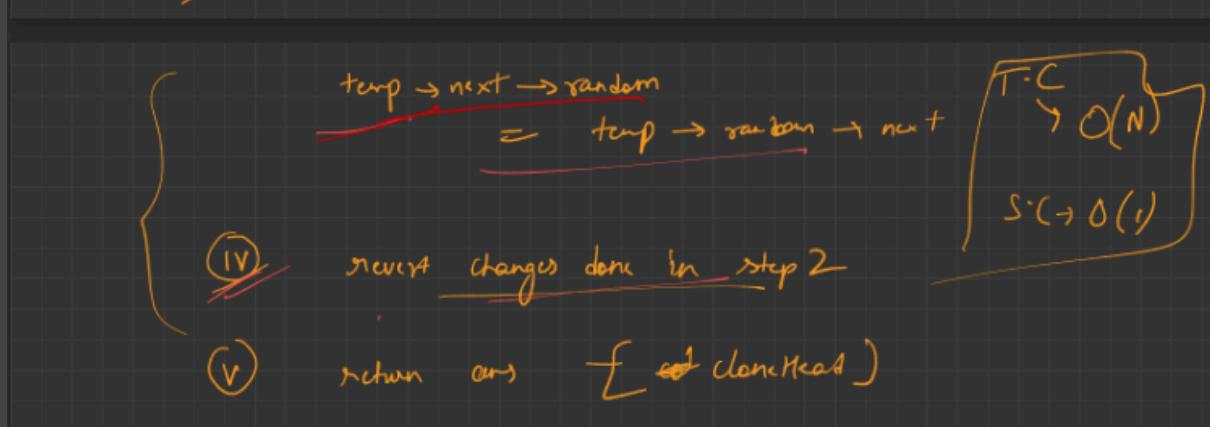
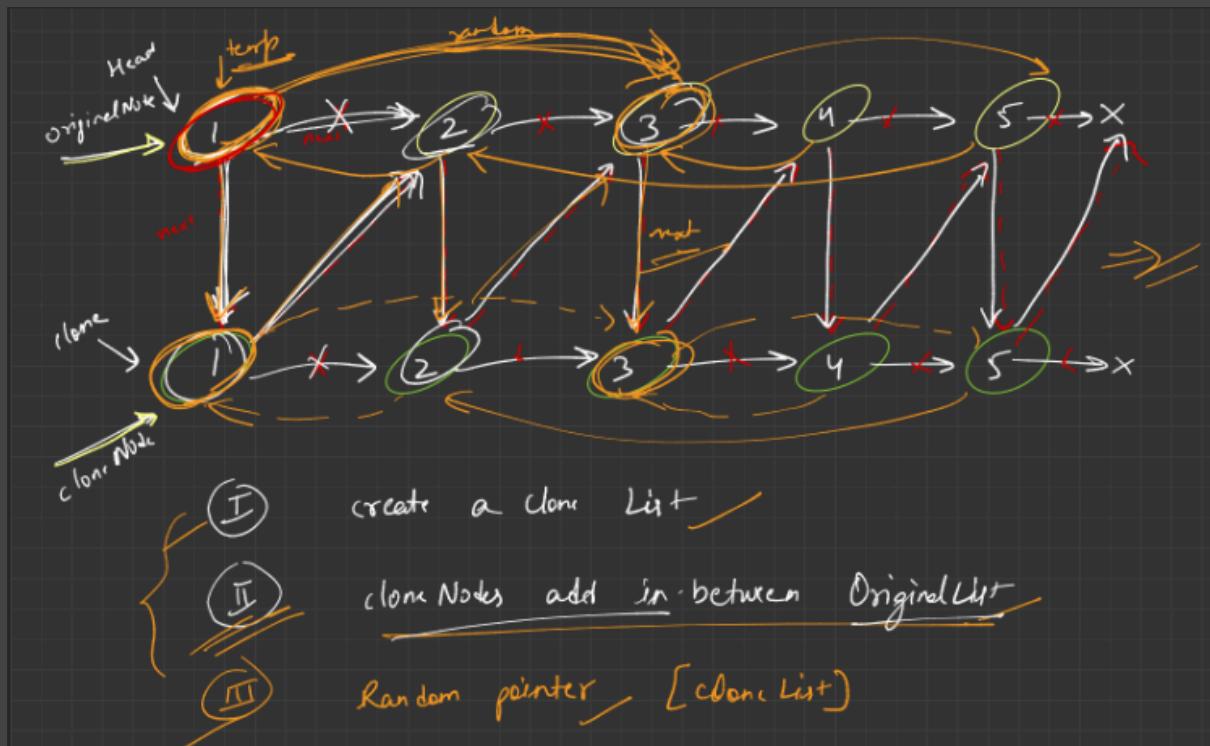
T.C $\rightarrow O(N)$

S.C $\rightarrow O(N)$

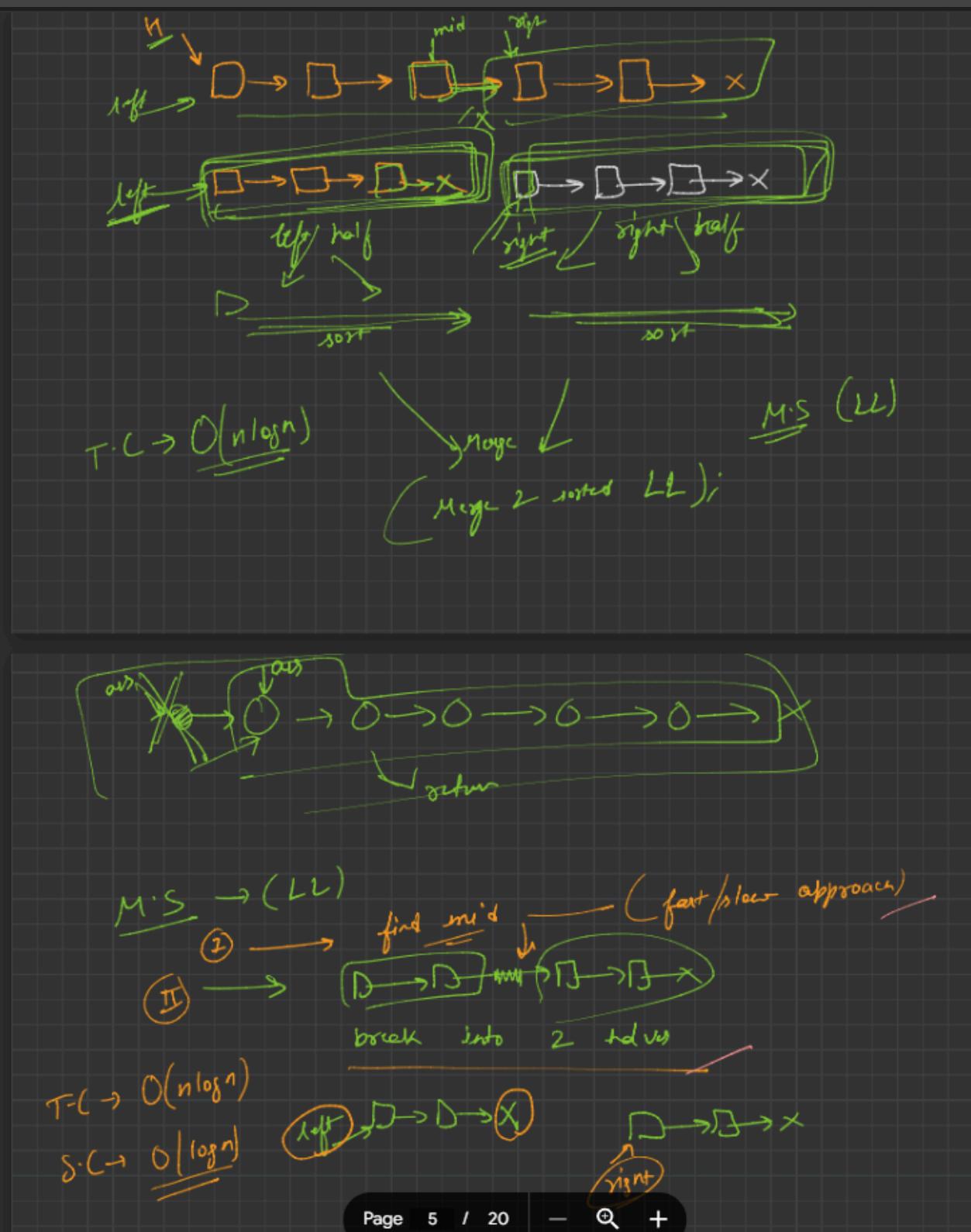
$O(1)$

map α

Clone A Linked List Approach-II:



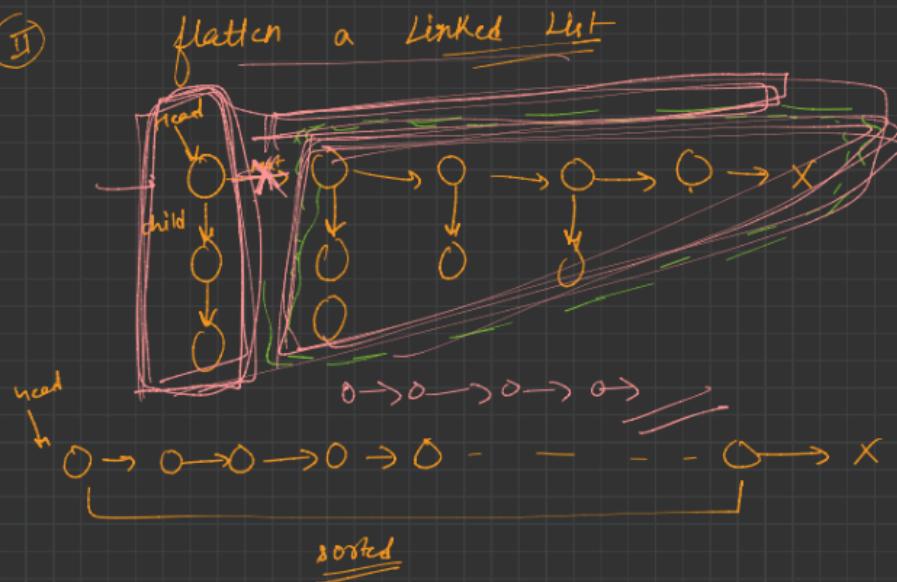
Merge Sort In Linked List:



- III Recursively sort left/right halves
- IV merge left/right sorted halves \rightarrow Merge 2 sorted LL
- V return merged list

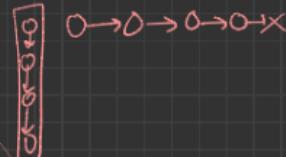
Flatten Linked List:

(ii)



flatten (head)

Node * down = head ;
down -> next = NULL ;
Node * right = flatten (head -> right)



Merge 2 sorted
linked list

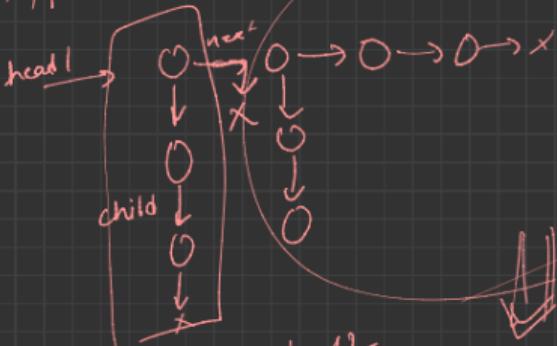
Exact
Order

Node * ans = merge (down, right)

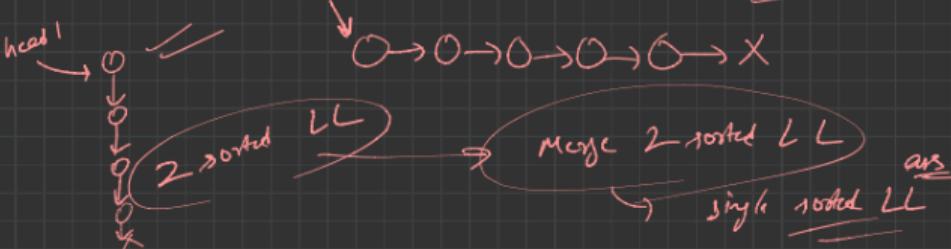
return ans ;

1 | 2 | 3

i/p

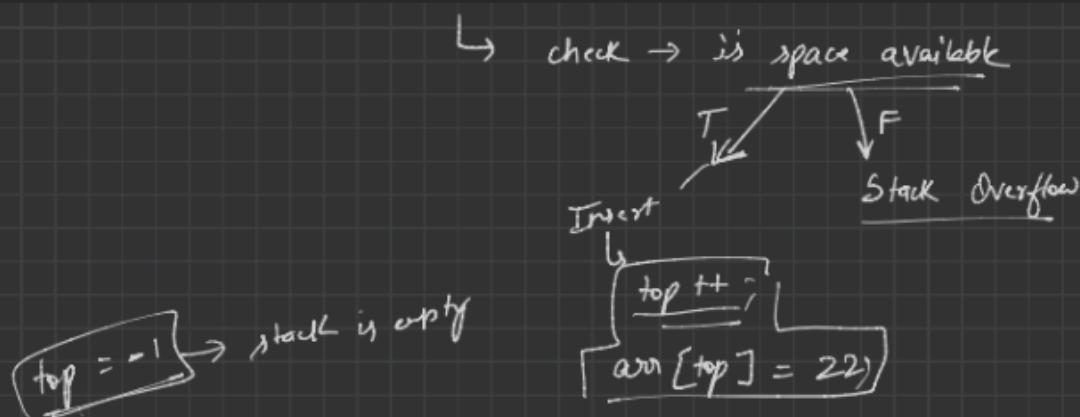
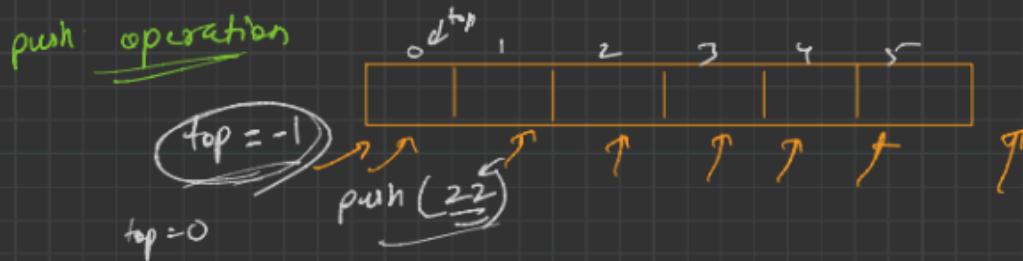
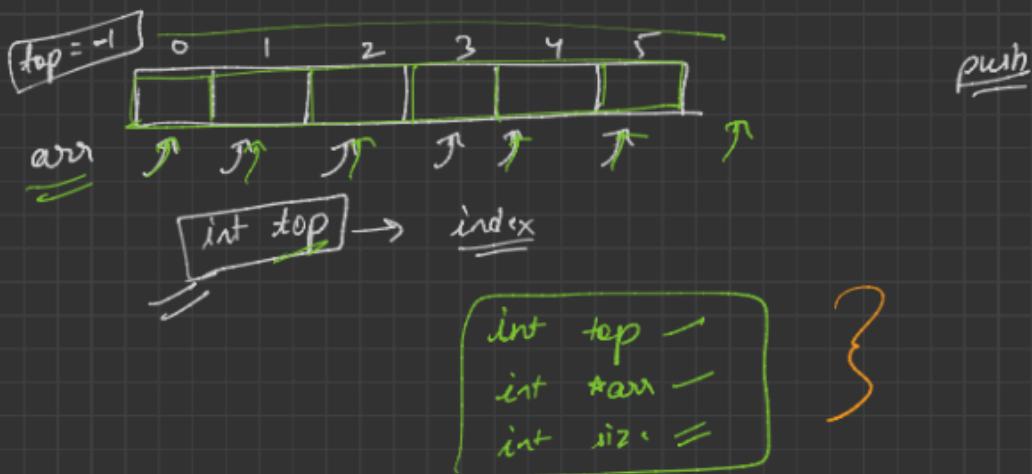
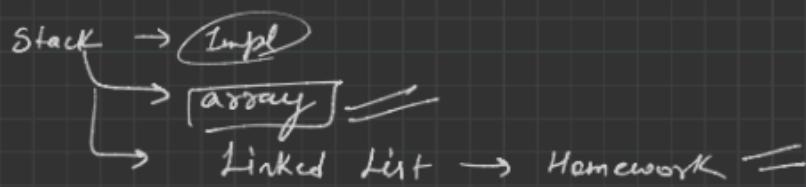


Recurr.

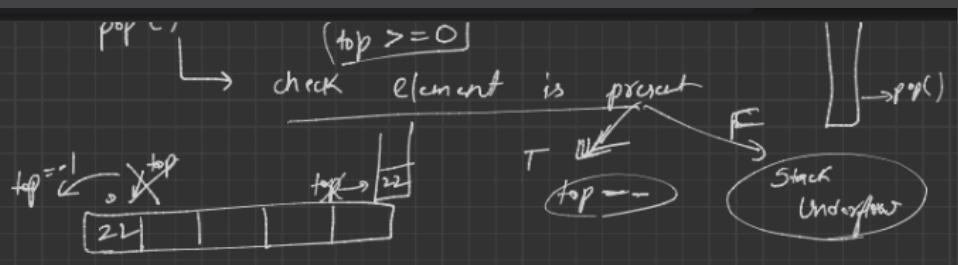


Stack

Create A Stack Using An Array:



Create A Stack Using A Linked List:



$\text{empty}()$

$\text{top} = -1 \rightarrow \text{stack empty}$

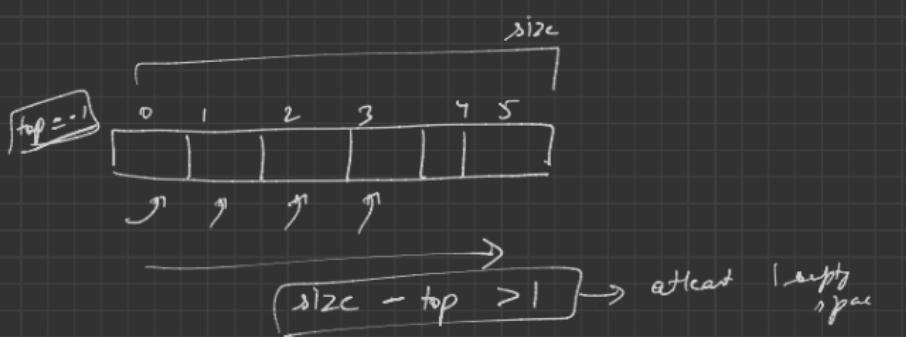
$\text{top}()$

$\text{top} \rightarrow 0$

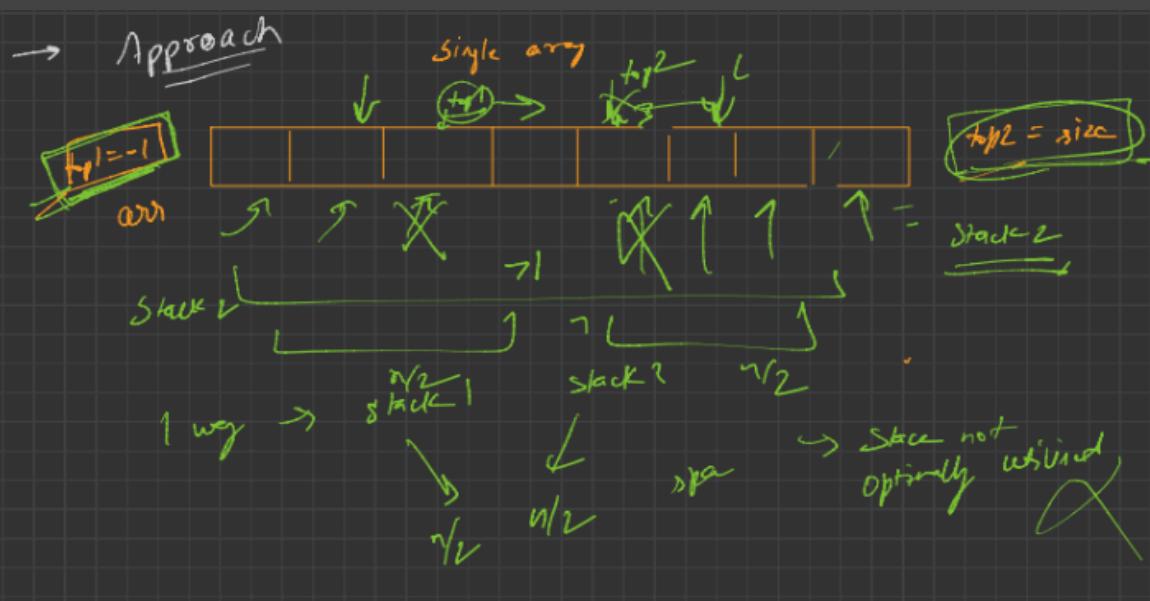
$\Rightarrow \text{return arr}[\text{top}]$

$\text{top} = -1 \rightarrow$

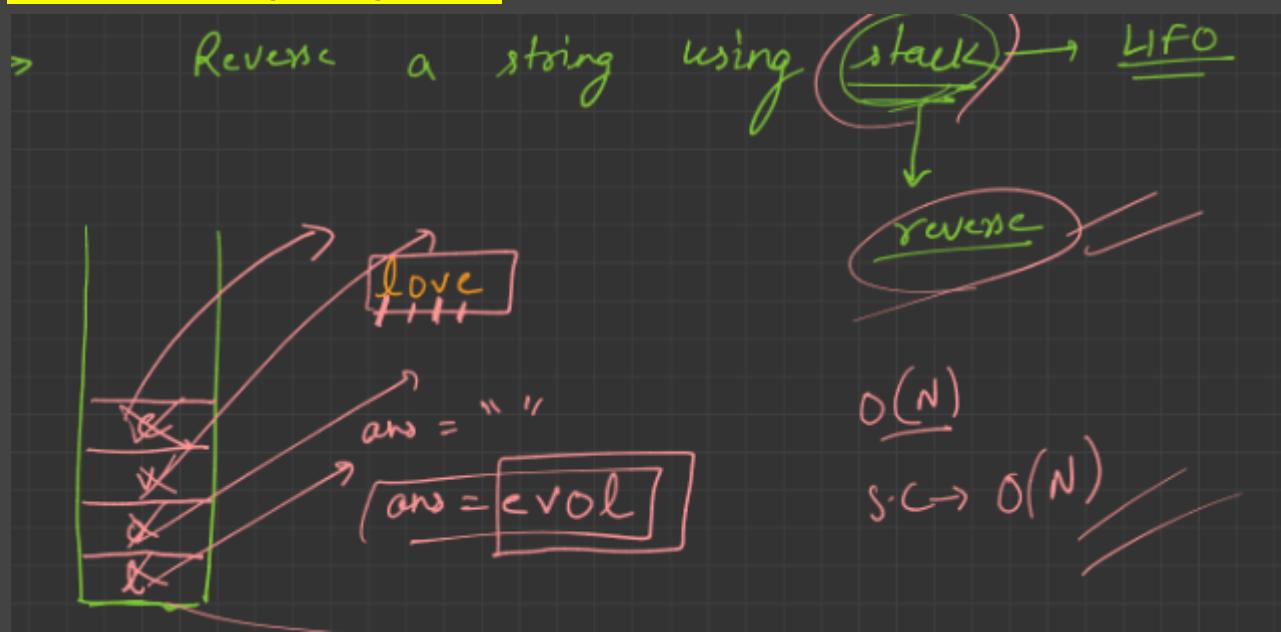
$\text{top} < \text{size} \rightarrow$



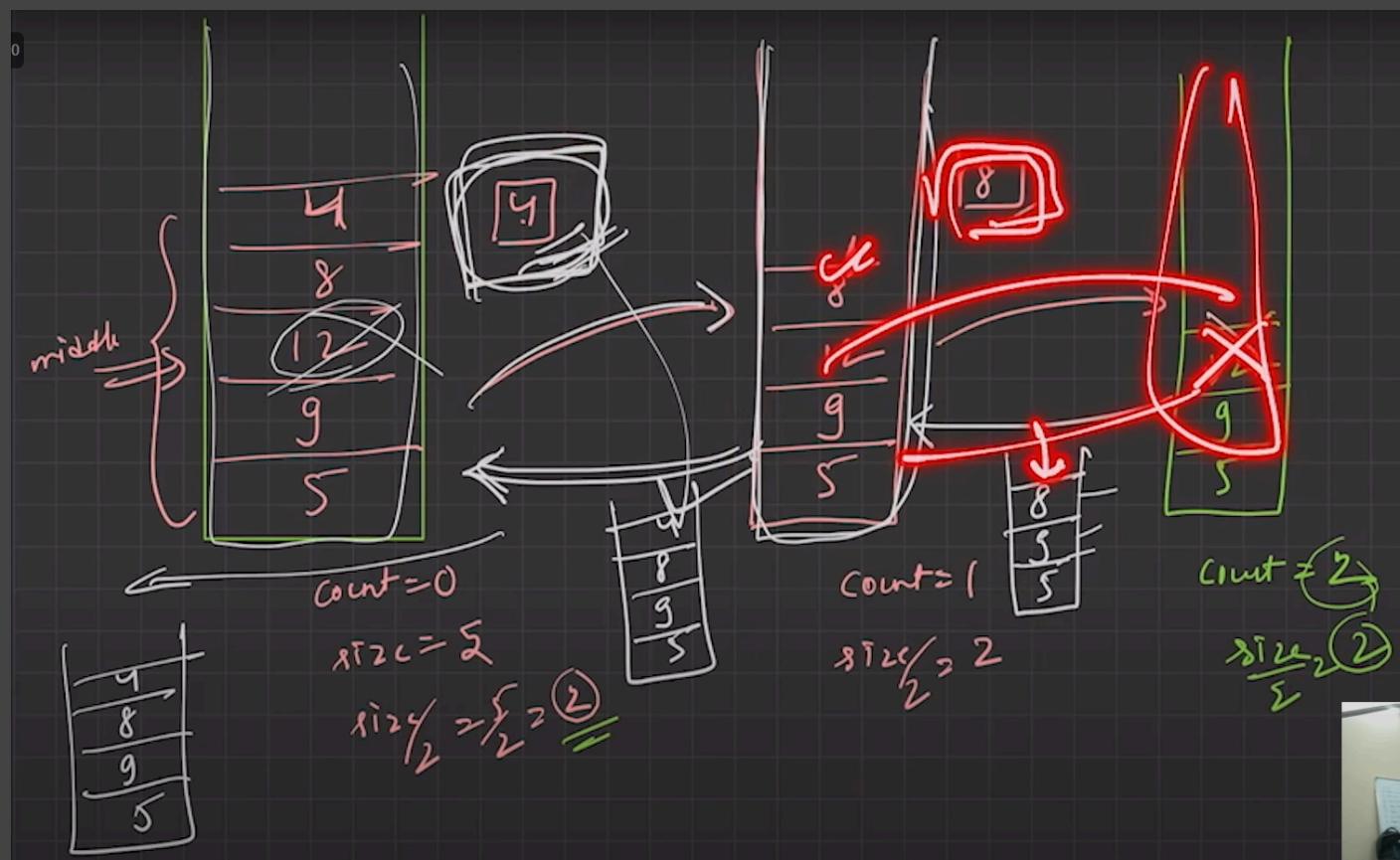
Create Two Stacks Using An Array:



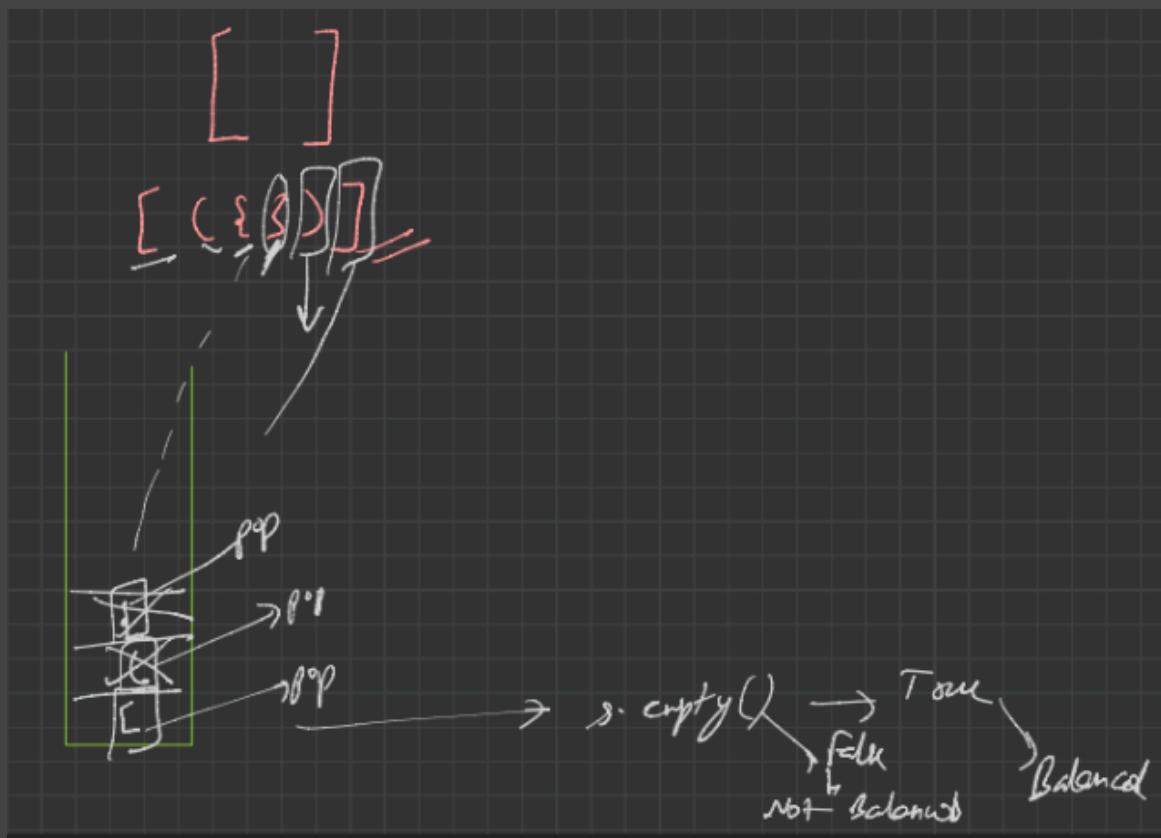
Reverse A String Using Stack:



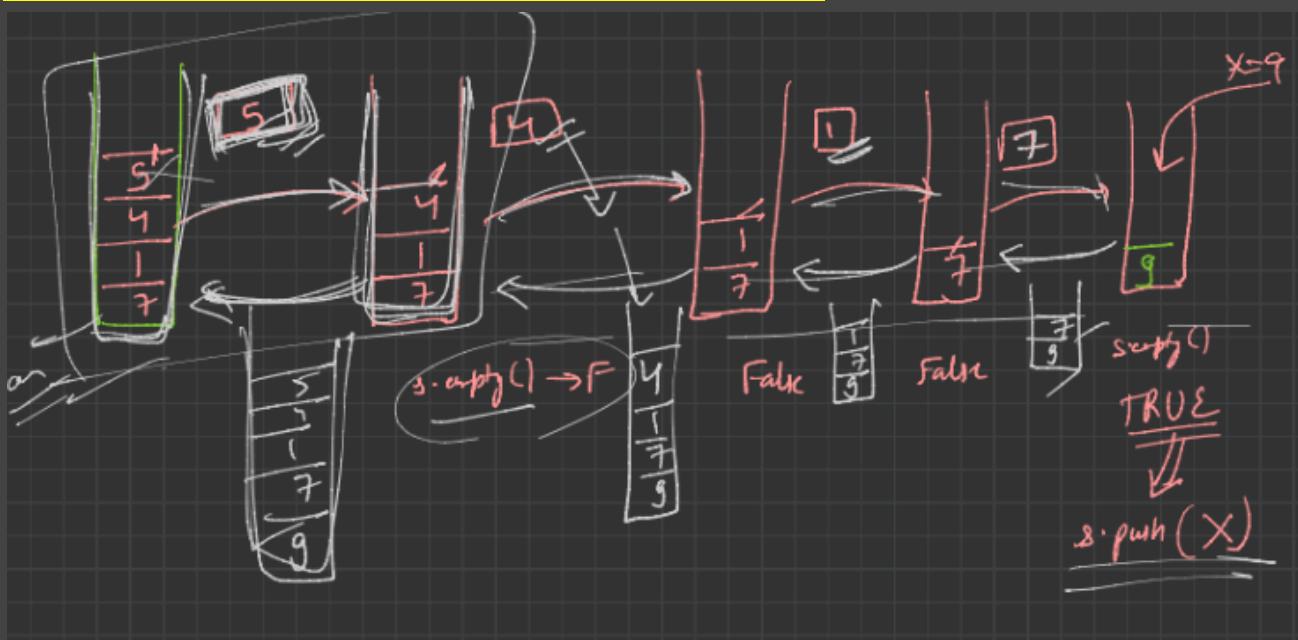
Delete Middle Element In A Stack:



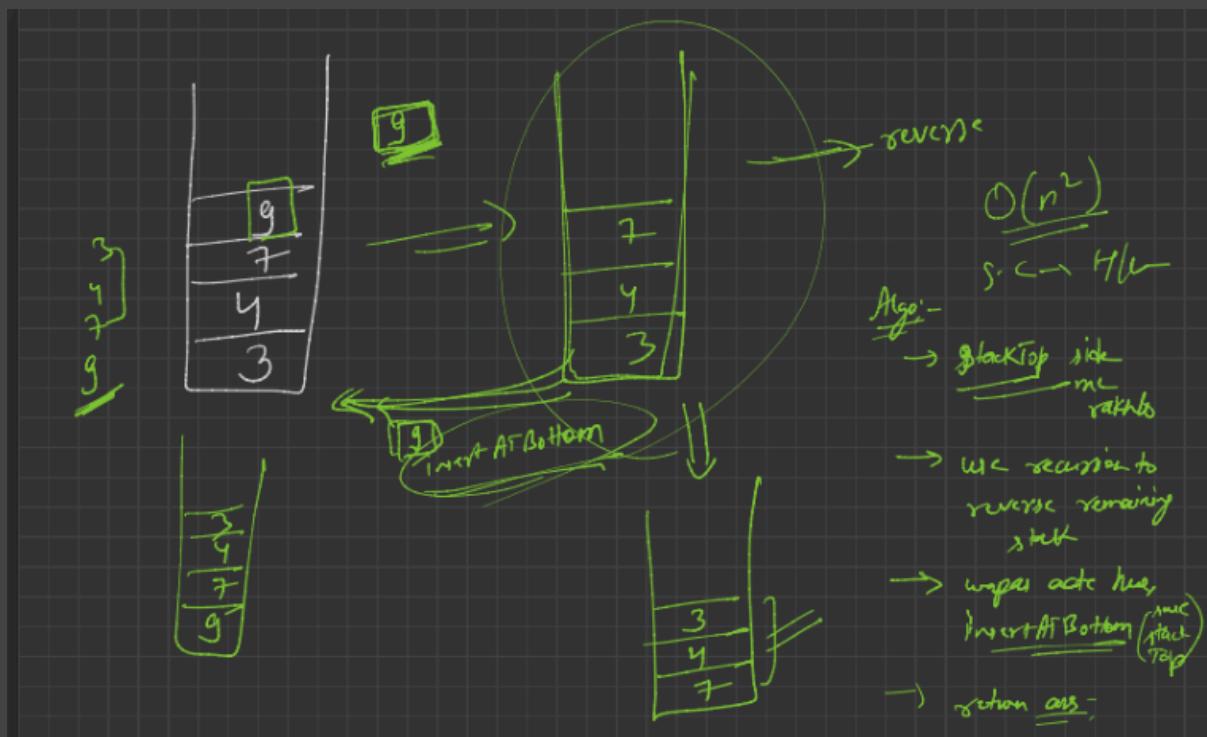
Check Whether the Parenthesis Are Valid:



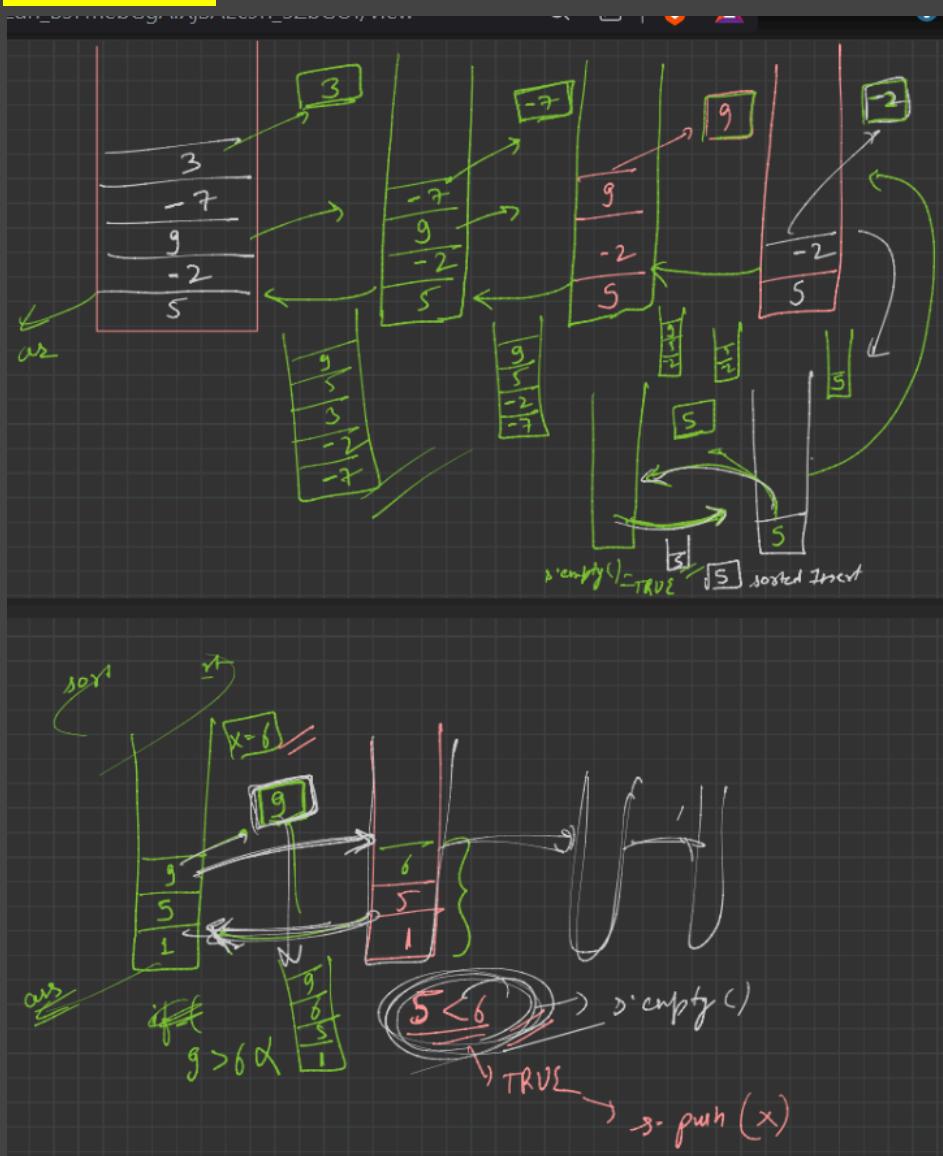
Insert An Element At Its Bottom In A Given Stack:



Reverse A Stack:



Sort A Stack:



Check Whether There Are Redundant Brackets Or Not:

$$\rightarrow \text{ifp} \rightarrow \text{string} = "(\underline{a+b})"$$

Approach:-

for (

 ch = str[i];

 if (ch == '(' || operator)

 stack.push(ch)

else

 if (ch == ')' || lower letter)

 if (ch == stack.top())

stack >:

([a+b])

"C" q + i - 1 push

operator

if ')' → if it is certain in stack
 → open bracket b/w top

jab tak stack me open bracket
nahi milta

stack top check karo

Redundant pair

Found

for operator

Not found

Redundant pair ==

([a+b])

DRY RUN

operator → R.B → Node



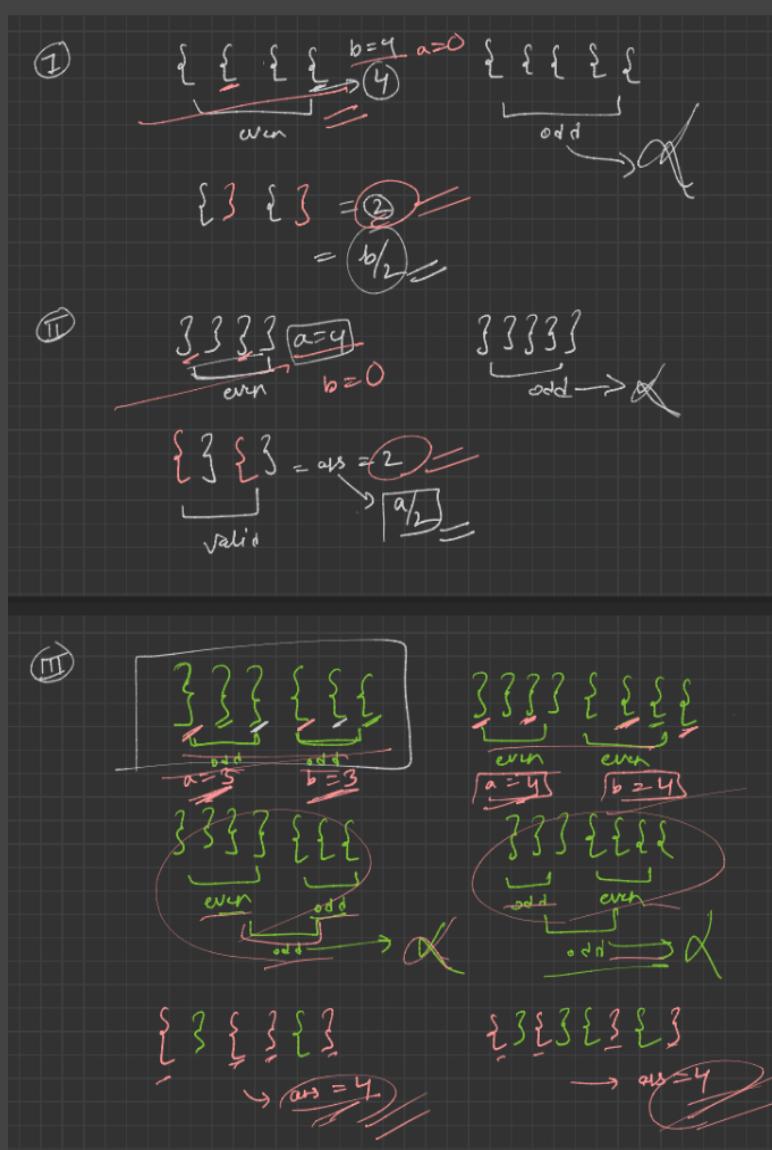
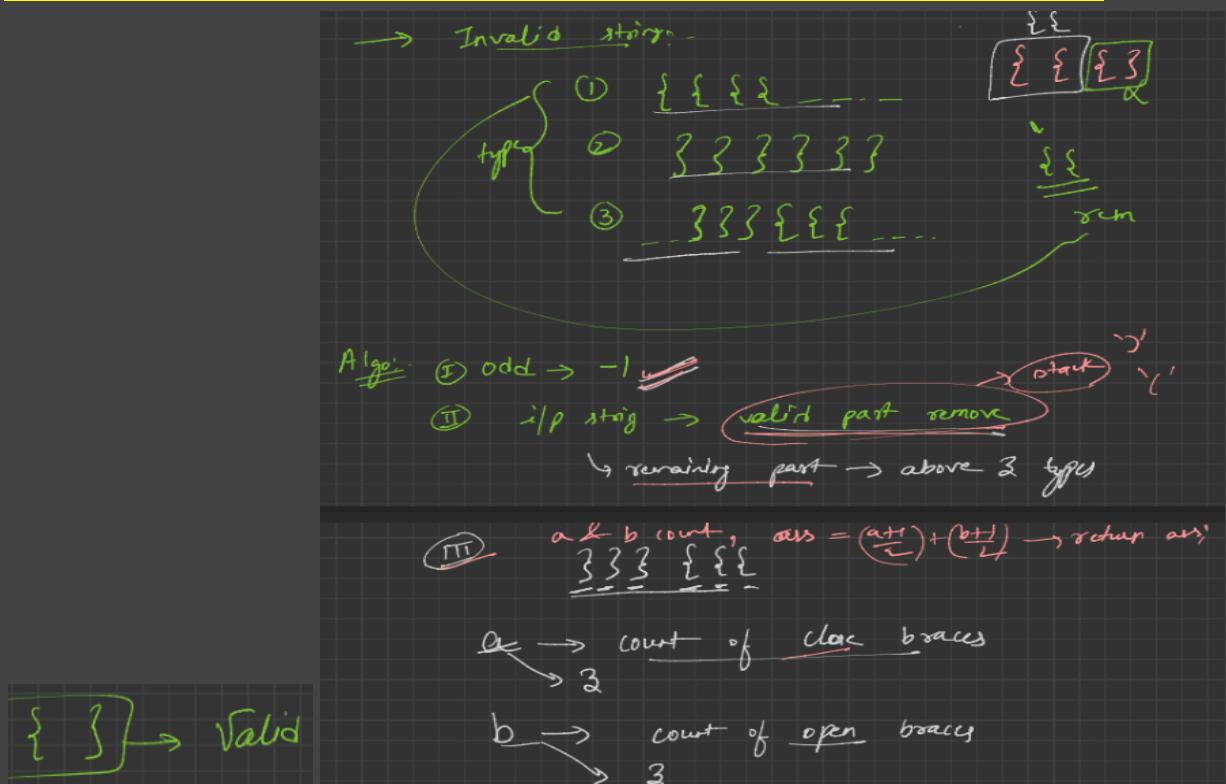
start

)'

operator Not found

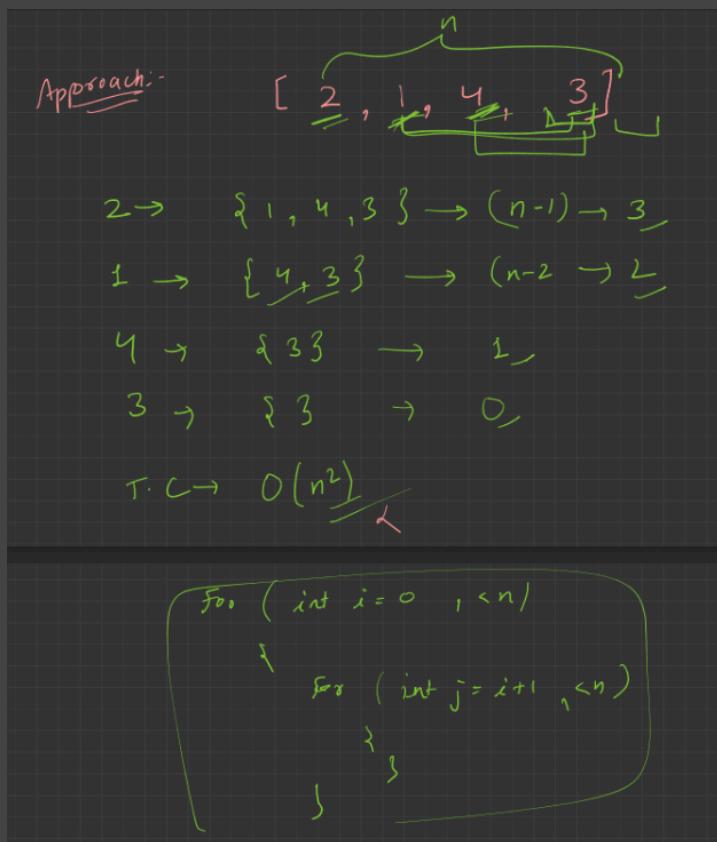
R.B → ↗
return TRUE

Minimum Number Of Operations To Make A Valid Bracket String:

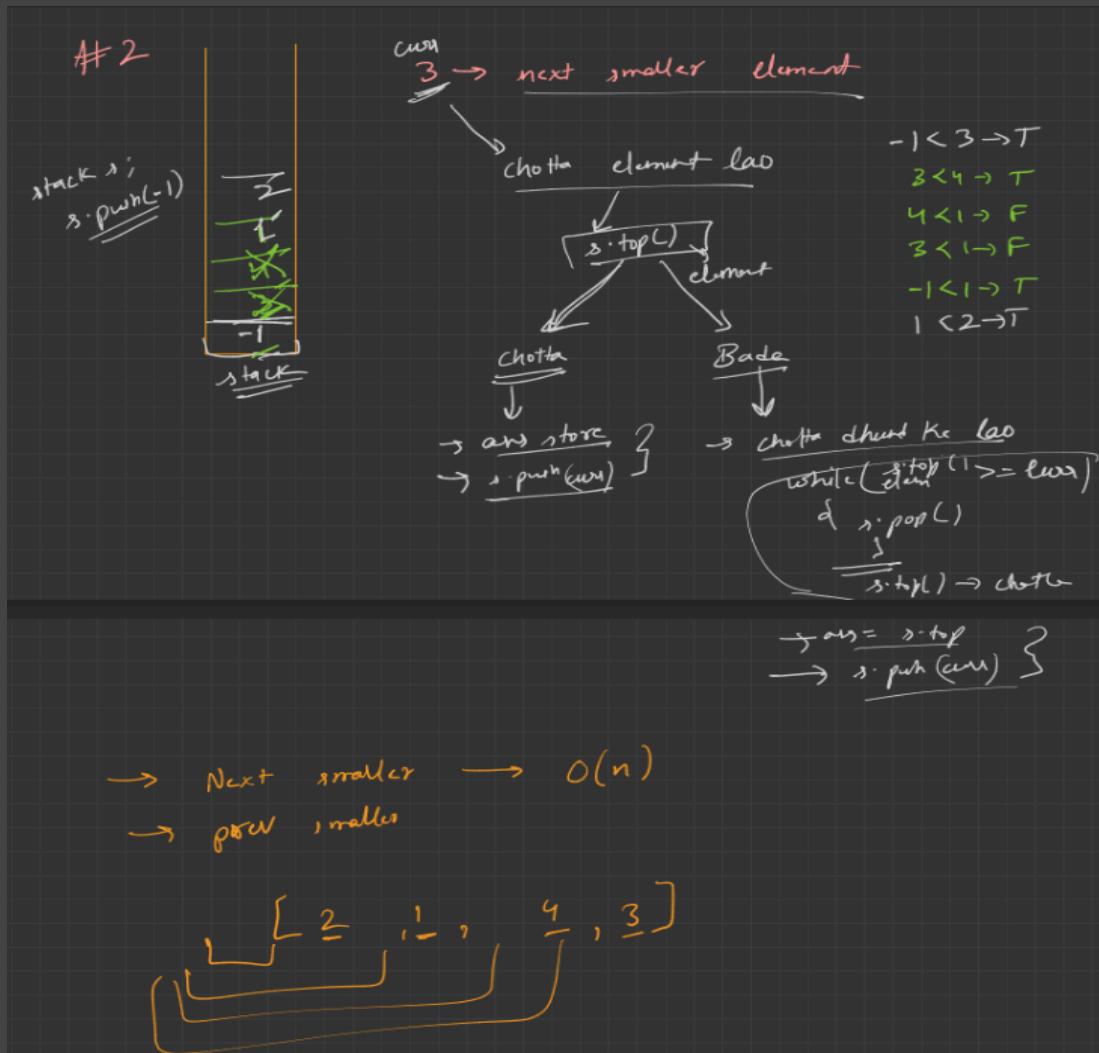


$$\begin{aligned}
 \text{ans} &= \left(\frac{a+1}{2}\right) + \left(\frac{b+1}{2}\right) \\
 &= \frac{0+1}{2} + \frac{4+1}{2} = \frac{5}{2} = 2.5 \\
 &= (4+1) + (0+1) = \frac{5+1}{2} = 3 \\
 &= (3+1) + \left(\frac{3+1}{2}\right) \\
 &= \frac{4}{2} + \frac{4}{2} = 2+2 = 4 \\
 &= \left(\frac{4+1}{2}\right) + \left(\frac{4+1}{2}\right) = \frac{5}{2} + \frac{5}{2} = 2+2 = 4
 \end{aligned}$$

Next Smaller Element Approach-I:



Next Smaller Element Approach-II:

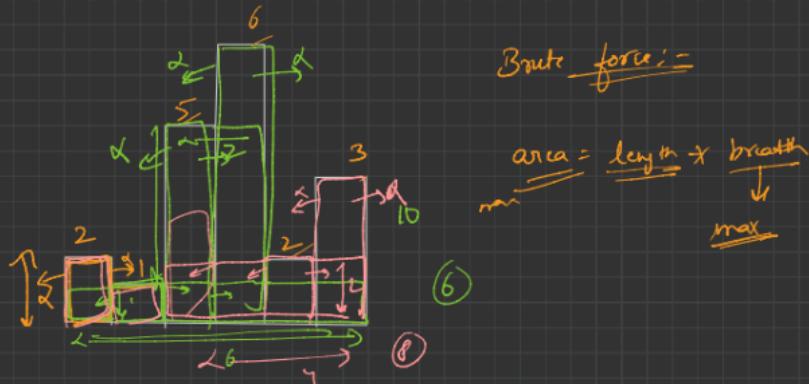


Previous Smaller Element:

If you want to find the previous smaller element for each element in the array, you would need to modify the code to iterate from left to right instead of from right to left.

Largest Rectangle In Histogram Approach-I:

→ Largest Rectangular Area in Histogram



BF

for (int i = 0; i < n; i++)

{

 while (left)

 {

 while (right)

 {

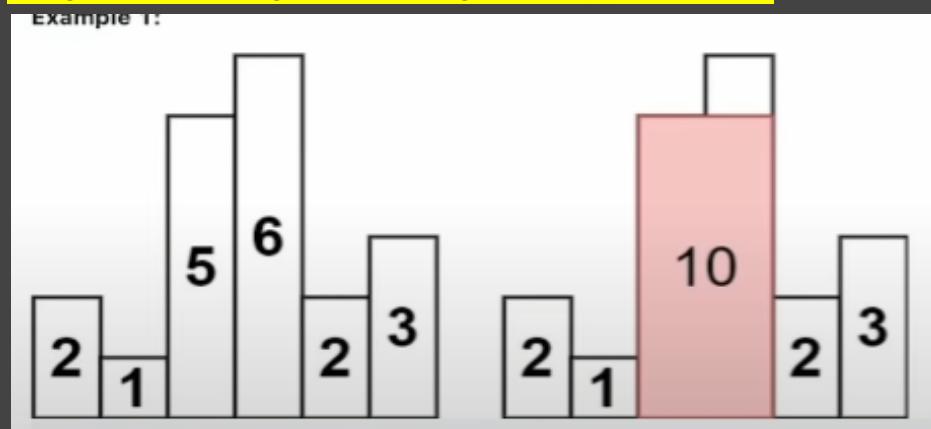
 area = max (area, min (heights));

T-C
 $O(n^2)$

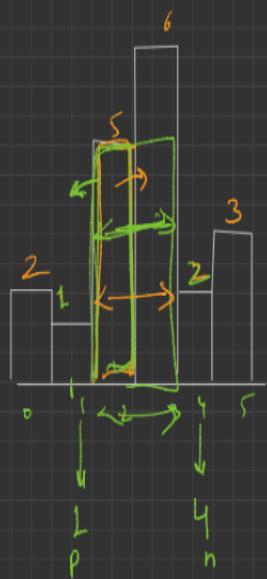
$O(nl)$?

}

Largest Rectangle In Histogram Approach-II:



$O(n)$ → Approach #2

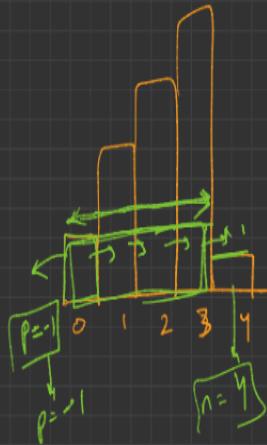


$$\text{width} = \frac{n-p-1}{2}$$

$$\text{area} = \frac{h_1 + h_2}{2} \times \text{width} = 4 - 1 - 1$$

$$= 2$$

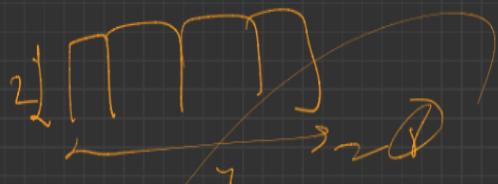
$$\begin{aligned} \text{width} &= \frac{n-p-1}{2} \\ &= \frac{4 - (-1) - 1}{2} - 1 \\ &= 4 - 1 - 1 \\ &= 2 \end{aligned}$$



next → next smaller element index

prev → prev ←

2 2 2 2



$$\begin{aligned} \text{next} &\rightarrow [2, 2, 2, 2] \quad \text{next} \\ &\rightarrow [-1, -1, -1, -1] \\ \text{prev} &\rightarrow [-1, -1, -1, -1] \\ \text{width} &= -1 + 1 = 0 \rightarrow \text{width} = 0 \end{aligned}$$

$$[-1, 2, 2, 2, 2]$$

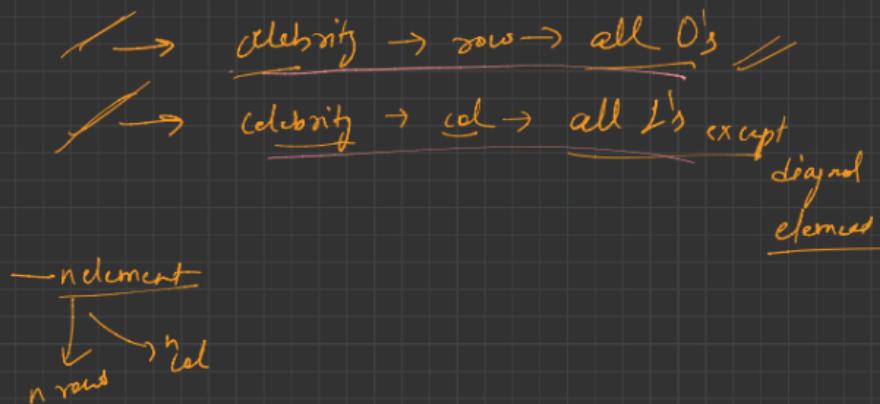
$$\begin{aligned} \text{next} &= -1 \quad -1 \quad -1 \quad -1 \quad \text{if } (\text{mod} = 0 - 1) \\ \text{prev} &= -1 \quad -1 \quad -1 \quad 1 \\ \text{width} &= -1 + 1 = 0 \rightarrow \text{width} = 0 \end{aligned}$$

$$\text{area} = -1 \times 0$$

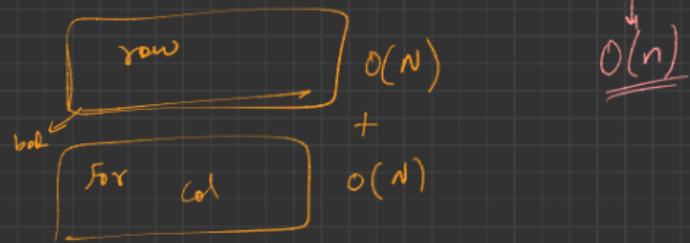
$T.C \rightarrow O(N)$ $S.C \rightarrow O(N)$ More edges

Celebrity Problem Approach-I:

Approach:- Brute force ~~Brute force~~



for (int i = 0 i < n) T.C $\rightarrow \mathcal{O}(n^2)$

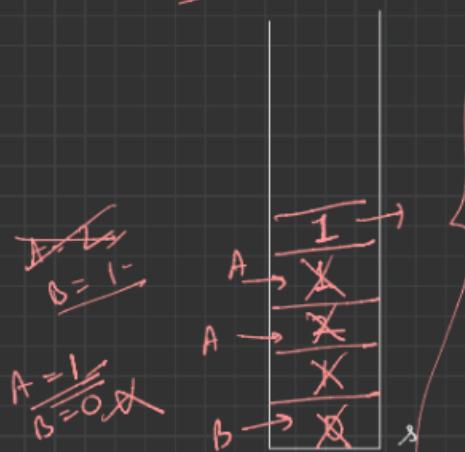


}

if (bool
 | or Not

Celebrity Problem Approach-II:

Approach #2



Algo:-

put all element inside stack

→ jab stack size != 1

→ A → s.top() → s.pop()

→ B → s.top() → s.pop()

→ if (A Knows B)

A → , B → wapas push karo

→ if (B Knows A)

B → , A → wapas add do

→ jo single element bache hua h,

vo ek "Potential Celebrity"

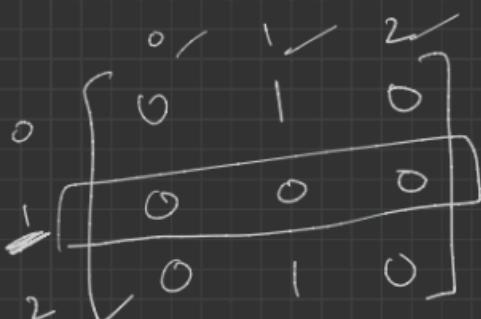
ha skta hai

→ Verify

→ Celebrity knows N.One
→ now check → all O's

Everyone Knows celeb

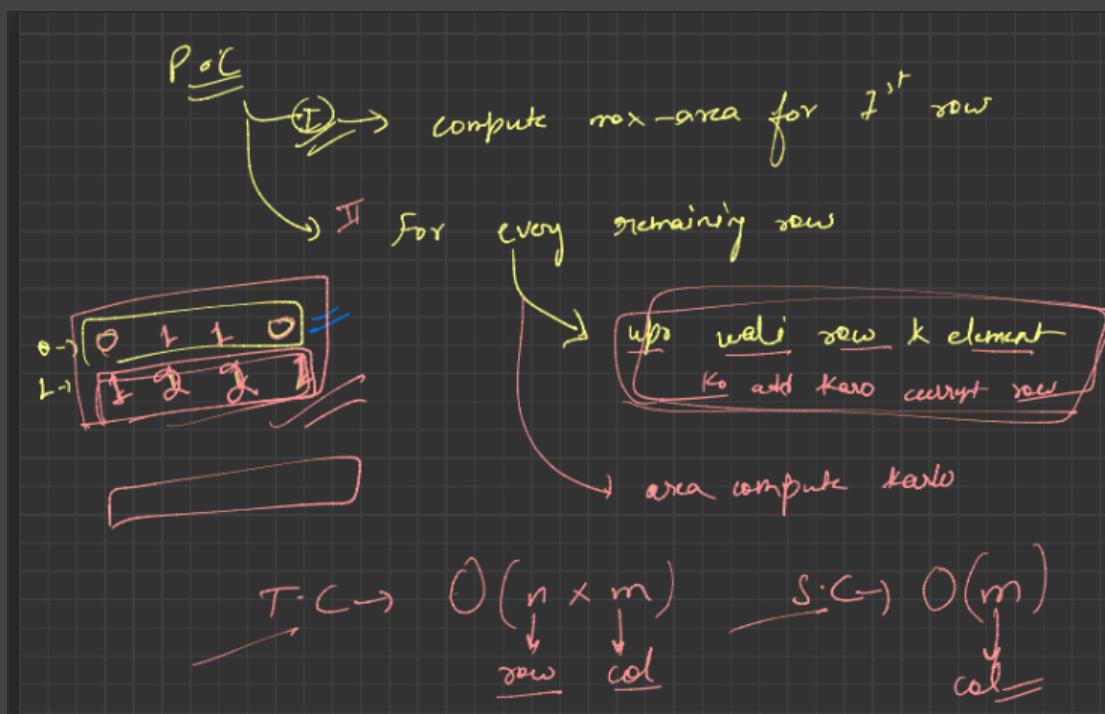
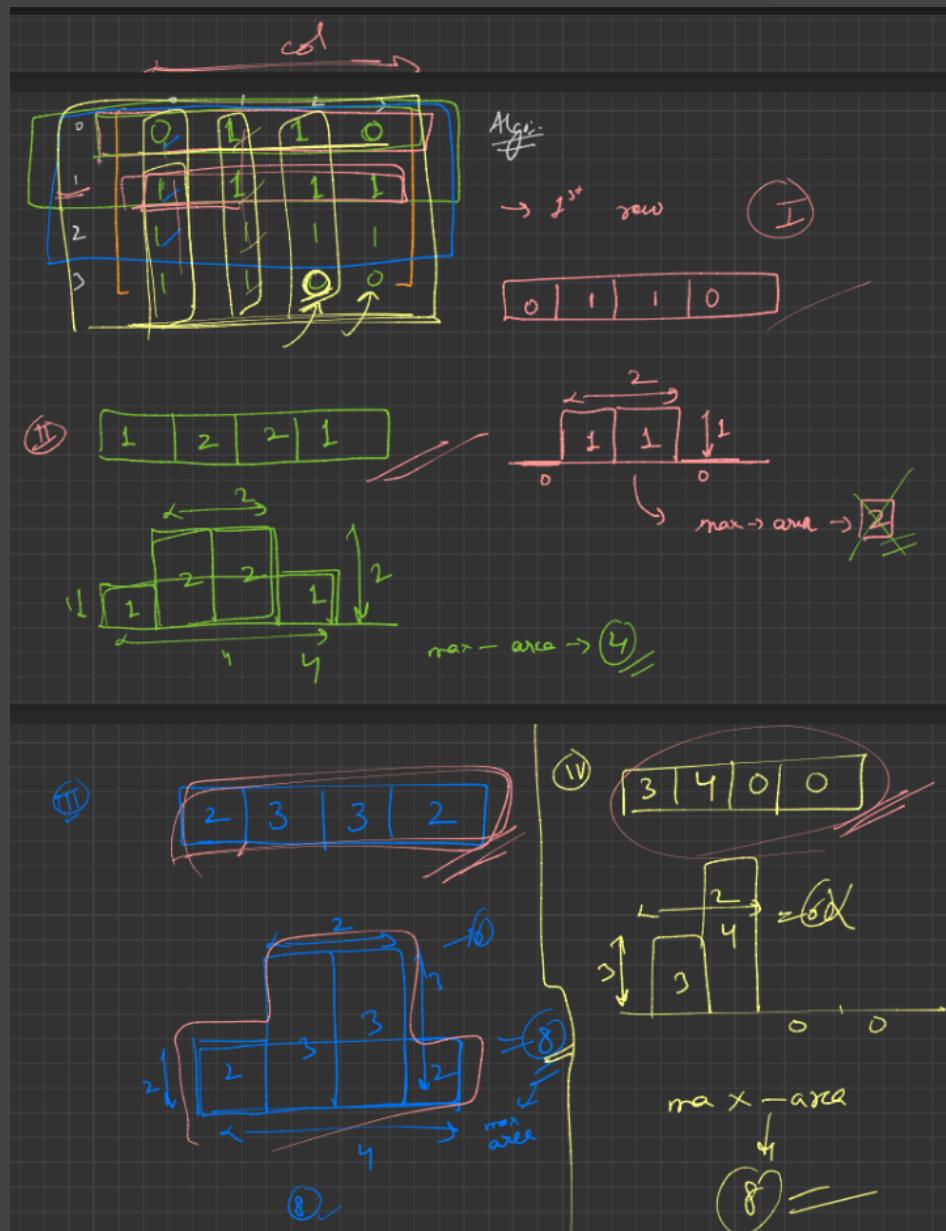
→ col → all 1's
except diagonal
diagonal
direct



T.C → O(N)

H/W → more approaches exploration

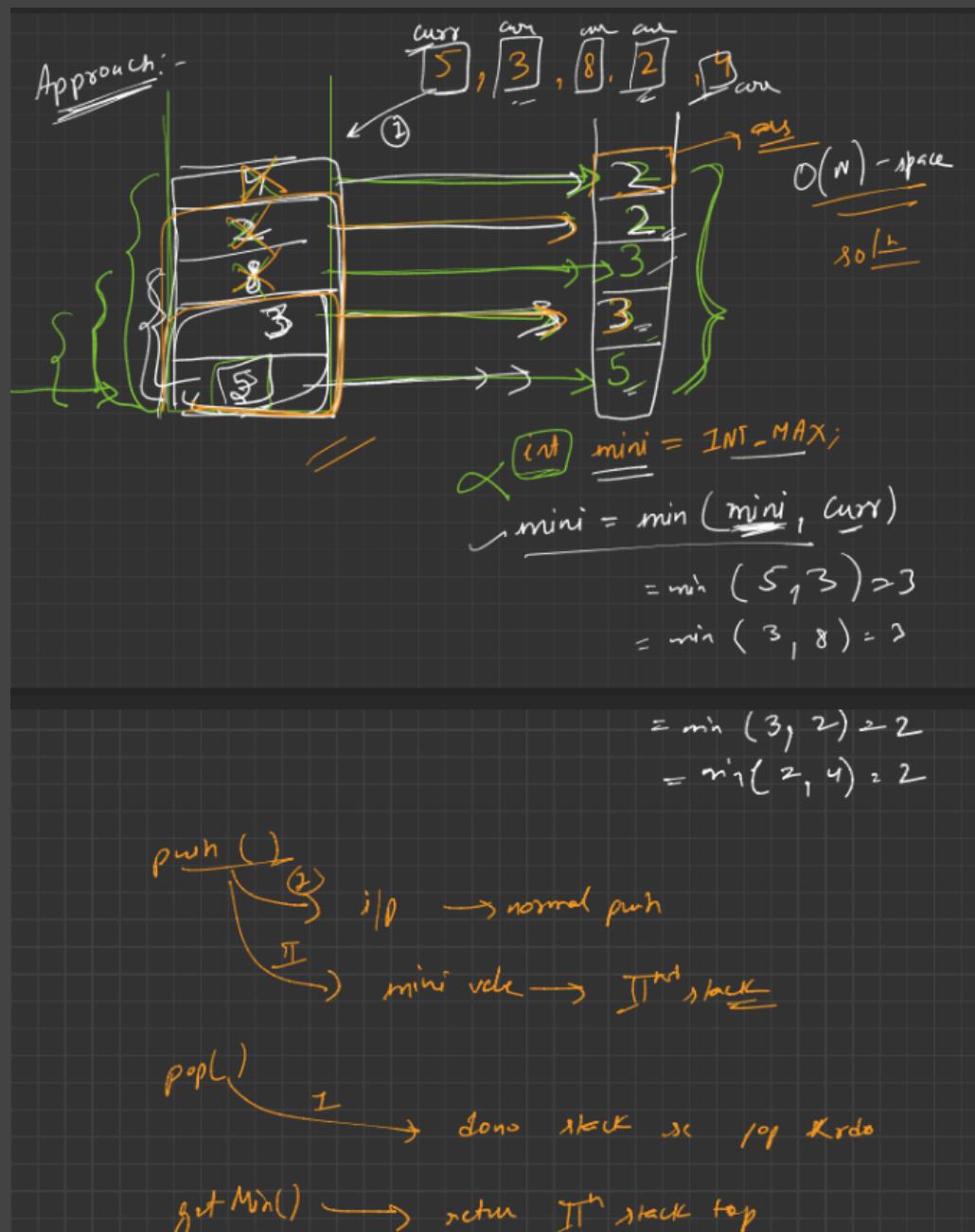
Maximum Rectangle In Binary Matrix:



Design A Stack That Supports getMin in O(1) Time Complexity and O(1) Space

Complexity:

Approach -I:



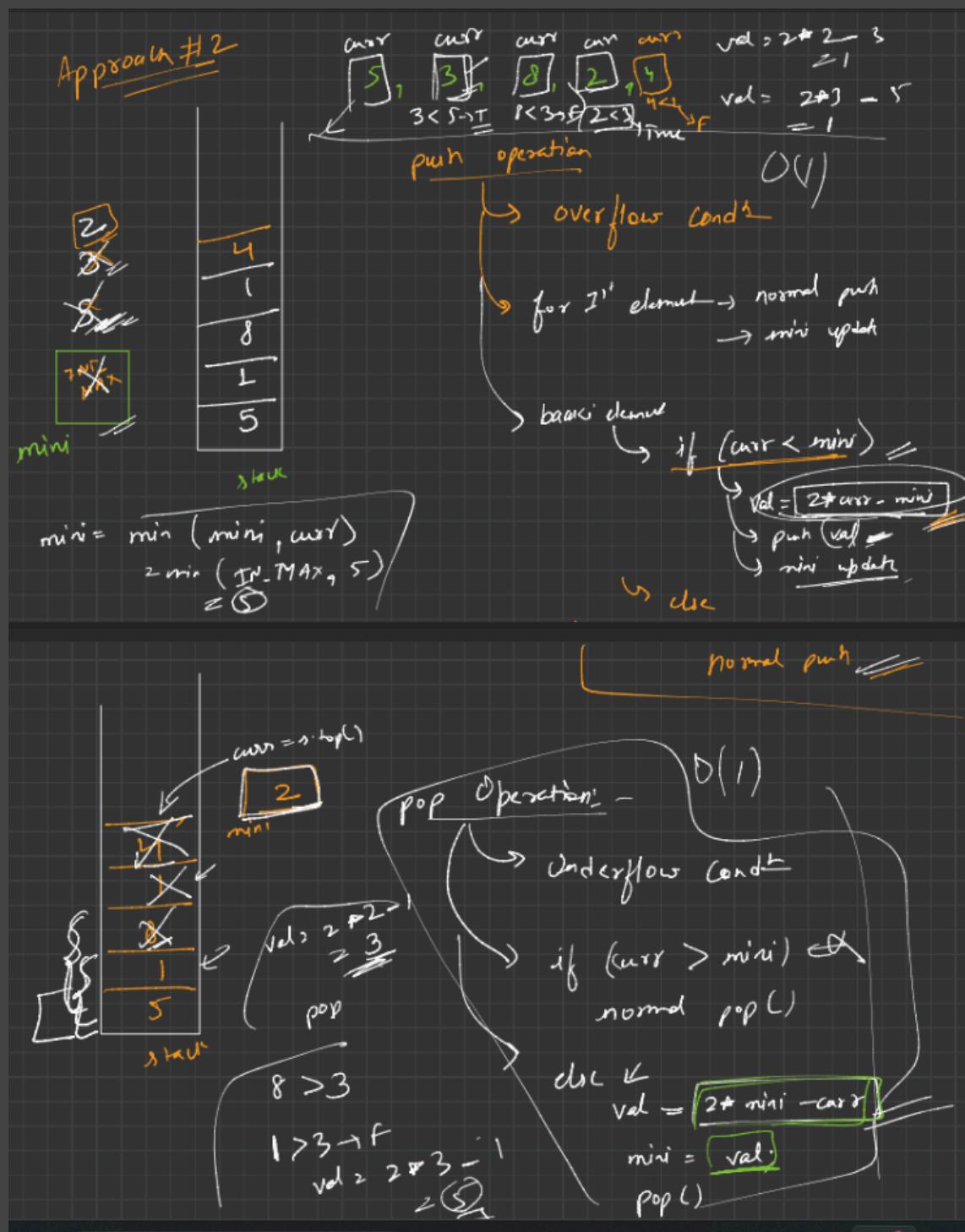
T: $\hookrightarrow \mathcal{O}(1)$

S: $\hookrightarrow \mathcal{O}(N) \rightarrow$ extra stack

Design A Stack That Supports getMin in O(1) Time Complexity and O(1) Space

Complexity:

Approach -II:



The SpecialStack class uses a single stack s to store the elements. The mini variable is used to keep track of the minimum element. When a new element is pushed onto the stack, if it is less than the current minimum, the stack stores a value derived from the new element and the current minimum (specifically, $2 * data - mini$). This derived value is not an additional element, but a transformation of the new element being pushed. Therefore, it does not count as additional space.

When an element is popped from the stack, if it is less than the current minimum, the minimum is updated using the derived value and the current minimum (specifically, $2 * mini - curr$). Again, this does not use additional space, as it's a calculation performed on existing values.

getMin() $O(1)$

min → stored
return

push → $2 * \text{curr} - \text{mini}$

pop() → $2 * \text{mini} - \text{curr}$

curr minimum
prev minimum

push

$3 < 5 \rightarrow \text{val} = \boxed{2 * \text{curr} - \text{mini}}$
 $= 2 * 3 - 1 = 5$

$2 * \text{curr} - \text{mini}$
 $= 2 * 3 - 1$

$\boxed{2 * n - \text{prevMinimum}}$
 $\boxed{\text{mini} \rightarrow n}$

pop()

pop()

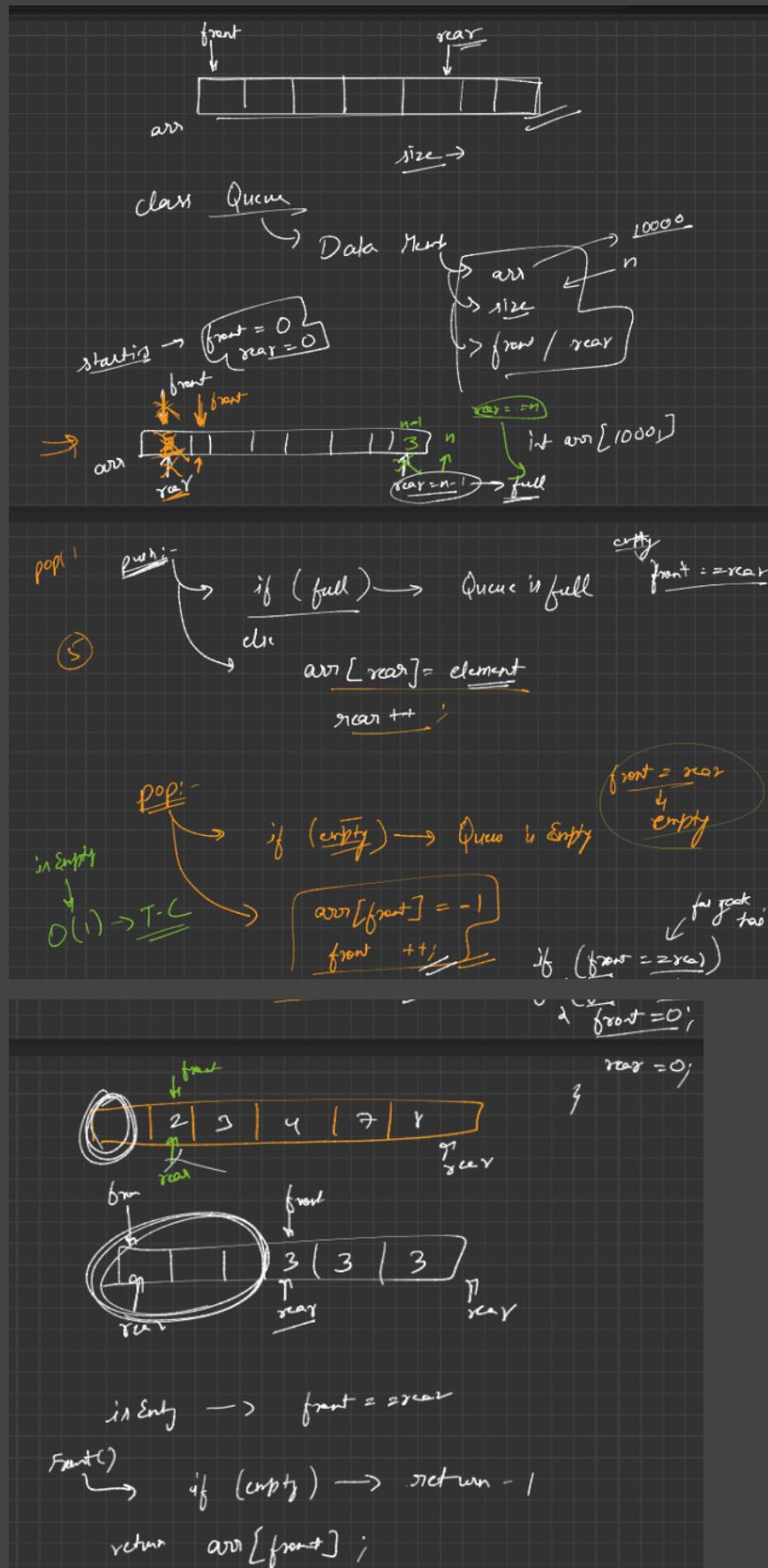
$2 * \text{mini} - \text{curr}$
 $2 * 5 - 1$

$2 * n - \text{curr}$
 $2 * 5 - (2 * 1 - \text{prevMin})$

$\boxed{\text{prev Minimum}}$

Queue

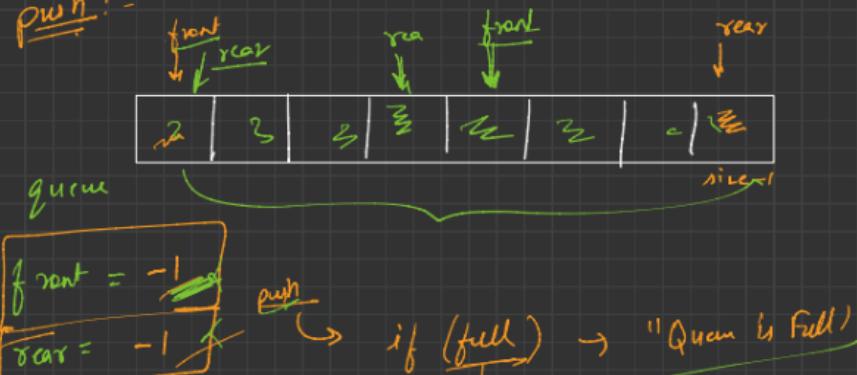
Implementing Queue Using Arrays:



Implementing Queue Using Linked-List:

Circular Queue:

push:



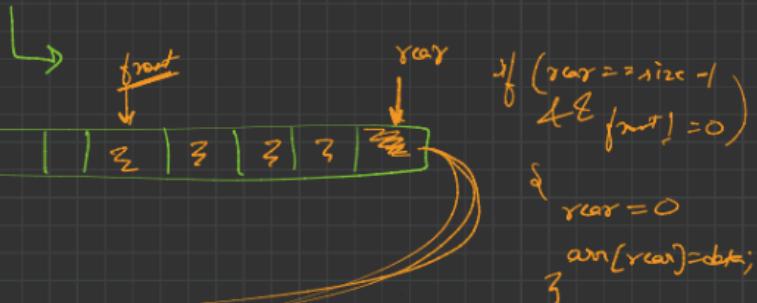
$$\left\{ \begin{array}{l} (\text{front} == 0 \text{ AND } \text{rear} == \text{size} - 1) \\ \text{or} \\ \text{rear} = (\text{front} - 1) \% (\text{size} - 1) \end{array} \right.$$

↳ if ($\text{front} == -1$) // first element

{
 $\text{front} = \text{rear} = 0$!

 arr[queue] = data;

}

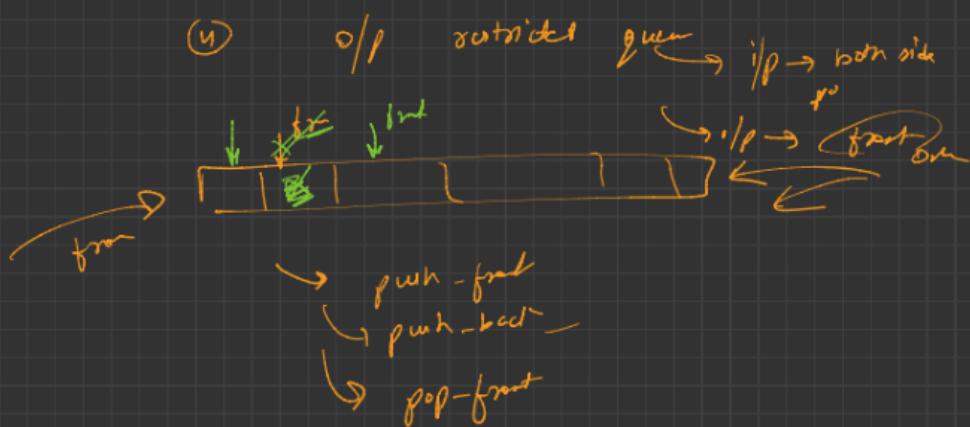
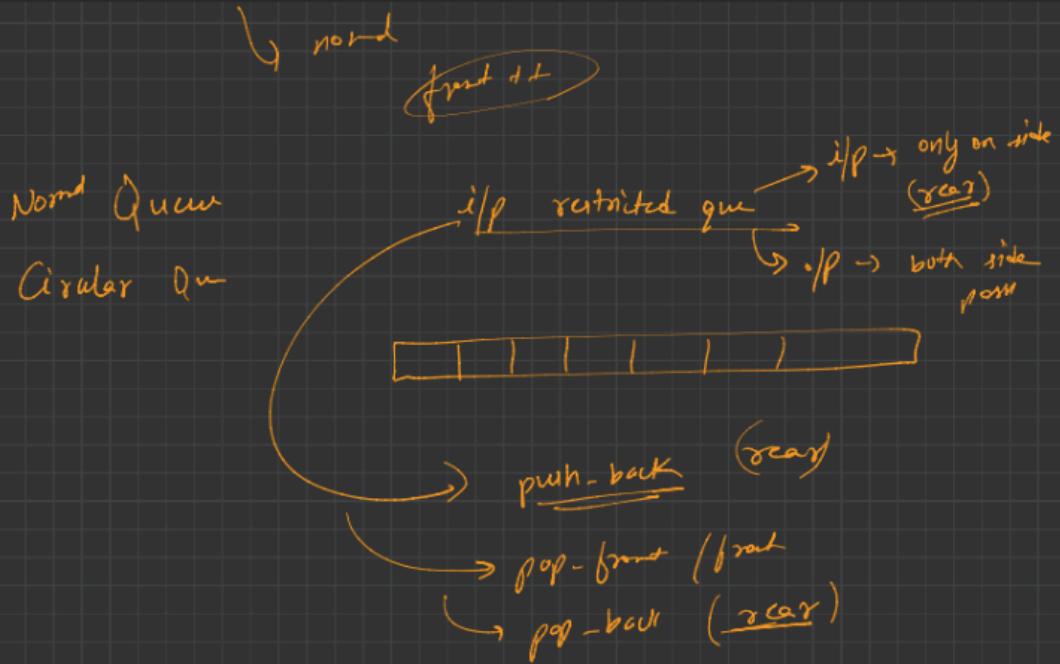


else

$\text{rear} + 1$

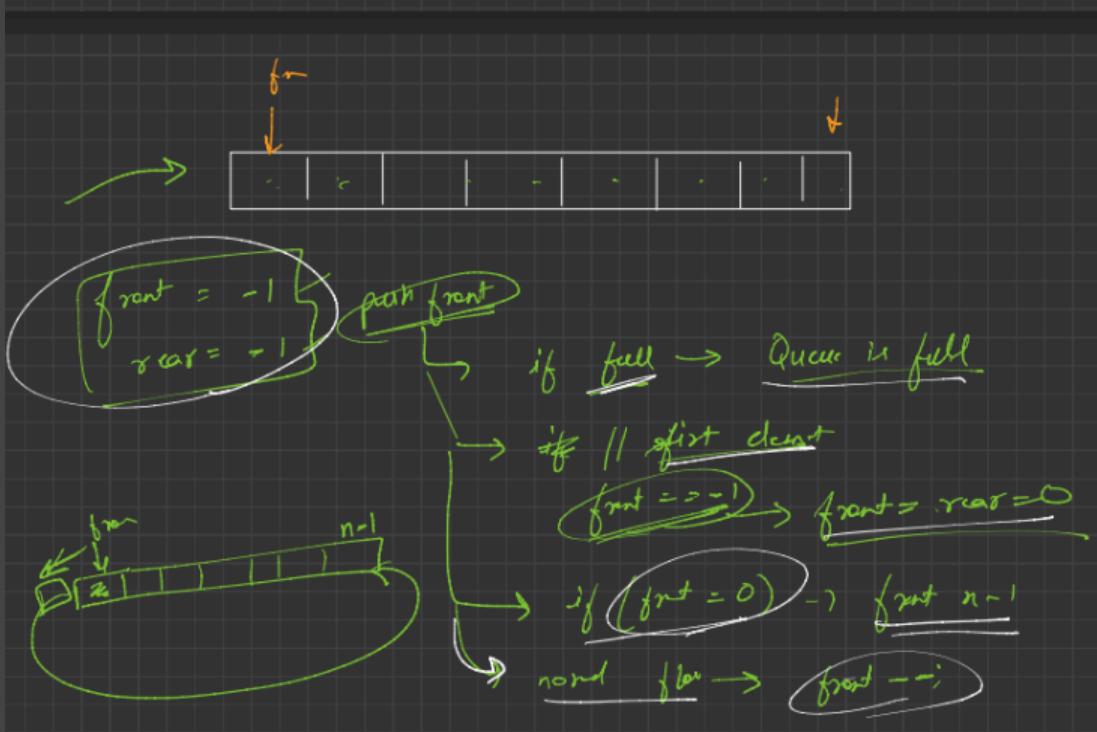
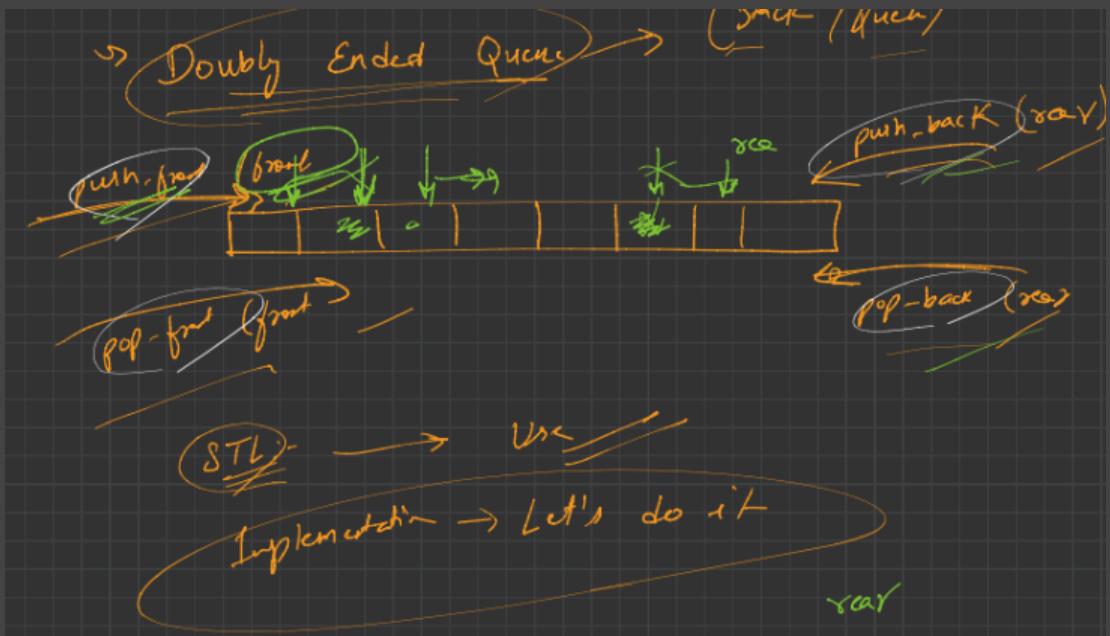
 arr[rear] = data;

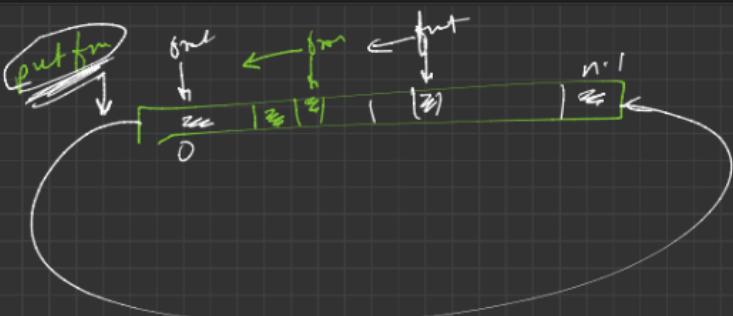
Input Restricted And Output Restricted Queue:



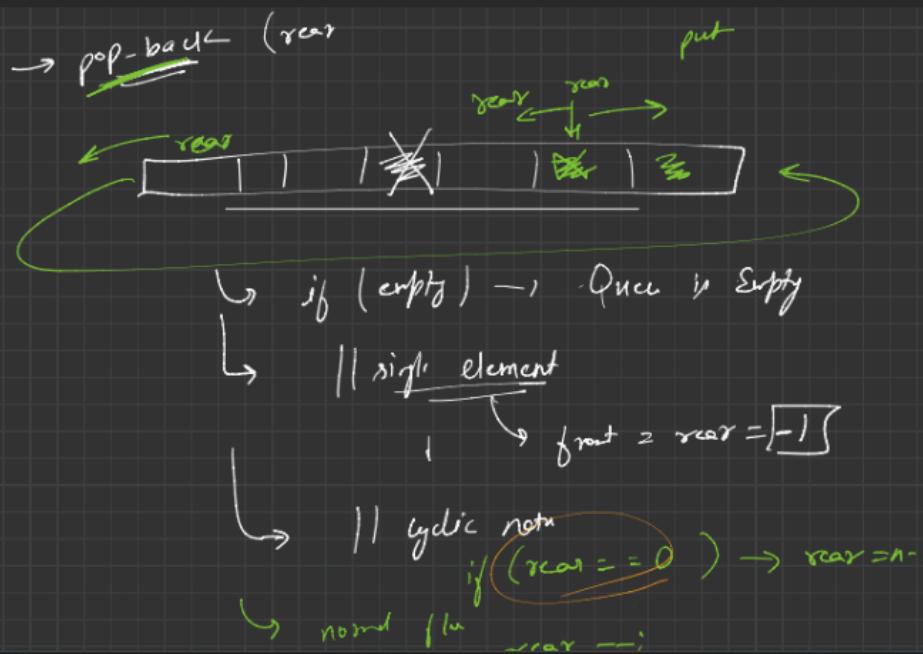
Doubly Ended Queue(Deque) STL Code:

Doubly Ended Queue(Deque) Implementation:

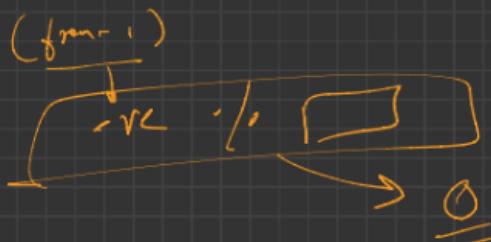




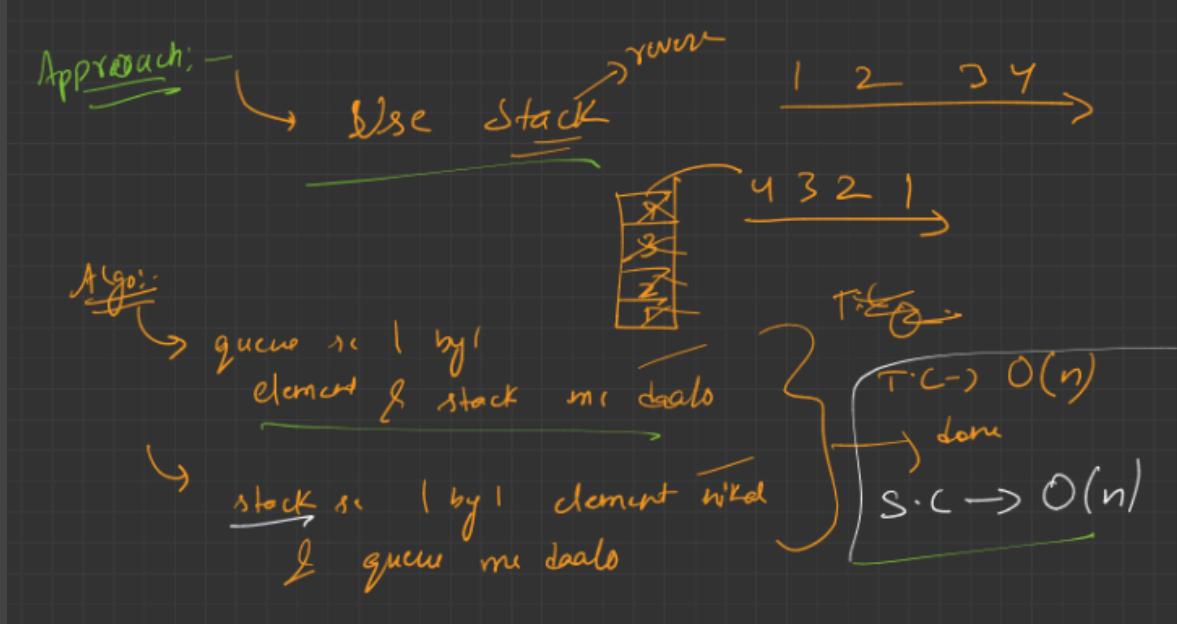
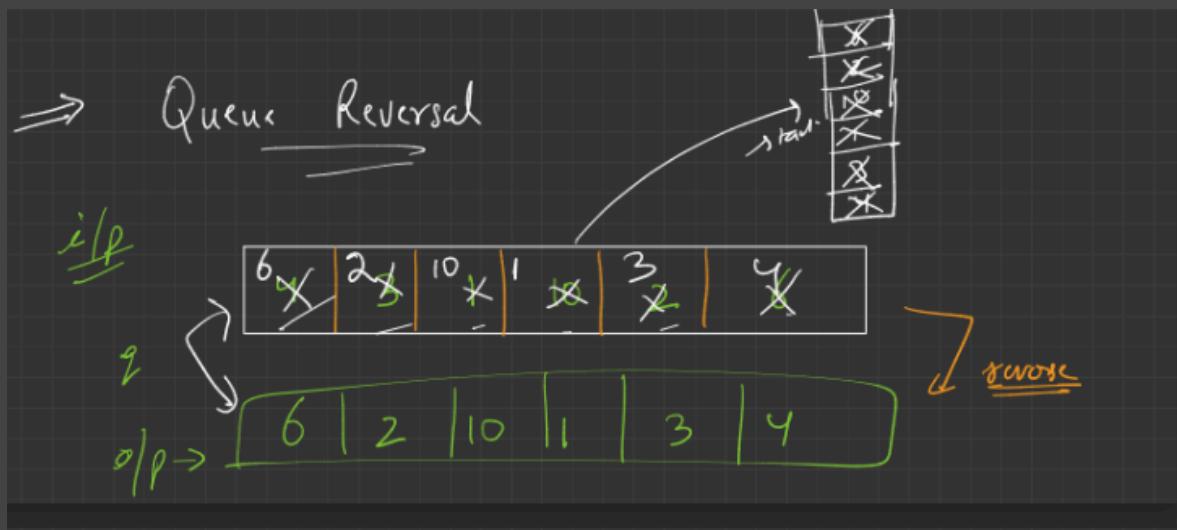
push rear → 8
rear → num →
→ pop front
→ pop-back



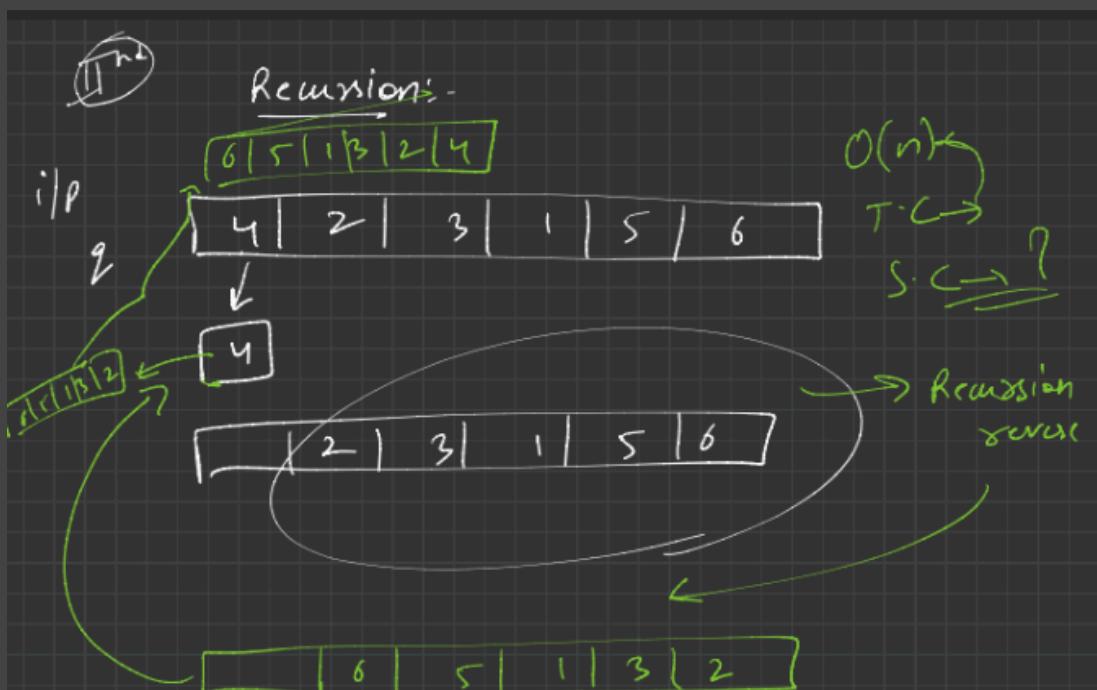
$$\text{front} = 0$$



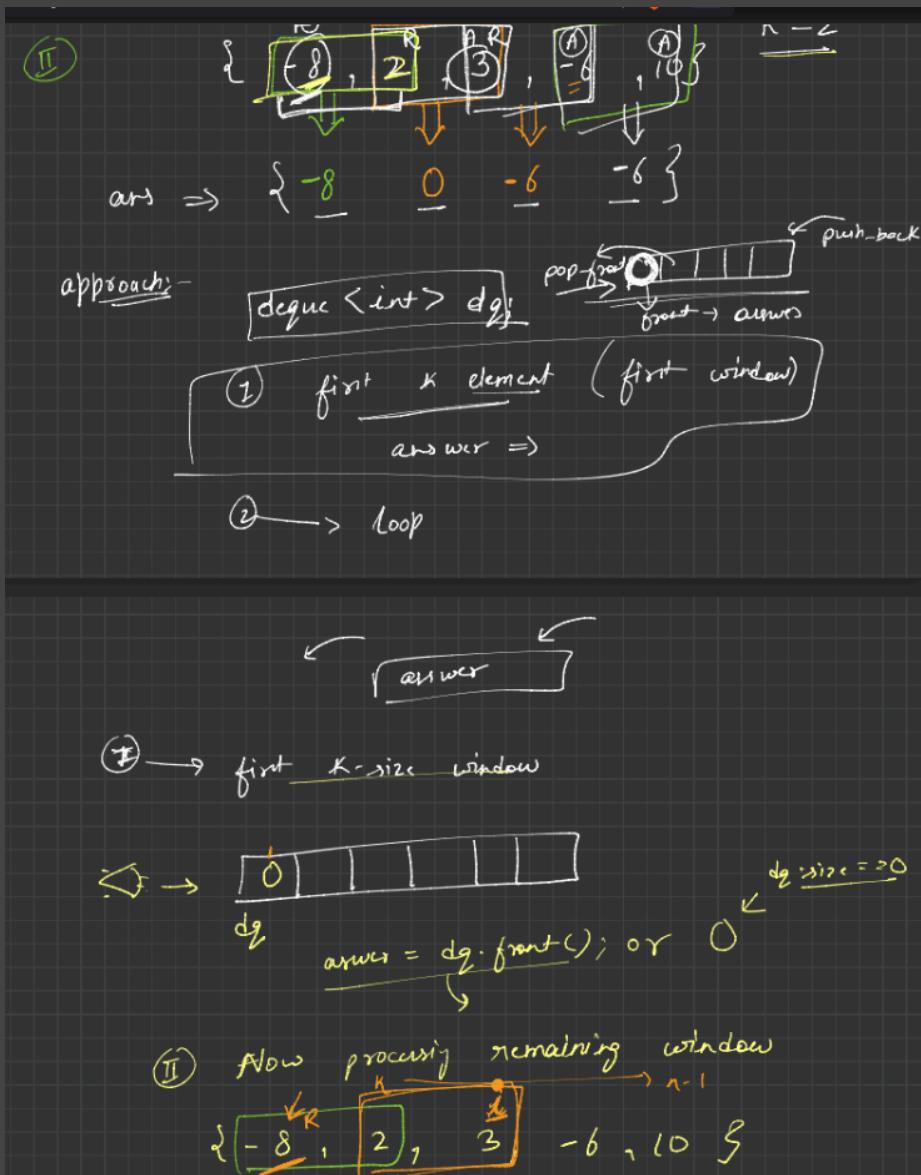
Reverse A Queue Approach-I:



Reverse A Queue Approach-II:

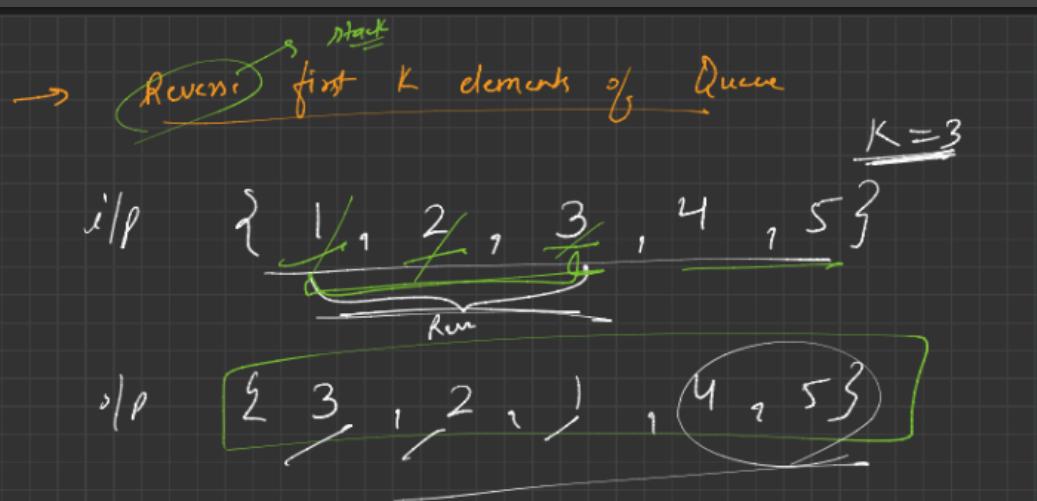


First Negative Integer In Every Window Of Size K:

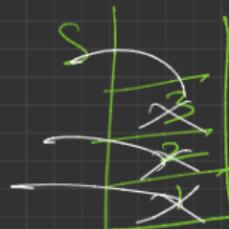
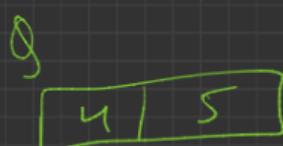


// Removal
 for ($i \rightarrow n$)
 {
 // Removal
 if ($\text{dq.front() - i} \geq k$)
 dq.pop_front();
 // addition
 if ($\text{arr}[i] < 0$)
 $\text{dq.push_back}(i);$
 $\text{ans} \xrightarrow{\text{dq.size} > 0} \text{ans} \rightarrow \text{dq.front}$
 size=0
 0
 }

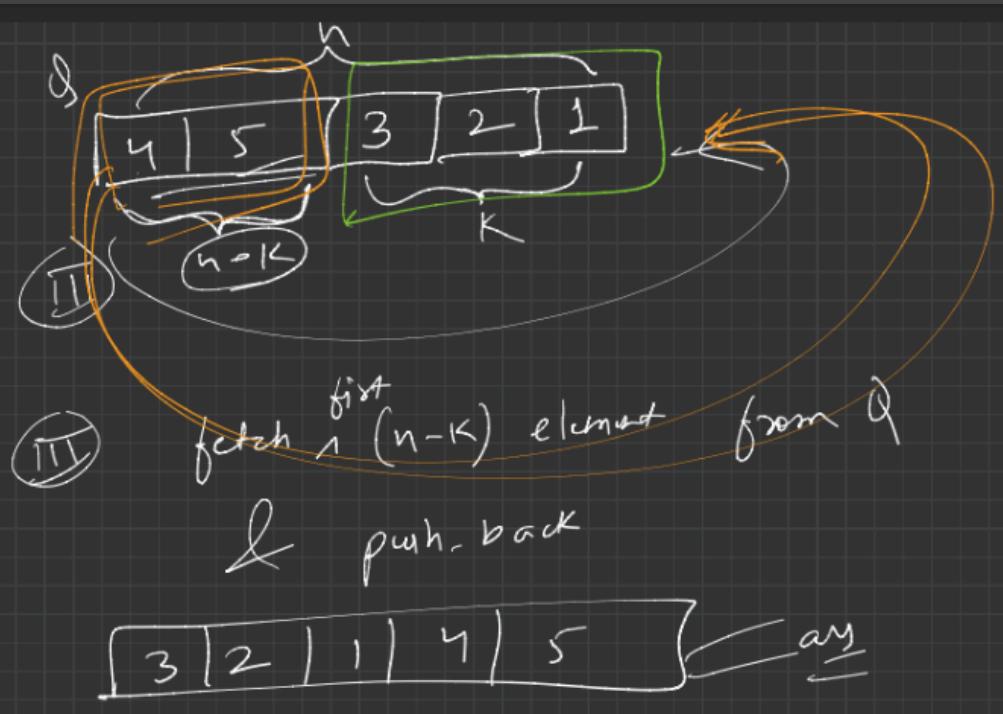
Reverse First K Elements In A Queue:



Algo:- (I) fetch first K element from Q
 ↳ put into stack

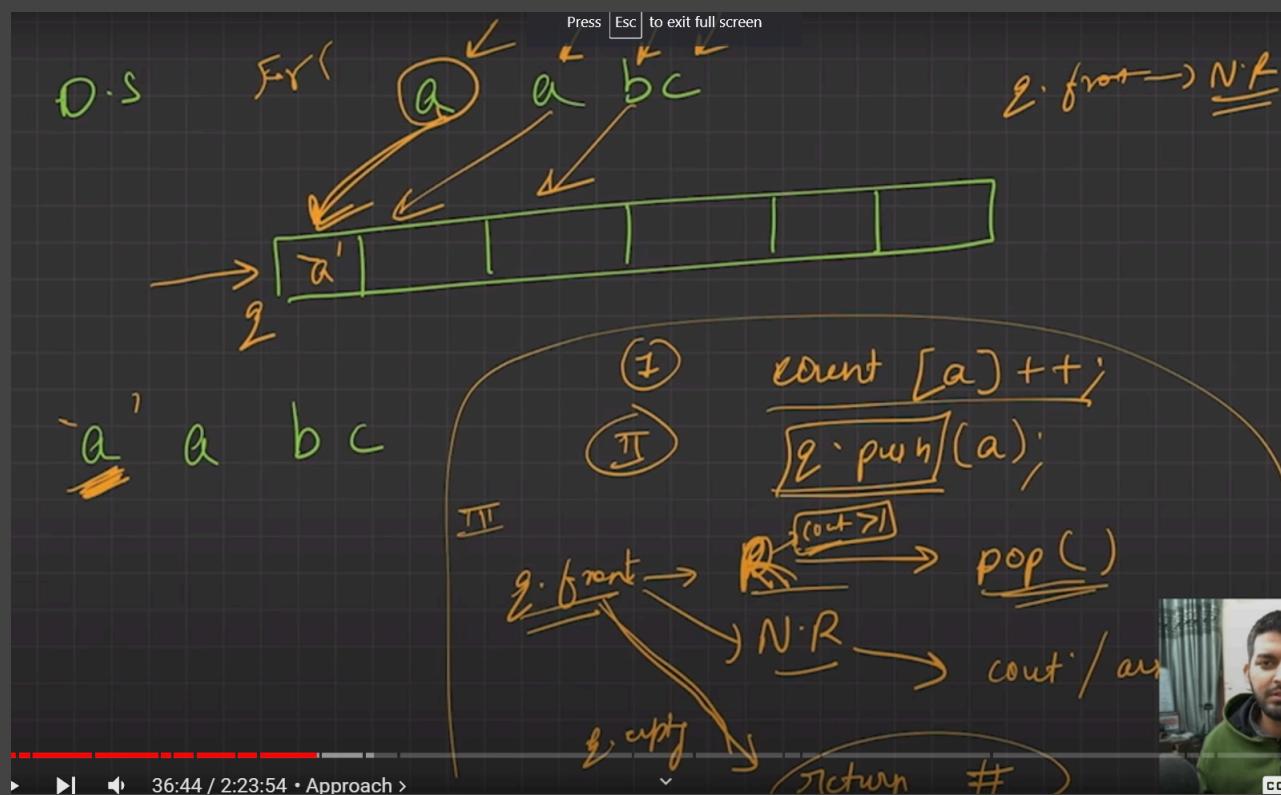
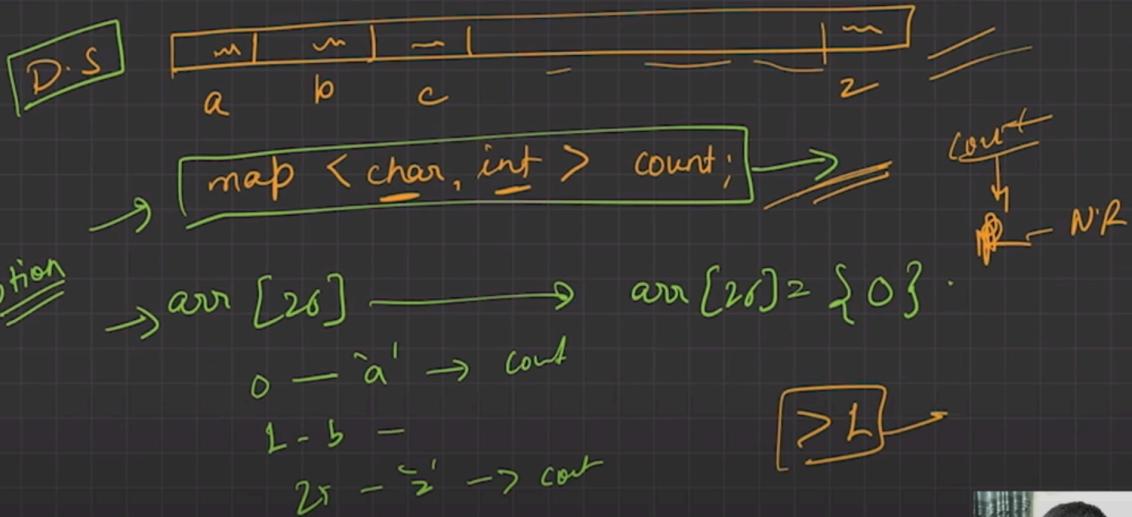


(II) fetch element from stack
 ↳ put into Q



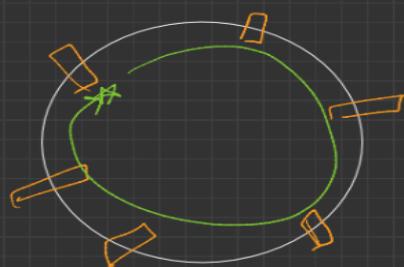
First Non-Repeating Character In A Stream:

Approach:-



Circular Tour:

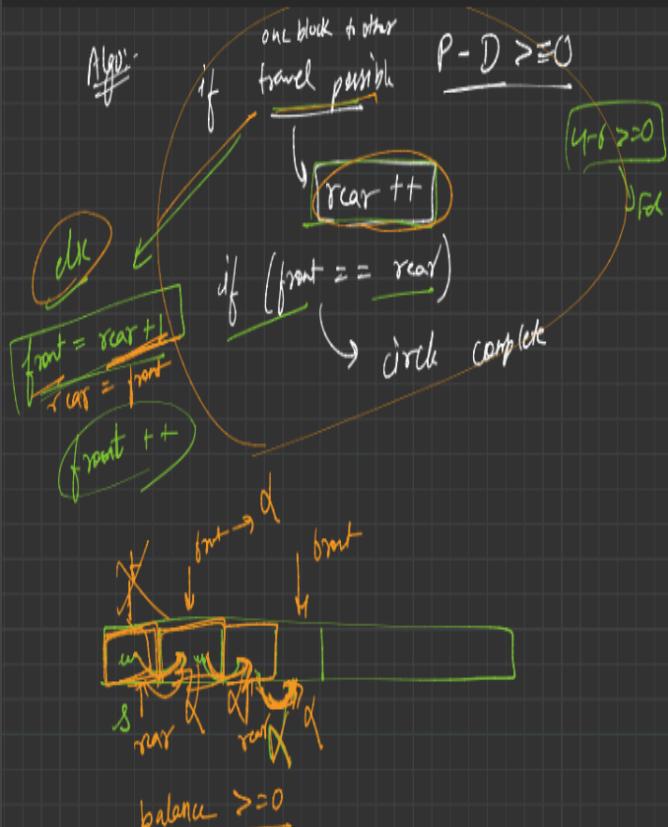
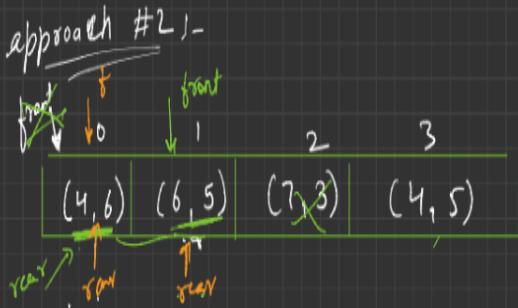
→ Circular tour:



P-P → Patrol data (x km)

→ mean P-P distance (y km)

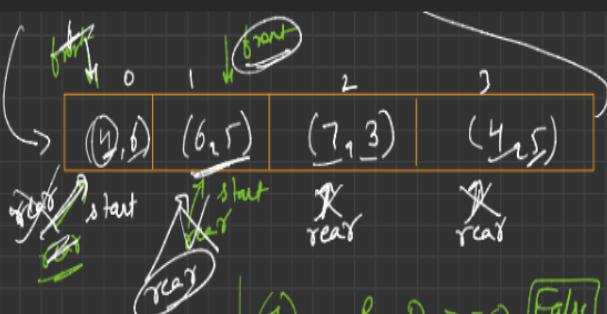
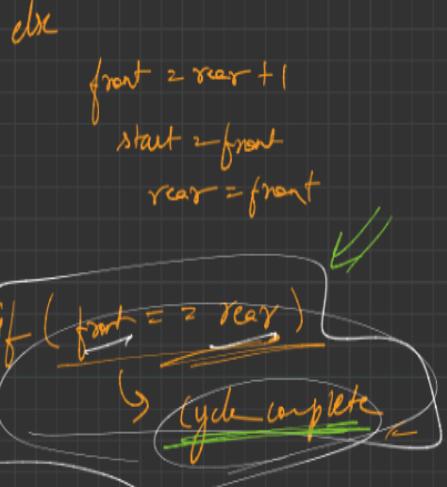
approach #1 - B.F

$$\rightarrow O(n^2)$$


Algorithm

start block to block

if (travel possible) \rightarrow rear++



(I) $P-D \geq 0$ [False]

$$4-6 = -2 < 0$$

$front = rear + 1$

(II) $P-D \geq 0$ [True]

$$8-5 = 3 \geq 0$$

$balance = 4$

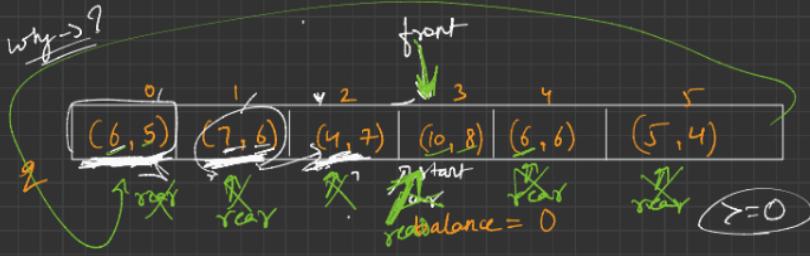
$balance = 1+7-8-3 = 5-8 = -3 \Rightarrow \text{False}$

$balance = 5+4 = 9-5$

$$= 4 \geq 0 \Rightarrow \text{True}$$

$balance = 4+4-6$

$$= 8-6 = 2 \geq 0 \Rightarrow \text{True}$$



\Rightarrow front $\leftarrow \alpha$

$$\begin{aligned} \text{balance} &= (\cancel{\text{balance}}) + p - 1 \\ &= 0 + 6 - 5 = 1 \geq 0 \rightarrow \text{TRUE} \end{aligned}$$

$$\boxed{\text{front} = \text{rear} + 1}$$

$$\begin{aligned} \text{balance} &= \cancel{1} + 7 - 6 \\ &= 8 - 6 = 2 \geq 0 \rightarrow \text{TRUE} \end{aligned}$$

$$\begin{aligned} \text{balance} &= \cancel{2} + 4 - 7 \\ &= 6 - 7 = \cancel{(-1)} \geq 0 \rightarrow \text{False} \end{aligned}$$

Want last
Block \rightarrow 2 visit
single visit

$$\begin{aligned} \text{balance} &= 0 \\ \text{balance} &= 0 + 10 - 8 \\ &\Rightarrow 2 \geq 0 \rightarrow \text{TRUE} \end{aligned}$$

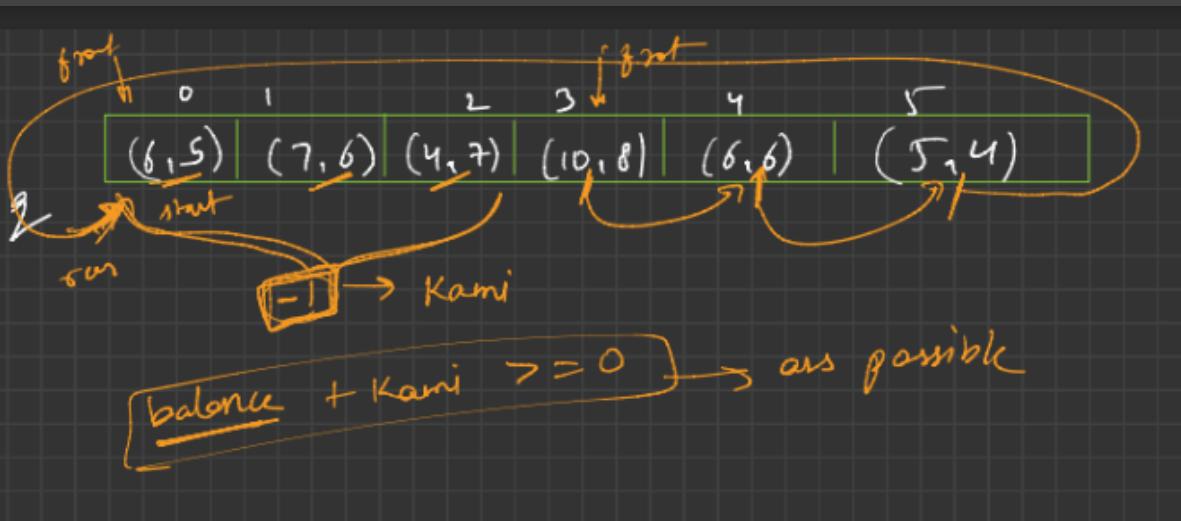
$$\begin{aligned} \text{balance} &= 2 + 8 - \cancel{6} \\ &= 2 \cancel{(2)} \geq 0 \rightarrow \text{TRUE} \end{aligned}$$

$$\begin{aligned} &= 2 + 5 - 7 \\ &= 7 - 4 \\ &= 3 \geq 0 \rightarrow \text{TRUE} \\ &\begin{aligned} &= 3 + 6 - 5 \\ &= 9 - 5 = 4 \geq 0 \rightarrow \text{TRUE} \end{aligned} \end{aligned}$$

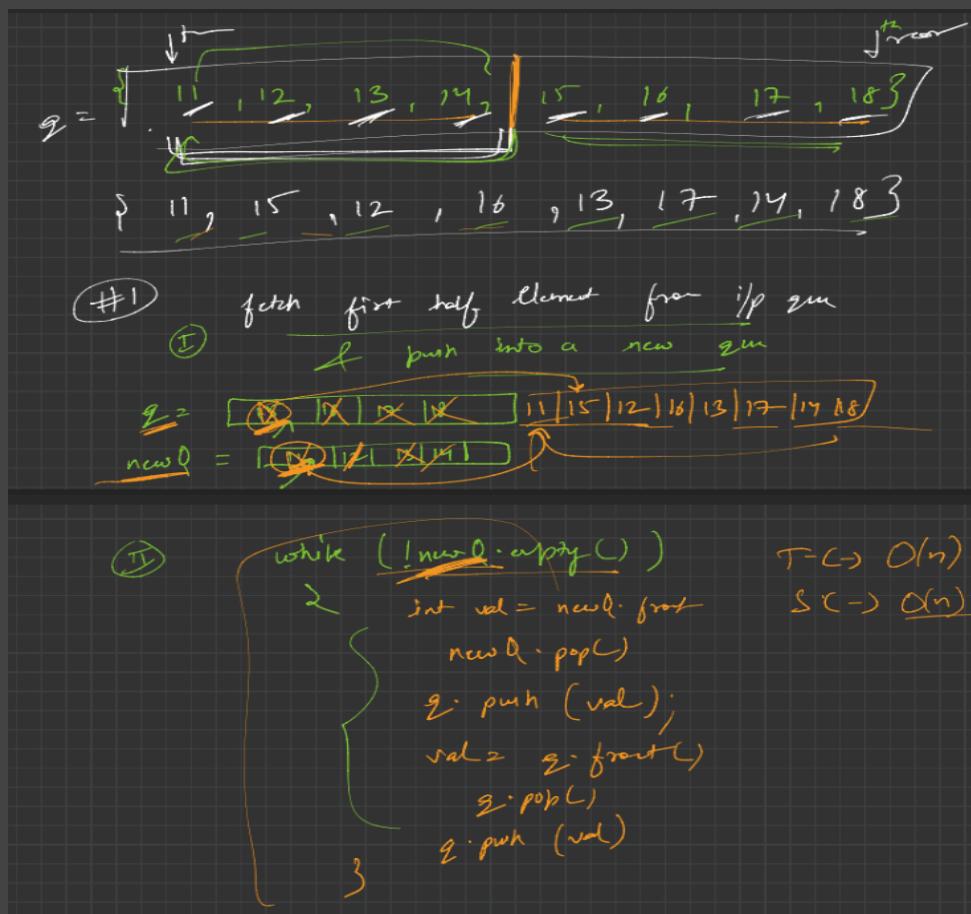
$$\begin{aligned} &= 3 + 6 - 5 \\ &= 9 - 5 = \cancel{4} \geq 0 \rightarrow \text{TRUE} \end{aligned}$$

$$\begin{aligned} &= 4 + 7 - 6 \\ &= 11 - 6 = 5 \geq 0 \rightarrow \text{TRUE} \end{aligned}$$

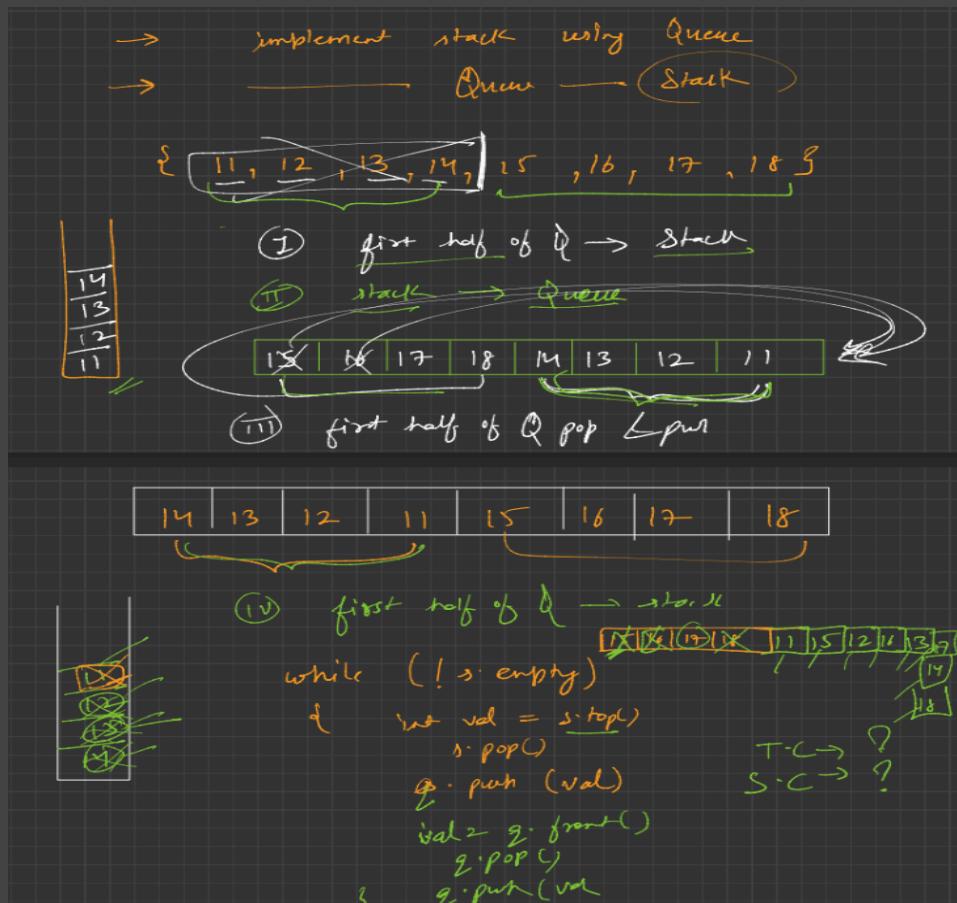
$$\begin{aligned} &= 5 + 4 - 7 \\ &= 9 - 7 = 2 \geq 0 \rightarrow \text{TRUE} \end{aligned}$$



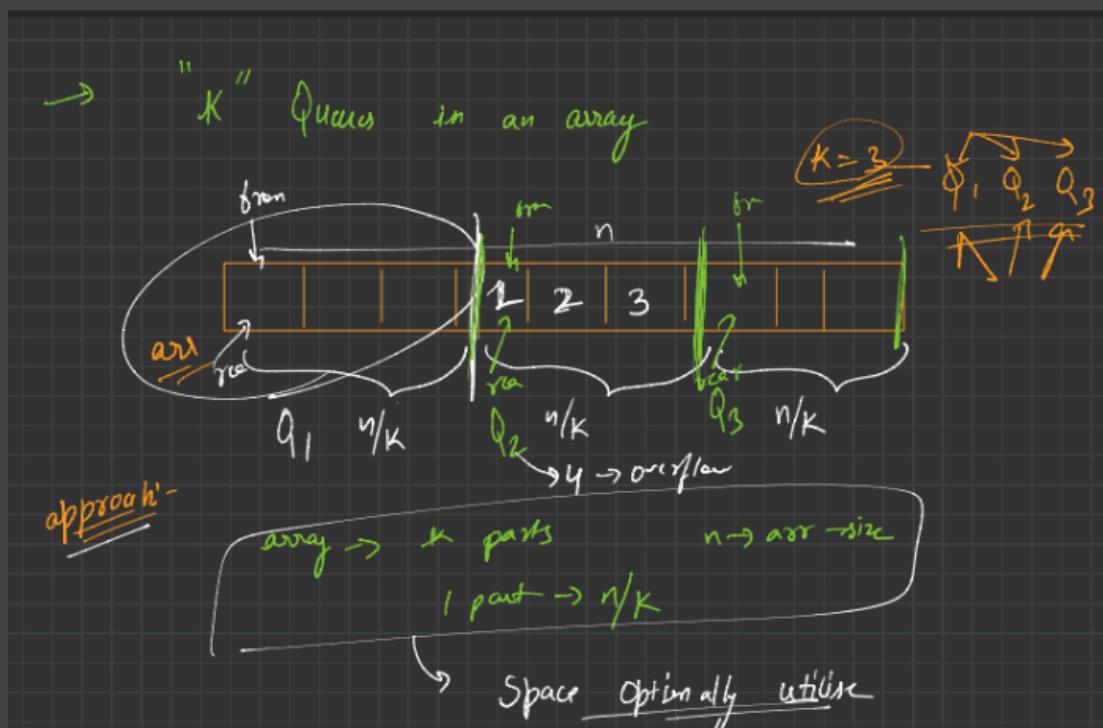
Interleave First and Second Halves Of A Queue:



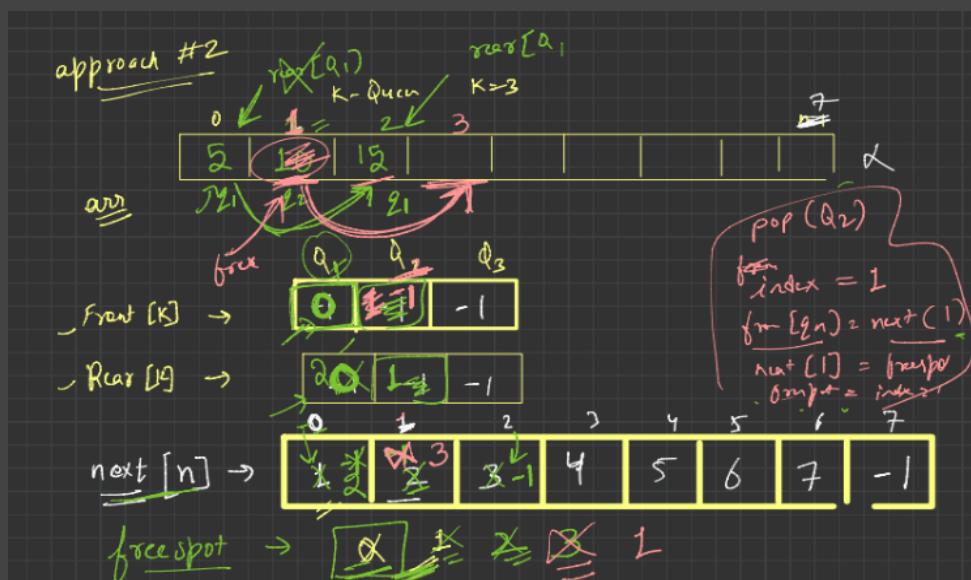
Interleave First and Second Halves Of A Queue Using Stack:



Insert K Queues In An Array Approach-I:



Insert K Queues In An Array Approach-II:



push:-
 → Overflow check → $\boxed{\text{free} = -1}$

→ // find index, where we want to insert

int index = freespot

→ // update freespot
 $\text{freespot} = \text{next}[\text{index}]$

↳ // if first element

if (front [gn] == -1)

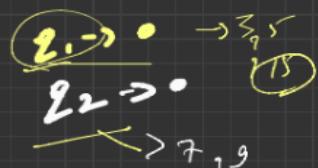
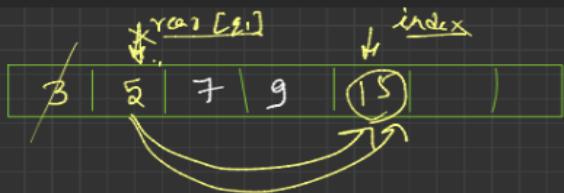
front [gn] = index;

else

{

next [rear [gn]] = index;

}

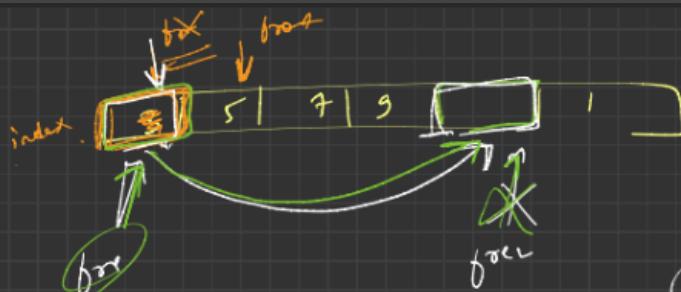


next [rear [gn]] = index

↳ next [index] = -1 ;

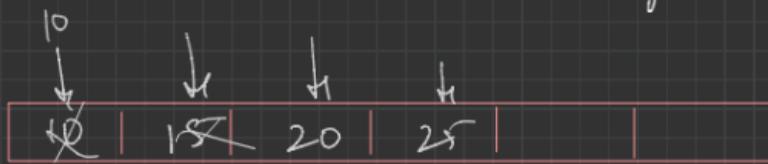
↳ // point rear to index
 rear [gn] = index;

↳ // push element
 arr [index] = n;



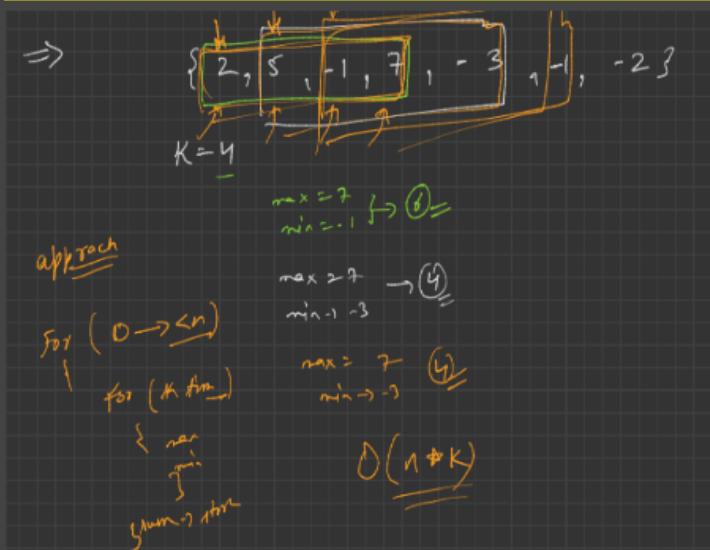
next [index] = free

free = index

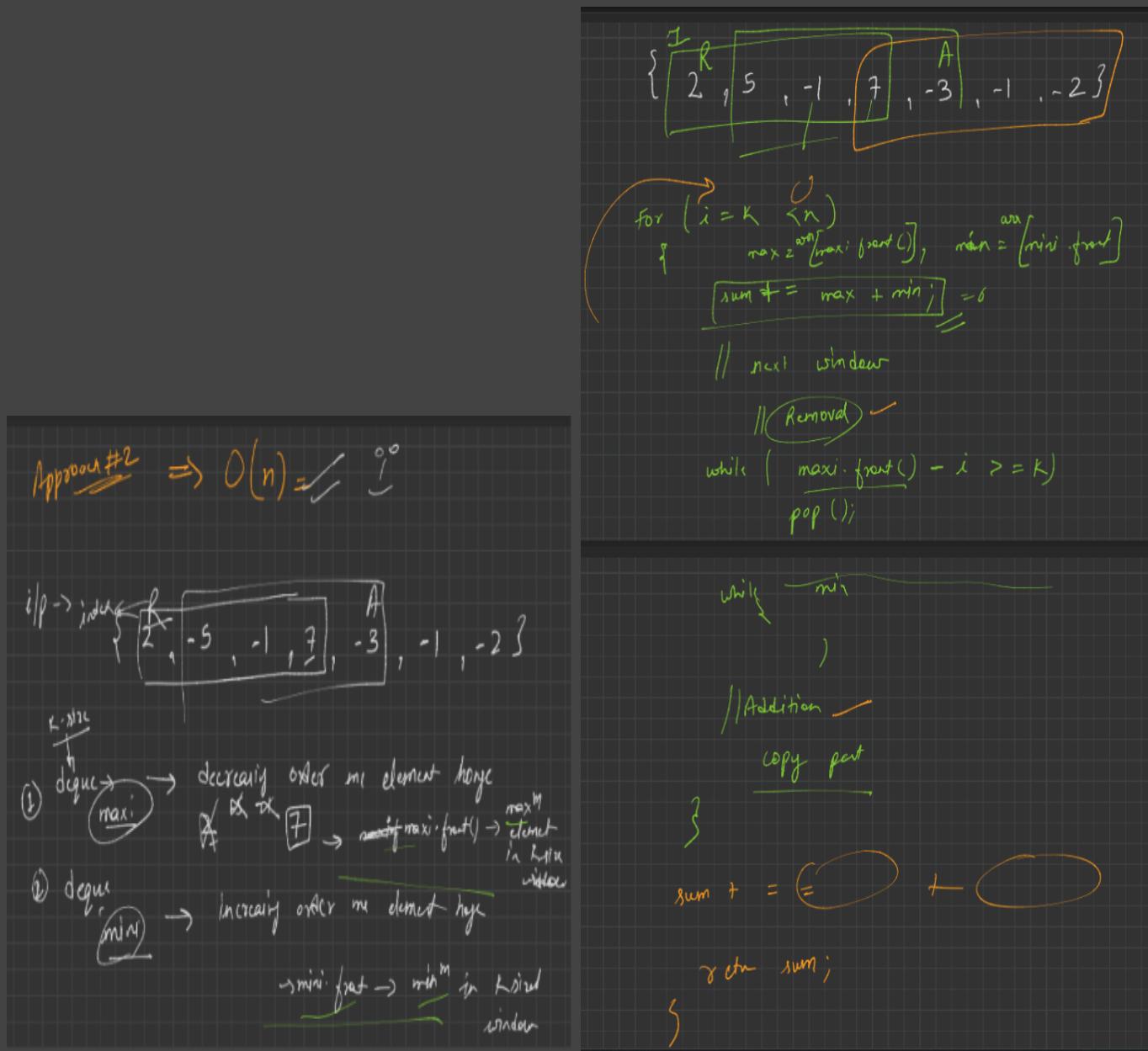


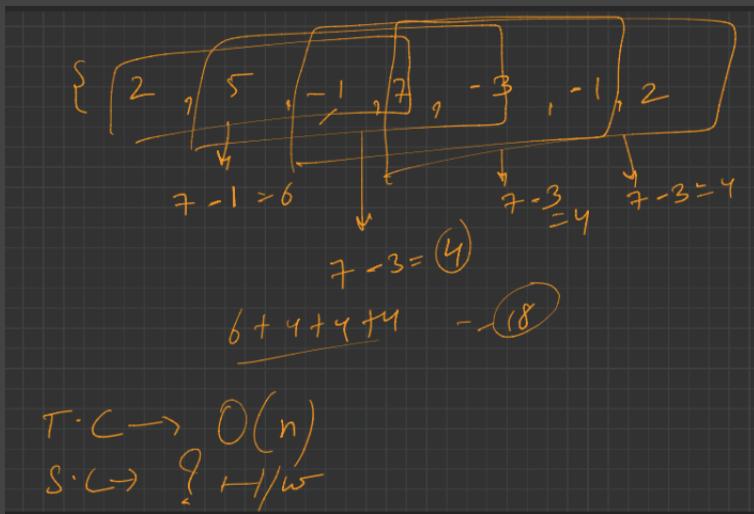
arr q1 q1 q2 q1

Sum Of Minimum And Maximum Elements Of All Subarrays Of Size K Approach-I:



Sum Of Minimum And Maximum Elements Of All Subarrays Of Size K Approach-II:





1. For the first k elements: The code enters the first for loop and processes the first k elements of the array. Each element is added to the deque's maxi and mini after removing elements from the back of the deque that are not needed. This process takes constant time for each element, so for k elements, it takes $O(k)$ time.
2. For the remaining elements: The code enters the second for loop and processes the remaining $n-k$ elements of the array. For each element, it first removes elements that are out of the current window from the front of the deque. Then it adds the current element to the deque after removing elements from the back of the deque that are not needed. This process also takes constant time for each element, so for $n-k$ elements, it takes $O(n-k)$ time.

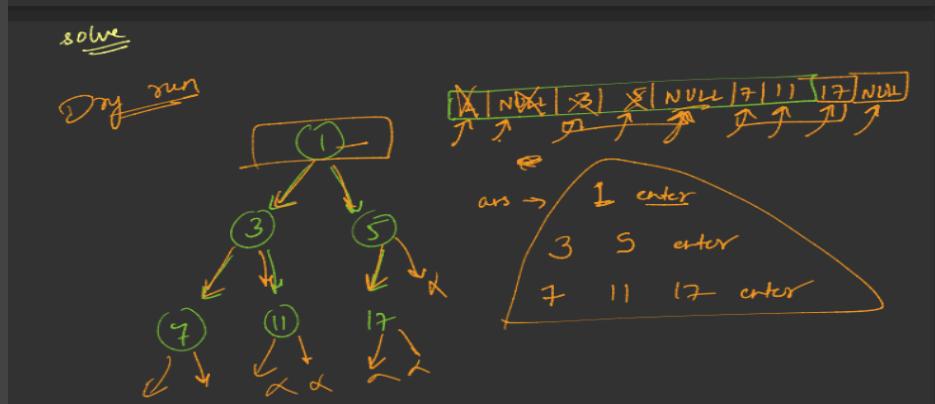
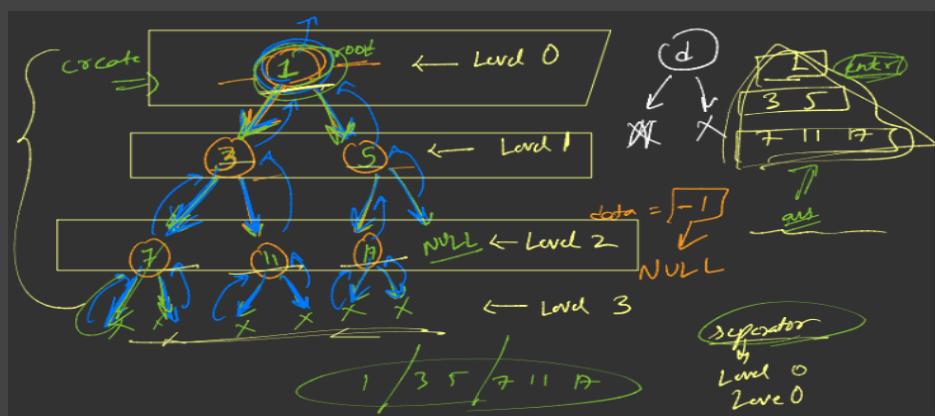
Since the code processes k elements in the first loop and $n-k$ elements in the second loop, the total time complexity is $O(k) + O(n-k) = O(n)$, where n is the total number of elements in the array. This is why we say each element in the array is processed only once in a single pass. The operations inside the loops are all constant time operations, so they do not change the overall time complexity.

Binary Tree

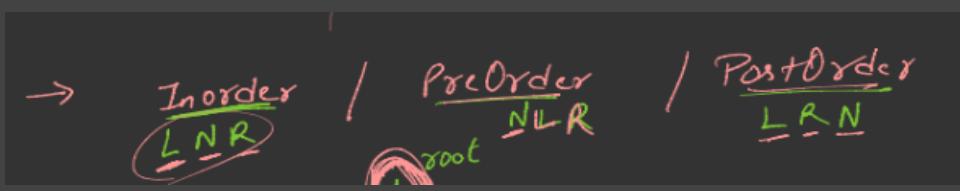
Basic Terms Of Binary Tree:



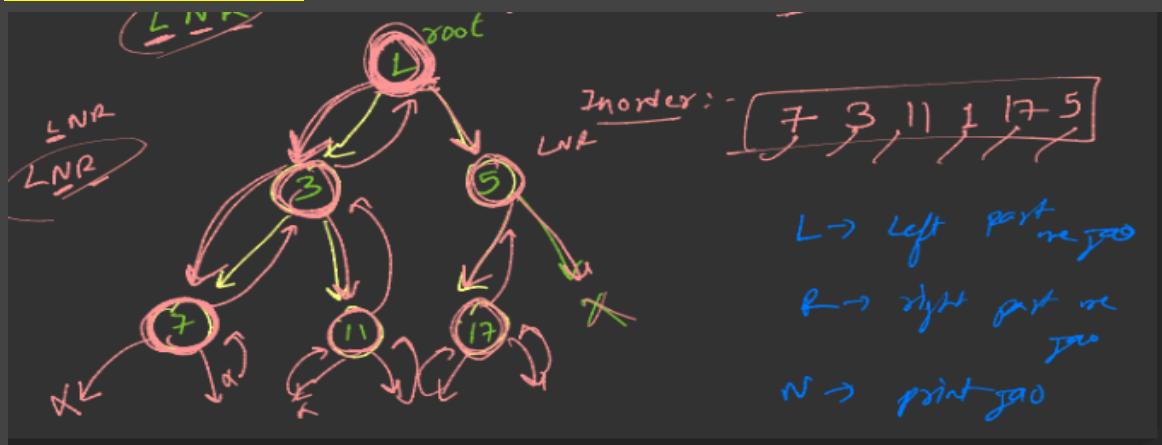
Creation Of Binary Tree & Level Order Traversal(LOT):



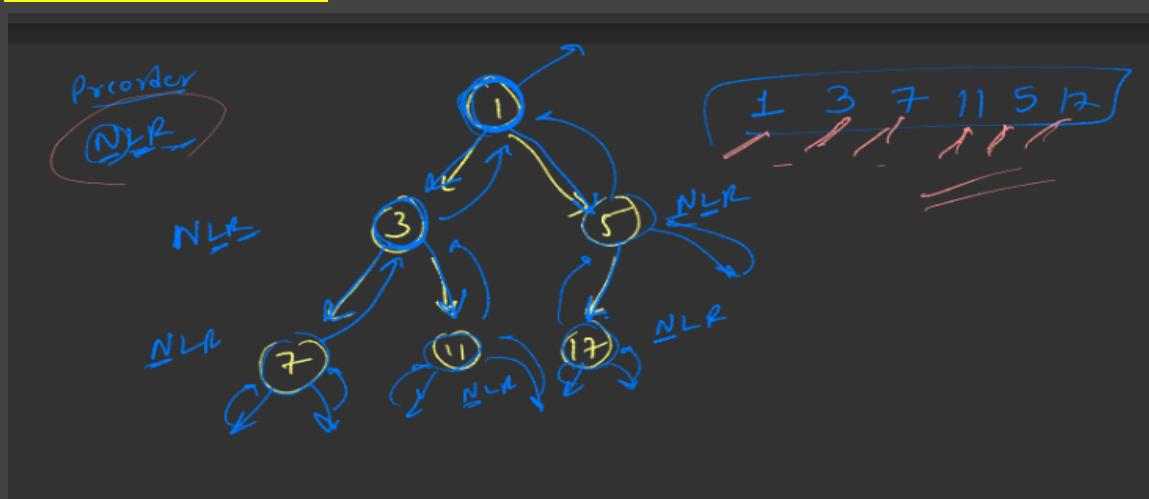
Reverse Level Order Traversal:



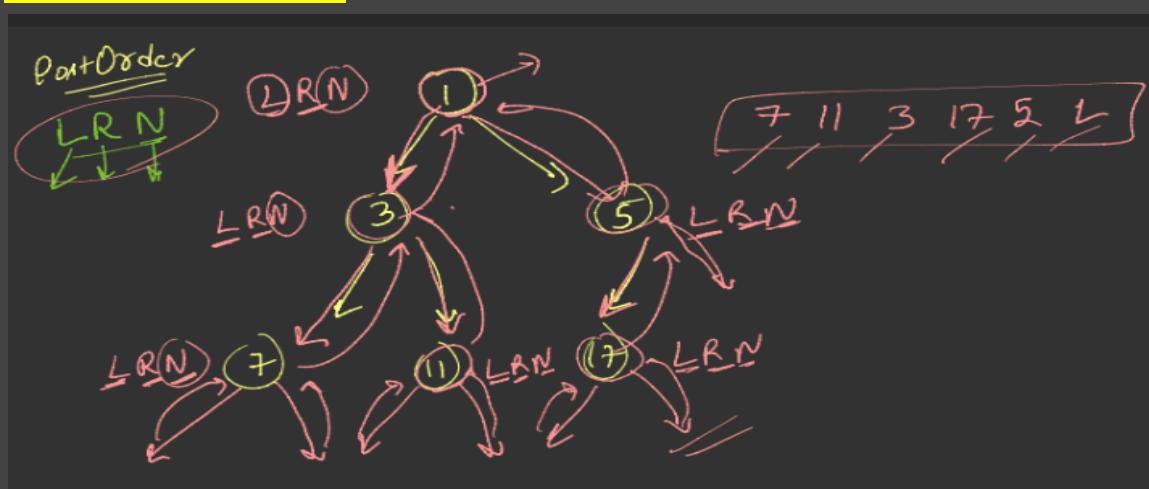
Inorder Traversal:



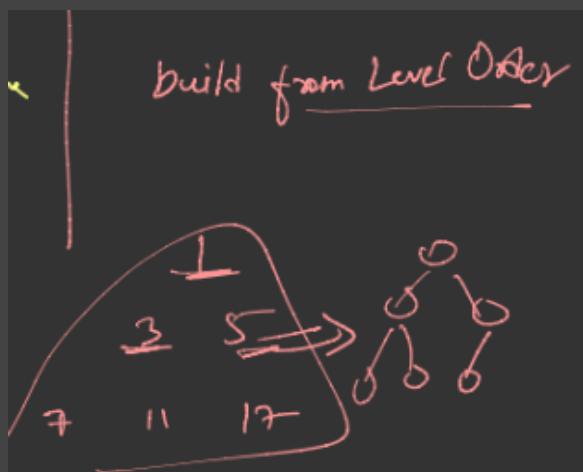
Preorder Traversal:



Postorder Traversal:

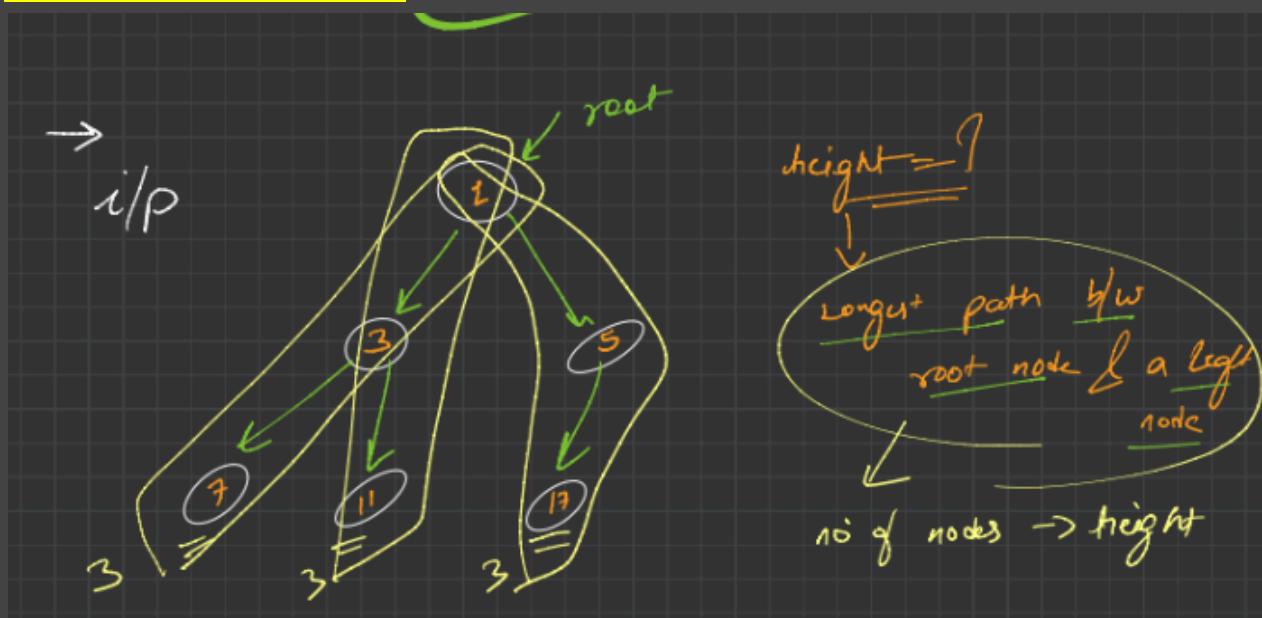


Build Binary Tree From Level Order:

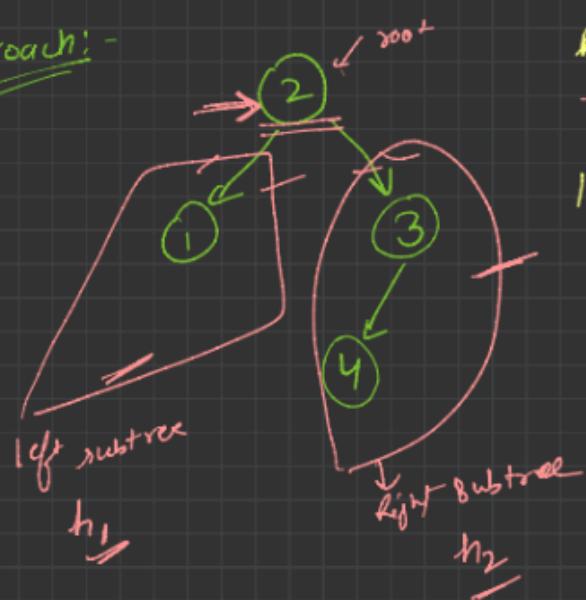


Count Leaf Nodes:

Height Of A Binary Tree:



approach:-

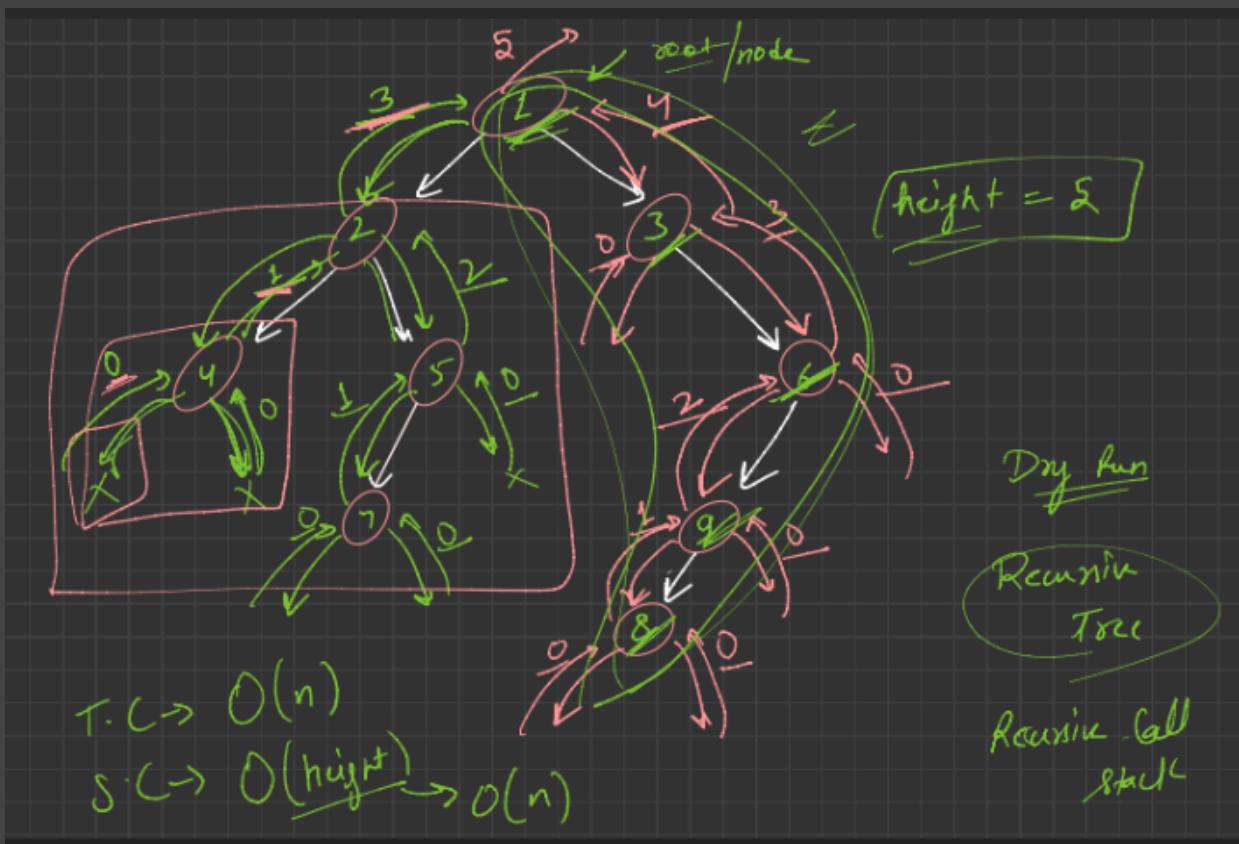


Recursion:-

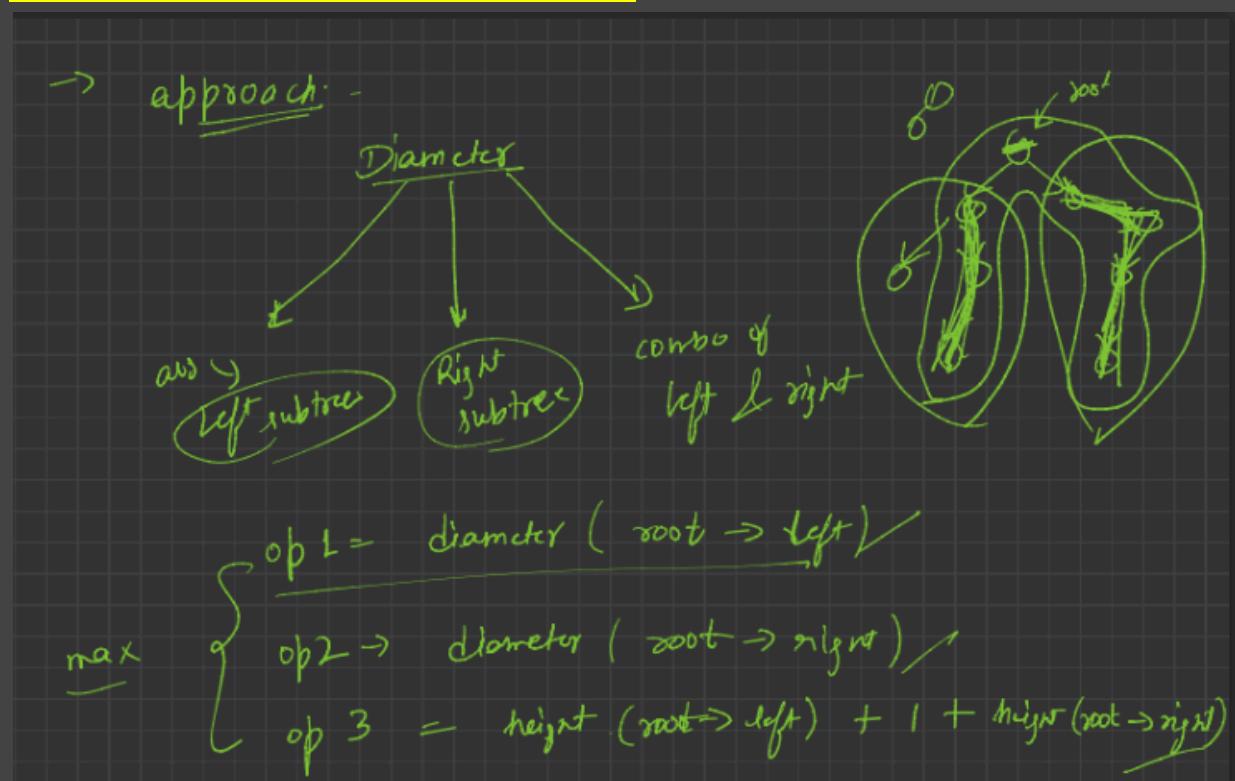
~~Recursion:-~~ → Backtracking
sub problem
1 case solve
Kando

$$\max(h_1, h_2) + 1$$

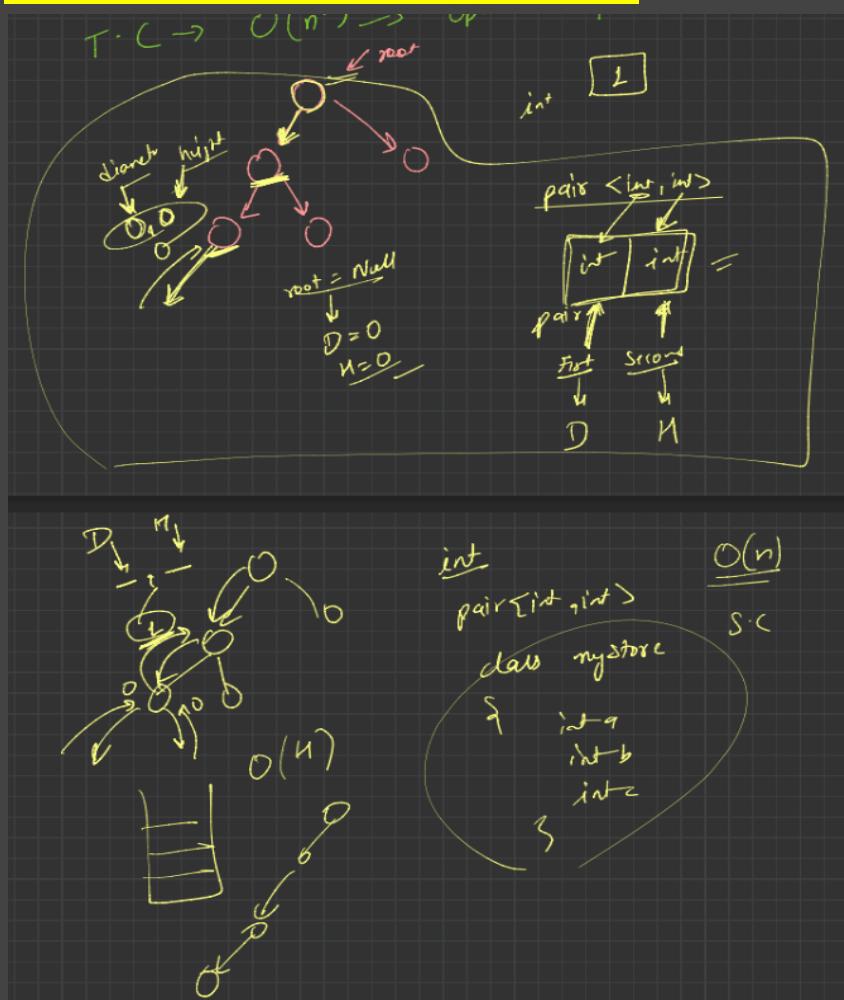
height



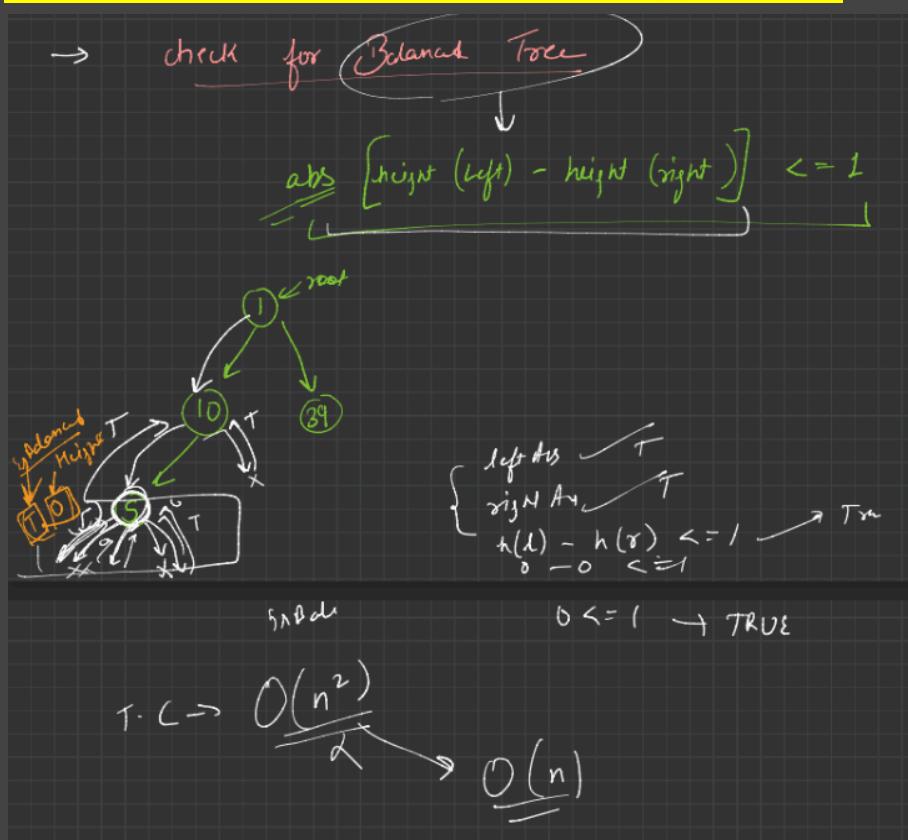
Diameter Of Binary Tree Approach-I:



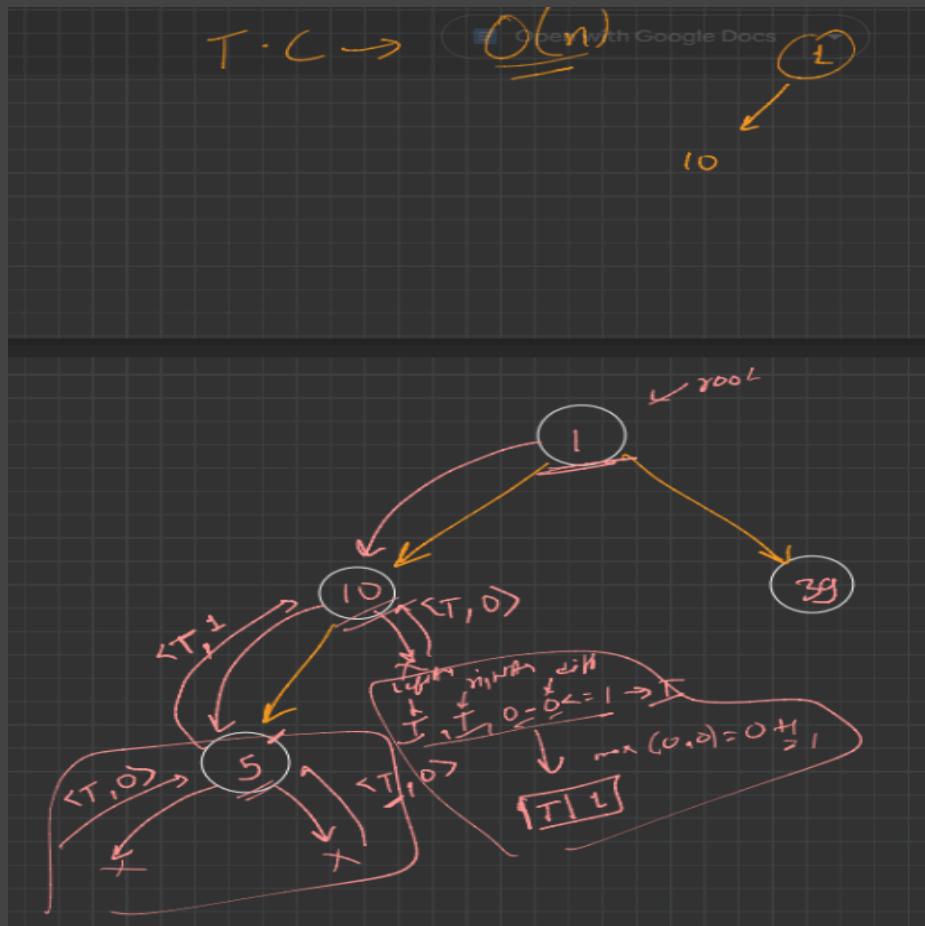
Diameter Of Binary Tree Approach-II:



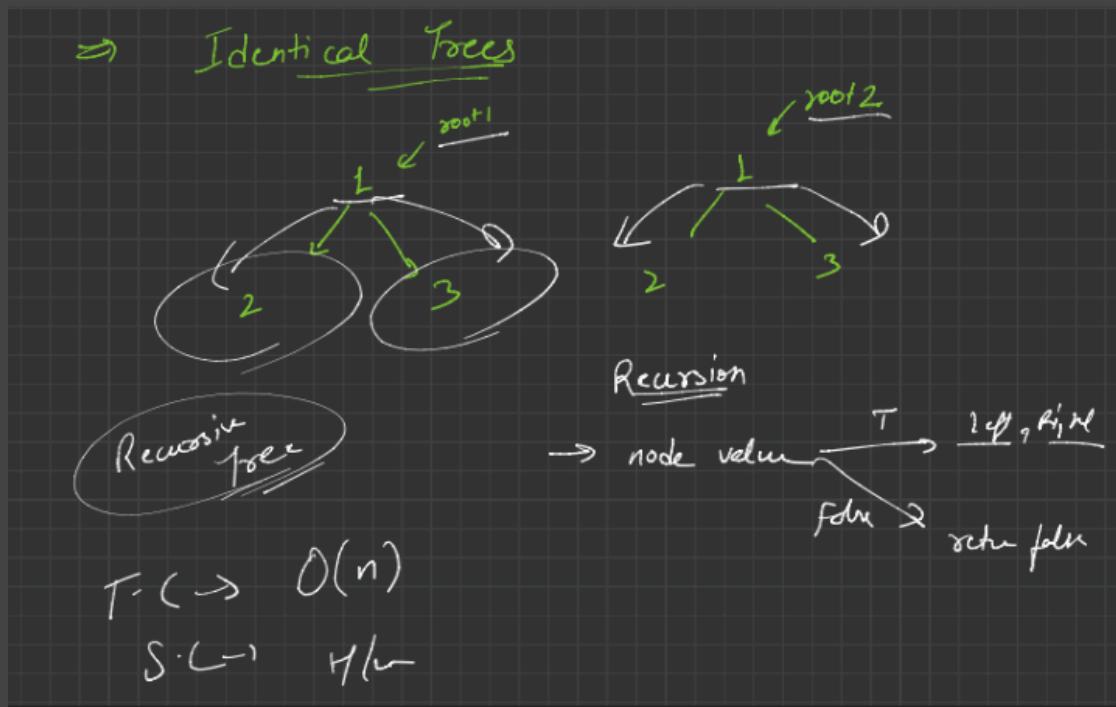
Check If The Tree Is Balanced Or Not Approach-I:



Check If The Tree Is Balanced Or Not Approach-II:

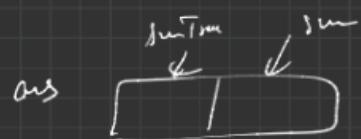
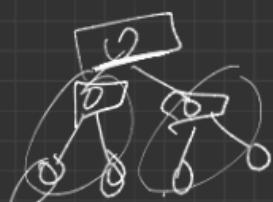
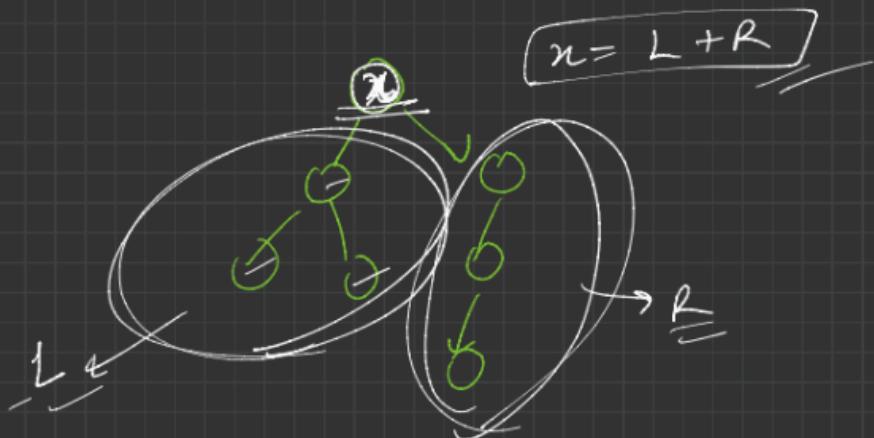


Check Whether The Two Trees Are Identical Or Not:



Sum Tree:

→ check Sum Tree or Not



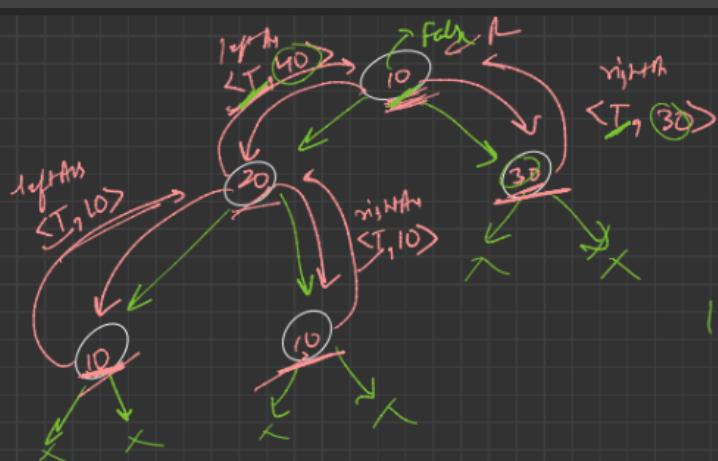
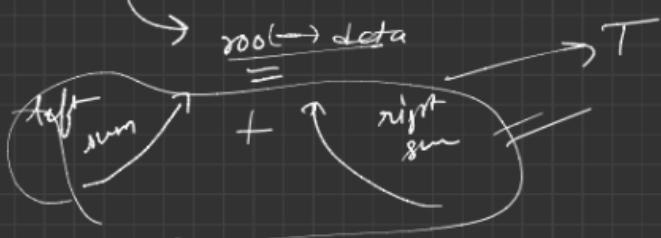
→ isSum ($\text{root} \rightarrow \text{left}$) → T

→ isSum ($\text{root} \rightarrow \text{right}$) → T

isSum → T/F
sum → int

$\begin{bmatrix} 0 \\ 1 \\ 1 \\ 0 \end{bmatrix}$

currNode



$$20 = 10 + 10$$

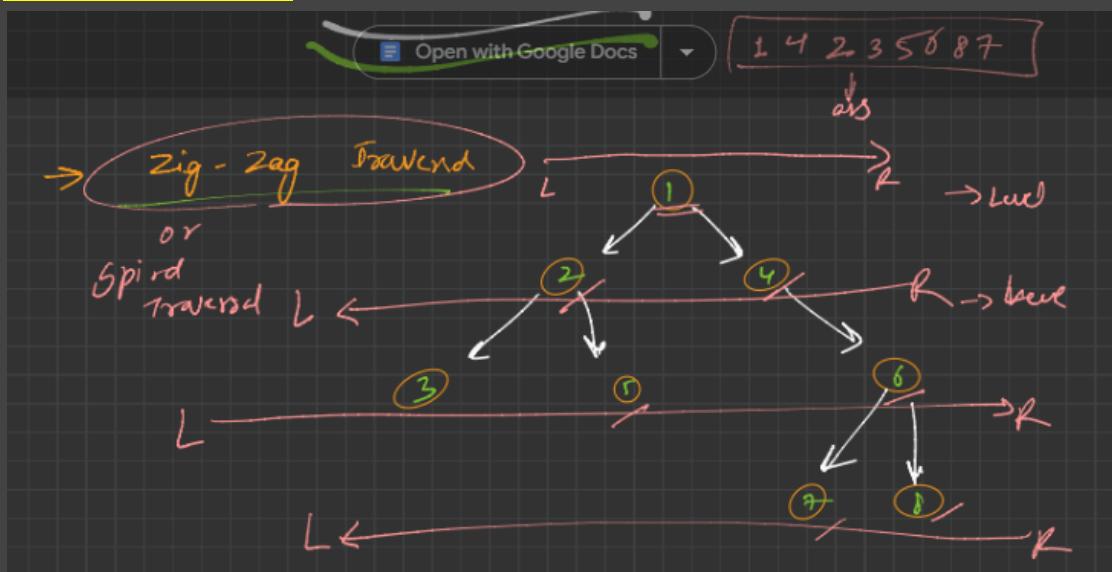
$$10 = 40 + 30$$

$$10 = 70$$

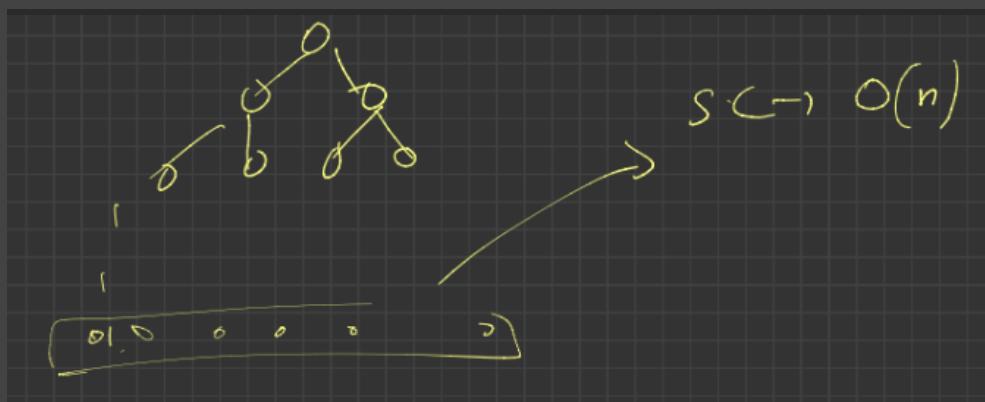
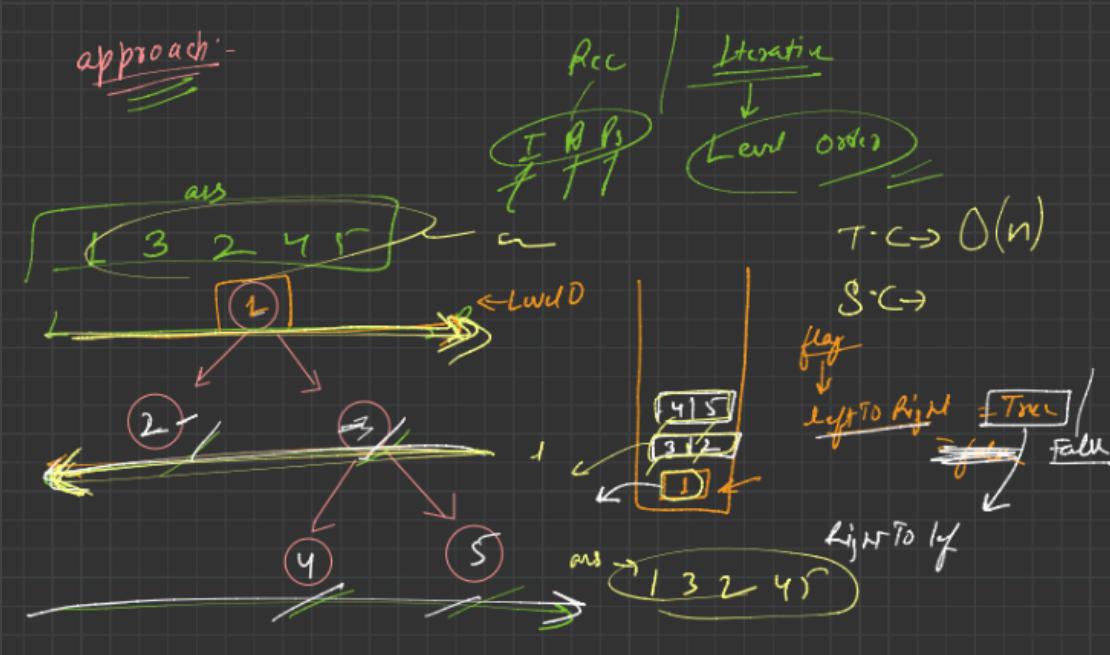
T.C → O(n)

S.C → O(H)

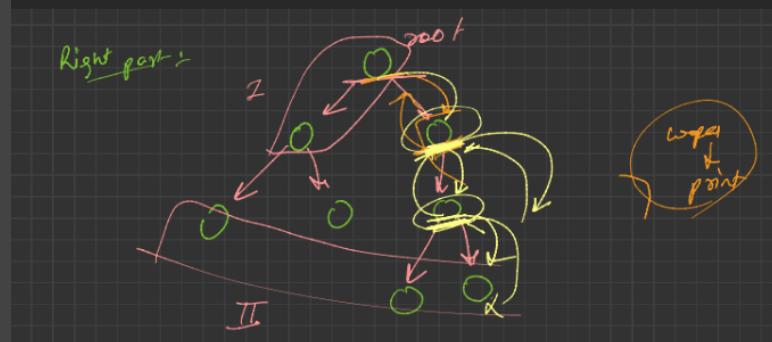
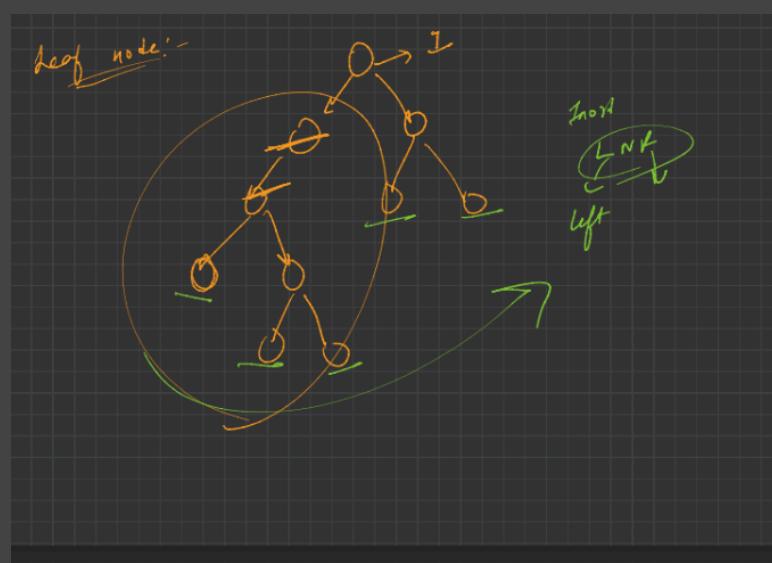
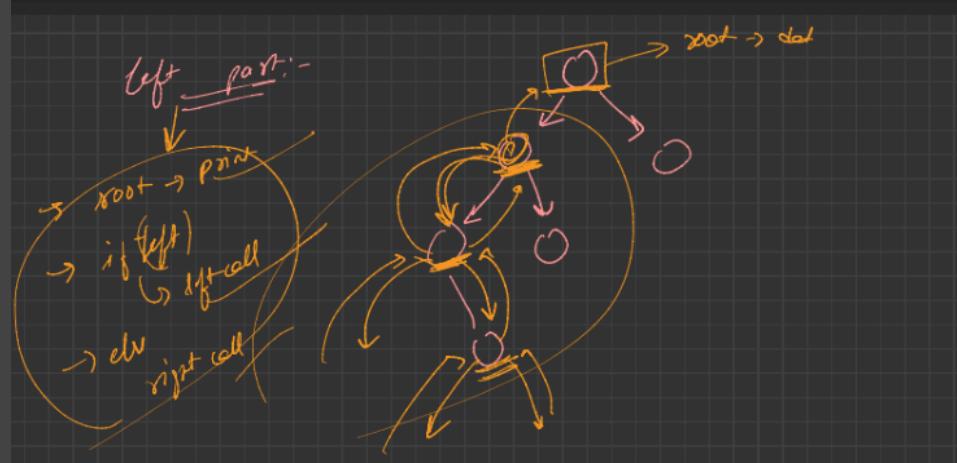
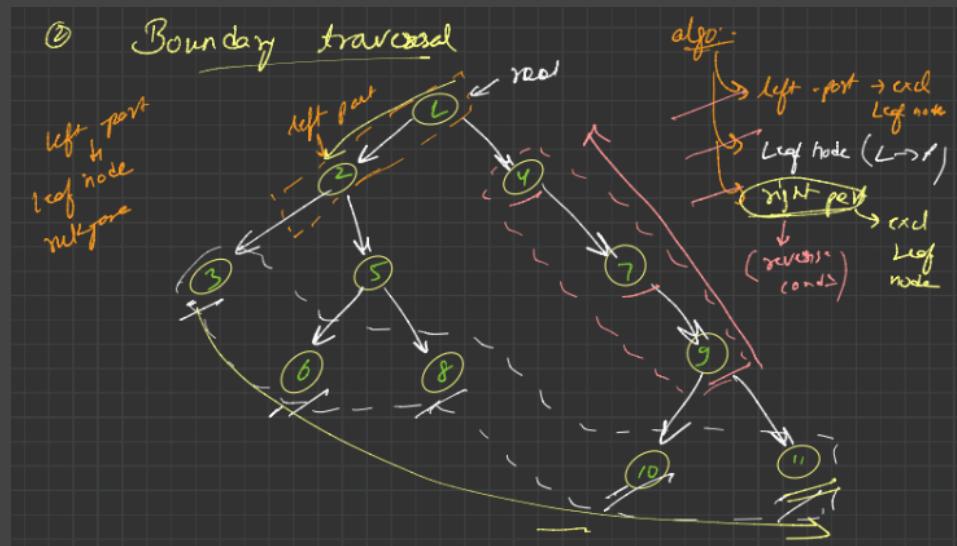
Zigzag Traversal:



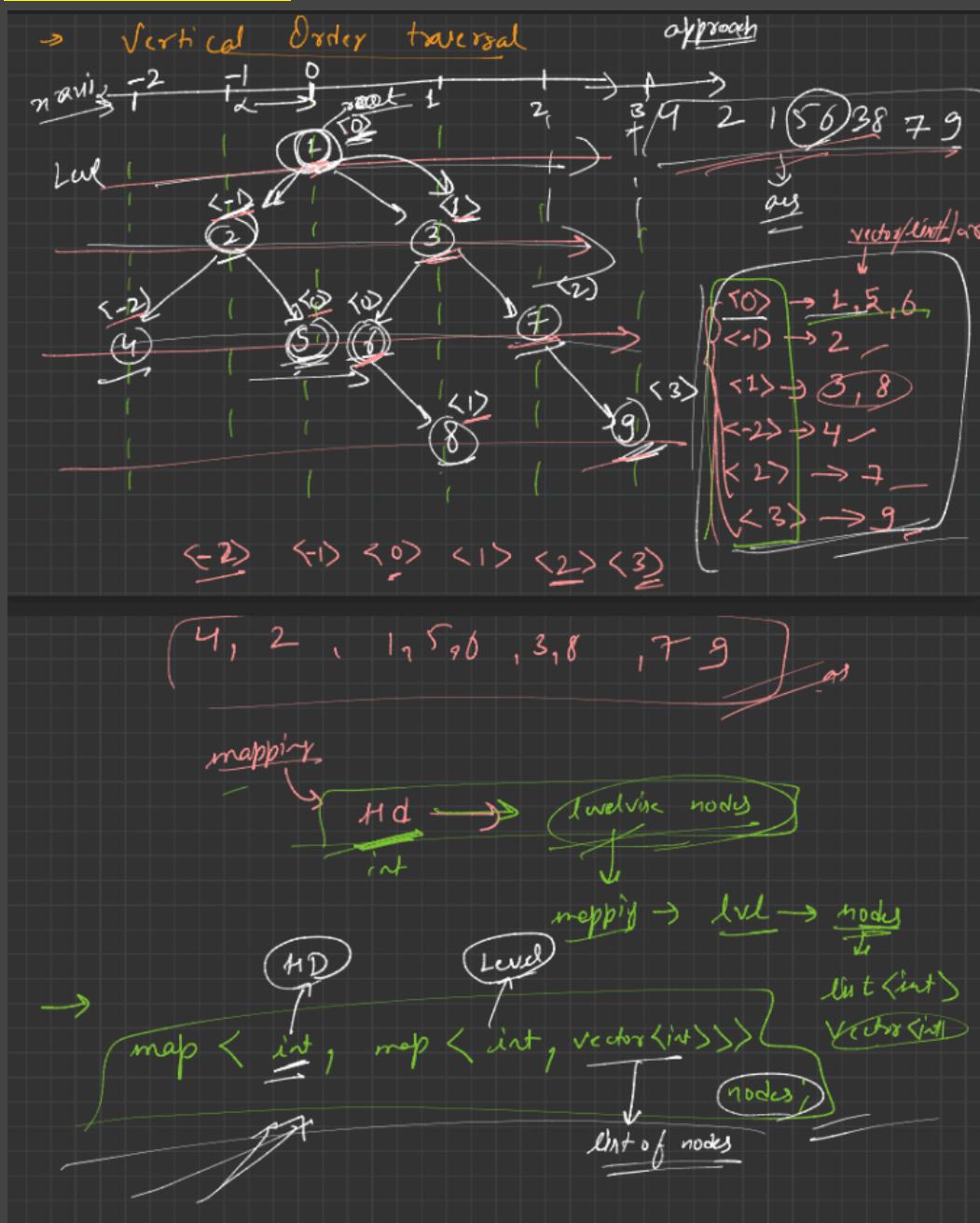
approach:-



Boundary Traversal:



Vertical Traversal:



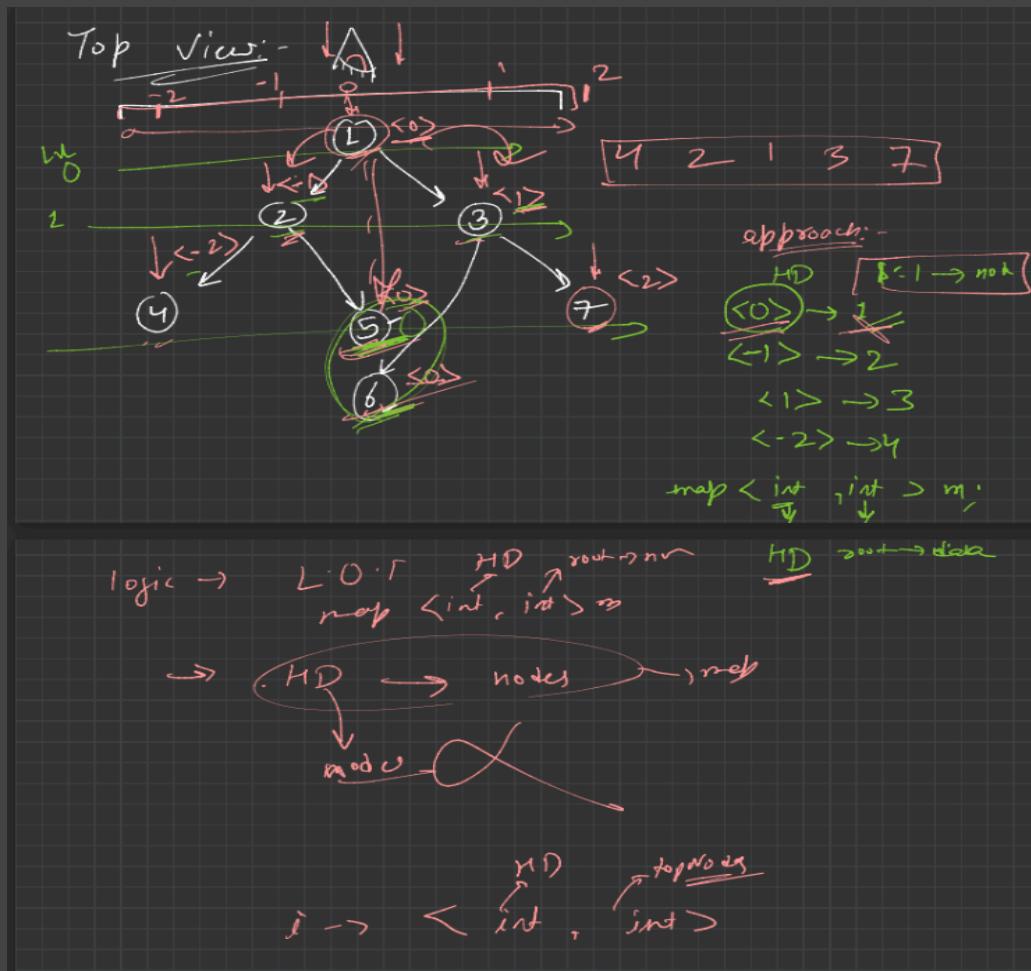
→ required → (HD, Lvl)

HD → pair< int, map < int, vector<int>>

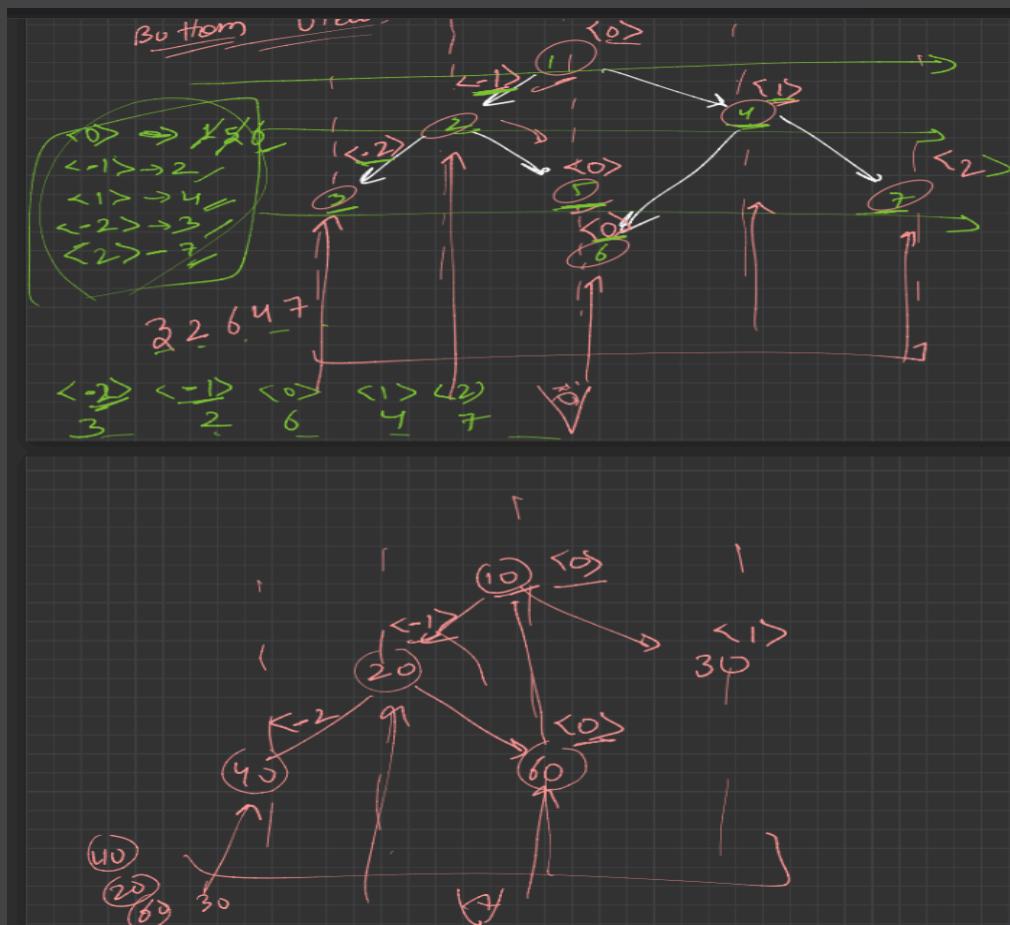
i → < int, map < int, vector<int>>

j → < int, vector<int>>

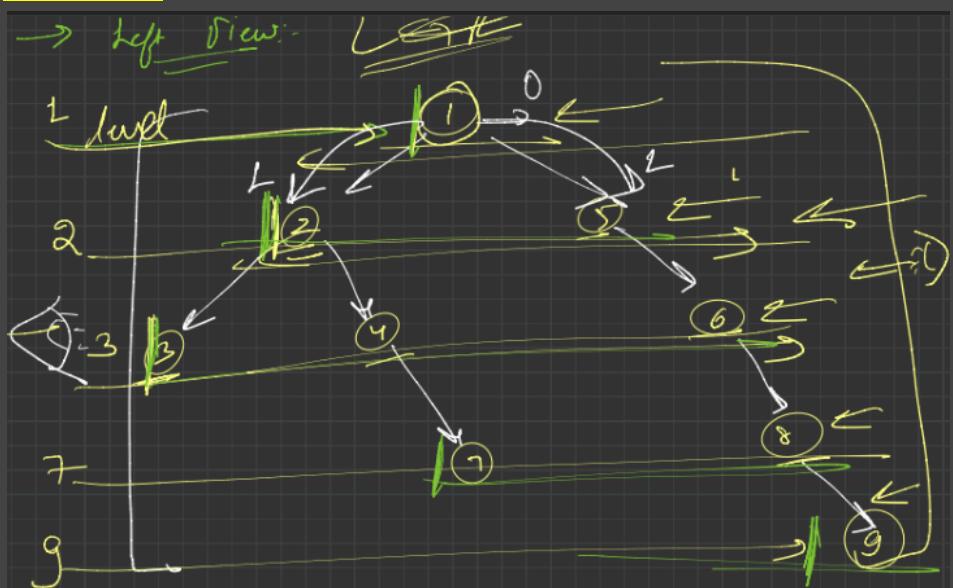
Top View:



Bottom View:



Left View:



Approach :-

$L \rightarrow R$

level → first node print

L.O.T

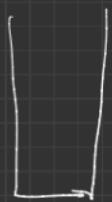
Recursive

Ith node → ?

level → stack
int level
next level

func (root, lvl)

{ // base case
if (root == NULL)
return;



you enter it
into & never
exit

if (lvl == Vector.size())
Vector
vector-store (root->val)

f(left, lvl + 1)

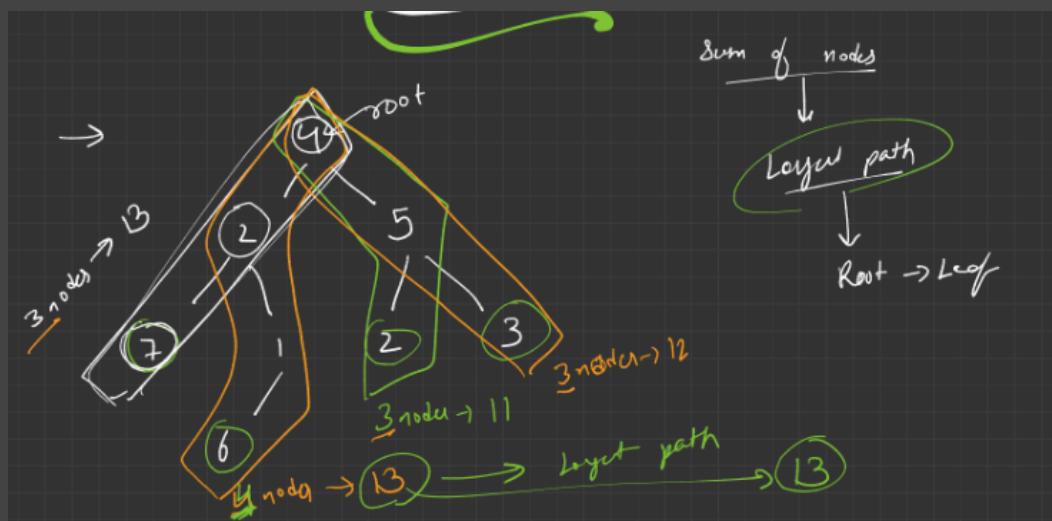
f(right, lvl + 1)

Right View:

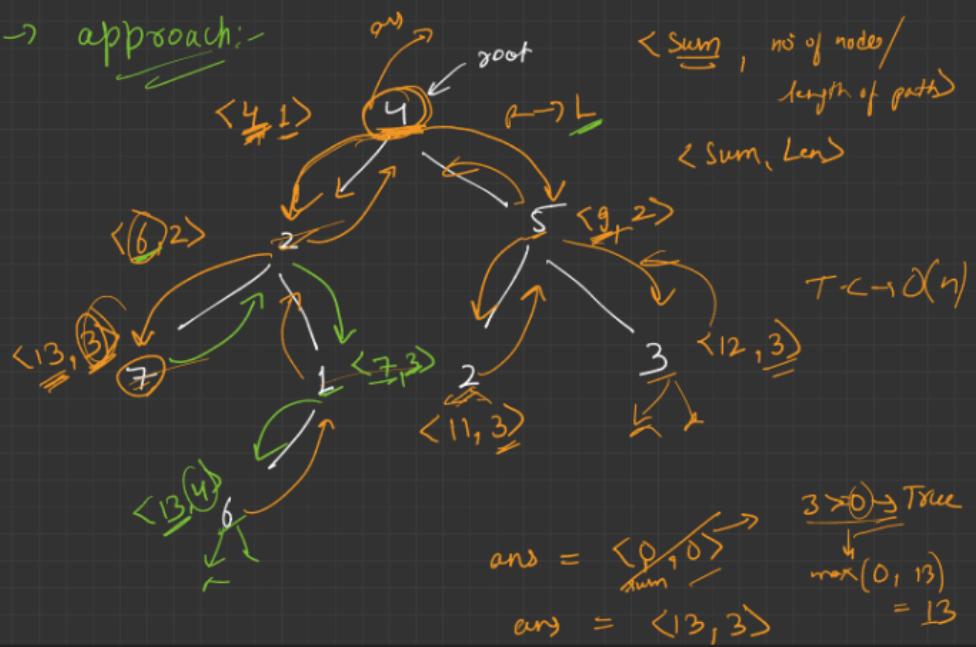
Just make the recursive call for right first and then left.

Diagonal Traversal:

Sum Of The Largest Bloodline Of A Tree (Sum Of Nodes On The Longest Path From Root To Leaf Node):

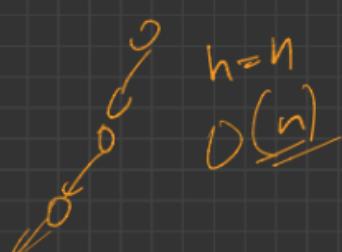


→ approach:-



$$\text{ans} = \begin{cases} <0, 0> & 3 > 0 \rightarrow \text{True} \\ \max(0, 13) & = 13 \end{cases}$$

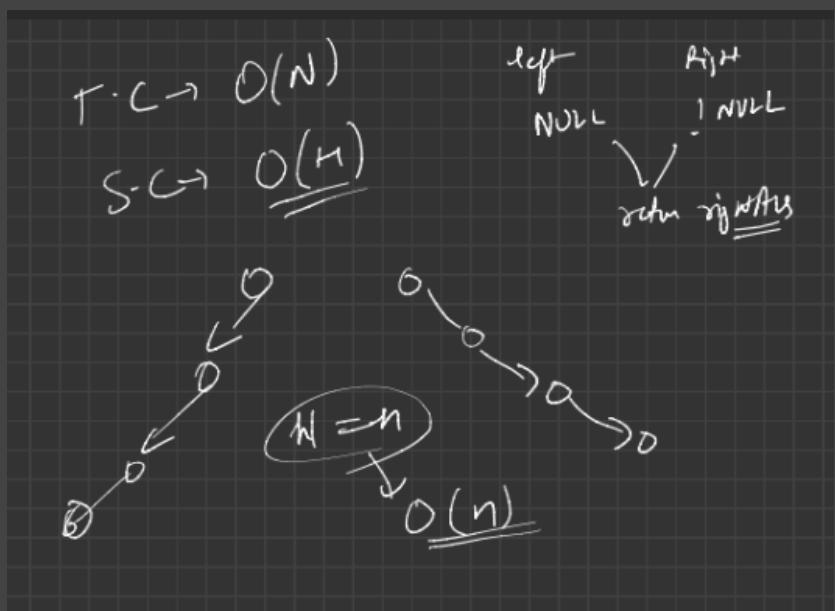
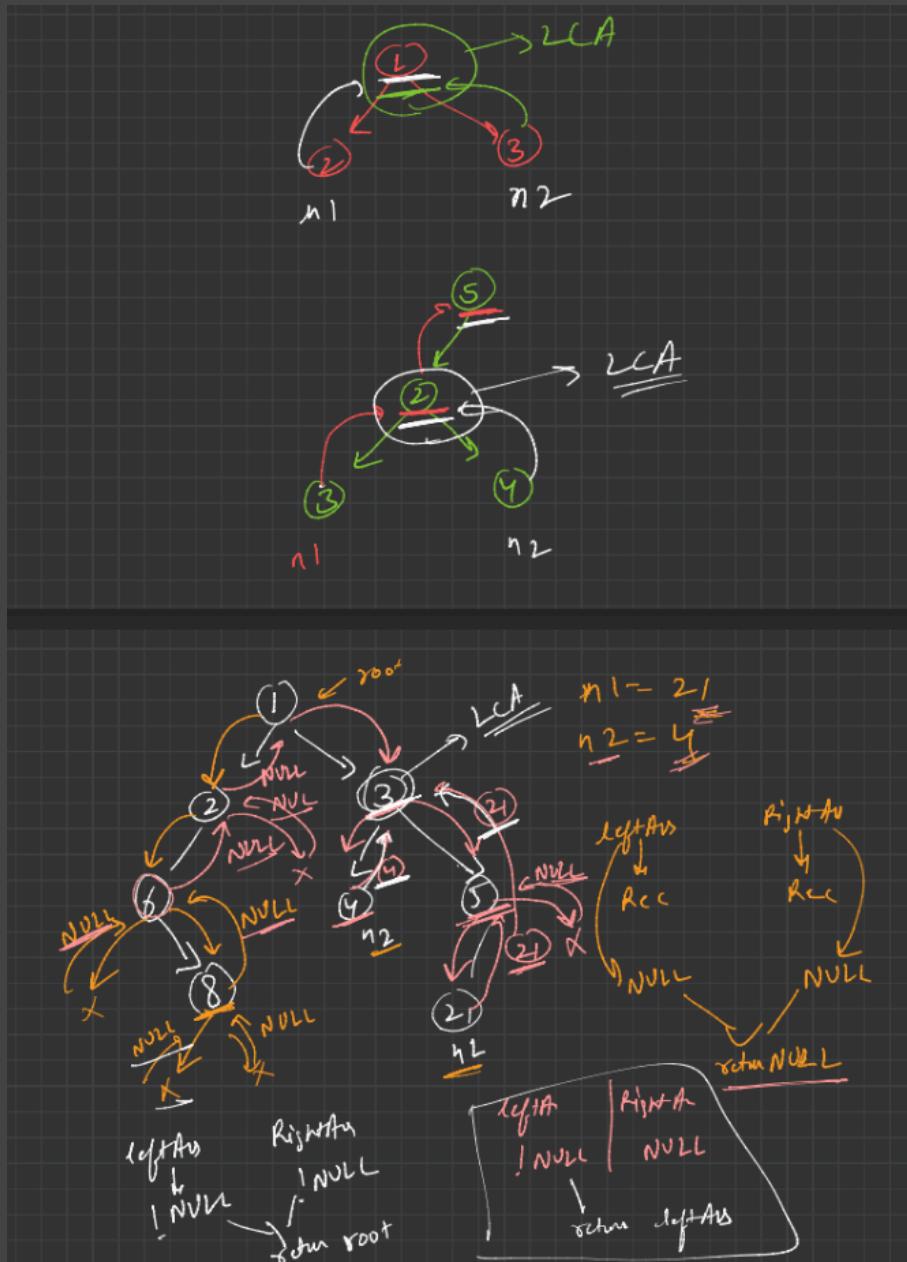
$S.C \sim O(n)$



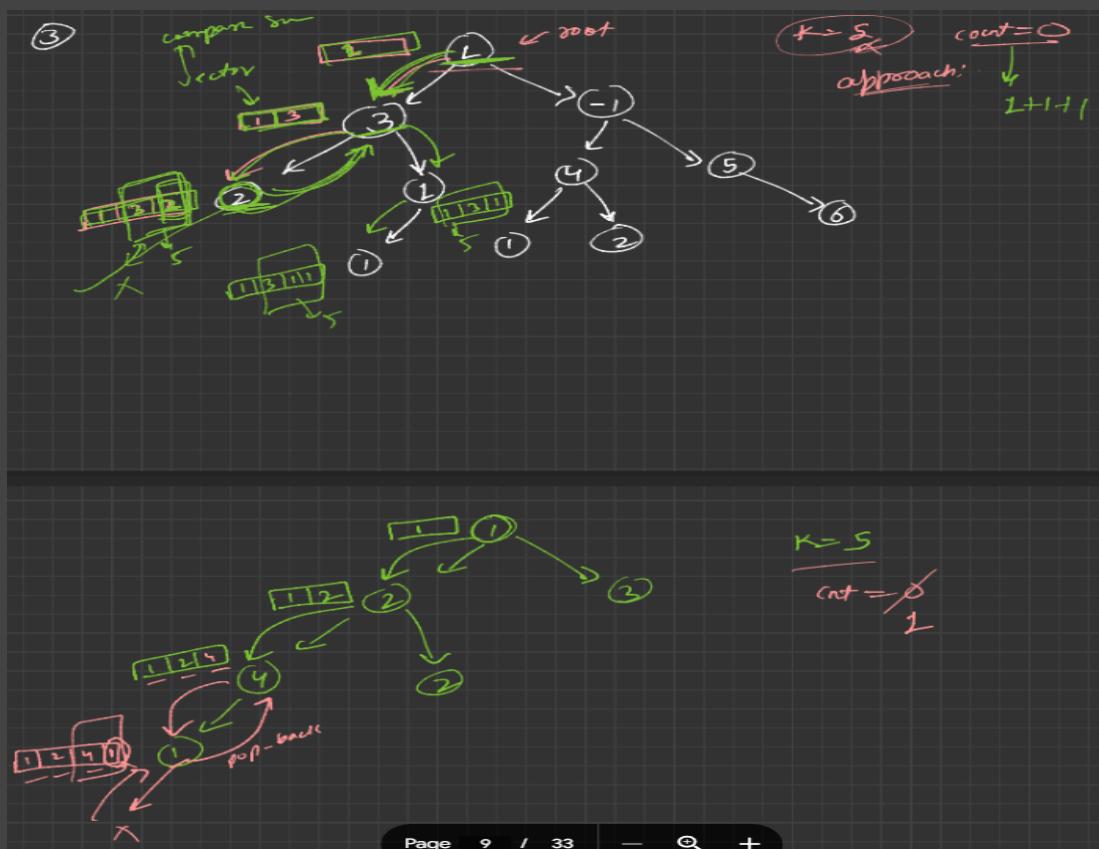
$$\begin{aligned} \text{ans} &= <13, 3> \\ &= <13, 4> \\ &\quad \text{sum} \\ &\quad \text{len} \end{aligned}$$

$4 > 3 \rightarrow \text{TRUE}$
 $\max(13, 13) = 13$
 $3 > 4 \rightarrow \text{False}$
 $3 > 4 \rightarrow \text{False}$

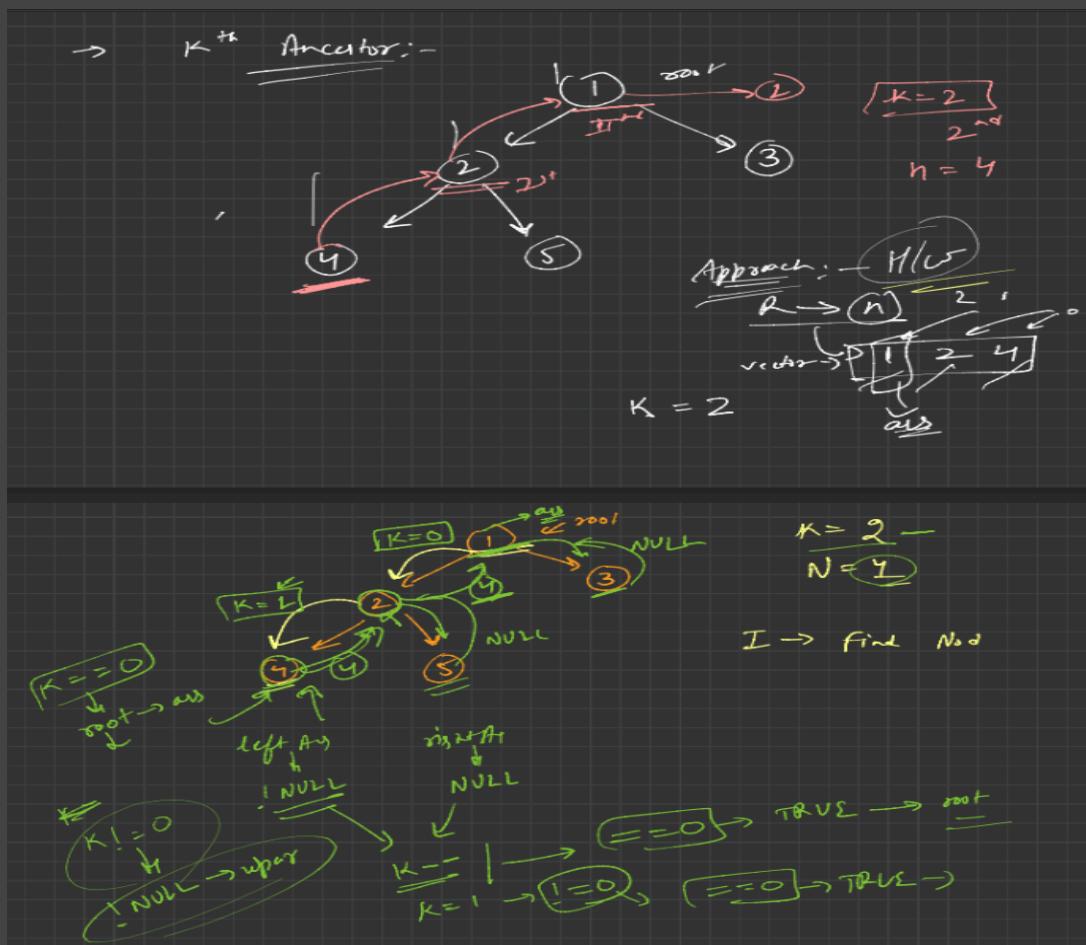
Lowest Common Ancestor:

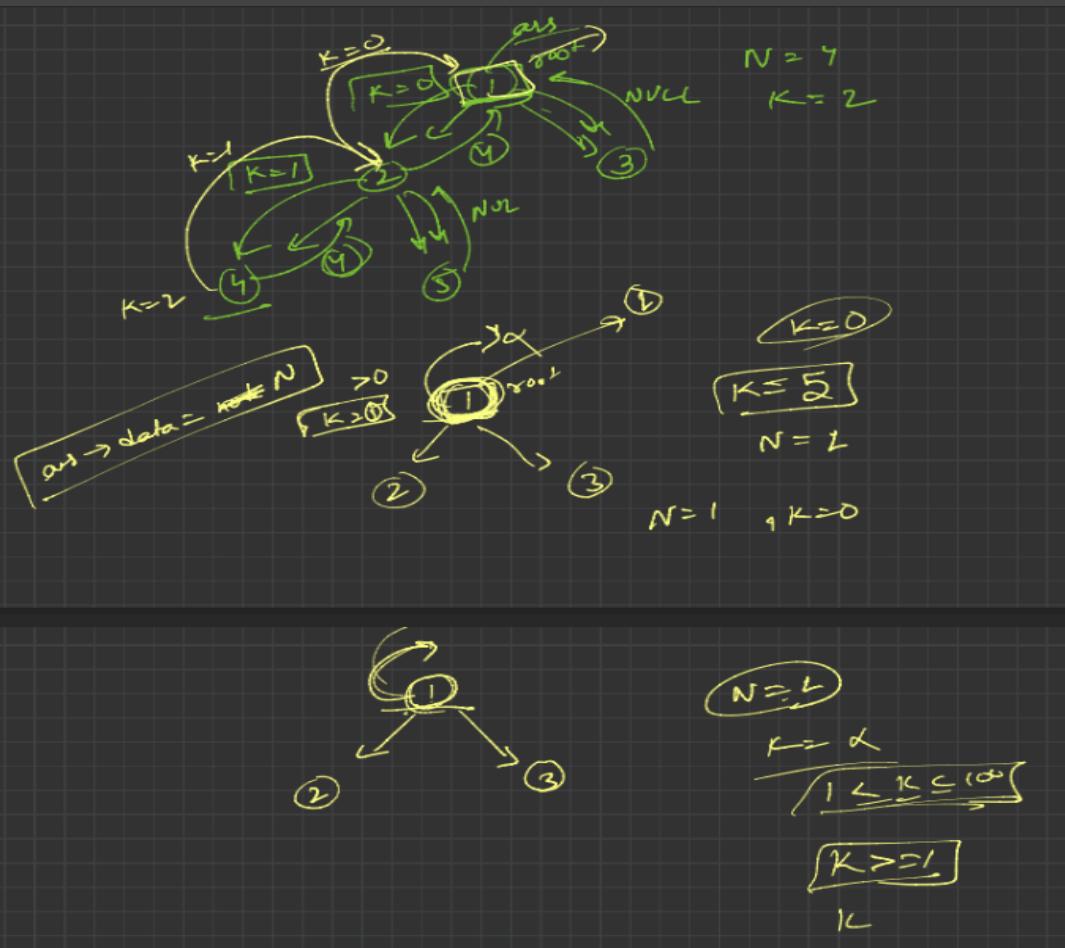


K Sum Paths:

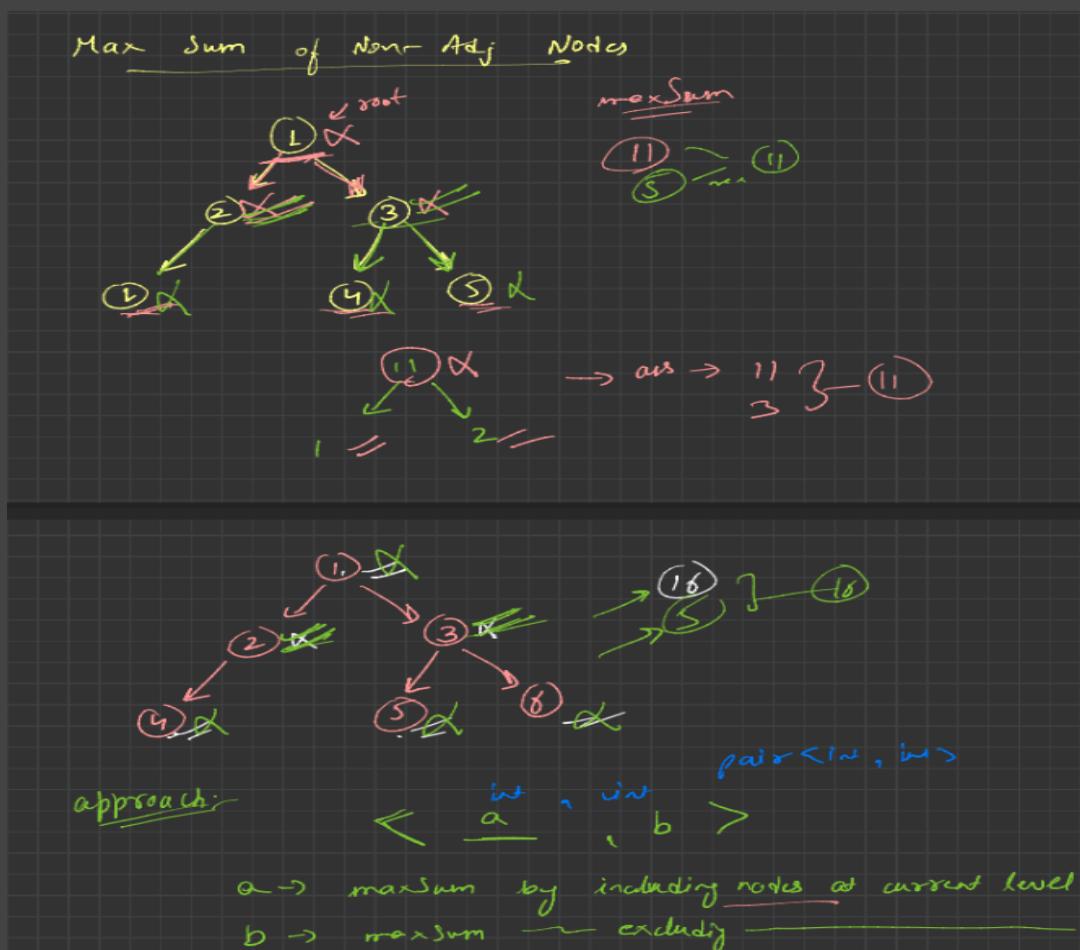


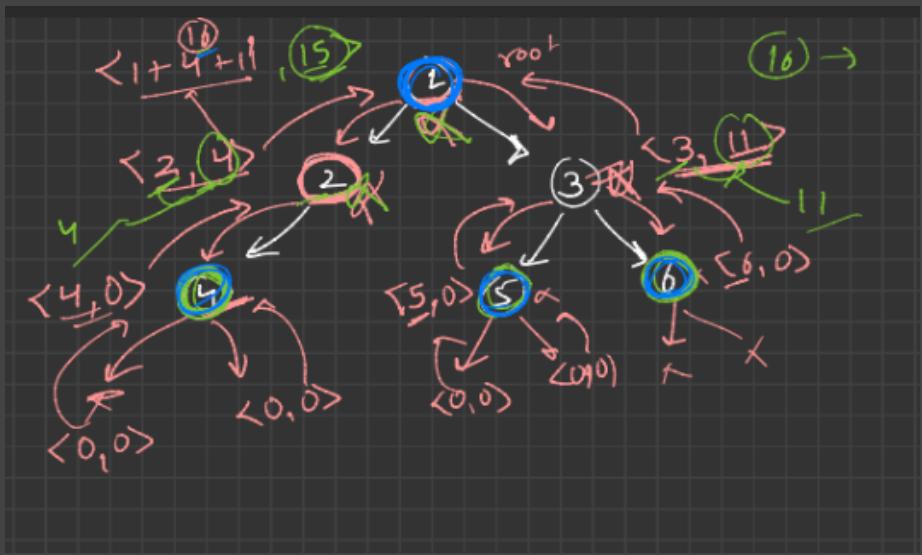
Kth Ancestor In A Tree:



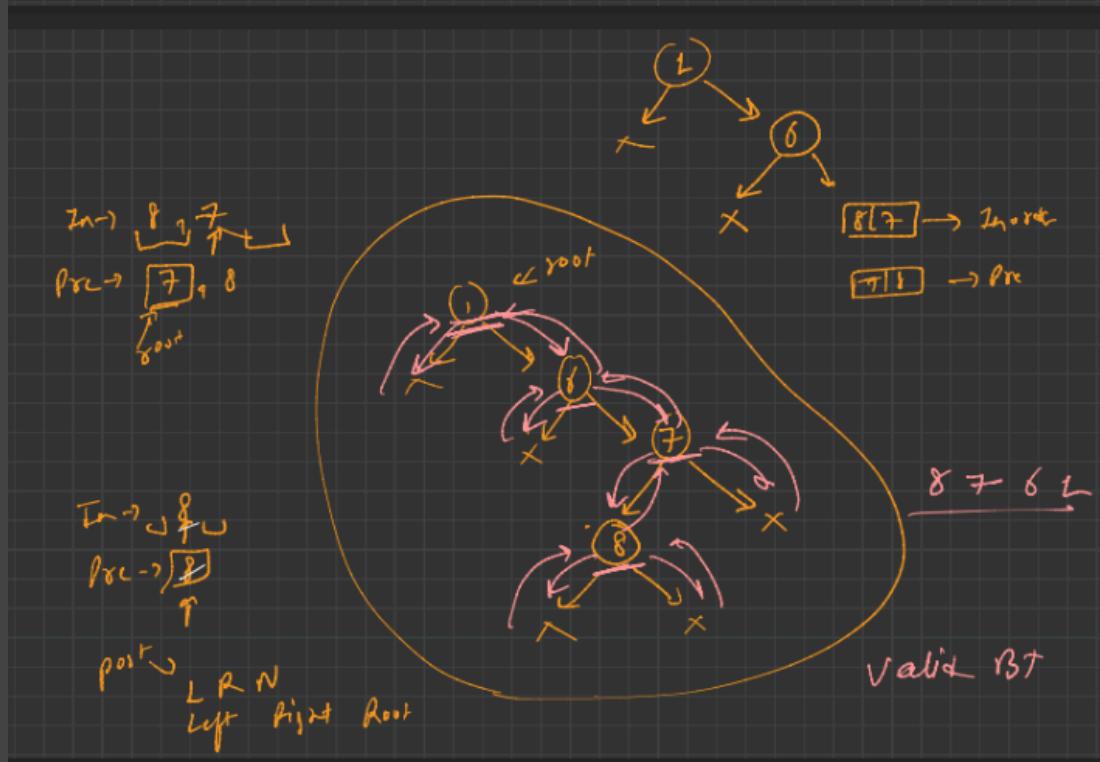
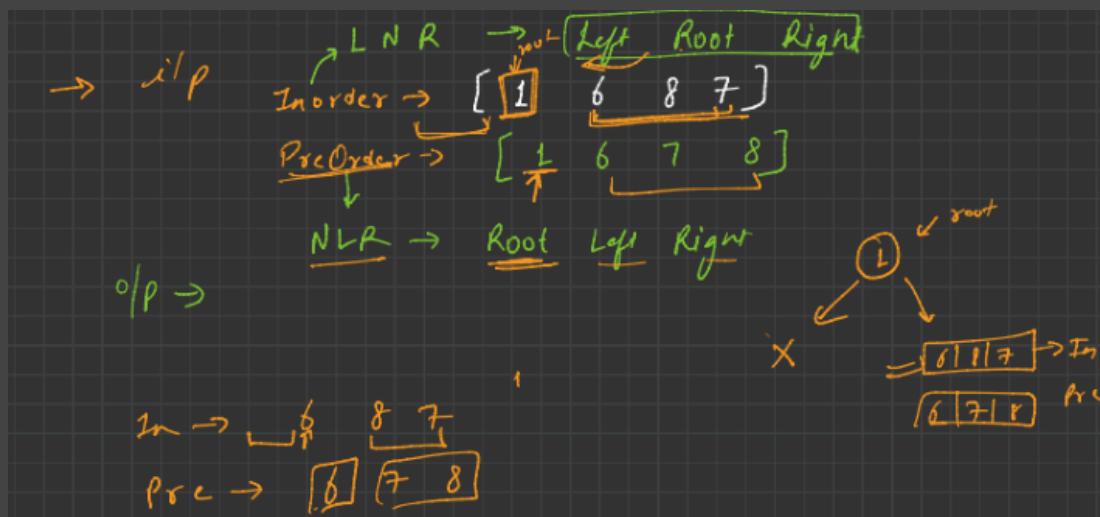


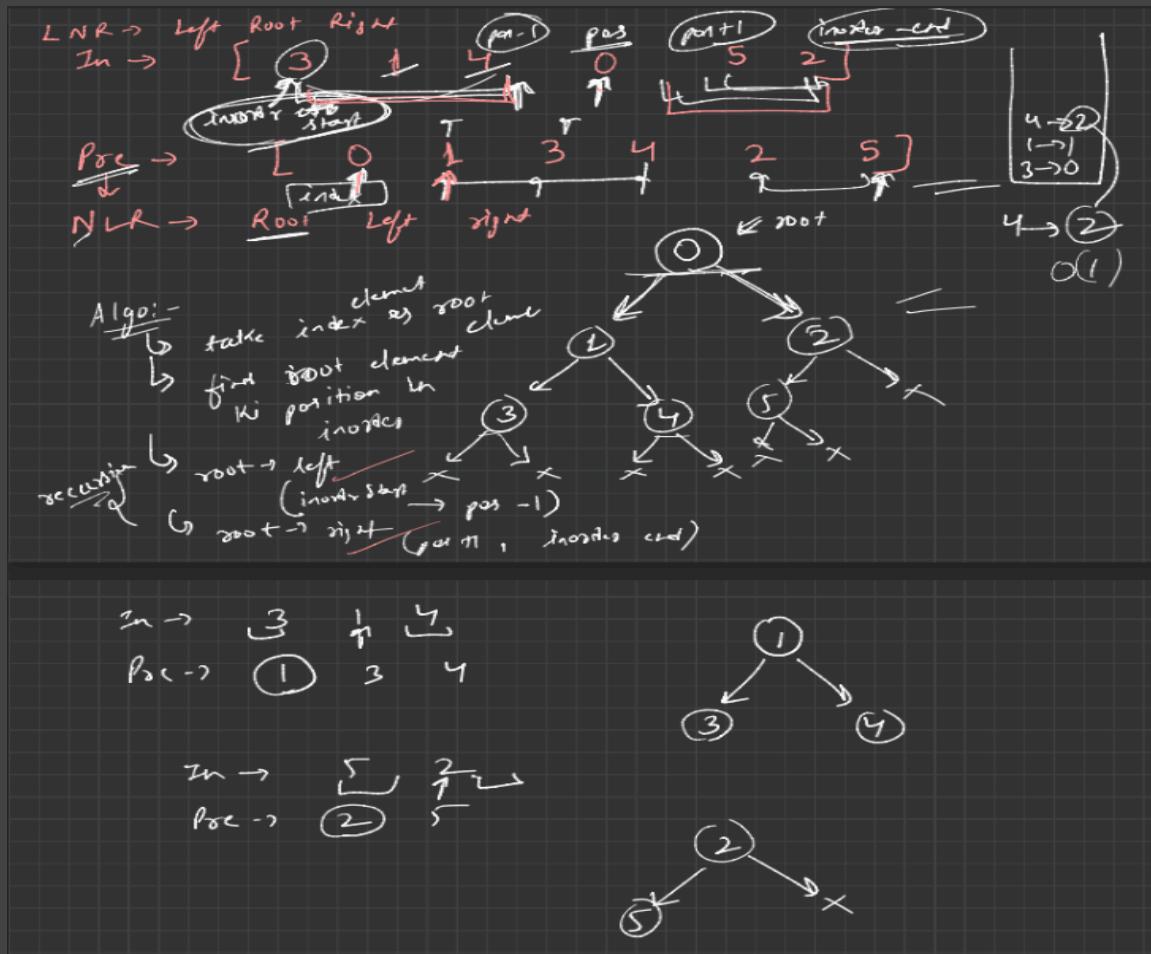
Maximum Sum Of Non-Adjacent Nodes:



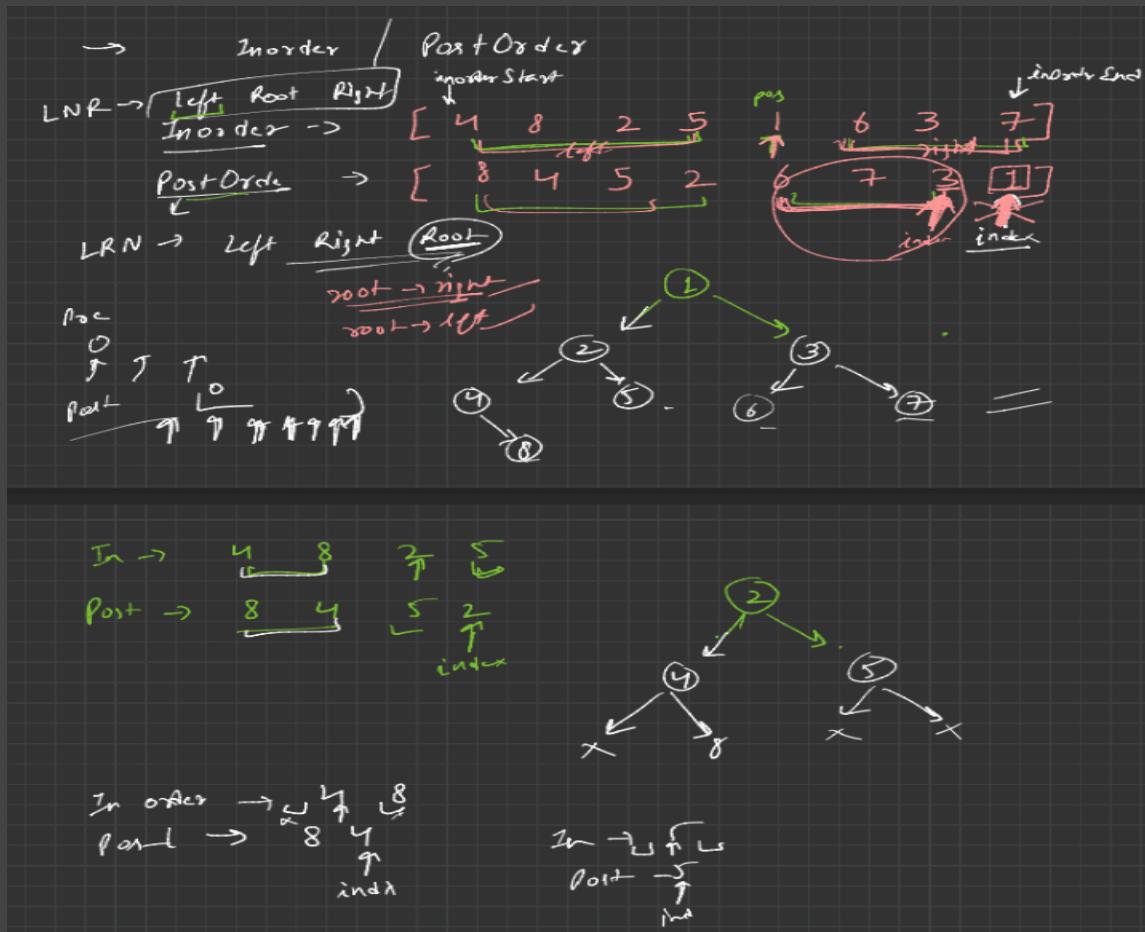


Construct Tree From InOrder And PreOrder:

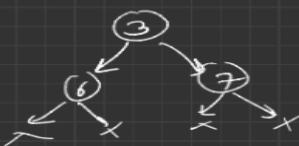




Construct Tree From InOrder And PostOrder:



In \rightarrow 6 3 7
 Post \rightarrow 6 7 3
 in+n



$\rightarrow BT \rightarrow construct$

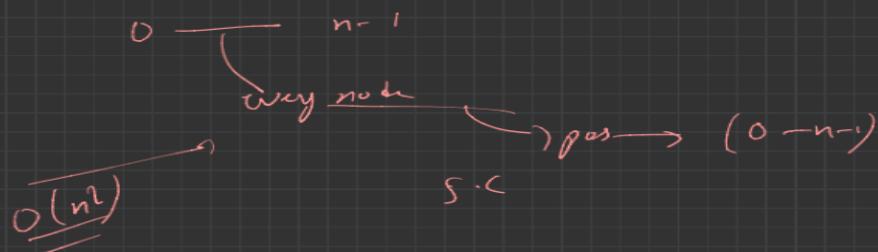
$\rightarrow \underline{In} / \underline{Post} \Rightarrow =$

$\rightarrow \underline{In} / \underline{Post} \Rightarrow =$

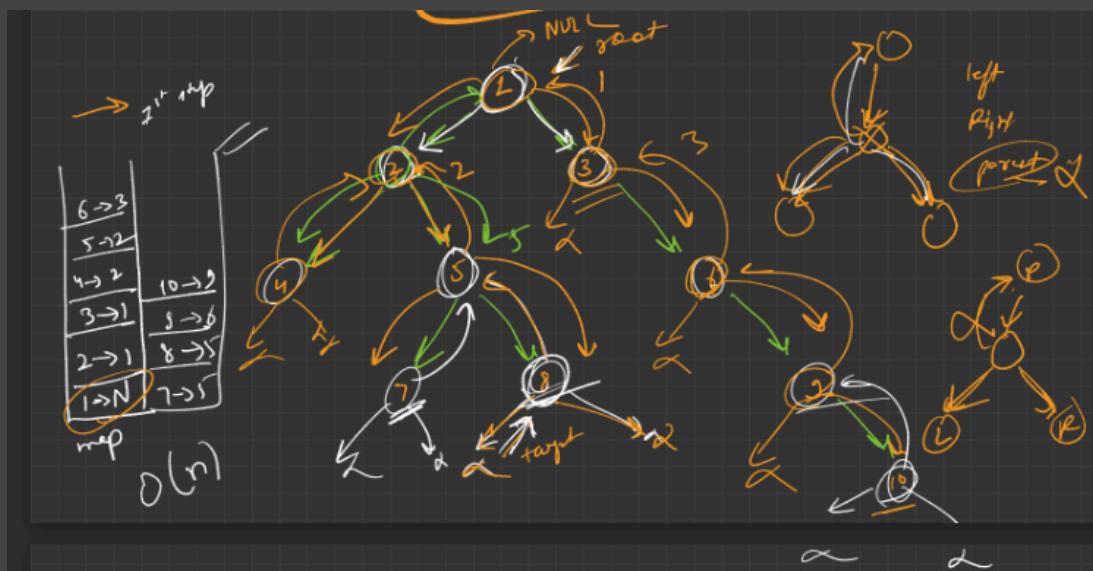
T.C / S.C

$O(n \log n)$

$O(n^+ \rightarrow O(n \log n))$



Minimum Tree To Burn The Entire Binary Tree:



approach:-

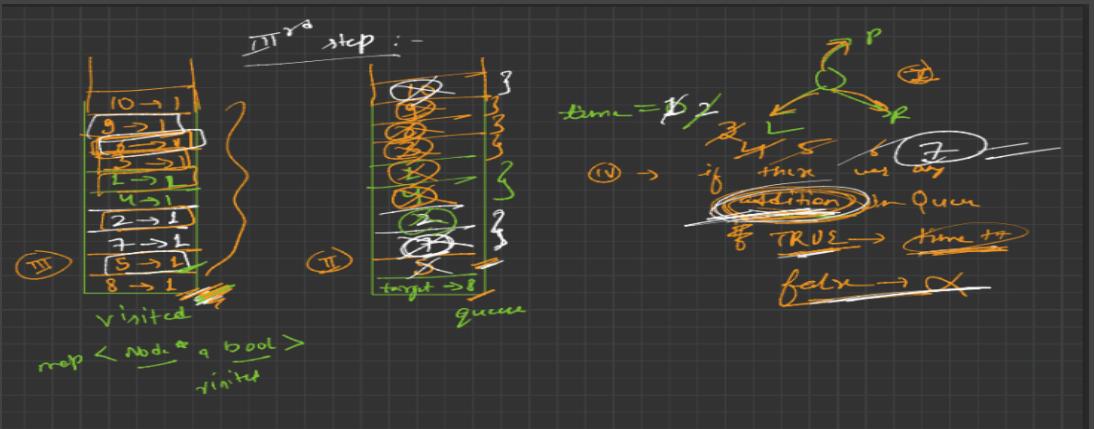
1st step

node to parent mapping

map < Node*, Node* > node to parent mapping

$\Rightarrow L.O.T$

2nd step \rightarrow find target Node
 $\hookrightarrow O(H)$



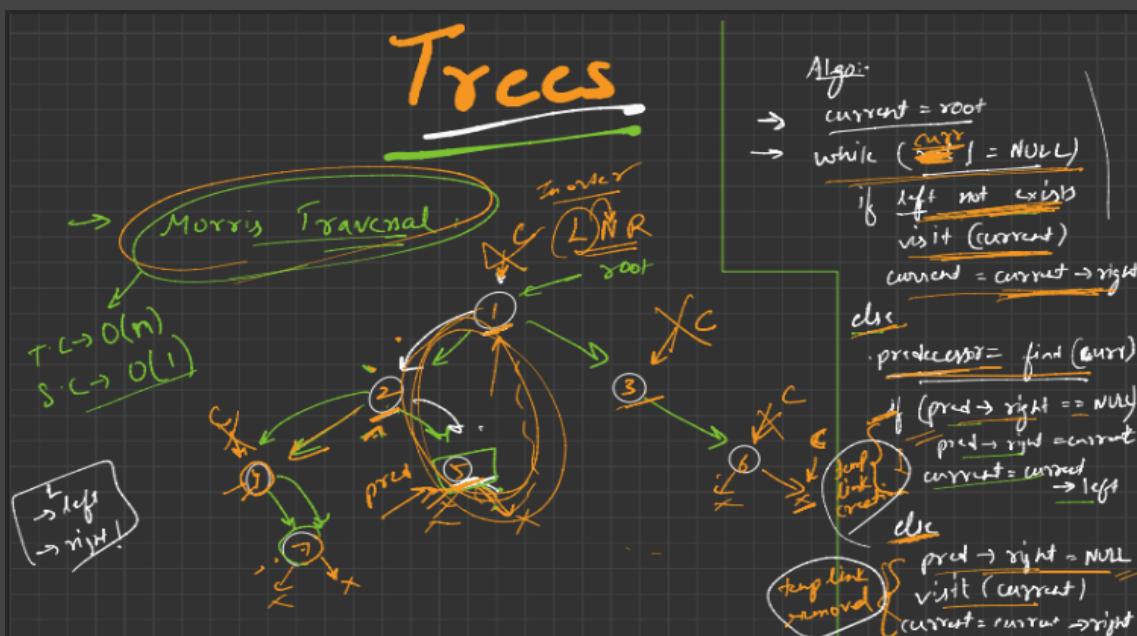
$$T \cdot \subset \Rightarrow \underline{\underline{O(N)}} + \underline{\underline{O(n)}}$$

= 

$\underline{\underline{O(N^{\log n})}}$

S.C $\rightarrow O(n) + O(N)$

Morris Traversal:



1 mark 4 7 2 5 1 3 6

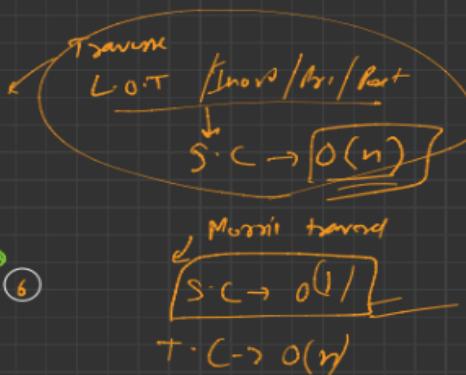
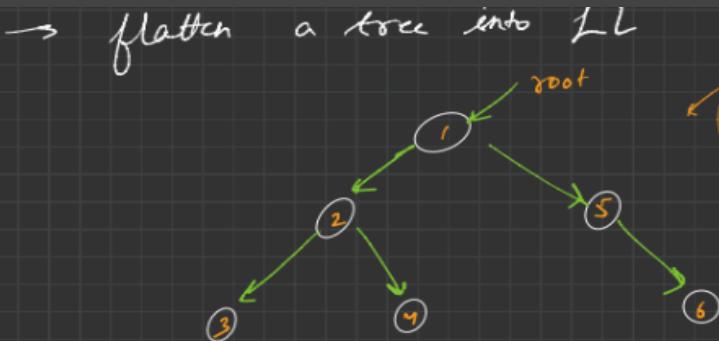
$\rho_{red} = \text{curr} \rightarrow \text{left}$

$$\rightarrow O(n)$$

$$T.C \rightarrow O(1)$$

while $\text{pred} \rightarrow \text{right}^! = \text{NULL}$ $\text{pred} \rightarrow \text{right}^! = \text{correct}$

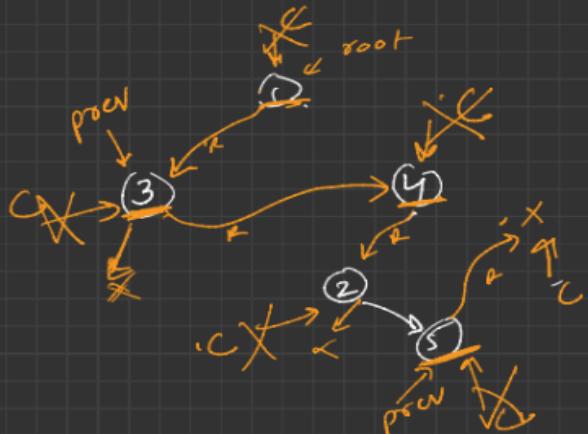
Flatten A Binary Tree To Linked List:



1 → traverse → each goeth node create
 Kriluge \times → in-place

2 → recursion → $O(n)$
 $O(n)$ $\rightarrow \times$

3 → Morris traversal



Alg - \rightarrow current = root

while (curr != NULL)

i

if curr left exists

i

predecessor {
 while (prev > right)
 prev = right;

prev > right = curr > right

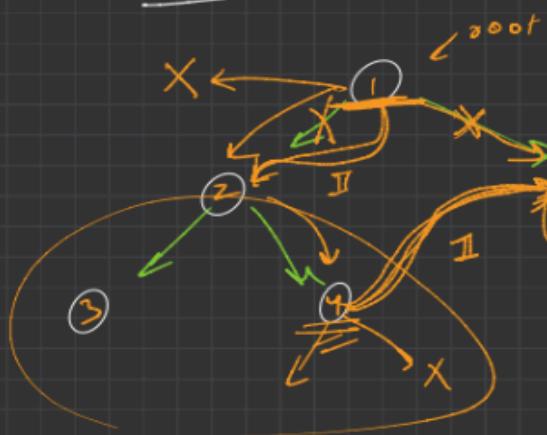
curr > right = curr > left

}

curr = curr > right;

}

Morris traversal



PerOrder \rightarrow N $\xrightarrow{\text{Root}}$ L $\xrightarrow{\text{R}}$

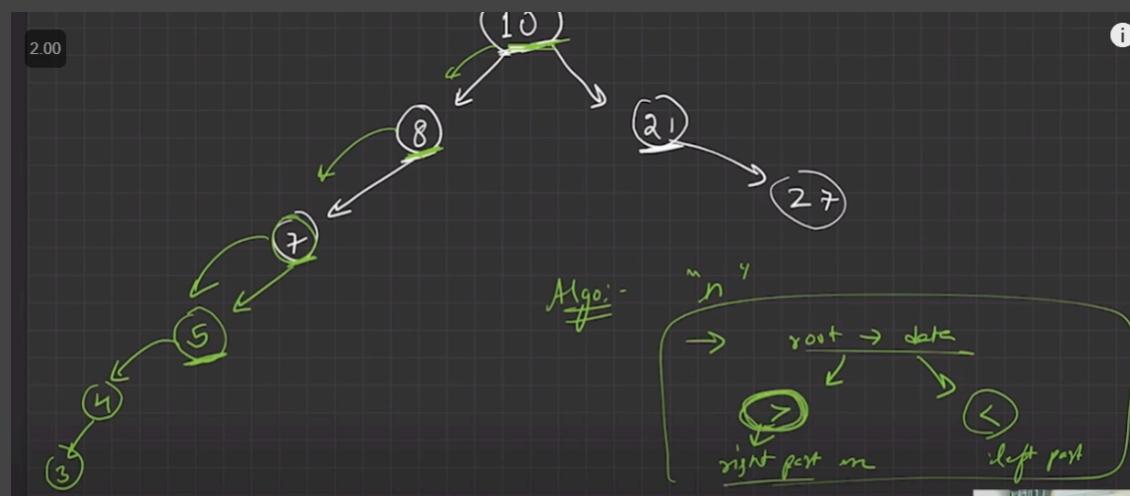
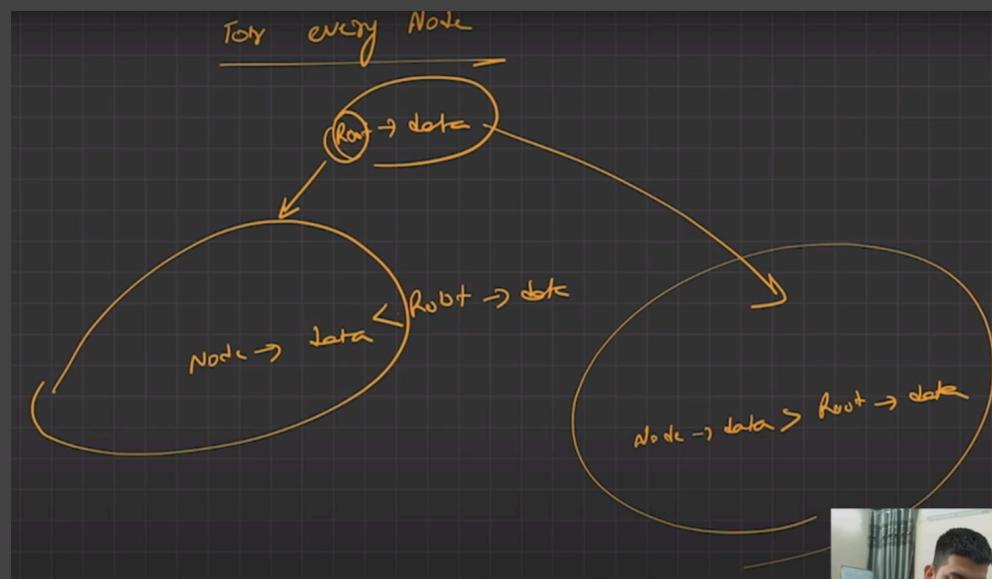
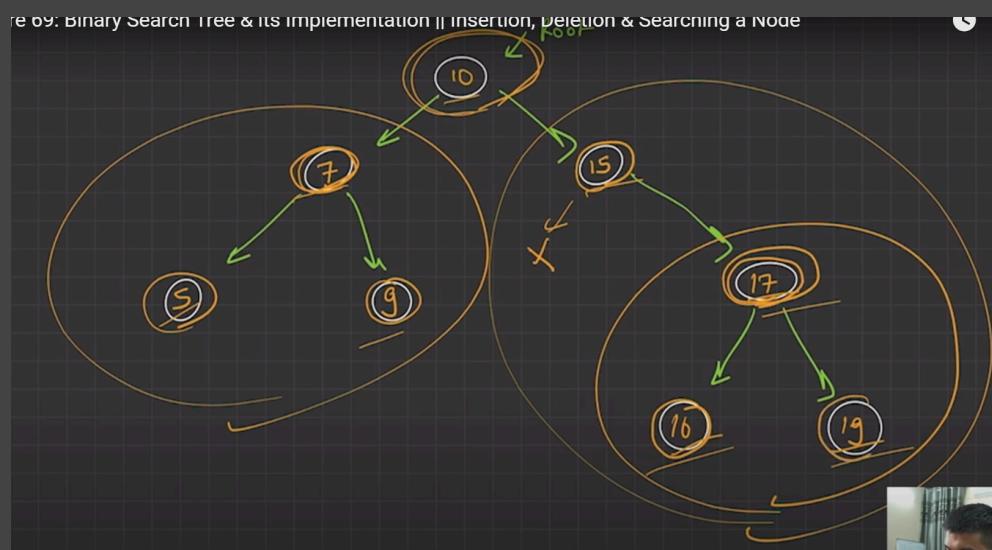
inorder predecessor
 \rightarrow right = curr > right

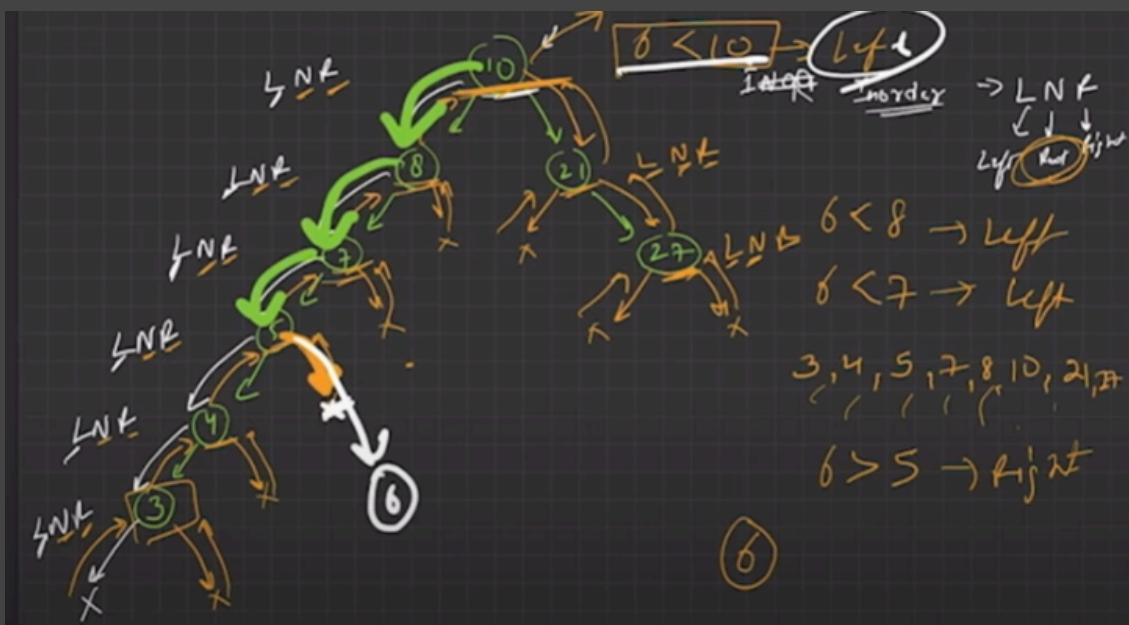
L \rightarrow R
 N \rightarrow L

N \rightarrow L
 L \rightarrow R

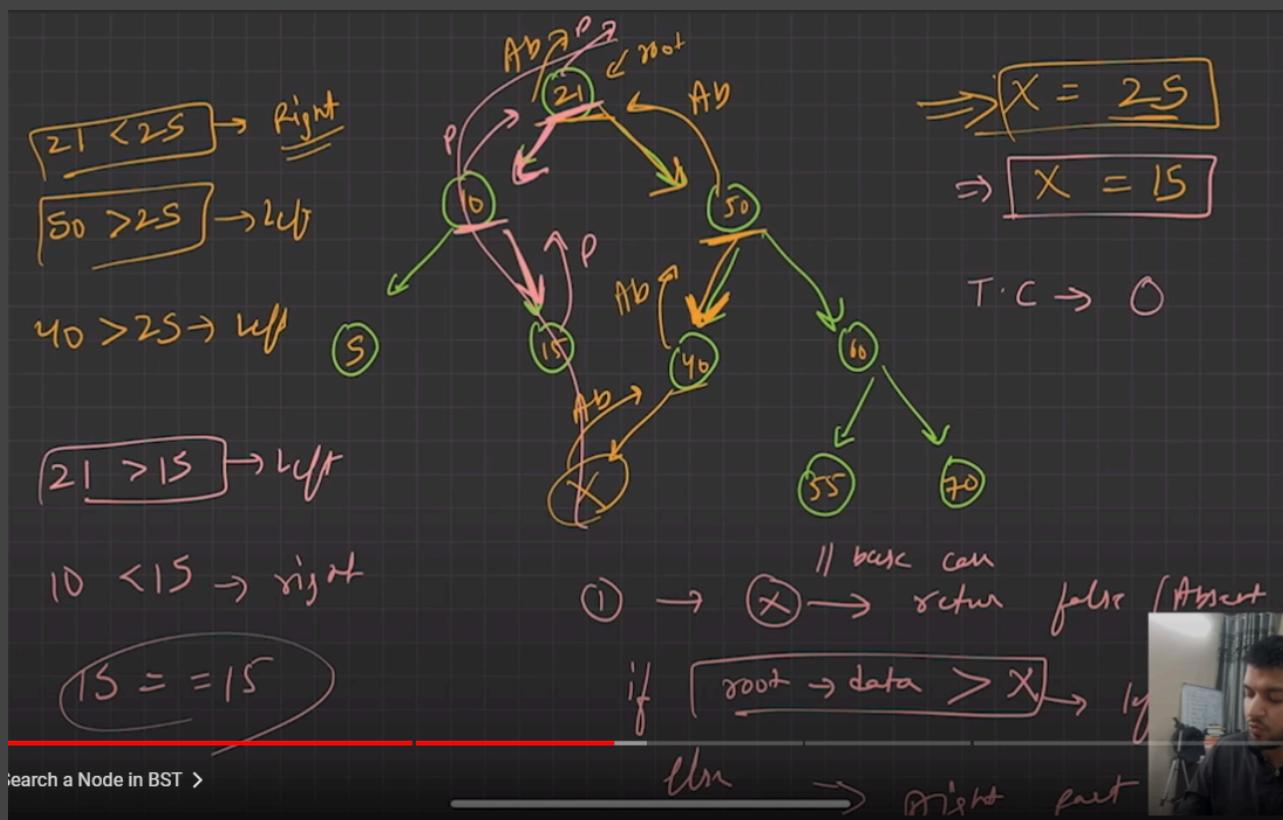
Binary Search Tree(BST)

Insert A Node In BST:



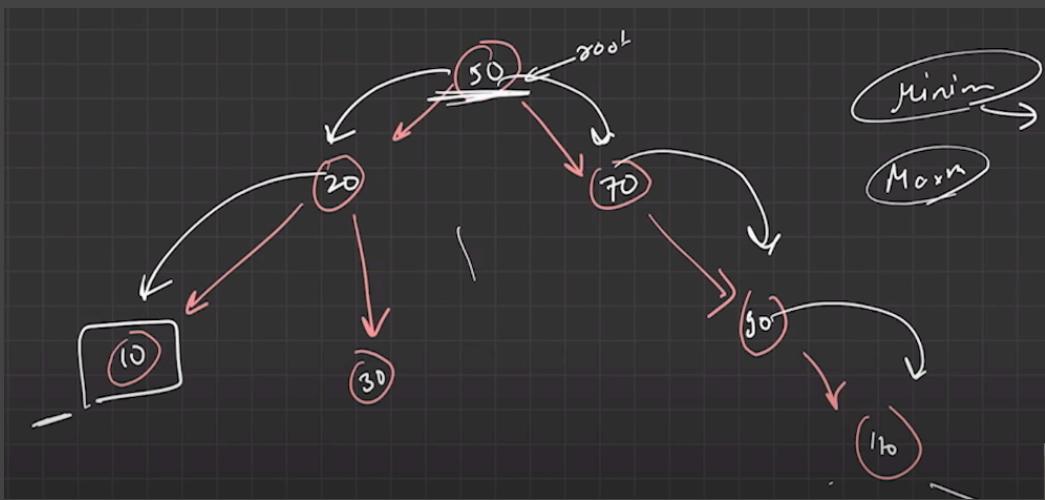


Search A Node In BST:



Minimum/Maximum Value In BST:

\Rightarrow Inorder of BST is sorted
(LNR)

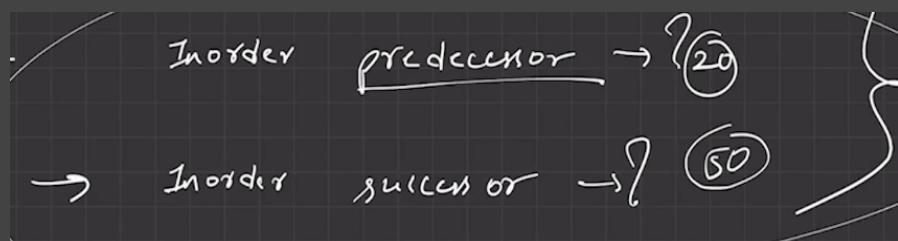


temp = root
 while (~~temp~~ → left != NULL)
 {
 temp = temp → left
 }
 return temp

temp = root
 while (~~temp~~ → right != NULL)
 {
 temp = temp → right
 }
 return temp

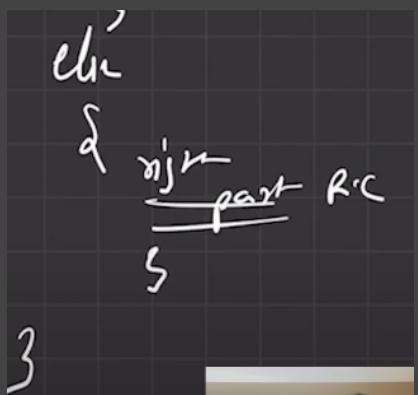
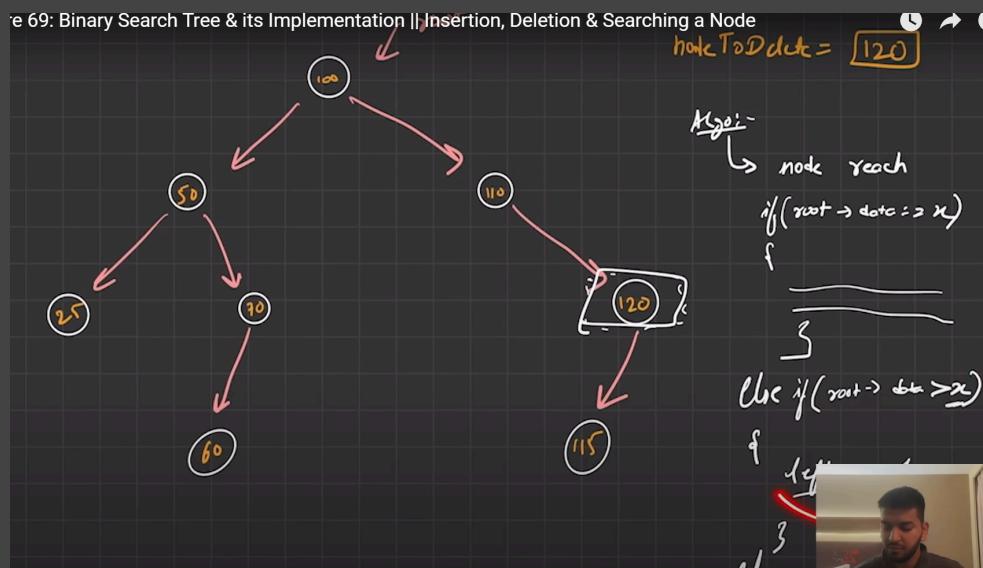
Inorder Predecessor In BST:

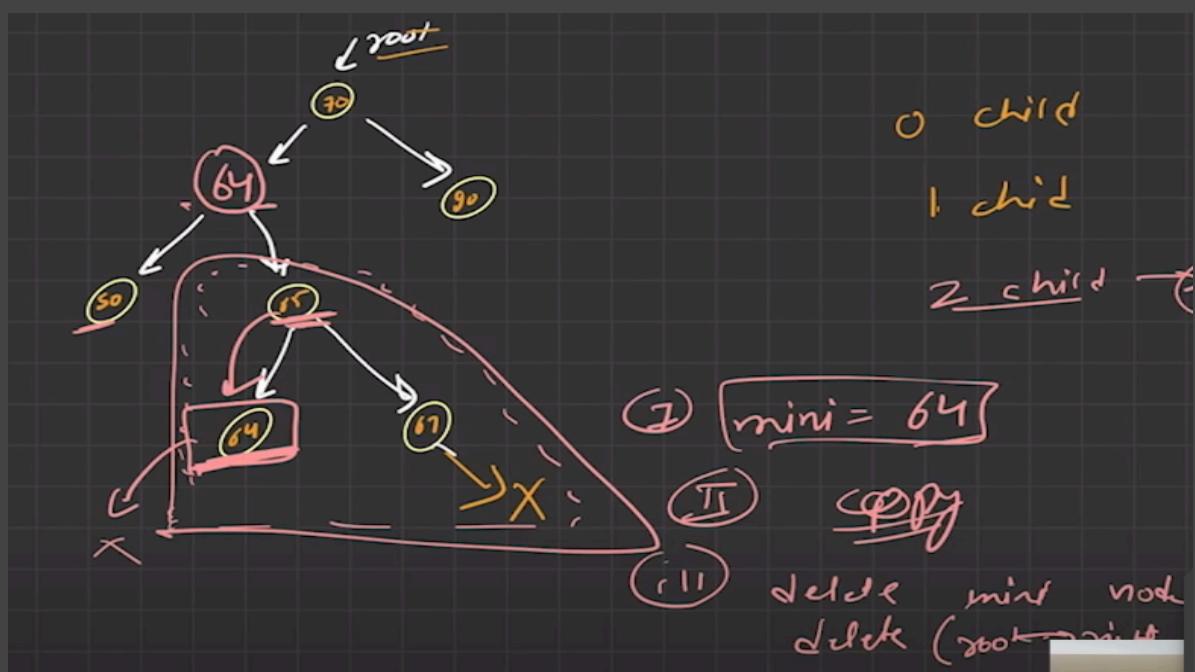
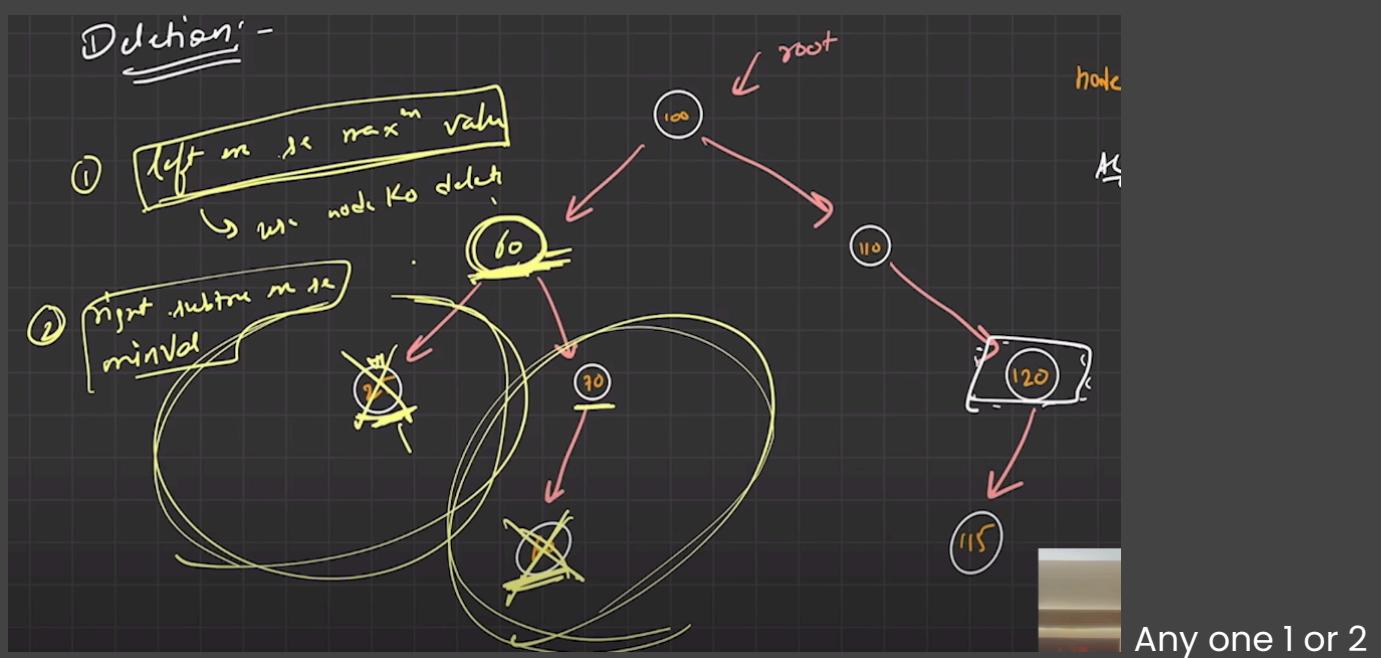
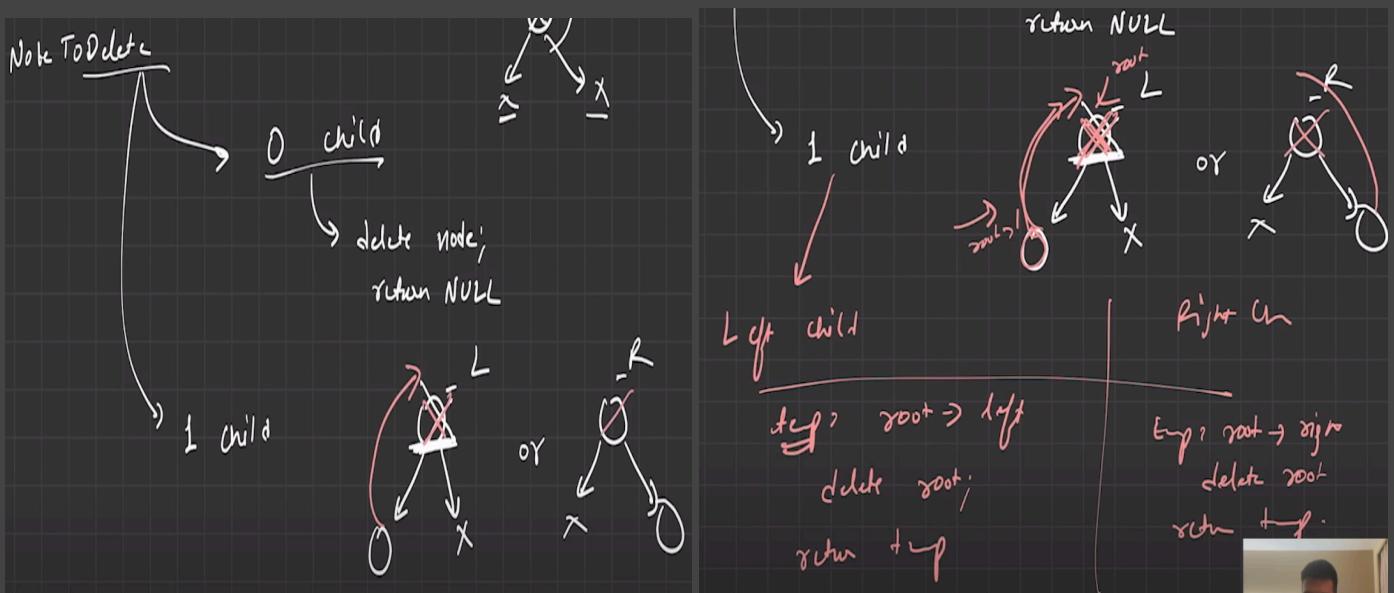
Inorder Successor In BST:



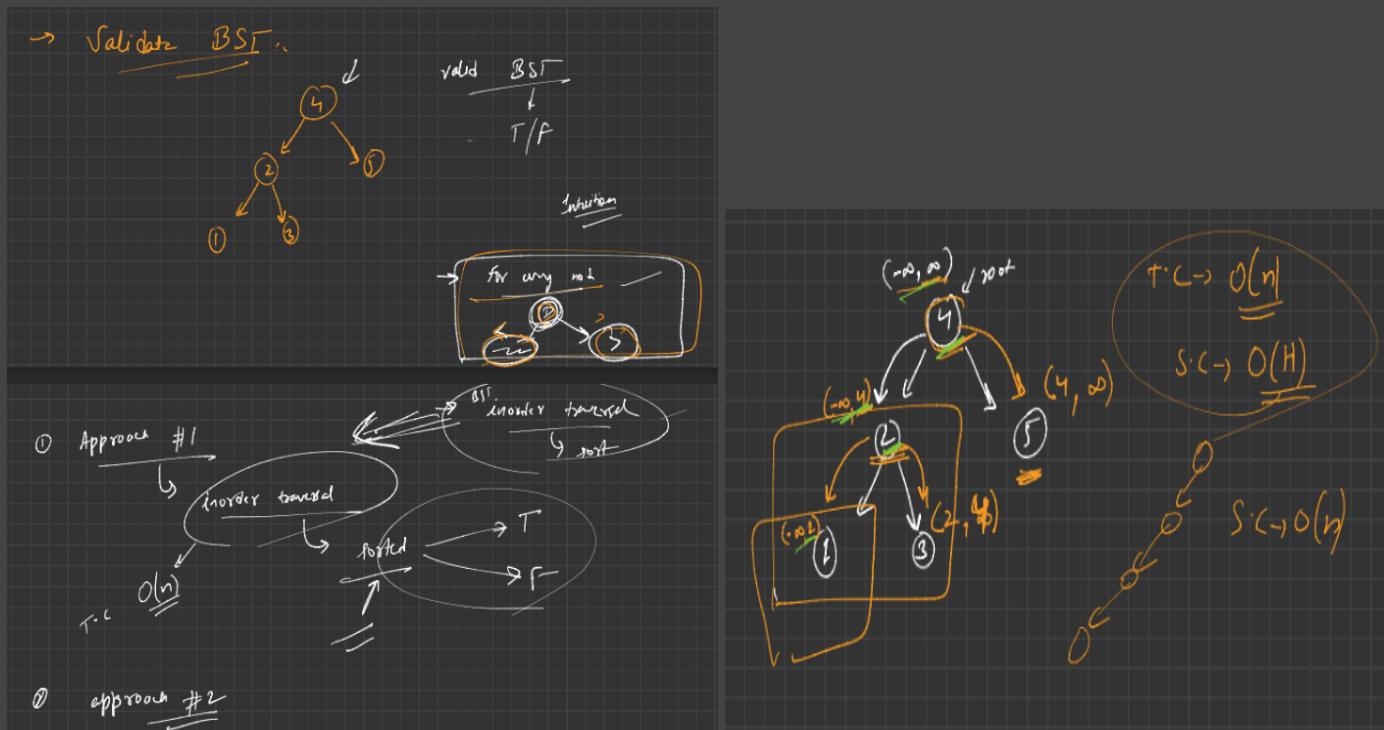
110
Printing Inorder
10 20 30 50 70 90 110
Printing Preorder

Delete A Node In BST:

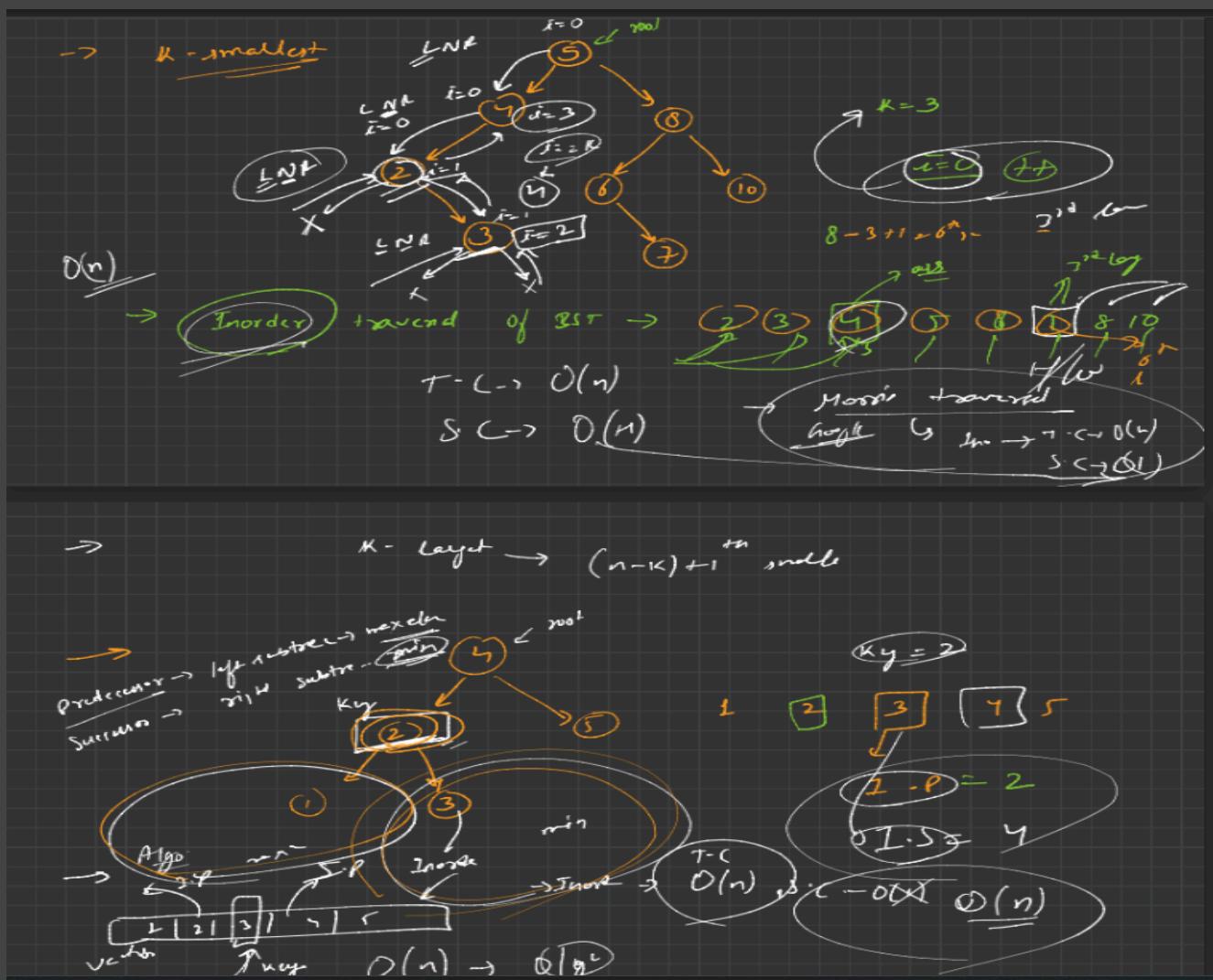


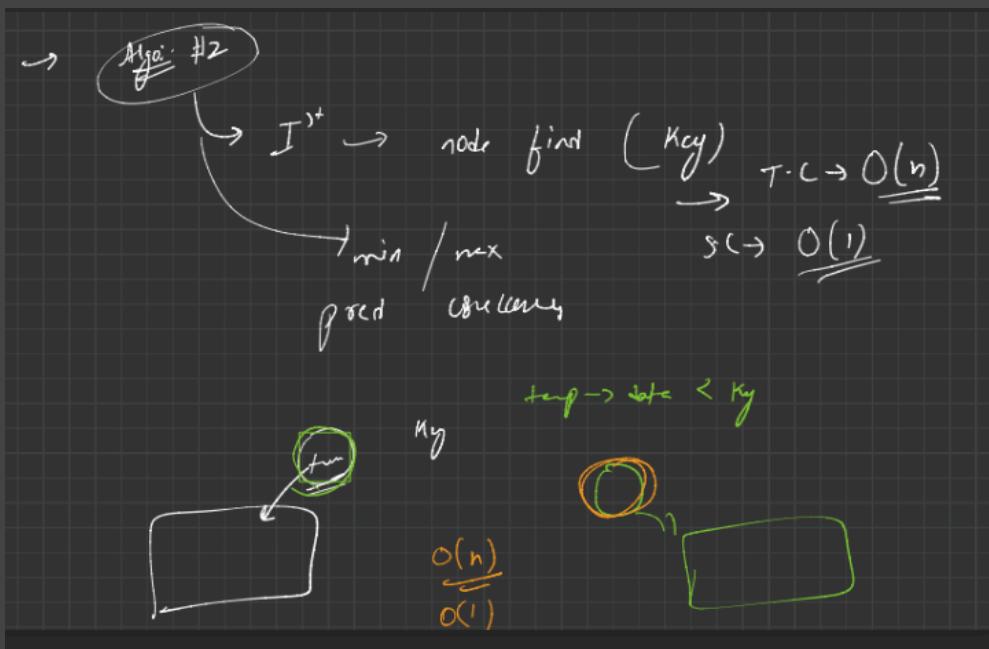


Validate BST:

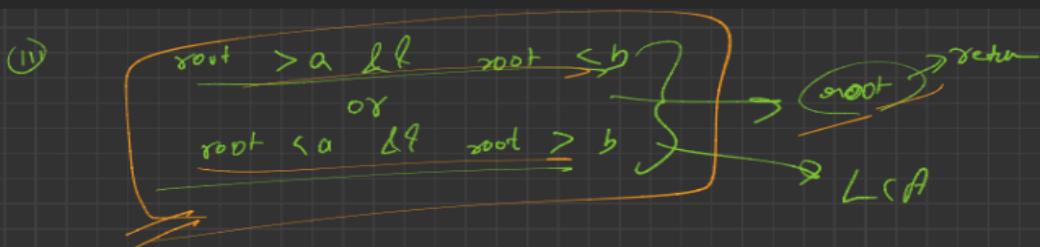
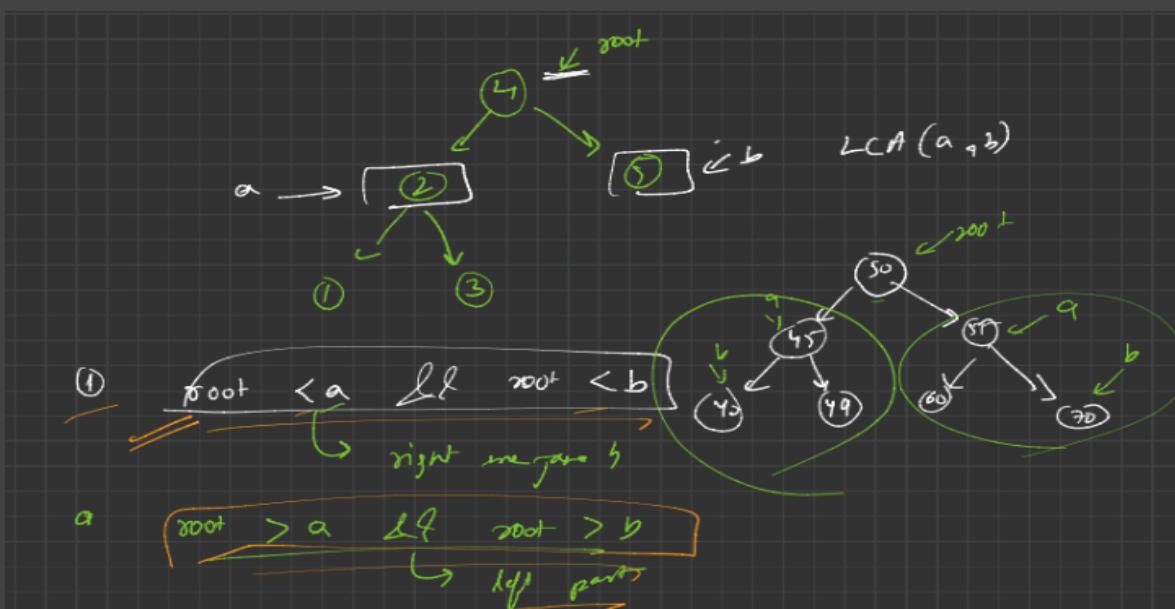


Kth Smallest/Largest Element In BST:



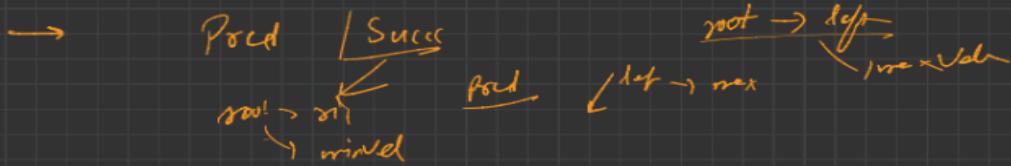


Lowest Common Ancestor In BST:

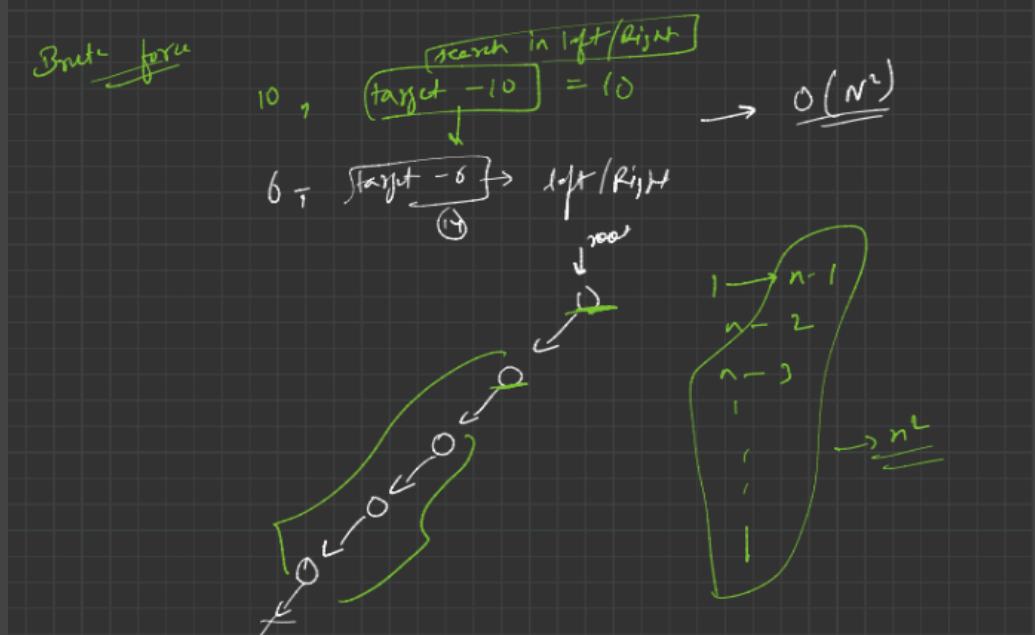
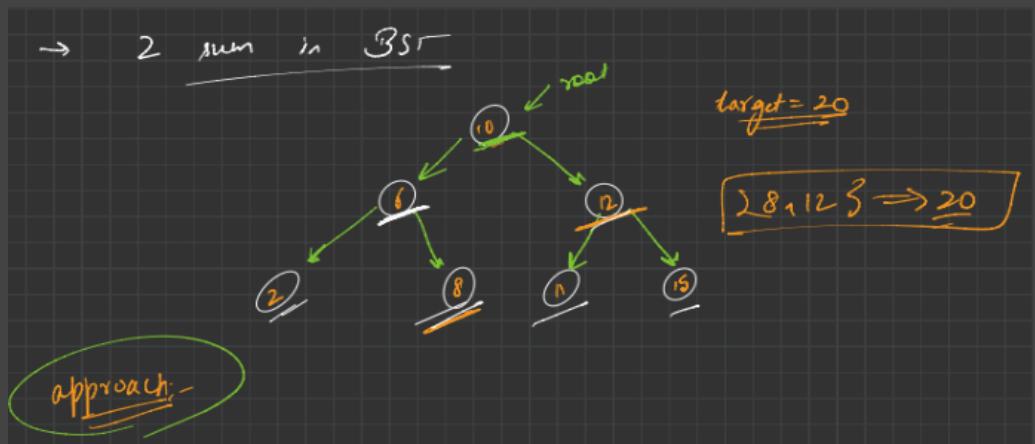


$\rightarrow K^m$ smaller / K^n longer

\rightarrow invalid BST

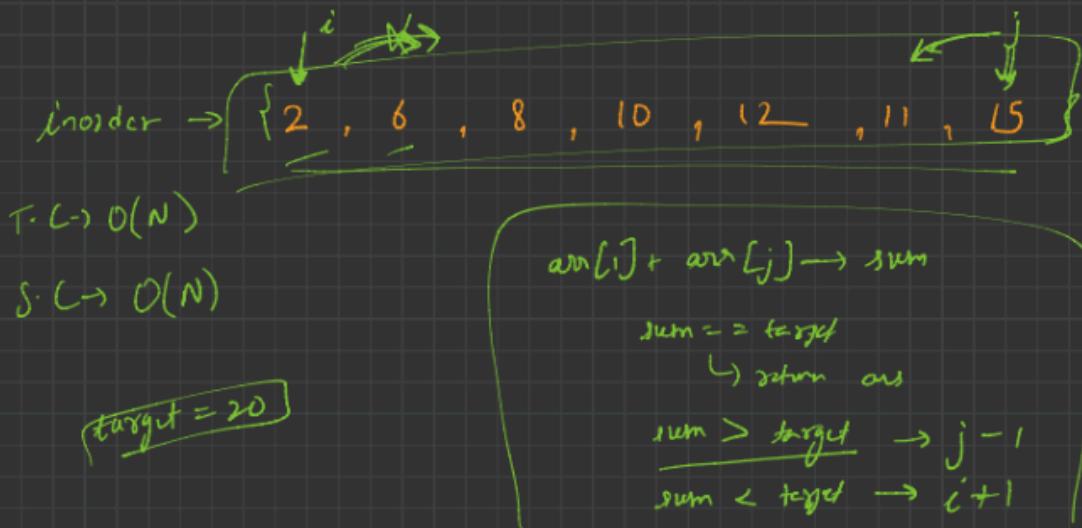


Two Sum In BST:

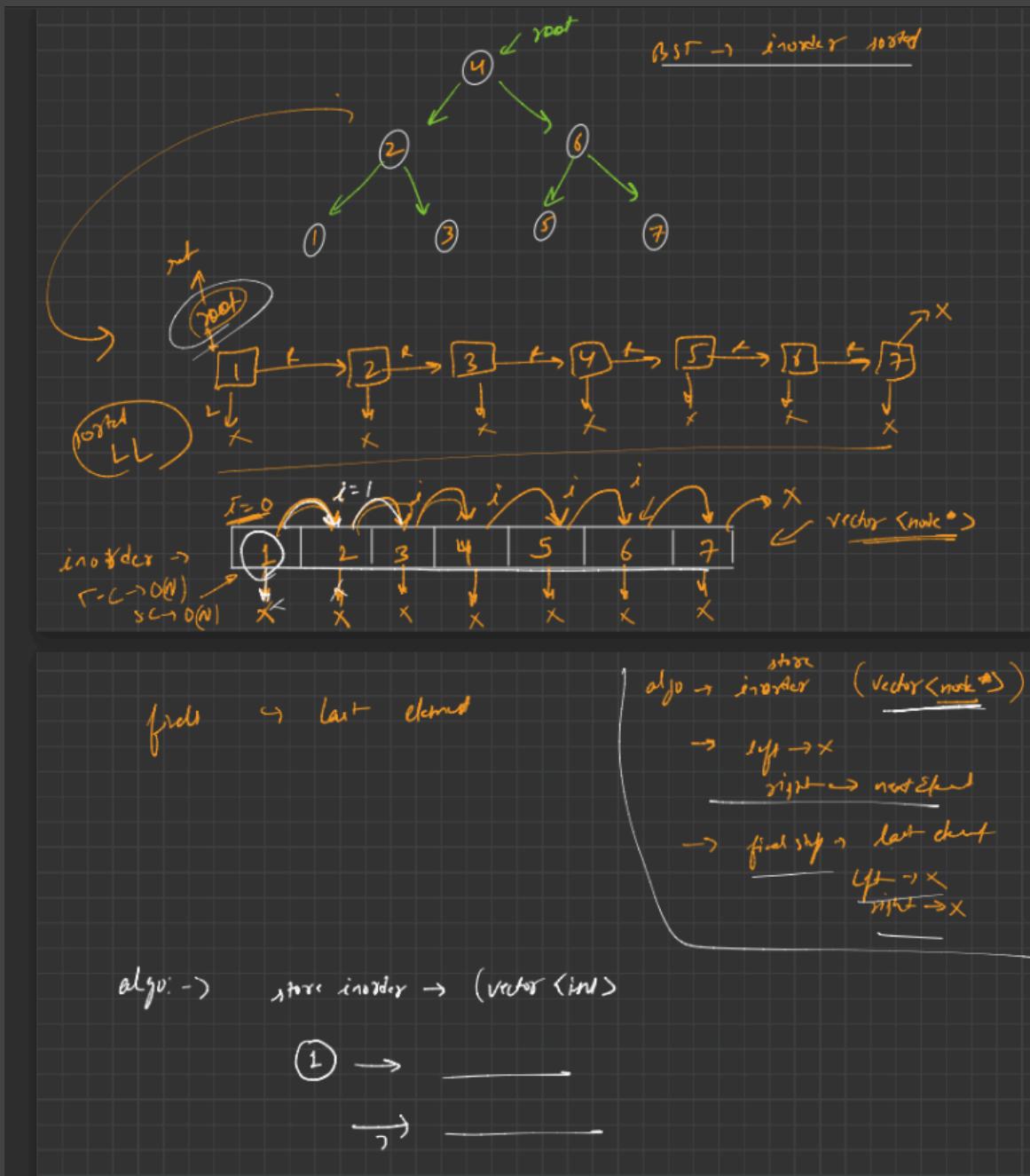


$\Rightarrow O(N) \rightarrow$ Single traversal

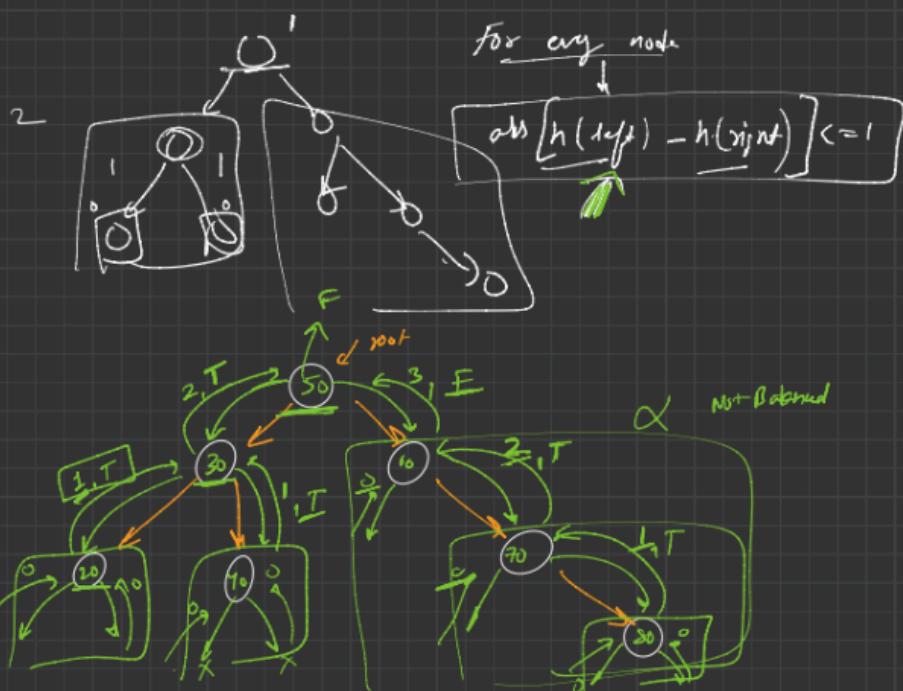
BST \rightarrow inorder sorted



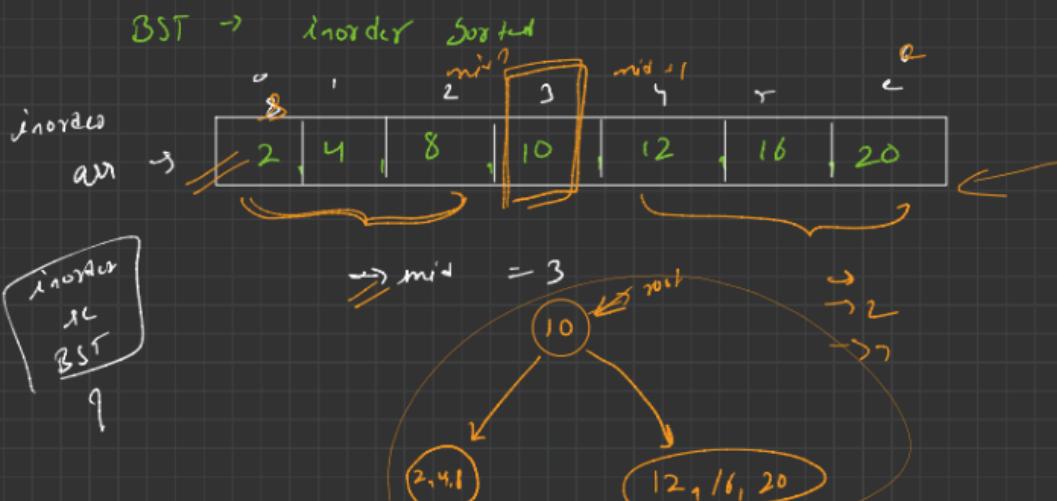
Flatten BST To A Sorted List:



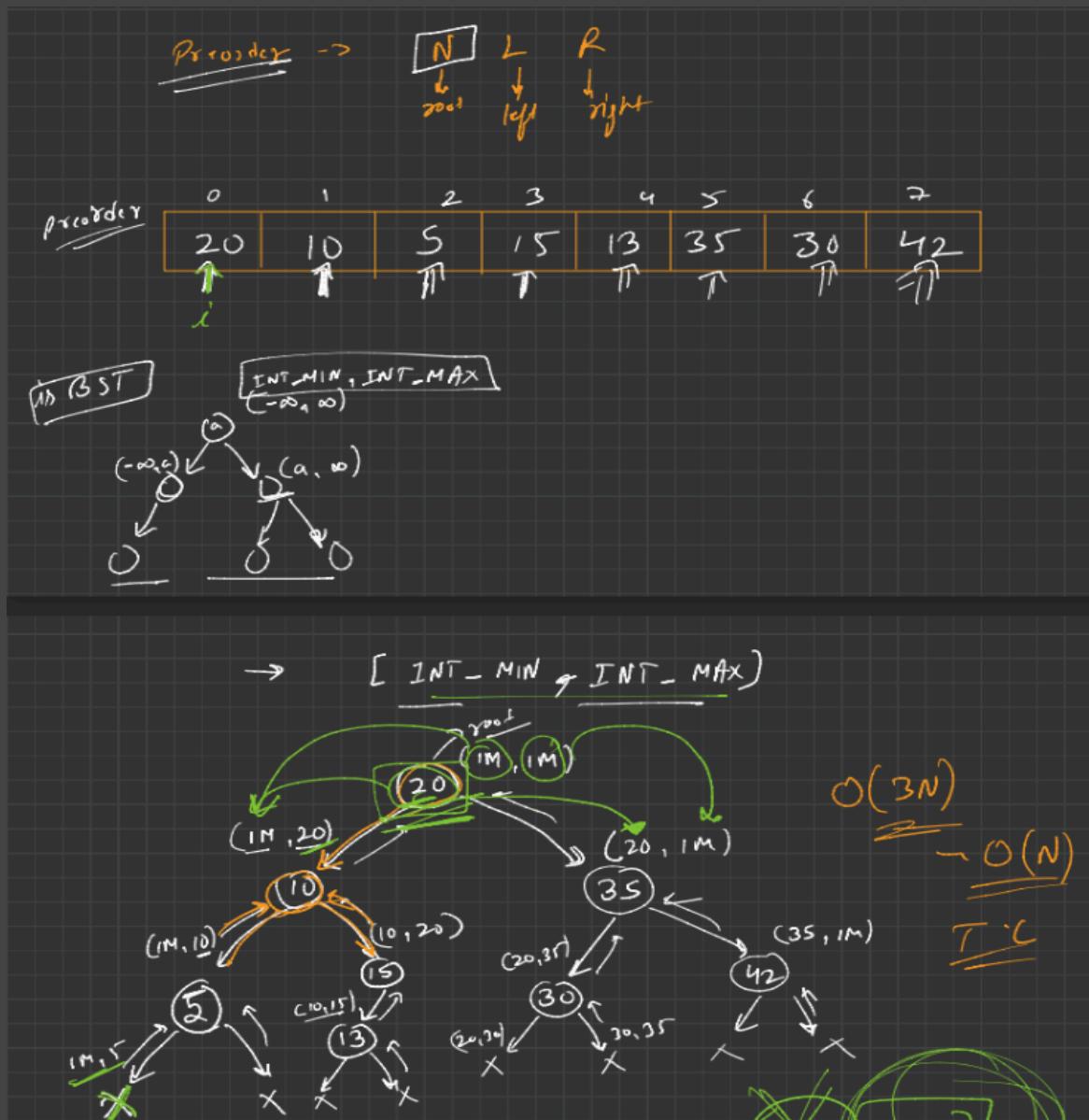
Normal BST To Balanced BST:



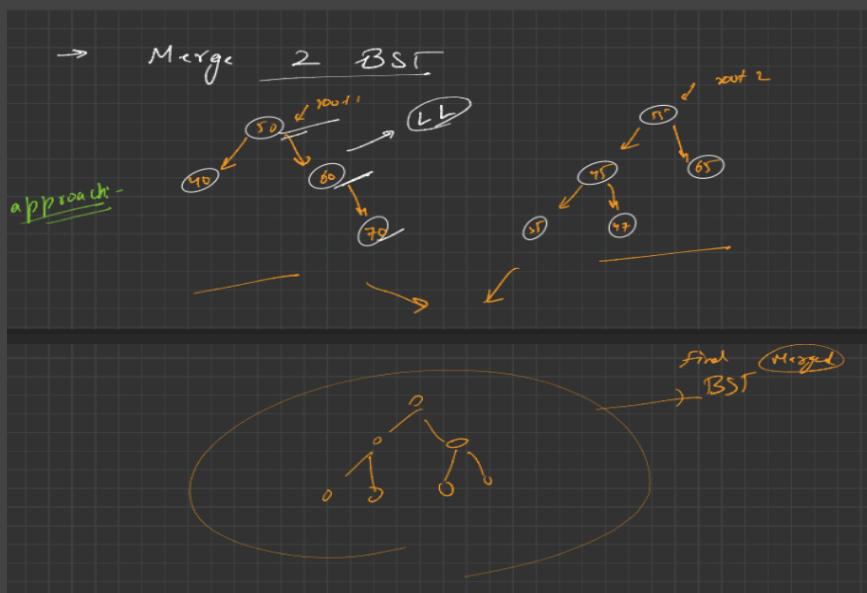
\rightarrow i/p \rightarrow Normal BST



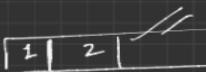
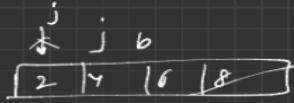
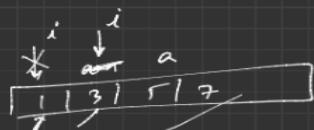
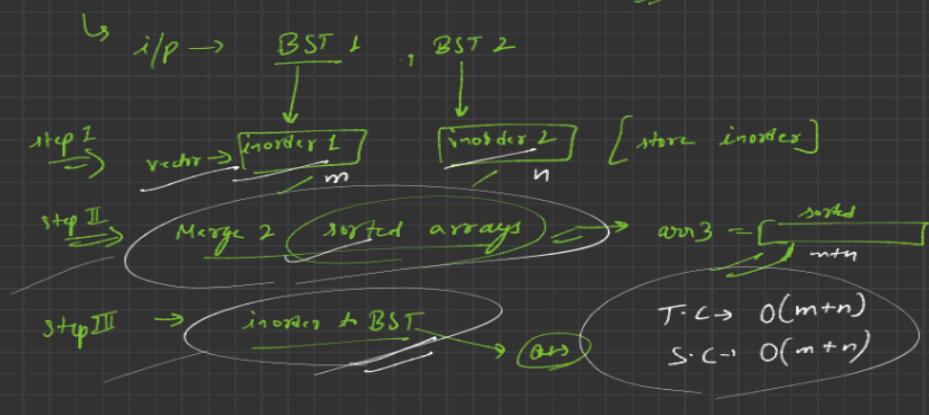
BST From Preorder Traversal:



Merge Two BST:



Approach #1

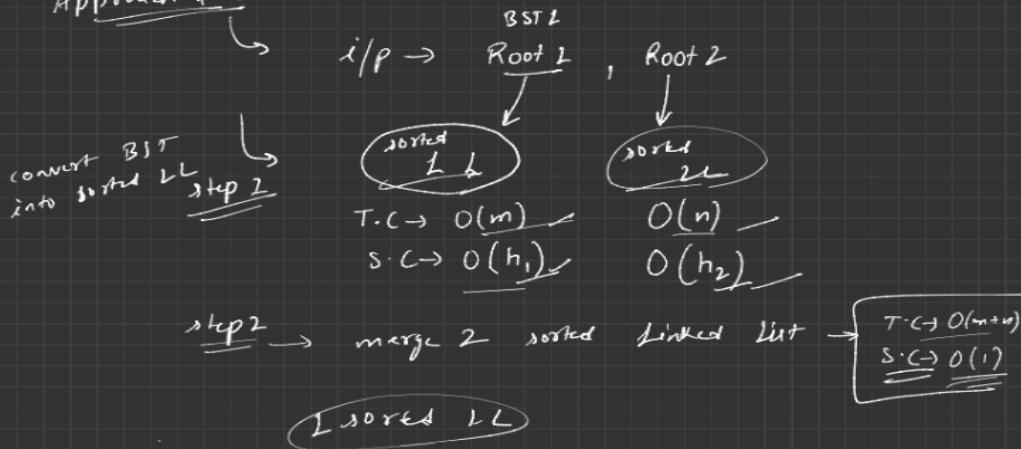


and $(a+b)$

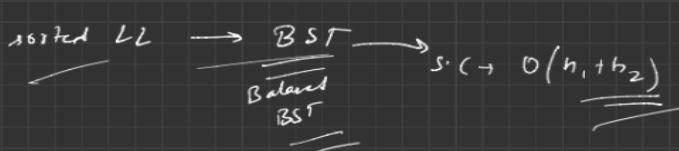
$\Rightarrow T.C \rightarrow O(m+n)$

$S.C \rightarrow O(h_1 + h_2)$

Approach #2

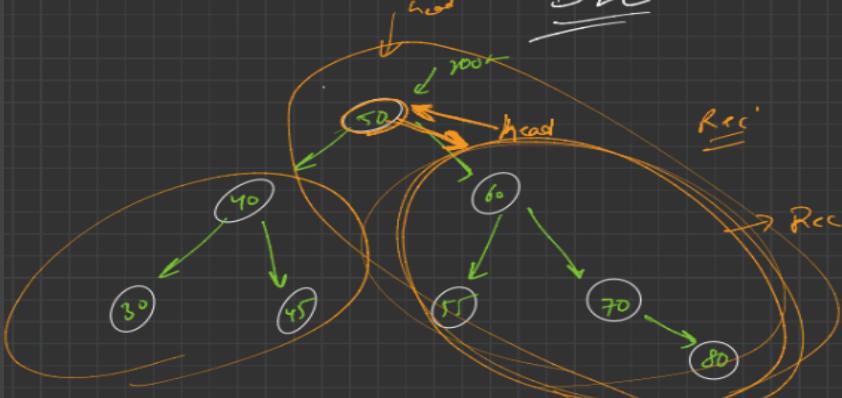


Step 3



- ① $(\text{convert a BST into sorted LL}) \rightarrow O(n)$
 $\rightarrow O(h)$
- ② $\boxed{\text{Merge 2 sorted linked lists}}$
- ③ $\boxed{\text{sorted LL} \rightarrow \text{BST}}$

→ convert a BST into DLL $\underline{\underline{O(H)}}$

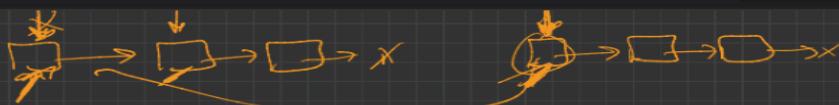
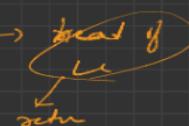


clgo → convert right subtree into LL → head of LL

→ root → right = head
head → left = root

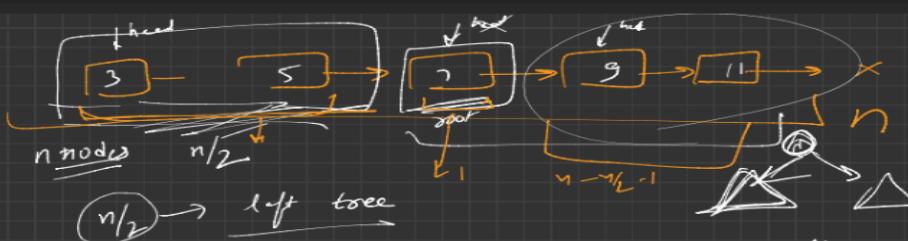
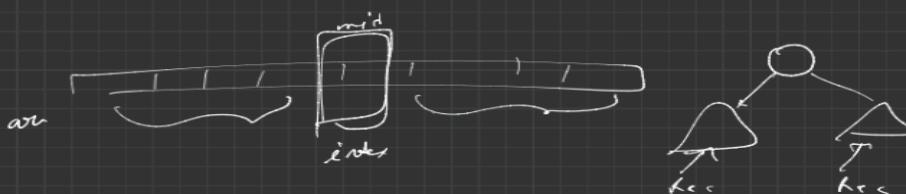
→ head = root

→ convert left part into LL → head of LL



head = NUL
tail = NUL

head

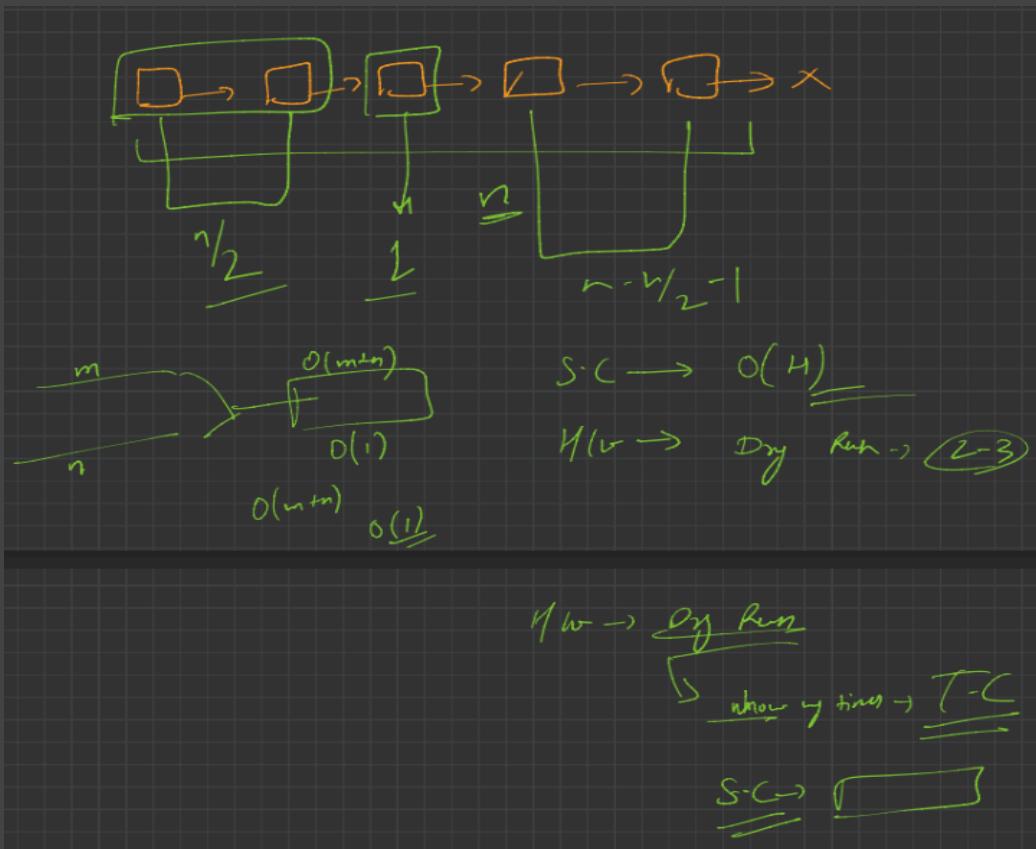


① $n/2 \rightarrow$ left tree \Rightarrow *left

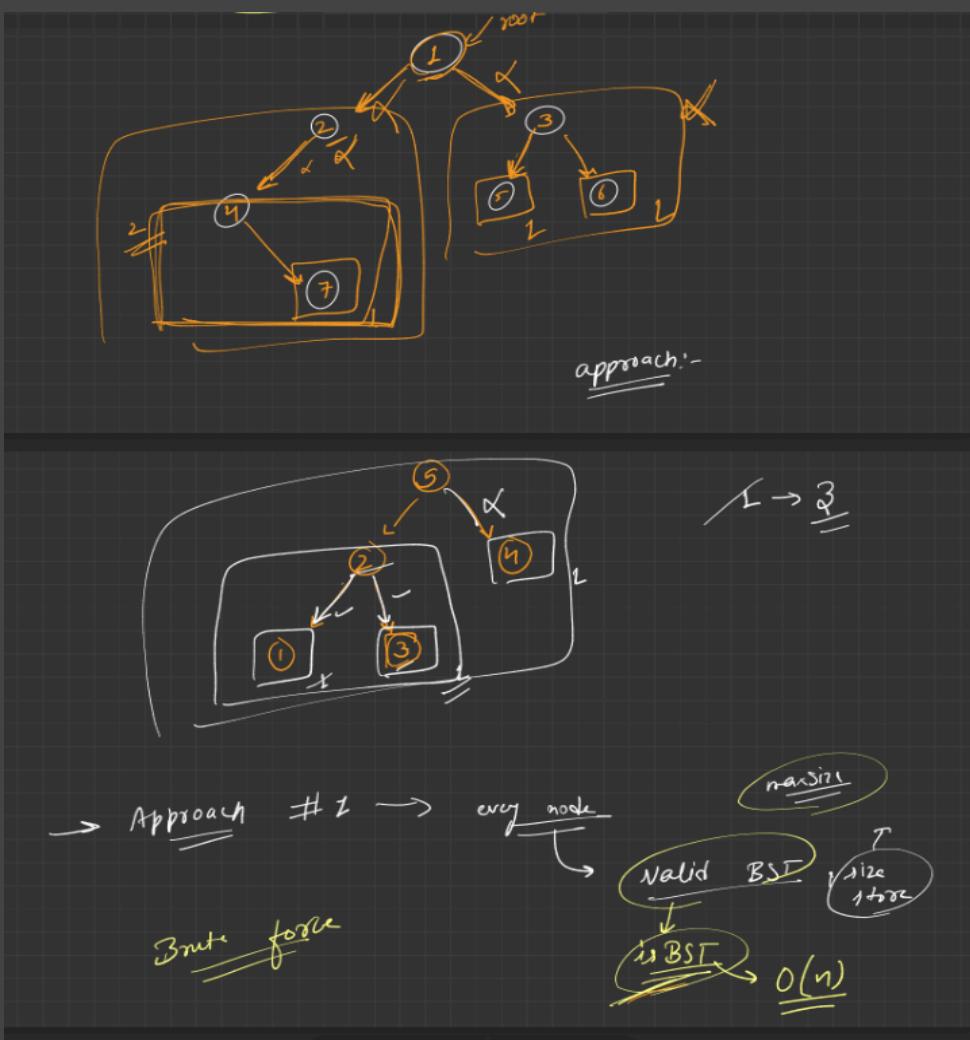
② create root
root → left = left

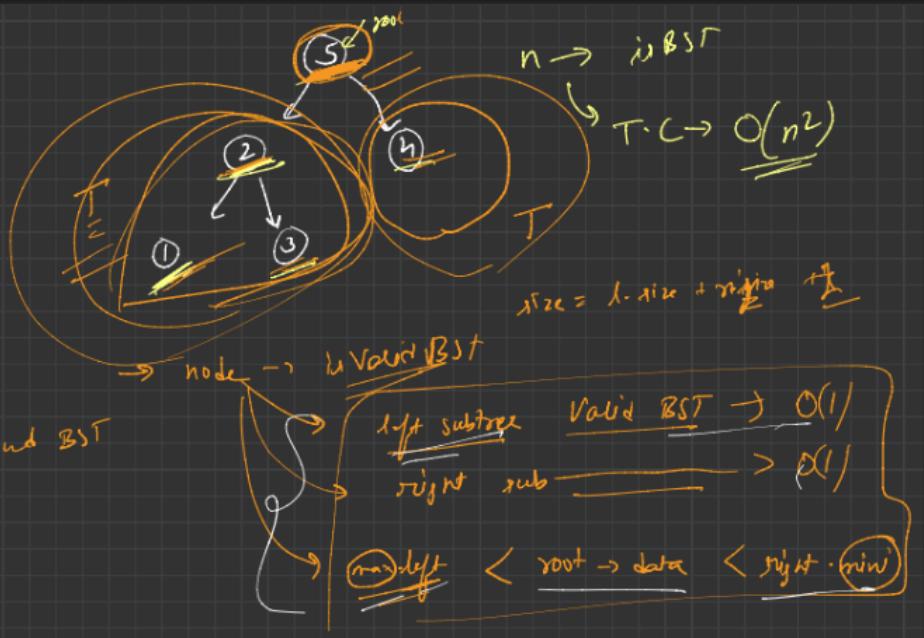
③ head → next

④ right subtree \Rightarrow tail
 $root \rightarrow right = Rec(right, n - n/2 - 1);$

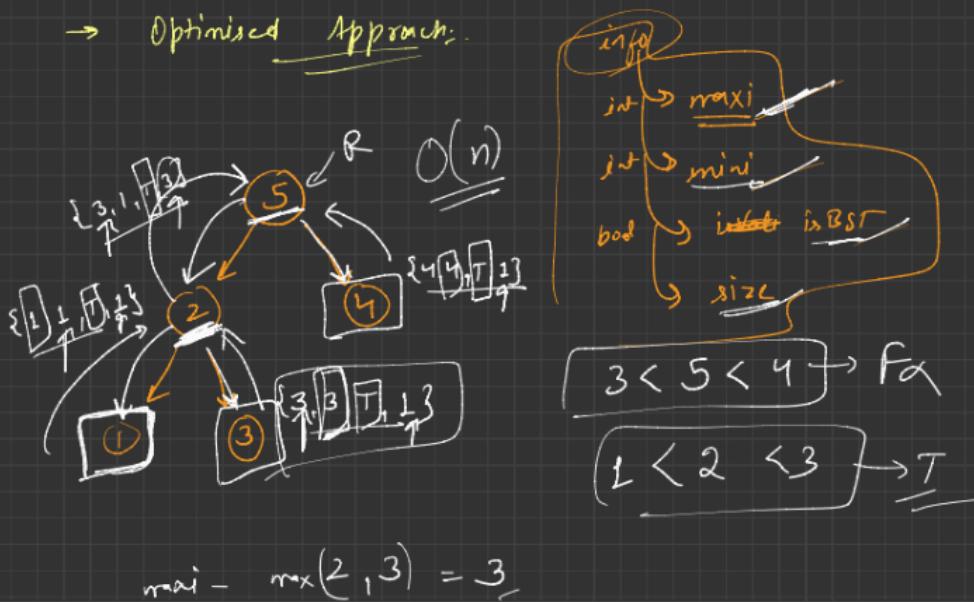


Largest BST In A Binary Tree:





\rightarrow Optimised Approach:



$$\text{max} = \max(2, 3) = 3$$

$$\begin{aligned}
 \text{min} &= \min(2, 1) = 1 \\
 \text{Valid} &= T \\
 \text{size} &= 1 \cdot \text{size} + 2 \cdot \text{size} + 1 \\
 &= 1 + 1 + 1 = 3
 \end{aligned}$$

maxSize return

99.999%
Dry run \rightarrow 3-4 except

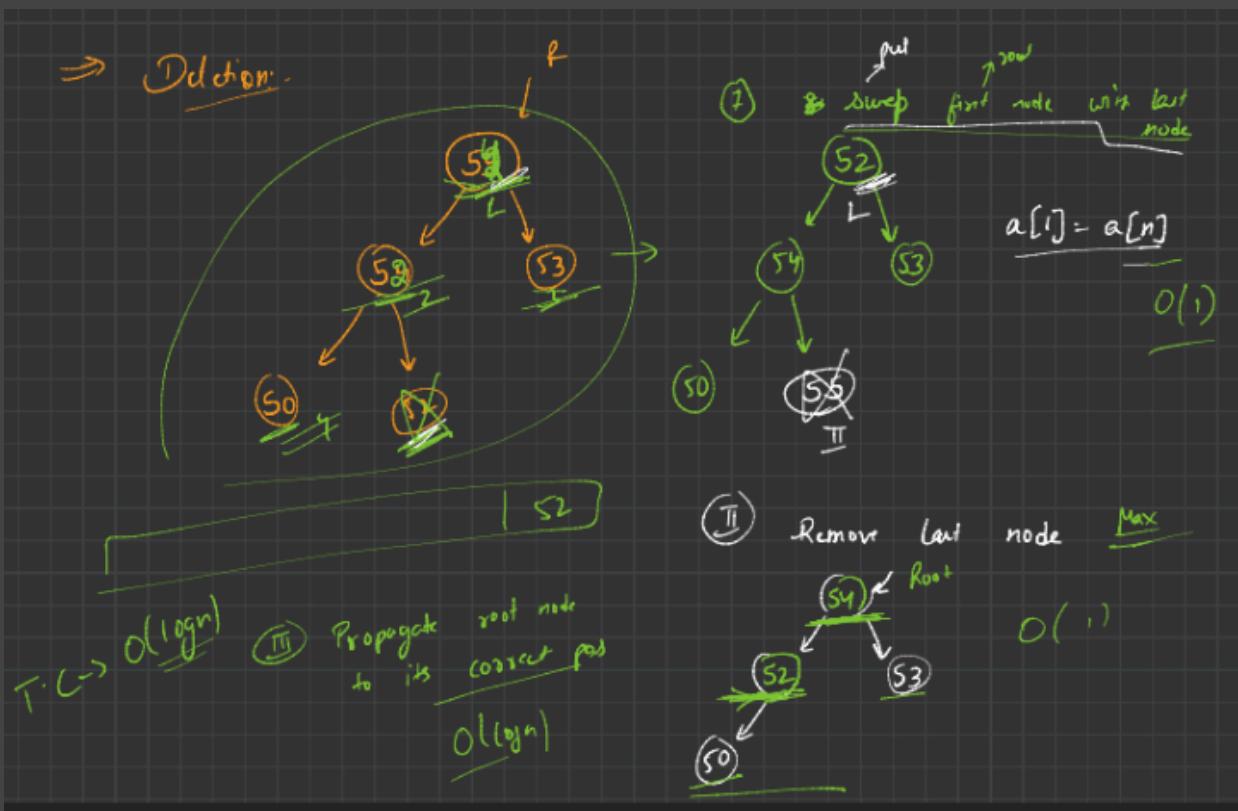
$$T.C \rightarrow O(n)$$

Heap

Insert:

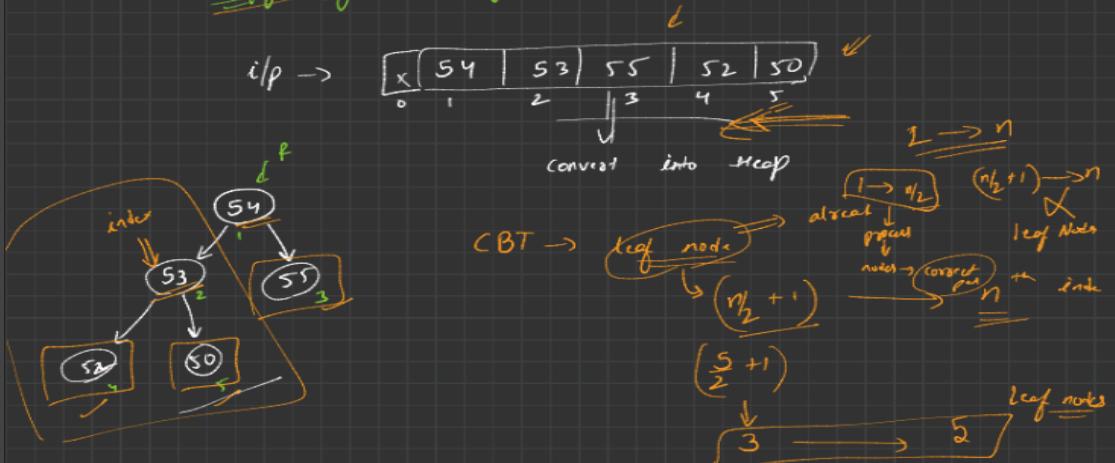
Delete:

\Rightarrow Deletion.



Heapify:

\Rightarrow Heapify algo $\Rightarrow O(\log n)$



for $(\frac{i=}{n/2} \rightarrow >0)$

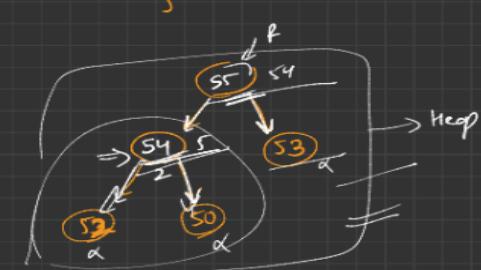
{ $\boxed{\text{heapify (arr, size, i);}}$ }

build heap

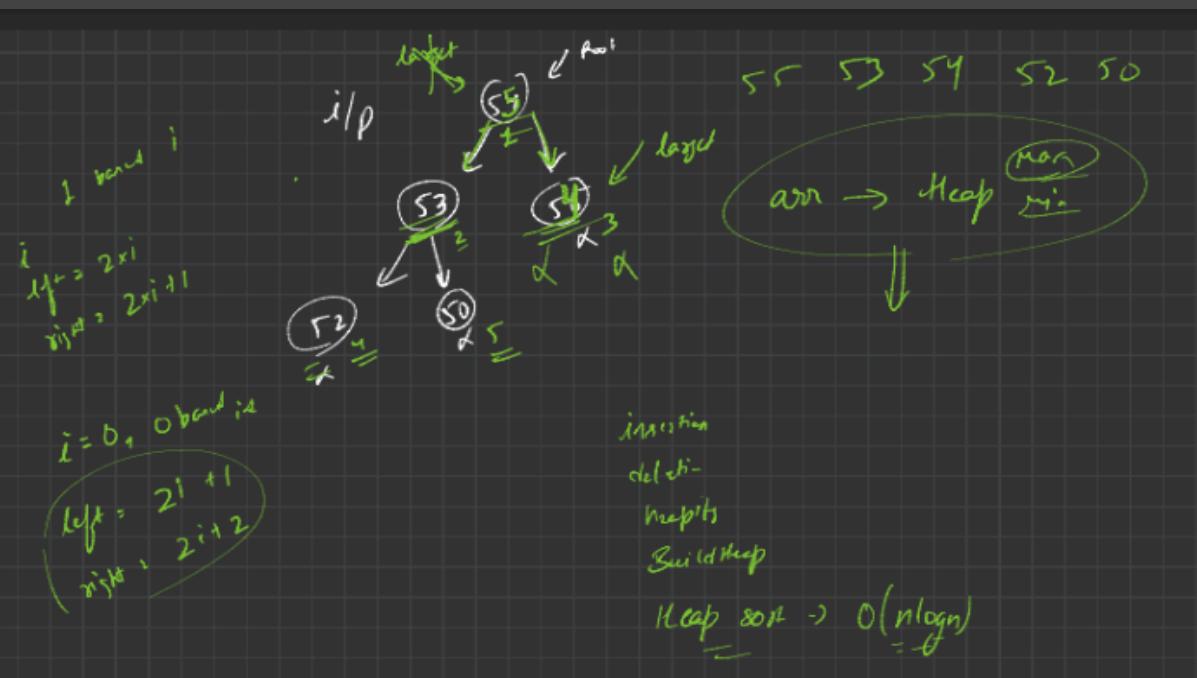
$O(n)$

if

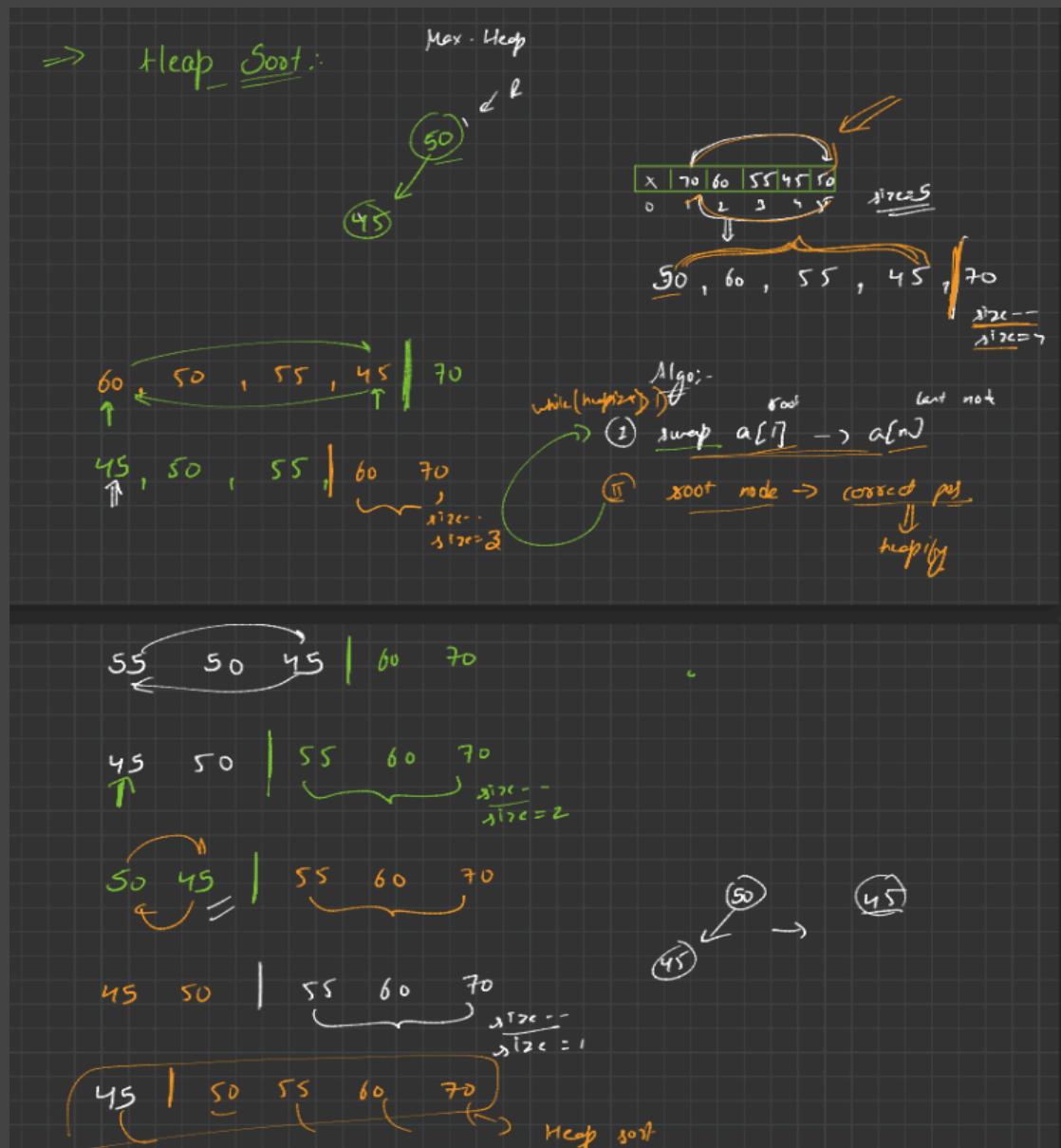
$\boxed{4/10}$

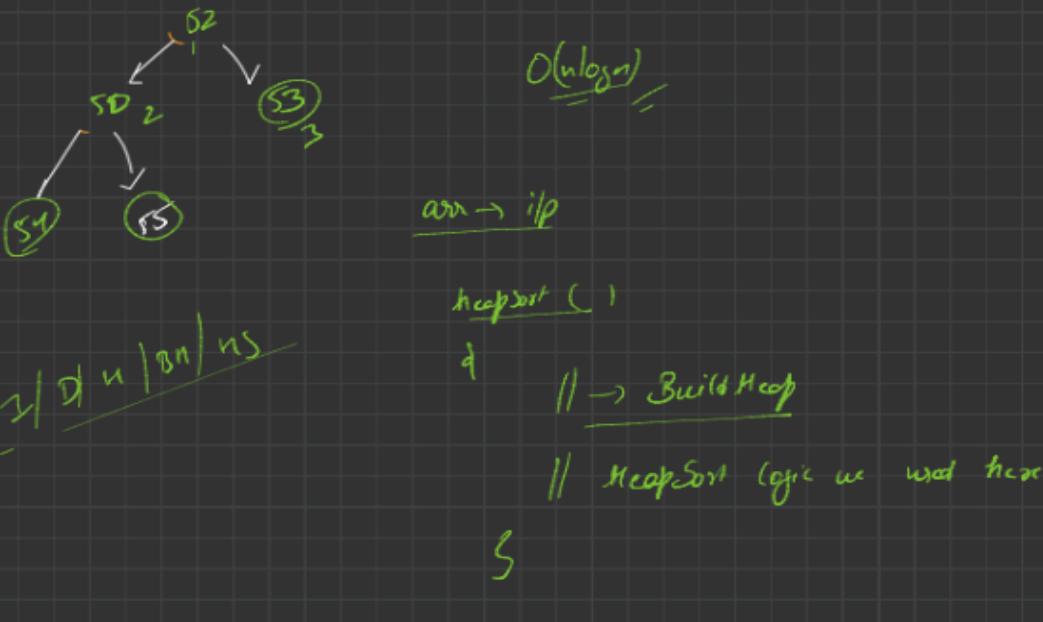


Build Min Heap:

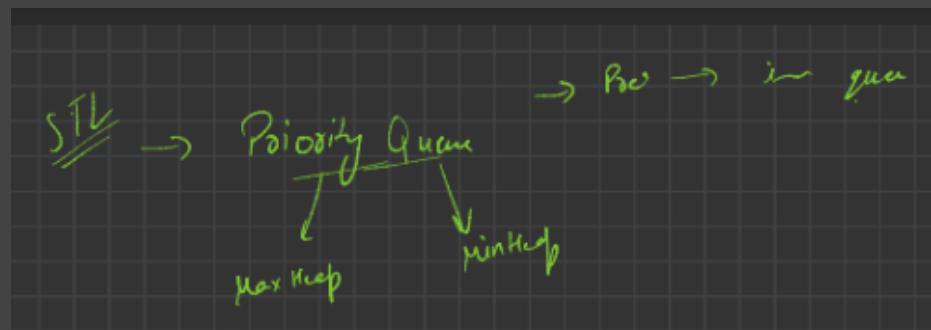


Heap Sort:

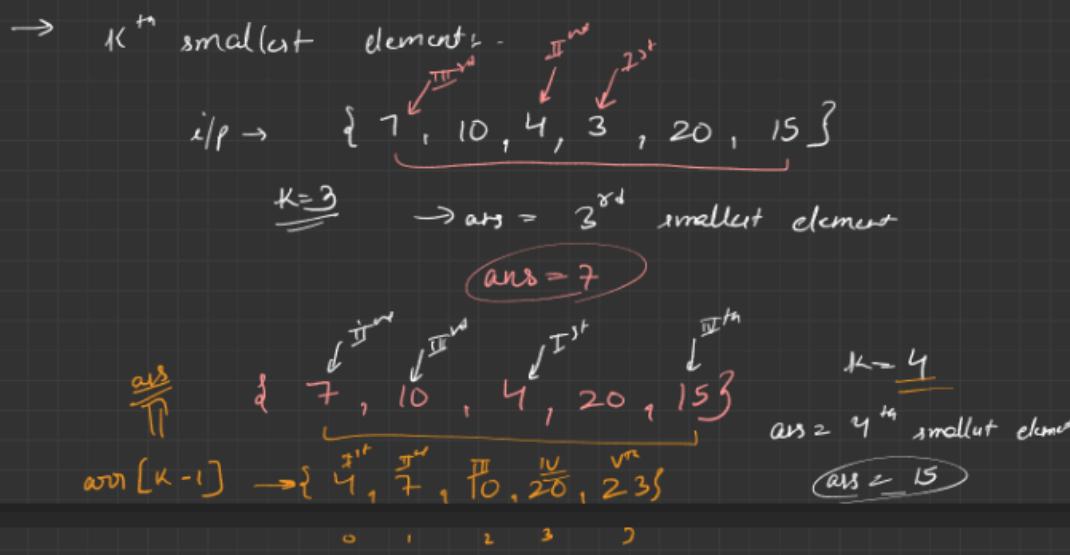




Priority Queue:



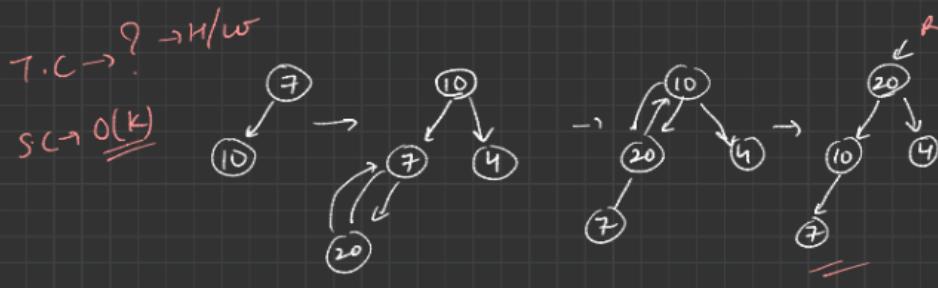
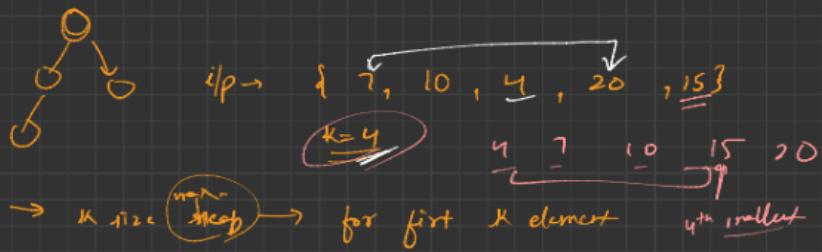
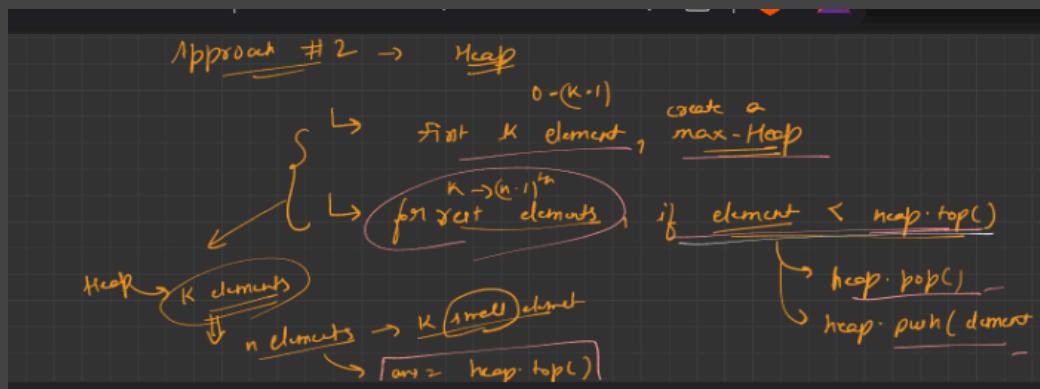
Kth Smallest Element Approach-I:



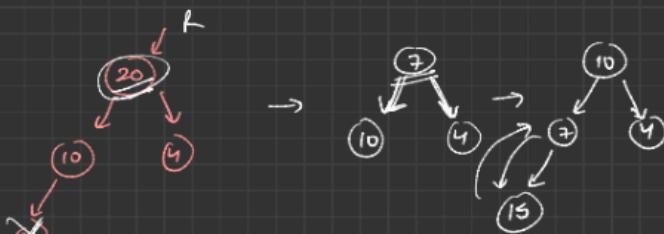
Approach:

- Algo #1
- \rightarrow Sort array in Inc order $\rightarrow O(n \log n)$
- \rightarrow Return $\boxed{ans = arr[K-1]}$ $\rightarrow O(1)$
- $T.C \rightarrow \boxed{O(n \log n)}$

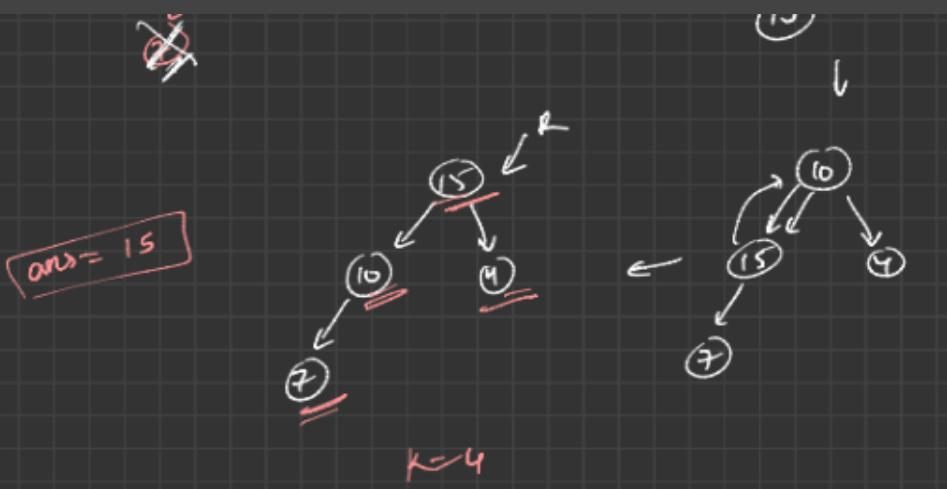
Kth Smallest Element Approach-II:



$15 < 20 \rightarrow \text{True}$



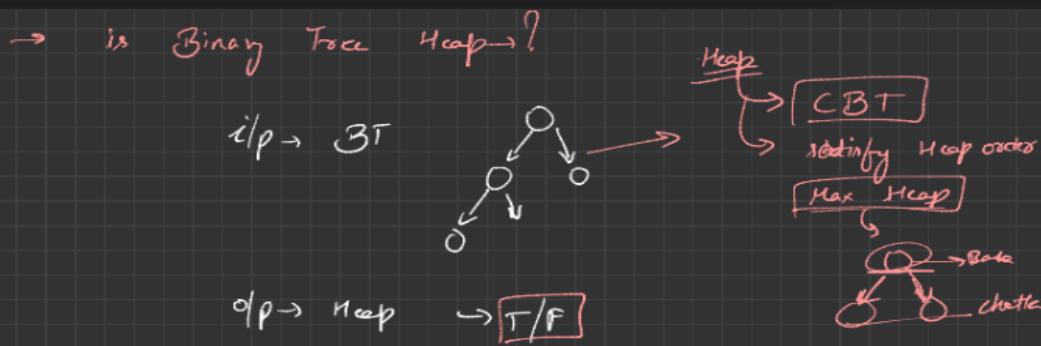
~~Ans~~



Kth Largest Element:

Use a min heap instead of a max heap to find the Kth largest element in an array.

Is The Given Binary Tree A Heap:



Algo:-

```

    solve(i)
    {
        if (is CBT(i)) && (is Max Order(i))
            return true
        else
            return false
    }

```

is CBT (root, i, nodeCount)

```

    {
        if (root == NULL)
            return True
        if (i > nodeCount)
            return false
    }

```

Use

```

    left = is CBT (root->left, 2i+1, nodeCount)
    right = is CBT (root->right, 2i+2, nodeCount)
    return (left && right)
}

```

O-based index

node → i

left → $2i+1$

right → $2i+2$

no left/right → total count

Note: CBT

CBT

is Max Order (root)

```

    {
        if (leaf node)
            if (leaf node)
                return true
        if (right == NULL)
            {
                return root->data > root->left->data
                && root->data > root->right->data
            }
    }

```

if

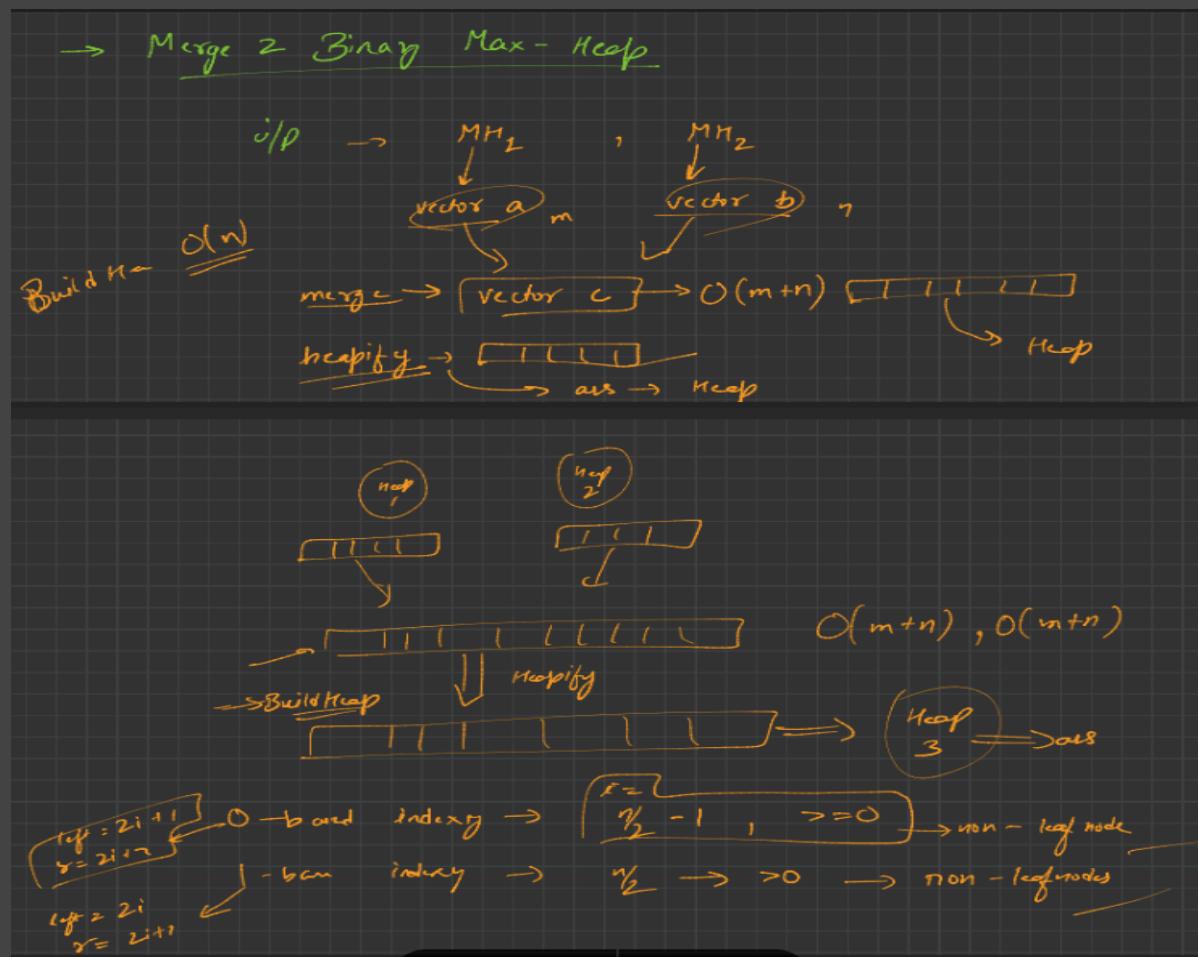
return $\text{root} \rightarrow \text{data} > \text{root} \rightarrow \text{left} \rightarrow \text{data}$
 $\text{root} \rightarrow \text{data} > \text{root} \rightarrow \text{right} \rightarrow \text{data}$

is Max Order (left) && is Max Order (right)

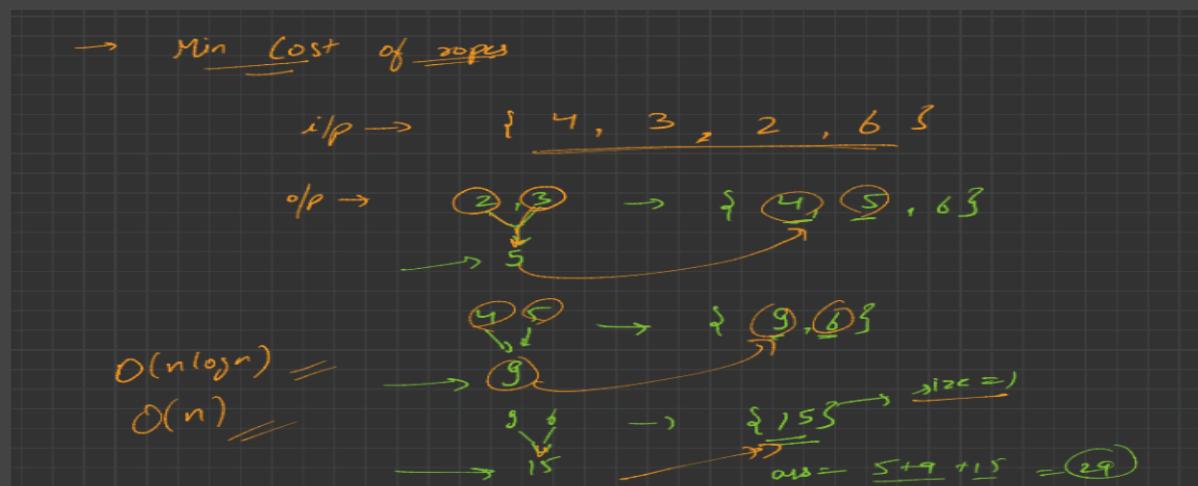
① Both child exist
② Leaf node
③ only left exist

$$T.C \rightarrow \underline{\underline{O(n)}} + \underline{\underline{O(n)}} + \underline{\underline{O(n)}} \rightarrow \underline{\underline{O(n)}}$$

Merge Two Binary Max Heaps:



Minimum Cost Of Ropes:



PQ:

while ($size > 1$)

```

int a = PQ.top()
PQ.pop()
int b = PQ.top()
PQ.pop()

```

```

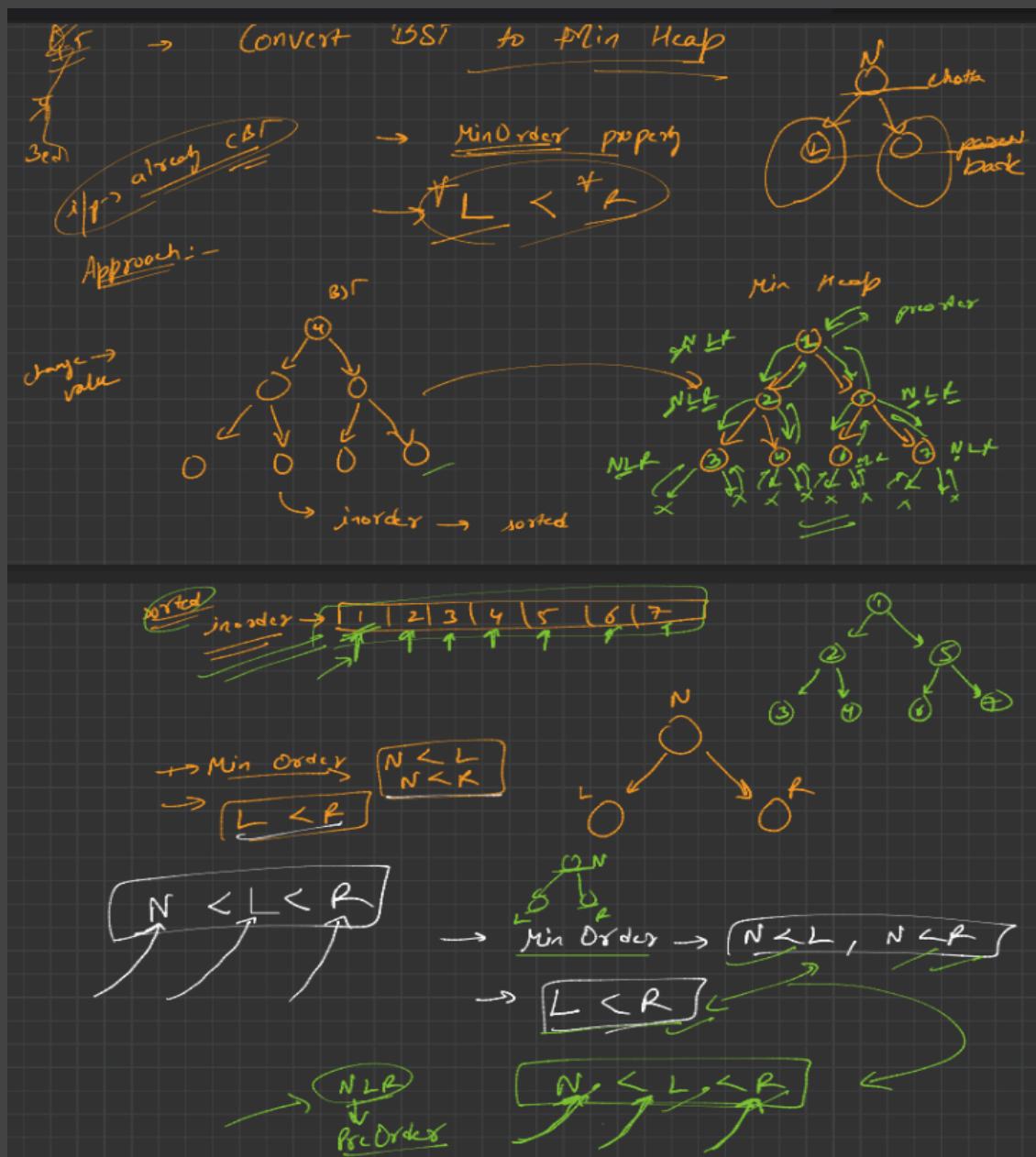
int sum = a+b
ans += sum
PQ.push(sum)

```

return ans

Min-Heap
↳ minimum
 $O(1)$

Convert BST To MinHeap:



```

    inorder ( root, vector in )
    {
        if call
            insert vector
            right call
    }
  
```

```

    fillPostOrder (root, inorder, index)
    {
        // left call
    }
  
```

```

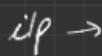
    root->data = inorder [index++]
  
```

```

    fillPostOrder (root->left, inorder, index)
    {
        // right call
    }
  
```

Kth Largest Sum SubArray Approach-I:

$\rightarrow K^{th}$ Largest sum Subarray



$\phi/\rho \rightarrow$

K^{th} largest Subarray sum

out

$$7 \cdot 1 \rightarrow 1$$

$$\{1, 2\} \rightarrow 3$$

$$\{1, 2, 2\} \rightarrow 1$$

$$\{1, 2, 2, 4\} \rightarrow 10$$

$$\{1, 2, 3, 4, 5\} \rightarrow 15$$

approach ✓



for ($i = 0$, $< n$)

2

8

```
vector<int> sum
```

$$\underline{\underline{O(n^2)}}$$

8

$$\text{sort} \rightarrow T.C \rightarrow \left(L \log(L) \right) \xrightarrow{\text{II}} \underline{n^2 \log n}$$

\downarrow is larger

increasing order \leftarrow
 K_m
as III

$$T \in \Theta(n^2 \log n)$$

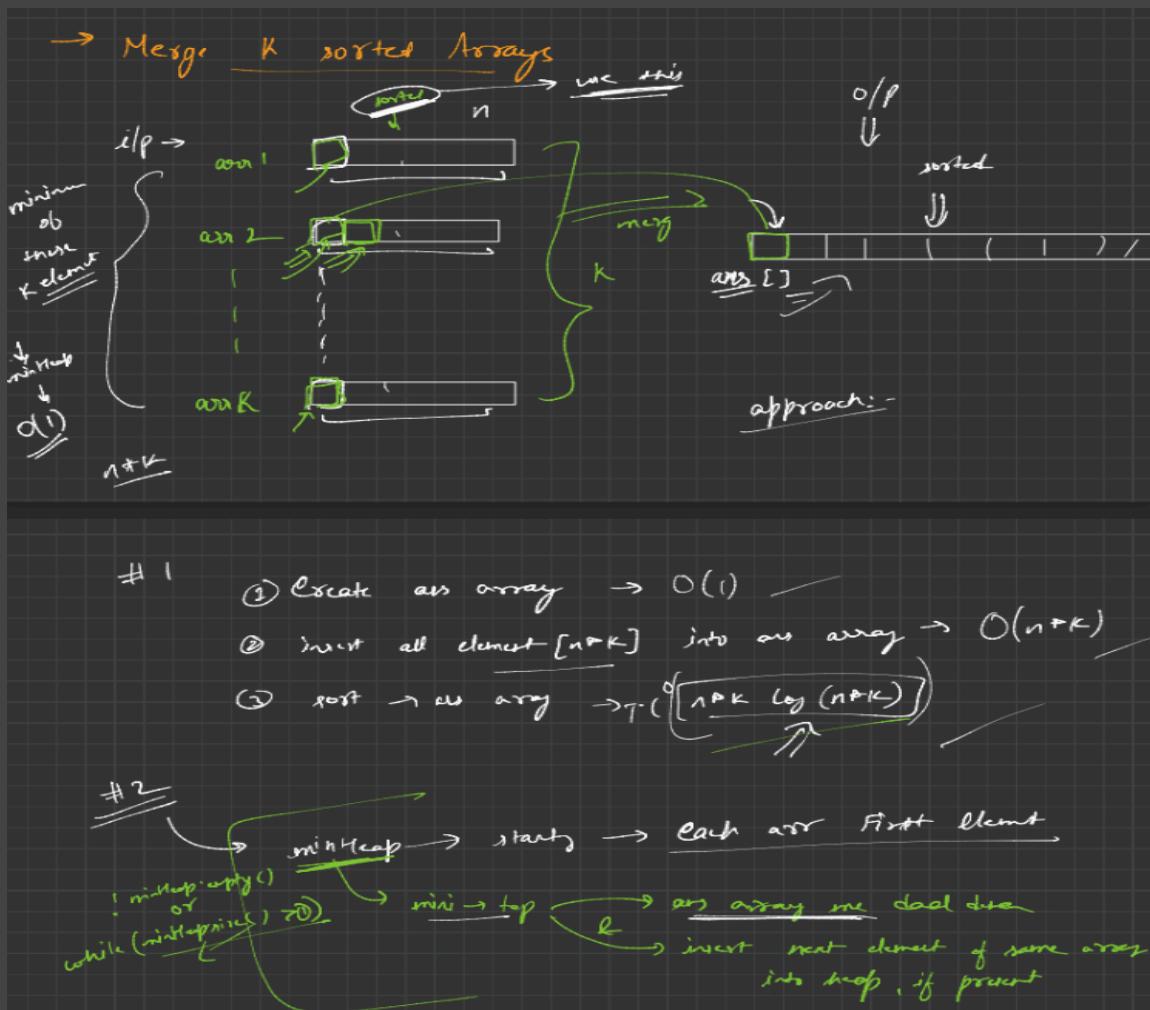
Ist → L-1 → inde

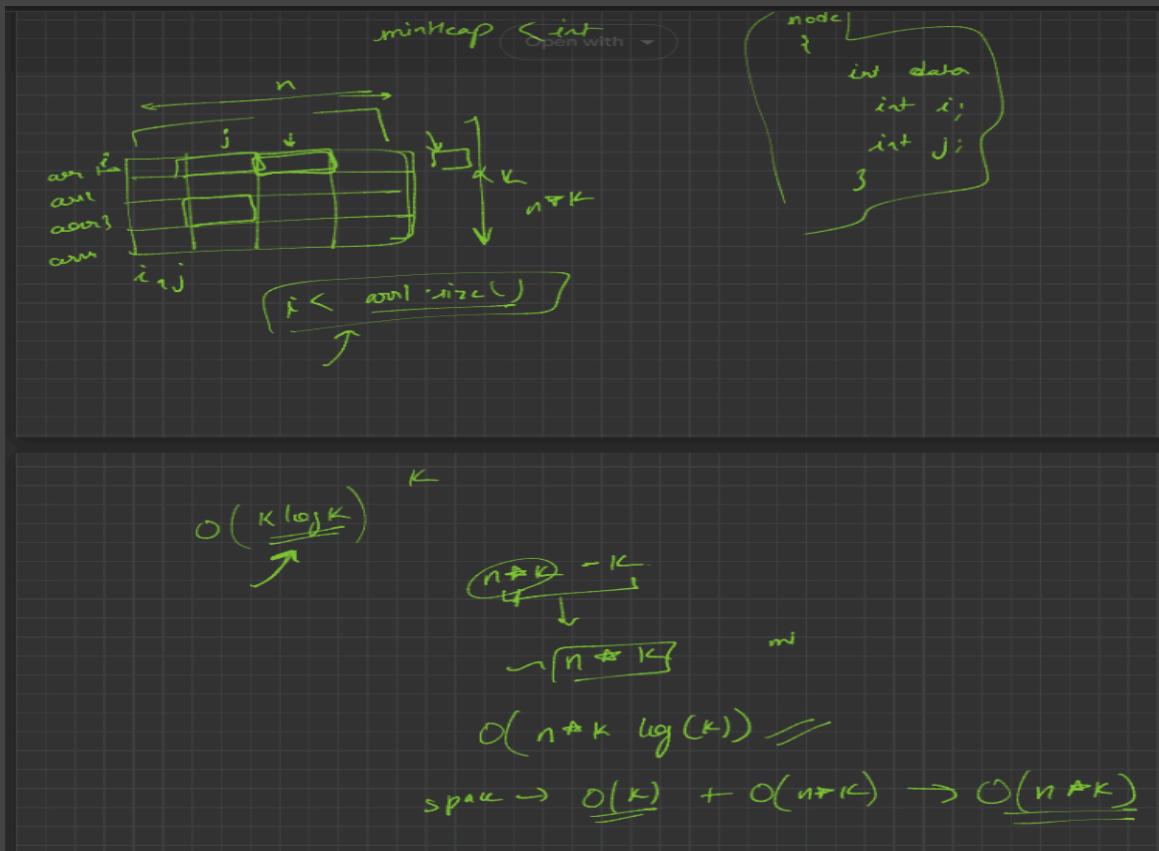
24 / 2-2

$$e^{\lambda t} \rightarrow e^{-kt}$$

Kth Largest Sum SubArray Approach-II:

Merge K Sorted Arrays:



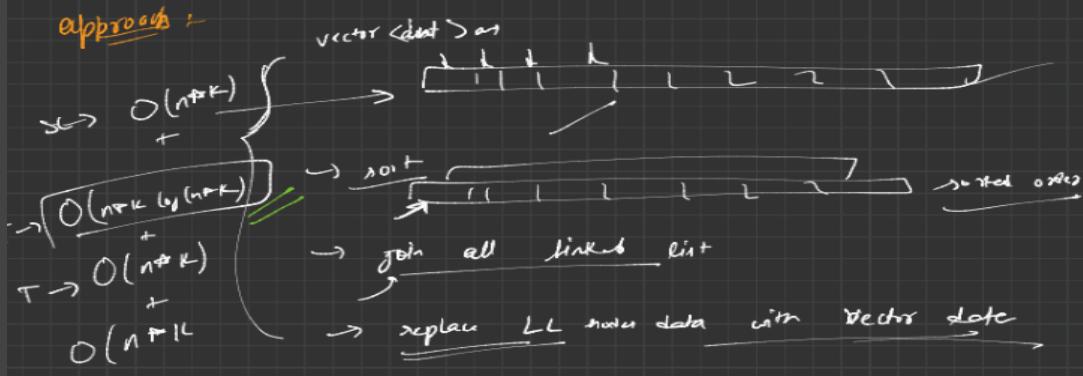


Dry Run:

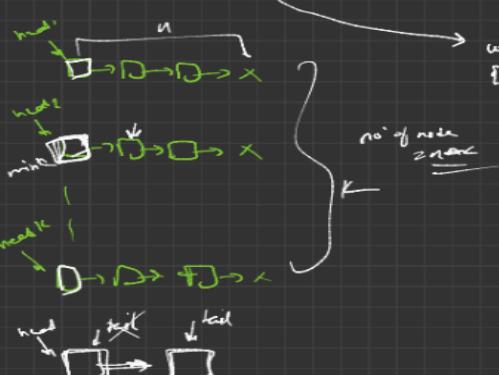
1. A min heap `minHeap` is created, which stores pointers to `node` objects. The heap is ordered by the `data` member of the `nodes`, in ascending order.
2. The first element of each array in `kAr` arrays is inserted into `minHeap`. After this step, `minHeap` contains the nodes $(2, 0, 0), (1, 1, 0)$, and $(3, 2, 0)$.
3. The while loop begins. In each iteration, the node at the top of `minHeap` is removed, its data is added to the `ans` vector, and if there is a next element in the same array, a new node is created for that element and pushed into `minHeap`.
 - o Iteration 1: The top node is $(1, 1, 0)$. 1 is added to `ans`, and the node is removed from `minHeap`. The next element in the same array is 3, so the node $(3, 1, 1)$ is pushed into `minHeap`.
 - o Iteration 2: The top node is $(2, 0, 0)$. 2 is added to `ans`, and the node is removed from `minHeap`. The next element in the same array is 6, so the node $(6, 0, 1)$ is pushed into `minHeap`.
 - o Iteration 3: The top node is $(3, 1, 1)$. 3 is added to `ans`, and the node is removed from `minHeap`. The next element in the same array is 14, so the node $(14, 1, 2)$ is pushed into `minHeap`.
 - o Iteration 4: The top node is $(3, 2, 0)$. 3 is added to `ans`, and the node is removed from `minHeap`. The next element in the same array is 5, so the node $(5, 2, 1)$ is pushed into `minHeap`.
 - o Iteration 5: The top node is $(5, 2, 1)$. 5 is added to `ans`, and the node is removed from `minHeap`. The next element in the same array is 8, so the node $(8, 2, 2)$ is pushed into `minHeap`.
 - o Iteration 6: The top node is $(6, 0, 1)$. 6 is added to `ans`, and the node is removed from `minHeap`. The next element in the same array is 12, so the node $(12, 0, 2)$ is pushed into `minHeap`.
 - o Iteration 7: The top node is $(8, 2, 2)$. 8 is added to `ans`, and the node is removed from `minHeap`. The next element in the same array is 10, so the node $(10, 2, 3)$ is pushed into `minHeap`.
 - o Iteration 8: The top node is $(10, 2, 3)$. 10 is added to `ans`, and the node is removed from `minHeap`. There is no next element in the same array.
 - o Iteration 9: The top node is $(12, 0, 2)$. 12 is added to `ans`, and the node is removed from `minHeap`. The next element in the same array is 15, so the node $(15, 0, 3)$ is pushed into `minHeap`.
 - o Iteration 10: The top node is $(14, 1, 2)$. 14 is added to `ans`, and the node is removed from `minHeap`. The next element in the same array is 20, so the node $(20, 1, 3)$ is pushed into `minHeap`.
 - o Iteration 11: The top node is $(15, 0, 3)$. 15 is added to `ans`, and the node is removed from `minHeap`. There is no next element in the same array.
 - o Iteration 12: The top node is $(20, 1, 3)$. 20 is added to `ans`, and the node is removed from `minHeap`. There is no next element in the same array.
4. The while loop ends because `minHeap` is empty. The `ans` vector is returned.

Merge K Sorted Linked List:

approbus :



minHeap \rightarrow first element of the linked list



```

while (!minHeap.empty())
{
    if (thead == NULL)
        thead = tail = minHeap.top() // LL
    minHeap.pop()
    if (thead->next != NULL)
        { minHeap.insert(thead->next) }
}
else
{
    tail->next = minHeap.top() // next
    minHeap.pop()
    tail = tail->next // LL
}

```

```

if (tail->next = NULL)
    ↴
    ↴ mixup insert
    ↴
return head;

```

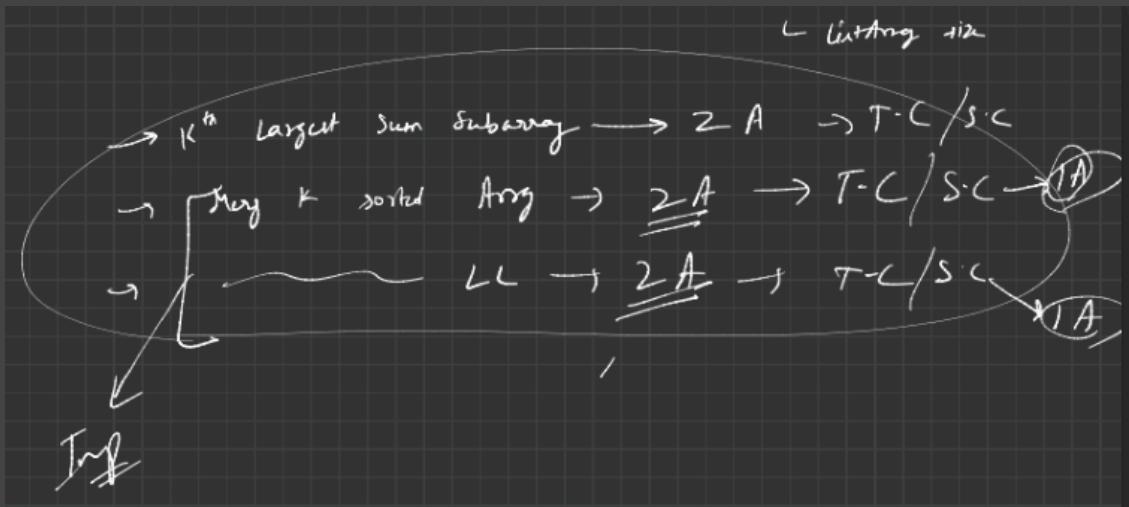
$$T \in \mathcal{O}(k \log k) + \mathcal{O}(n * k \log k)$$

$n * k = k$
 $\approx n$

$\mathcal{O}(n * k \log k)$
 no. of nodes in a

$\underline{s \in \mathcal{O}(k)}$

$\mathcal{O}(N \log k) \rightarrow N = T_{\text{total}}$



Smallest Range From K Sorted List:

① Smallest Range in K-Sorted List $K \rightarrow \text{int}$

i/p $\square \rightarrow \square \rightarrow \square \rightarrow \dots \rightarrow \times$ $\Rightarrow \text{Q.P} \rightarrow \underline{\text{smallest range}}$

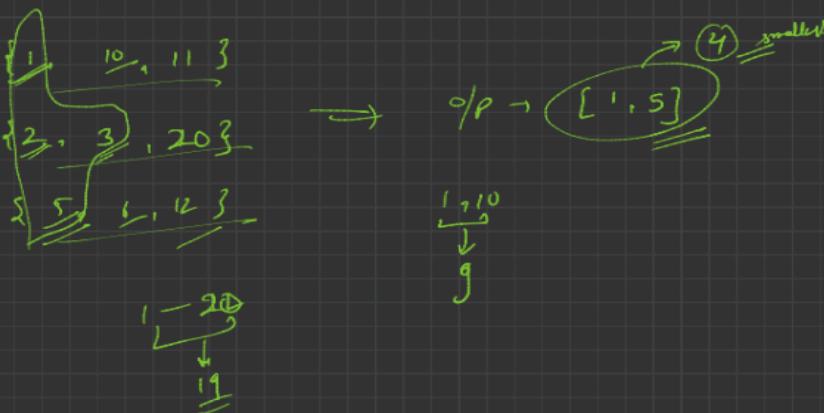
K $\left\{ \begin{array}{l} \square \rightarrow \square \rightarrow \square \rightarrow \dots \rightarrow \times \\ \square \rightarrow \square \rightarrow \square \rightarrow \dots \rightarrow \times \\ \square \rightarrow \square \rightarrow \square \rightarrow \dots \rightarrow \times \end{array} \right.$

sorted

$[x, y]$

\downarrow

the list has
at least one element
to make it range



approach:- (Brute force) $K = 3$

*1 $\rightarrow \{1, 10, 11\}$

K $\left\{ \begin{array}{l} \rightarrow \{1, 10, 11\} \\ \rightarrow \{2, 3, 20\} \\ \rightarrow \{5, 6, 12\} \end{array} \right.$

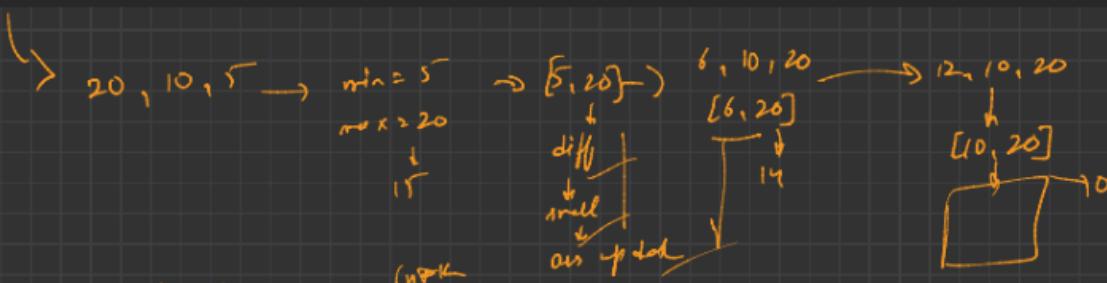
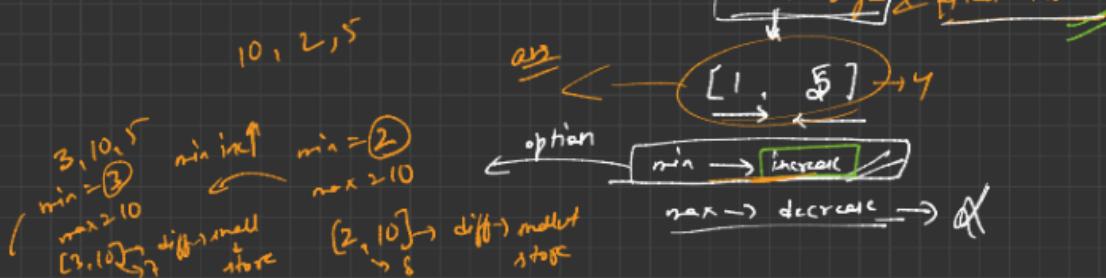
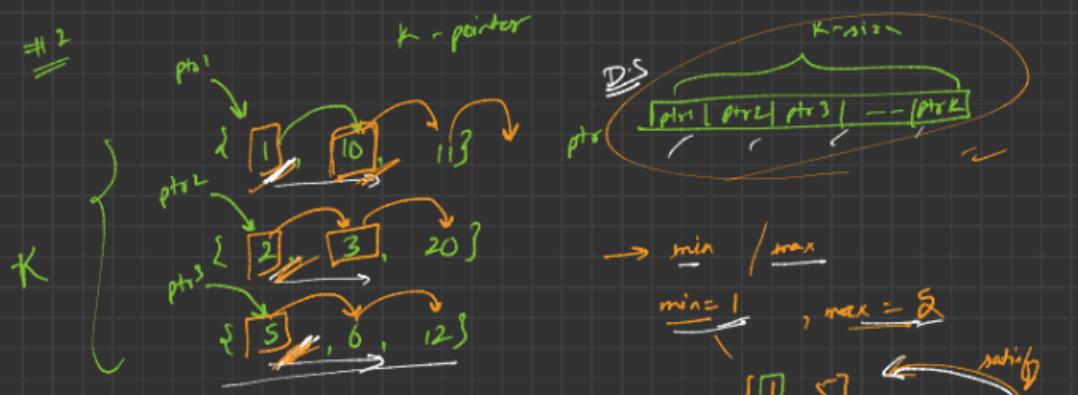
n

smaller range \rightarrow range \Rightarrow diff

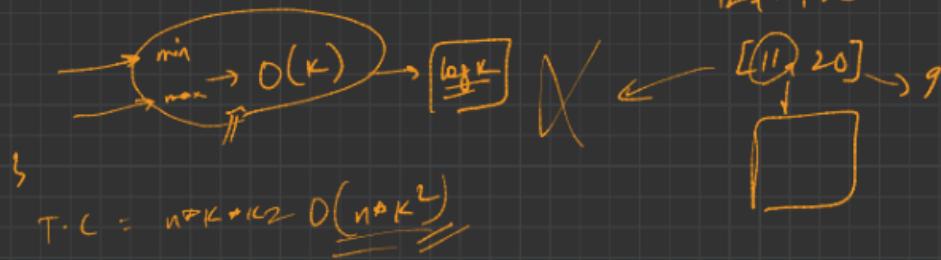
total no. of diff $= \boxed{n+K} \Rightarrow N$

$O(N^2) = \boxed{n^2 K^2} \Rightarrow O(n^2 K^2)$

$$\{1, 2, 3, 4\} \rightarrow O(n^2)$$

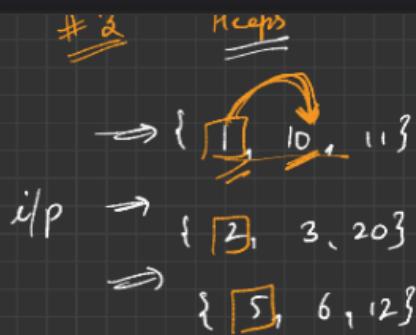


while () → next element ^(input) K



$$T.C = nPK + \Theta O(\underline{\underline{nPK^2}})$$

$$S.C \rightarrow O(K)$$



Algo.

- 1 \rightarrow min / max \rightarrow min- K cap \rightarrow K size
 ↳ list \leftarrow starting element
- 2 \Rightarrow double tree
 ↳ acquire row-track layout

```
int ansStart, ansEnd;
(max - min) / (ansEnd - ansStart)
```

while (!pq.empty(),
 {
 min = pq.top().row,
 p = pq.pop();

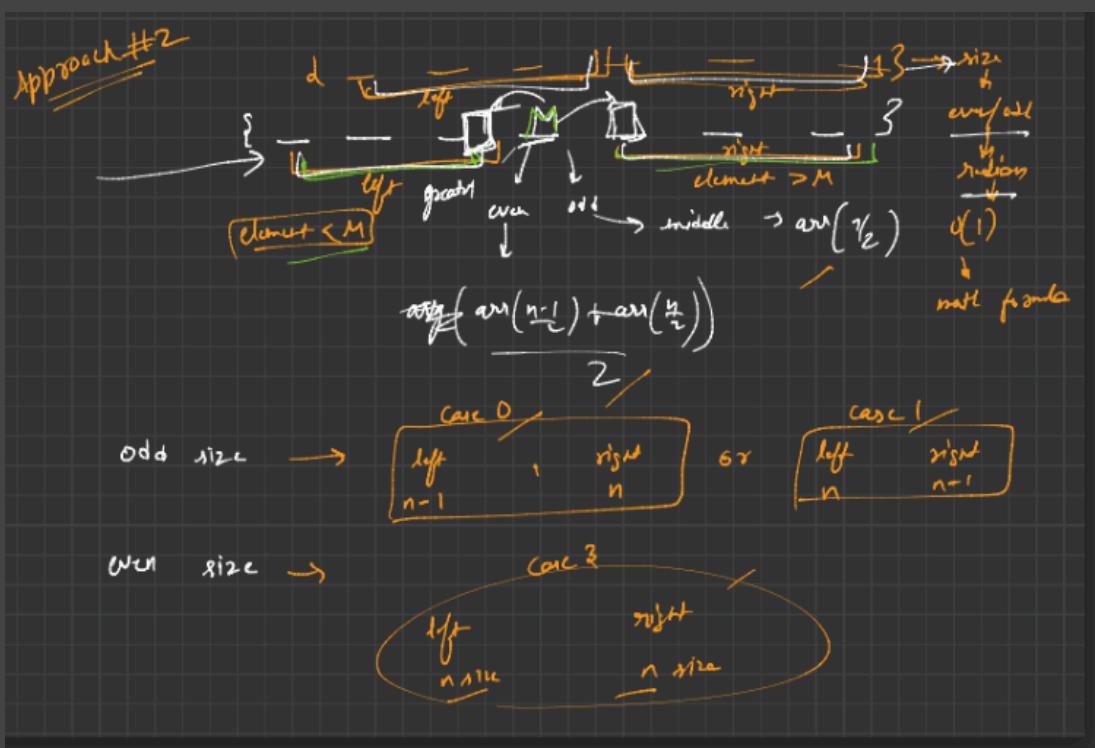
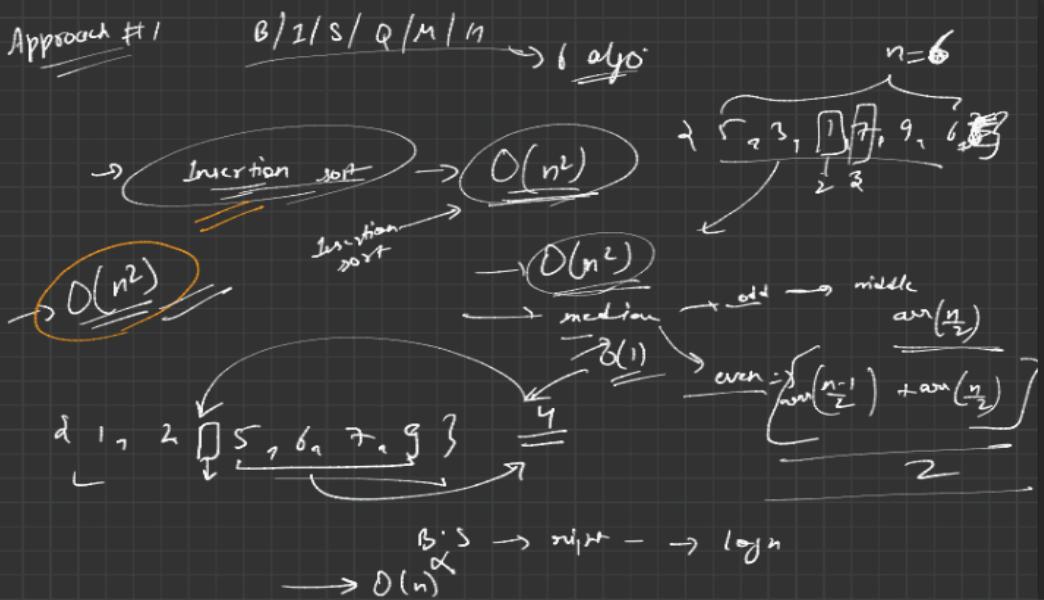
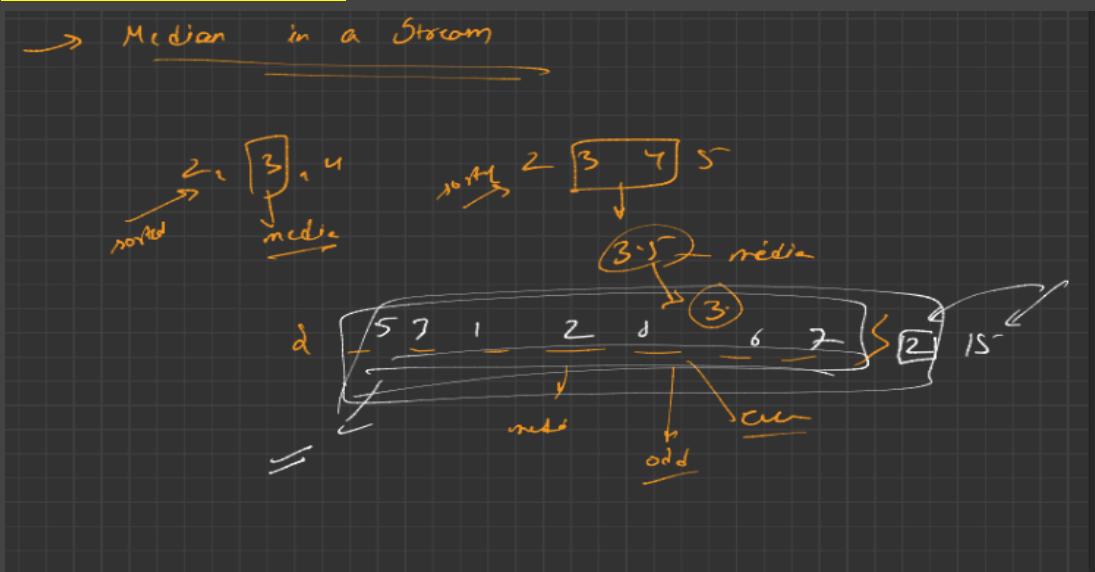
on update
 if ($\frac{\max - \min}{\text{step}} < \text{ansEnd} - \text{ansStart}$)
 {
 update ans
 }
 max = update
 if ($\underline{\min \cdot col} < n$)
 {
 max = max(max, $\max(\text{curr_val}, \min \cdot \text{val})$)
 pq.push(new node(
 min row
 == == ==))
 }
 else
 break;

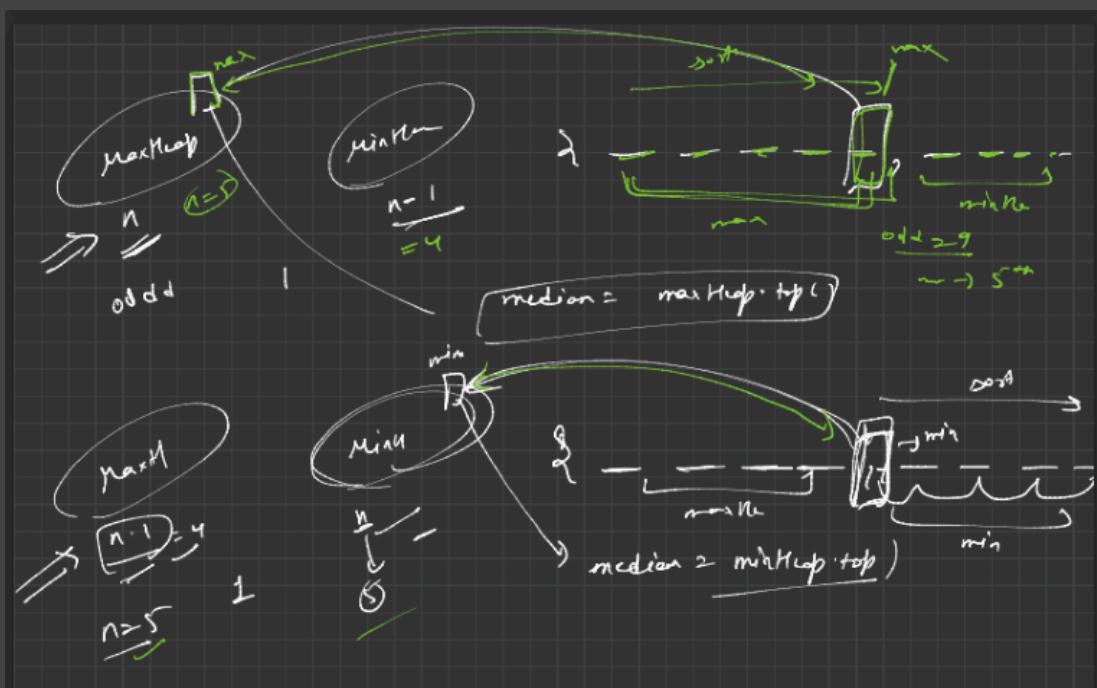
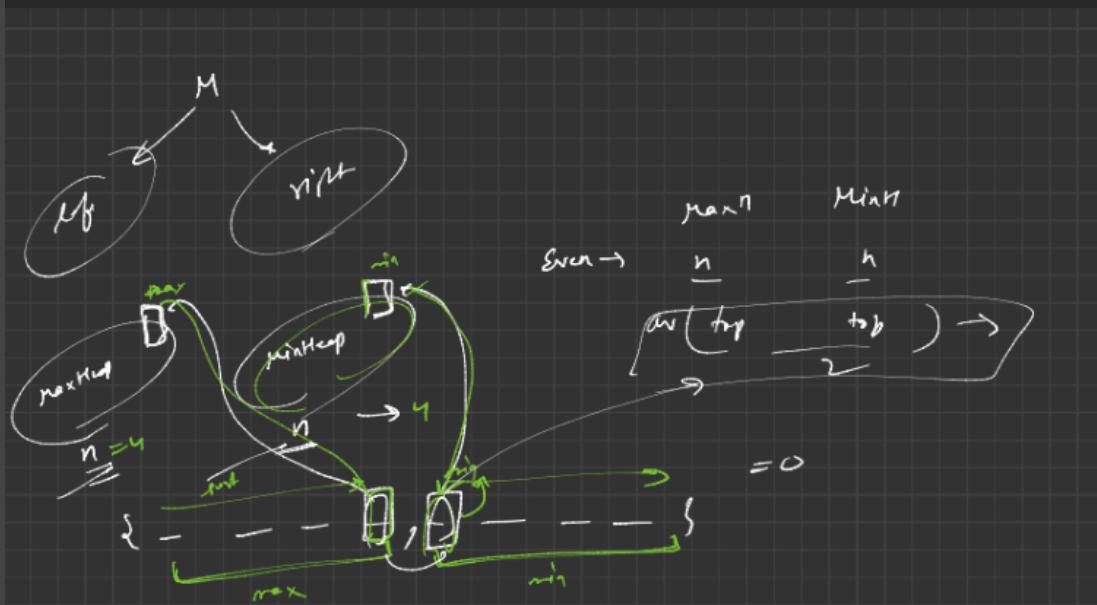
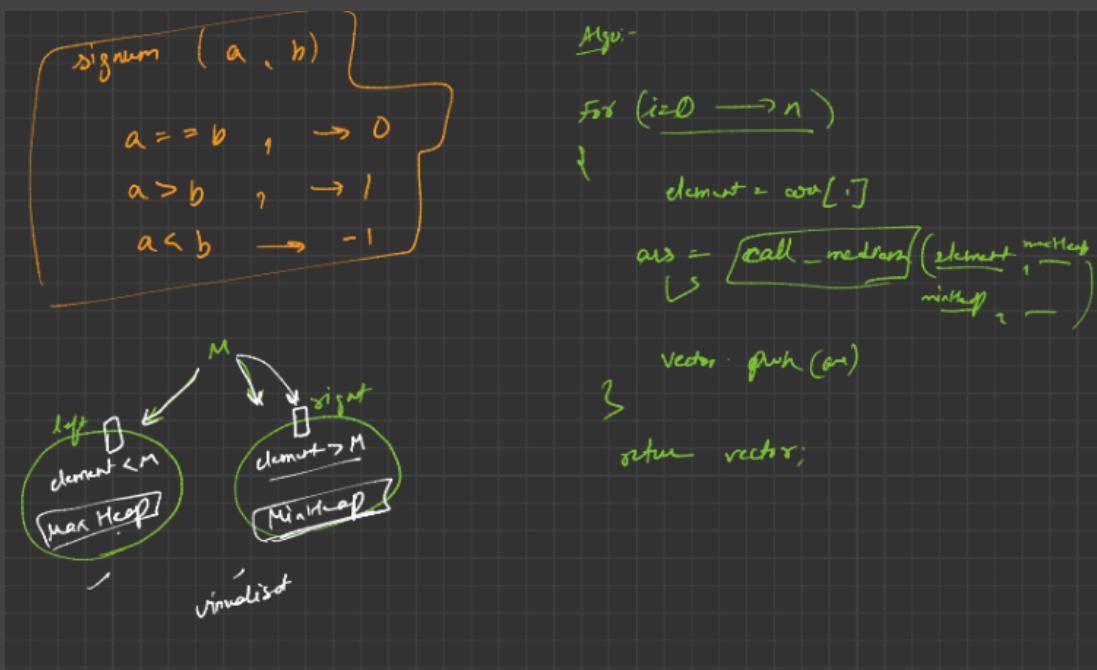
$(S_1, r) \rightarrow 1$

$S_1 - S_2 + 1 = 1$

$[3 - 9] \rightarrow 9 - 3 \cdot n$

Median In A Stream:





call `median ([clen], -max, min, &median)` by rff

?

`switch (signum (maxHeap.size() , minHeap.size()))`

{

case 0: if (`element > M`)

{ `minHeap.push (element)`
`median = minHeap.top()` }



else

{ `maxHeap.push (element)`
`median = maxHeap.top()` }

}

case 1: if (`element > M`)

{ `minHeap.push (element)`

`median = avg (maxTop(), minTop())` }

else

{ `minHeap.push (maxHeap.top())`

`maxHeap.pop()`

`maxHeap.push (element)`

→ // copy

}

$a < b$

case -1 :

if (`element > M`)

{ `maxHeap.push (minHeap.top())`

`minHeap.pop()`

`minHeap.push (element)`

$\boxed{\text{Median} = \text{avg} (\text{minTop}, \text{maxTop})}$

}

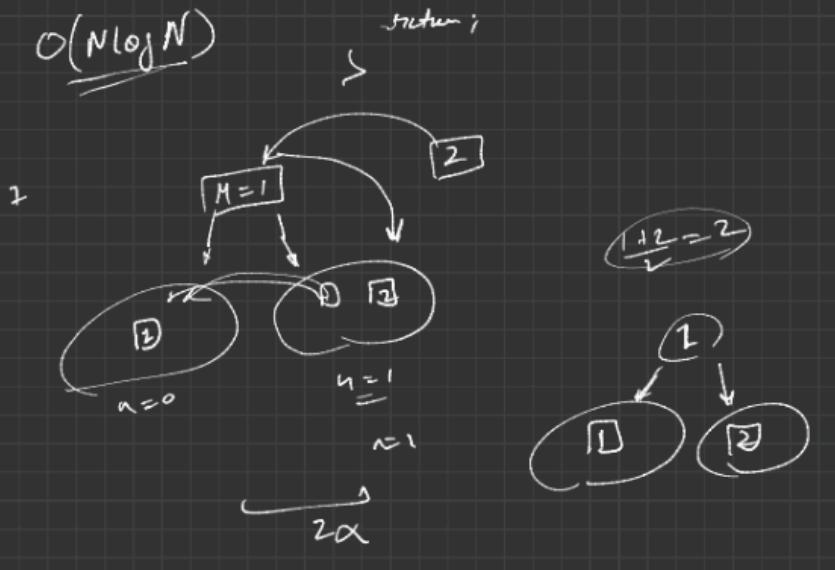
else

{ `maxHeap.push (element)`

→ // copy

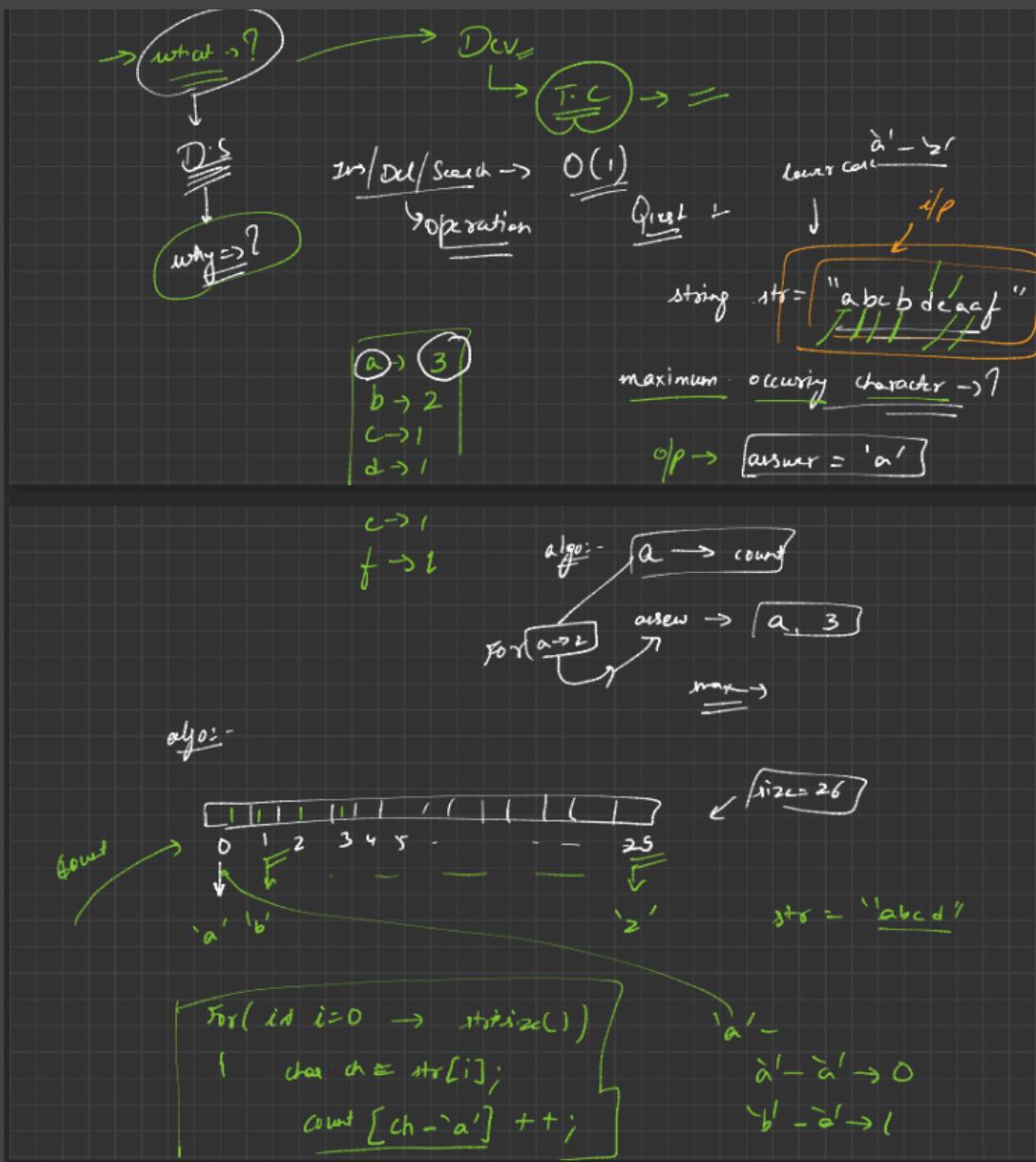
}

$T.C \rightarrow O(N \log N)$



HashMaps

Intro:



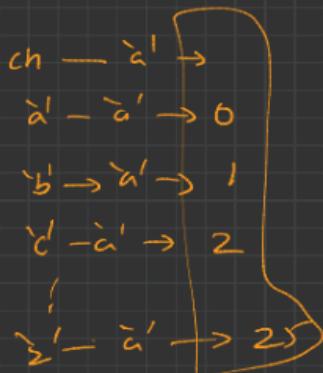
3

$z \rightarrow a \rightarrow \alpha$

for (int i=0 ; i < 25)

\downarrow
 max →

'a' → 0
'b' → 1
'c' → 2
'd' → 3
'
'
'z' → 25



str → " mera naam hai babbaz mera babbaz babbaz "

O/p → maximum occurring word

mera → 2

naam → 1

hai → 1

babbaz → 3

mera → 2
 naam → 1
 hai → 1
 babbaz → 3

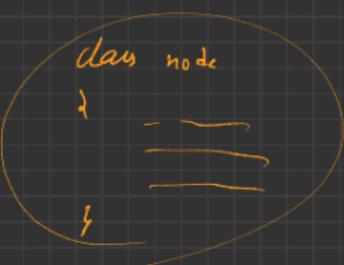
→ mapping possible

answer



< mera, 2 >

STL



map < node, int > m;

map

Implementation:

↳ Using linked list



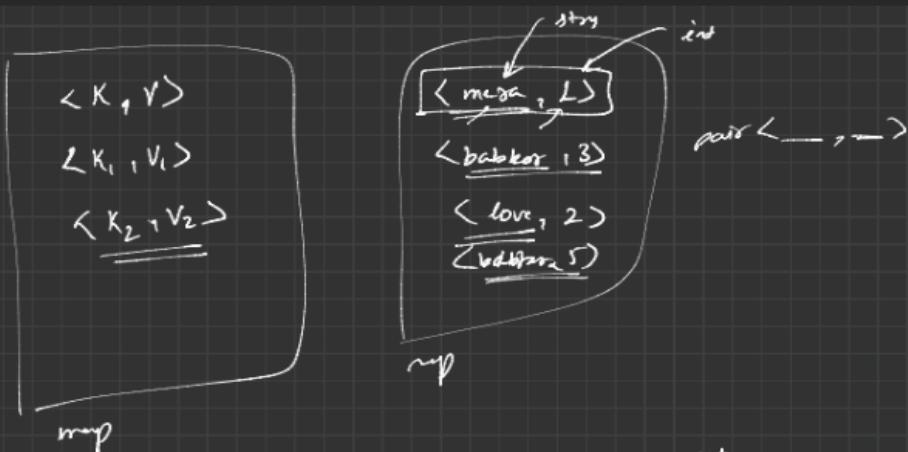
Deletion → O(n), Search → O(n)

Using BST $\Rightarrow O(\text{ordered-map})$

Insertion $\rightarrow O(\log n)$
 Search $\rightarrow O(1)$
 Delete $\rightarrow O(\log n)$

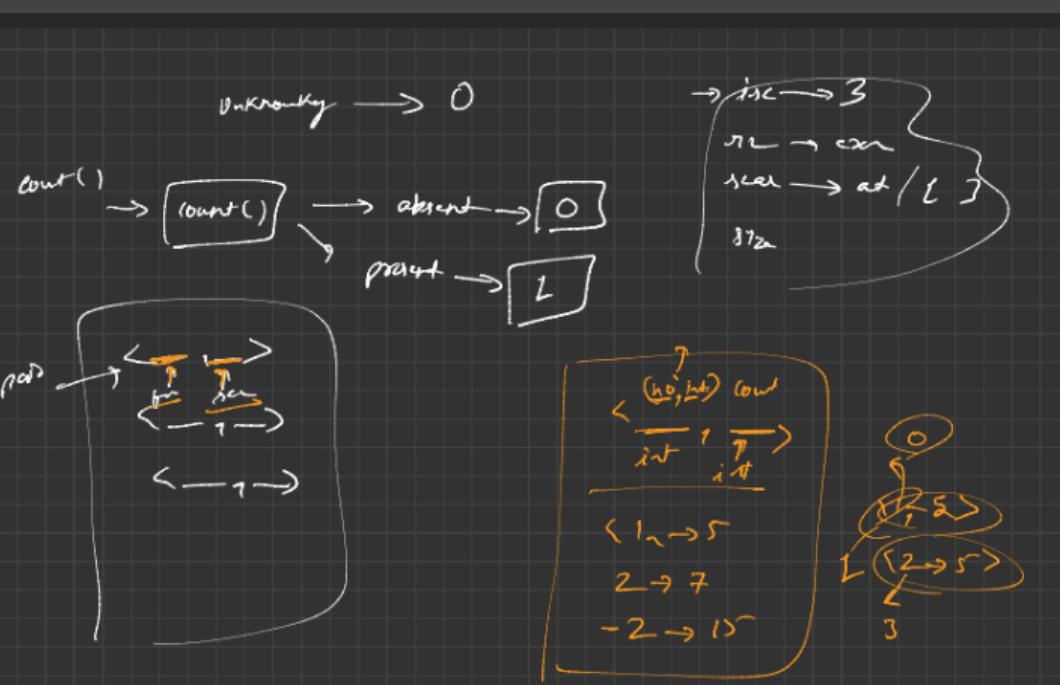
Inbuilt stuff
 $\rightarrow \text{map} \rightarrow O(\log n)$
 $\rightarrow \text{unordered-map} \rightarrow O(1)$

Hashtable
 $I/D/S \rightarrow O(1)$

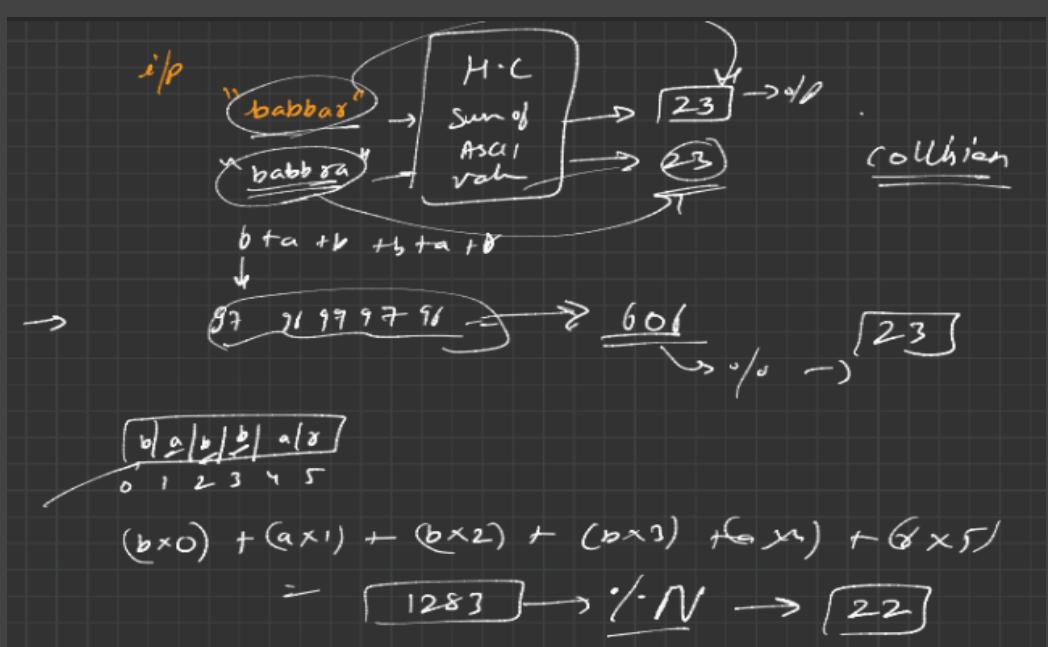
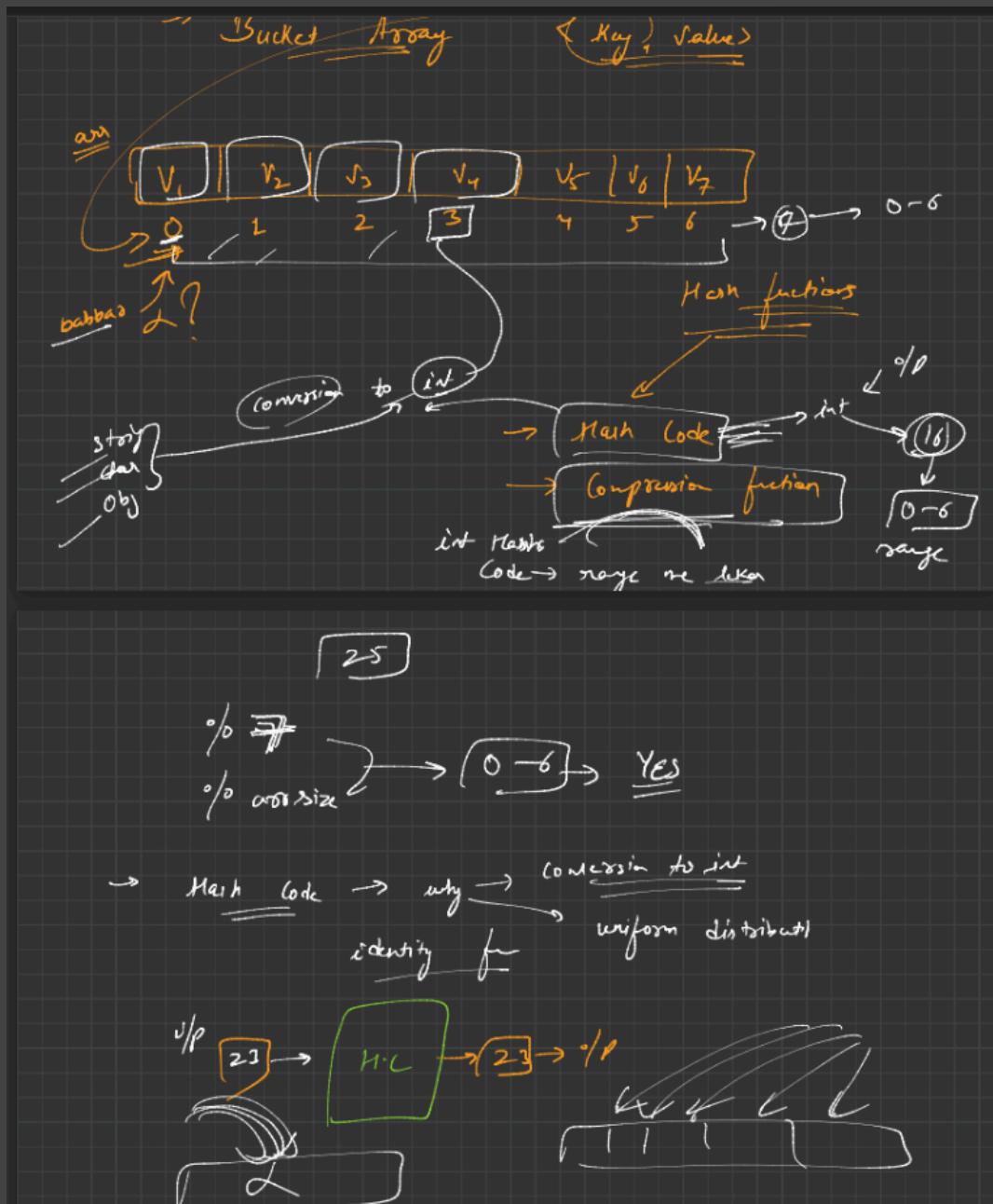


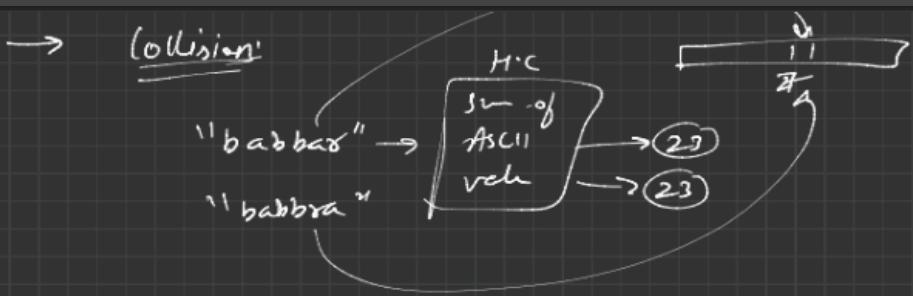
$$m["\text{mera"}] = 1 \rightarrow \text{new entry} \\ \langle \underline{\text{mera}}, \cancel{1} \cancel{2} \rangle$$

$$m["\text{mera"}] = 2$$



Bucket Array:



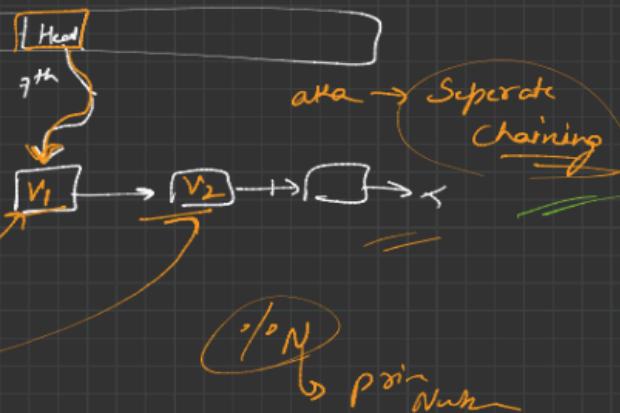


Collision Handling :-

→ Open Hashing → same place pr hi jaw

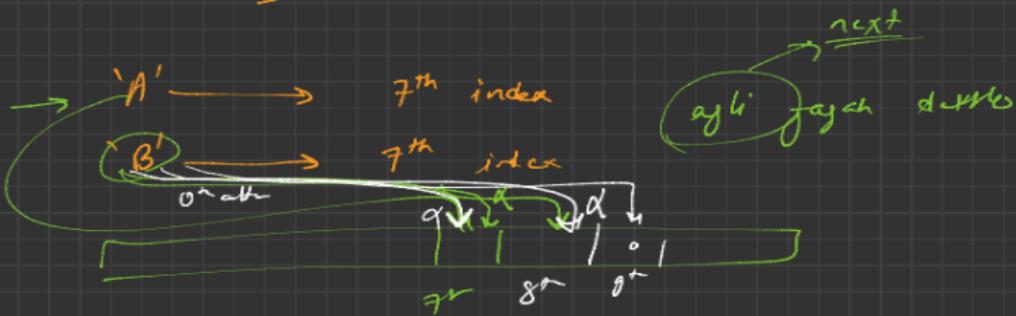
→ Closed Addressing

→ "babbar" → 23 → 7th index
 → "babbar" → 7th index



100 word → index → 100 LL α

→ Open Addressing



$$\rightarrow h_i(a) = \underbrace{h(a)}_{7^{th}} + \underbrace{f_i(a)}_{+1}$$

in attempt in Kata people

\rightarrow Linear probing

$$f(i) \rightarrow i$$

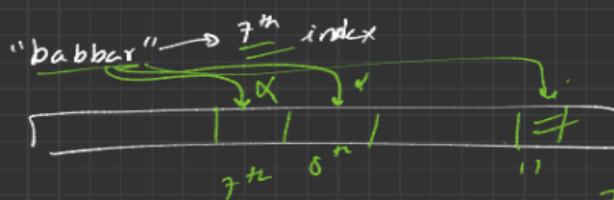
$$f(1) \rightarrow 1$$

$$f(2) \rightarrow 2$$

\rightarrow Quadratic Probing

$$f(i) \rightarrow i^2$$

$$f(0) \rightarrow 0$$



$$f(1) \rightarrow 1^2 \rightarrow 1$$

$$f(2) \rightarrow 2^2 \rightarrow 4$$

$$h_i(a) = \underbrace{h(a)}_{7} + \underbrace{f_i(a)}_{+1} = 8$$

$$= 7 + 4 = 11$$

(S.C)

$$\overline{i^3 + D}$$

$$\overline{(i^2 + B)}$$

$$\overline{i^2 + q}$$

\Rightarrow Complexity analysis

"maza bhai love babbar too kya had"

injection

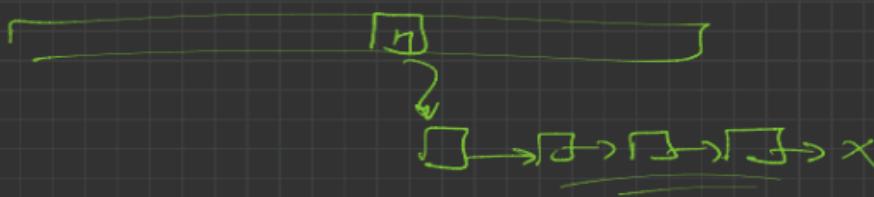
$n \rightarrow$ total no. of west

$K \rightarrow$ word length

if $\underline{n > K}$

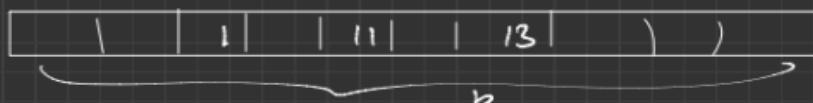
$H.C \rightarrow O(K) \rightarrow \boxed{O(1)}$

\rightarrow traverse $\rightarrow \underline{\cancel{O(n)}}$



$n \rightarrow$ no. of entries in map

$b \rightarrow$ no. of boxes available $n=3$



no. of entries in a box $\rightarrow \underline{n/b} \rightarrow$ Load factor

we always ensure $\underline{n/b} < 0.7$

$\rightarrow H.C \rightarrow \underline{\text{acha}} \rightarrow O(1)$

L.F = $\underline{n/b} < 0.7$

it is very safe to assume

$\underline{\underline{O(1)}}$

$(n/b) \rightarrow \underline{\underline{n}}$

$n/b < 0.7 \Rightarrow$

$b \uparrow$

$\frac{\text{no. of available boxes}}{\text{ReHashing}}$

\hookrightarrow ReHashing

\hookrightarrow increase bucket size

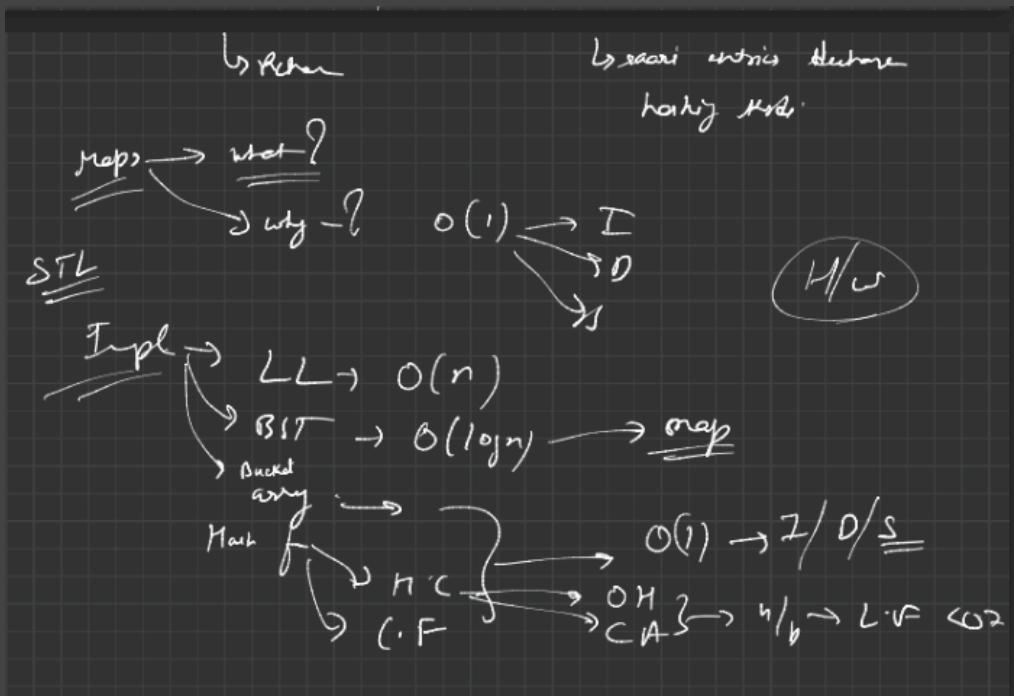
$(2x)$

$n/b \rightarrow$ half

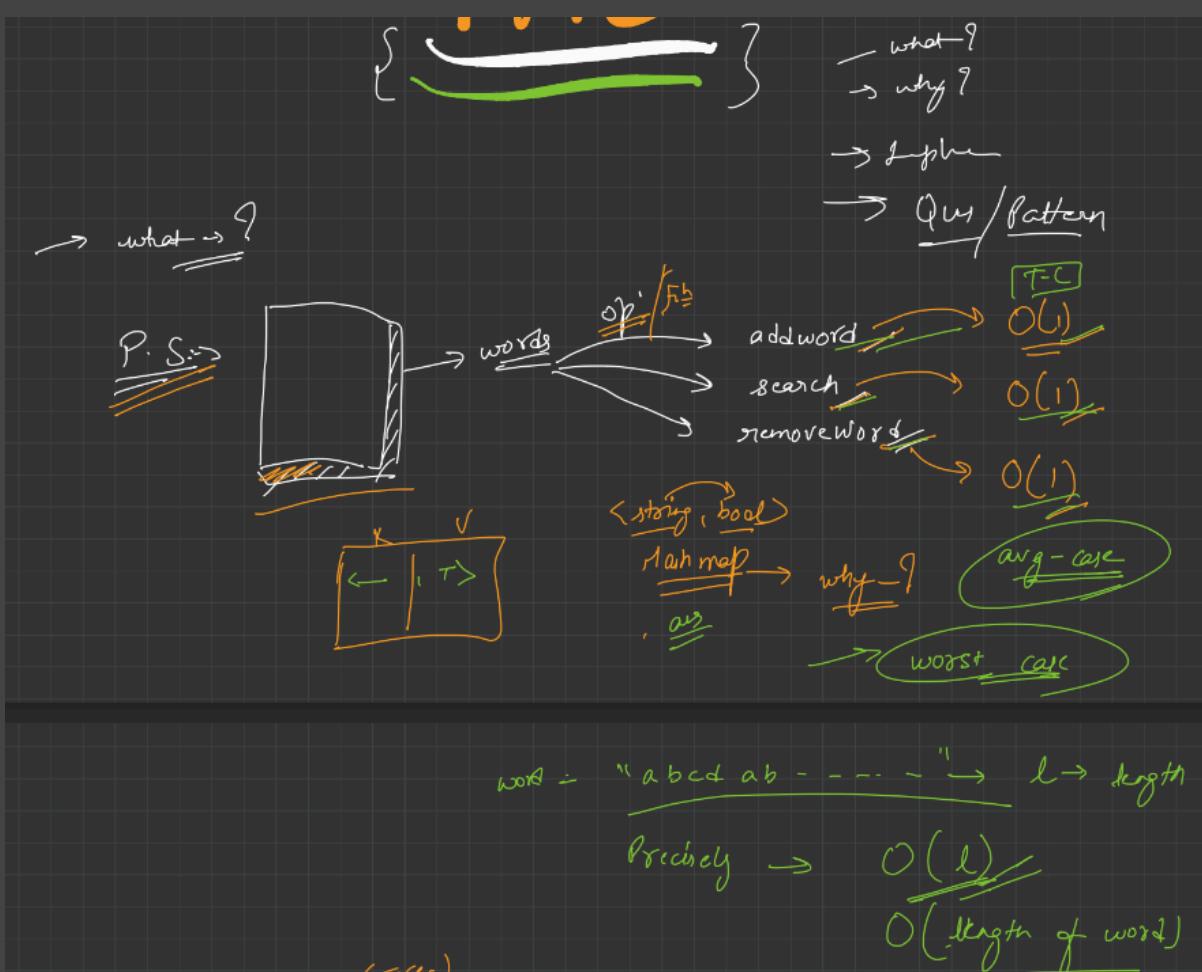
insertion

Deletion/Search

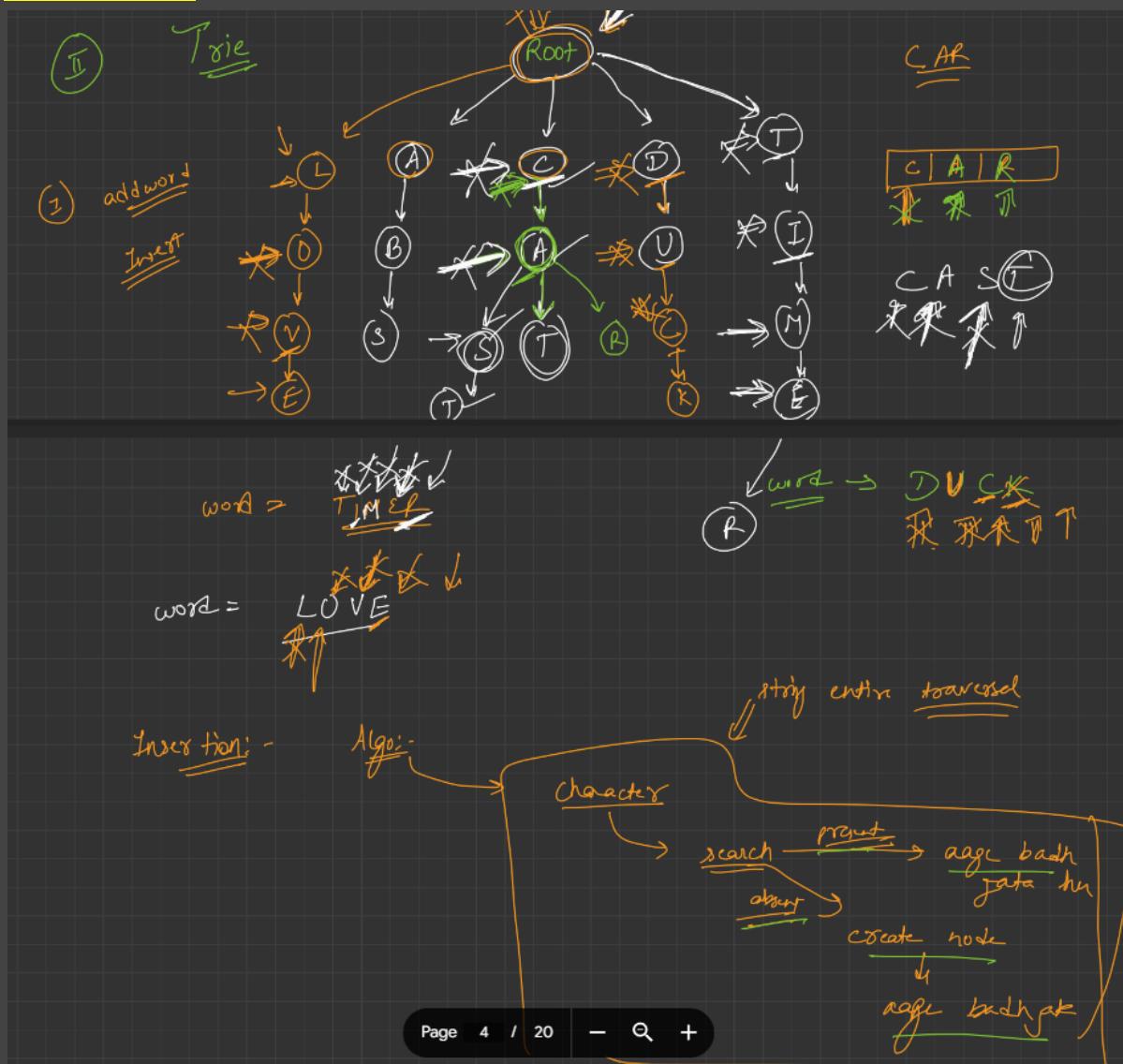
$H.C \rightarrow O(1)$
 $\rightarrow L.F < 0.7$



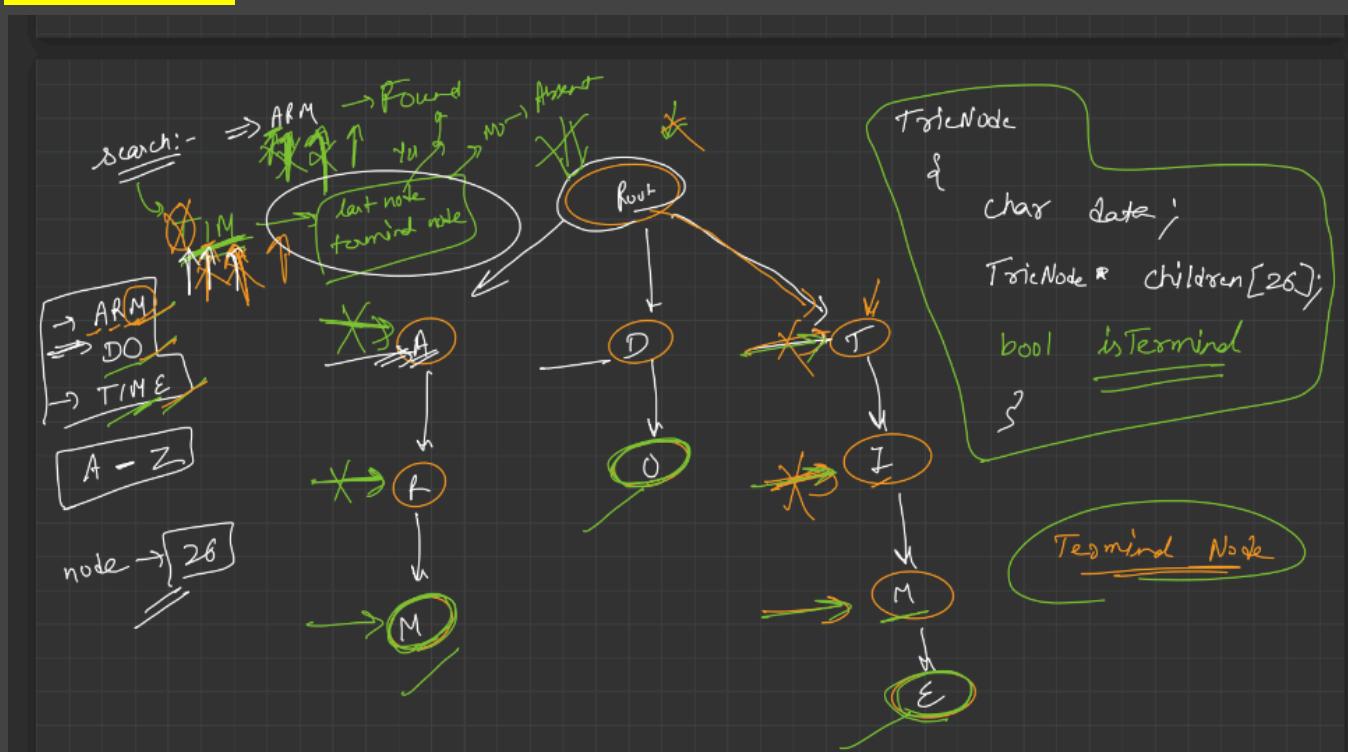
Trie

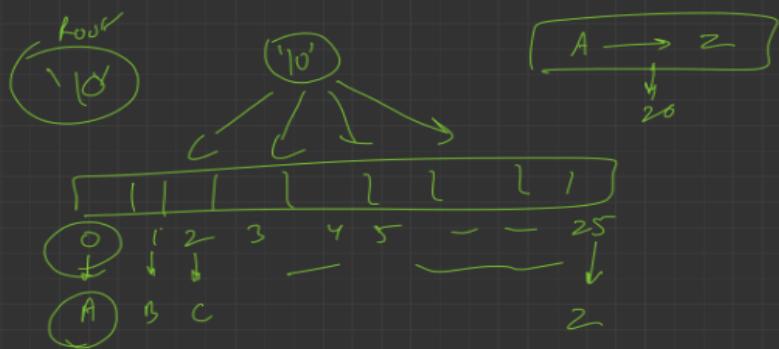
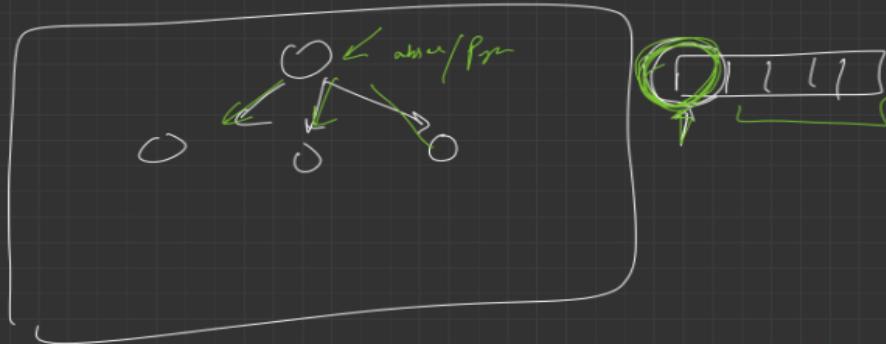
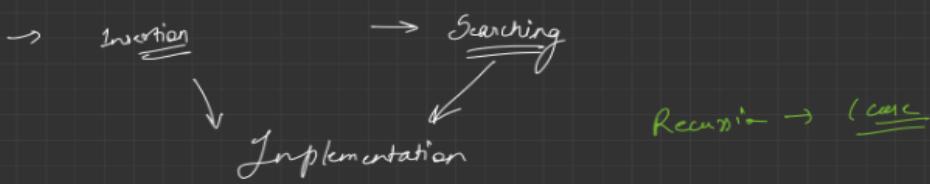


Insert Word:



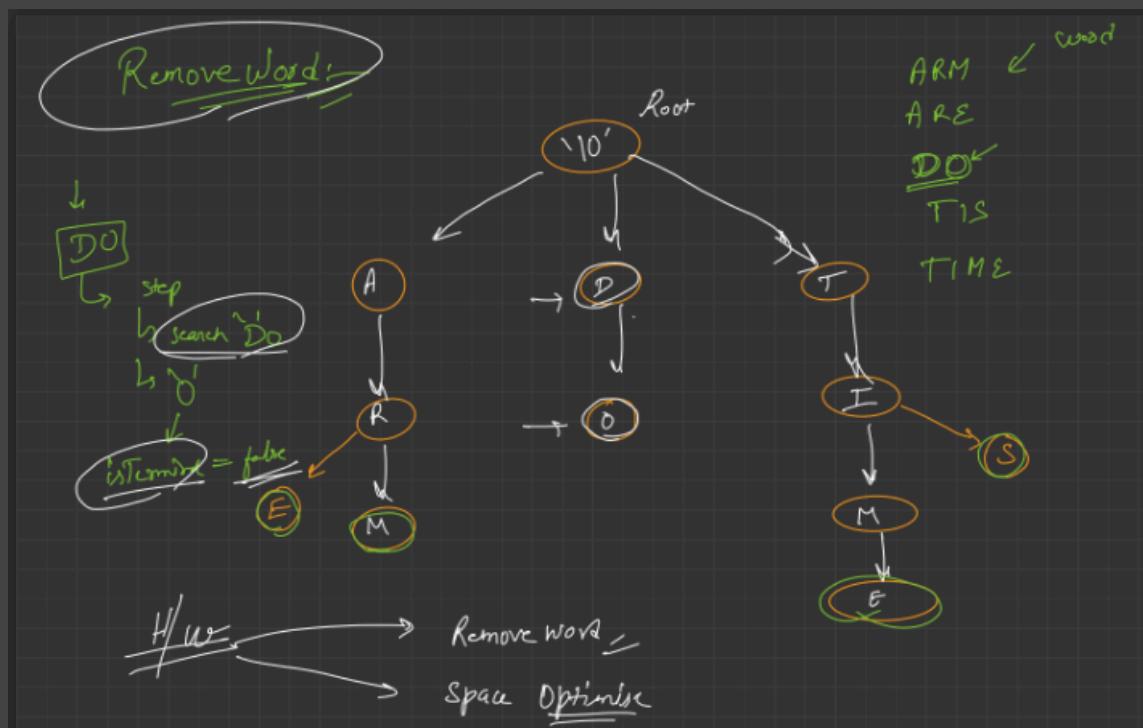
Search Word:



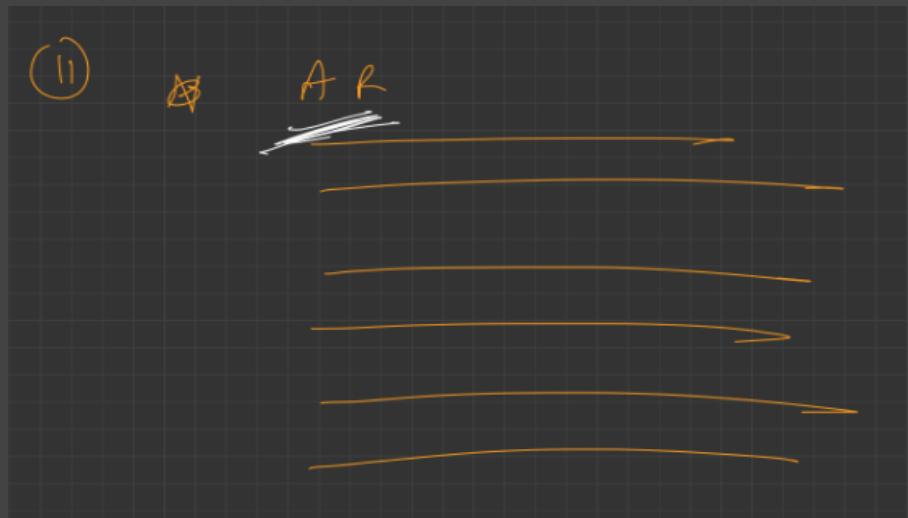
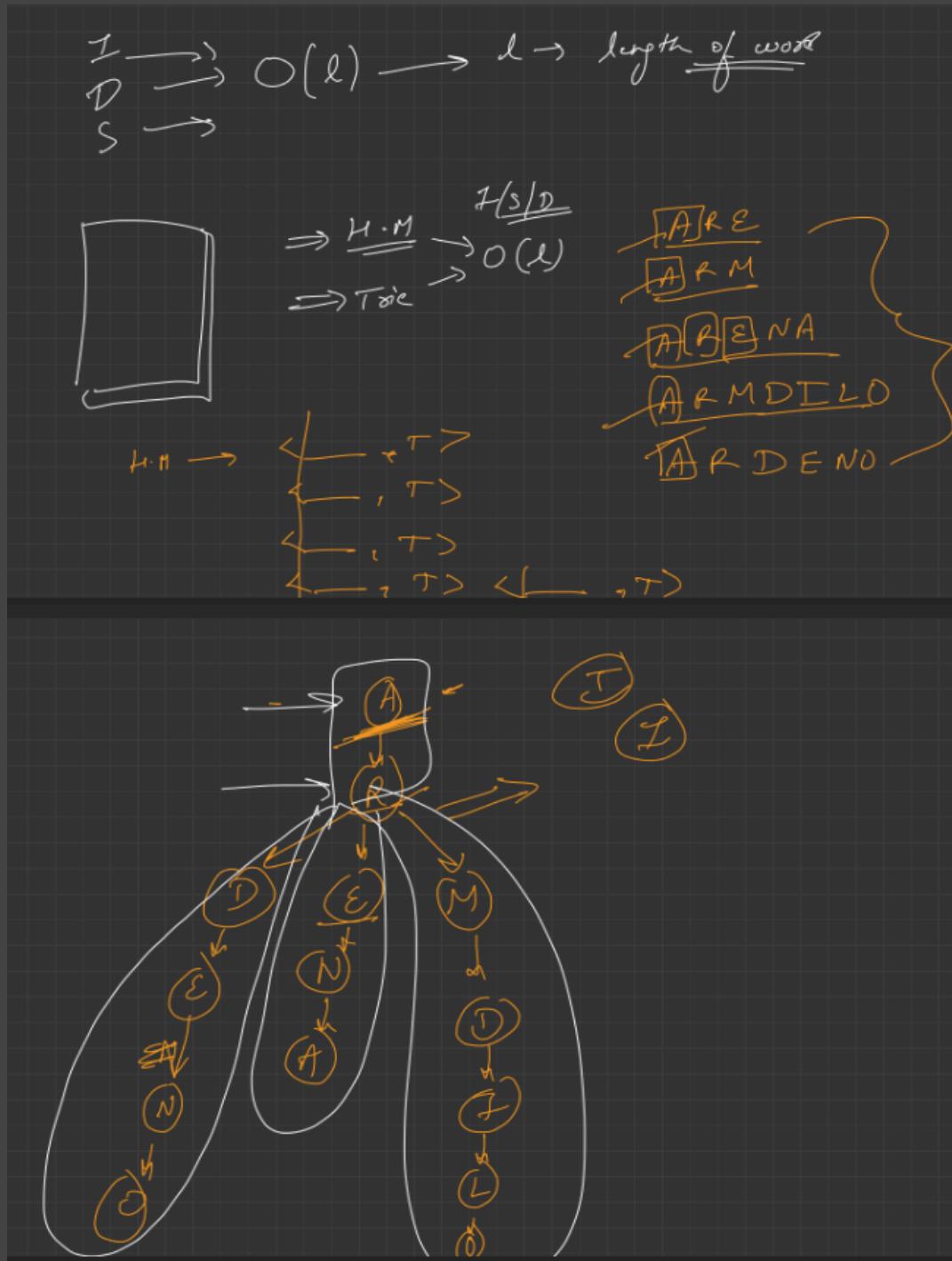


T.C → Invention → $O(l)$ → $l \Rightarrow$ length of word
 → Search → $O(l)$

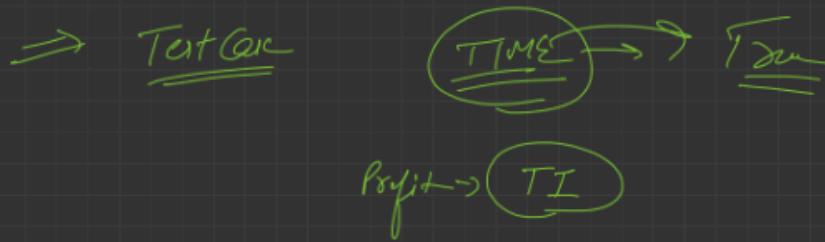
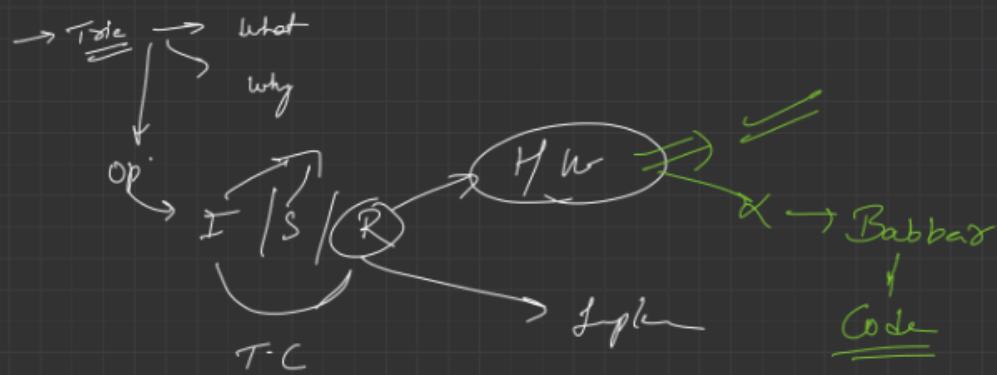
Remove Word:



HashMap v/s Trie:

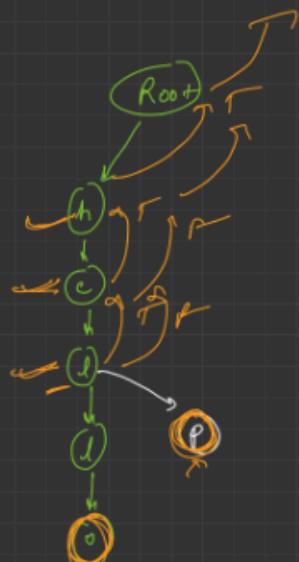


Implement Trie Problem:



CARS

Trie
1
2
3
4
5
Prefix Search

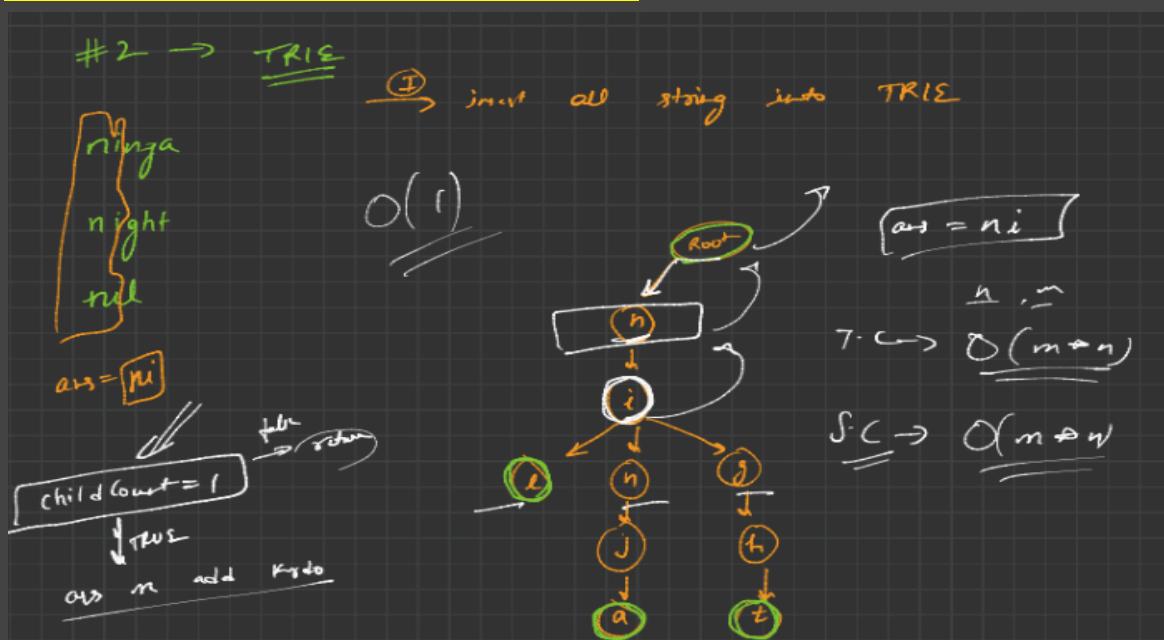


1 → hell
1 → hello
1 → help
2 → help → true
3 → hel hel
2 → hel

Longest Common Prefix Approach-I:

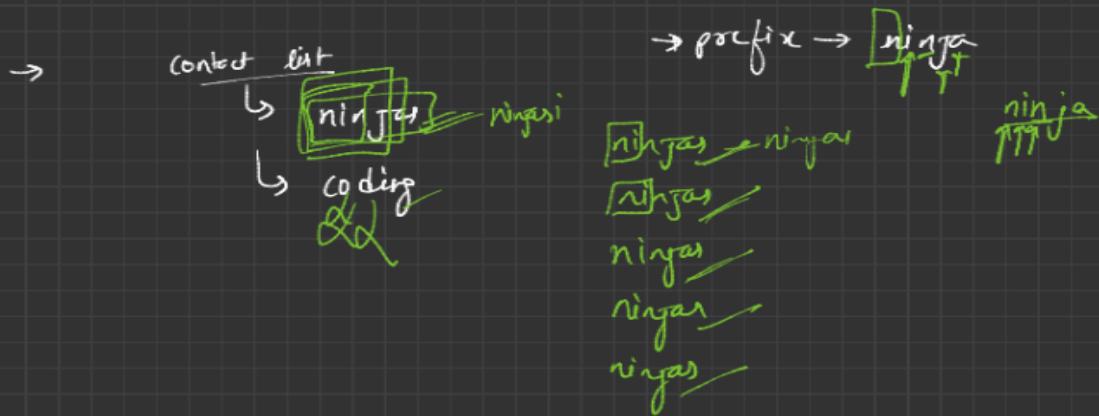
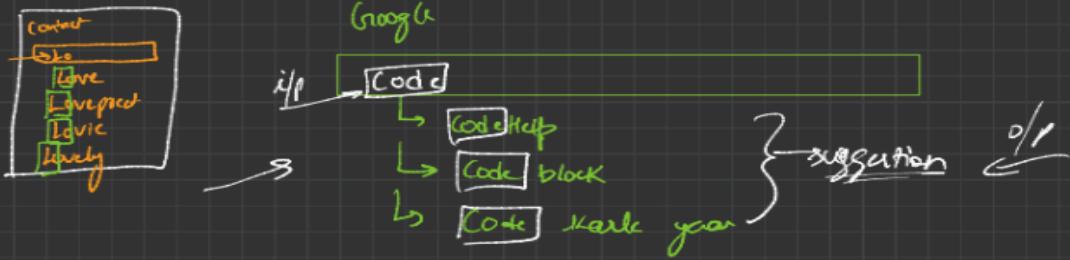


Longest Common Prefix Approach-II:



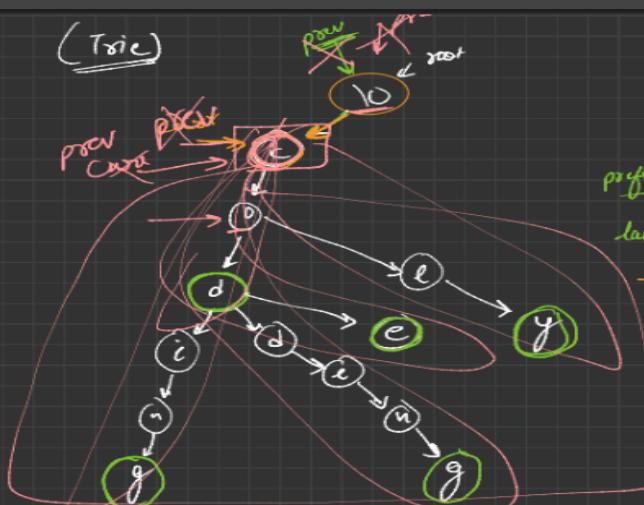
Implement A Phone Directory:

→ Implement a phone directory



- cod
- coding
- coddng
- code
- caly

prefix → coding



Algo:-

prefnStr = co

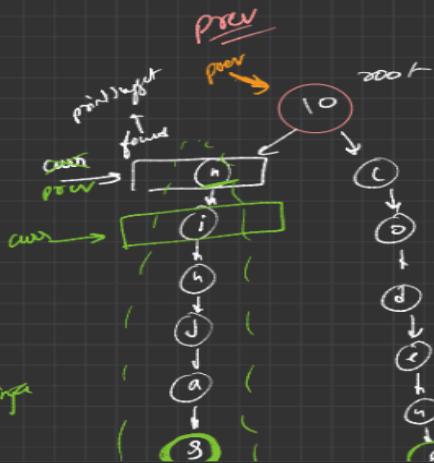
last character = ~~o~~
→ last char found
↓
print suggest

→ nintex
→ coding

→ copy

$$i/p \rightarrow \begin{smallmatrix} n & i \\ \uparrow & \uparrow \\ q & q \end{smallmatrix}$$

ninja →  → ninja



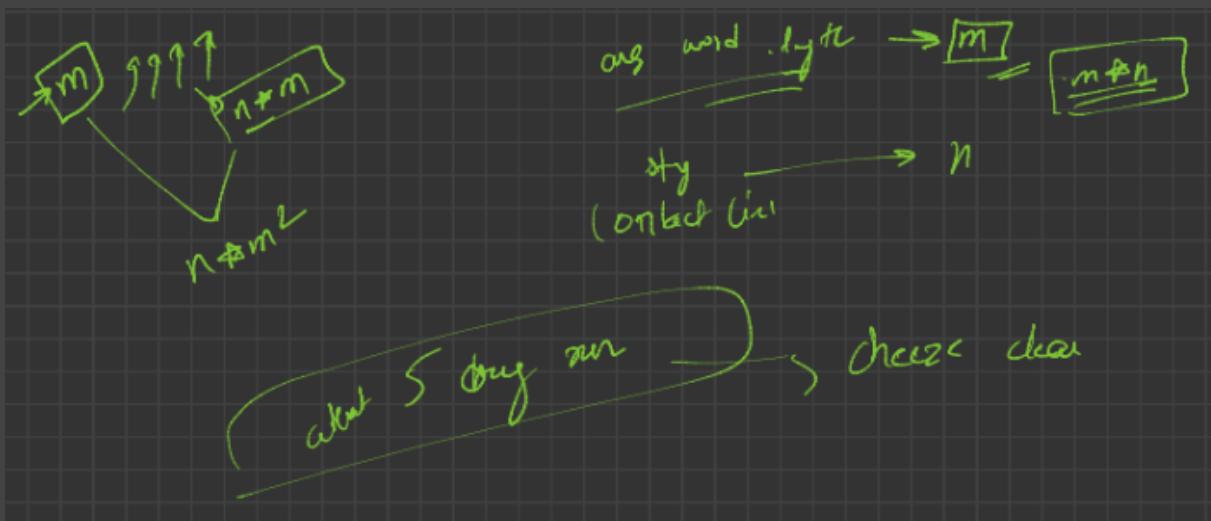
$$\text{last character} = c$$

alpha

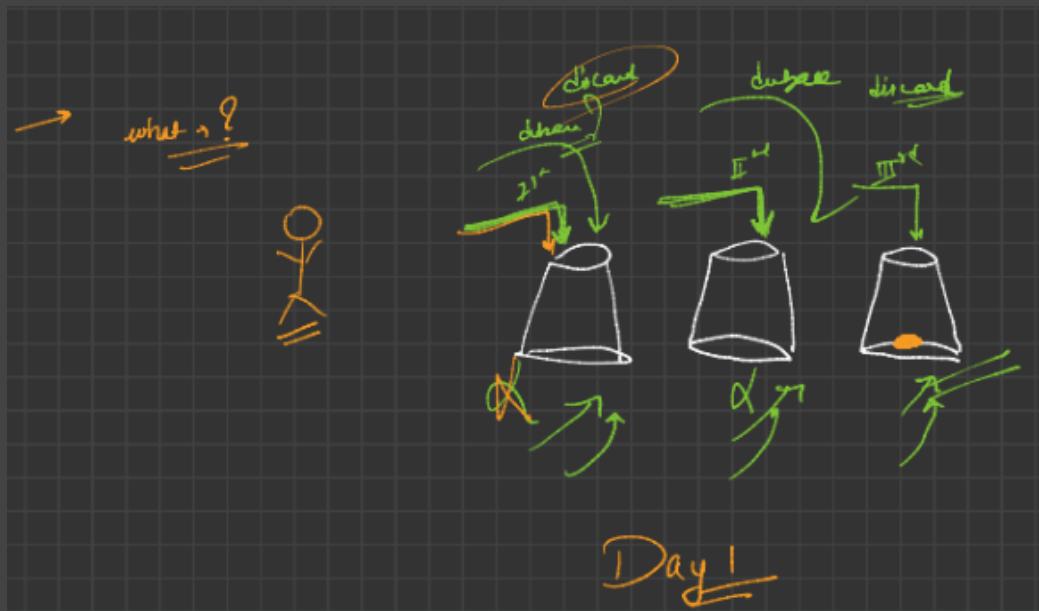
$$\text{prefix} = \underline{n} i$$

$$T.C \rightarrow O(\underline{nm^2})$$

$S \hookrightarrow \boxed{m \oplus n}$

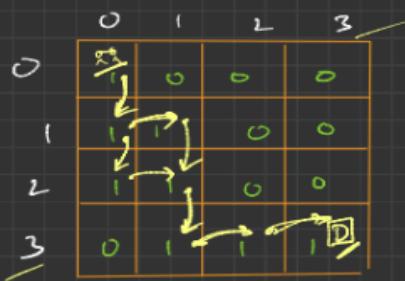


BackTracking



Rat In A Maze Problem:

Rat in a maze Problem



src $\rightarrow (0,0)$
dst $\rightarrow (n-1, n-1) \rightarrow (3,3)$

U, D, L, R \leftarrow movement

1 \rightarrow open path
0 \rightarrow closed

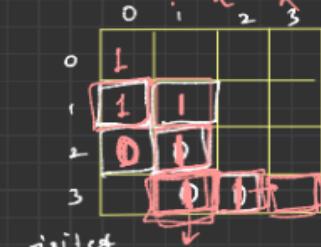
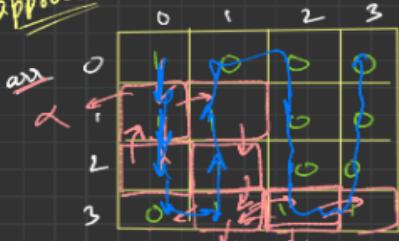
✓ safe

✗ safe

$\begin{array}{l} \text{arr[nx][ny]} = 1 \\ \text{visited[nx][ny]} \\ ! = 1 \\ \rightarrow nx \geq 0, < n \\ ny \geq 0, < n \end{array}$

D D R D F R \leftarrow possible solution
D F D D P P \leftarrow lexicographical \rightarrow D L R U

approach:-



$f(0,0, "") \rightarrow (D, L, R, U)$
via[0][0] = 1

$f(1,0, "D") \rightarrow (D, L, R, U)$
 $v[2][0] = 0$ $v[1][0] = 1$ $f(1,1, "DR") \rightarrow DLRU$
 $v[1][1] = 1$

$f(2,0, "DD") \rightarrow (D, L, R, U)$ $f(2,1, "DDR") \rightarrow DLRU$
 $v[2][0] = 1$ $v[2][1] = 1$

$f(2,1, "DDR") \rightarrow (D, L, R, U)$ $f(3,1, "DDDD") \rightarrow DLRU$
 $v[2][1] = 1$ $v[3][1] = 1$

$f(3,1, "DDDD") \rightarrow (D, L, R, U)$ $f(3,2, "DFDDR") \rightarrow DLRU$
 $v[3][1] = 1$ $v[3][2] = 1$

$f(3,2, "DFDDR") \rightarrow DLRU$

$f(3,3, "DFDDR") \rightarrow DLRU$

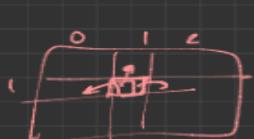
$f(3,2, "DFDDR") \rightarrow DLRU$

f
dst reached
 \rightarrow on return

D L R U

D D R D F R

dst reached
and store

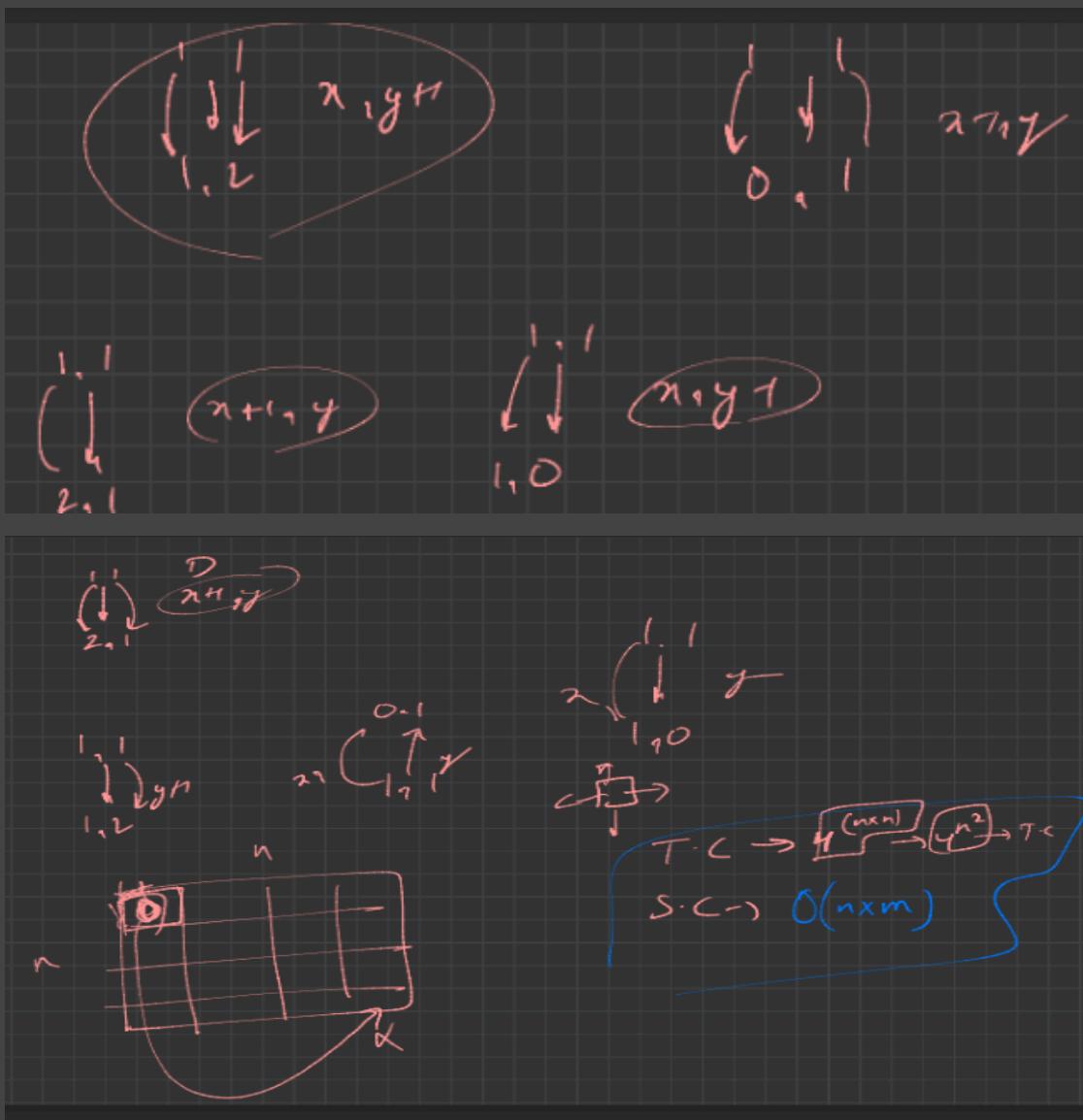


0, 1
↓
1, 0

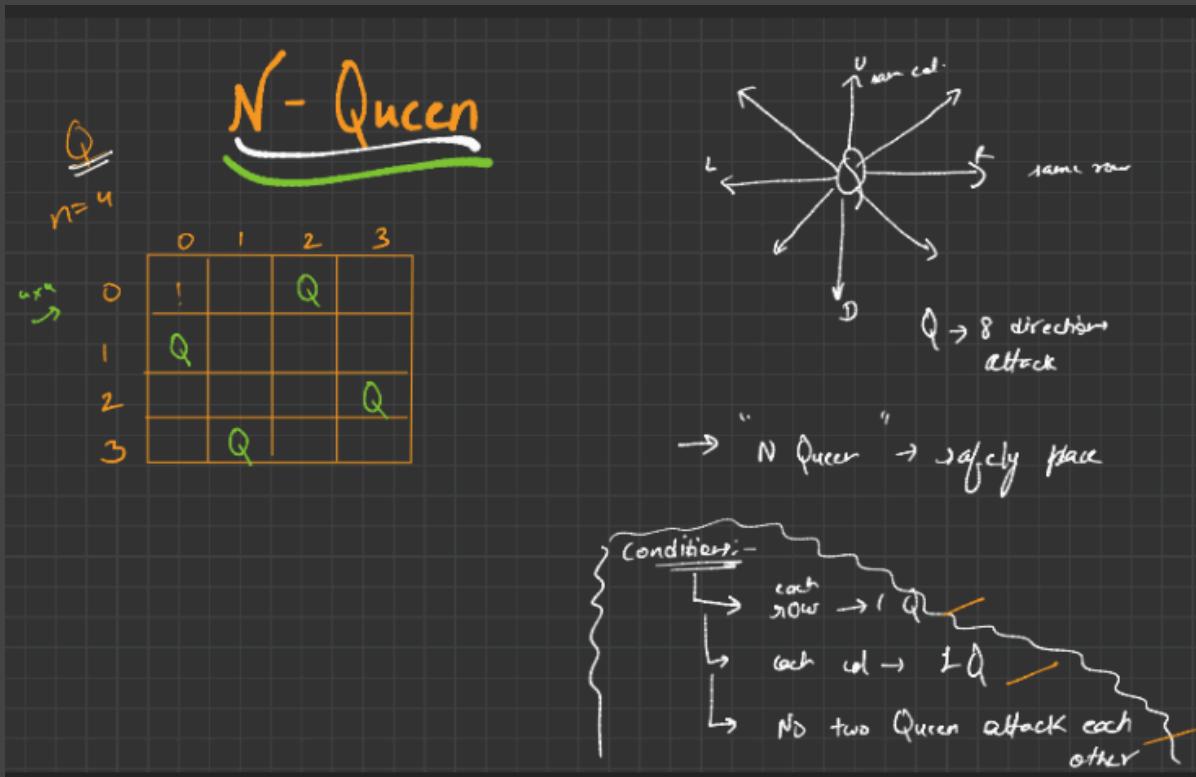
$x + 1, y$

1, 1
↓
1, 0

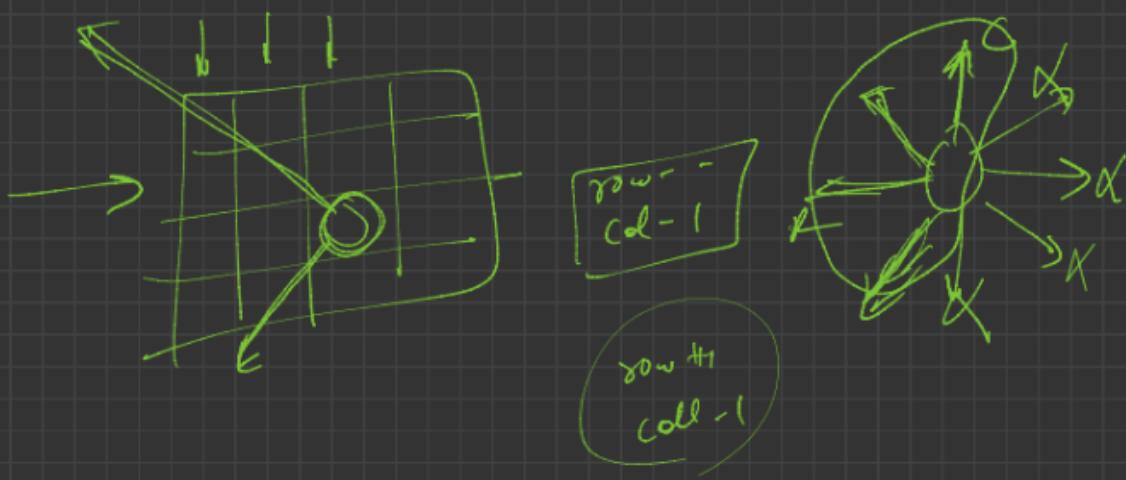
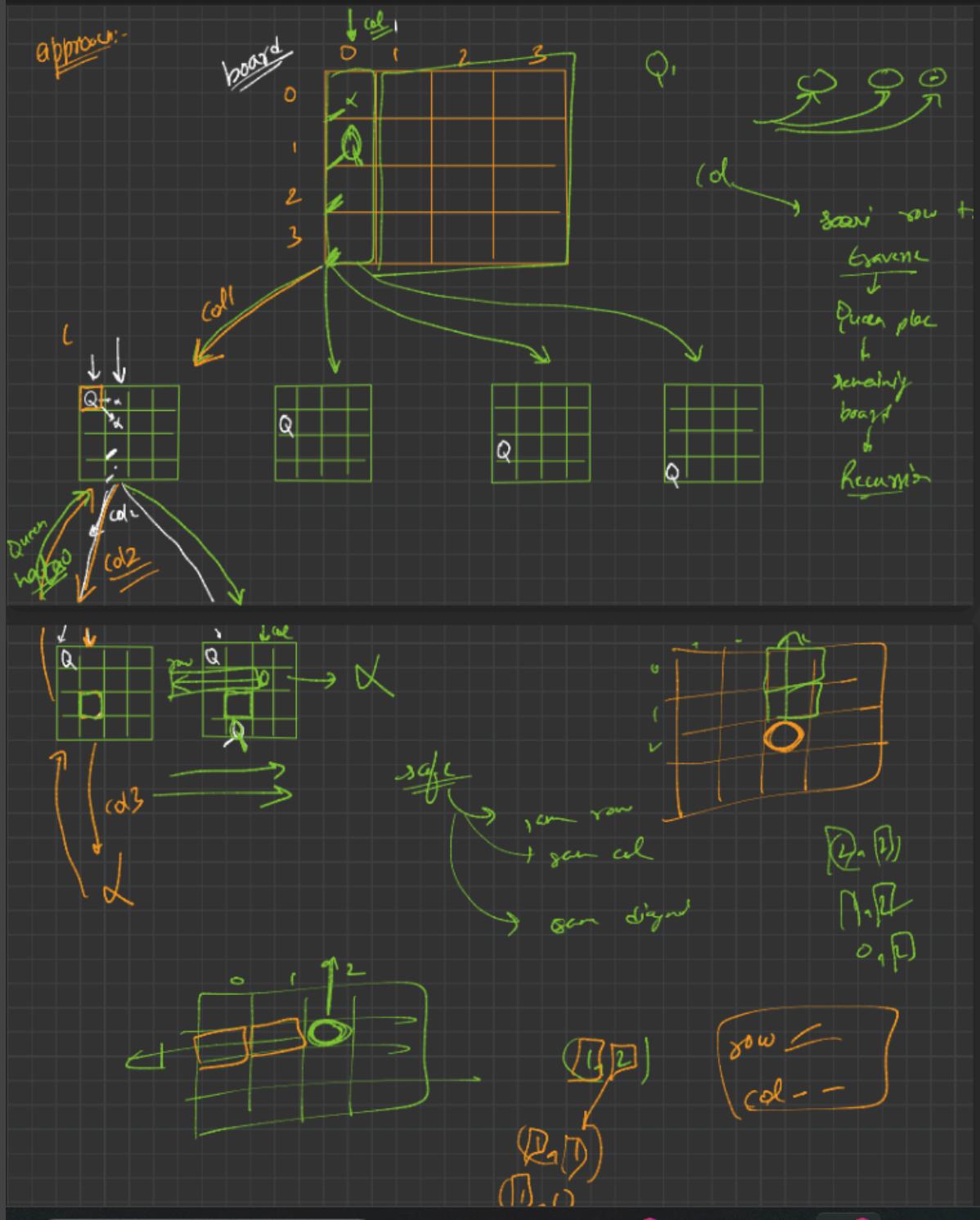
$x, y - 1$
left

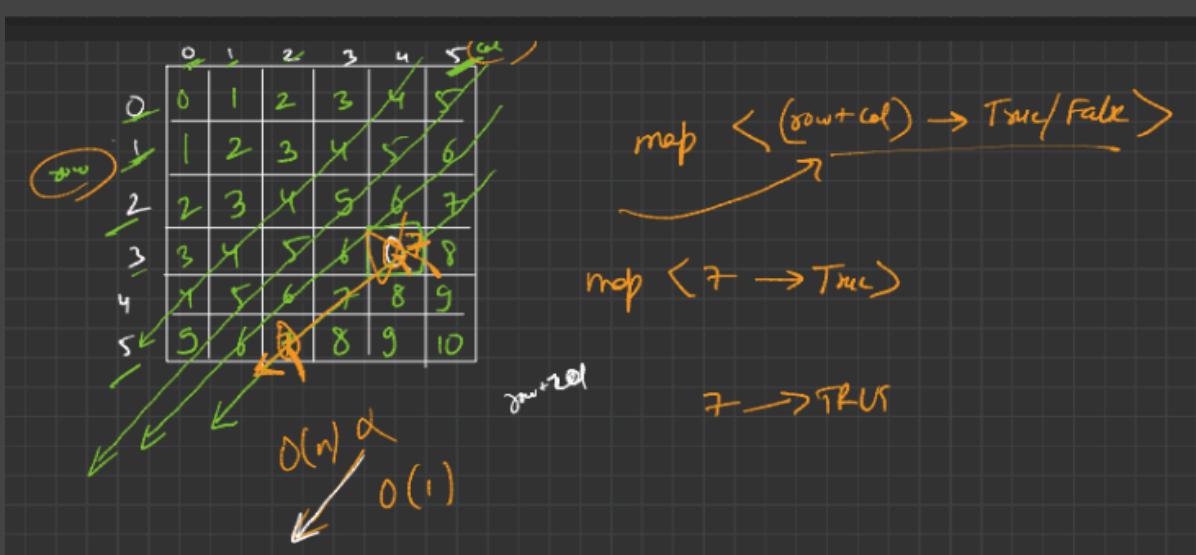
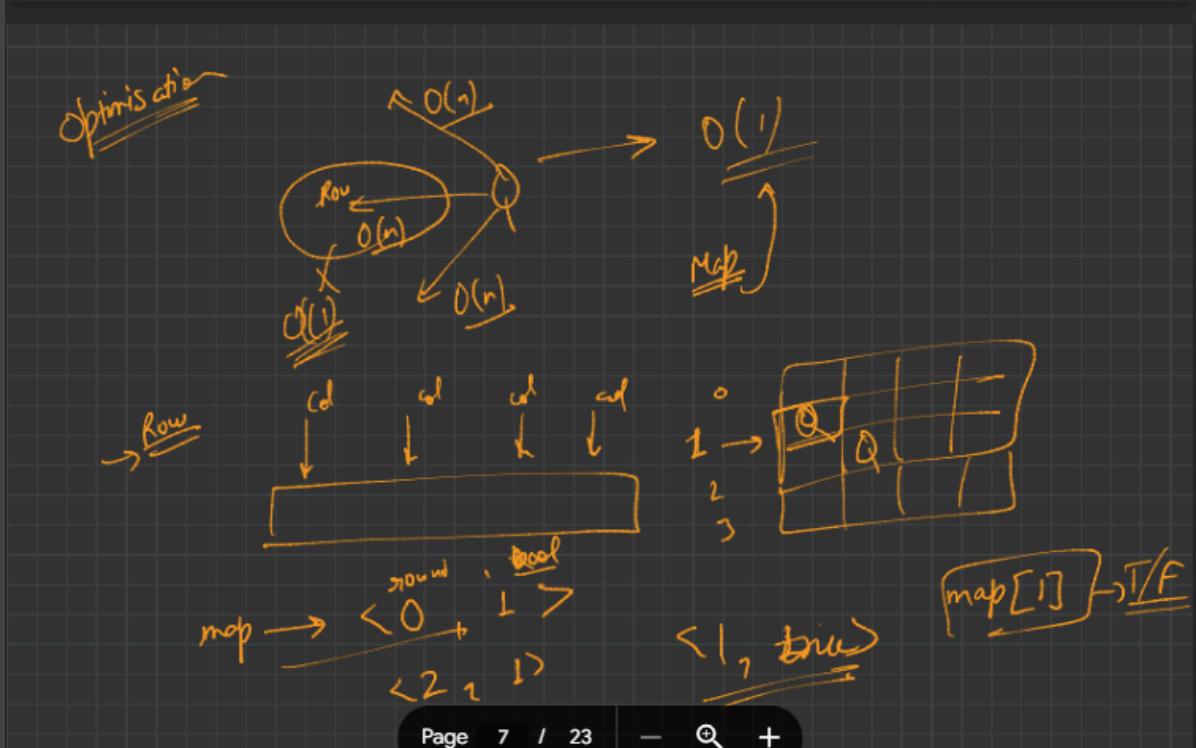
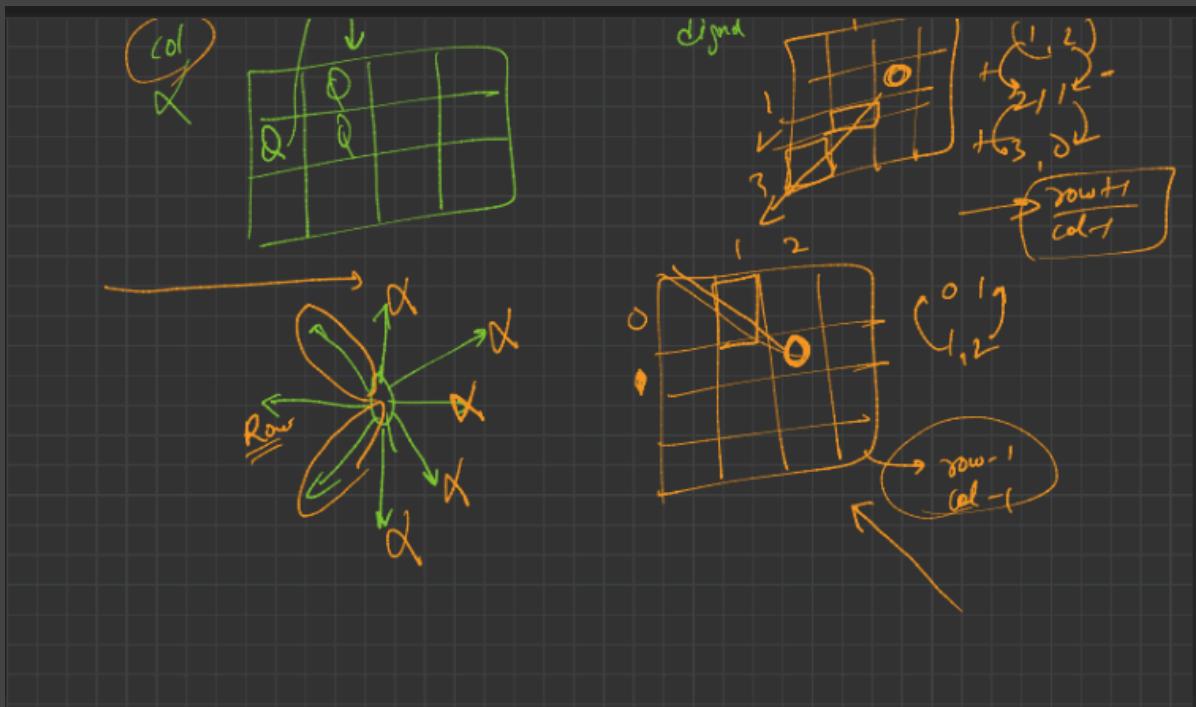


N Queen Problem:



approach:





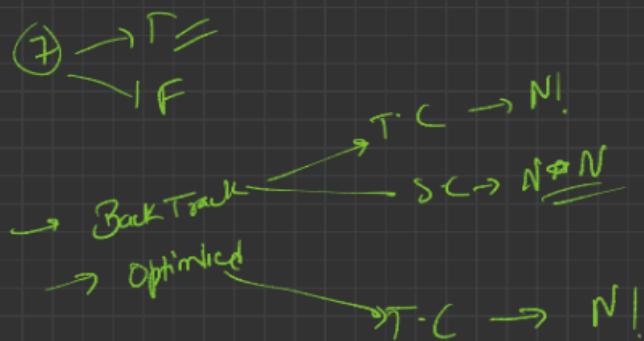
0	5	2	6	7	3	8	9	10
1	4	5	6	7	8	9		
2	3	4	5	6	7	8		
3	2	3	4	5	6	7		
4	1	2	3	4	5	6		
5	0	1	2	3	4	5		

map < $(n-1 + \text{col_row}) \rightarrow \text{T/F}$ >

$$\begin{aligned}
 & n-1 + r-o \\
 & = 6-1 + 5-0 \\
 & = 10 \\
 & \boxed{(n-1) + (\text{col_row})} \\
 & = 6-1 + 1-0 \\
 & = 6 \\
 & n-1 + 2-1 \\
 & = 5 \\
 & n-1 + 4-0 \\
 & = 6-1 + 5-1 \\
 & = 10-1-9 \\
 & = 1 \\
 & n-1 + 5-1 \\
 & = 6-1 + 4-1 \\
 & = 11-2 \\
 & = 9
 \end{aligned}$$

map \rightarrow T \rightarrow True

~~O(N)~~ $\underline{\underline{O(1)}}$



Sudoku Solver Problem:

Sudoku Solver

3	6	5	7	8	-	9	2
5	2	9	1	3	4	7	6
4	8	-	6	2	9	5	3
2	6	3	4	1	5	8	7
3	7	4	8	6	3	1	2
8	5	1	7	9	2	1	4
1	3	8	9	4	7	2	5
6	9	2	3	5	-	8	7
7	4	5	2	8	6	3	1

i/p \rightarrow $9 \times 9 \rightarrow$ Puzzle

Valid soln

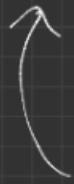
- ① \rightarrow 1 row \rightarrow $\boxed{1-9}$ \rightarrow exactly one
- ② \rightarrow 1 col \rightarrow $\boxed{1-9}$ \rightarrow exactly one
- ③ \rightarrow $\boxed{3 \times 3}$ \rightarrow $\boxed{1-9}$ \rightarrow exact

Sudoku

3×3

→ approach:-

1-9



3	1	6	5	7	8	4	9	2
5	2	9	1	3	4	7	6	8
4	8	7	6	2	9	5	3	1
2	6	3	4	1	5	9	8	7
3	7	4	8	6	3	1	2	5
8	5	1	7	9	2	6	4	3
1	3	8	9	4	7	2	5	6
6	9	2	3	5	-	8	7	4
7	4	5	2	8	6	3	1	9

matrix

for (int i = 0 - 9) {
 for (int j = 0 - 9)

 if cell == empty

 for (int val = 1 - 9)

3	1	6	5	7	8	4	9	2
5	2	9	1	3	4	7	6	8
4	8	7	6	2	9	5	3	1
2	6	3	4	1	5	9	8	7
3	7	4	8	6	3	1	2	5
8	5	1	7	9	2	6	4	3
1	3	8	9	4	7	2	5	6
6	9	2	3	5	-	8	7	4
7	4	5	2	8	6	3	1	9

1 2 3 4
X
L

if (isSafe)

 board[i][j] = val
 recursion

//backtrack

 board[i][j] = 0
}

1
2
3
4
5
6
7

4
↓
↓

3	1	6	5	7	8	4	9	2
5	2	9	1	3	4	7	6	8
4	8	7	6	2	9	5	3	1
2	6	3	4	1	5	9	8	7
3	7	4	8	6	3	1	2	5
8	5	1	7	9	2	6	4	3
1	3	8	9	4	7	2	5	6
6	9	2	3	5	-	8	7	4
7	4	5	2	8	6	3	1	9

3	1	6	5	7	8	4	9	2
5	2	9	1	3	4	7	6	8
4	8	7	6	2	9	5	3	1
2	6	3	4	1	5	9	8	7
3	7	4	8	6	3	1	2	5
8	5	1	7	9	2	6	4	3
1	3	8	9	4	7	2	5	6
6	9	2	3	5	-	8	7	4
7	4	5	2	8	6	3	1	9

3
3

1

3	1	6	5	7	8	4	9	2
5	2	9	1	3	4	7	6	8
4	8	7	6	2	9	5	3	1
2	6	3	4	1	5	9	8	7
3	7	4	8	6	3	1	2	5
8	5	1	7	9	2	6	4	3
1	3	8	9	4	7	2	5	6
6	9	2	3	5	1	8	7	4
7	4	5	2	8	6	3	1	9

$\text{val} = 1$ $\text{col} = 1$ $\text{row} = 0$ 	$\text{for } i \rightarrow 0 \rightarrow 9$ $3 * (\frac{\text{row}}{3}) + \frac{i}{3}$ $3 * (\frac{\text{col}}{3}) + i \% 3$
$i \rightarrow 0 \rightarrow 3 * \frac{0}{3} + \frac{0}{3} = 0 \quad (0,0)$ $3 * \left(\frac{1}{3}\right) + 0 \% 3 = 0$	$i \rightarrow 1 \quad 3 * \left(\frac{0}{3}\right) + \frac{1}{3} = 0 \quad (0,1)$ $3 * \left(\frac{1}{3}\right) + 1 \% 3 = 0 + 1 = 1$
$i \rightarrow 3 \rightarrow 3 * \frac{0}{3} + \frac{2}{3} = 0 + 1 = 1 \quad (1,0)$ $3 * \left(\frac{1}{3}\right) + 3 \% 3 = 0 + 0 = 0$	$i = 2 \rightarrow 3 * \left(\frac{0}{3}\right) + \frac{2}{3} = 0 \quad (0,2)$ $3 * \left(\frac{1}{3}\right) + 2 \% 3 = 0 + 2 = 2$

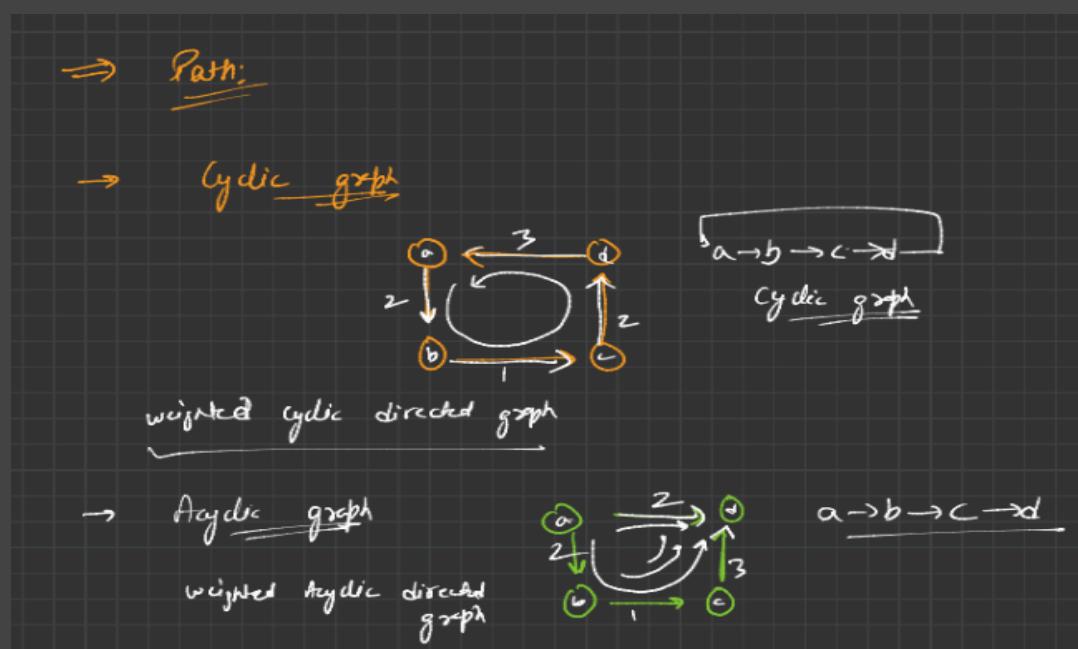
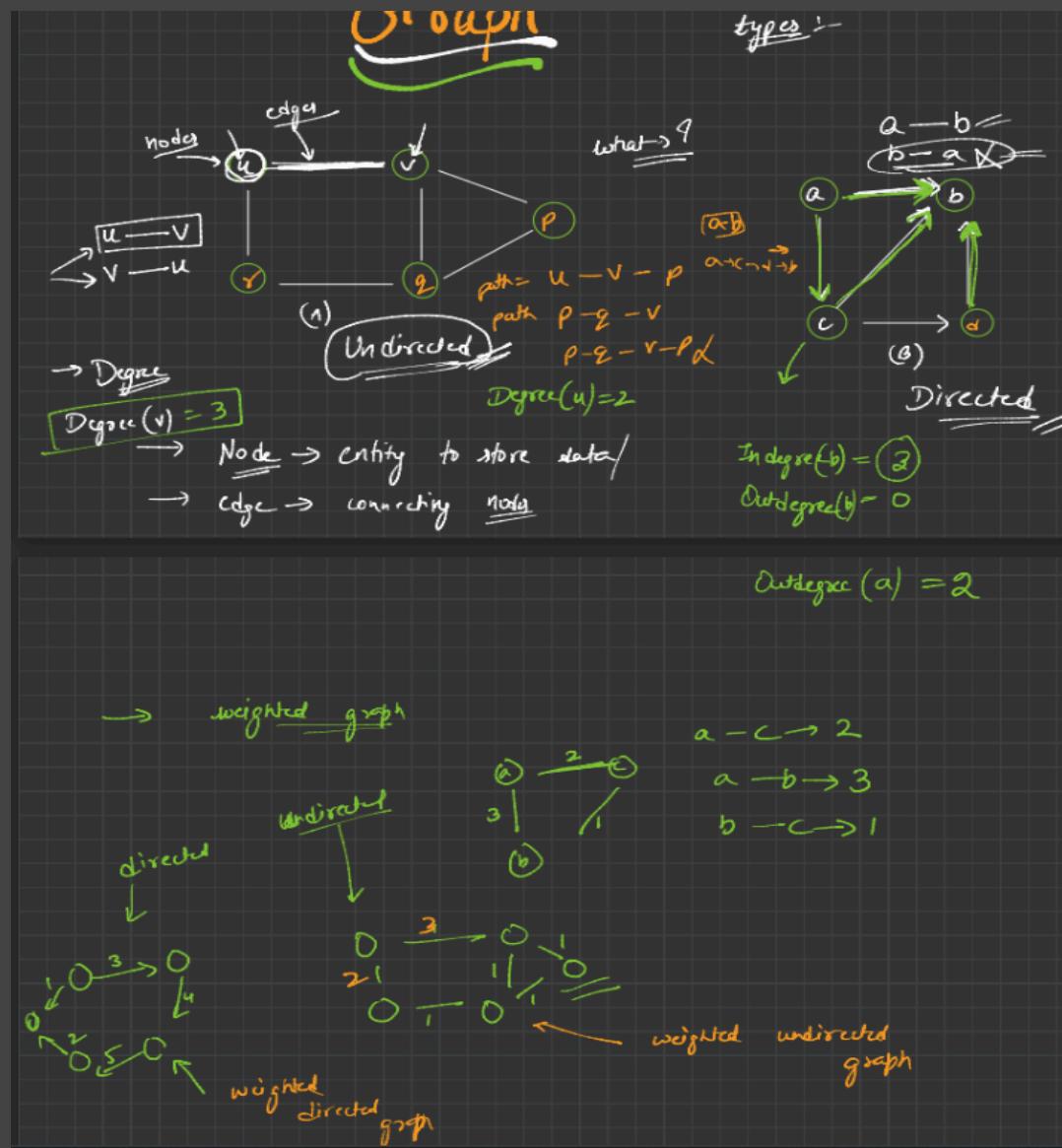
$T \cdot C \rightarrow \sqrt{g^m}$ $m \rightarrow \text{no. of empty cells}$

$S \cdot C \rightarrow O(1)$

$$9 \times 9 = \boxed{81} \rightarrow$$

Graph

Introduction:



Adjacency Matrix:

→ Graph:-

- Adjacency matrix
- Adjacency List

→ Adjacency matrix

0	1	2
0	0 1 0	
1	0 0 1	
2	1 0 0	

$0 \rightarrow 0$
 $0 \rightarrow 1$
 $0 \rightarrow 2$
 $1 \rightarrow 0$
 $1 \rightarrow 1$
 $1 \rightarrow 2$
 $2 \rightarrow 0$
 $2 \rightarrow 1$
 $2 \rightarrow 2$

→ 2D matrix

$O(n^2)$

i/p ↴

\rightarrow number of nodes (n)
 \rightarrow no. of edges \rightarrow (m)

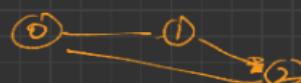
($n=3, m=3$)

$0 \rightarrow 1$
 $1 \rightarrow 2$
 $2 \rightarrow 0$

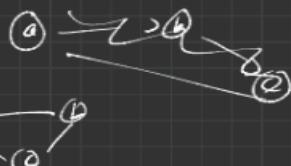
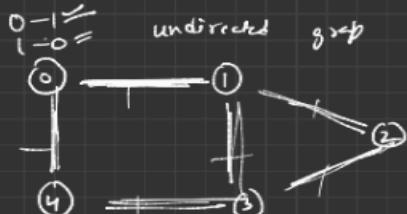
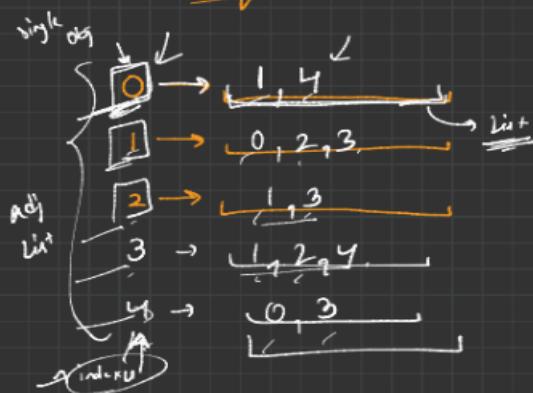
edges
 $m=3$



Adjacency List:



② Adjacency List



→ Implementation:-

adj. list

vector < vector < int > >

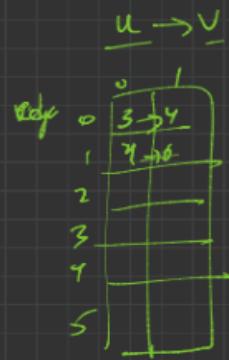
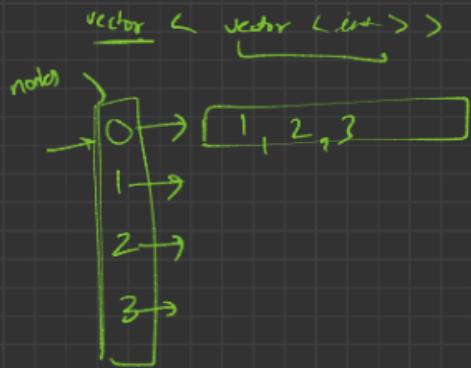
\mapsto map < $\frac{\text{int}}{\text{char}}$, list < int > >;
 atm

$0 \longrightarrow 1$

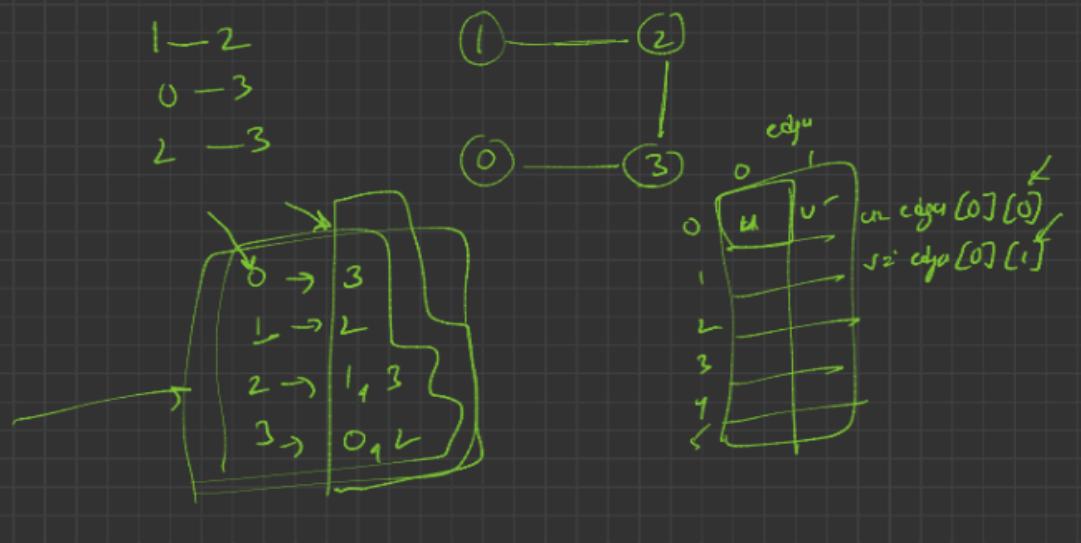
$0 \longrightarrow 1$

0d → $\begin{cases} 0 \rightarrow 1 \\ 1 \rightarrow 0 \end{cases}$

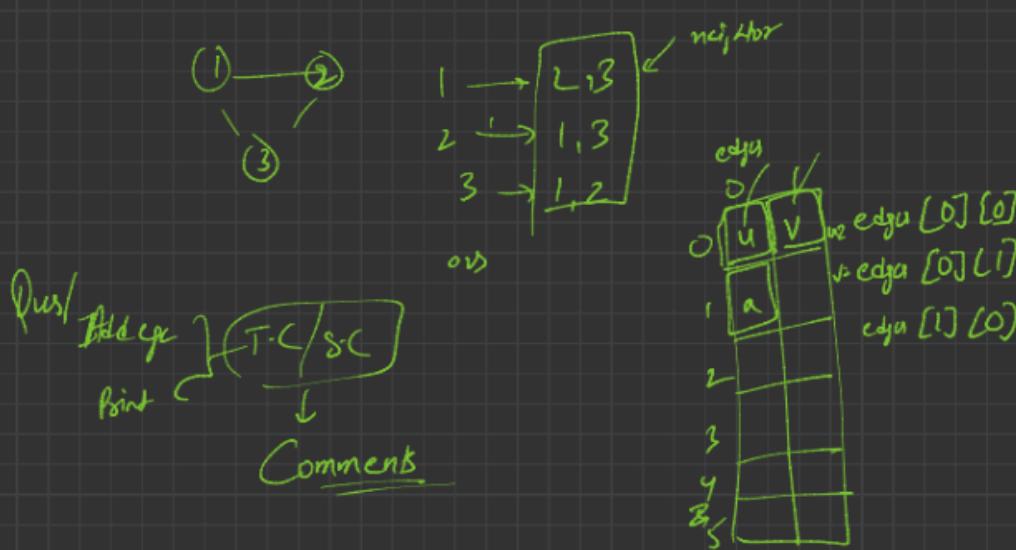
$0 \rightarrow 1$
 $1 \rightarrow 0$



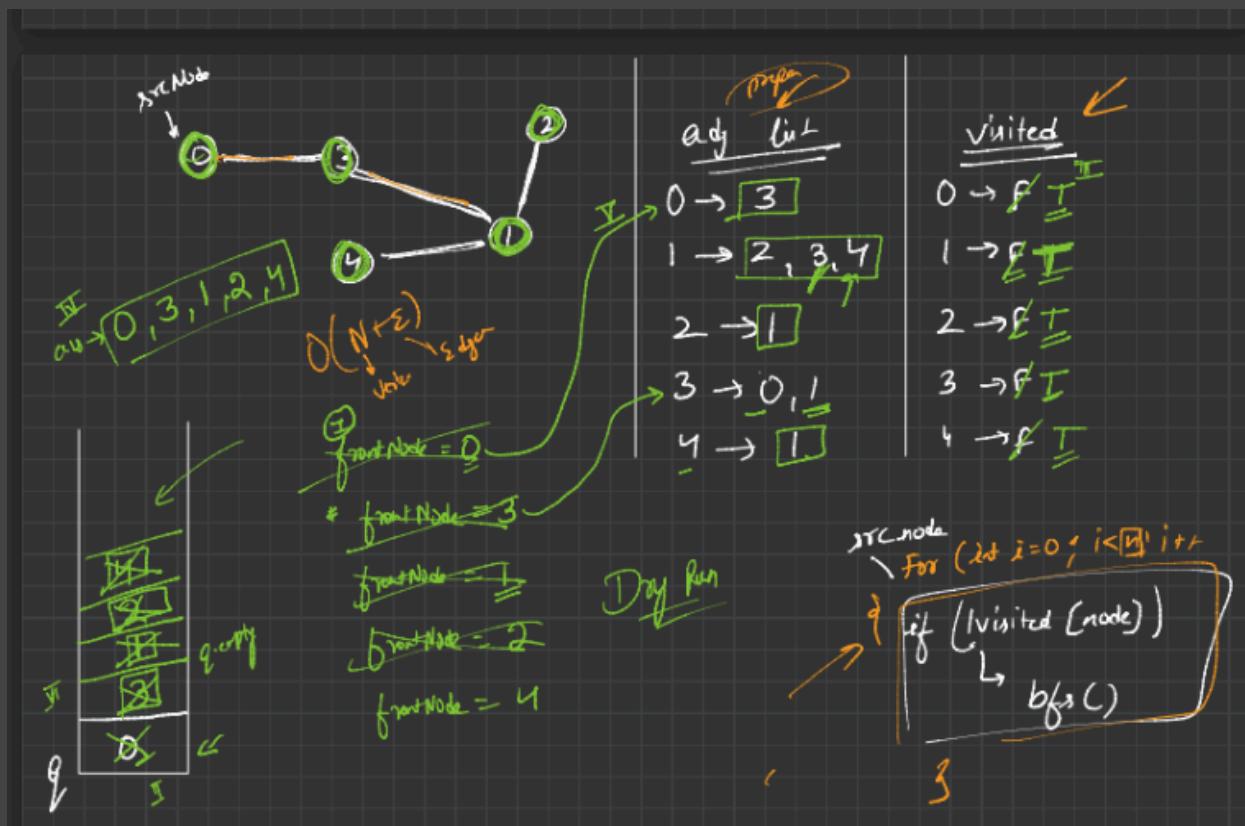
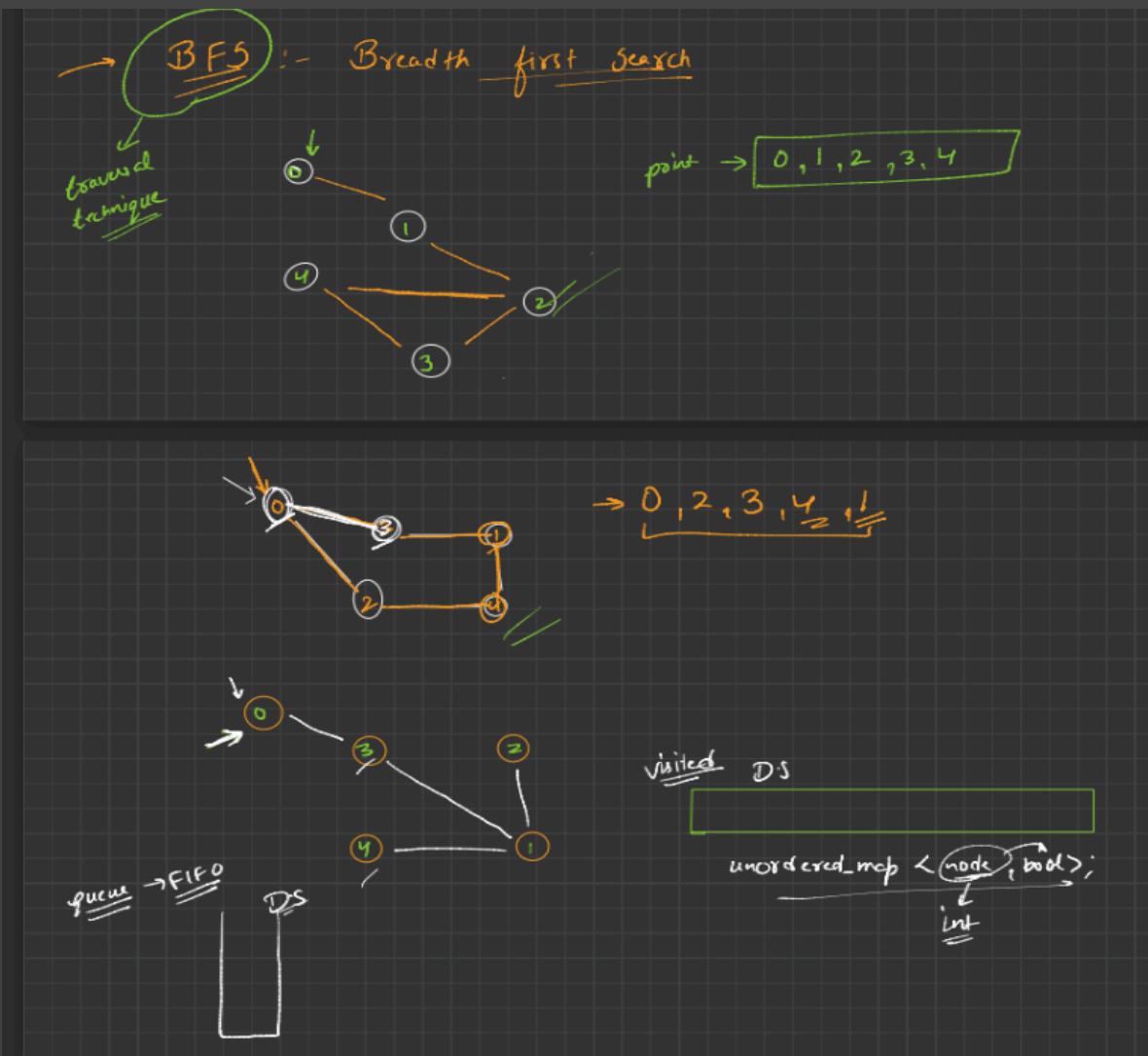
ans

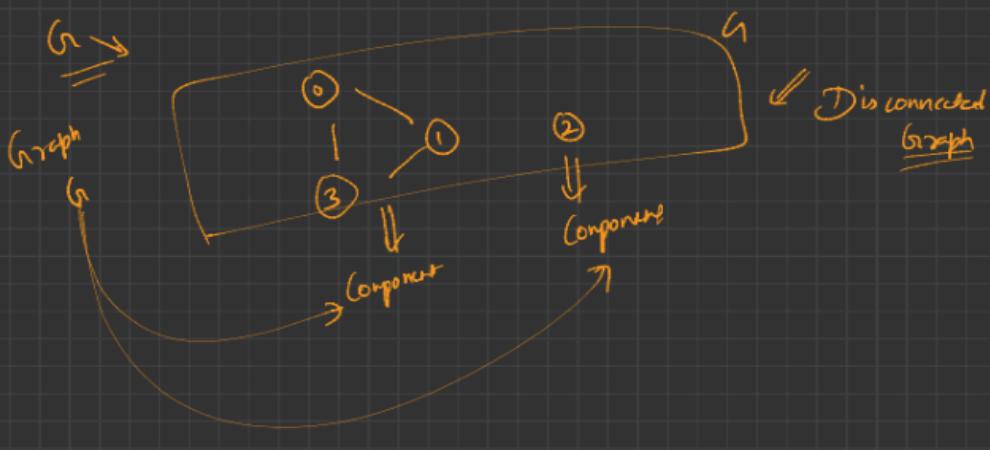


Creating And Printing A Graph:

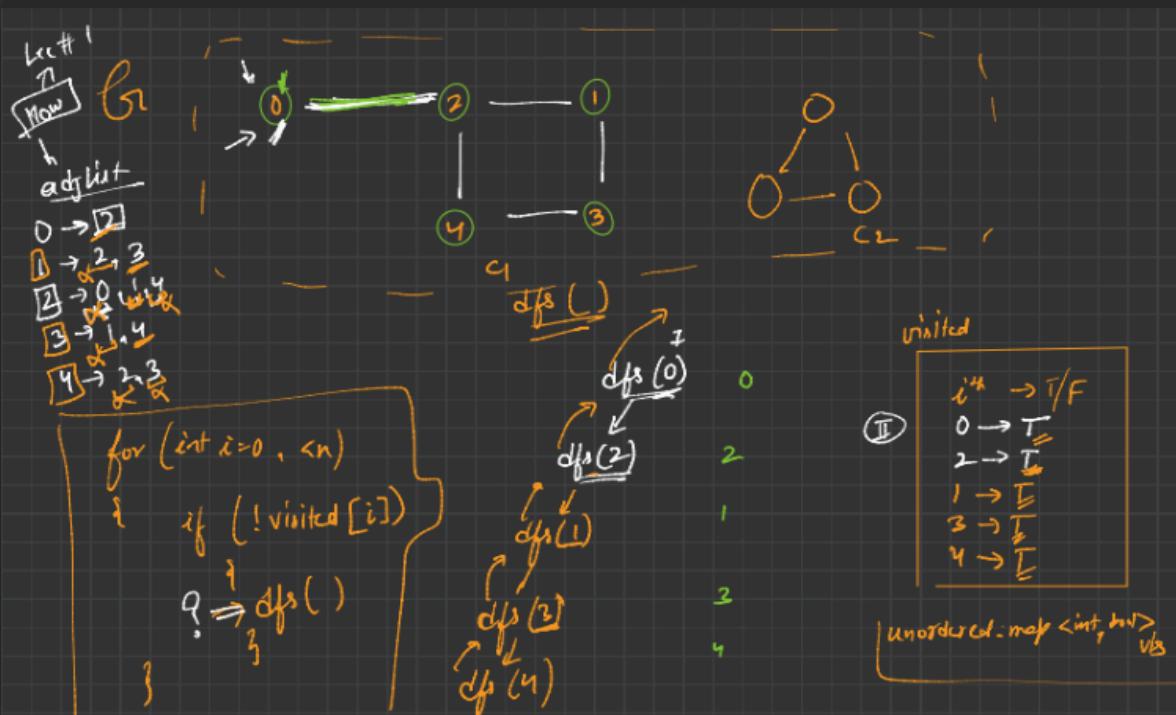
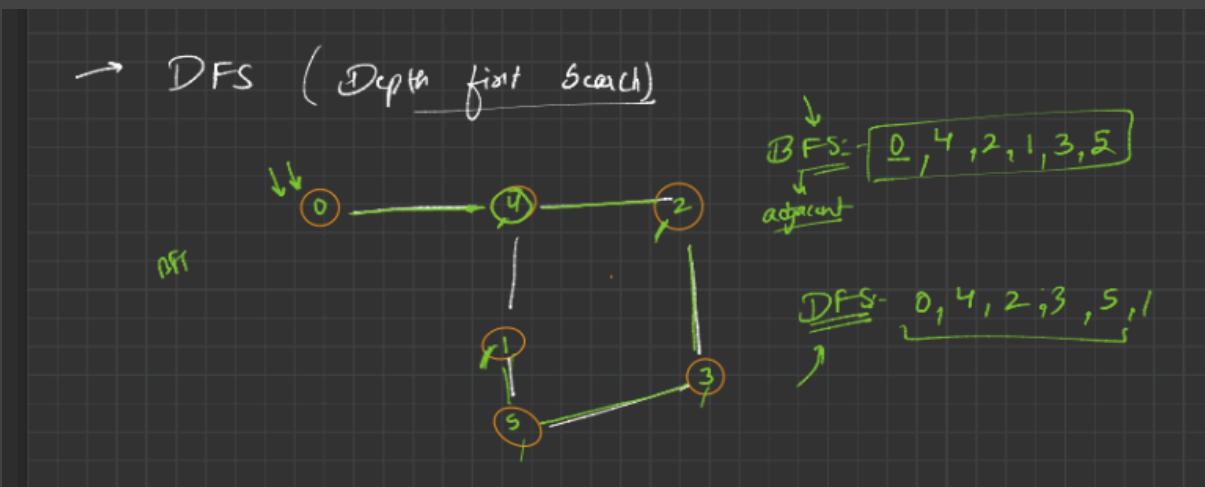


Breadth First Search(BFS) Traversal:



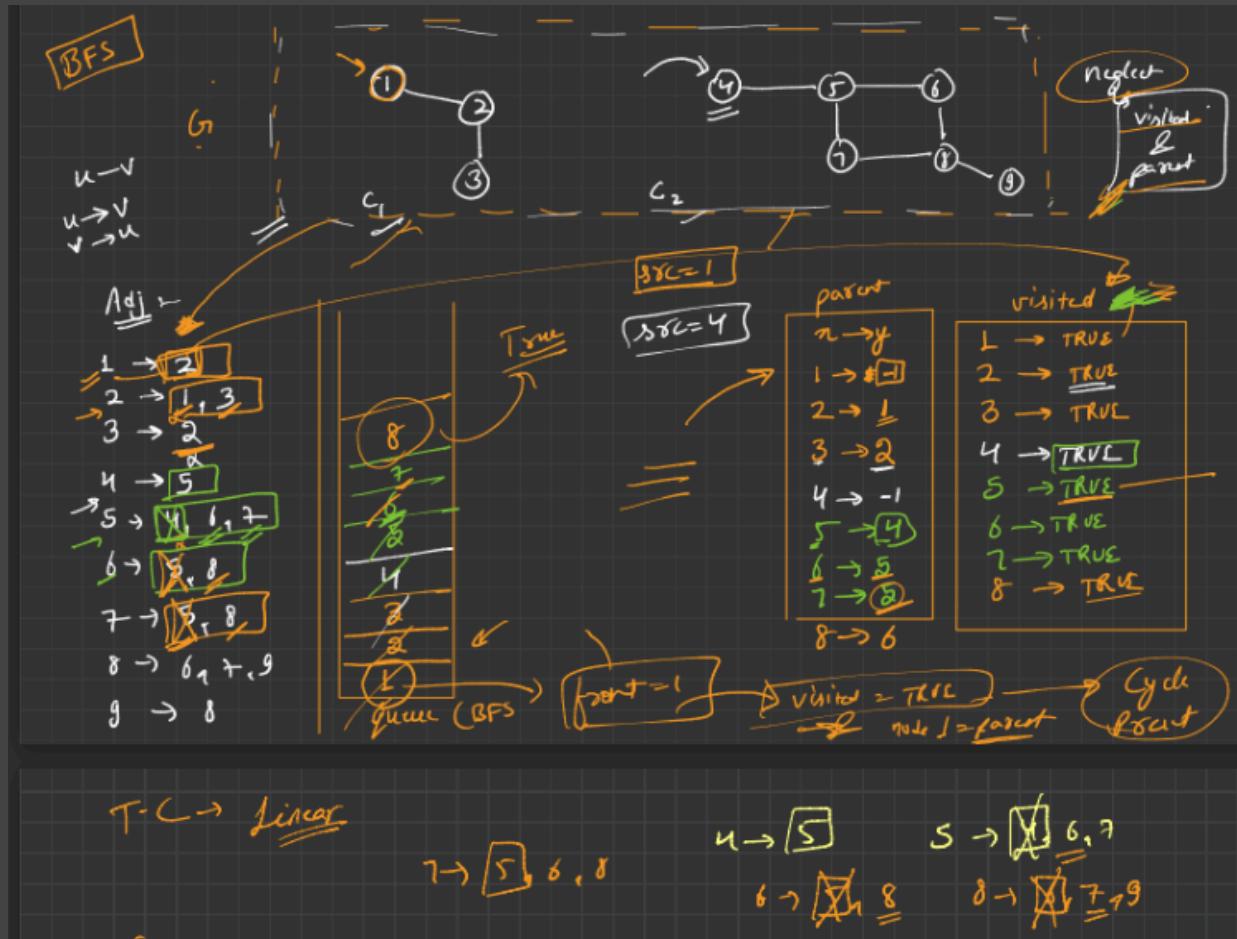


Depth First Search(DFS) Traversal:

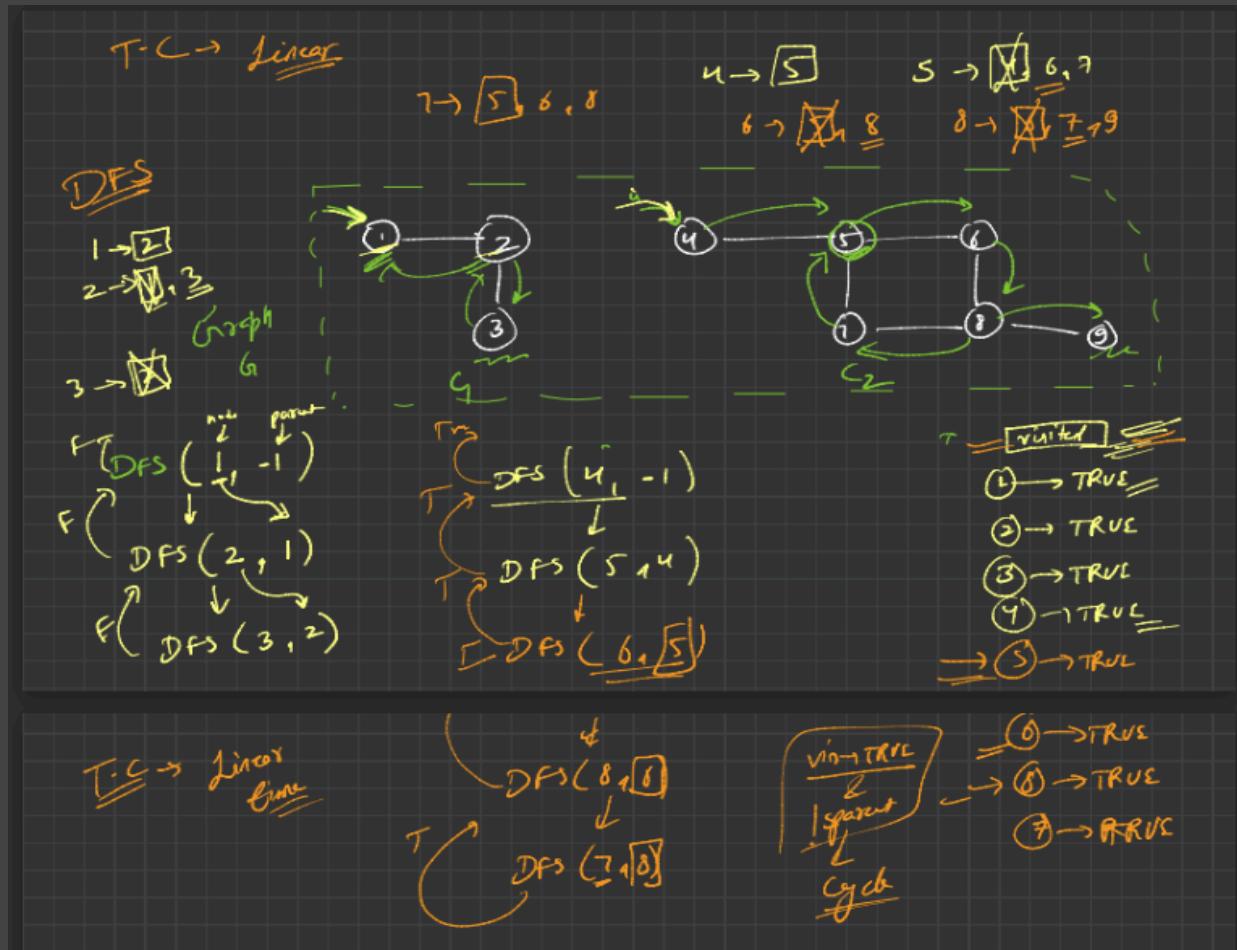


T.C → Linear
S.C

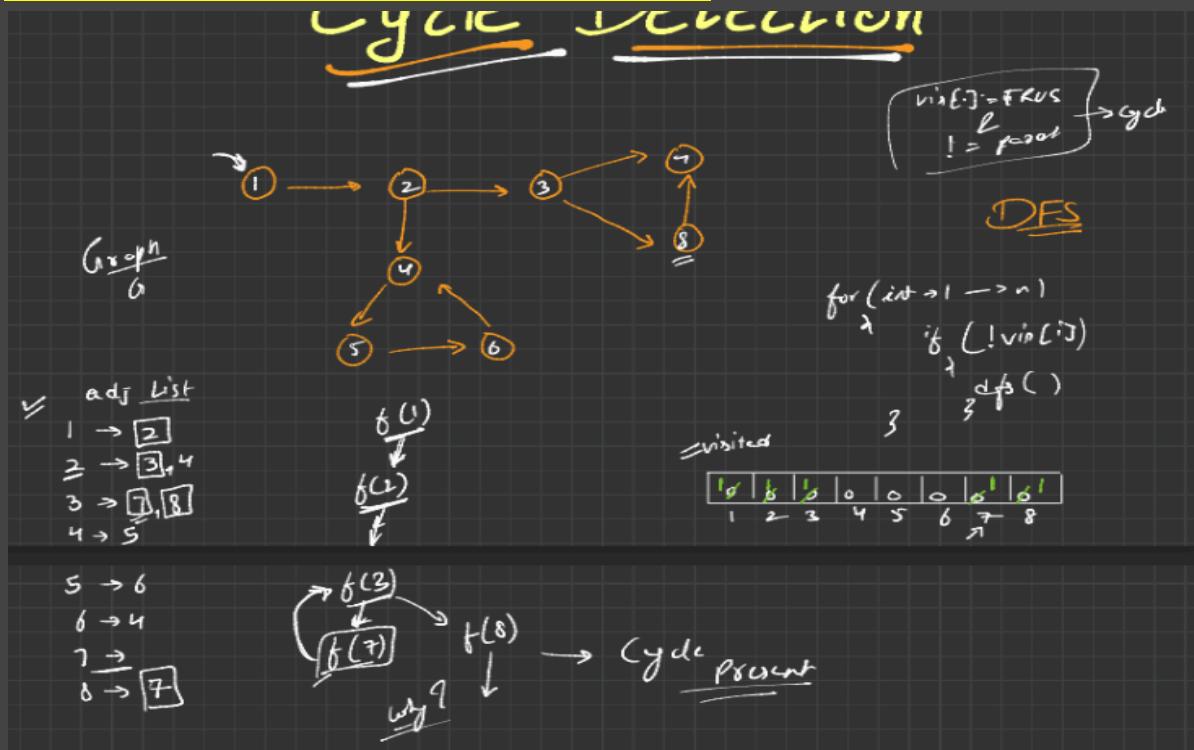
Cycle Detection In Undirected Graphs(BFS):



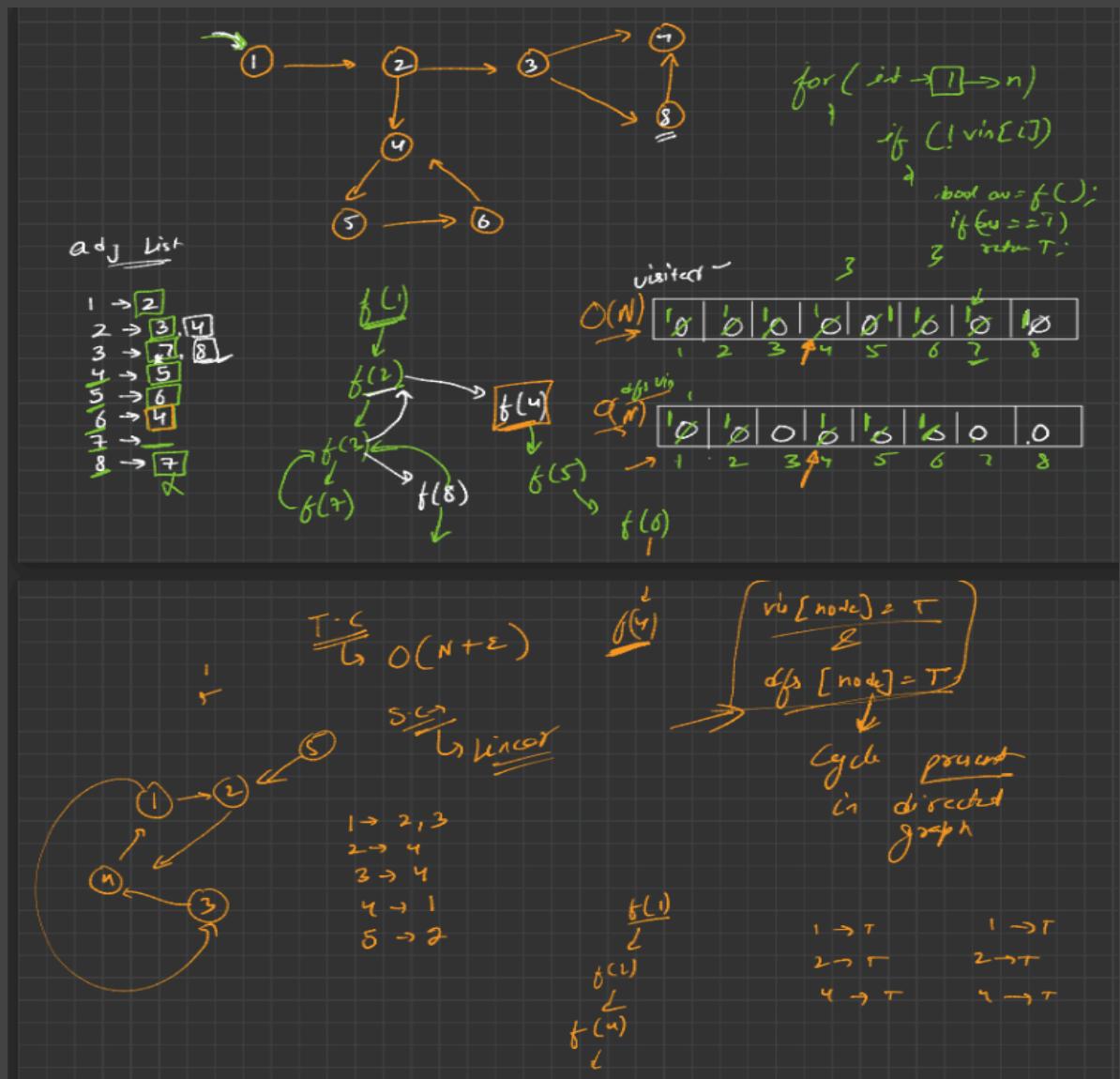
Cycle Detection In Undirected Graphs(DFS):



Cycle Detection In Directed Graphs(DFS):



The above method will not work so, we go with the below method

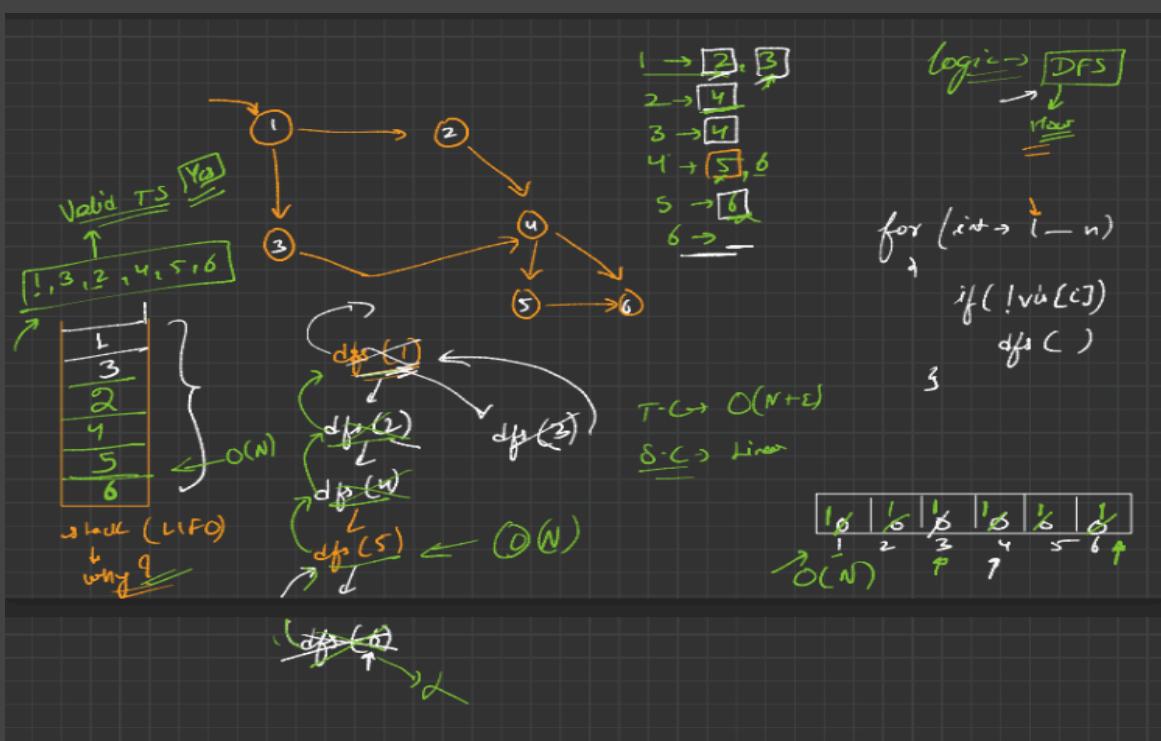
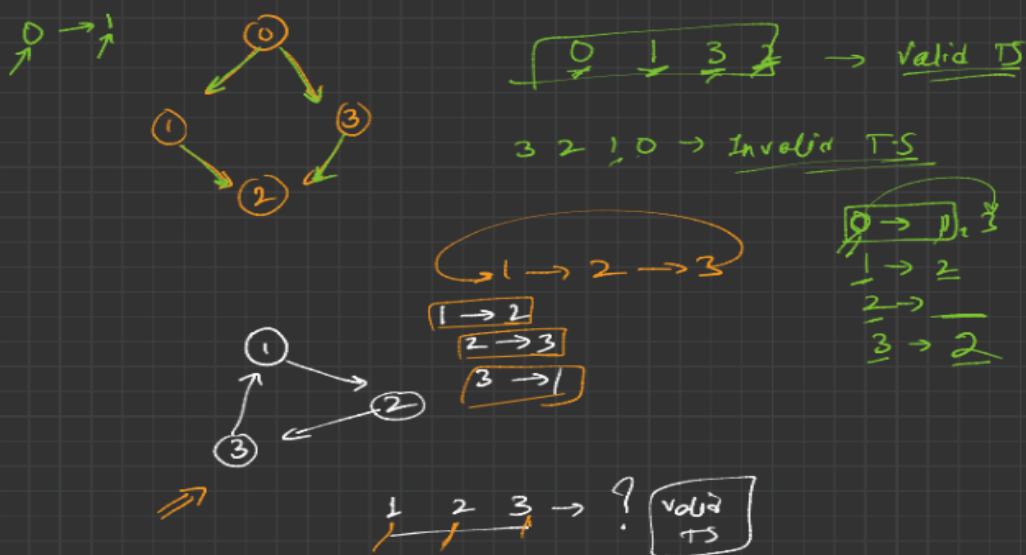


Topological Sort Using DFS:

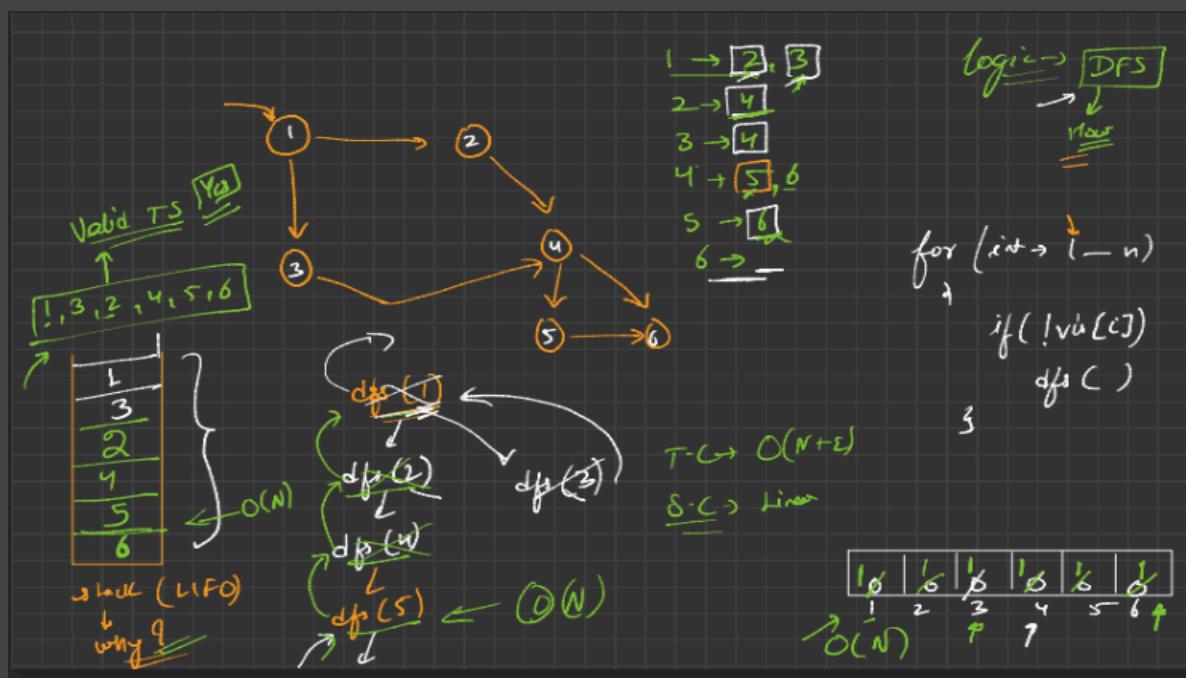
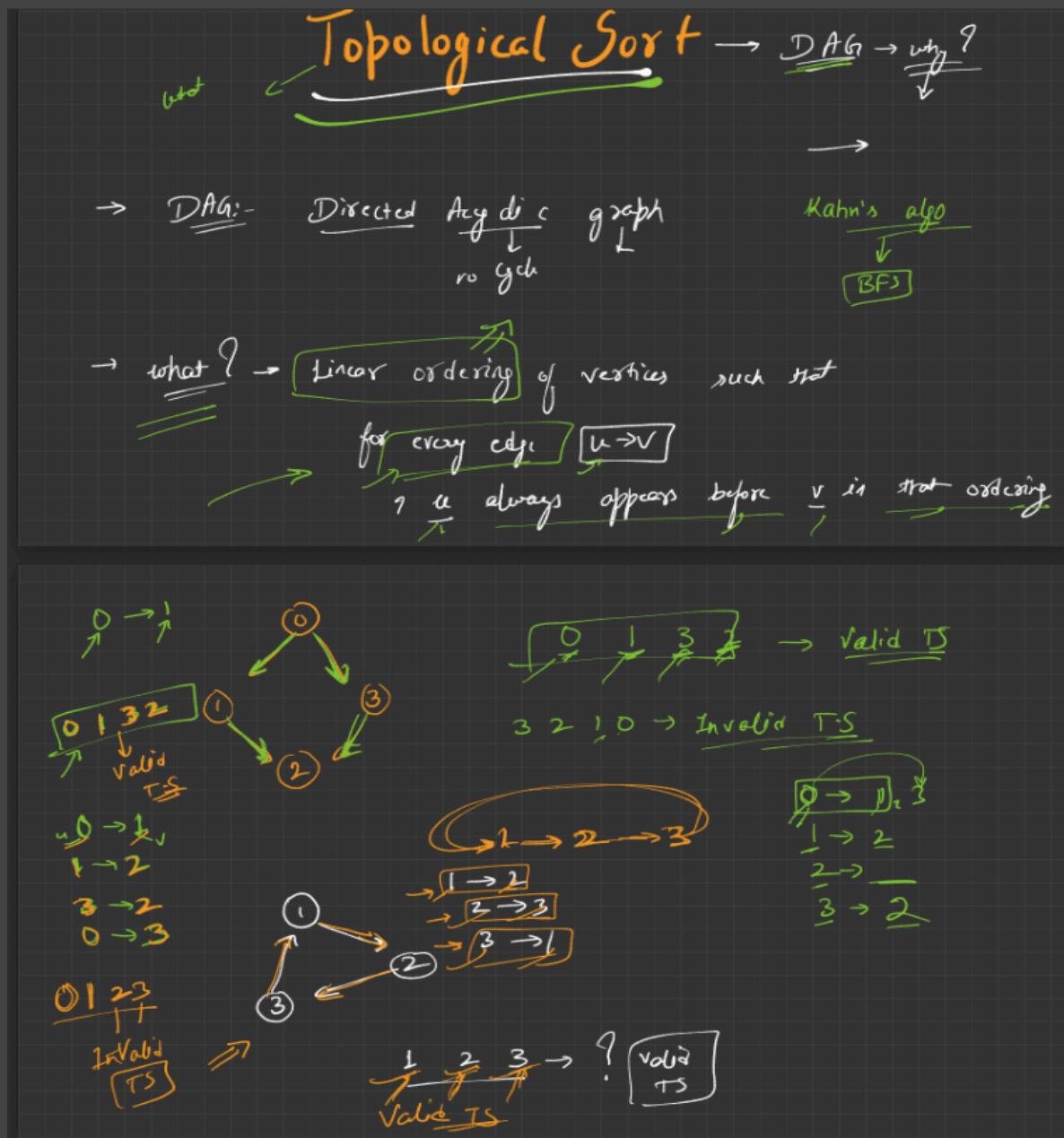
Topological Sort → DAG → why?

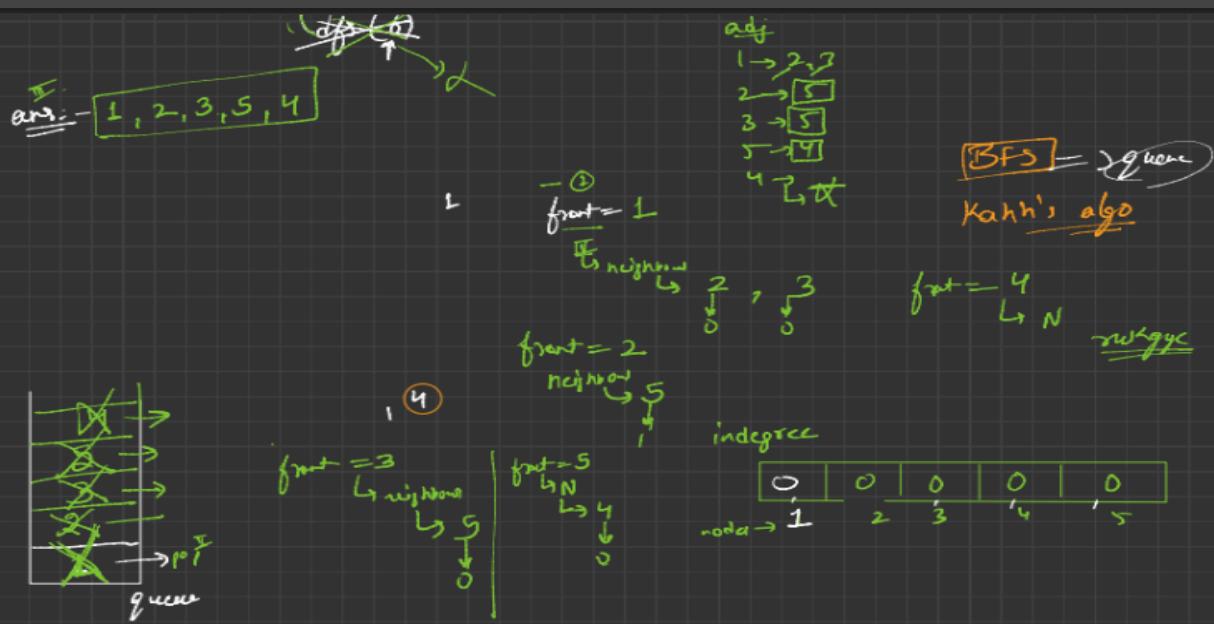
→ DAG: - Directed Acyclic graph
no cycle

→ what? → linear ordering of vertices such that
for every edge $[u \rightarrow v]$
 u always appears before v in that ordering



Topological Sort Using Kahn's Algorithm(BFS):



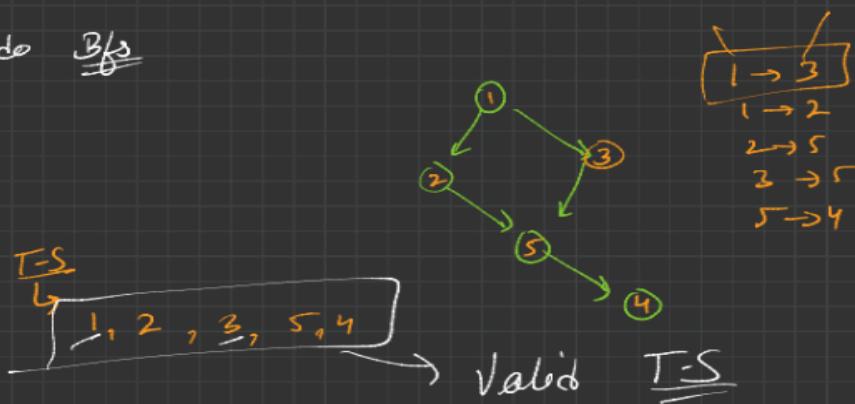


- (1) find indegree of all nodes
- (2) queue \rightarrow $\text{O} \rightarrow$ indegree nodes
 \hookrightarrow insert
- (3) do BFS

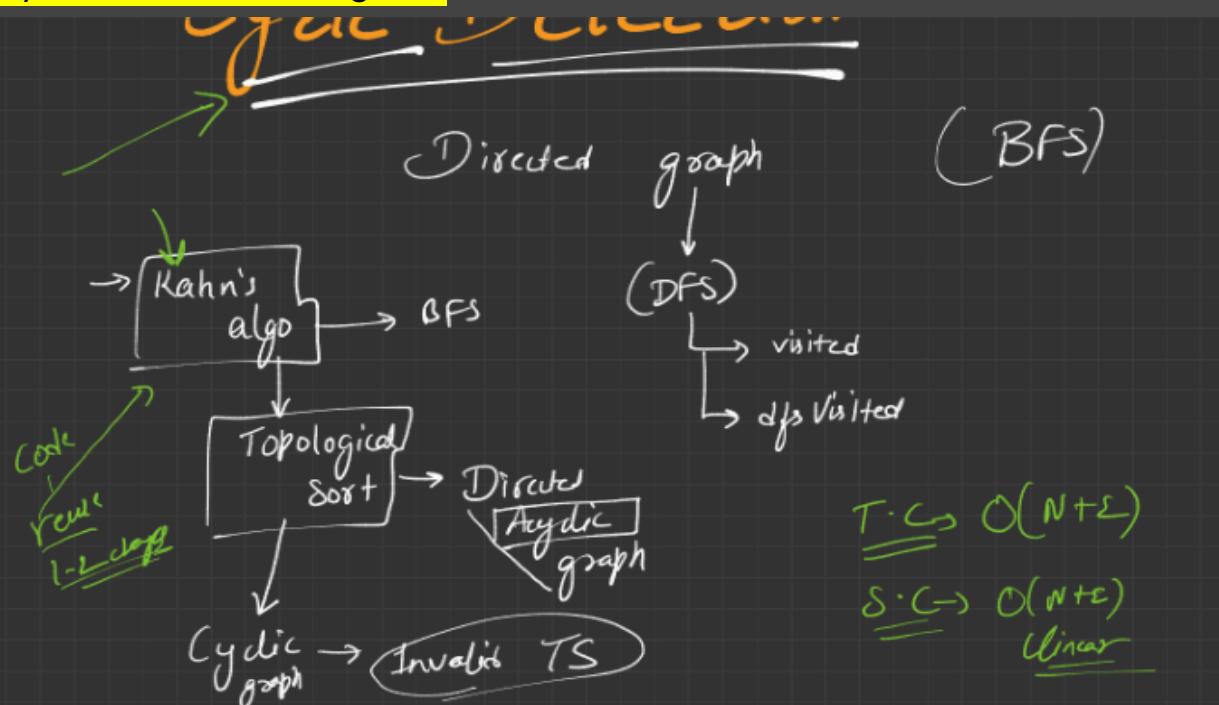
$$T \hookrightarrow O(N + \Sigma)$$

$$S \hookrightarrow \underline{O(N + \Sigma)}$$

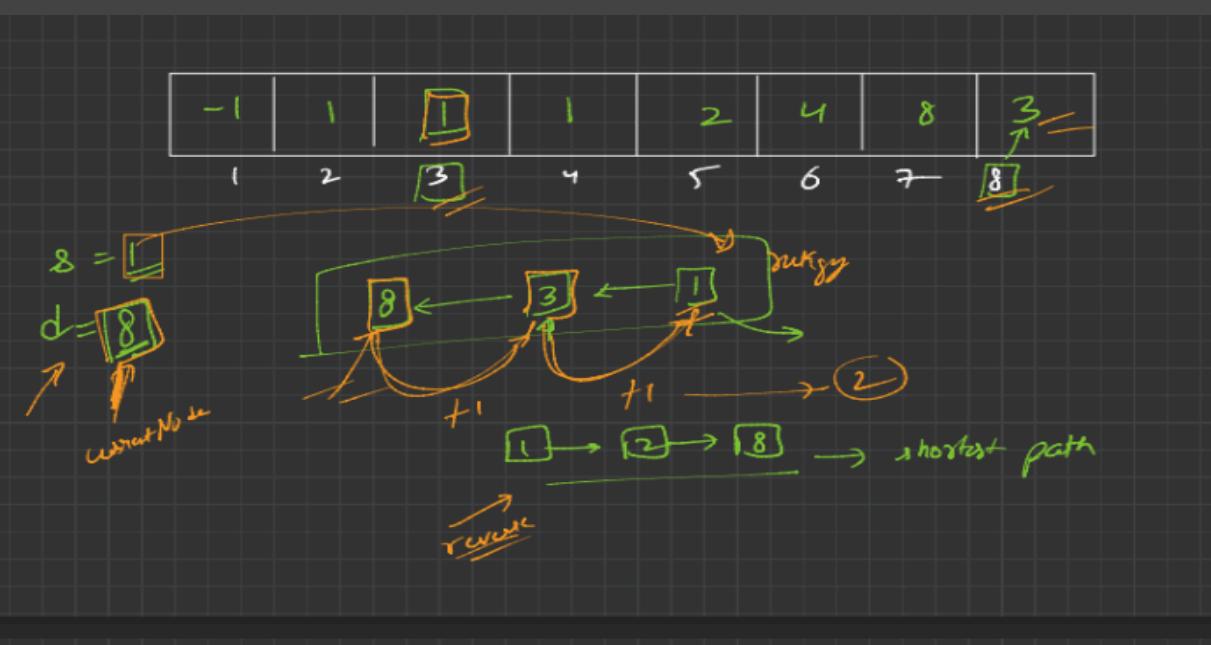
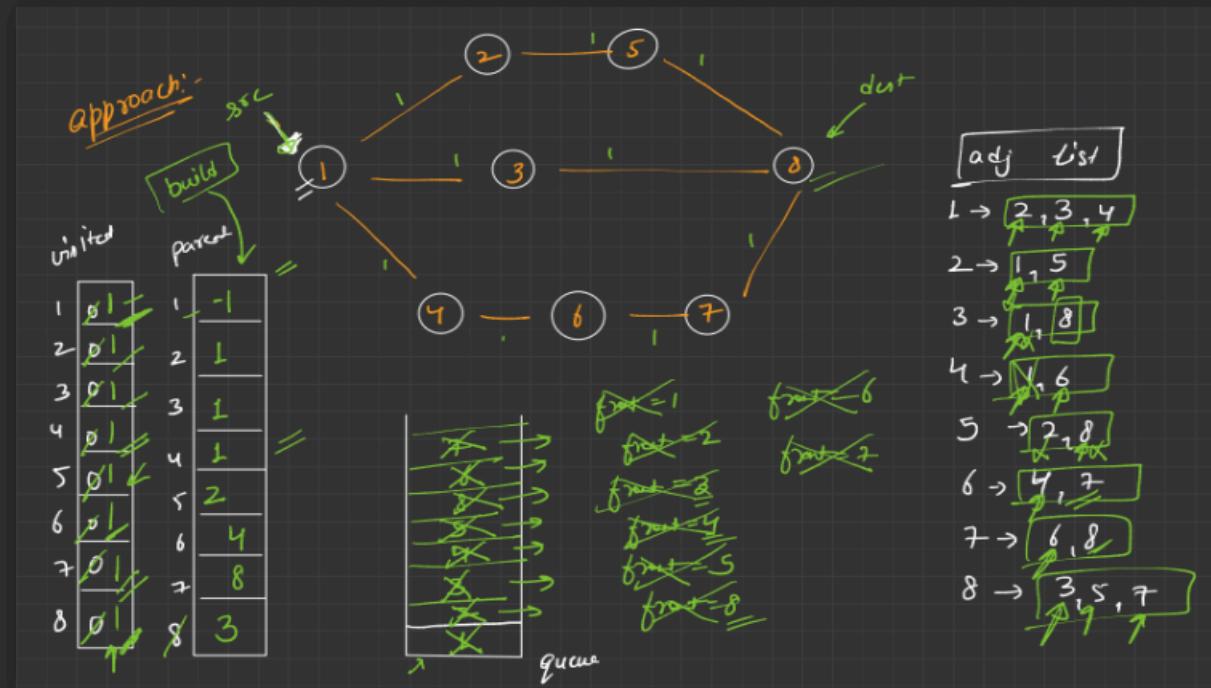
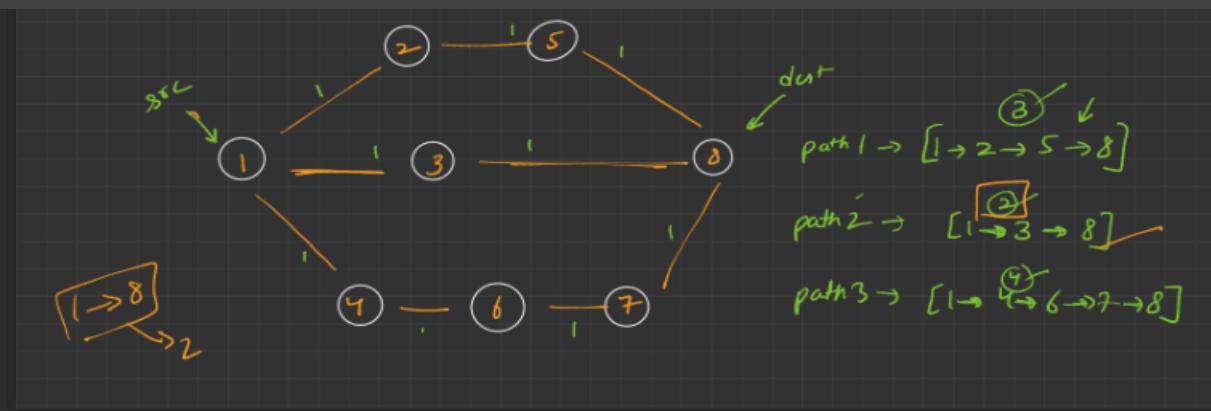
Linear



Cycle Detection Using BFS:

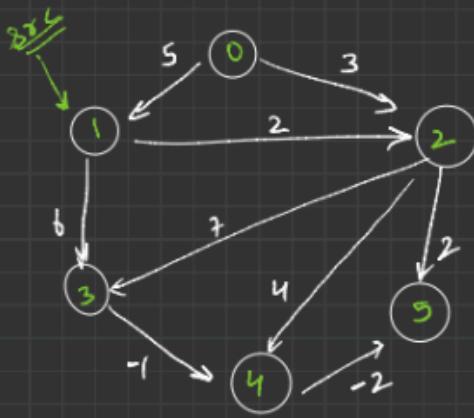


Shortest Path In Undirected Unweighted Graph Using Modified BFS:



$$\begin{cases} T.C \Rightarrow O(N+E) \\ S.C \Rightarrow O(N+E) \end{cases}$$

Shortest Path In Directed Acyclic Graph(DAG) Using DFS(Modified):



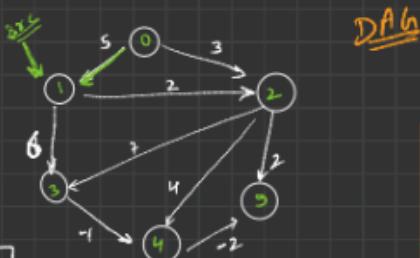
$1 \rightarrow 0 \rightarrow \text{INF}$
 $1 \rightarrow 1 \rightarrow 0$
 $1 \rightarrow 2 \rightarrow 2$
 $1 \rightarrow 3 \rightarrow 6$
 $1 \rightarrow 4 \rightarrow 5$
 $1 \rightarrow 5 \rightarrow 3$

$\text{SRC} \rightarrow 1$

shortest path $\rightarrow \{ \text{INF}, 0, 2, 6, 5, 3 \}$

Approach:

	0	1	2	3	4	5
0	0					
1	0	1				
2	0	1	2			
3	0	1	2	3		
4	0	1	2	3	4	
5	0	1	2	3	4	5



DAG

0
1
2
3
4
5

algo:-

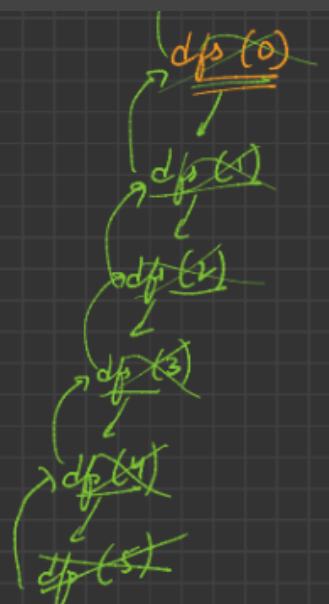
Topological sort \rightarrow why?

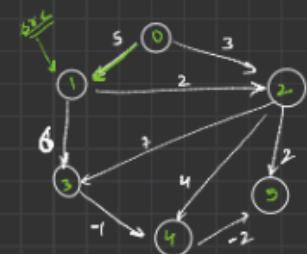
Linear Ordering

distance array update

```

for (int i = 0; i < n)
{
    if (!vis[i])
        dfs(i)
}
  
```





$$\text{dist}[1 \text{ to } C] = 0$$

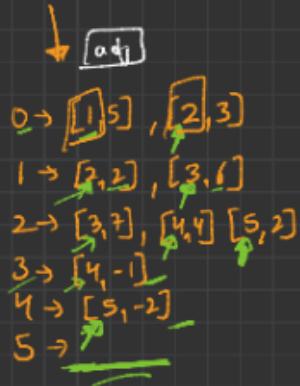
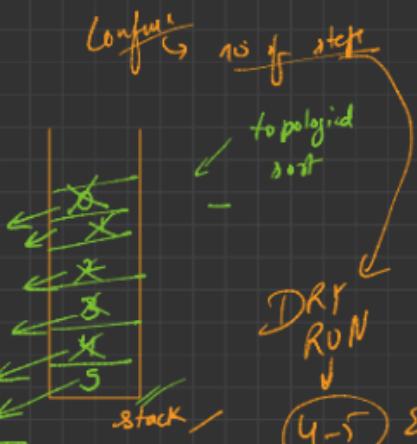
$\text{top} = 0 \rightarrow$

$\text{top} 1 \rightarrow [0]$

$\text{top} 2 \rightarrow [6]$

$T.C \rightarrow O(N+E)$

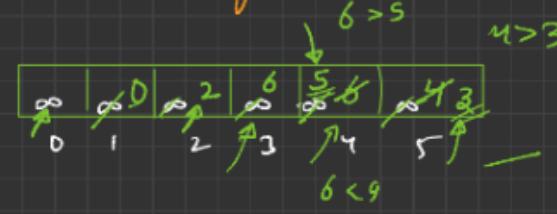
S.C



DRY RUN

(4 → 5) ex

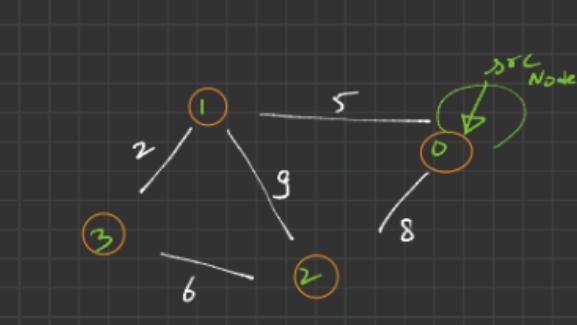
Dry Run



3 → 5

$\text{dist} \rightarrow \{ \infty, 0, 2, 6, 5, 3 \}$

Dijkstra's Algorithm / Shortest Path In Undirected Weighted(excluding negative weights) Graph:



$0 \rightarrow 0 \rightarrow 0$
 $0 \rightarrow 1 \rightarrow 5$
 $0 \rightarrow 2 \rightarrow 8$
 $0 \rightarrow 3 \rightarrow 7$

$\{ 0, 5, 8, 7 \}$

adj list

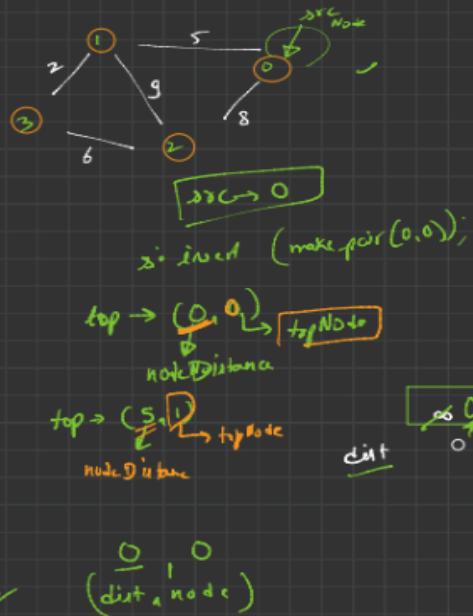
0 → [1, 5], [2, 8]

1 → [0, 5], [2, 9], [3, 2]

2 → [0, 8], [1, 9], [3, 6]

3 → [1, 2], [2, 6]

approach:

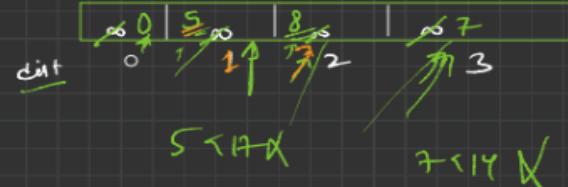


top → (0, 0) \rightarrow top Node

Node Distance

top → (5, 1) \rightarrow top Node

Node Distance

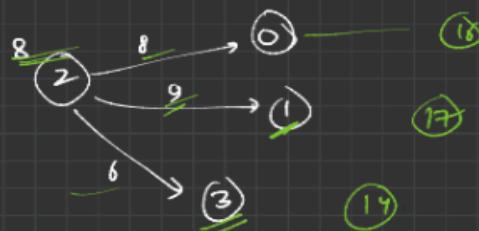
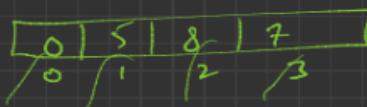


top → (7, 3) \rightarrow top Node

Node Distance

top → (8, 2) \rightarrow top Node

Node Distance

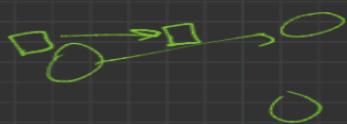


adj

- 0 → [1, 3], [2, 1] [3, 2]
- 1 → [0, 3], [2, 3] [3, 5] [4, 1]
- 2 → [0, 1], [1, 3]
- 3 → [0, 2] [1, 1] [4, 7]
- 4 → [1, 1] [3, 7]



$\text{dist} \rightarrow [1, 0, 4, 1, 2, 5]$



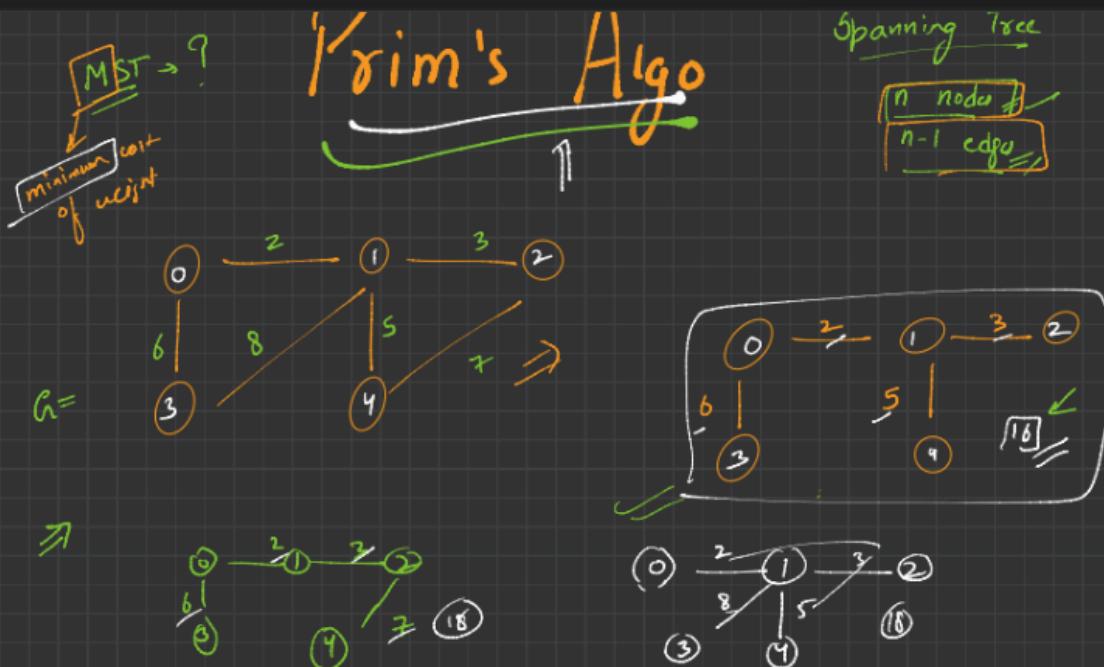
$T.C \rightarrow O(E \log V)$

\downarrow
edges
vector

$S.C \rightarrow O(N + \Sigma)$

\downarrow
linear

Prim's Algorithm / Minimum Spanning Tree:

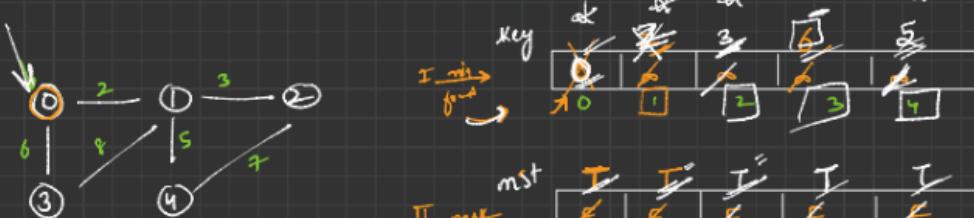


Prim's Algo:-

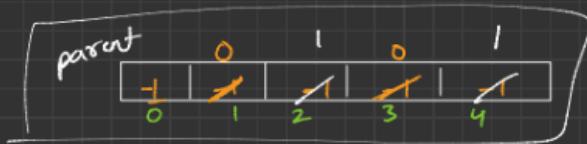


$O(n^2)$

$\cancel{O(n \log n)}$

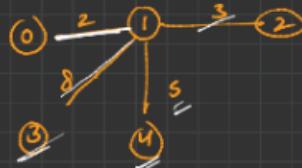
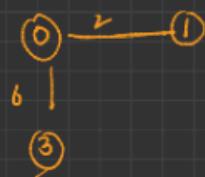


key[0] = 0
parent[0] = -1



$\begin{cases} \text{(i)} \rightarrow u \rightarrow 0 \\ \text{(ii)} \rightarrow \text{mst}[u] \rightarrow \text{true} \\ \text{(iii)} \rightarrow \text{adj} \end{cases}$

(i) $\rightarrow \text{mst}[i] = \text{false} \text{ & } \text{key}[i] < \text{mini}$
 $u \rightarrow 1$
(ii) $\text{mst}[u] = \text{true}$
(iii) adj

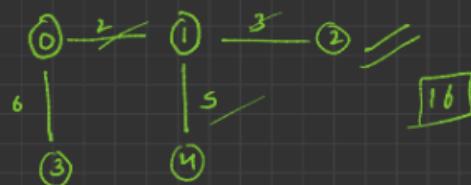
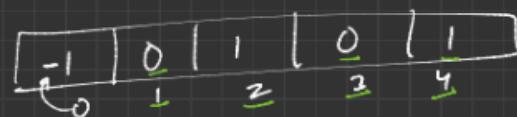
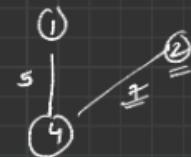
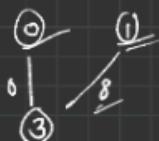


$\textcircled{1} \rightarrow u \rightarrow 2$
 $\textcircled{1} \rightarrow \text{mt}[2] = \text{True}$
 $\textcircled{1} \rightarrow \text{ab}$

$\textcircled{2} \quad u \rightarrow 3$
 $\text{mt}[3] = \text{true}$

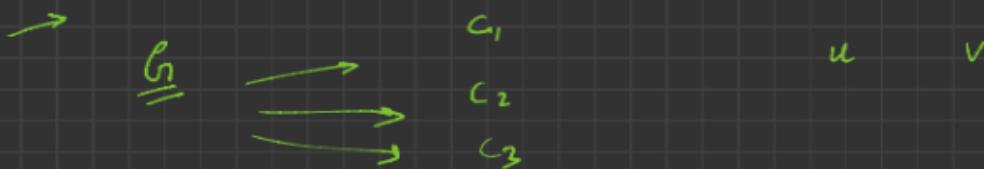
STOP

$\textcircled{1} \rightarrow \text{min}$
 $u \rightarrow 4$
 $\text{mt}[4] = \text{true}$



Disjoint Set & Kruskal's Algorithm:

Disjoint Sct

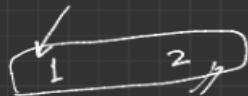


2 inp
 \downarrow $\text{findParent}()$ or $\text{findSet}()$
 \downarrow $\text{Union}()$ or $\text{UnionSet}()$

5 disconnected comp



Union (1, 2)



Union (3, 5)



find parent (1) $\rightarrow 1$

(2) $\rightarrow 2$

(3) $\rightarrow 3$

(4) $\rightarrow 4$

(5) $\rightarrow 5$

Union (4, 5)

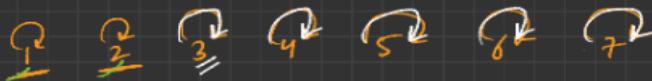


Union (1, 3)

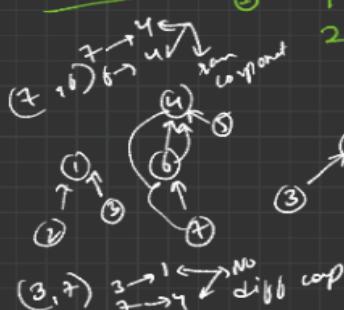


\hookrightarrow Union by Rank & Path Compression

③



Union (1, 2)



Rank

0
0

find Parent (1) - 1

2 -> 2

3 -> 3

4 -> 4

5 -> 5

6 -> 6

7 -> 7

same rank

① parent [2] = 1
② rank [1] ++

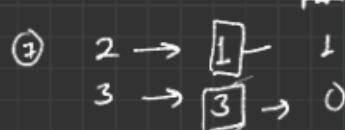
③ parent [5] = 4
rank [4] ++

rank	1	2	3	4	5	6	7
X	1	0	0	0	2	0	0

rank

0
1
2
3
4
5
6
7

Union (2, 3)



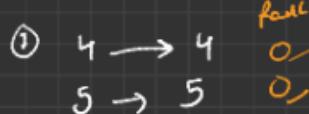
rank

1
1

rank [3] < rank [1]
parent [3] = 1

?

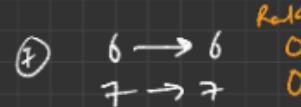
Union (4, 5)



rank

0
0

Union (6, 7)



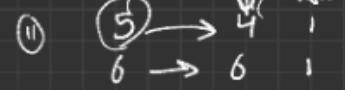
rank

0
0

parent [7] > 6

rank [6] ++

Union (5, 6)



rank

1
1

parent [6] = 4

rank [4] ++

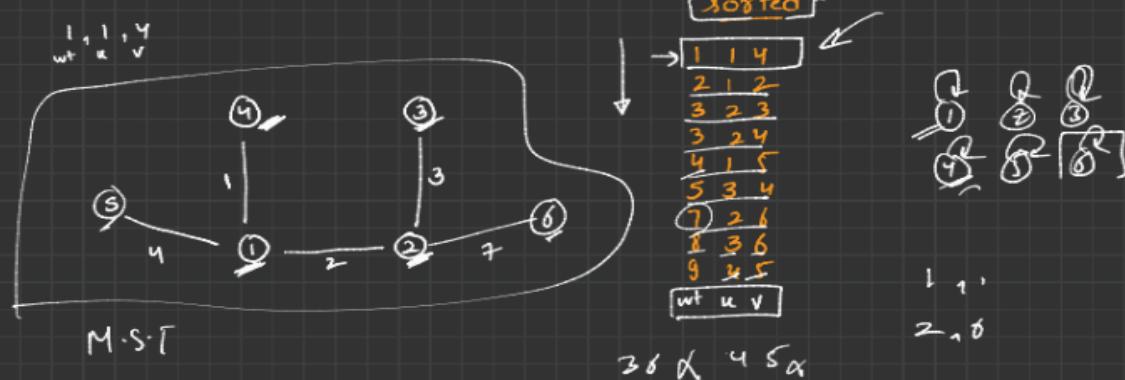
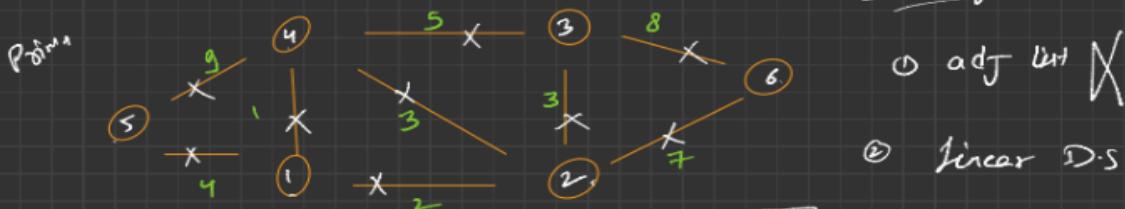
Union $(3, 7)$

①	$3 \rightarrow 1$	rank 1
	$7 \rightarrow 4$	2

$\frac{\text{rank}[1] < \text{rank}[4]}{\text{parent}[1] = 4}$



Kruskall's algo:-



1 2 3
 \times

2 4 \times

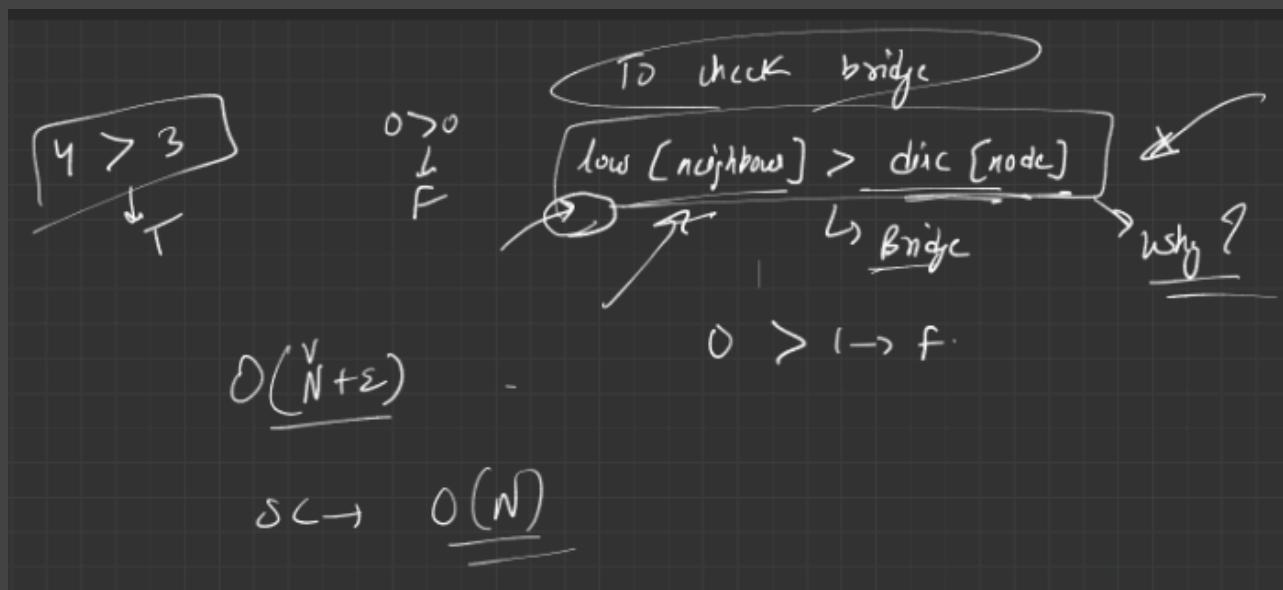
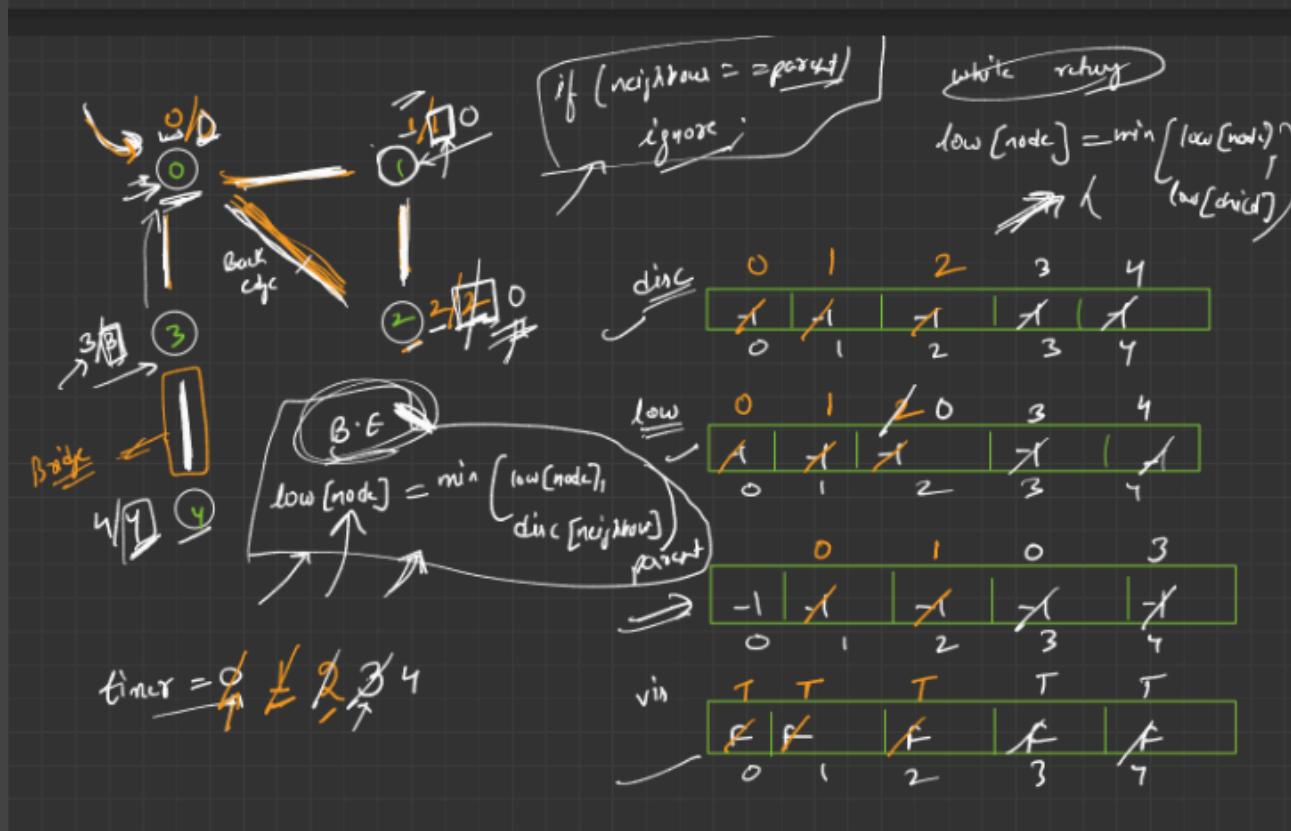
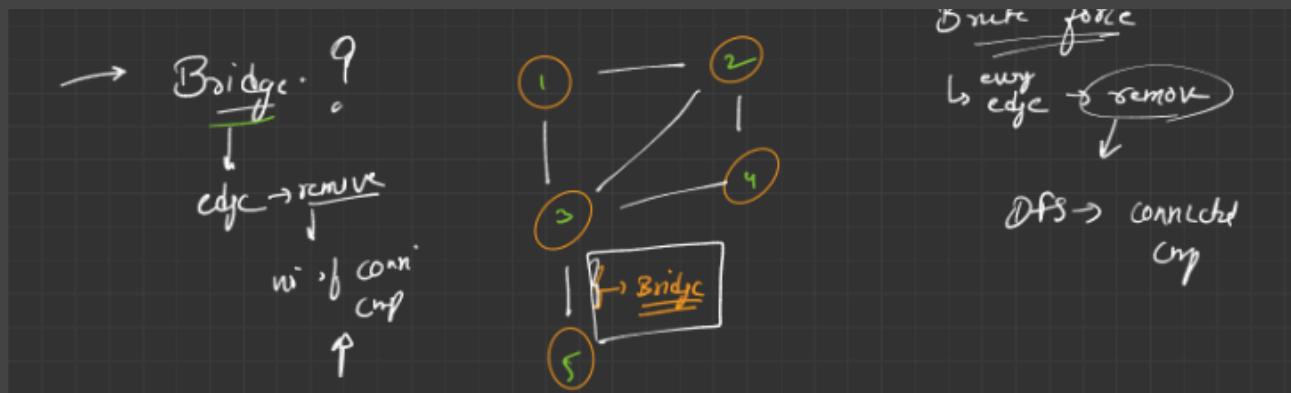
$\partial(u) = \partial(v)$
first row \rightarrow 0 \Rightarrow
Union set

T.C \rightarrow $O(m \log m)$

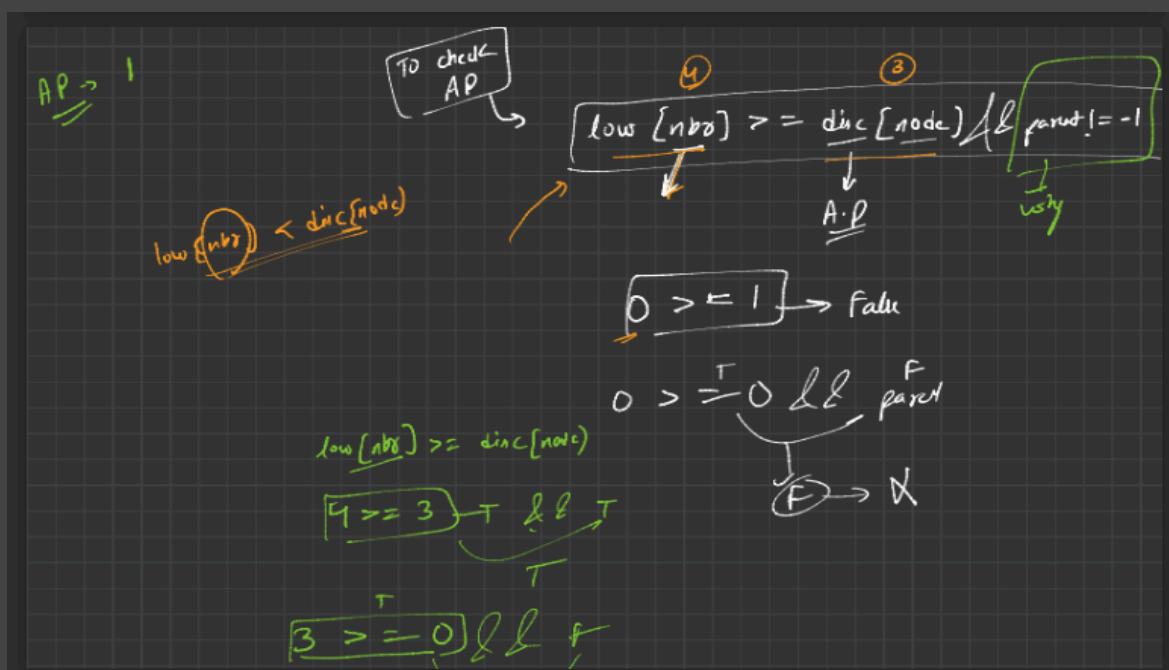
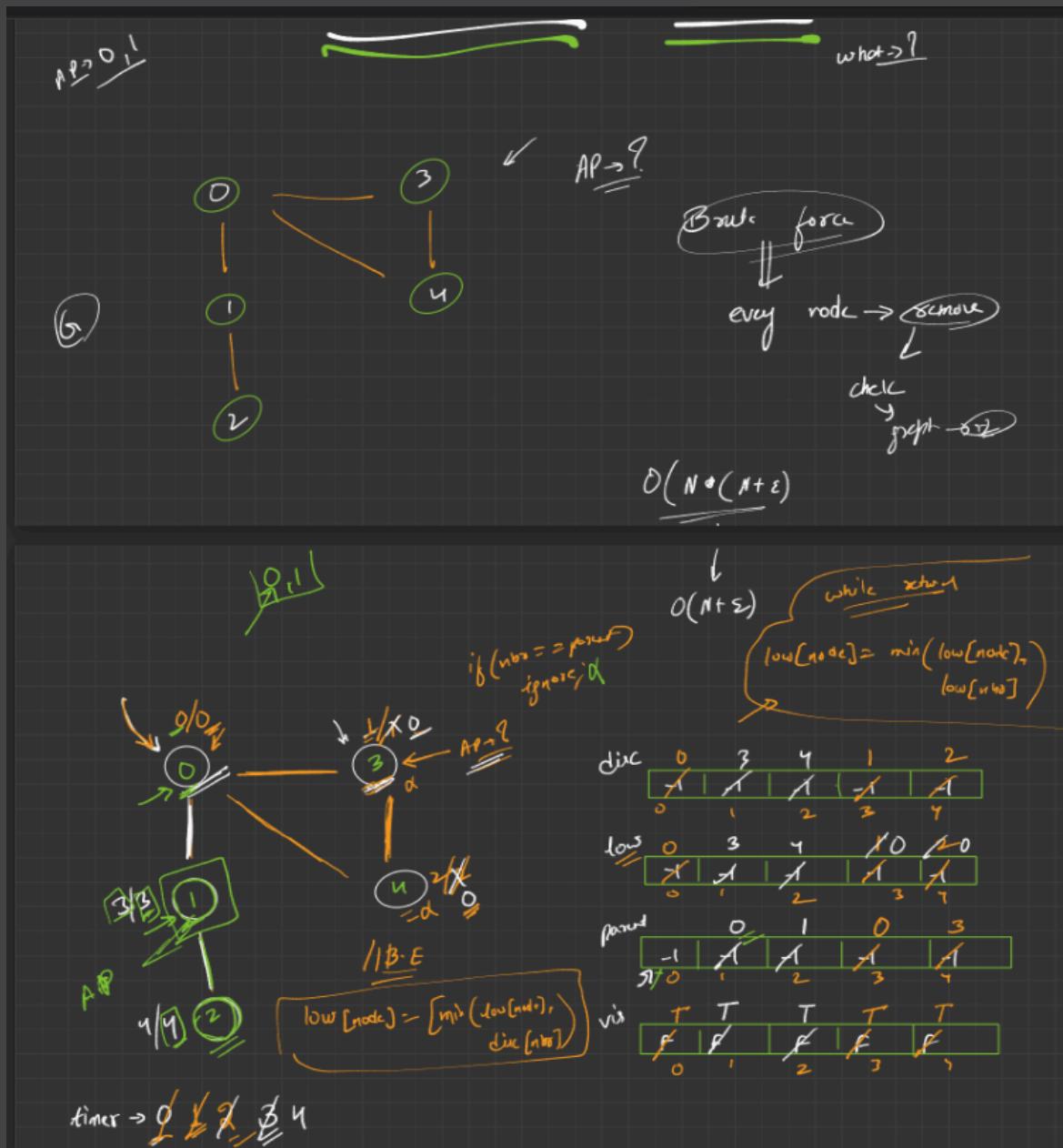
S.C \rightarrow $O(n)$

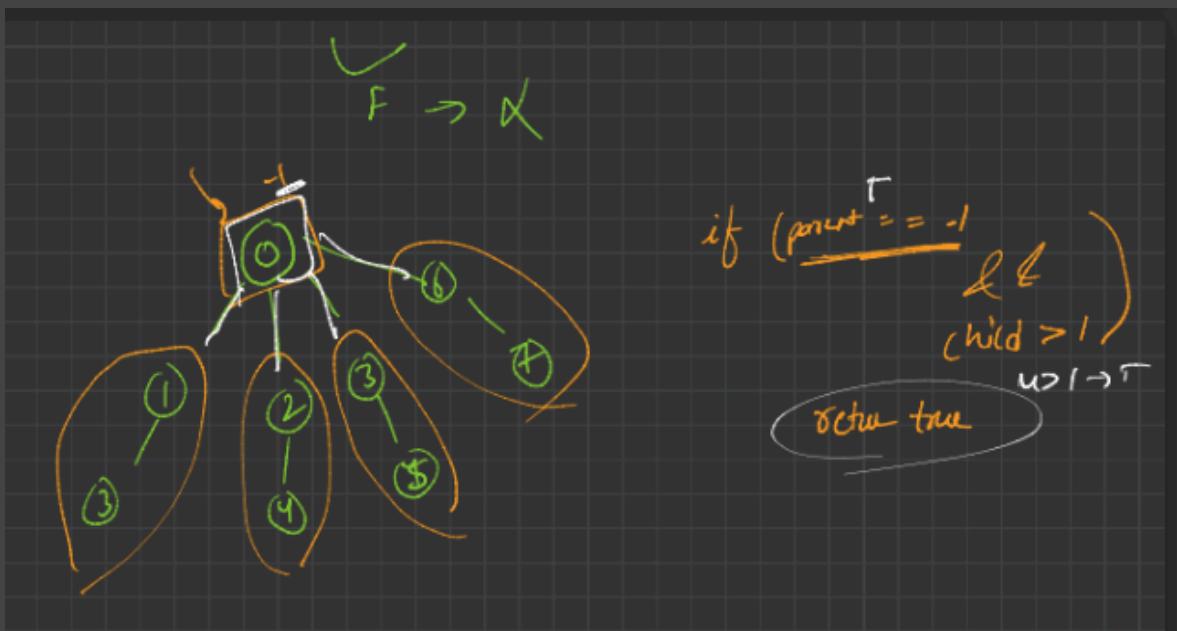
① 1 \rightarrow 1 \leftrightarrow diff \rightarrow merge / Union
4 \rightarrow 4 \leftrightarrow same \rightarrow \times ignore

Find Bridges In A Graph:

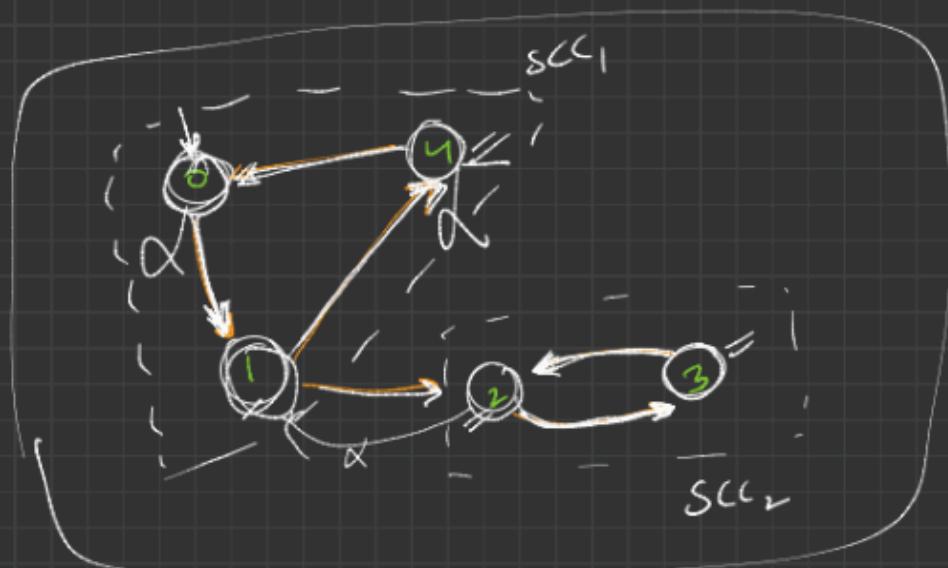
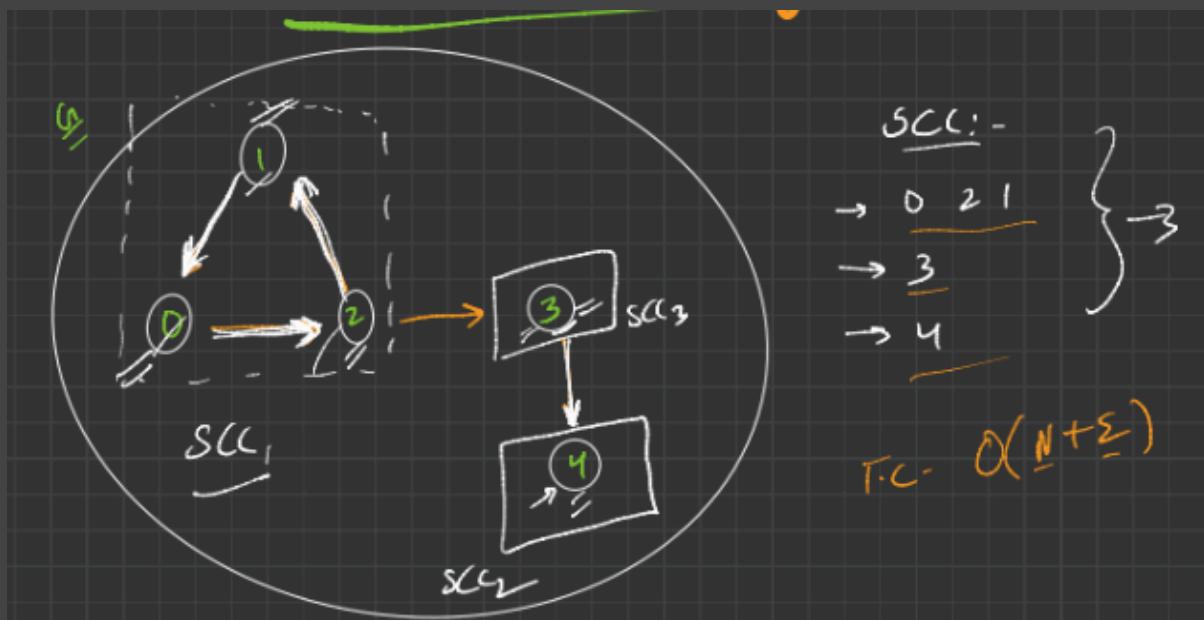


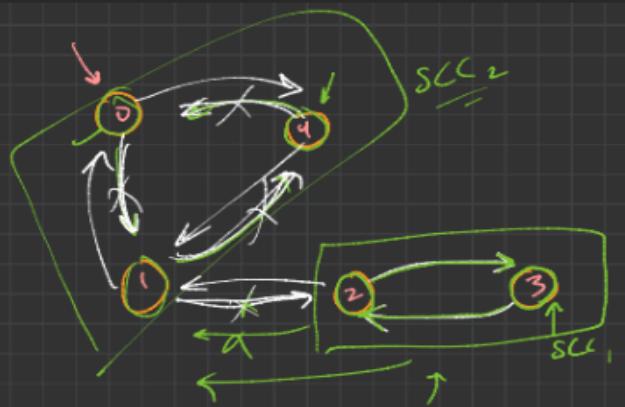
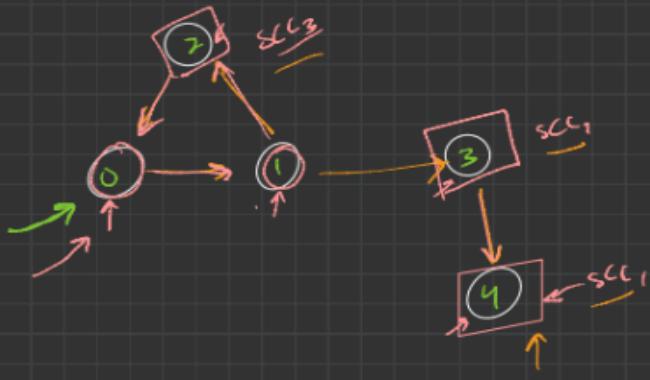
Find Articulation Points In A Graph:





Find the Strongly Connected Components In A Graph / Kosaraju's Algorithm:



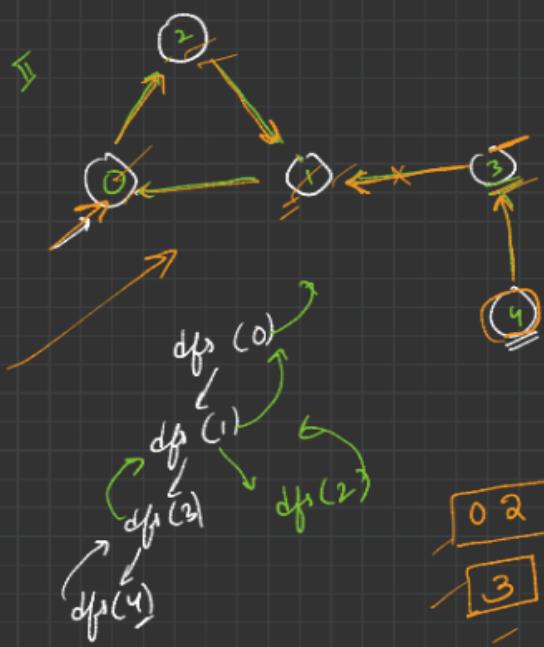


W.A
 → sort all nodes
 basis on their
 finishing time
 ↓
 [Topological Sort]

→ Transpose graph

→ dfs → count/print
 scc

Page 4 / 20 - ⌂ +



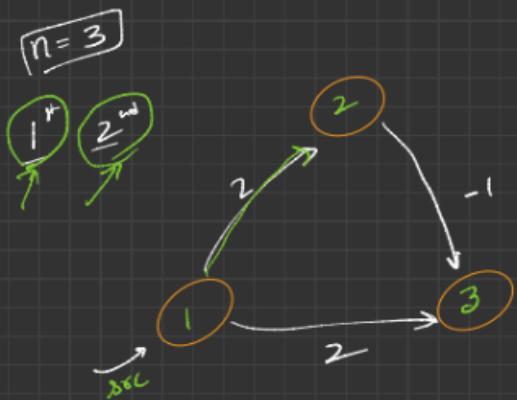
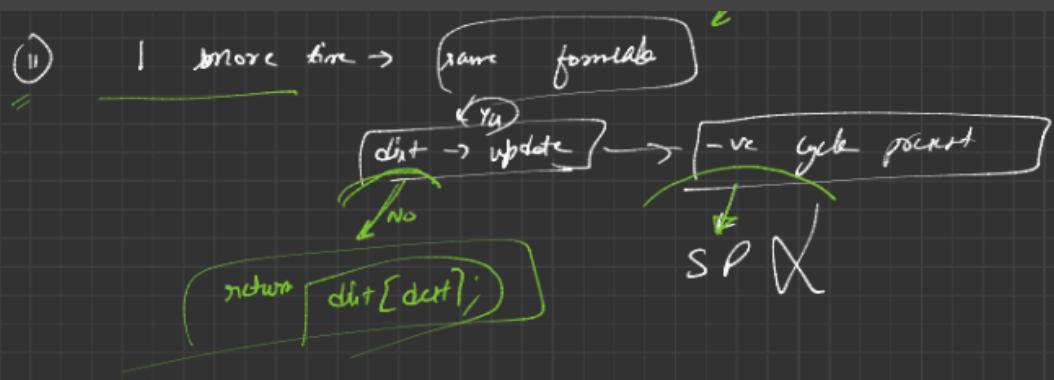
III

0 2 1
 3
 4

→ scc

Shortest Path In Undirected/Directed Weighted(including negative weights)

Graph: / Bellman Ford's Algorithm:



$$T = C \approx (n-1) \times \Sigma_m$$

$$O(n \times m)$$

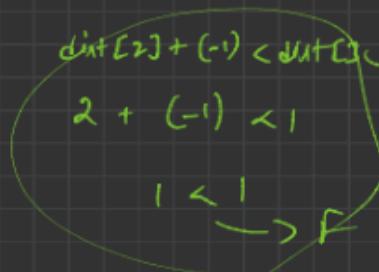
$\text{cdpa})$
 $\rightarrow 2 \quad w^1$
 $2 \rightarrow 3 \quad (-1)$
 $1 \rightarrow 3 \quad (2)$

0	2	1
1	/ 2	3 ↑

0	2	1	1
/	/ 2	/ 3	↑

check cycle -

\neg ve cycle
 \downarrow
 no + point



$\rightarrow 1 \rightarrow 2 \quad (2)$

$\rightarrow 2 \rightarrow 3 \quad (-1)$

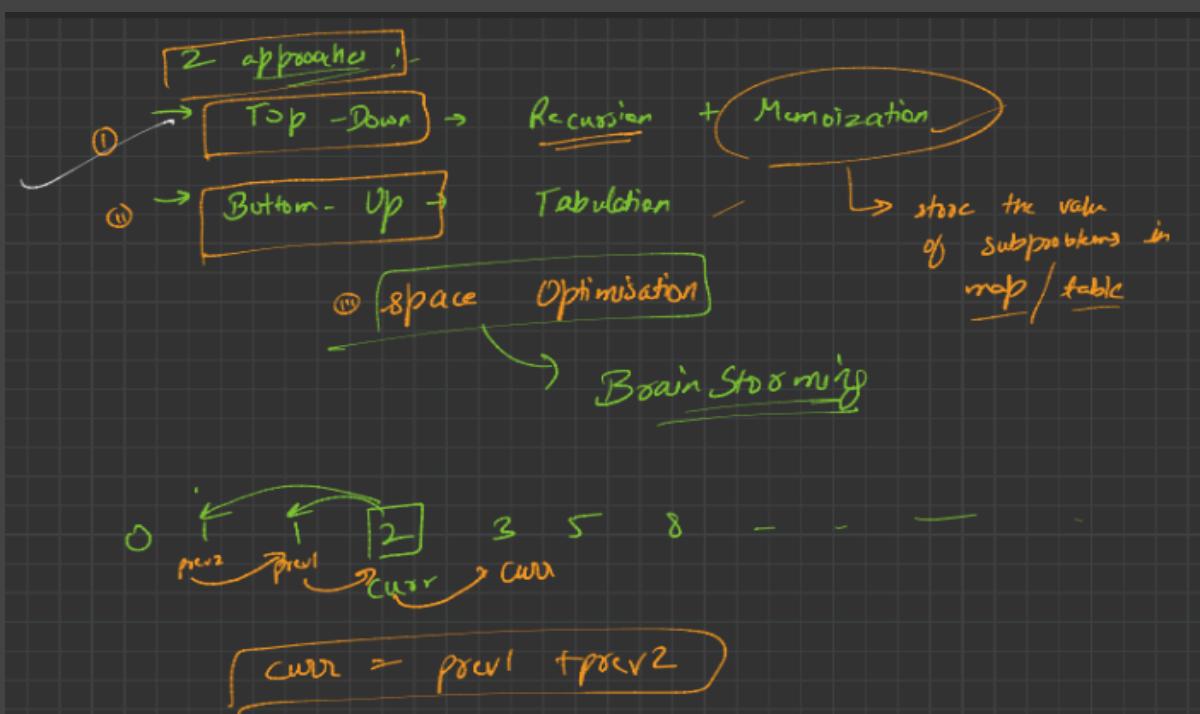
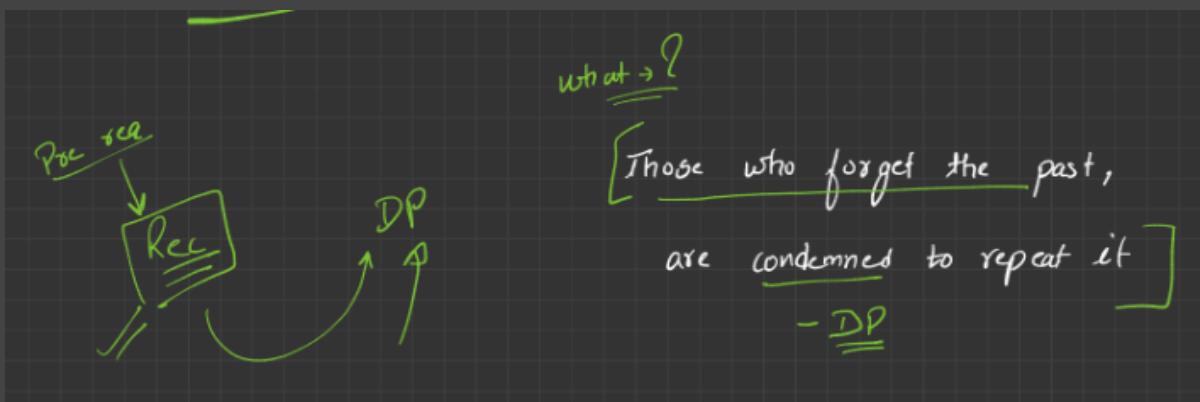
$1 \rightarrow 3 \uparrow \quad (2)$

$\text{dist}[1] + 2 < \text{dist}[3]$

$0 + 2 < 1$

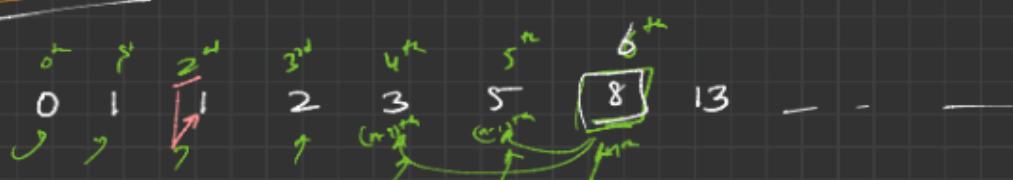
$2 < 1$
 \downarrow
 F

Dynamic Programming



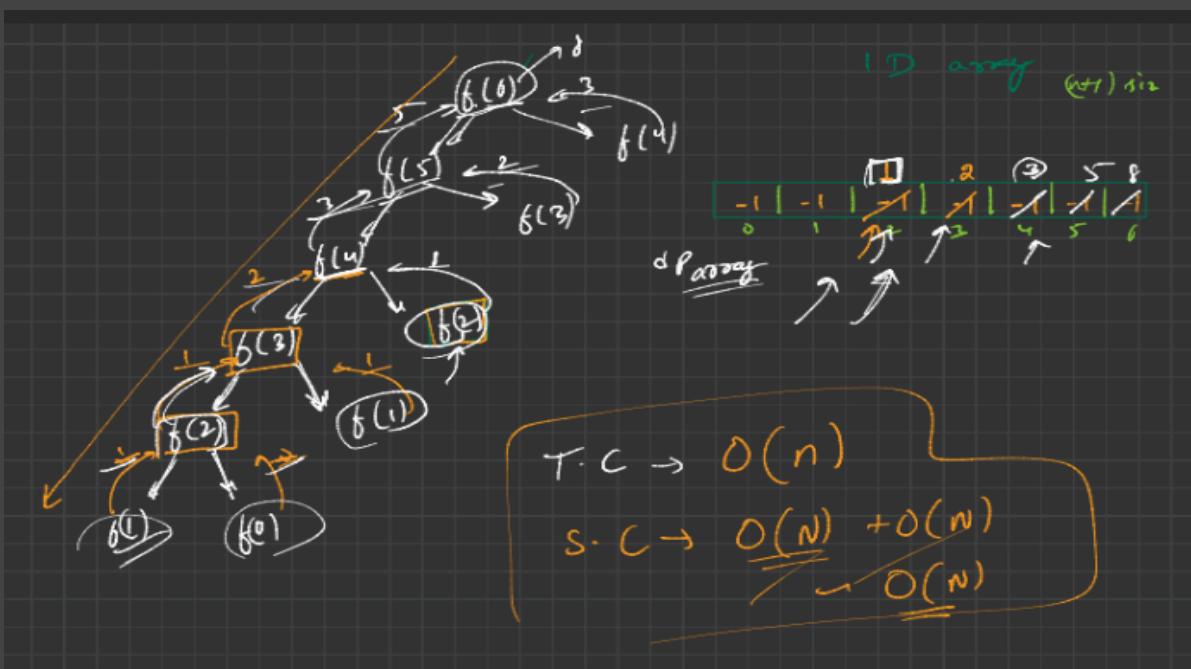
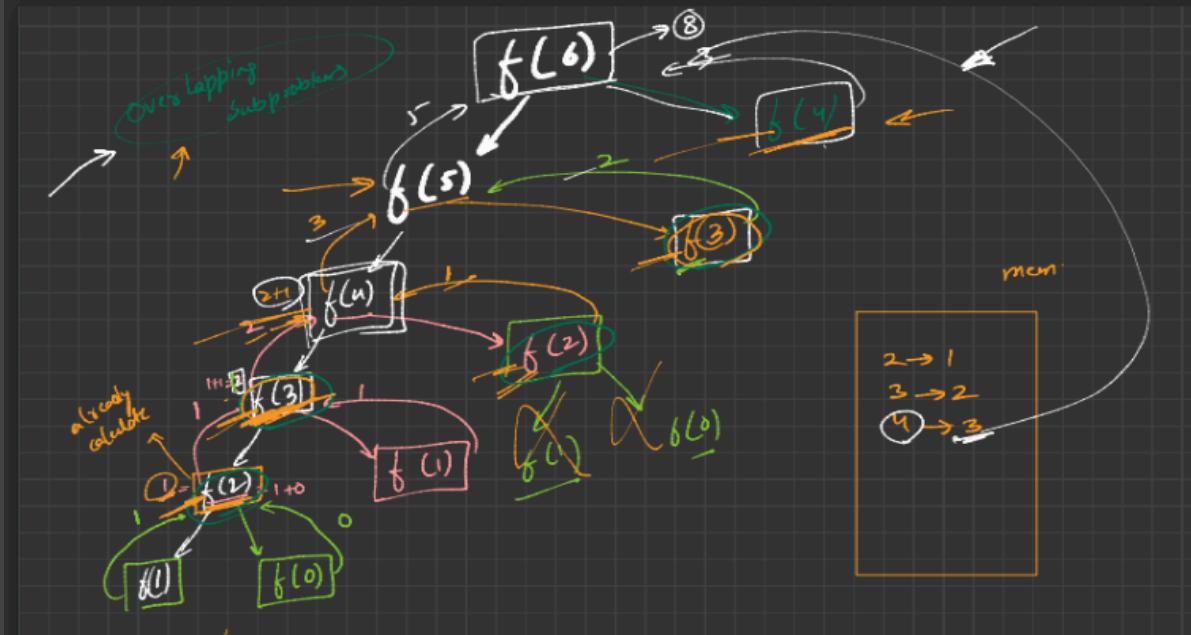
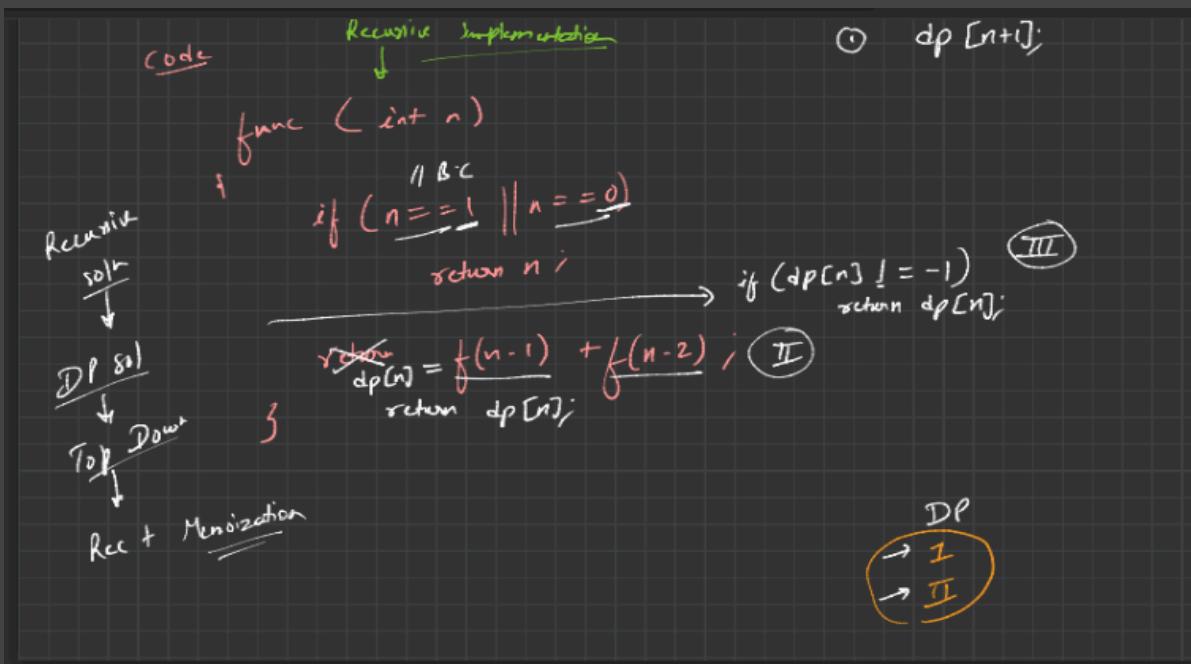
Fibonacci By Top-Down Approach:

Fibonacci Series:-

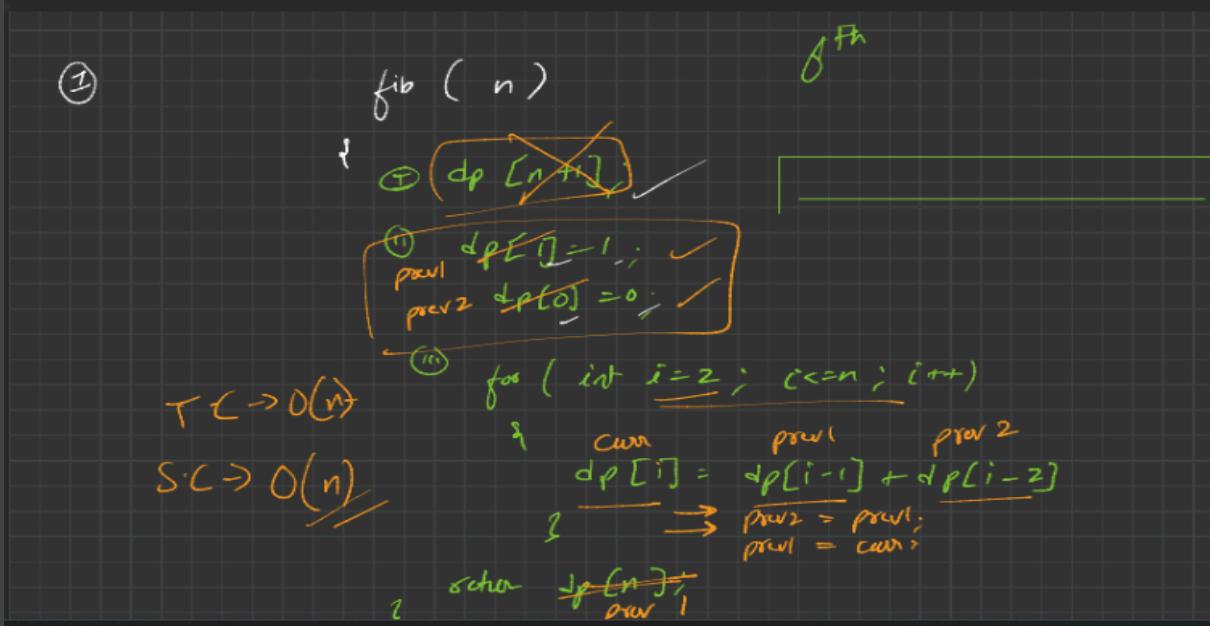
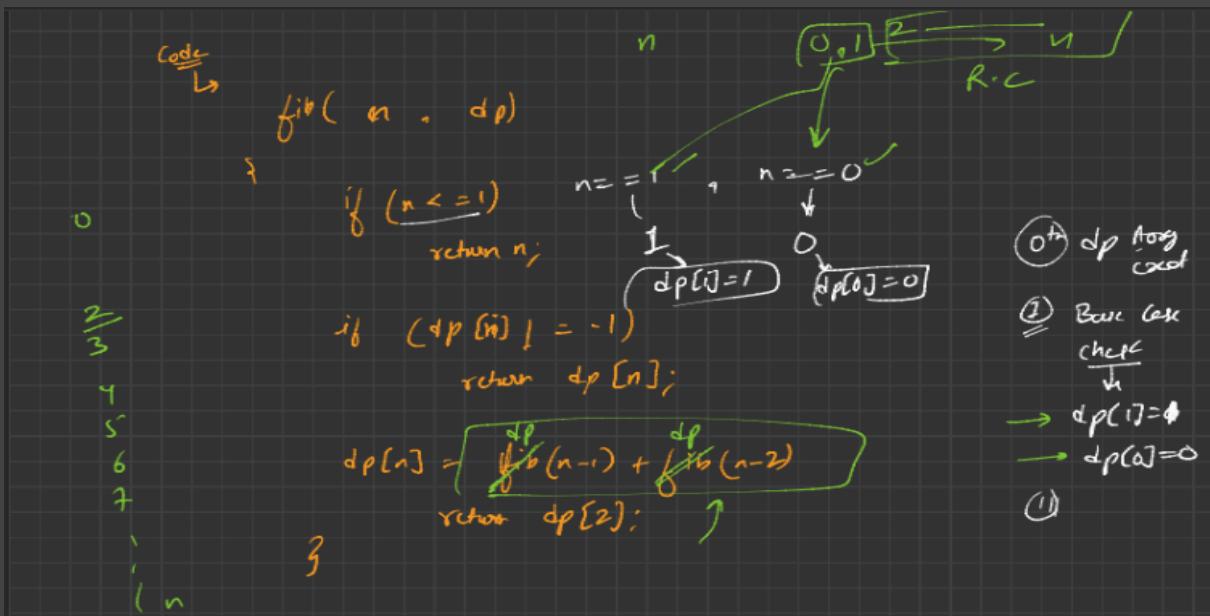


$$f(n) = f(n-1) + f(n-2)$$

n^{th} fibonacci number



Fibonacci By Bottom-Up Approach:

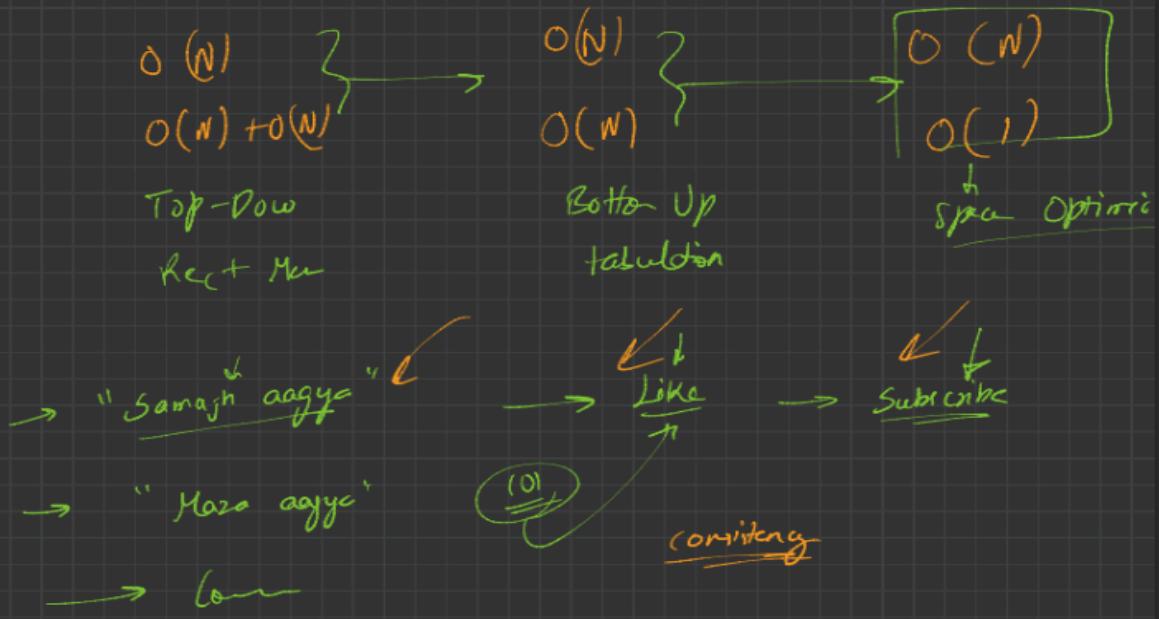


Fibonacci By Space Optimization Approach:

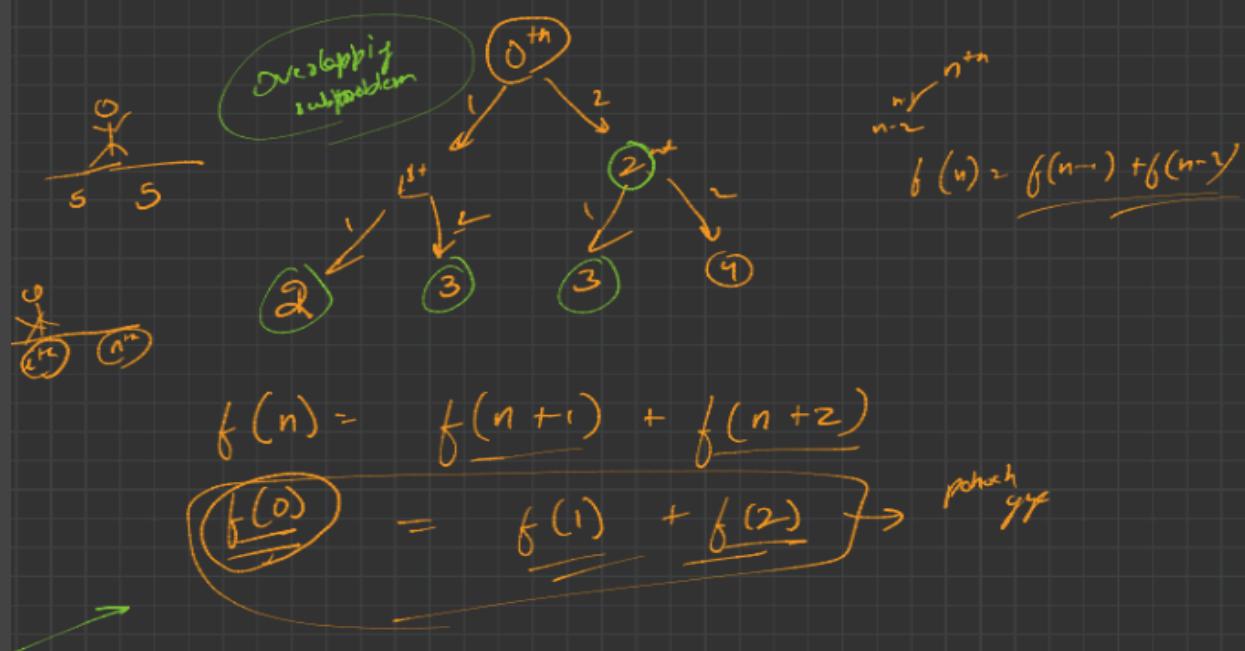
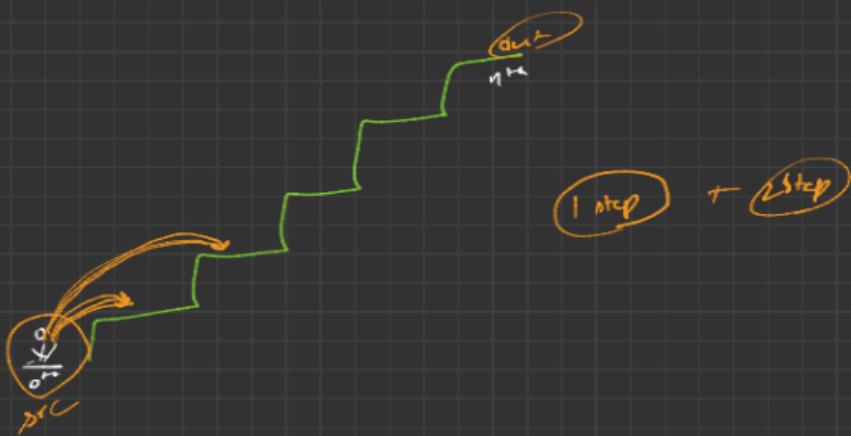


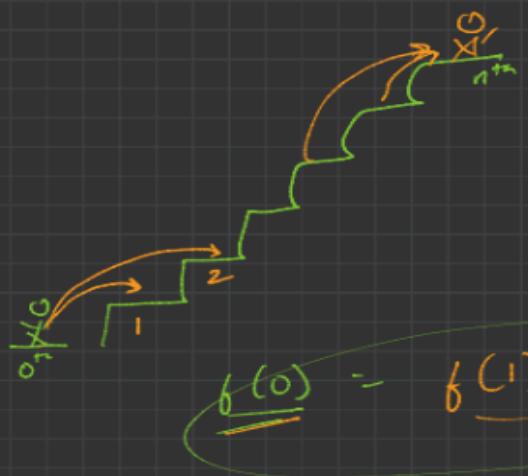
$T \subset O(N)$

$S.C \rightarrow O(1)$



Minimum Cost Of Climbing Stairs By Recursion / Top-Down Approach /
 Bottom-Up Approach / Space Optimization Approach:





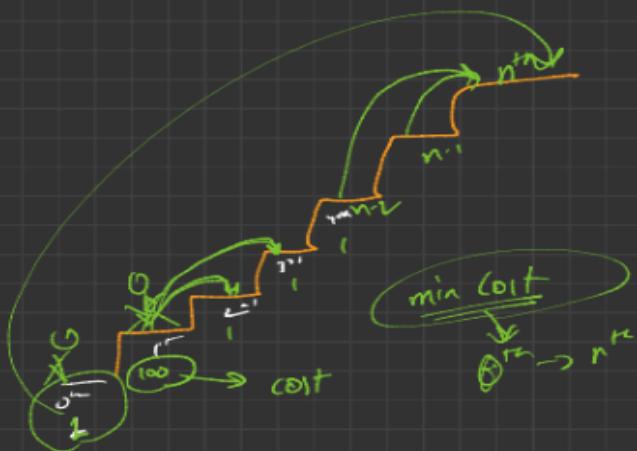
$$f(n) = f(n-1) + f(n-2)$$

Min Cost Climbing Stair

① we can start from 0th or 1st stair

② we have to pay cost, only then we can move 1 or 2 steps ahead

③ Action min Cost to reach top floor



Recursion

$$f(n) = \min(f(n-1), f(n-2))$$

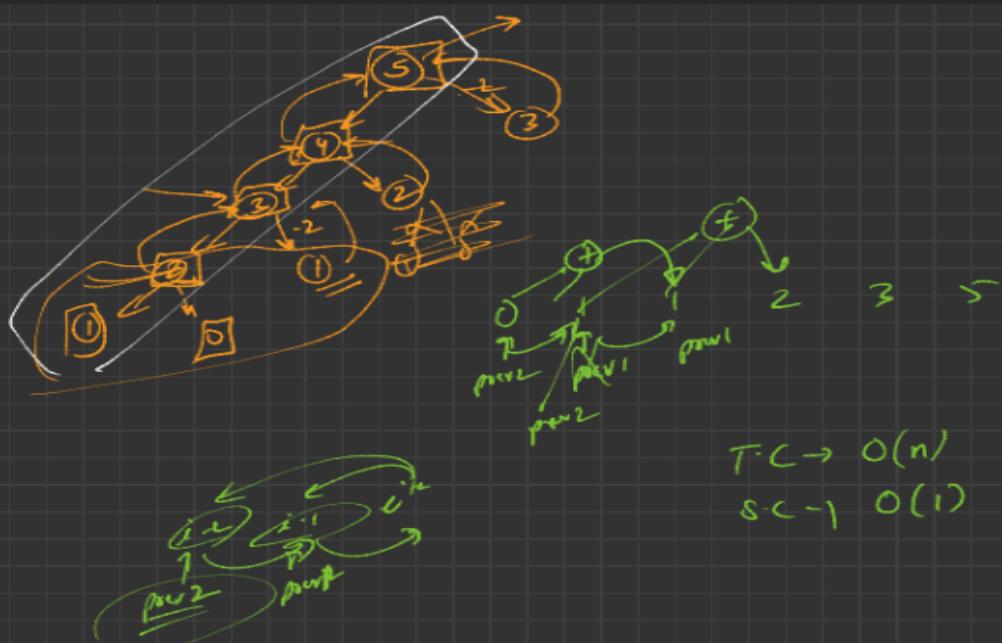
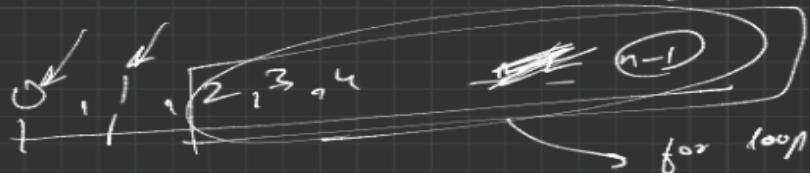


$$f(n) = \min(f(n-2), f(n-3)) + \text{cost}[i]$$

$$f(k) \leftarrow m(f(k-1), f(k-2)) + \text{cost}[k]$$

(1) Recursion + Memoization $\rightarrow O(n)$
 $O(n) + O(n)$

(3) Tabulation \rightarrow Bottom - Up \rightarrow $T.C \rightarrow O(n)$
 $S.C \rightarrow O(n)$ $\rightarrow O(1)$



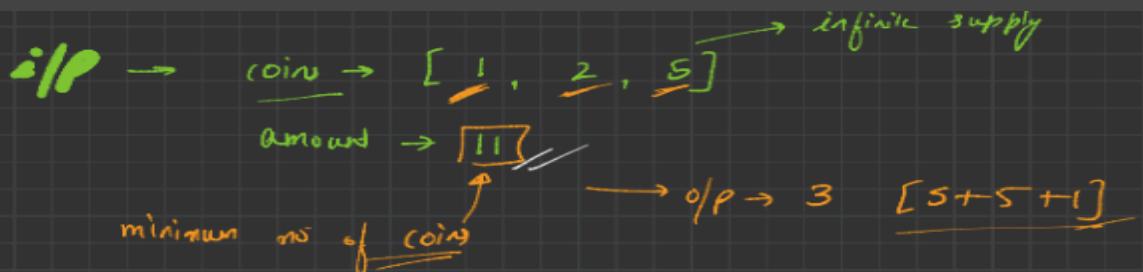
→ Recursion + Memoization $\rightarrow T.C \rightarrow O(n)$
 $S.C \rightarrow O(n) + O(n)$

→ Tabulation $\rightarrow T.C \rightarrow O(n)$
 $S.C \rightarrow O(n)$

→ Space Optimisation $\rightarrow T.C \rightarrow O(n)$
 $S.C \rightarrow O(1)$

Minimum Number Of Coins By Recursion / Top-Down Approach / Bottom-Up

Approach:



coin $[2]$

target $\rightarrow 3 \rightarrow$

ans $\rightarrow 1$

i/p

$T \rightarrow 0 \rightarrow o/p \rightarrow 0 \text{ coin}$

$[1, 2, 3] \times \rightarrow 7$

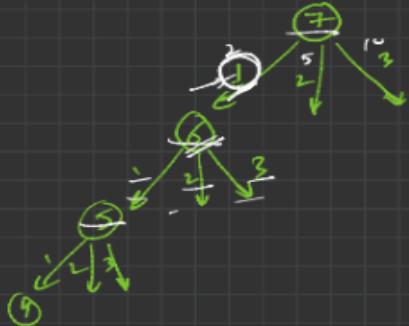
$1+1+1+1+1+1+1 \rightarrow 7$

$2+2+2+1 \rightarrow 7$

$(3+3+1) \rightarrow 7$

\rightarrow Rec + Mem \rightarrow tabulation \rightarrow S.O.

① Recursion



$[1, 2, 3]$

7
 $[2, 5, 10]$

// B.C

if ($\text{target} == 0$)
return 0;

if ($\text{target} < 0$)

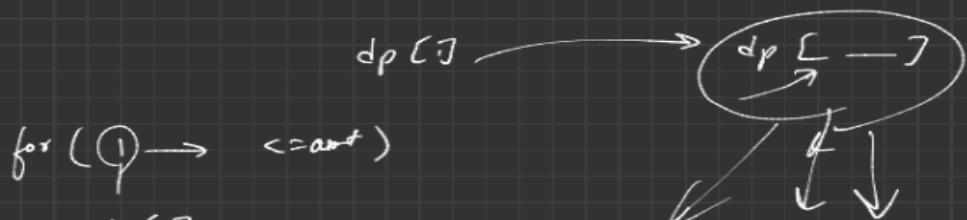
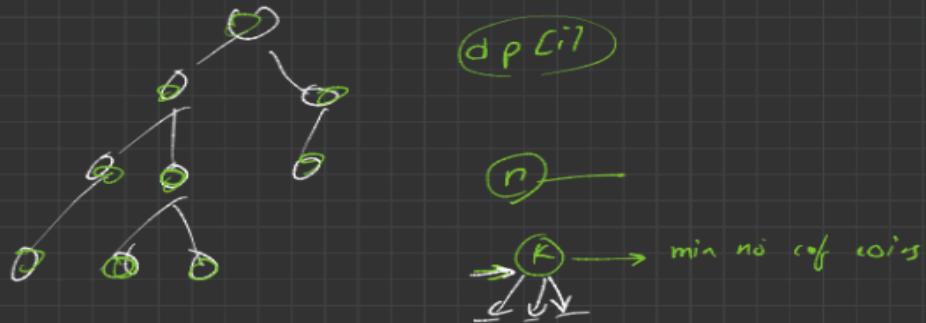
INT_MAX

int $\text{min} = \text{INT_MAX}$;

for (no. of coins)
int $\text{ans} = f(\text{amt} - \text{coin[i]})$

memoization

$\text{if } (\text{ans}! = \text{INFINITY})$
 $\min_i = \min(\min_i, \lceil \frac{\text{ans}}{a_i} \rceil)$
 $\text{order } a_i$



for ($i \rightarrow \leq \text{amt}$)

$dp[i]$

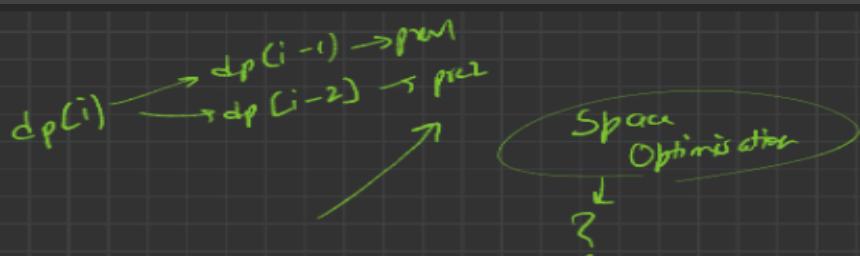
$dp[i-1]$

$dp[i-2]$

$dp[\text{amount}]$

① Recursion :-
 $T.C \rightarrow \underline{O(n)}$
 $T.C \rightarrow \underline{x \times n}$
 amount \rightarrow no. of coins
 $S.C \rightarrow \underline{O(x)}$

② Tabulation $\rightarrow T.C \rightarrow \underline{x+n}$

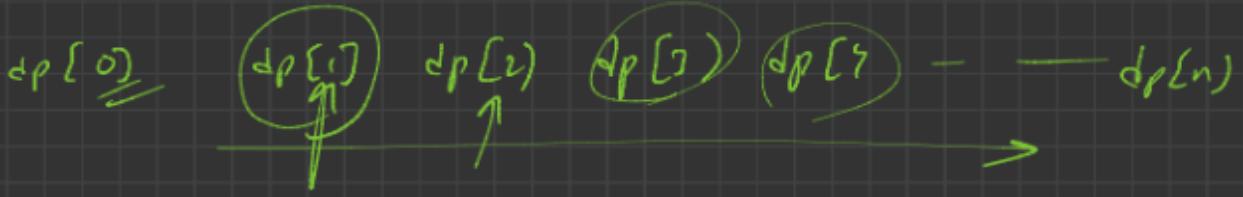


$S.C \rightarrow \underline{O(x)}$
 $S.C \rightarrow \underline{O(1)}$

$dp[i] \rightarrow dp[i - \text{num}[j]]$
 $i-1$
 $i-2$
 $i-3$
 $i-4$
 $i-5$
 \vdots
 i

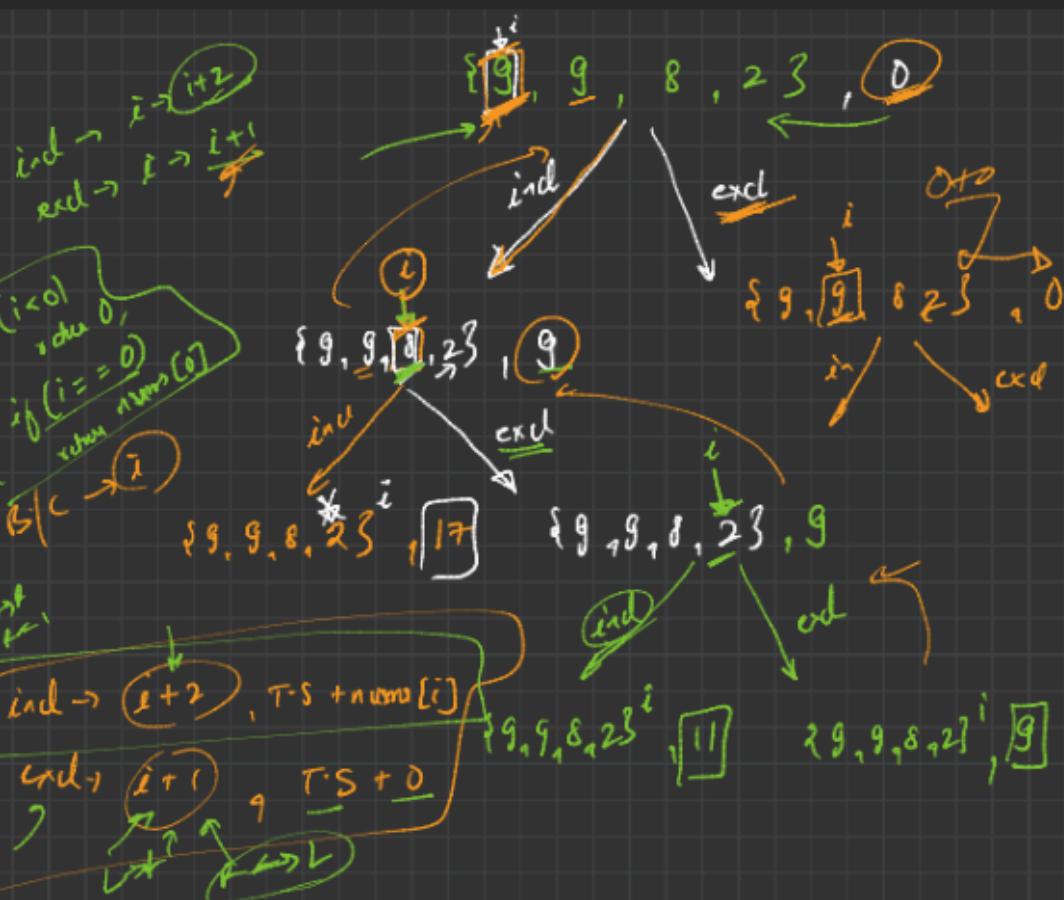
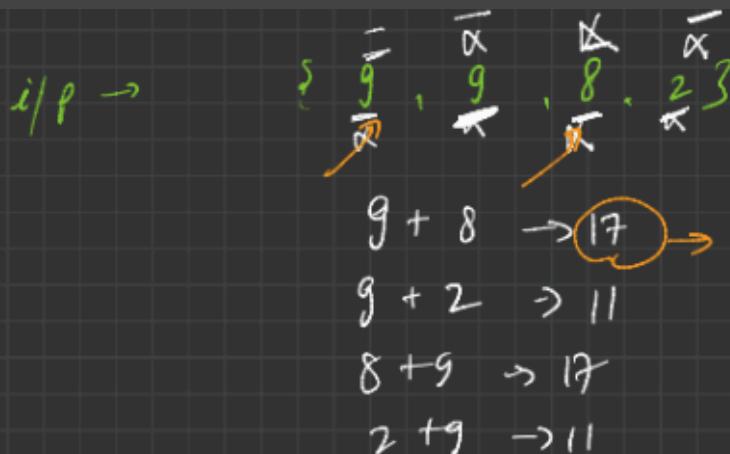
⑤

$\text{dp } x \rightarrow \text{variable}$
 $\text{dp } x \rightarrow \underline{O(x)}$



Maximum Sum Of Non-Adjacent Elements By Recursion / Top-Down Approach /

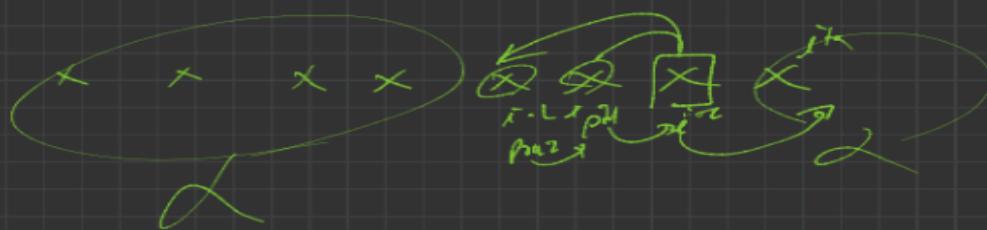
Bottom-Up Approach / Space Optimization Approach:



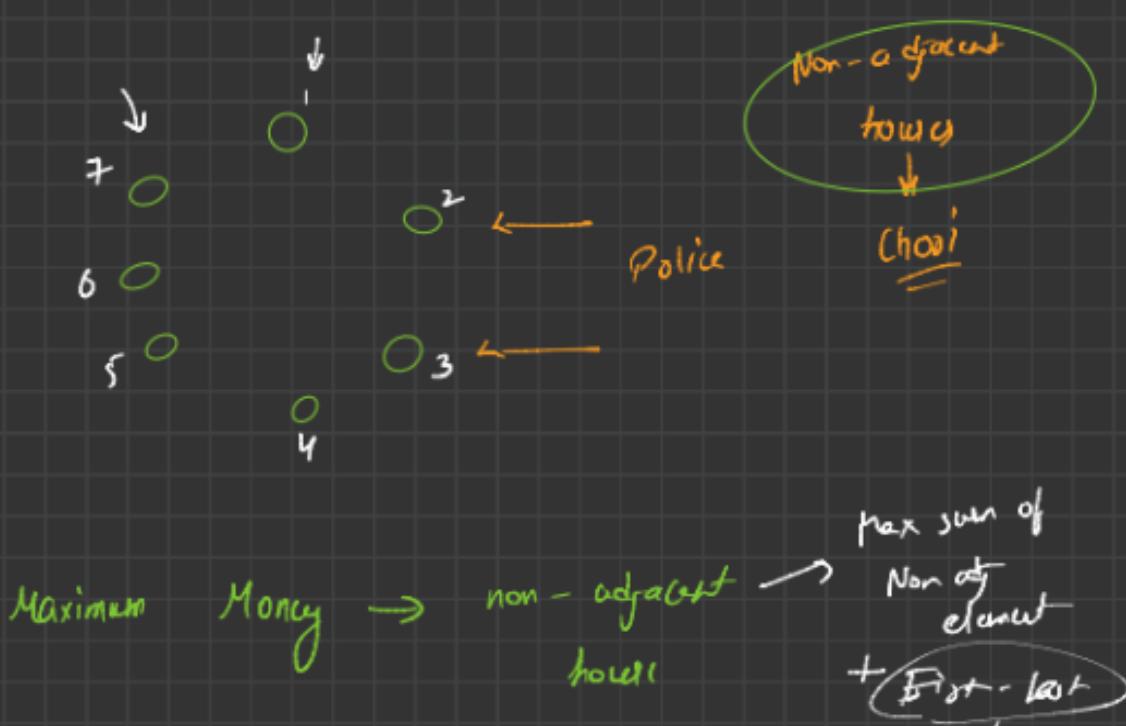
\rightarrow Recursive + Memoisation $\xrightarrow{\quad}$ T.C $\rightarrow O(N)$
 \rightarrow Tabulation $\xrightarrow{\quad}$ T.C $\rightarrow O(N)$
 \rightarrow Space Optimisation $\rightarrow O(1)$

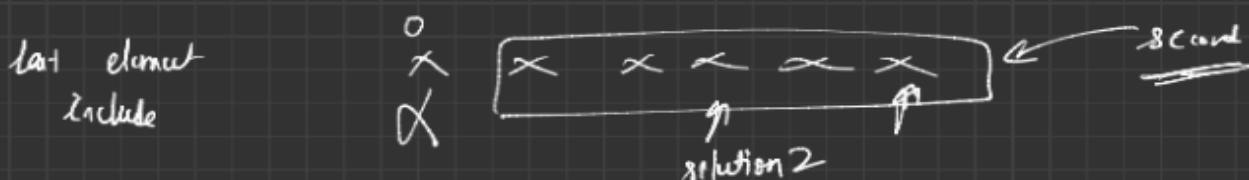
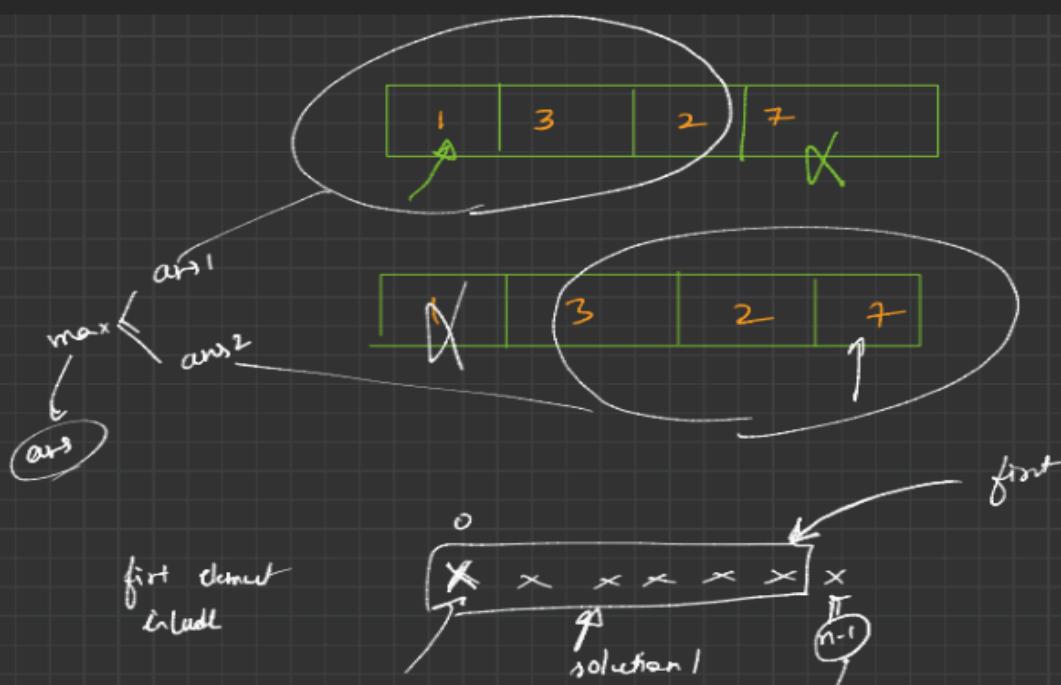
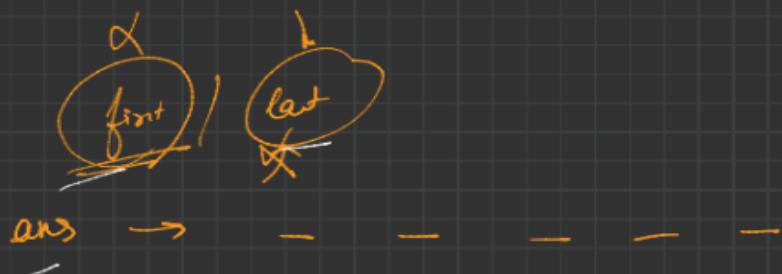
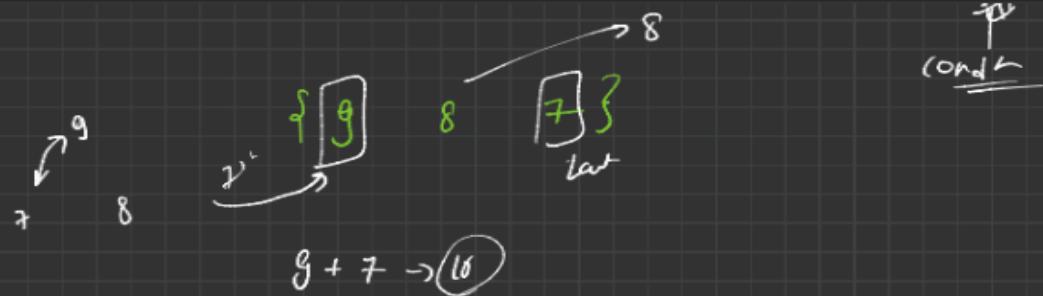
$dp[i] \xrightarrow{\quad} \text{ind} \rightarrow dp[i-2]$
 $\xrightarrow{\quad} \text{excl} \rightarrow dp[i-1]$

$dp[i] \xrightarrow{\quad} dp[i-2] -$
 $\xrightarrow{\quad} dp[i-1] -$



House Robbery Problem By Tabulation With Space Optimized Approach:





$$ans = \max(\underline{\text{sol}_1, \text{sol}_2})$$

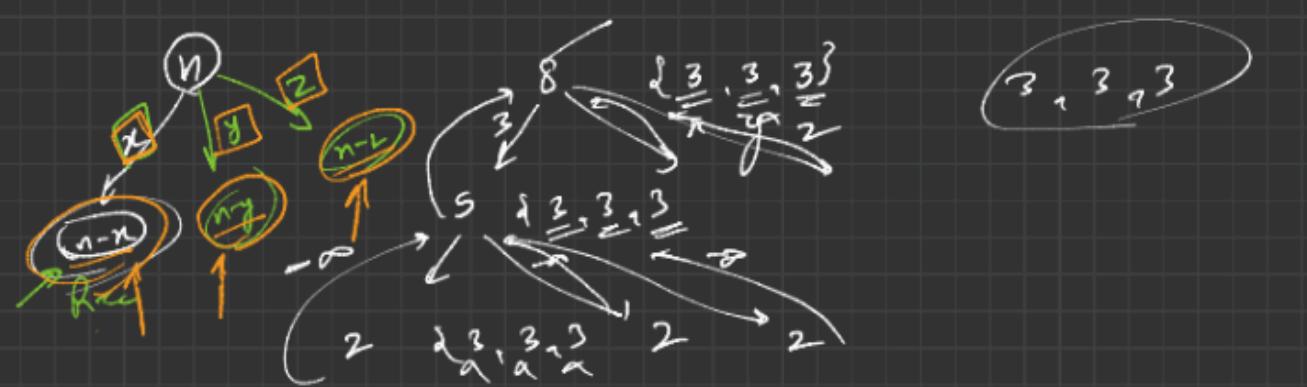
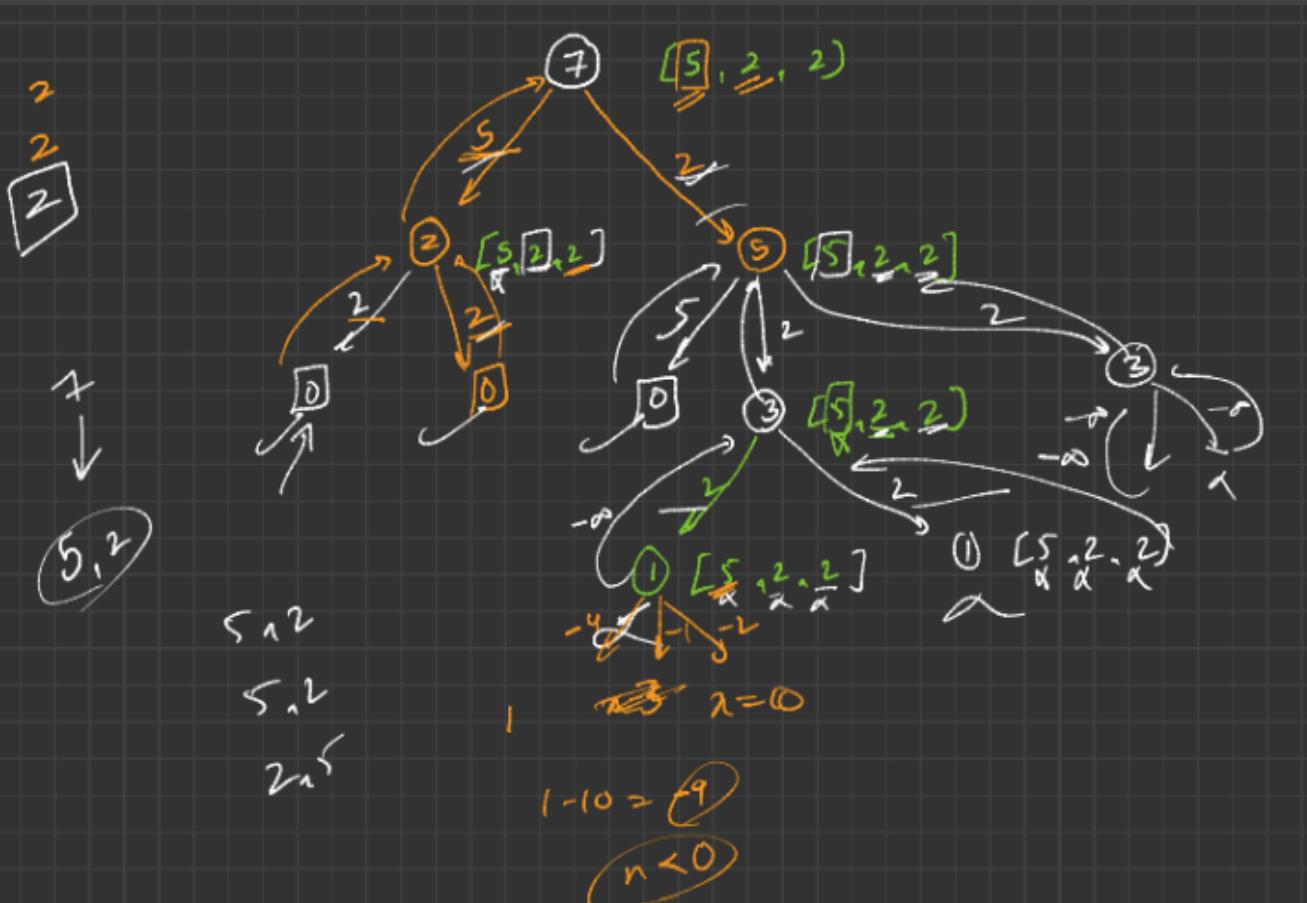
$T \in O(N)$
 $S \in O(N)$

Cut Rod Into Segments X,Y,Z.... By Recursion / Top-Down Approach / Bottom-Up

Approach:

$$\rightarrow N \rightarrow 7$$

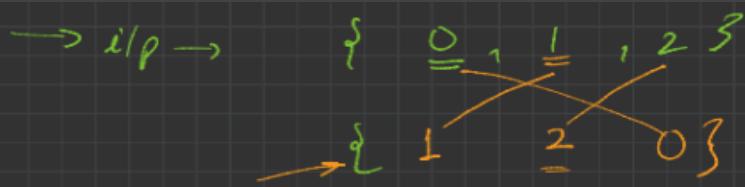
15 2 2 3
入 Y Z



$$d\mu^{(0)} > 0 \quad + \quad \xrightarrow{n}$$

Count Derangements By Recursion / Top-Down Approach / Bottom-Up

Approach / Space Optimization Approach:



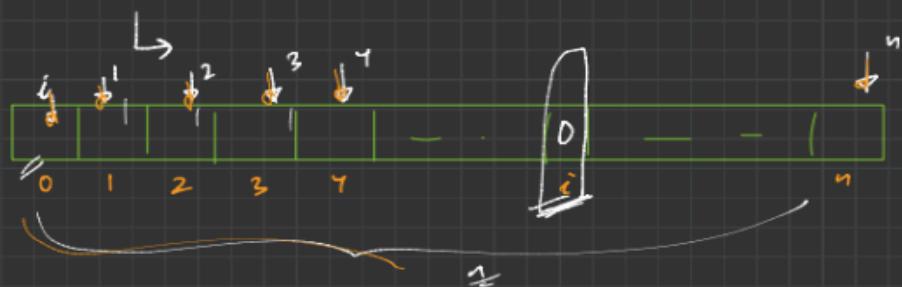
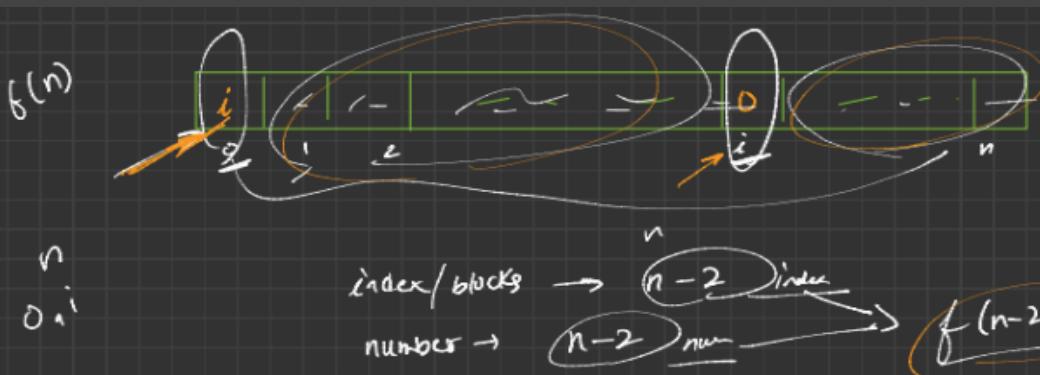
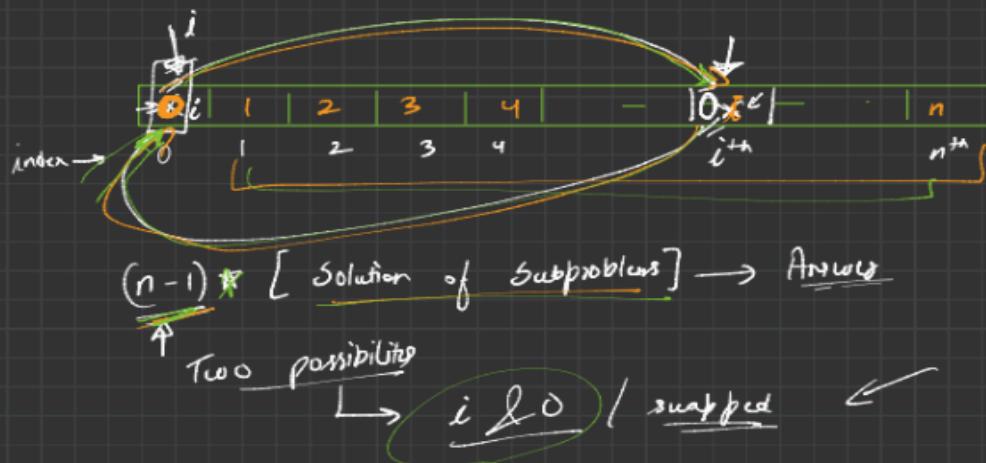
$N = 3$

{0, 1, 2}

$N = 7$

{0, 1, 2, 3, 4, 5, 6, 7}

i/p $\rightarrow N \rightarrow \{0, 1, 2, 3, \dots, N-1\}$



index / blocks \rightarrow $n-1$
 number \rightarrow $n-1$ num $\Rightarrow f(n-1)$

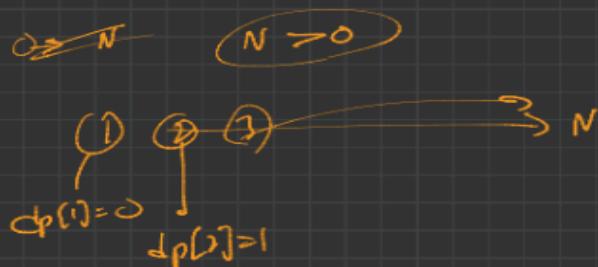
$$f(n) \rightarrow (n-1) * [f(n-2) + f(n-1)]$$

$N=2$
 $\{0, 1\}$

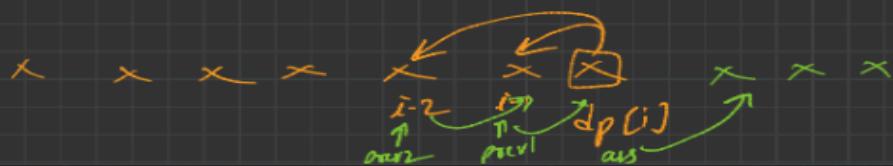
$N=1$
 $\{0\}$

$\boxed{0}$

$$\boxed{\begin{matrix} 0 & 1 \\ 0 & 1 \end{matrix}} \rightarrow \boxed{\begin{matrix} 1 & 0 \\ 0 & 1 \end{matrix}}$$



$$\underline{S.O} \rightarrow dp[i] \xrightarrow{\quad} dp[i-1] \xrightarrow{\quad} dp[i-2]$$



$$\text{aus} = \text{prev1} + \text{prev2}$$

$$\text{prev2} = \text{prev1}$$

$$\text{prev1} = \text{aus}$$

$$\Rightarrow O(1)$$

Rec \rightarrow expo

Rec + Mem \rightarrow T.C $\rightarrow O(n)$

T.C $\rightarrow O(n) + O(n)$

Tab \rightarrow T.C $\rightarrow O(n)$

T.C $\rightarrow O(n)$

S.O
 \downarrow
 S.C $\rightarrow O(1)$

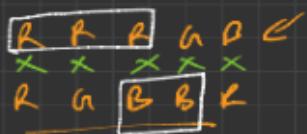
Painting Fence Problem By Recursion / Top-Down Approach / Bottom-Up

Approach / Space Optimization Approach:

\rightarrow i/p \rightarrow "n" post, "k" color

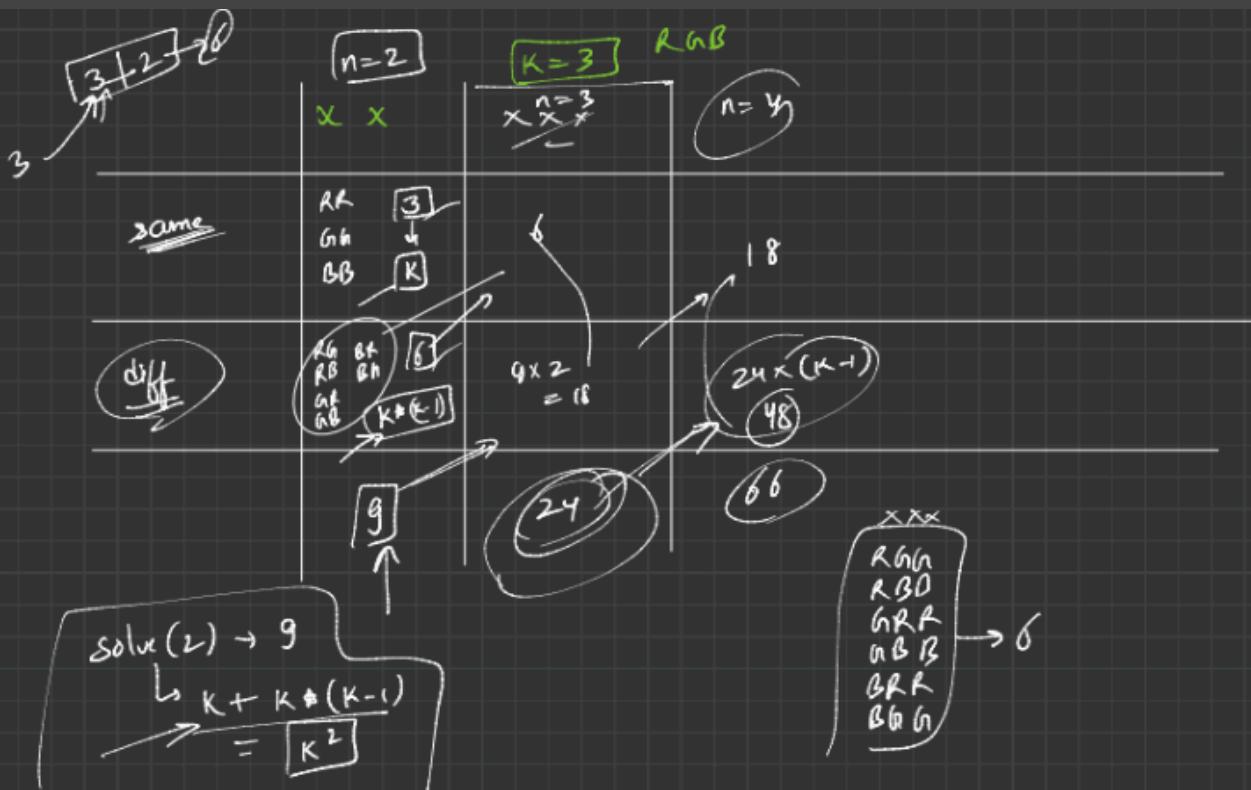
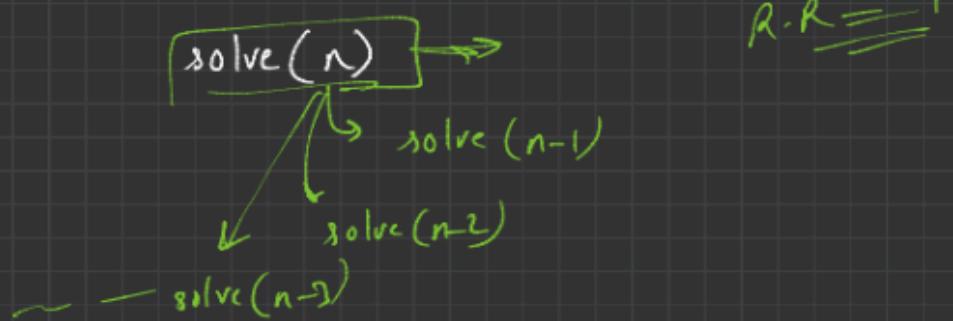
$k=3$
R G B

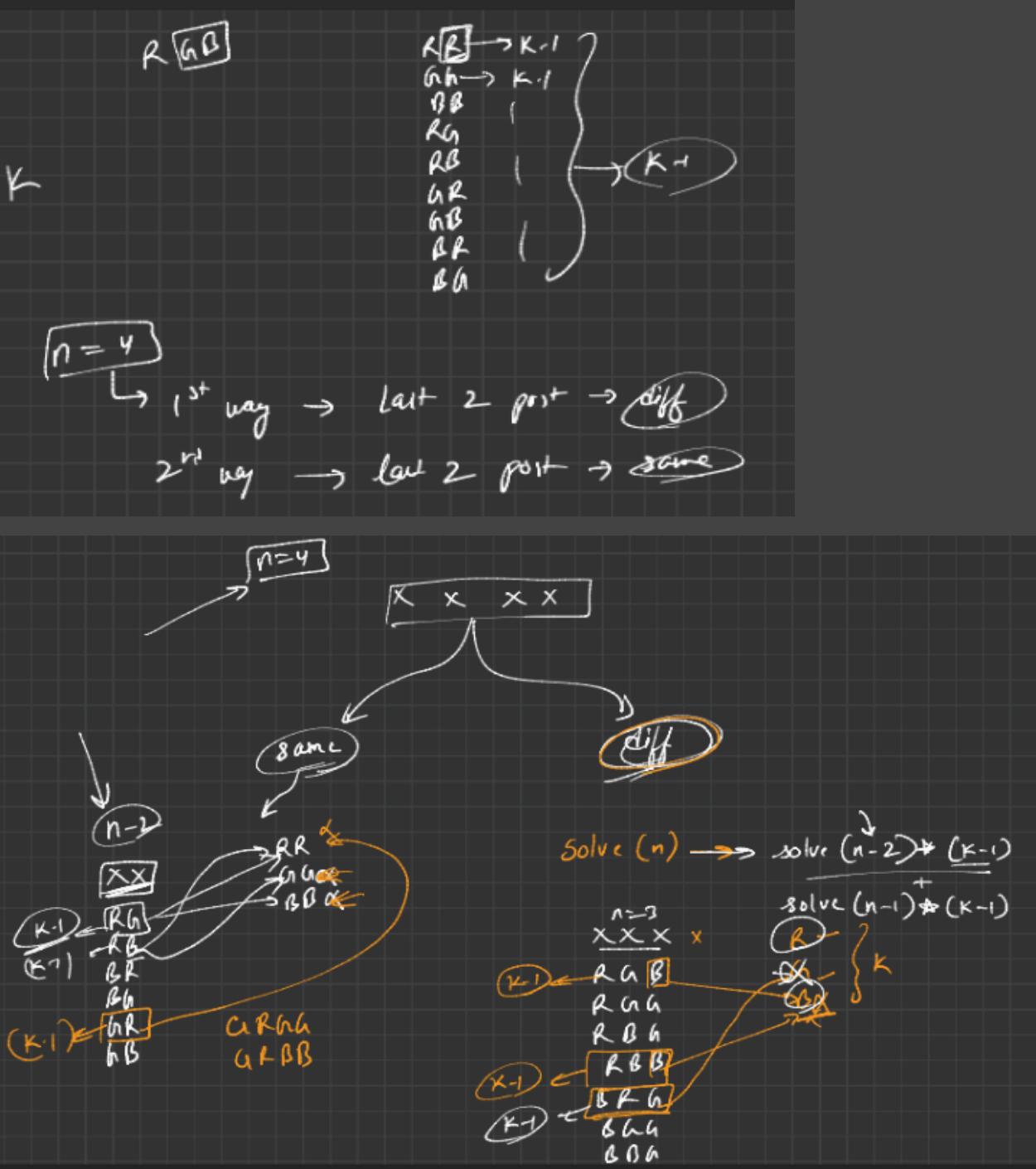
5 post



Cond Δ \rightarrow not more than adjacent post has same color

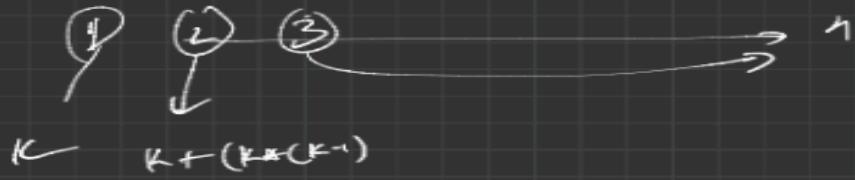
solve (n, k)





$R.R$

$solve(n) = solve(n-2) + (K-1)$
 $+ solve(n-1) + (K-1)$
 same
 diff

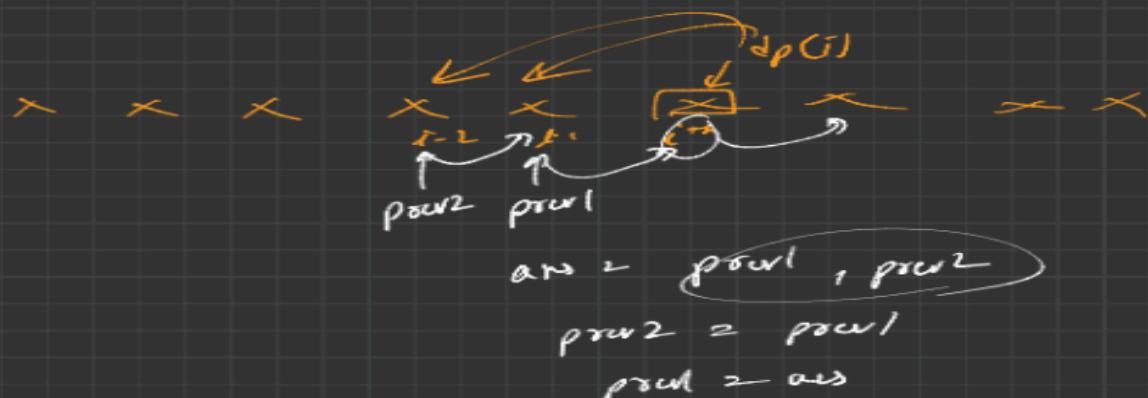


Rec \rightarrow expo

$$\text{Rec + Memo} \rightarrow T \hookrightarrow O(n) \\ S \hookrightarrow O(n) + O(n)$$

$$\text{Tab} \rightarrow T \hookrightarrow O(n) \\ S \hookrightarrow O(n) \xrightarrow[S \cdot O]{} O(1)$$

$$dp[i] \xrightarrow{\quad} dp[i-1] \\ dp[i] \xrightarrow{\quad} dp[i-2]$$



0/1 KnapSack Problem By Recursion / Top-Down Approach / Bottom-Up

Approach / Space Optimization Approach:

This \rightarrow Knapsack \rightarrow can carry W

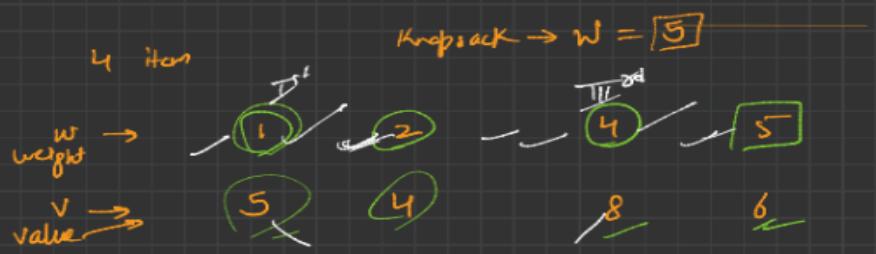
n item

1 2 3 4 5 - n^{th}

$w_1 \quad w_2 \quad w_3 \quad w_4 \quad \dots \quad w_n$

$v_1 \quad v_2 \quad v_3 \quad v_4 \quad \dots \quad v_n$

Value max



$$\{5\} \rightarrow \text{value } 6$$

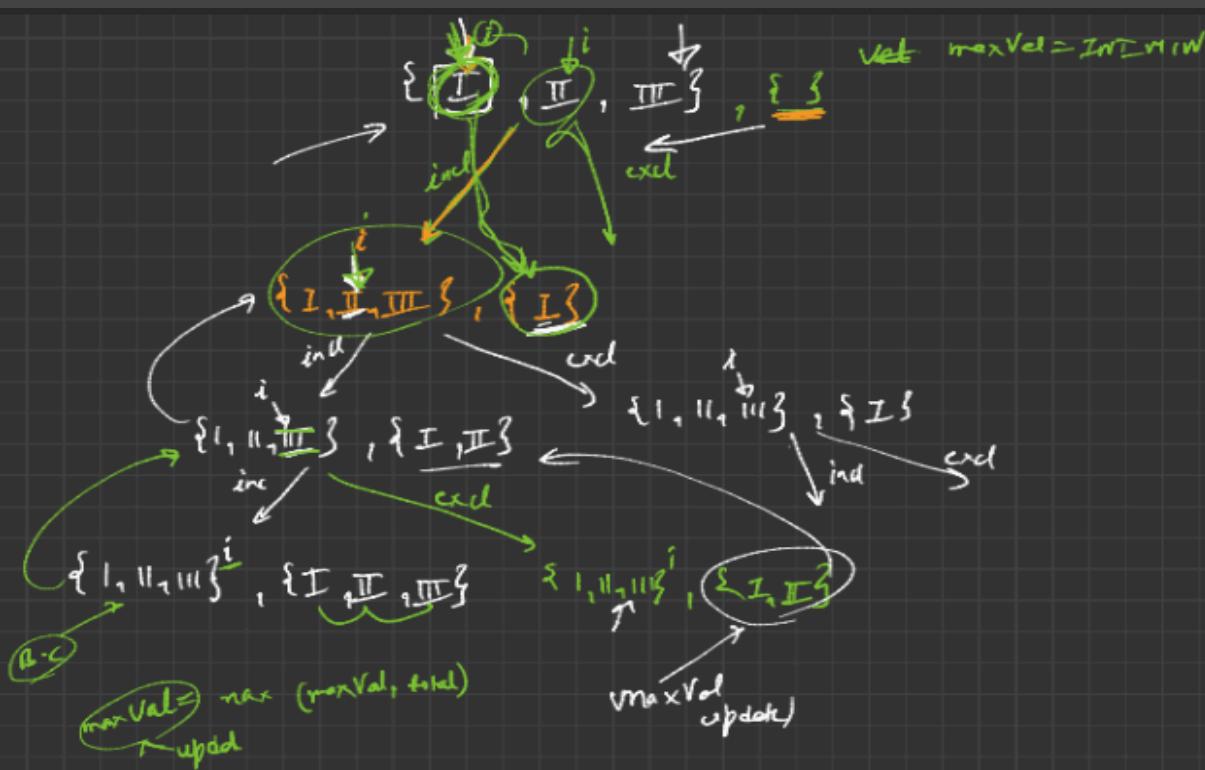
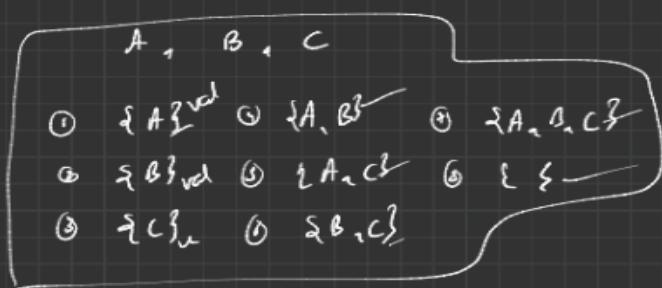
$$\{1, 4\} \rightarrow 8+5 \rightarrow \text{value } 13$$

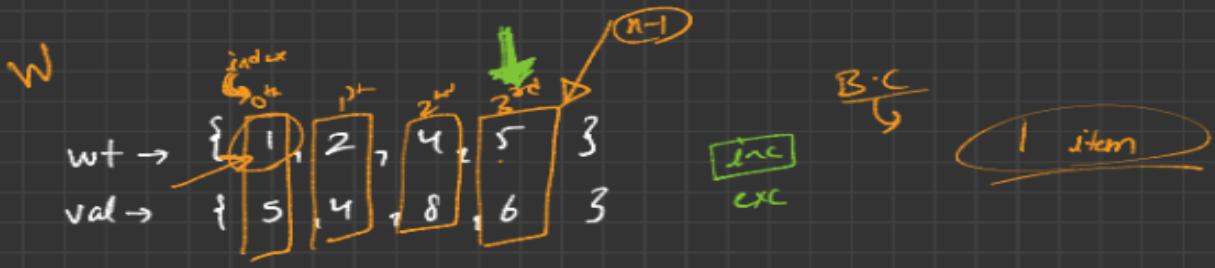
$$\{1, 2\} \rightarrow 5+4 \rightarrow \text{value } 9$$

$$\{1, 2, 3, 4\} \rightarrow \underline{\underline{13}} \quad \underline{\underline{12}} \quad \underline{\underline{11}} \quad \underline{\underline{10}} \quad \underline{\underline{22}} \quad \underline{\underline{21}}$$

Approach \rightarrow Brute force

3 items





W

```

if ( $wt[0] \leq maxWeight$ )
    return  $val[0]$ 
else
    return 0
  
```

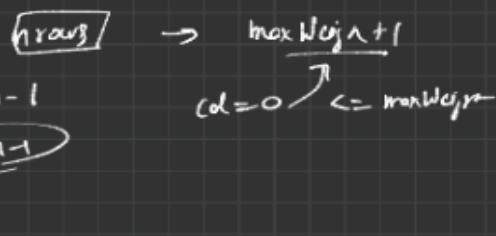
① Recursive + Memoization (Top-Down)

Step 1 \rightarrow dp array $\rightarrow (-1)$

Step 2 \rightarrow Rec call \rightarrow dp \rightarrow cur state

Step 3 \rightarrow B.C. \rightarrow if dp array contains any then return

② Bottom-Up Approach (Tabulation) ~~(Top-Down)~~



①

rows $\rightarrow n$

cols $\rightarrow maxWeight+1$

$0 \rightarrow maxWeight$

$for (= 0, < maxWeight+1)$

$for (= 1, < n)$



O)

can be improved ↴

prev



curr [w]

prev [w]

prev [w - wt(index)]

curr



curr [w]

prev [w]

prev [w - weight[index]]

curr

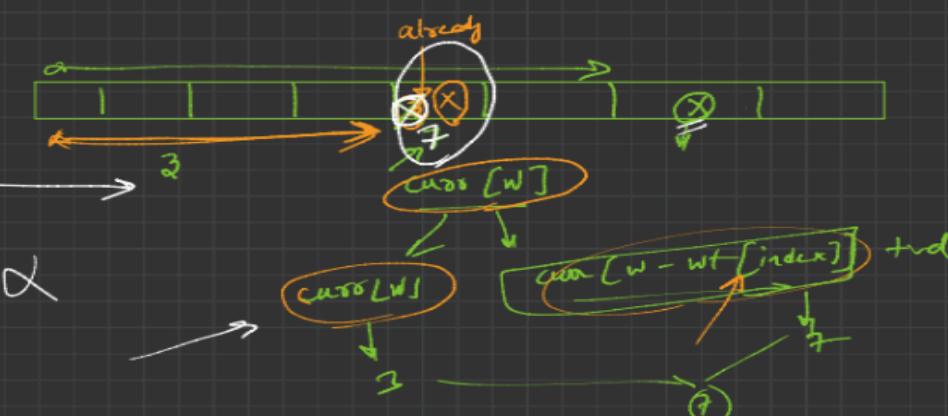


exclude → curr [w]

ind →

$$\rightarrow + \left[curr [w - weight[index]] \right]$$

curr



curr

Recursive →

+ memoisation =

$$O(n \cdot w) \rightarrow \text{SC}$$

Tabulation → $O(n \cdot w)$

$$SC \rightarrow O(1)$$

$$SC \rightarrow O(2^w \cdot n)$$

$$\underline{O(w)}$$

Combination Sum Problem By Recursion / Top-Down / Bottom-Up Approach:

Input $\rightarrow \boxed{N=3} \rightarrow \{1, 2, 5\}$

target = 5

$\{1, 1, 1, 1, 1\}$

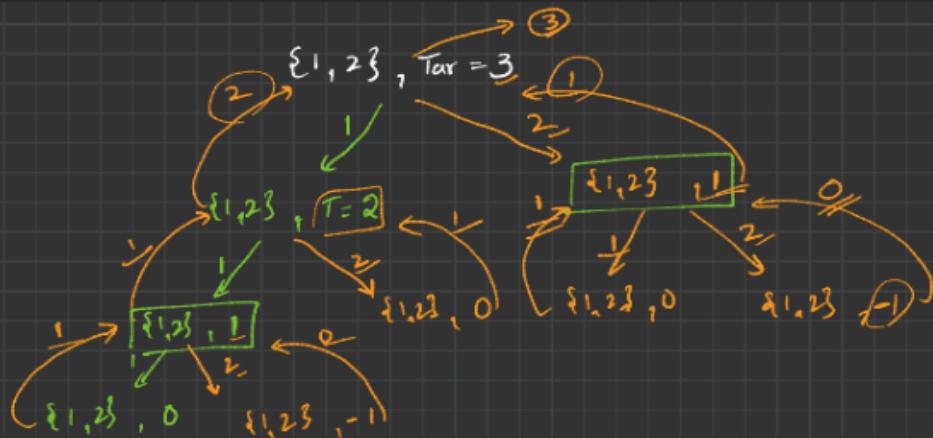
$\{1, 1, 1, 2\}$

$\{1, 2, 2\}$

$\{2, 1, 2\}$

$\{2, 2, 1\}$

$\{5\}$

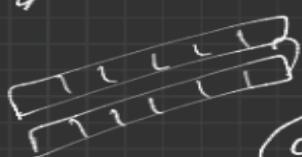


if $T < 0$ return 0
if $T = 0$ return 1

$\frac{S \cdot O}{T}$

$dp[n]$

$n \rightarrow$ target
possible ways



$dp[i] \rightarrow dp[i - num[j]]$

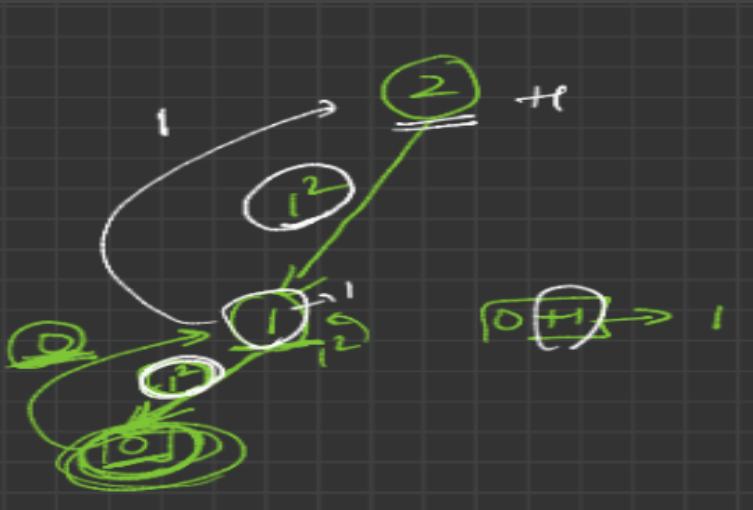
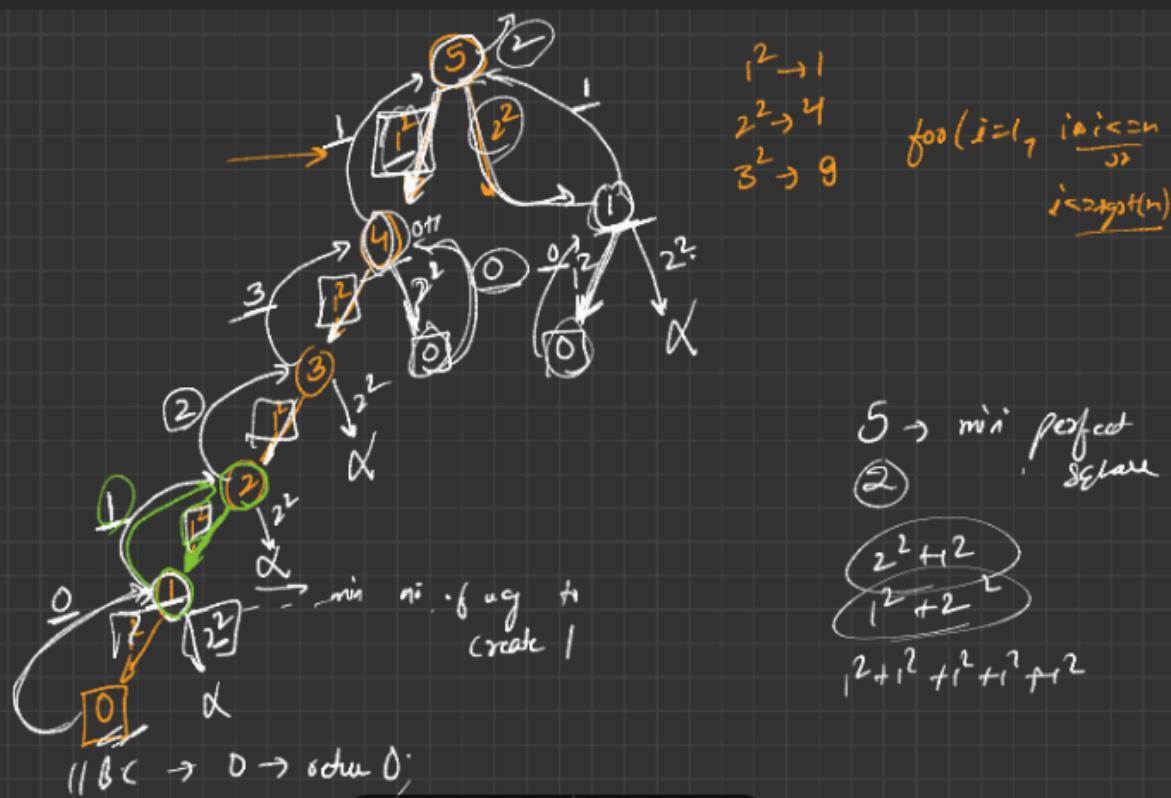
ID

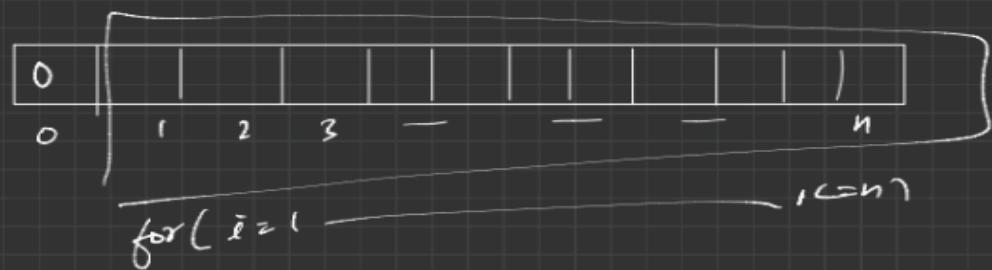
$\frac{a | x | \times | + |}{L} \rightarrow \frac{(*) | L |}{L}$

Get Minimum Squares By Recursion / Top-Down / Bottom-Up Approach:

$$\underline{i/p} \rightarrow n = 100$$

$$\begin{aligned}
 & \rightarrow (10 \times 10) \rightarrow 1 \rightarrow a+b=1 \\
 & \rightarrow (5^2 + 5^1 + 5^2 + 5^2) \rightarrow 4 \\
 & \rightarrow \text{---} \rightarrow f \\
 & \text{---} \rightarrow s \\
 & \text{---} \rightarrow 10 \\
 & \text{---}
 \end{aligned}$$

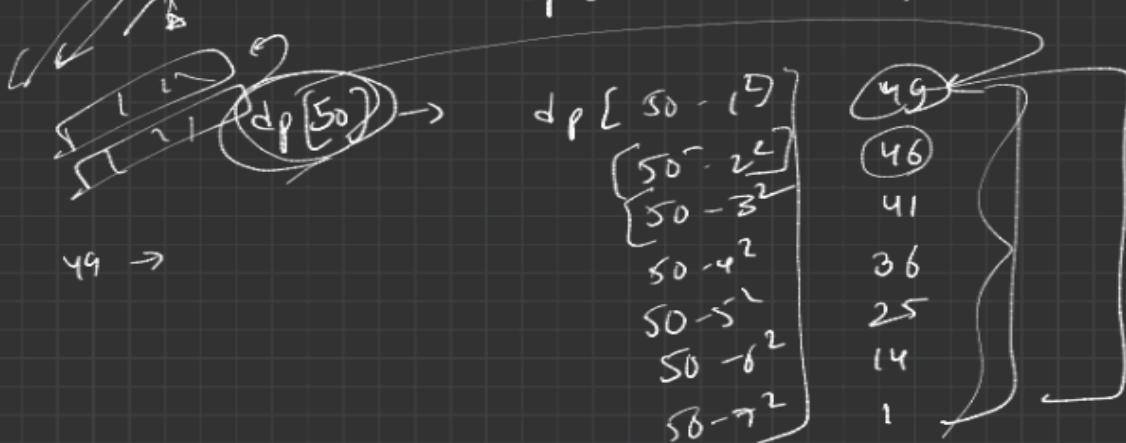




$$\underline{5.0} \rightarrow ?$$

$$dp[i] \rightarrow dp[i - j \oplus j]$$

$$\begin{aligned} \text{dp}[5] &\rightarrow \text{dp}[5 - 1^2] \rightarrow \text{dp}[4] \\ &\quad \text{dp}[5 - 2^2] \rightarrow \text{dp}[1] \end{aligned}$$

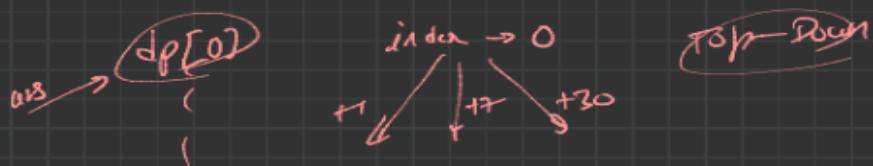
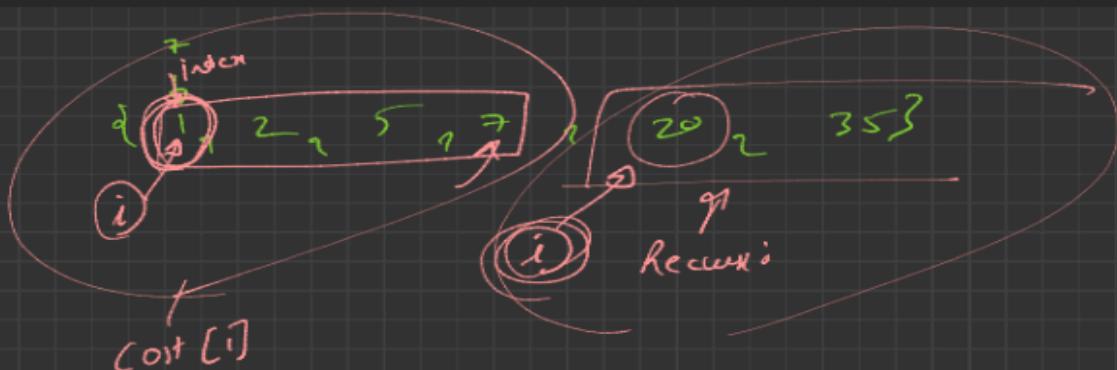
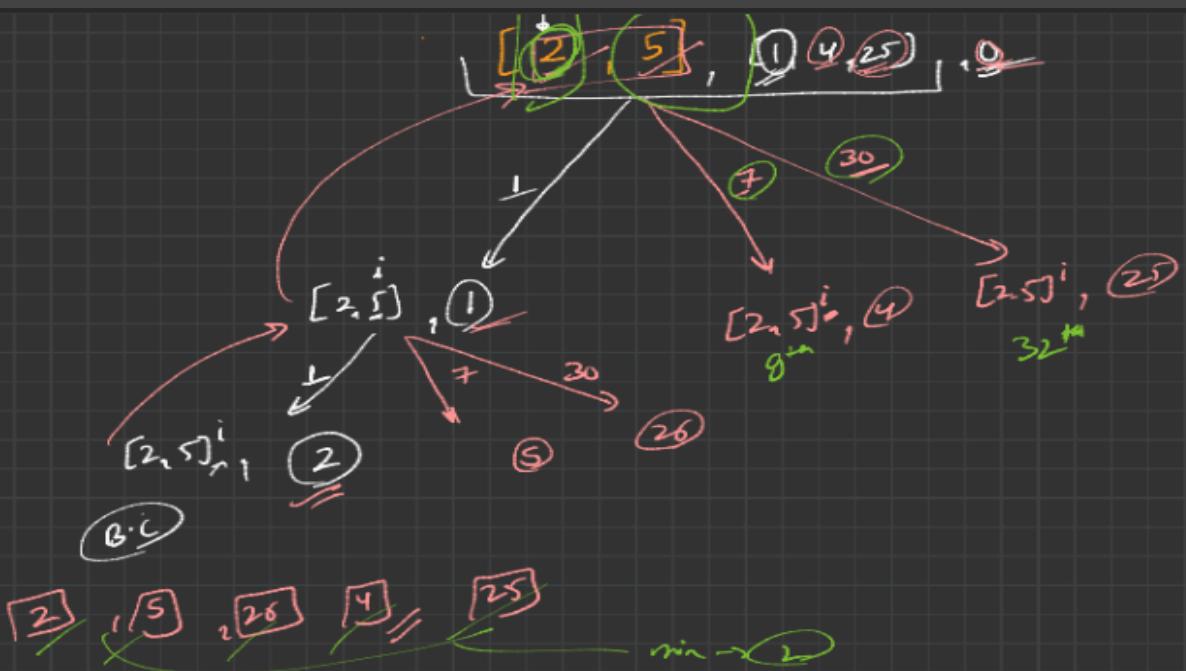


Minimum Cost For Tickets By Recursion / Top-Down / Bottom-Up Approach:

i/p \rightarrow days $\rightarrow \{ \downarrow, 4, 6, \uparrow, 7, 8, 120 \}$

$\text{Corr} \rightarrow [2, 7, 15]$

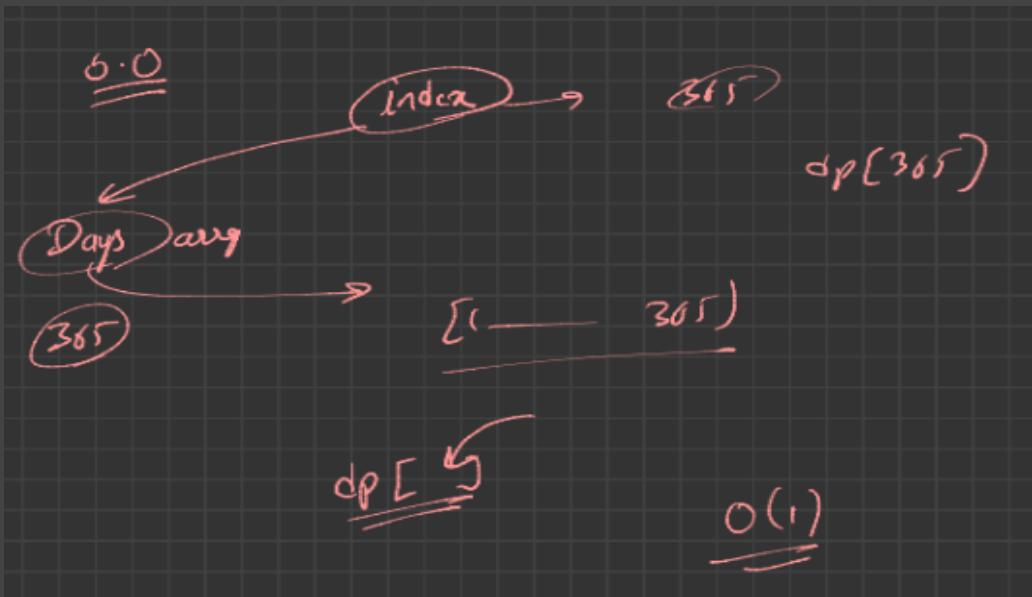
$$\begin{aligned} f \times 2 &\quad (2) \\ 7 + 2 + 2 &\rightarrow (11) \text{ E } \quad \left. \right\} \quad (11) \text{ E} \\ 30 \rightarrow 15 \text{ E} & \quad \left. \right\} \end{aligned}$$



$$\begin{array}{c} dp(n) \\ dp(n-1) \\ \vdots \\ dp(0) \end{array}$$



for ($n-1 \rightarrow 0$)



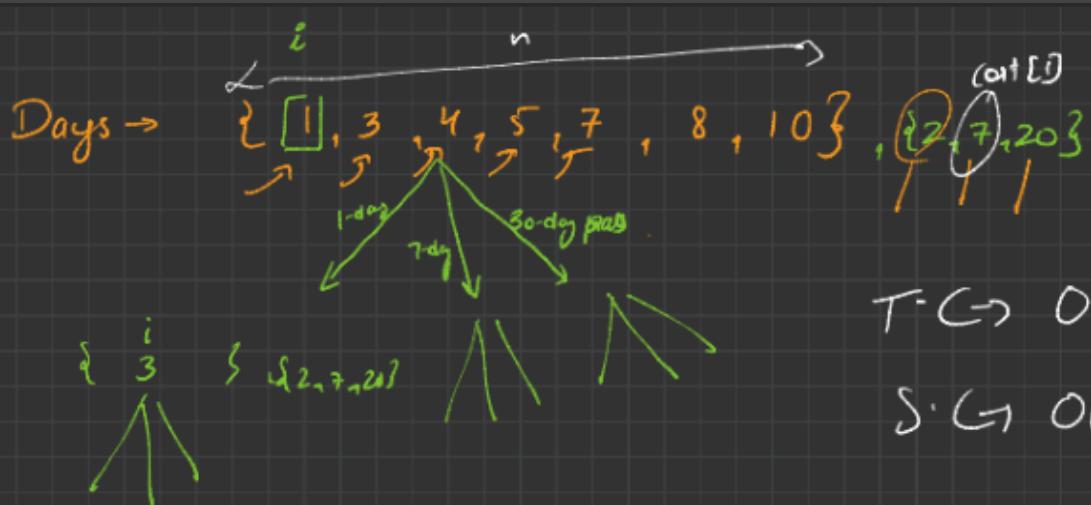
#4 → Space Optimisation] next Episode 20min

→ Bottom-up Approach -

$$T.C \hookrightarrow O(n)$$

$$S.C \hookrightarrow O(n)$$

$$\underline{\underline{O(1)}}$$



→ ans → min no of coins

$$\boxed{\text{int ans = INT_MAX;}}$$



$S.C \rightarrow O(1)$

$\text{int ans} = \text{INIT_MAX};$

$\boxed{\text{for (day : days)}}$

// 1 step → remove expired days from queue

$\text{while } (\cancel{\text{size}} \text{ monthly.front - first + 30} \leq \text{day})$

monthly.pop
 $\text{while } (\cancel{\text{size}} \text{ weekly.front - first + 7} \leq \text{day})$
 weekly.pop()

// Step 2 → push current day's cost

$\text{weekly.push}(\text{make_pair}(\text{day}, \text{ans} + \text{cost}[1]));$

$\text{monthly.push}(\text{make_pair}(\text{day}, \text{ans} + \text{cost}[2]));$

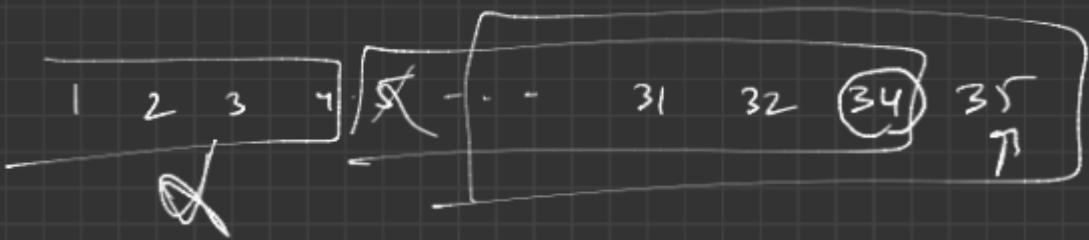
// Step 3 → ans update

$\text{ans} = \min(\text{ans} + \text{cost}[0], \min(\text{monthly.front - second},$
 $\text{weekly.} \cancel{-} \text{---}))$

}

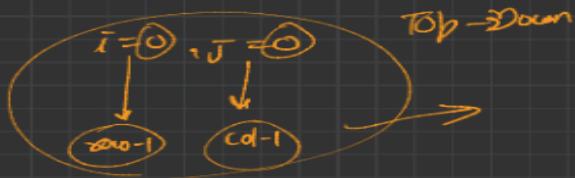
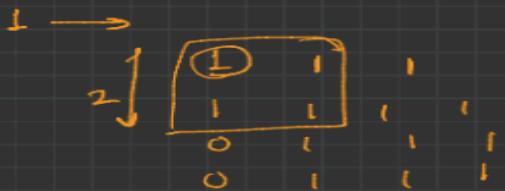
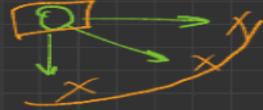
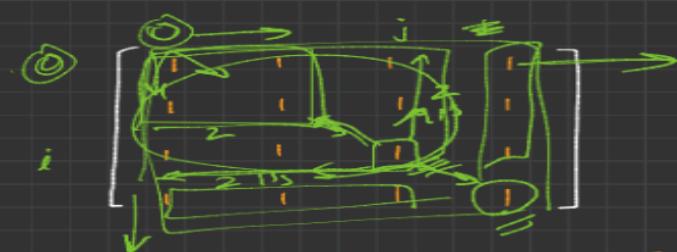
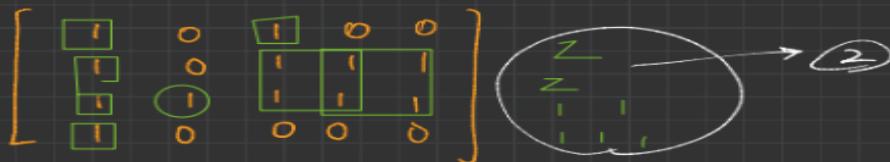
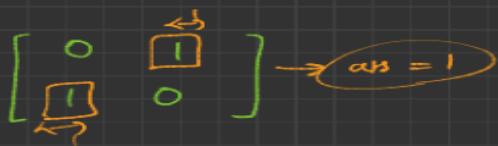
return ans;

3



Largest Square Area In Matrix By Recursion / Top-Down Approach / Bottom-Up

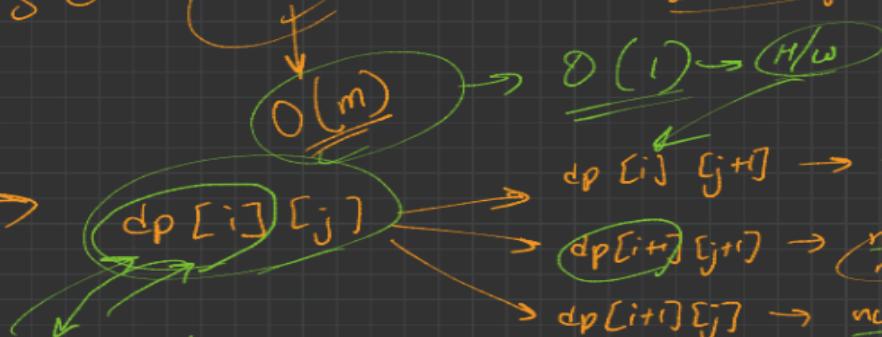
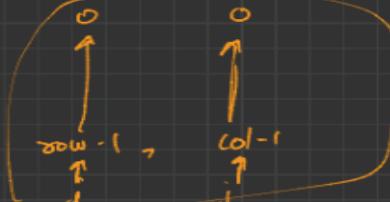
Approach / Space Optimization Approach:



Space Optimisation

$T \rightarrow O(m+n)$
 $S \rightarrow O(m+n)$

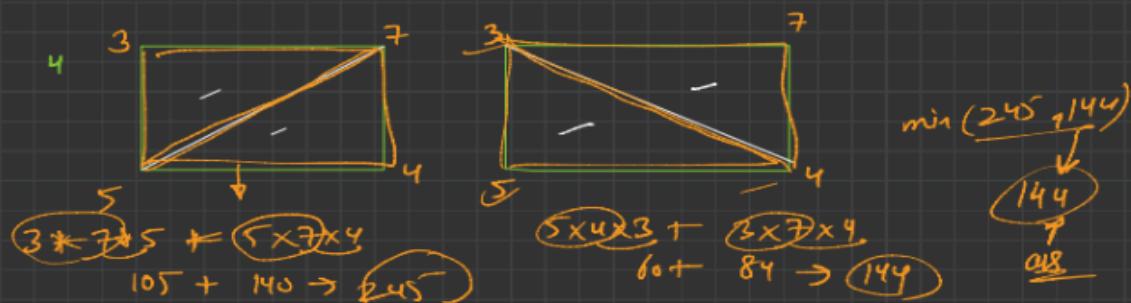
Bottom-UP



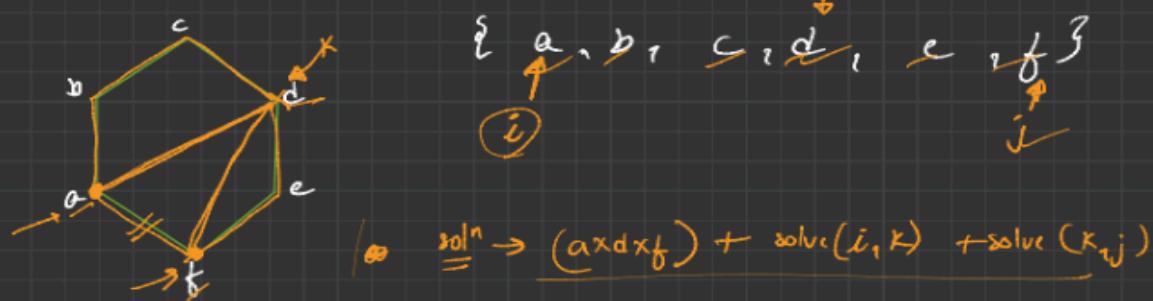
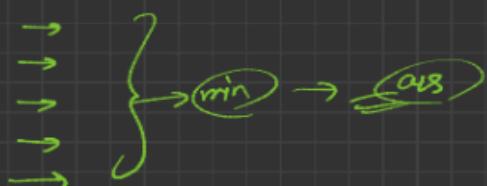
2 rows



Minimum Score Triangulation By Recursion / Top-Down / Bottom-Up Approach:

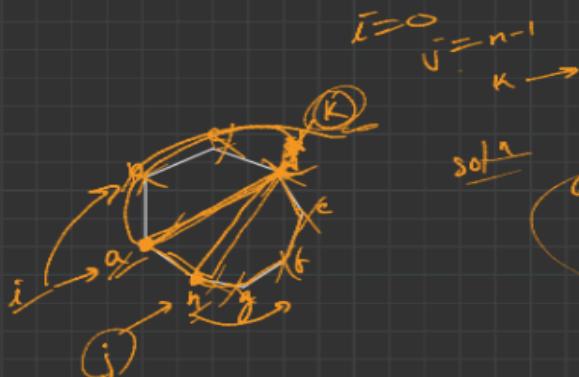


5 → 5 ways



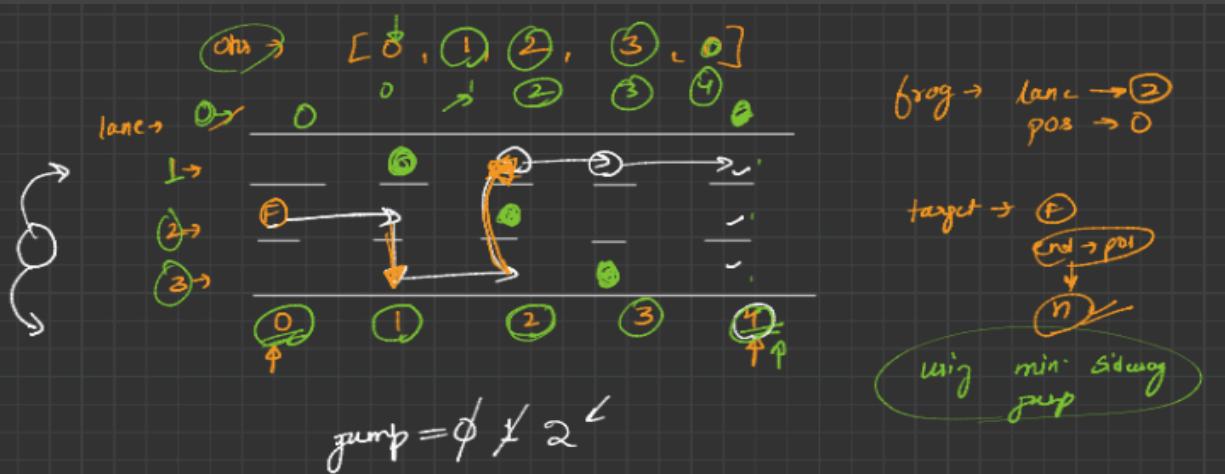
solve

$$solve(i, j) = (a \times d \times f) + solve(i, k) + solve(k, j)$$



Minimum Sideways Jumps By Recursion / Top-Down Approach / Bottom-Up

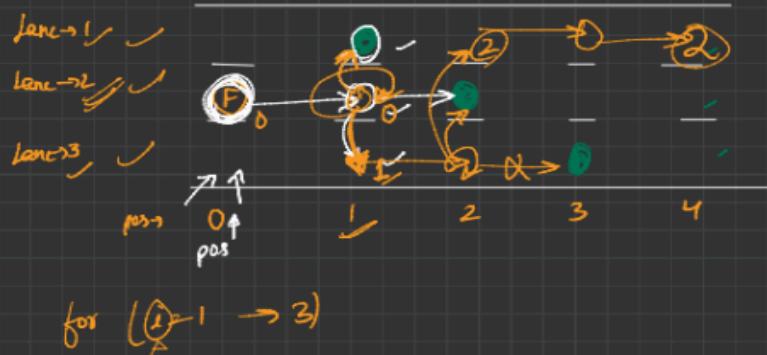
Approach / Space Optimization Approach:



obstacle [i] = 2

c^{4n} pos \rightarrow obs \rightarrow 2nd Lane

Approach



if ($pos == n$)
 return 0;

if (else [post+1])
! = curLane)

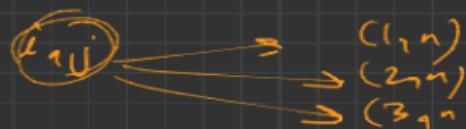
// S.W. Trap



if (rearLane != i)
 ↗ & obs[pos].! = i
 ↓
 update group

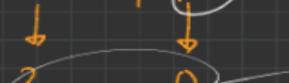


$d\rho [ij] [i]$



Top-Down

Lane, pos = n



(2, 0)

(1, n)

(2, n)

(3, n)

Bottom-Up

(1, n)

(2, n)

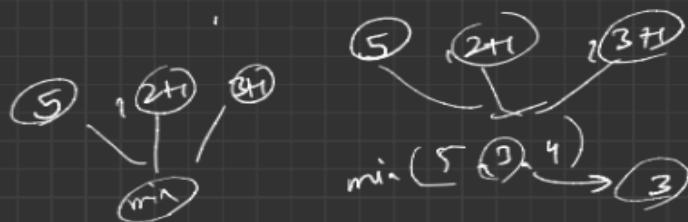
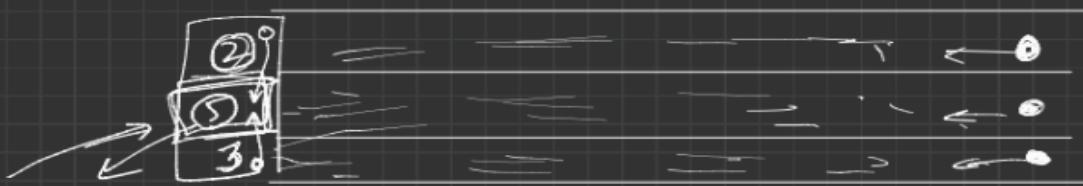
(3, n)

(1, n-1)

(2, n-1)

(3, n-1)

(2, 0)



Reducing Dishes By Recursion / Top-Down Approach / Bottom-Up Approach / Space Optimization Approach:

$$i/p \rightarrow s \rightarrow \{ -1, -8, 0, 5, -9 \}$$

↑ ↑ ↑ ↑ ↑
 0^{th} 1^{st} 2^{nd} 3^{rd} 4^{th}

time → 1 unit of time
1 dish

$L-K \rightarrow \text{Coeff} \rightarrow$ time $\rightarrow s[i]$

$\Gamma \vdash C$

 Open with Google Docs

~~0, 5, -1~~

negate \downarrow include

$$[-1, 0, 5]$$

$$\frac{1}{-1 \times 1 + 0 \times 2 + 5 \times 3}$$

$$-1 + 0 + 15 \rightarrow \boxed{\sqrt{14}}$$

$$[4, 3, 2]$$

~~1017~~

$$[\frac{2}{1}, \frac{3}{1}, \frac{4}{1}]$$

$$2 \times 1 + 3 \times 2 + 4 \times 3 = \boxed{\sqrt{20}}$$

$$[-\infty, -4, -\infty]$$

$$[]$$

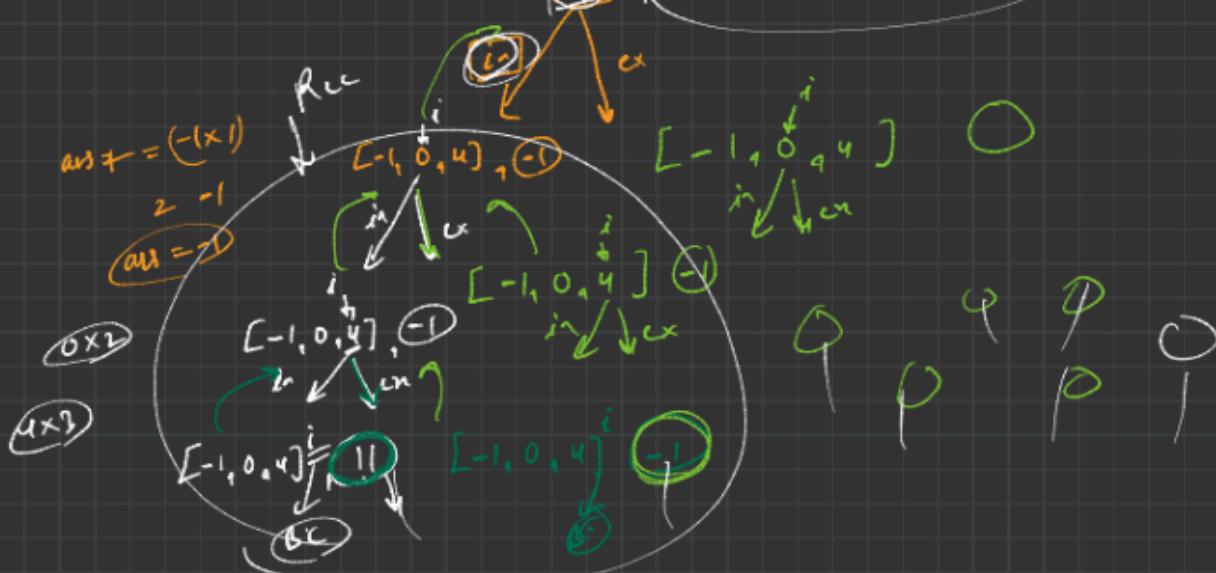
$$\rightarrow \underline{0}$$

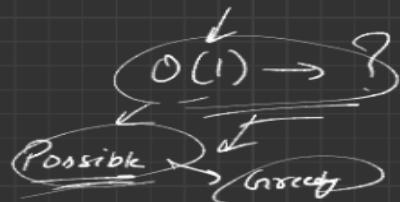
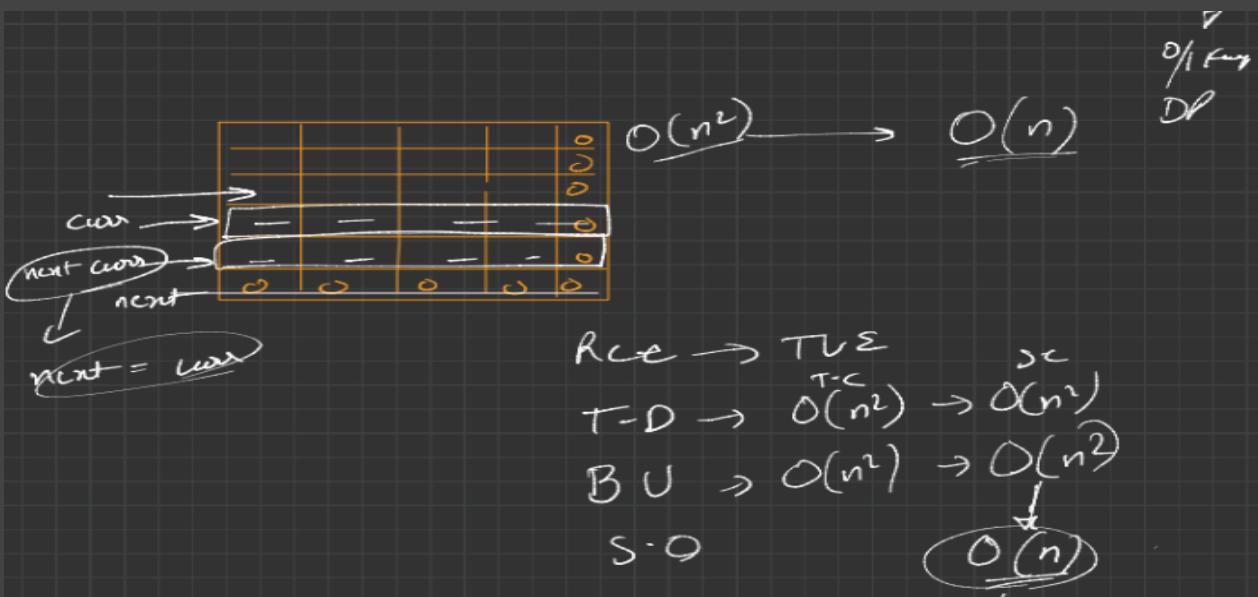
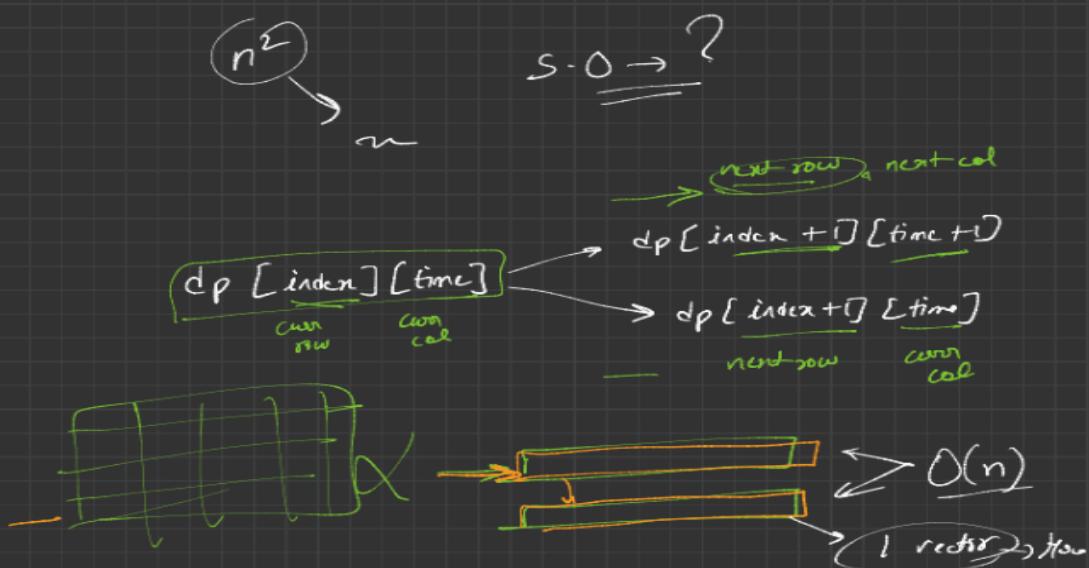
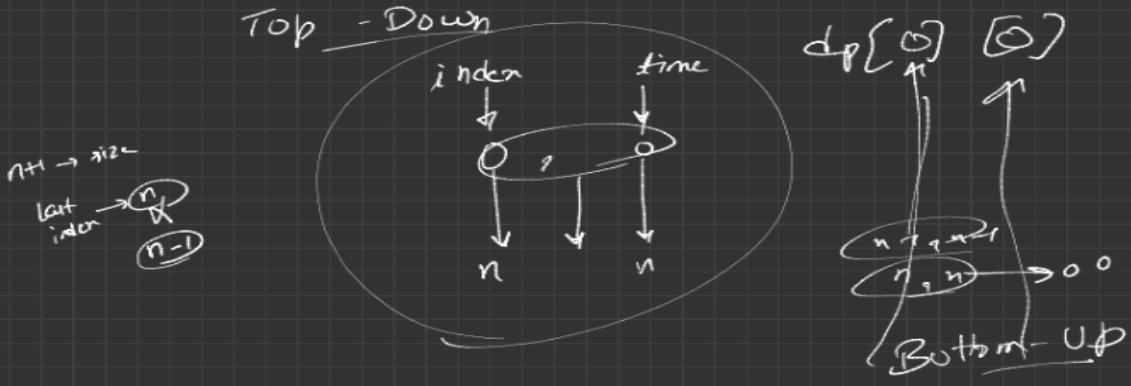
~~discard~~ $\rightarrow [a, b, c, d]$ ~~include~~

$\frac{x_1}{\text{Page } 1/5}, \frac{x_2}{\text{time}}, \frac{x_3}{\text{time}} + \frac{1}{\text{time}}$ ~~of Knapsack~~

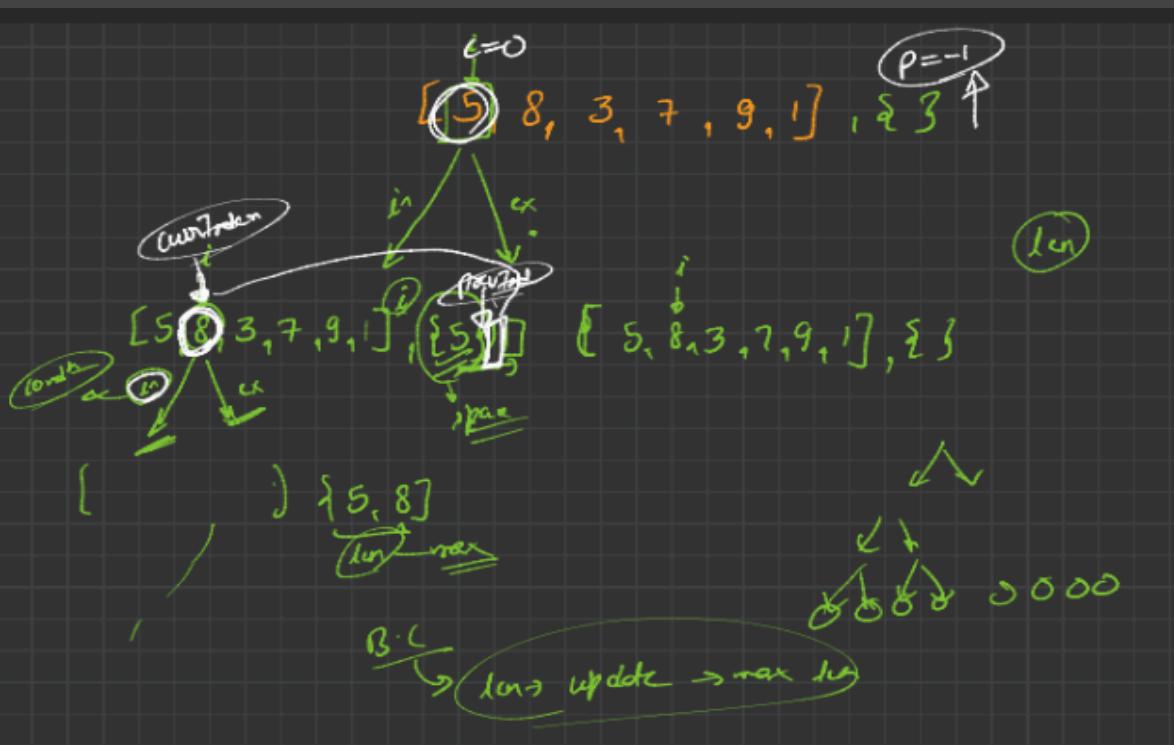
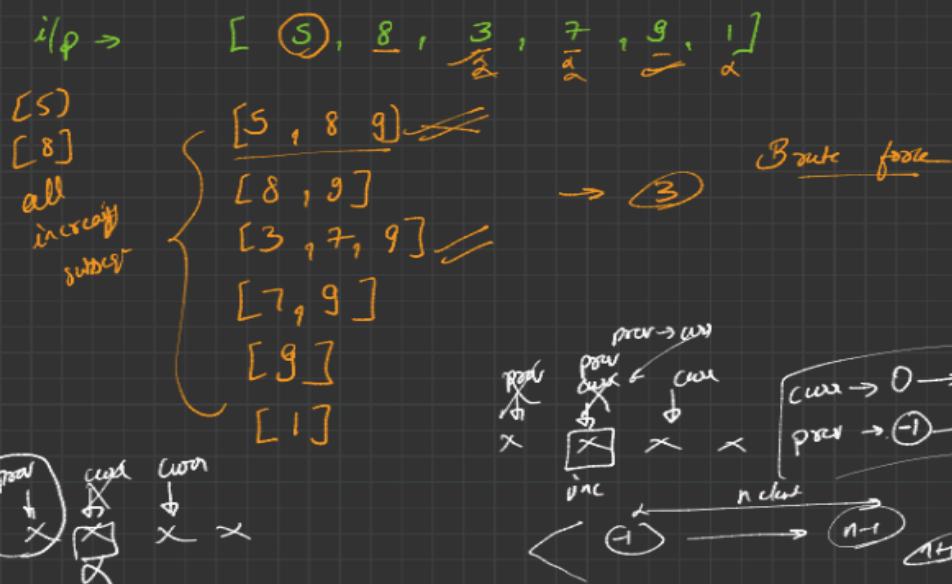
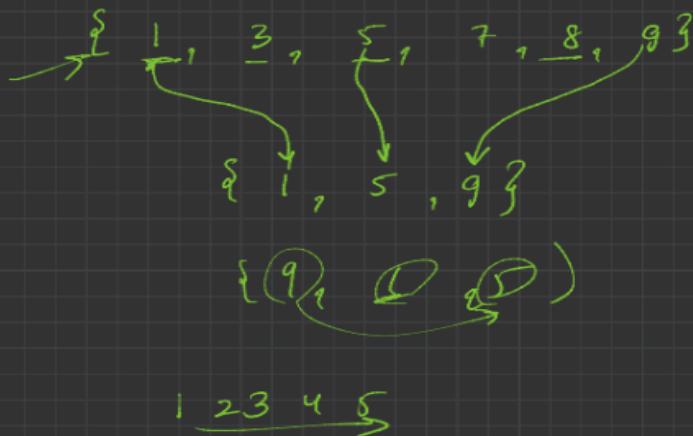
$$d \rightarrow [4, 0, -1]$$

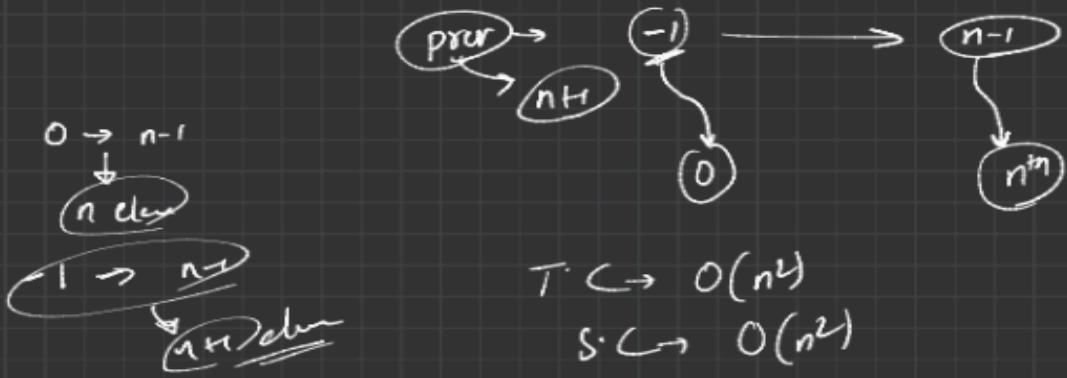
$\text{sol} \rightarrow [-1, 0, 4]$



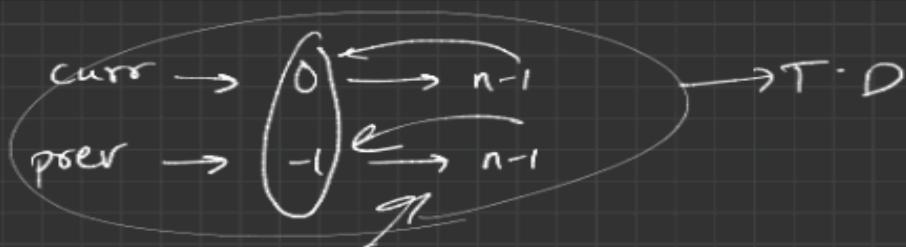


Longest Increasing Subsequence And Russian Doll Envelopes By Recursion /
 Top-Down Approach / Bottom-Up Approach / Space Optimization Approach:

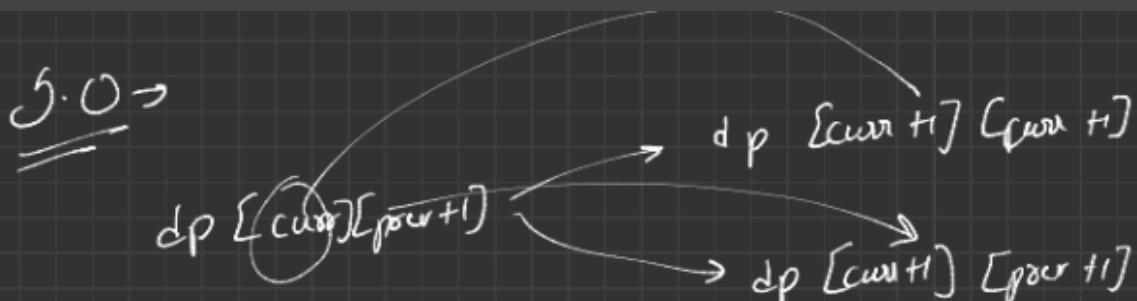




Bottom-up

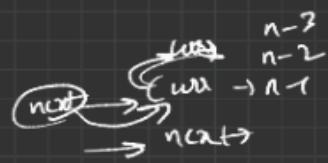


$B \cdot U \rightarrow$ $\boxed{T \hookrightarrow O(n^2)}$
 $S \hookrightarrow O(n^2)$



2 roots





$$T \in O(n^2)$$

$$S \cdot C \rightarrow O(2 \times (n+1))$$

$\mathcal{O}(n)$

curr

~~curr~~ →

~~next~~ →

→ DP with Binary Search :-

$$i/p \rightarrow [\frac{5}{\overline{1}}, \underline{\underline{8}}, \underline{\underline{\frac{3}{\overline{1}}}}, \underline{\underline{\frac{7}{\overline{1}}}}, \underline{\underline{\frac{9}{\overline{1}}}}, \underline{\underline{\frac{1}{\overline{1}}}}]$$

$$\left[\begin{array}{c} \cancel{-3, 7, 5} \\ \hline \cancel{-}, 1, \cancel{8}, 9 \\ \cancel{-} \quad \cancel{+ 9} \end{array} \right], 9$$

$$T \in \Theta(n \log n)$$

$$S \in \mathcal{O}(n)$$

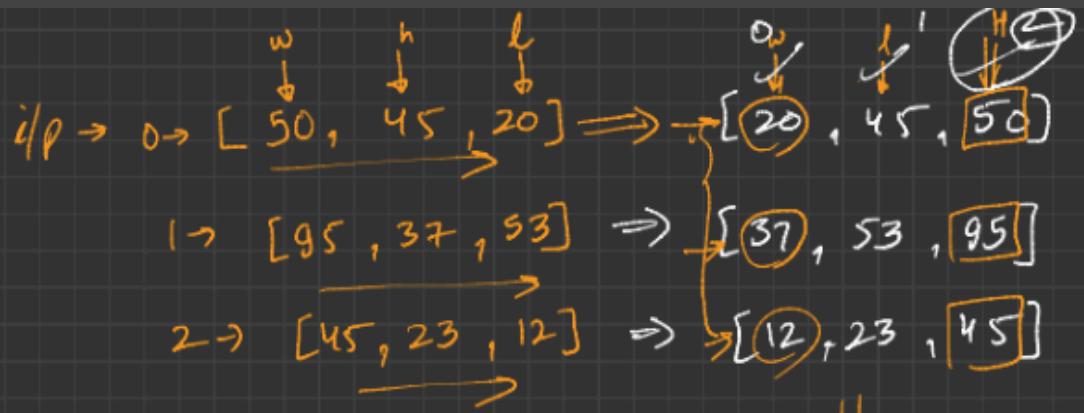
$\left[\frac{1}{8}, \frac{7}{8}, \frac{9}{8} \right]$

$\text{len} \rightarrow \text{arg}$
 \downarrow
length Inc Sub
length

Maximum Height By Stacking Cuboids Space Optimization Approach:

i/p \rightarrow n cuboids

Wintertide

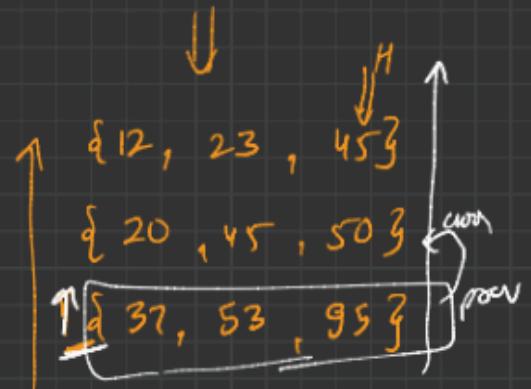


Algo:-

① sort all dimension for every cuboid

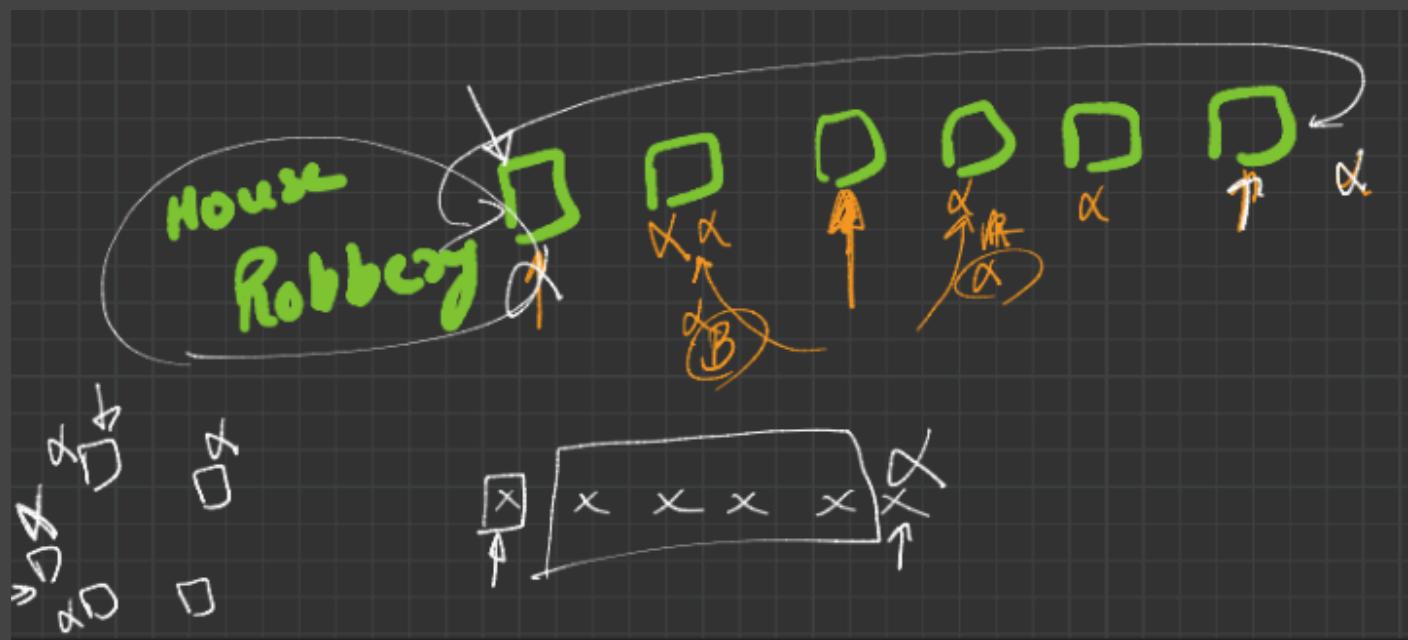
② sort all cuboids basis of w

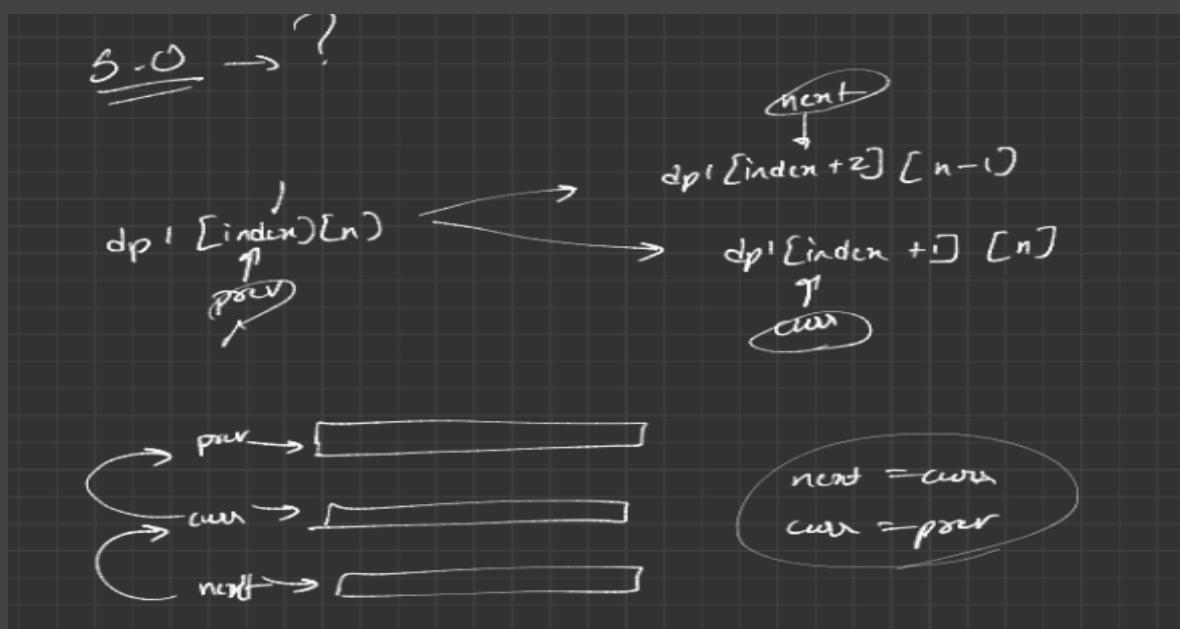
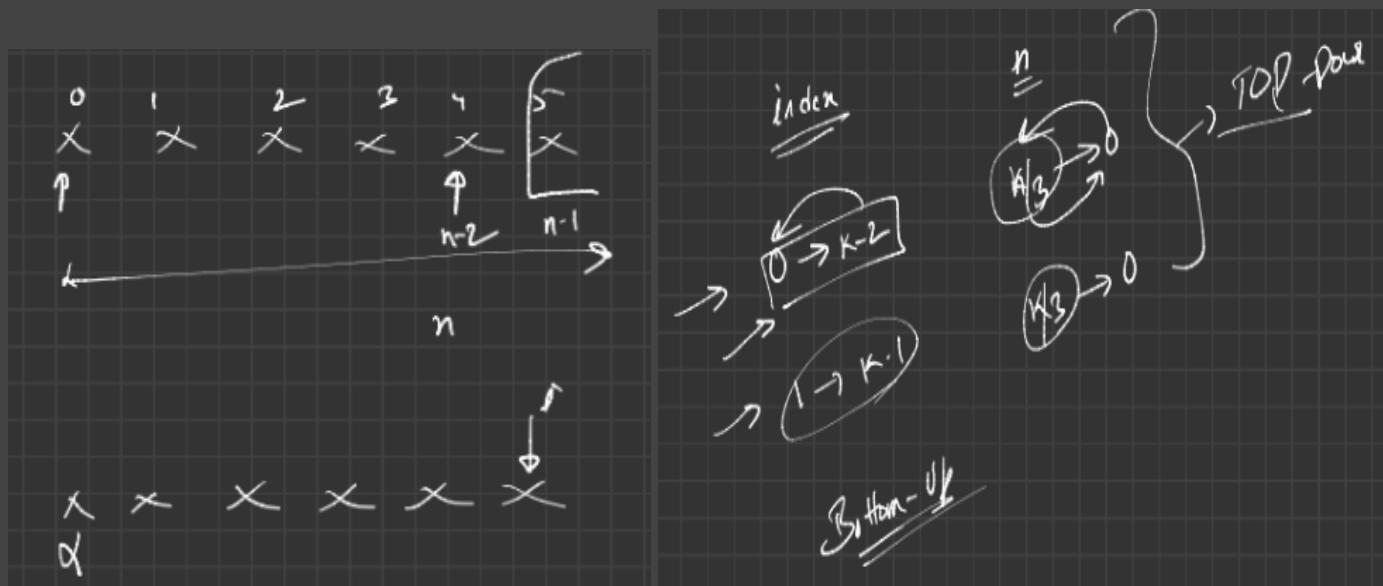
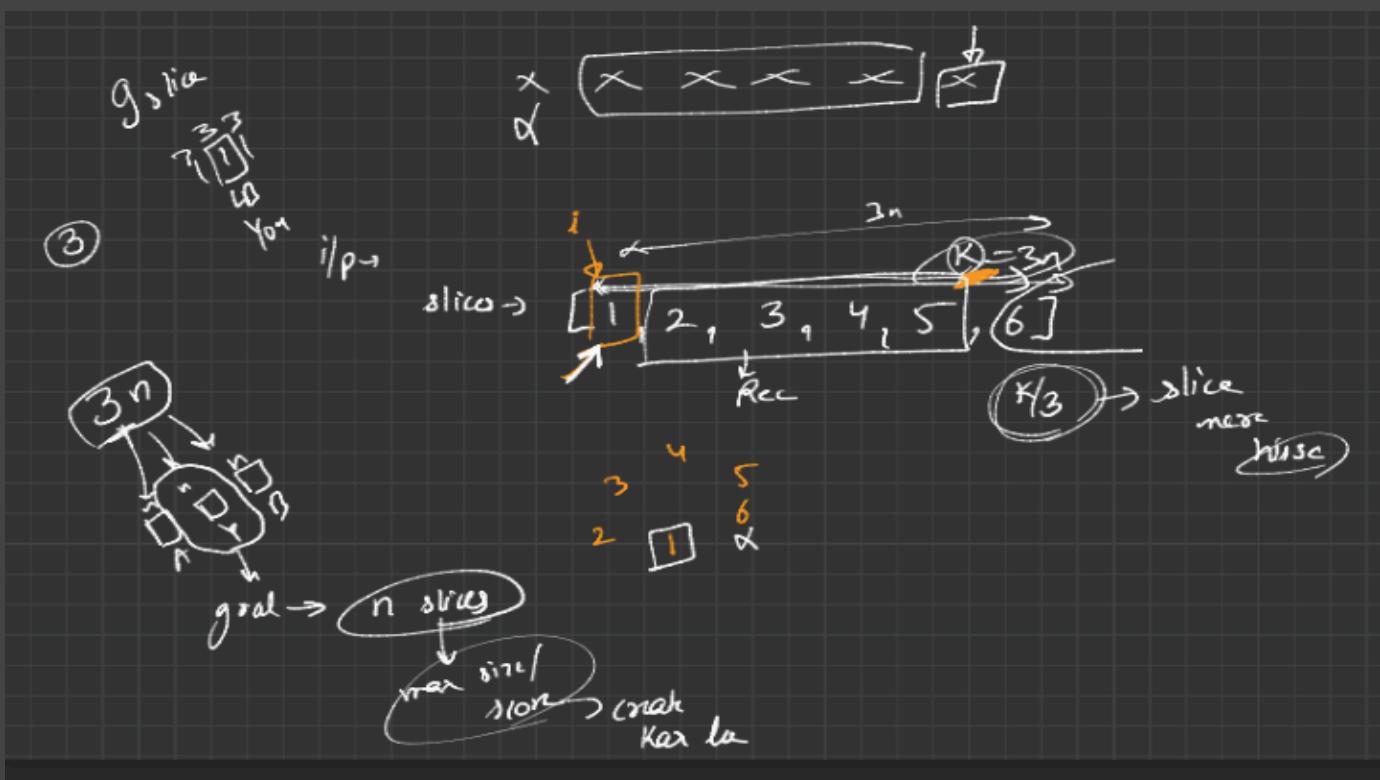
③ use logic of LIS problem



Pizza With 3n Slices Recursion / Top-Down Approach / Bottom-Up Approach /

Space Optimization Approach:





Number Of Dice Rolls With Target Sum Recursion / Top-Down Approach /

Bottom-Up Approach / Space Optimization Approach:

iP → / N → dice

M → faces

X → target sum

$$N = 3$$

$$M = 6$$

$$X = 12$$



$$\begin{matrix} D_1 \rightarrow 1 \\ D_2 \rightarrow 5 \\ D_3 \rightarrow 6 \end{matrix}$$

$$\begin{matrix} D_1 \rightarrow 1 \\ D_2 \rightarrow 6 \\ D_3 \rightarrow 5 \end{matrix}$$

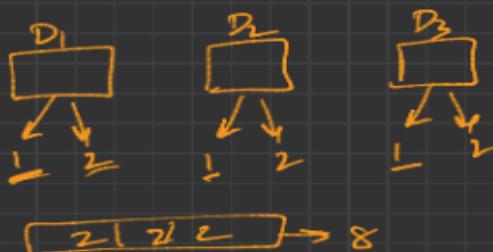
$$\begin{matrix} D_1 \rightarrow 2 & 2 \\ D_2 \rightarrow 4 & 5 \\ D_3 \rightarrow 6 & 5 \end{matrix} \quad \begin{matrix} 2 \\ 5 \\ 4 \end{matrix}$$

$$\boxed{6 \ 6 \ 6} \rightarrow 216$$

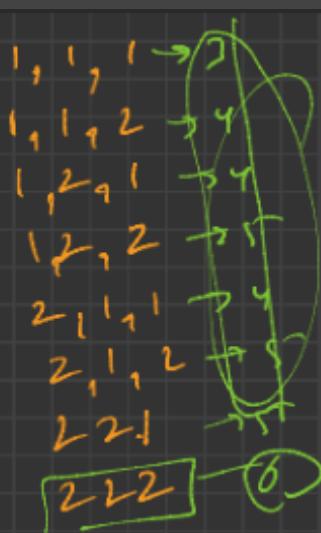
$$N = 3$$

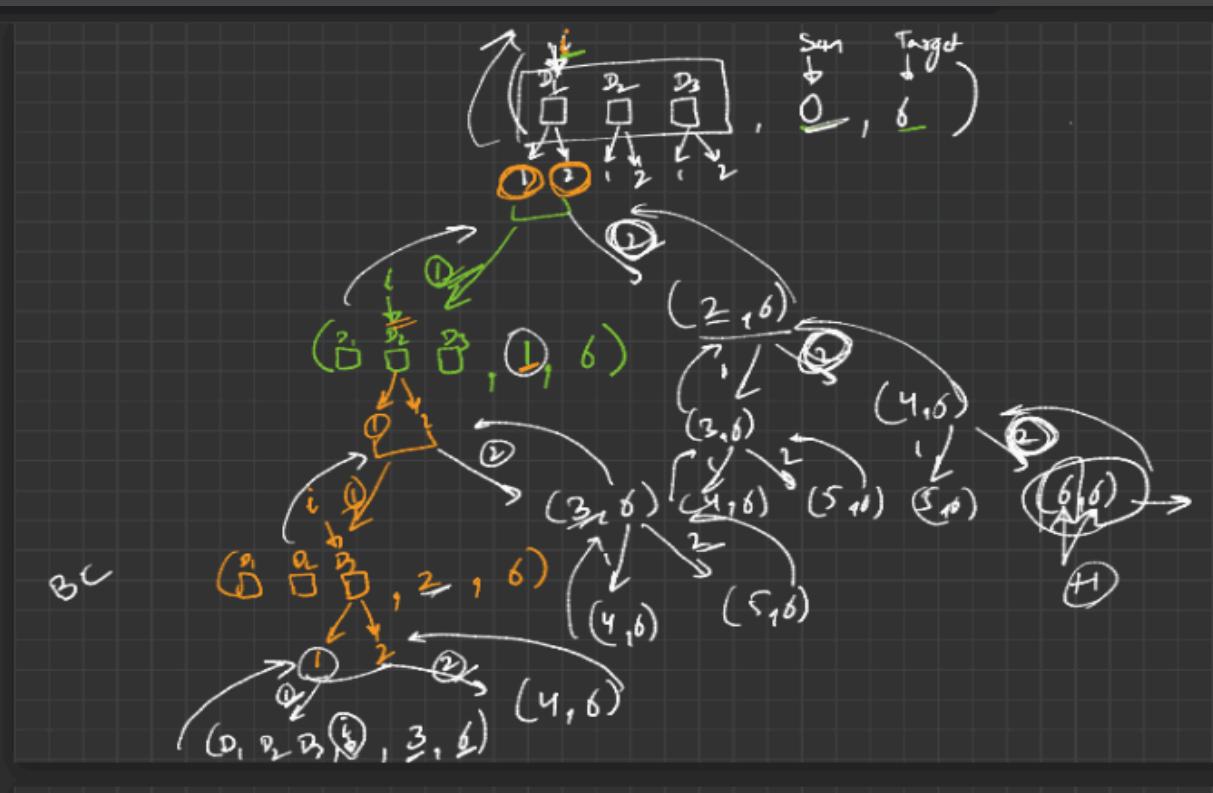
$$M = 2$$

$$X = 6$$



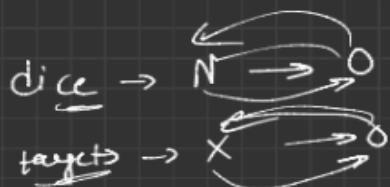
$$ans \rightarrow 1$$





Top Down

5-2



Bottom-up

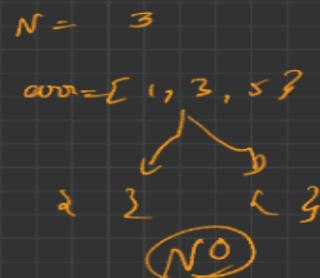
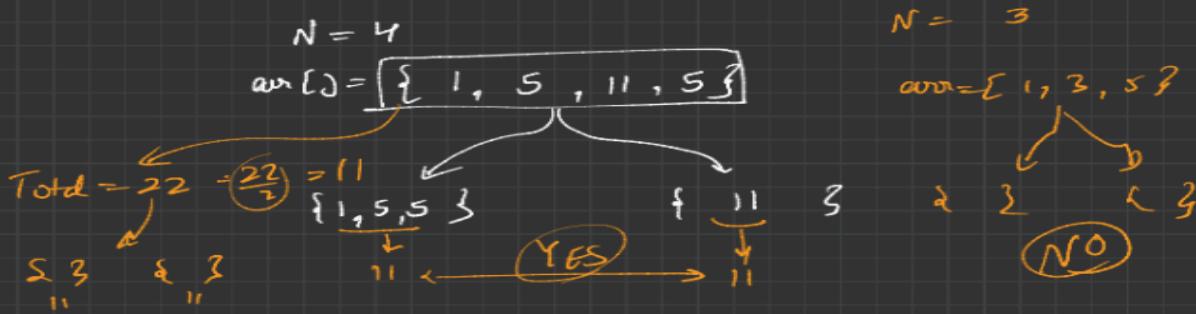
$$dp[\text{dice}] [\text{target}] \rightarrow dp[\underbrace{\text{dice} - i}_{\text{post}}] [\underbrace{\text{target} - i}_?]$$



Partition Equal Subset Sum By Recursion / Top-Down Approach / Bottom-Up

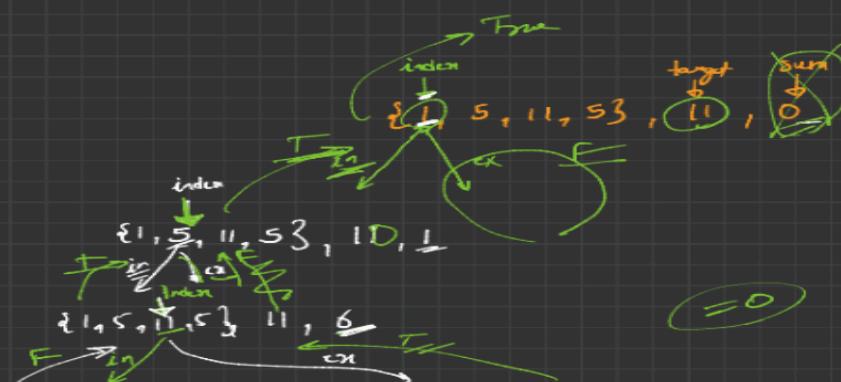
Approach / Space Optimization Approach:

→ Partition Equal Subsets Sum:-

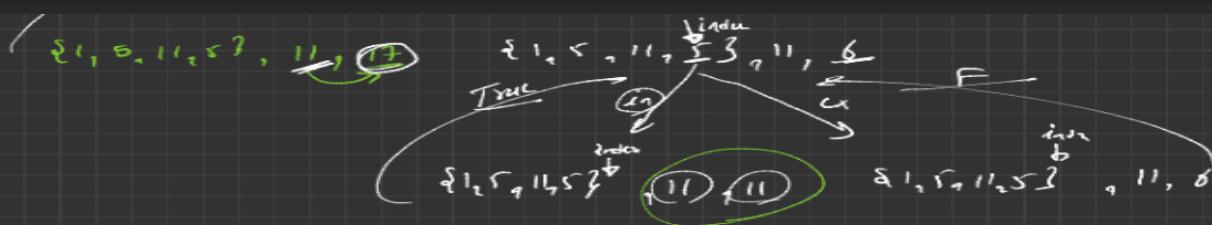


$$\text{Total} = 22 \rightarrow \text{Even}$$

$$\log x = \frac{22}{3} \approx 11$$



T or F



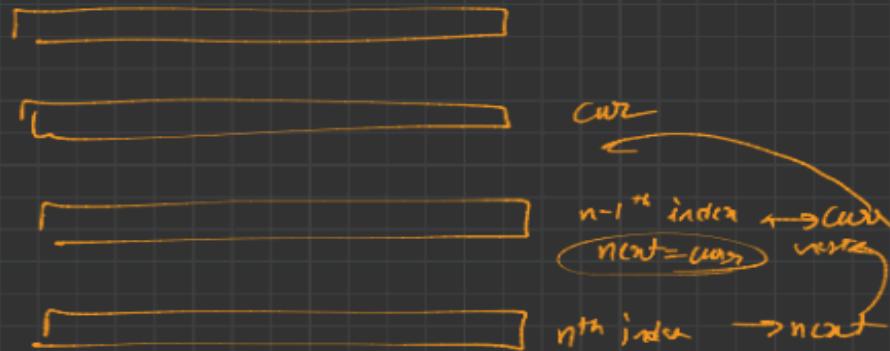
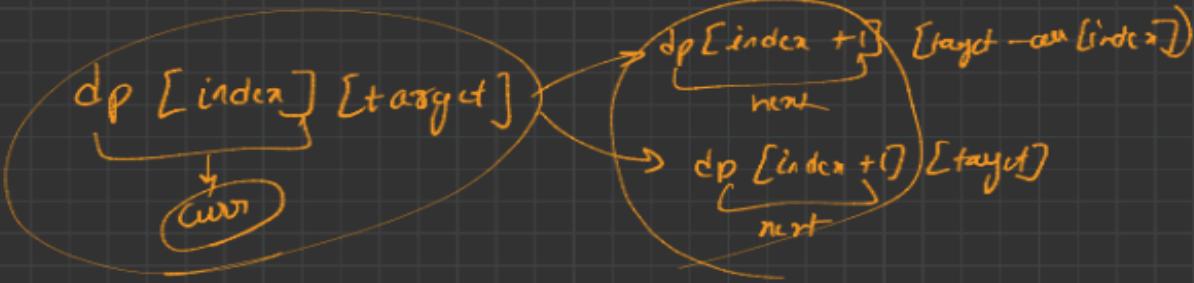
Top Down

```

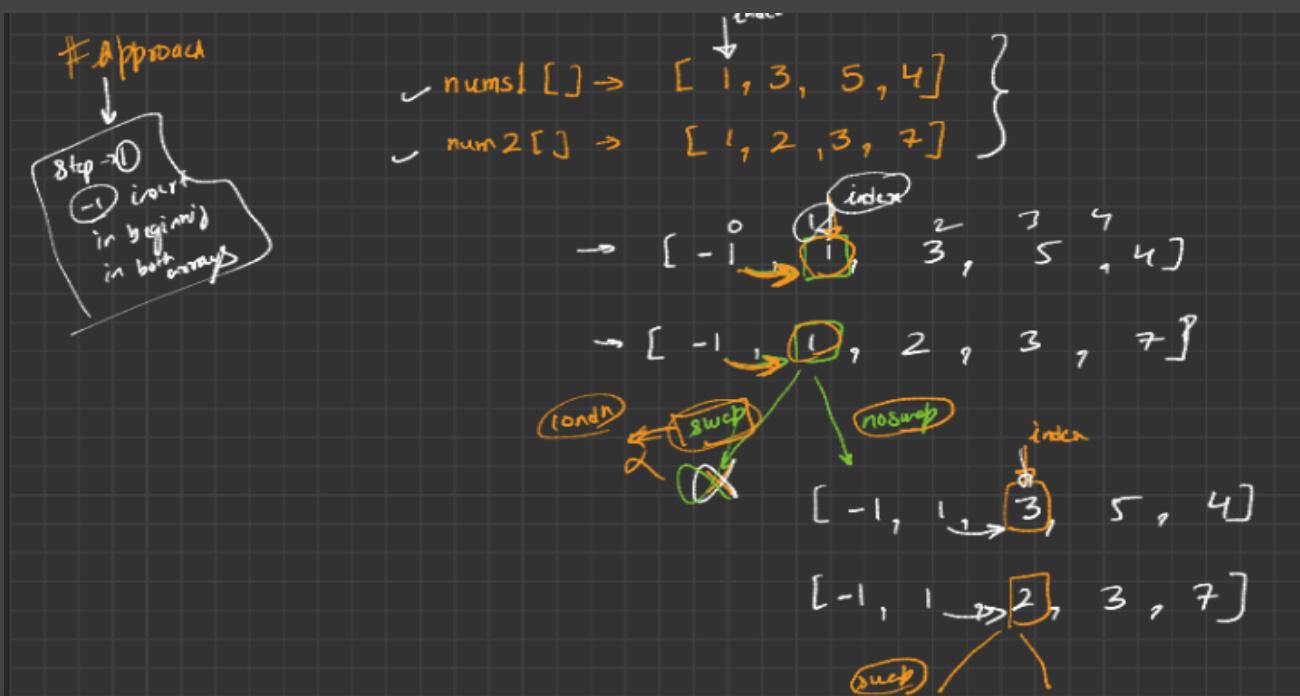
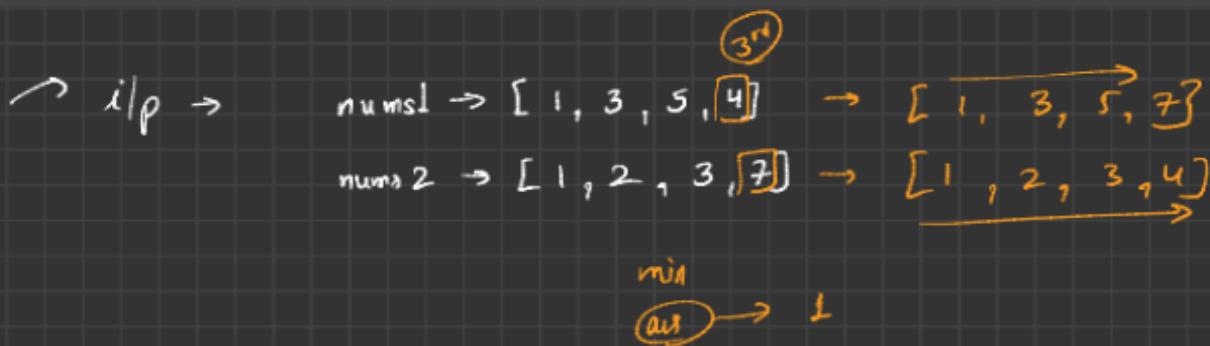
graph LR
    index[index] --> 0_1[0]
    target[target] --> 0_2[0]
    total["total/2"] --> 0_3[0]
    N[N] --> 0_4[0]
    0_1 <--> 0_2
    0_1 <--> 0_3
    0_1 <--> 0_4
  
```

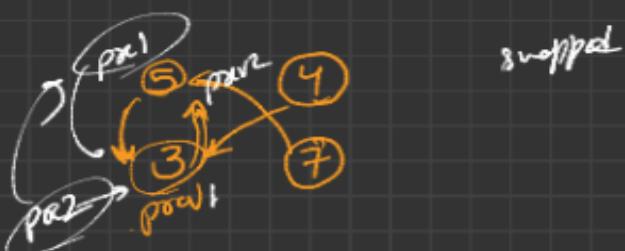
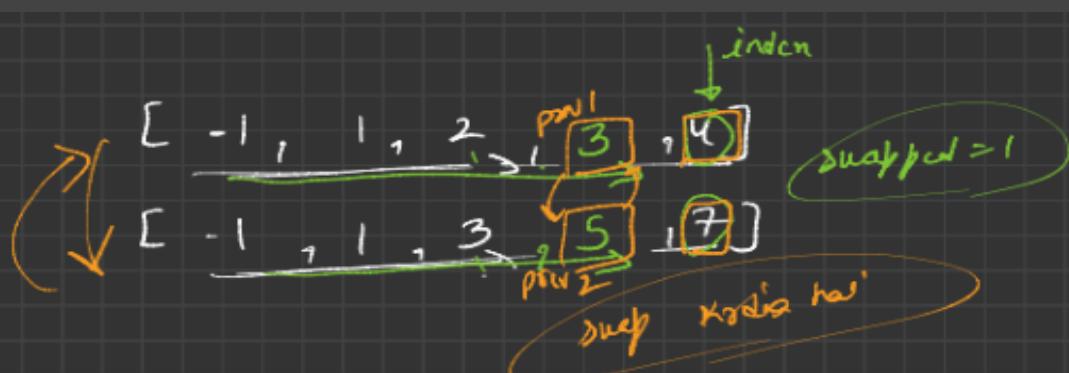
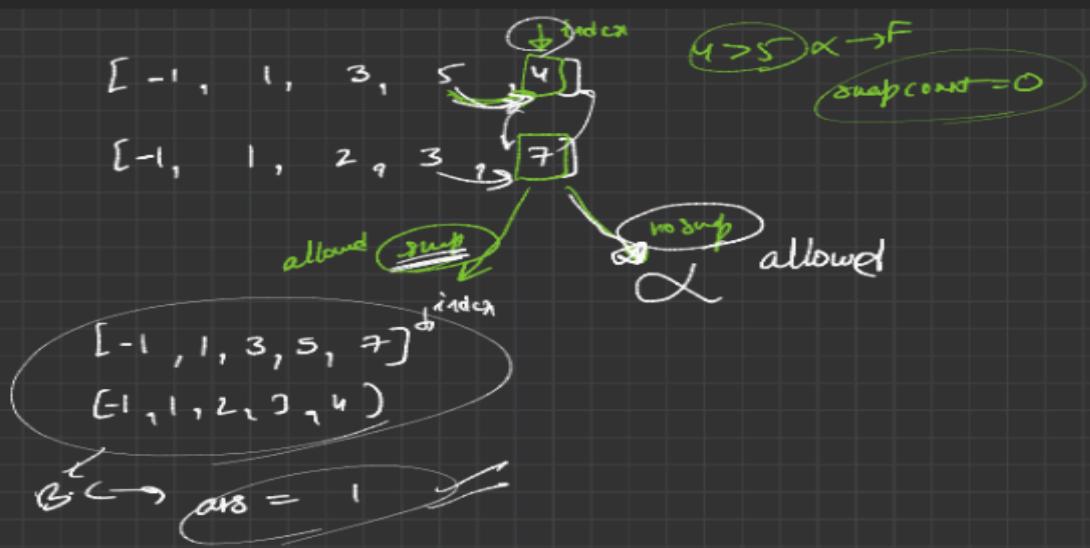
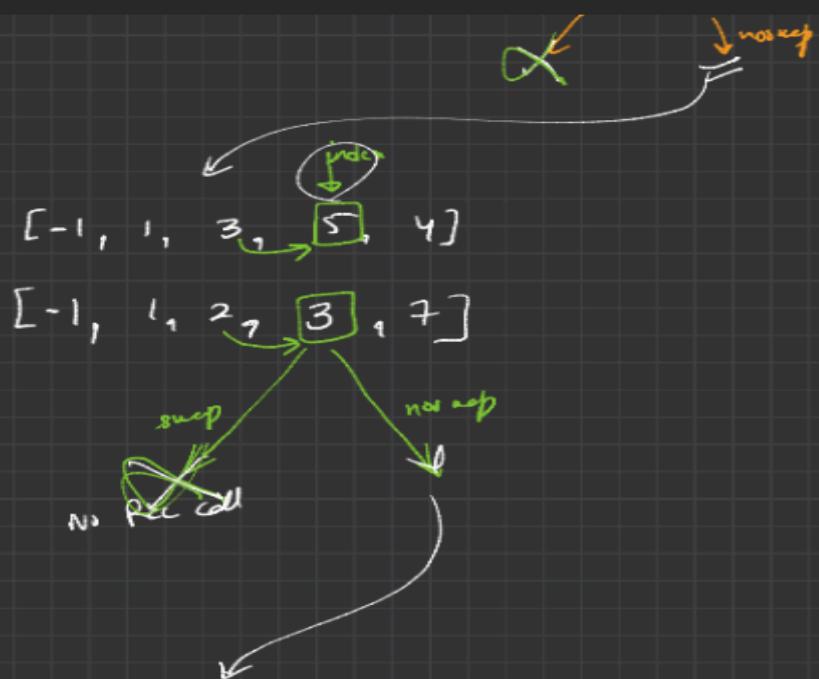
Bottom-up

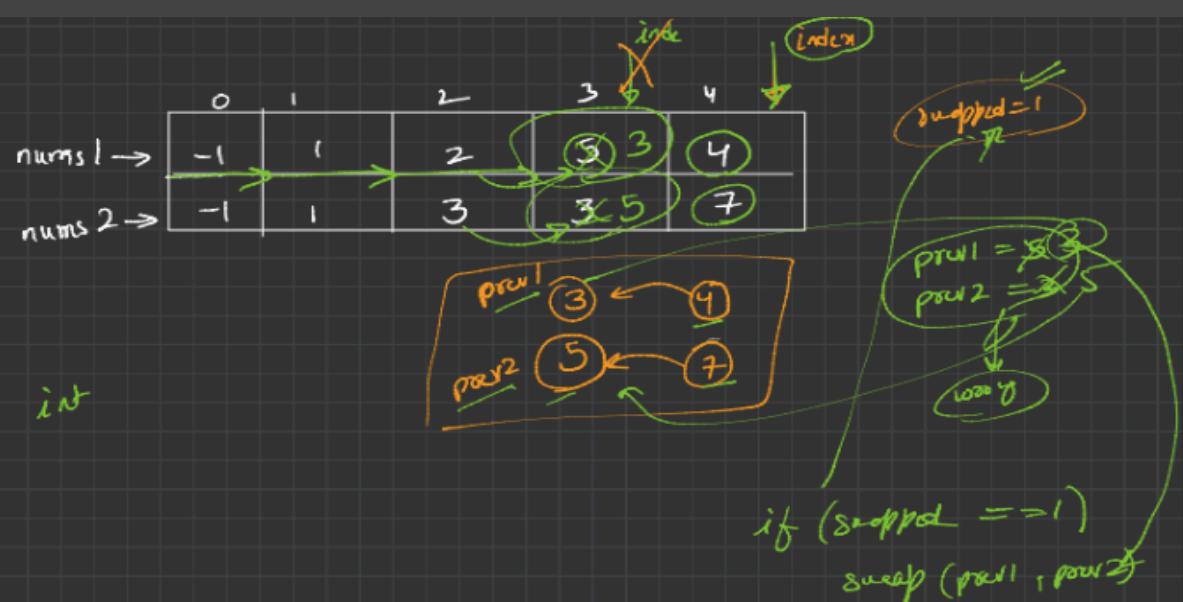
50 ⇒ ?



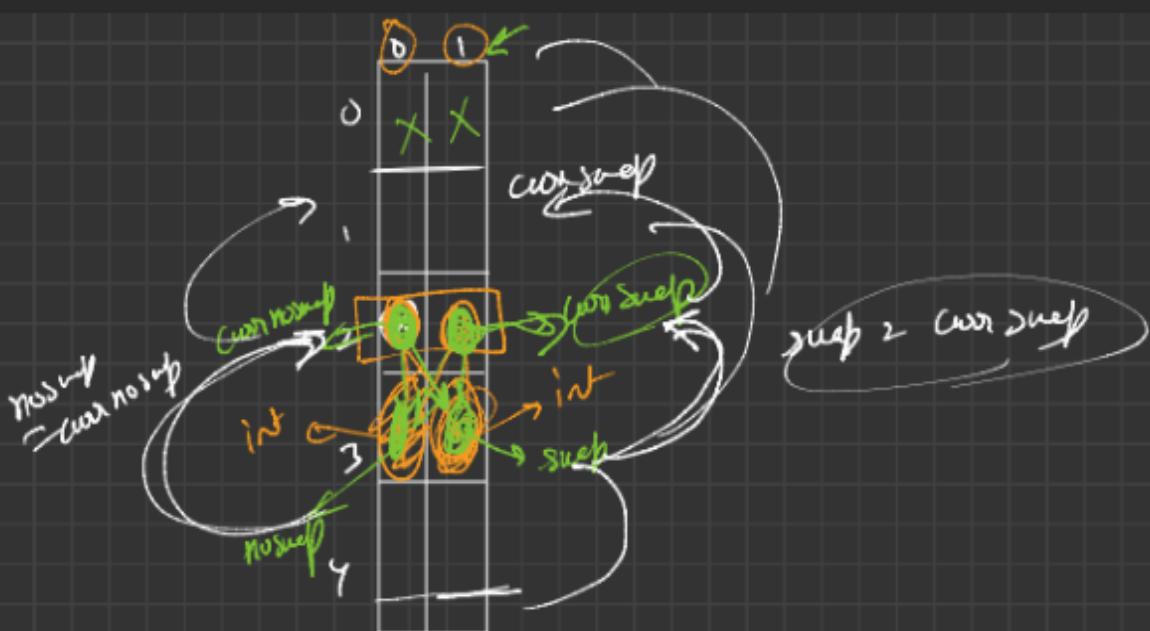
Minimum Swaps To Make Subsequence Increasing By Recursion / Top-Down Approach / Bottom-Up Approach / Space Optimization Approach:





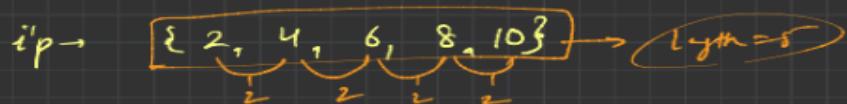
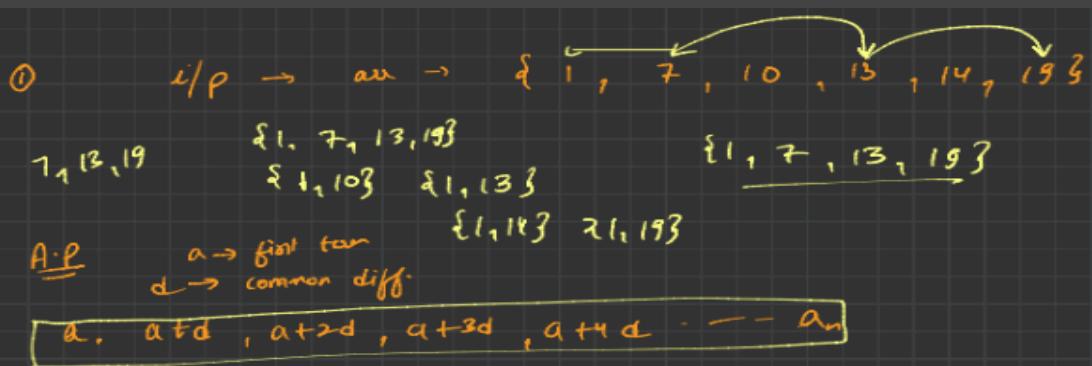


The diagram illustrates the state transition in a dynamic programming solution. It shows two arrows originating from the same node labeled $dp[\underline{\text{index}}][\underline{\text{swapped}}]$. One arrow points to a node labeled $dp[\underline{\text{index}} + 1][0]$, and another arrow points to a node labeled $dp[\underline{\text{index}} + 1][1]$.

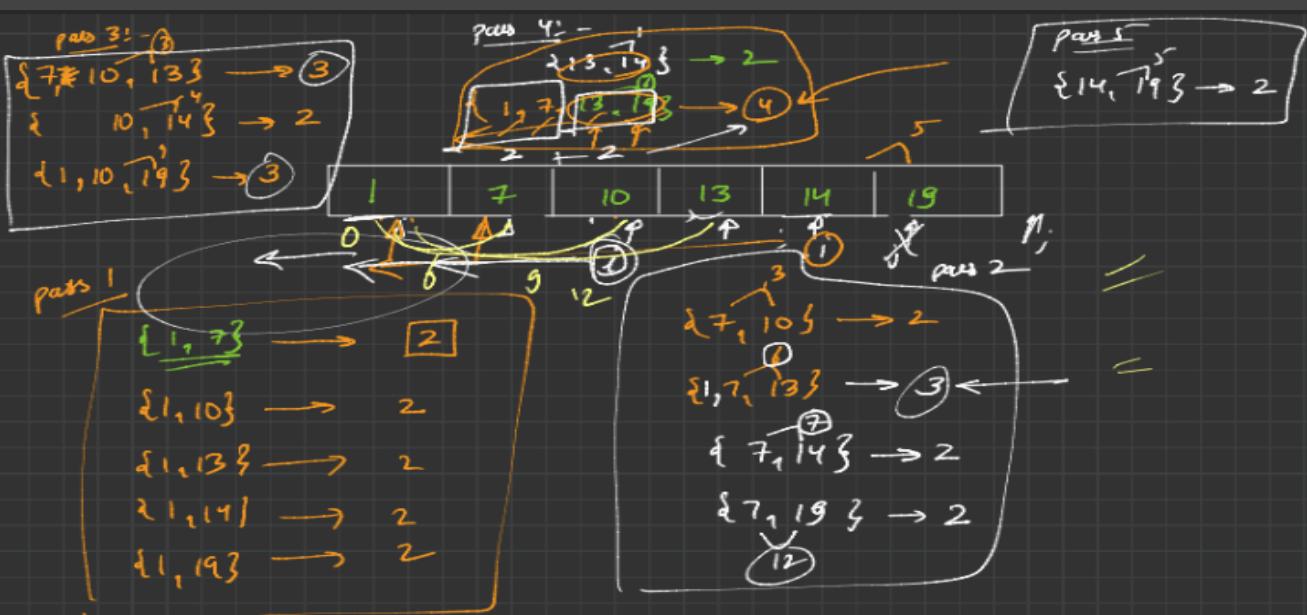
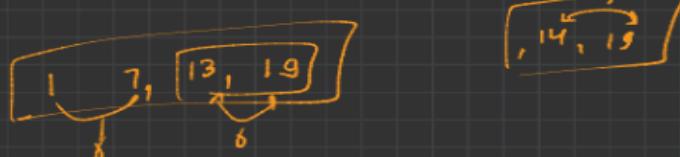
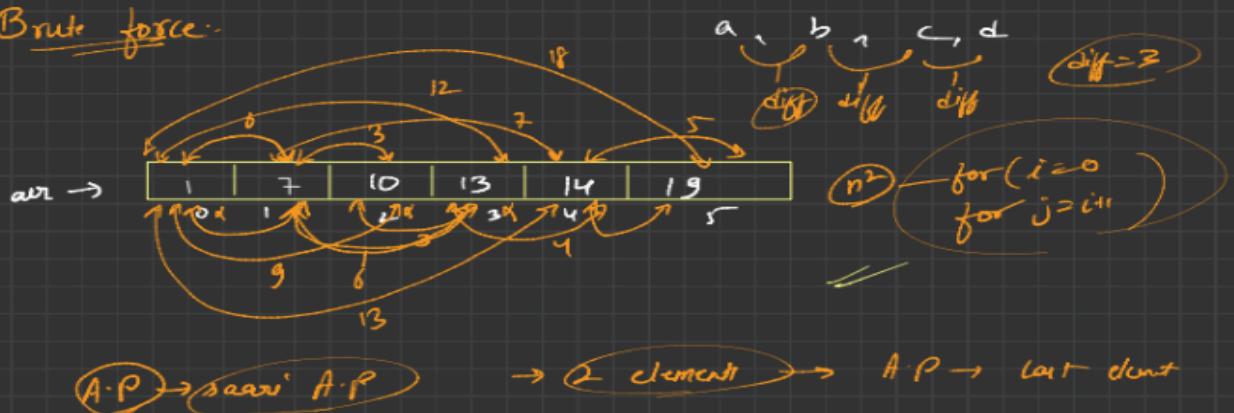


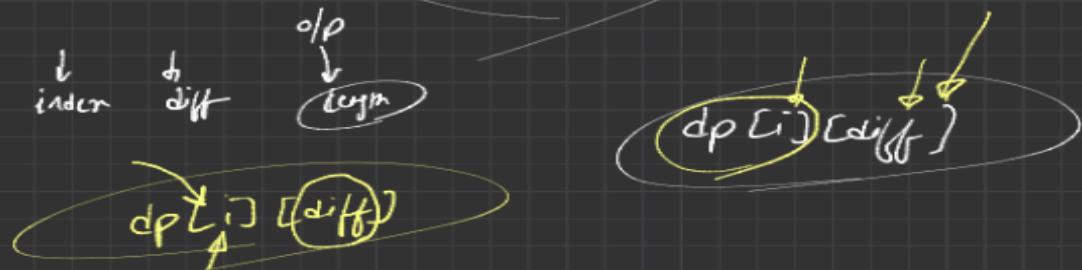
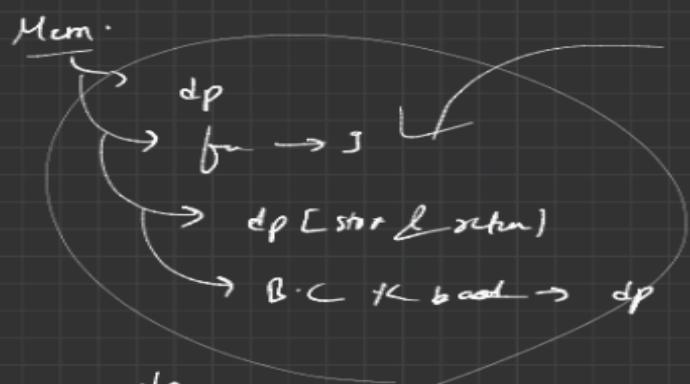
Longest Arithmetic Subsequence And Russian Dolls Increasing By Recursion /

Top-Down Approach / Bottom-Up Approach:



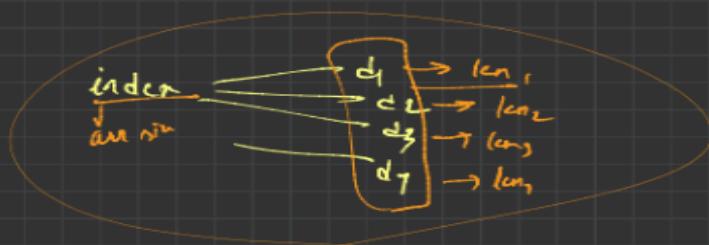
Brute force..



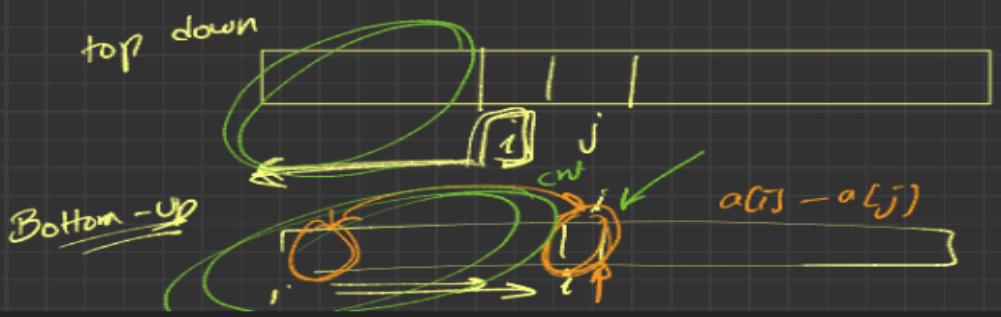
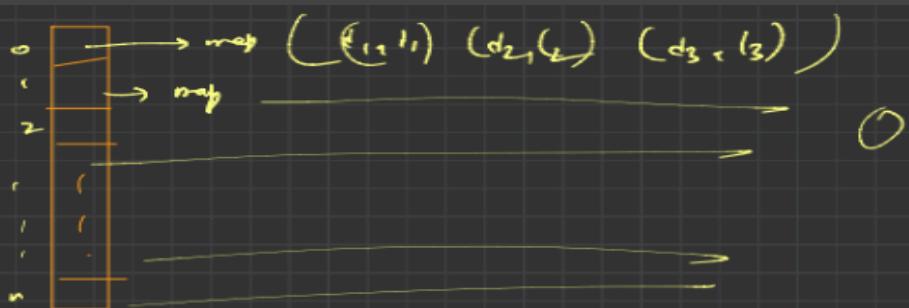


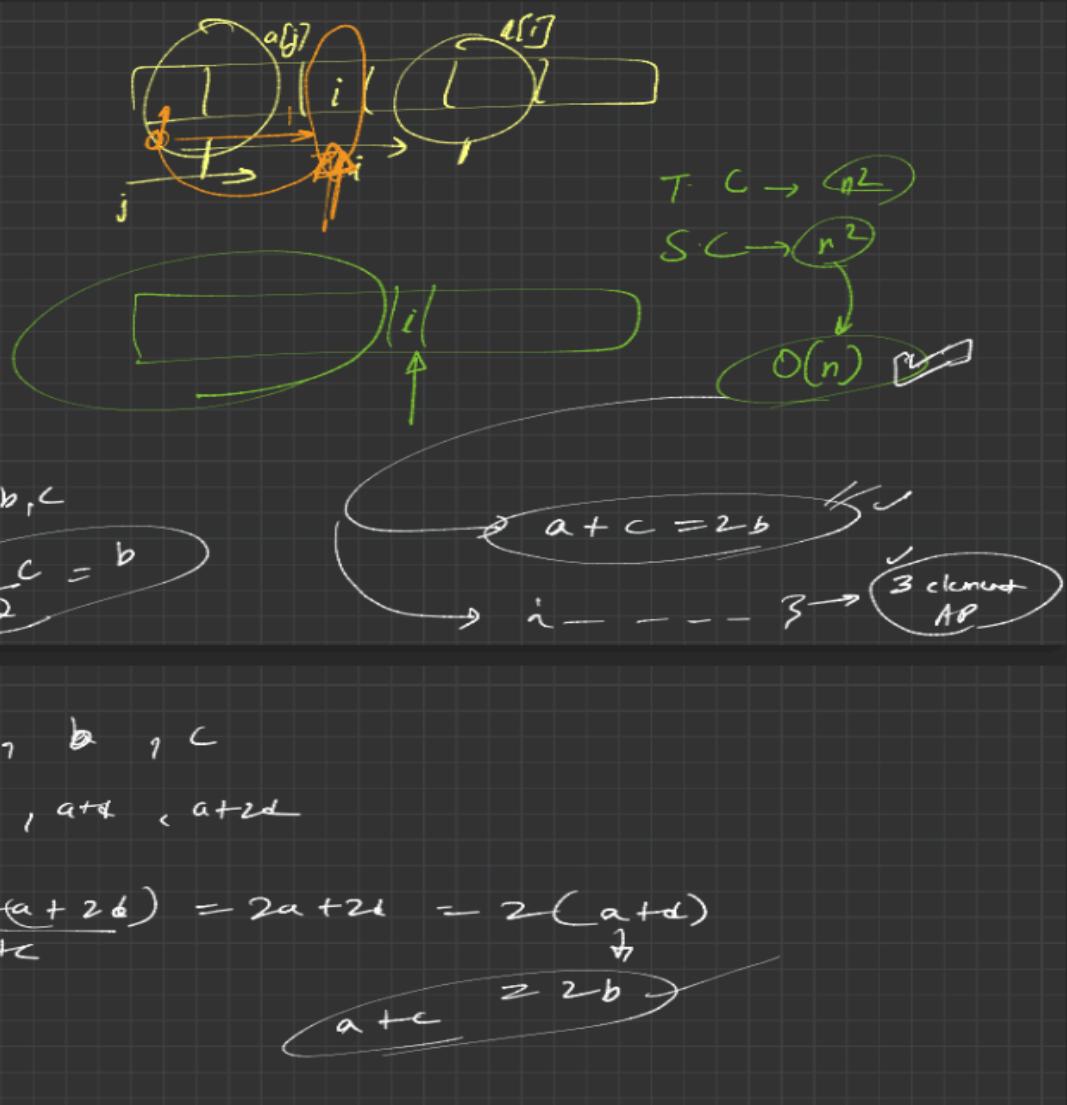
index < arr.size

dp [len+1]

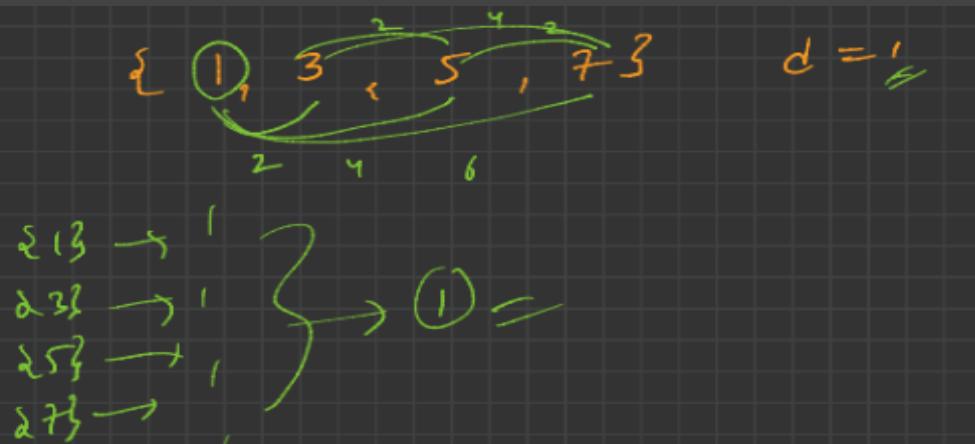
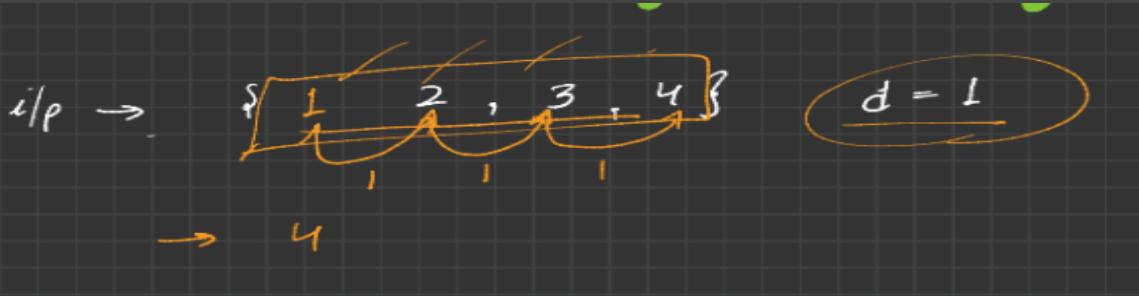


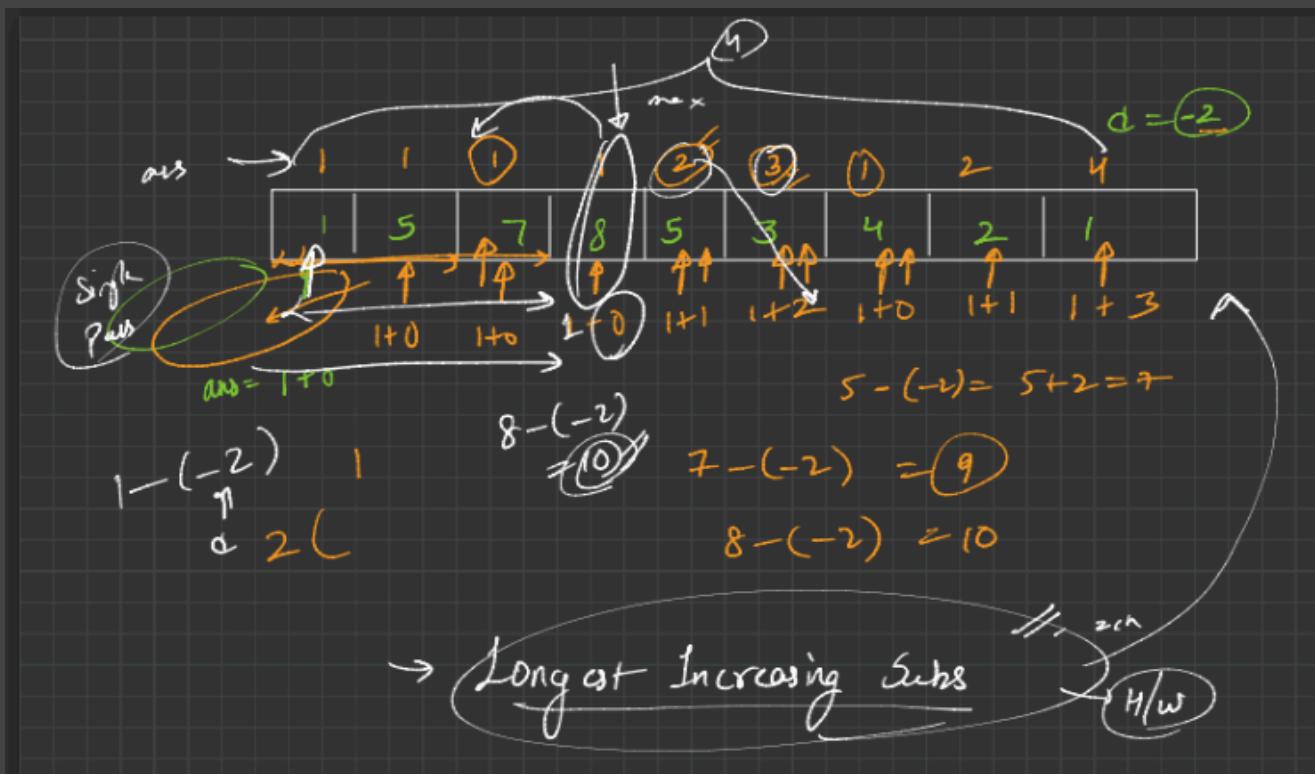
unordered_map<int, int> dp[1000000]



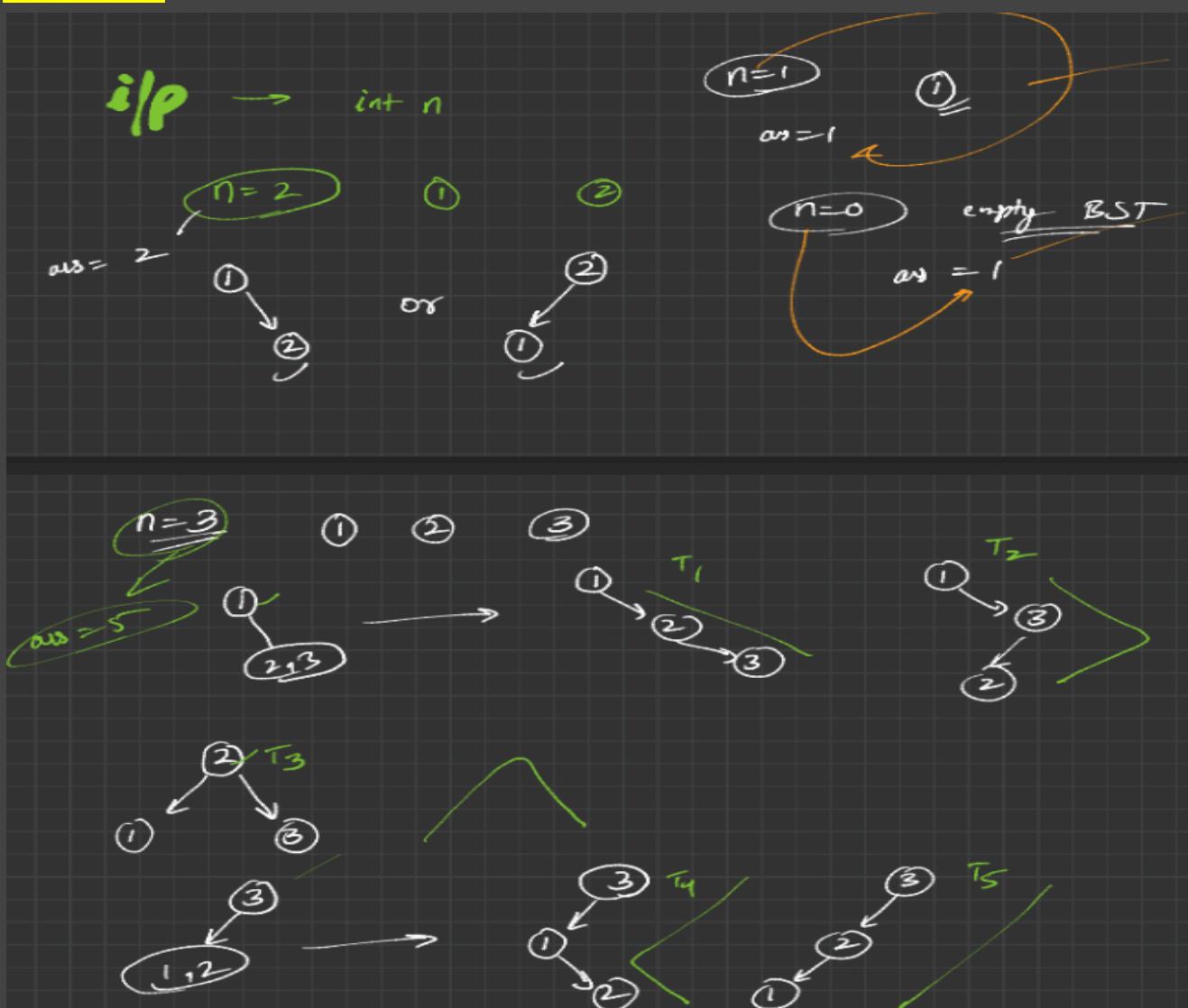


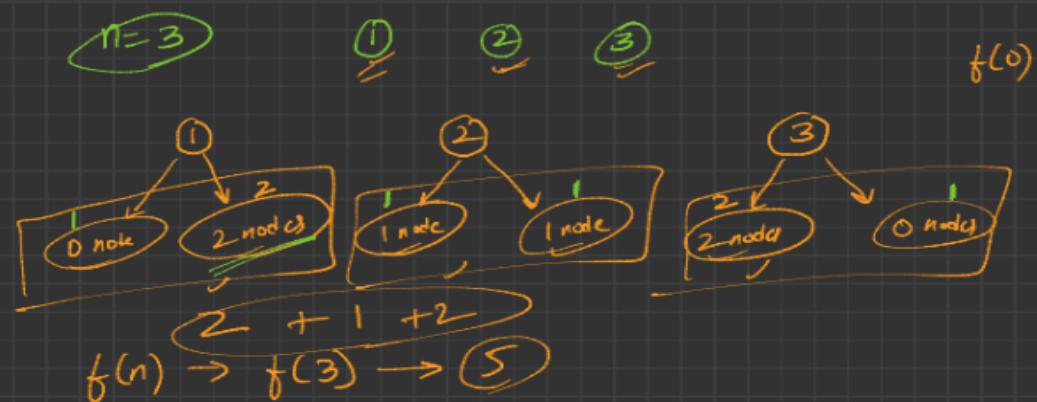
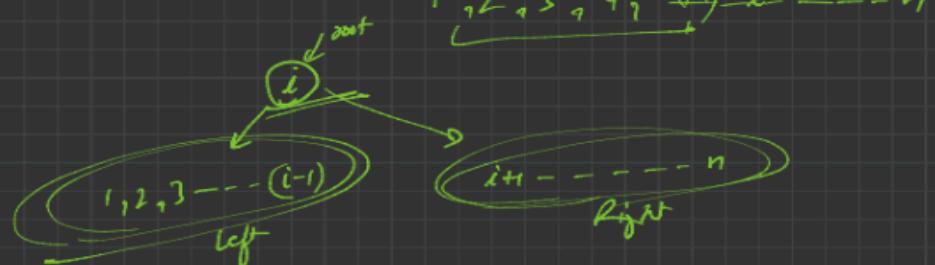
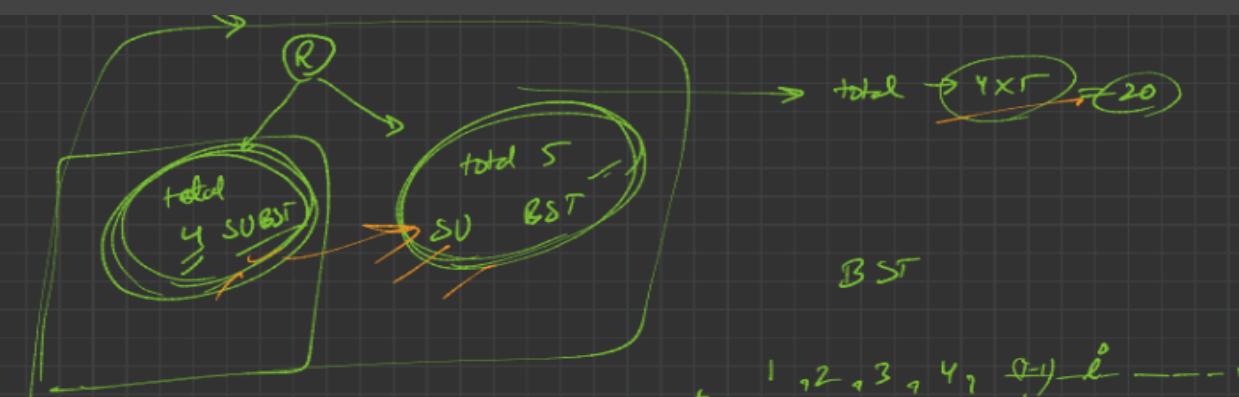
Longest AP With Given Difference(d) By Recursion / Top-Down Approach / Bottom-Up Approach / Space Optimization Approach:





Unique Binary Search Tree By Recursion / Top-Down Approach / Bottom-Up Approach:





n nodos

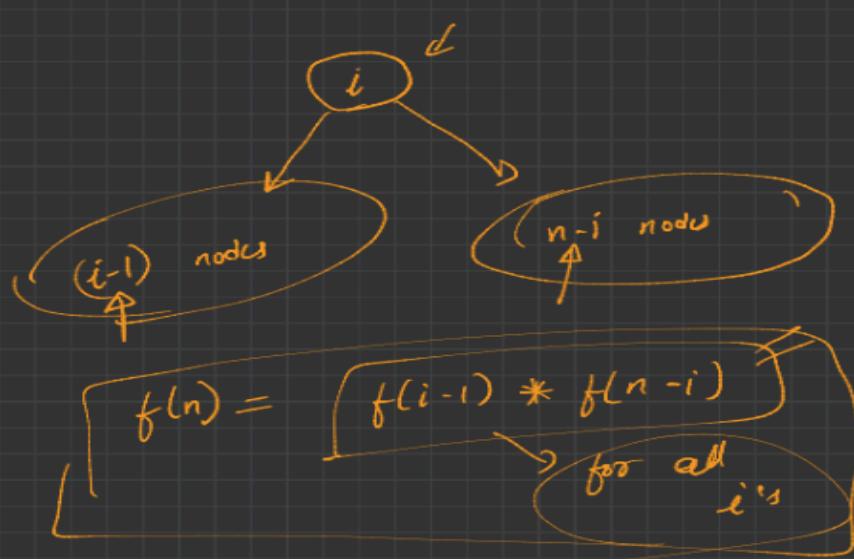
1 \rightarrow Root

2 \rightarrow Root

3 \rightarrow Root

i \rightarrow Root

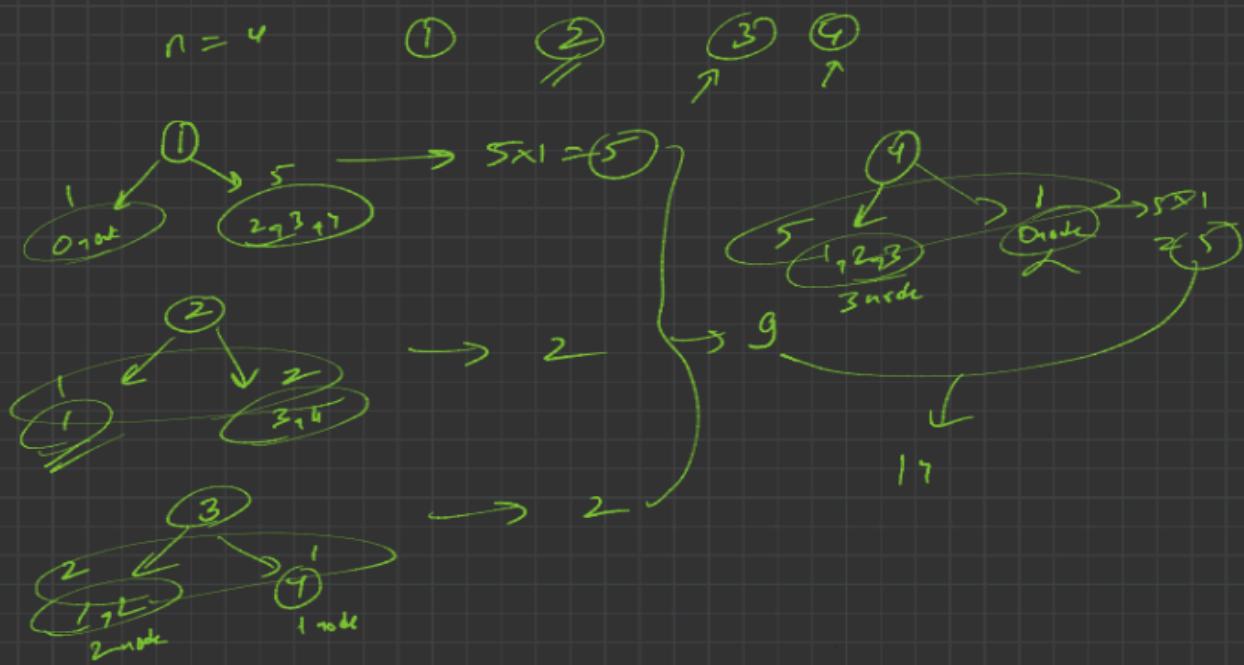
n \rightarrow Root



$$f(n) = \sum_{i=1}^n f(i-1) * f(n-i)$$

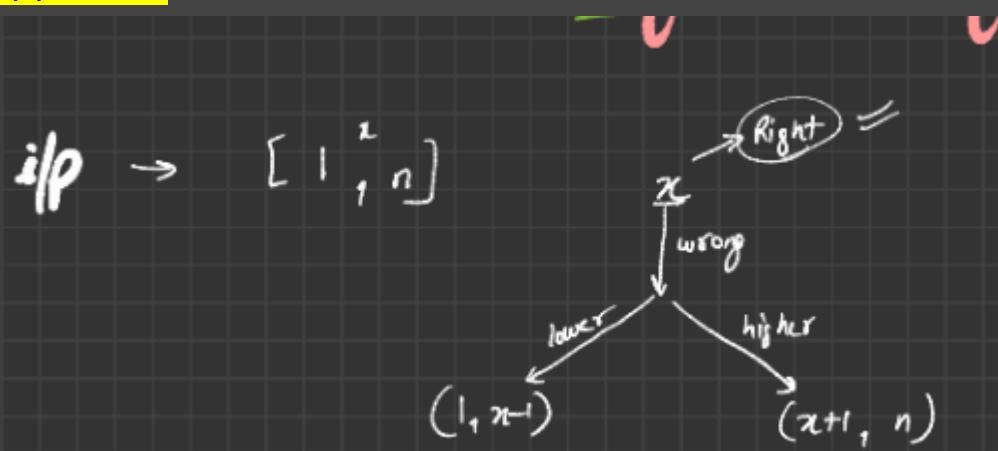
$n=0 \rightarrow 1$
 $n=1 \rightarrow 1$
 $n=2 \rightarrow 2$
 $n=3 \rightarrow 5$
 $n=4 \rightarrow 14$

Catalan numbers

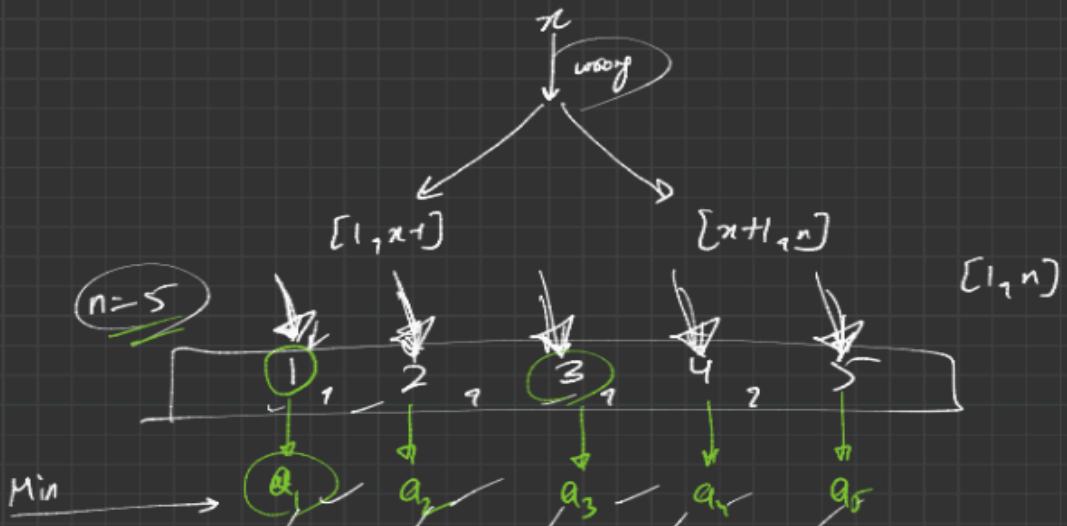


Guess Number Higher Or Lower By Recursion / Top-Down Approach / Bottom-Up

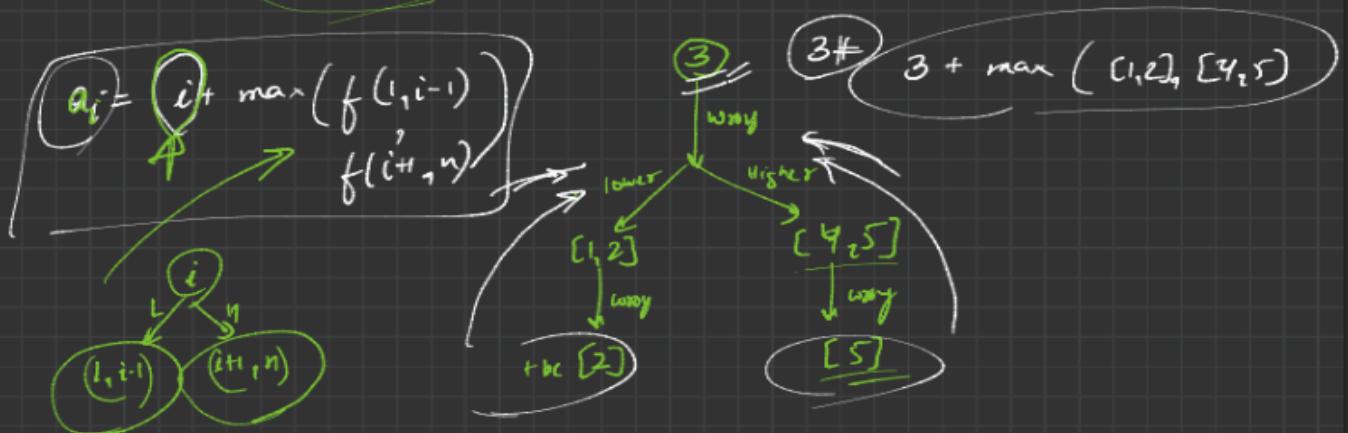
Approach:



$$\underline{[1, n]}$$

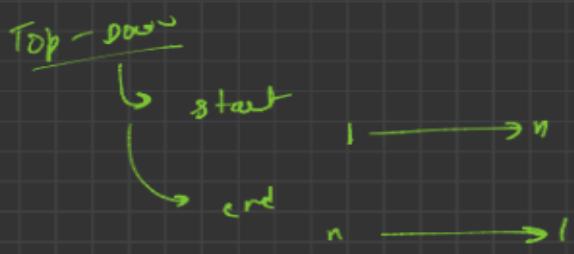


$a_i \rightarrow ?$

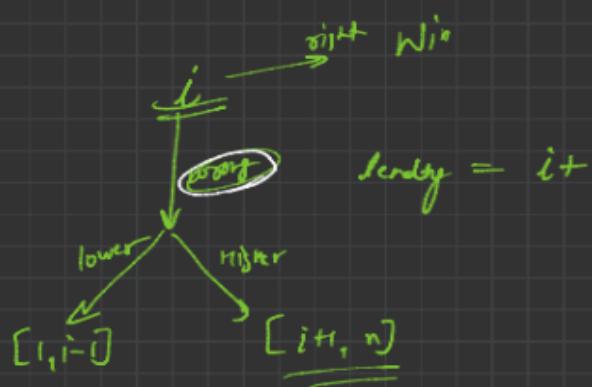
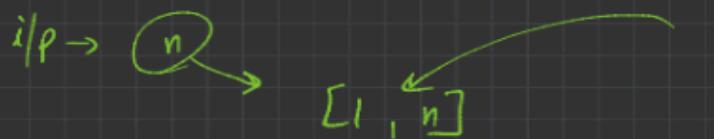


```
for (int i=start ; i<=end ; i++)
{
    ans = min(ans, i + max(f([1, i-1]), f([i+1, n])));
}
```

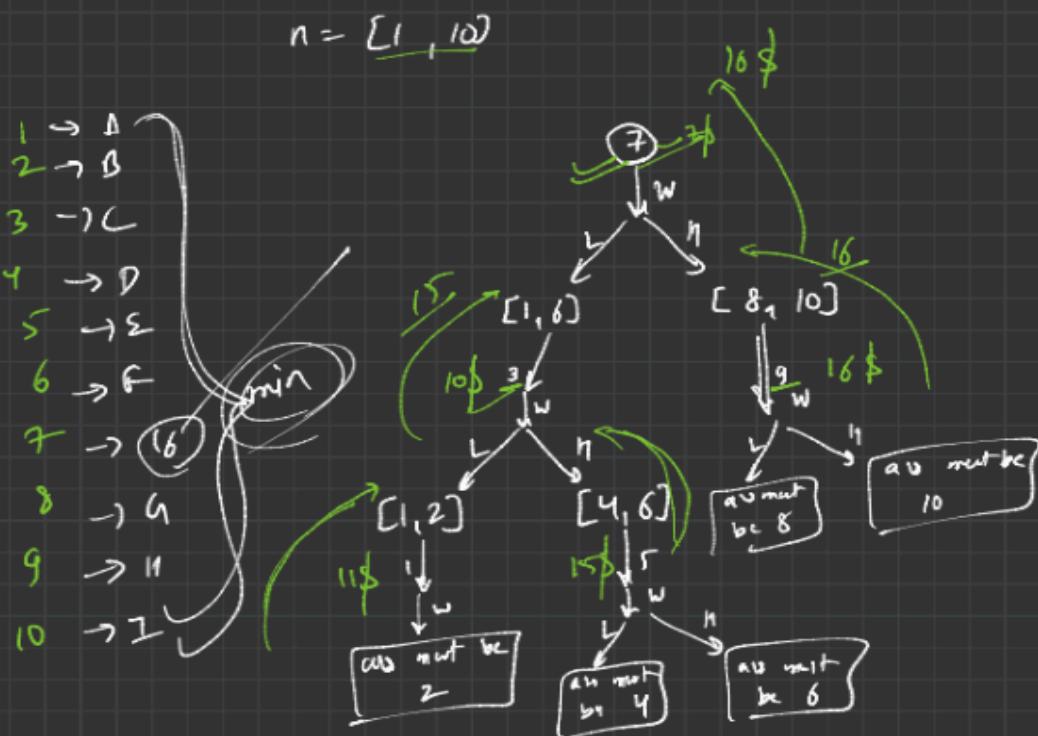
R.R



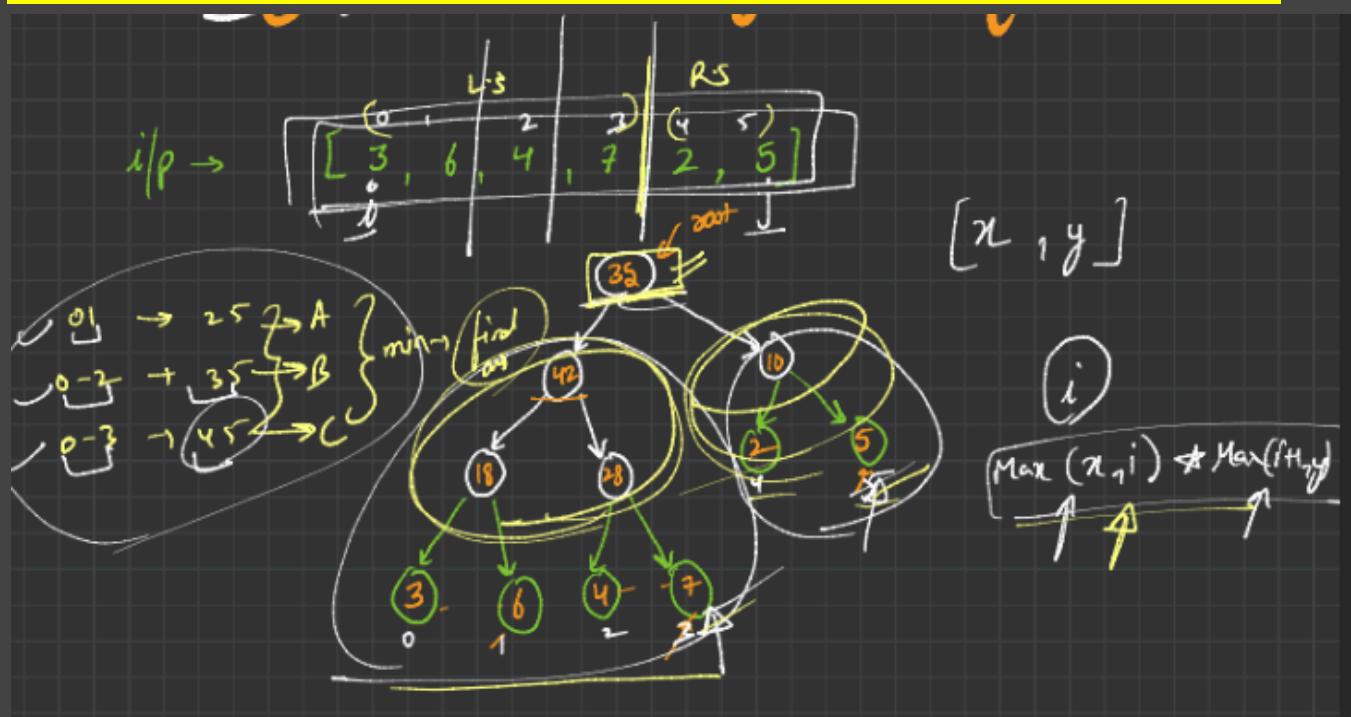
Bottom UP



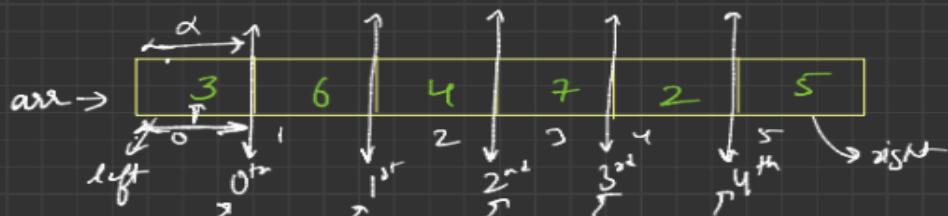
$dp(i, j) \rightarrow$ min amount of money req to win
for range $[i, j]$



Minimum Cost Tree From Leaf Values By Recursion / Top-Down Approach:



$$f(i, j) = \min \left[\frac{\max(i, k) * \max(k+1, j)}{f(i, k) + f(k+1, j)} \right]$$



$$f(left, right)$$

$$f(0, 5) \rightarrow \text{for (int } k=\text{left}; \ k < \text{right}; \ k++)$$

\downarrow

$k=0$

$$\rightarrow \frac{\max(0, 0) * \max(1, 5)}{f(0, 0) + f(1, 5)}$$

\downarrow

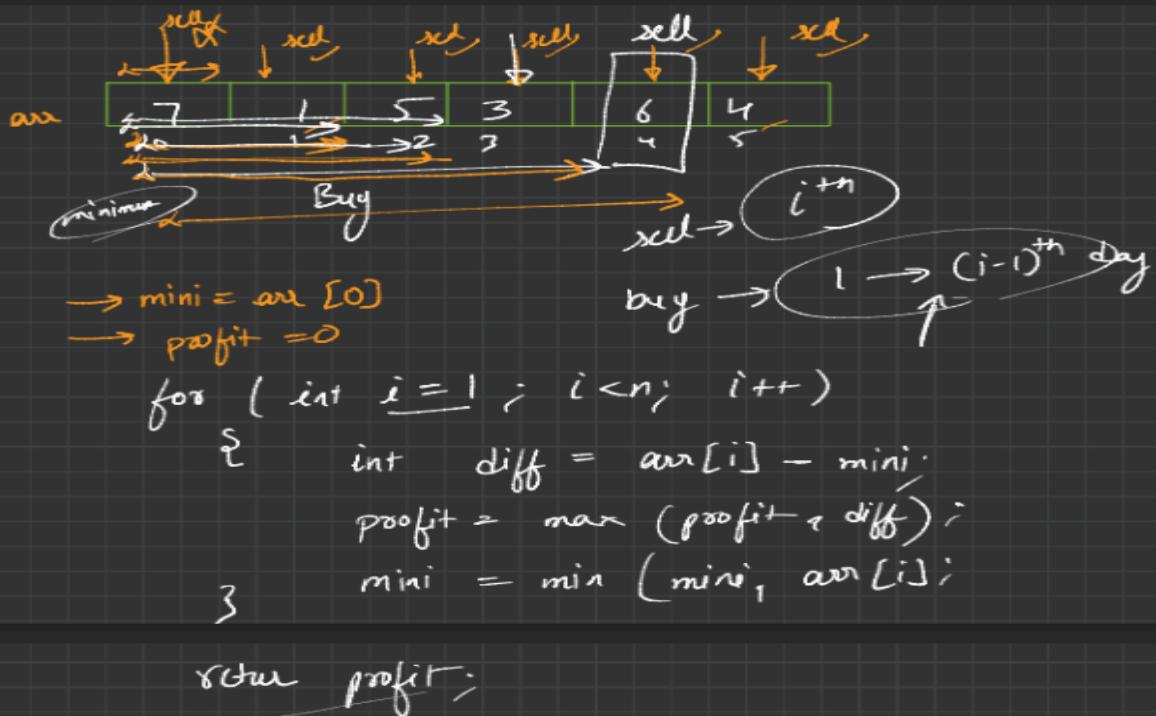
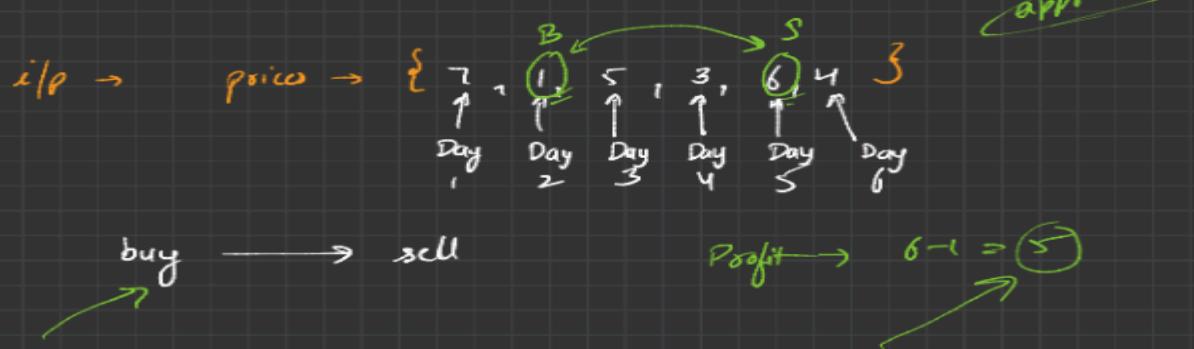
$$\rightarrow 3 * 7 + \boxed{}$$

$$O(n)$$

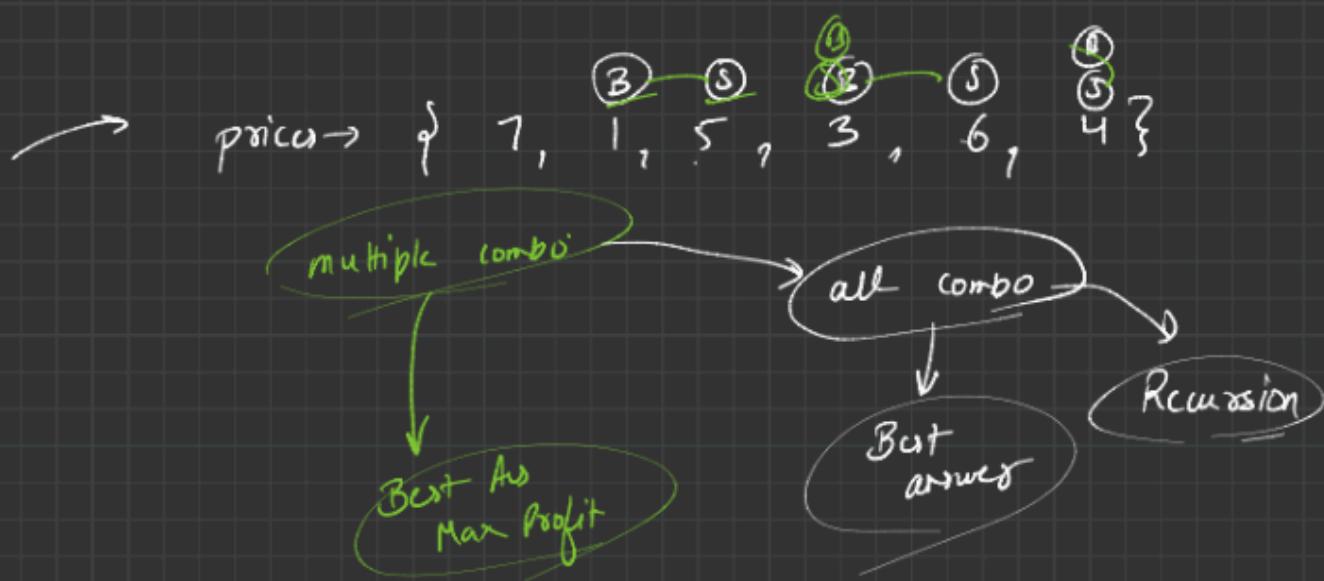
\rightarrow

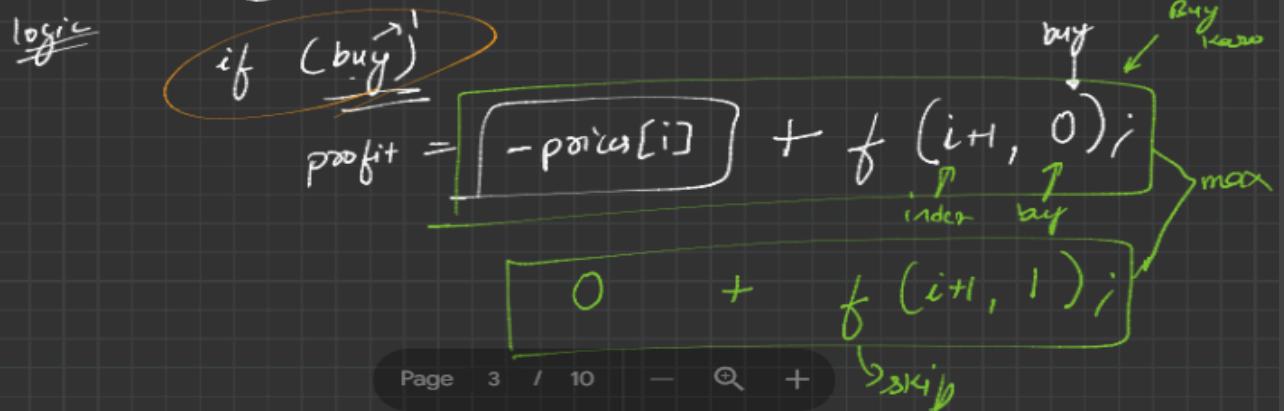
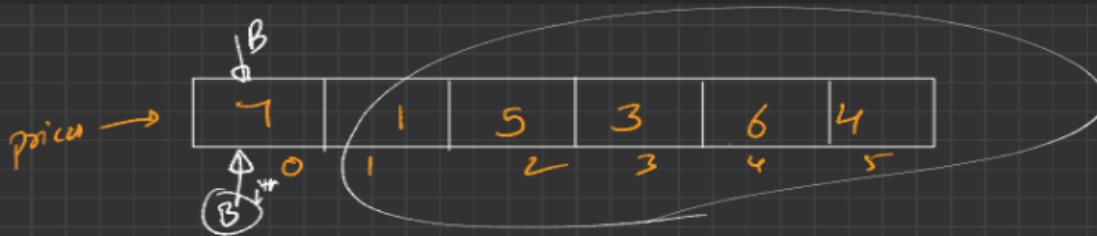
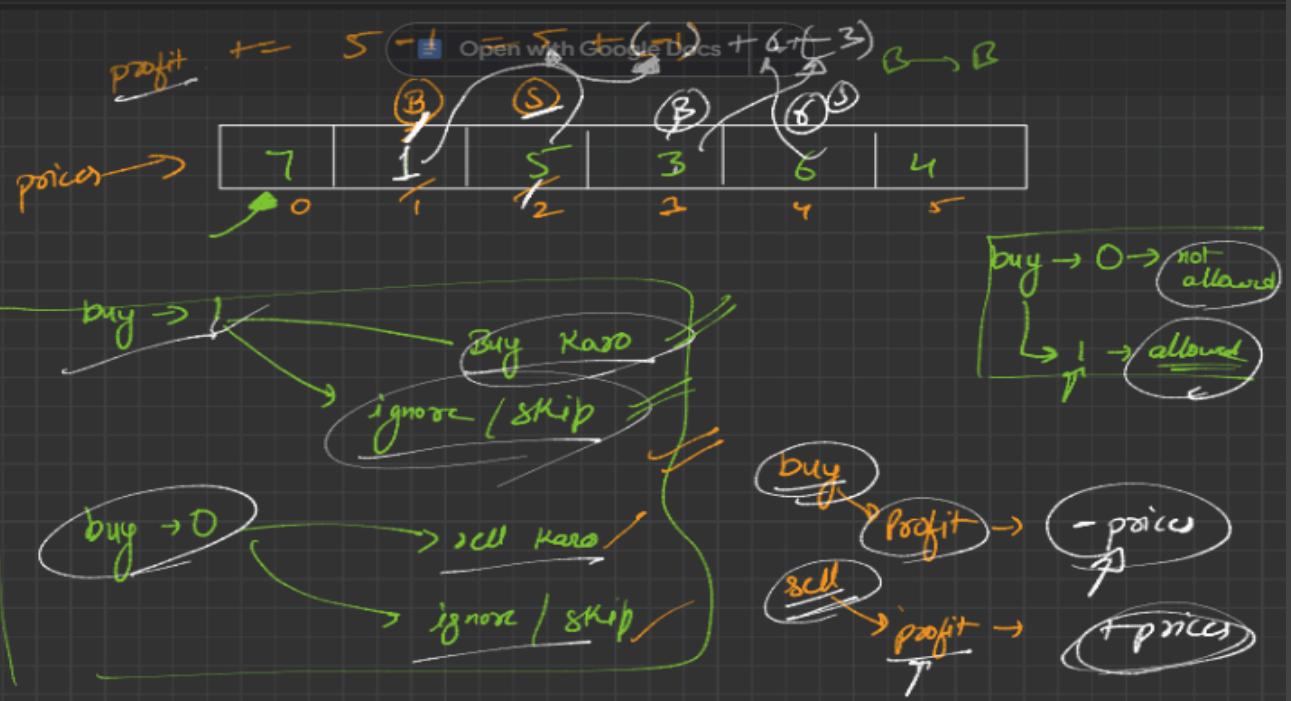
$k=1 \rightarrow$	$a_{0,1}$	$a_{0,2}$	\vdots	\rightarrow	$O(n^3)$
$k=2 \rightarrow$	$a_{0,3}$	$a_{0,4}$	\vdots	\rightarrow	\min
$k=3 \rightarrow$	$a_{0,5}$				
$l=4$					

Buy And Sell Part-I:



Buy And Sell Part-II By Recursion / Top-Down Approach / Bottom-Up Approach / Space Optimization Approach:





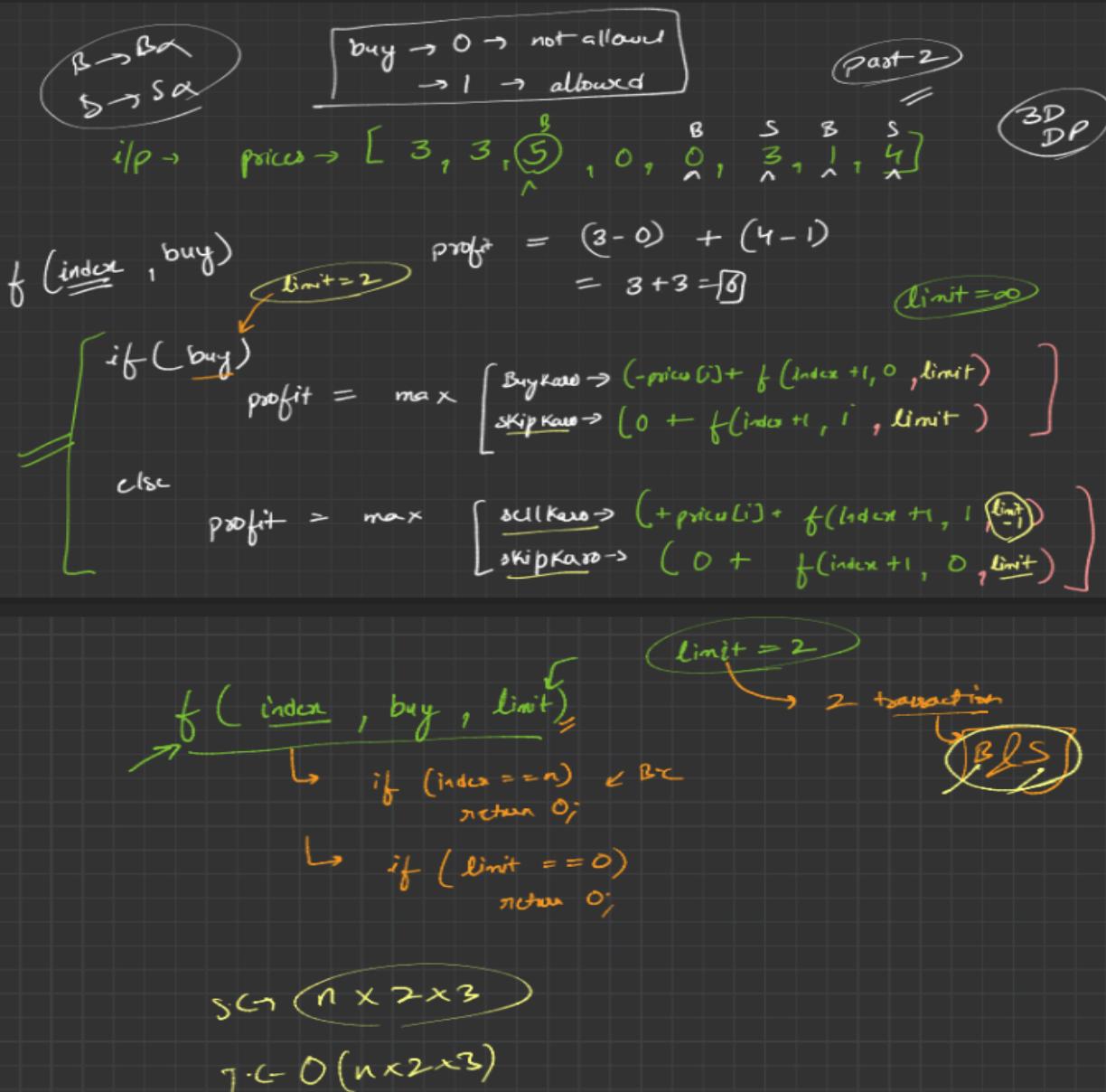
else // $\underline{\text{buy}} \rightarrow 0$

$$\text{profit} = \boxed{+\text{prices}[i] + f(i+1, 1)} \max$$

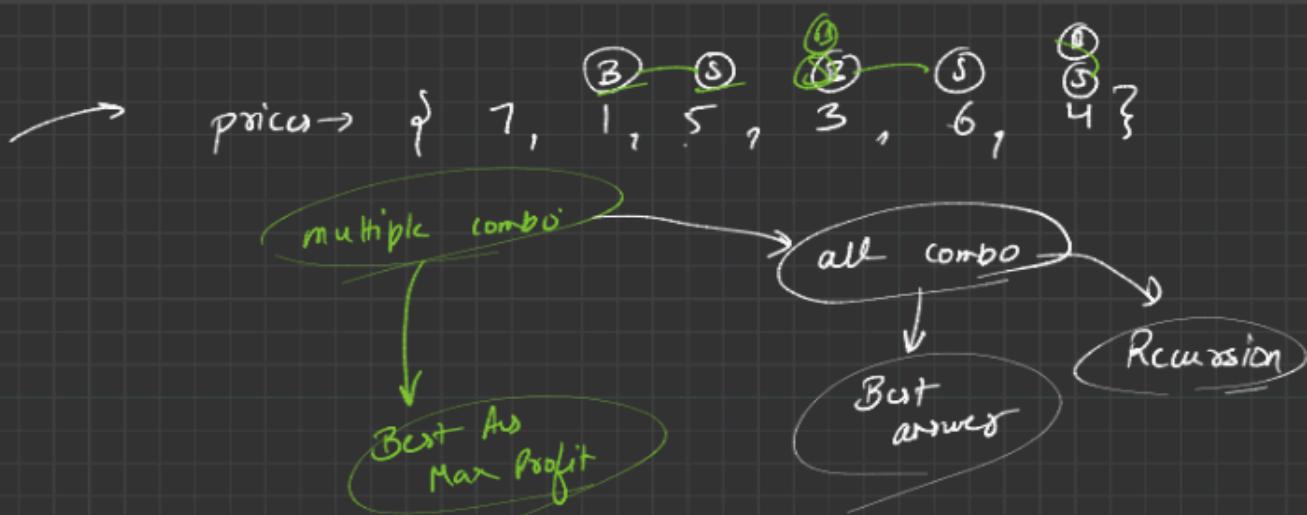
or

$$\boxed{0 + f(i+1, 0)} \rightarrow \text{skip Karo}$$

Buy And Sell Part-III By Recursion / Top-Down Approach / Bottom-Up Approach / Space Optimization Approach:

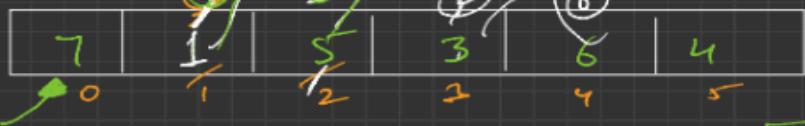


Buy And Sell Part-IV By Recursion / Top-Down Approach / Bottom-Up Approach
/ Space Optimization By Previous Approach / Space Optimization Approach:



$$\underline{\text{profit}} = \underline{5} - \underline{1} = \underline{5} + (\underline{-1}) + \underline{6} + \underline{-3}$$

police



buy

Buy Kaoz

buy -

- sell keep
- ignore / skip

buy

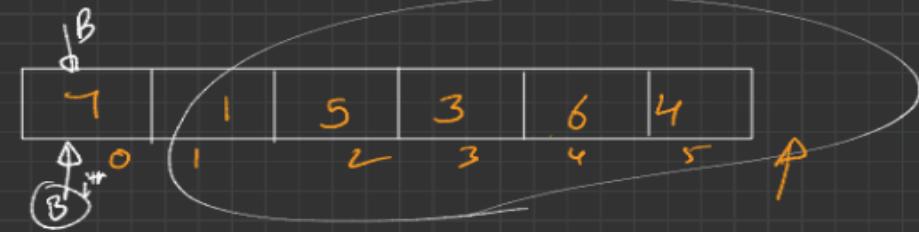
1

sell

1

The diagram illustrates the relationship between the words 'buy' and 'sell'. The word 'buy' is connected by a horizontal arrow pointing right to the word 'not allowed'. Below 'buy', another horizontal arrow points right to the word 'sell'. From 'sell', a vertical arrow points down to the word 'allowed'.

300



~~logic~~

if (buy)

$\text{if } (\text{index} == n)$

$$\text{profit} = \boxed{-\text{prices}[i]} + f(i+1, 0);$$

↓
 index
 buy

max

$$\boxed{0 + f(i+1, 1);}$$

skip

else

// buy → 0

8

$$\text{profit} = \max_{0 \leq i \leq n-1} \left[+\text{price}[i] + f(i+1, 1) \right]$$

$0 + f(i+1, 0)$ } skip Karo

~~rec~~

+ Mem

↓

①

dp array create

func call add

②

ans return

↳ dp mem store

③

B.C → K back

dp check Kalo → answer already

present

return Kalo

Top - Down

index →
0 → n

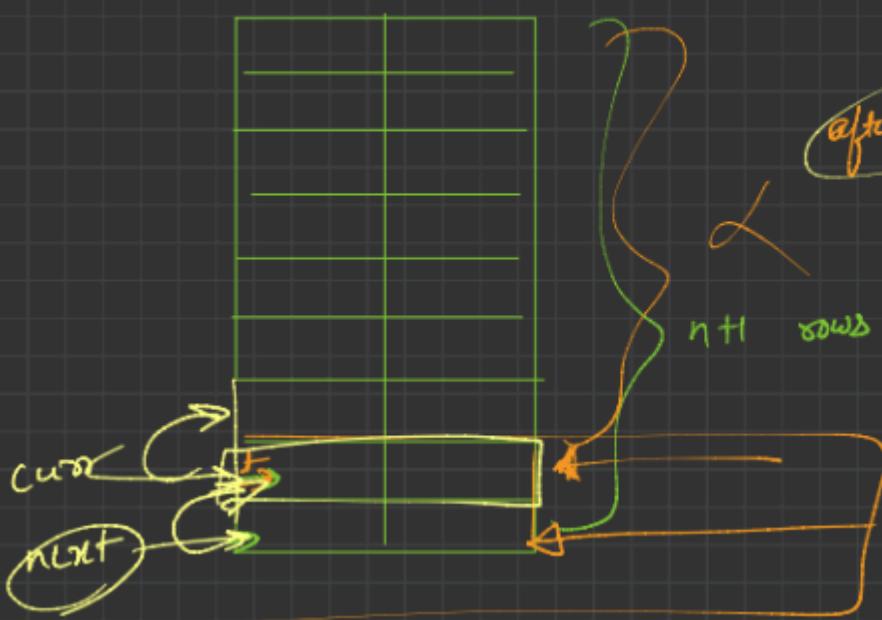
Bottom - Up

n-1 → 0

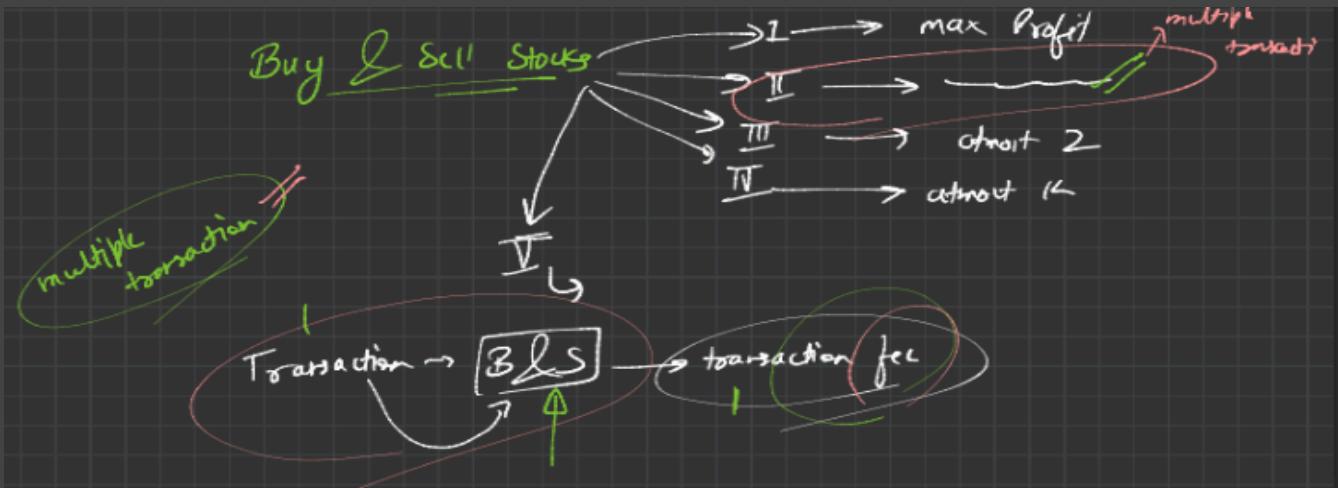
S. O → ? O(n)

→ O(1) =

dp [index] [buy]



Buy And Sell With Transaction Fee:



$$\text{prices} \rightarrow [1, 3, 2, 8, 4, 9] \quad \text{fee} = 2$$

$$\text{Transaction 1} \rightarrow \text{profit} \rightarrow [8 - 1] = 7 \text{ } (-\text{fee})$$

$\xrightarrow{-7-2}$
 ≥ 5

$$\text{Transaction 2} \rightarrow \text{profit} = 9 - 4 = 5 - \text{fee}$$

$\xrightarrow{= 5-2}$
 $= 3$

$$\text{Total profit} = 5 + 3 = 8$$

Logic:-

$f(\text{index}, \text{buy})$

$\text{buy} \rightarrow 0 \rightarrow N$
 $\rightarrow 1 \rightarrow A$

$$\begin{cases} \text{if } (\text{buy}) \\ \text{profit} = \max \left[\begin{array}{l} \text{Buy} \rightarrow (-\text{price}[i]) + f(\text{index}+1, 0) \\ \text{Skip} \rightarrow (0 + f(\text{index}+1, 1)) \end{array} \right] \\ \text{else} \\ \text{profit} = \max \left[\begin{array}{l} \text{Sell} \rightarrow (+\text{price}[i]) + f(\text{index}+1, 1) \\ \text{Skip} \rightarrow (0 + f(\text{index}+1, 0)) \end{array} \right] \end{cases}$$

Longest Common Subsequence By Recursion / Top-Down Approach /

Bottom-Up Approach / Space Optimization Approach:

→ [Longest Common Subsequence]

Common Subsequence

a = "abcde" → ace
b = "ace"
Subsequence
"a b c d e f g a f a"
↓
ace
↓
acd
↓
cad
Relative ordering

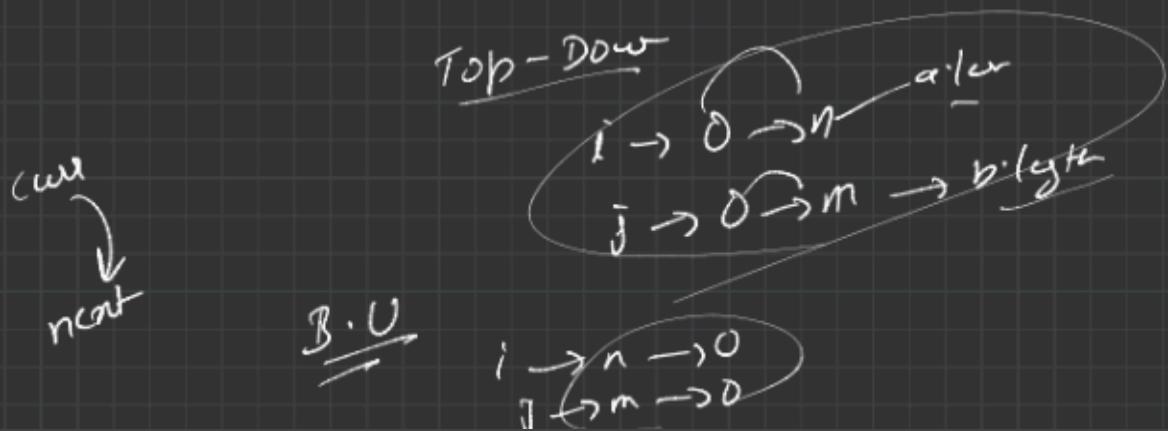
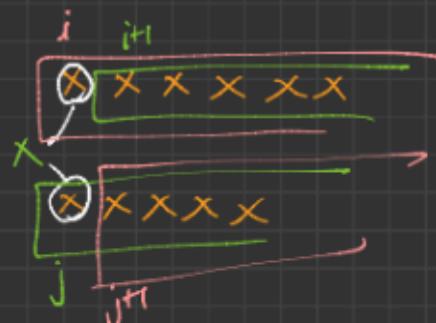
a = "abc"
b = "abc"
↓
a
b
c
ac
bc
ab
abc
③

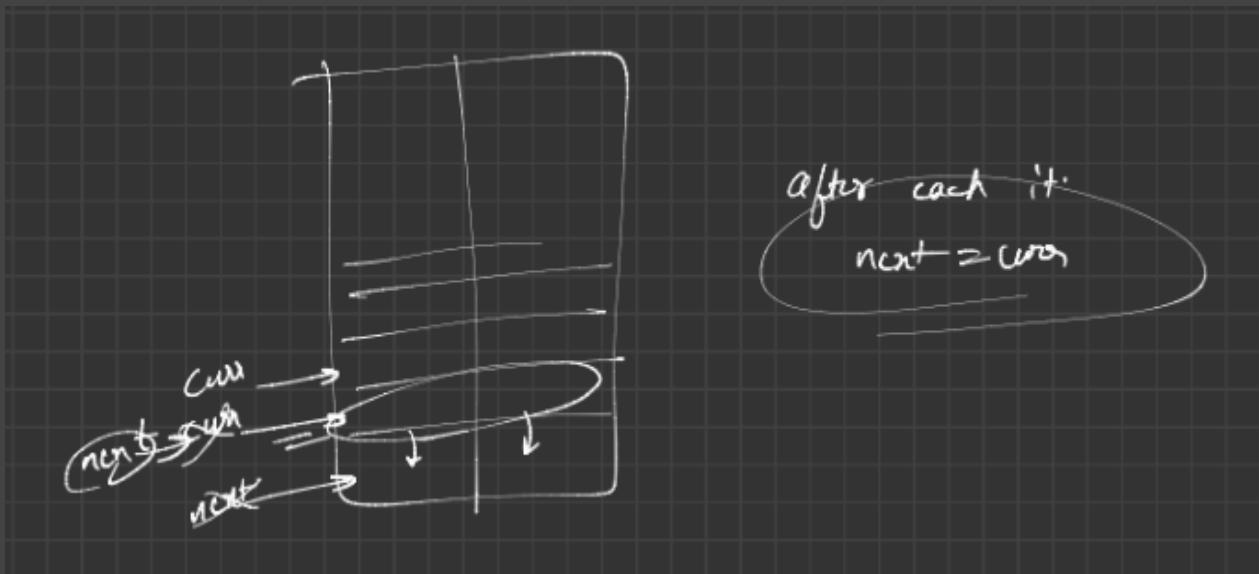
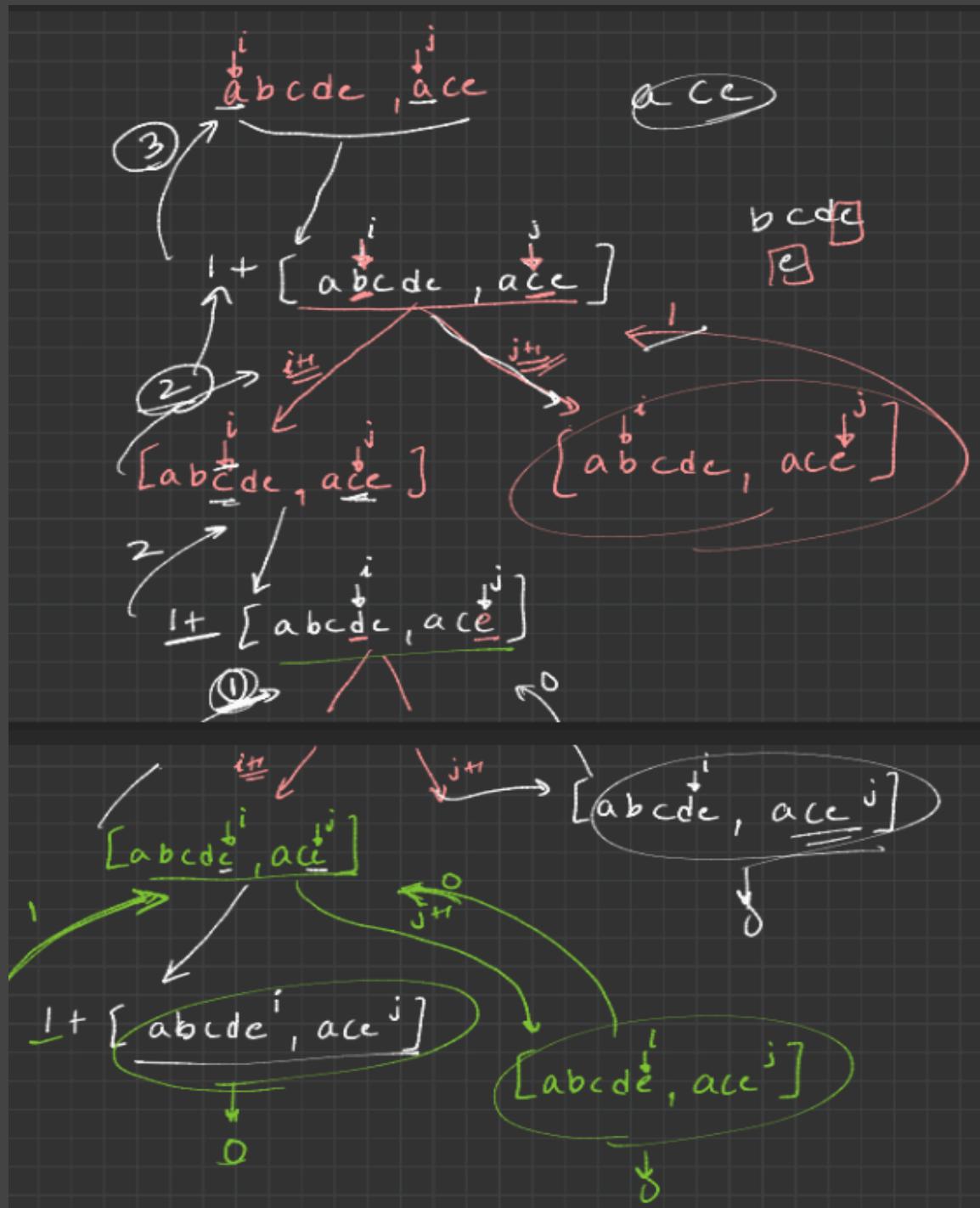
a = "abc"
b = "dcf"
" "
a
b
c
ab
bc
ac
abc
20
d
e
f
de
cf
df
dcf
ans = 0

$\underline{a} = \text{" } \begin{matrix} x \\ a \end{matrix} b \left[\begin{matrix} c & d & c \end{matrix} \right] \text{"}$
 $\underline{b} = \text{" } \begin{matrix} x \\ a \end{matrix} \left[\begin{matrix} c & e \end{matrix} \right] \text{"}$

$f(a, b, i, j)$

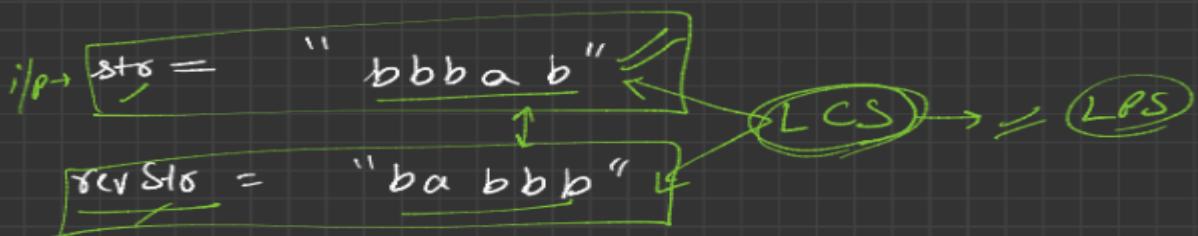
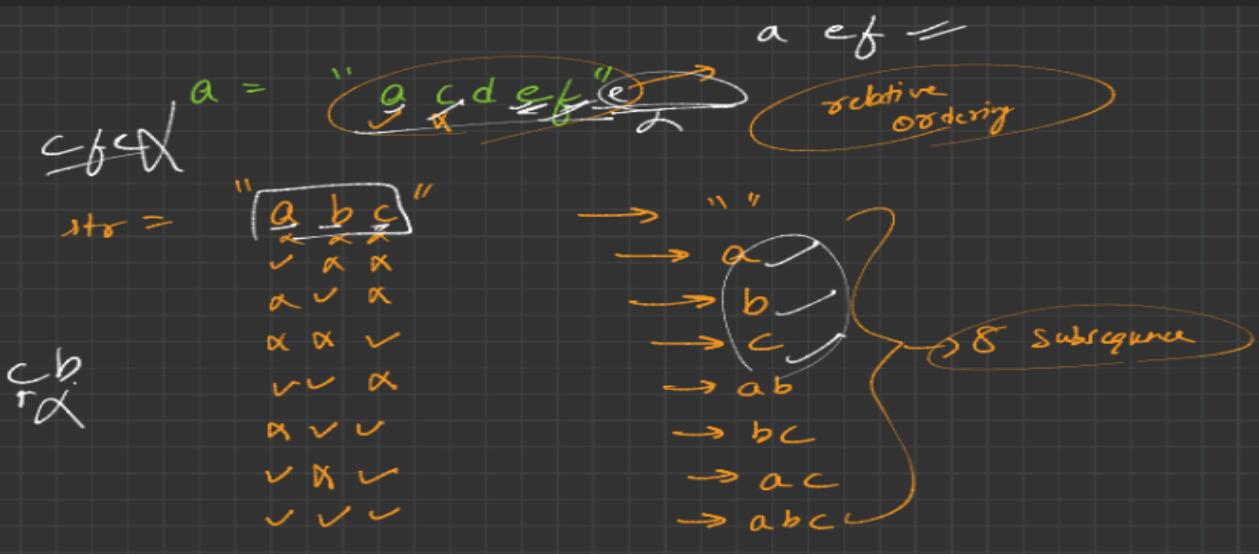
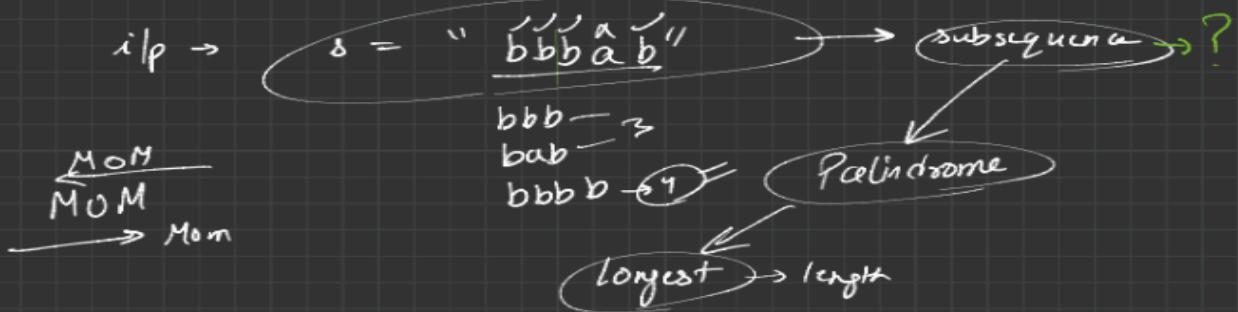
if $(a[i] == b[j]) // \text{match}$
 return $1 + f(a, b, i+1, j+1)$
 else
 return $\max \left[f(a, b, i, j+1), f(a, b, i+1, j) \right]$;





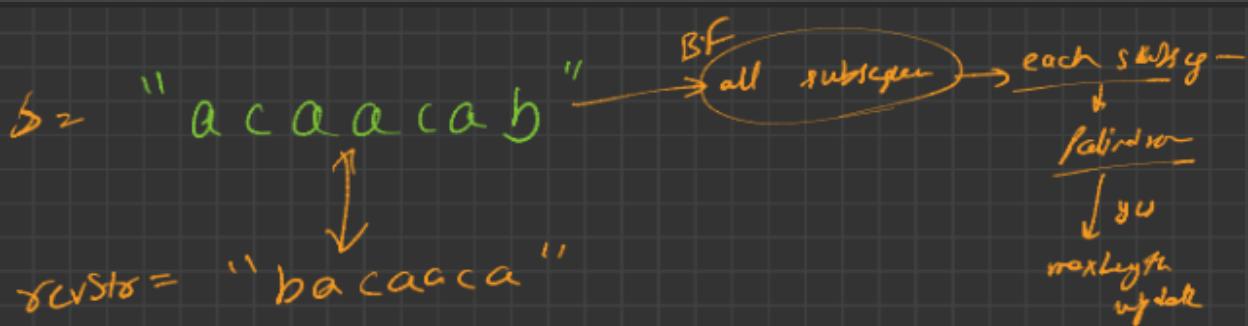
Longest Palindromic Subsequence:

\rightarrow Longest Palindromic Subsequence



Palindrome \rightarrow revs

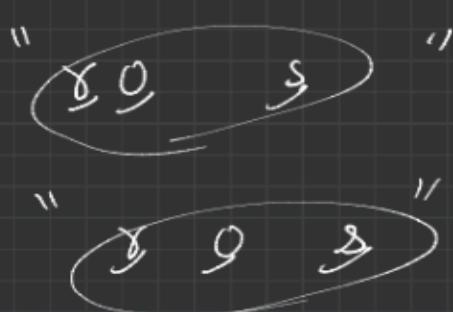
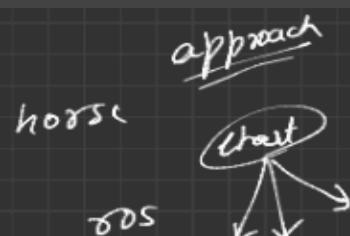
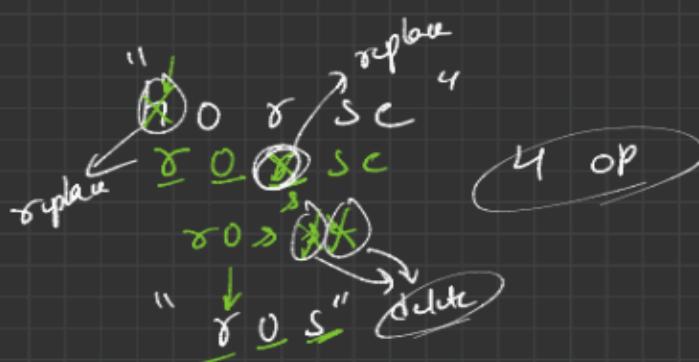
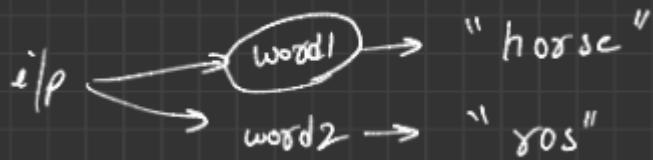
(aca) \rightarrow (aca)



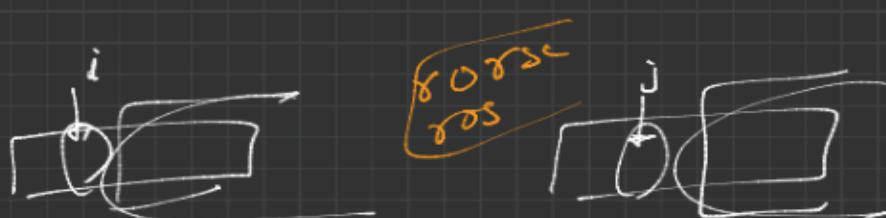
Edit Distance By Recursion / Top-Down Approach / Bottom-Up Approach /

Space Optimization Approach:

→ EDIT Distance



- ① replace h with r
 - ② delete o
 - ③ delete e
- 3 op

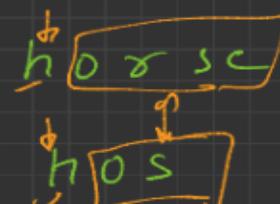


horse
 ros
r h o r s
r o s

if (char match)
 ↳ call for remaining string

else

- insertAns
- deleteAns
- replaceAns



$$\text{findAns} = \min(\text{insertAns}, \text{deleteAns}, \text{replaceAns})$$

word1 → sos

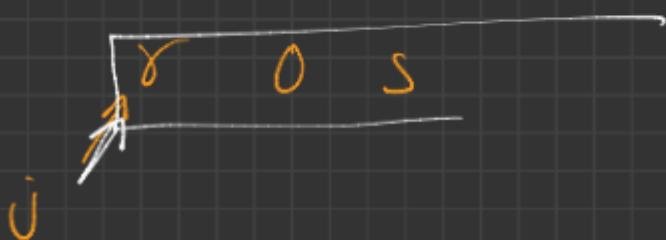
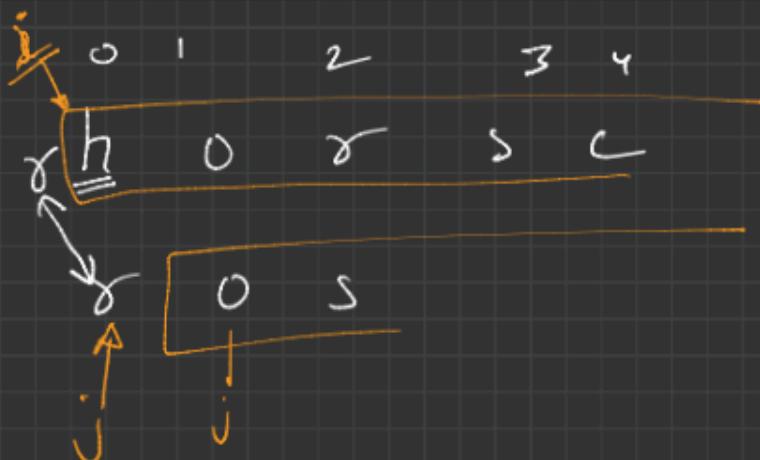
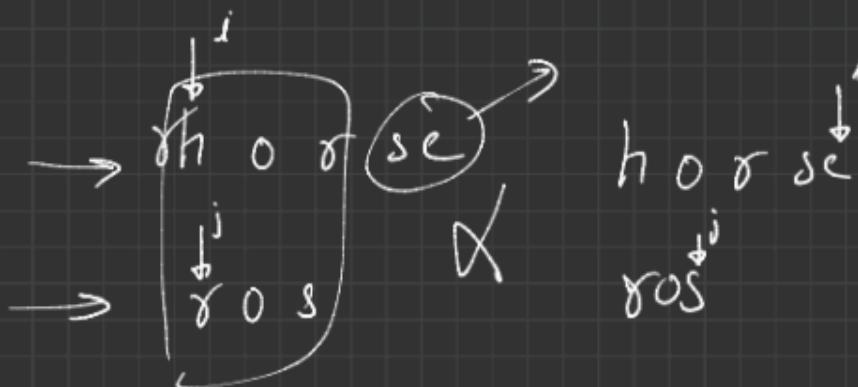
h o s

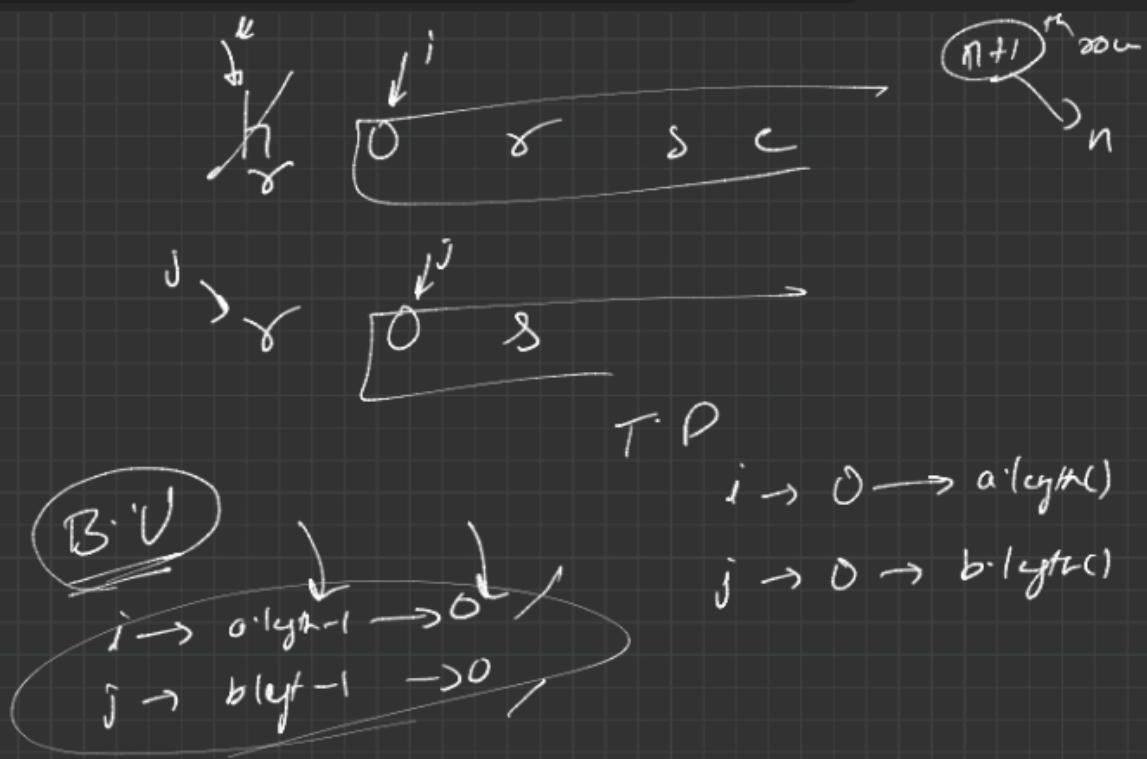
h o r i s c

word2 → horse

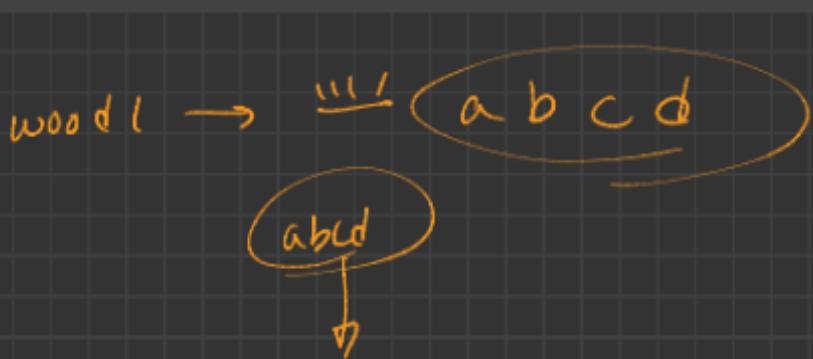
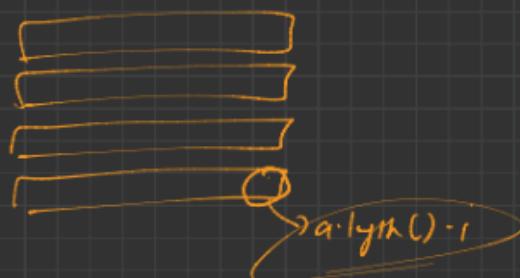
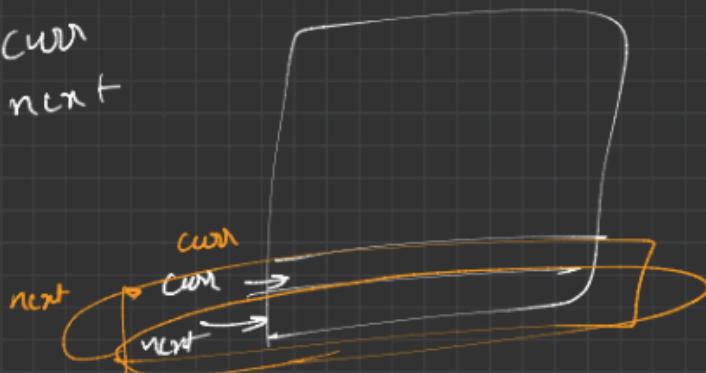
h o r s e

h o r s e i





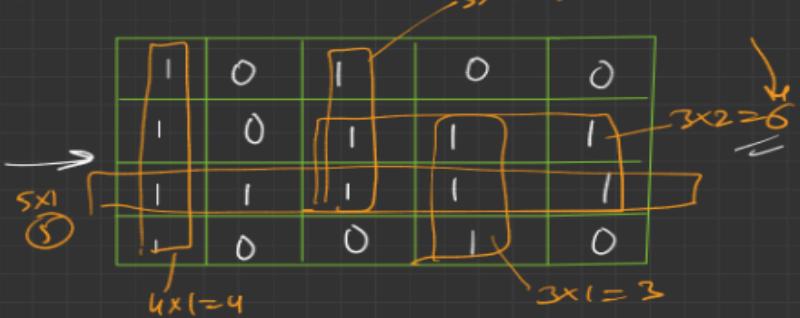
curr
 next



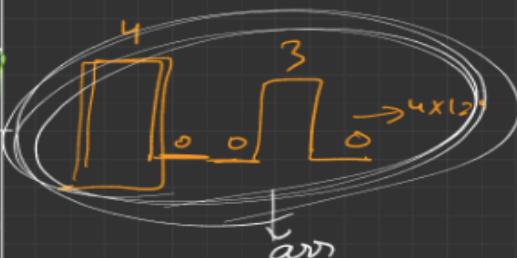
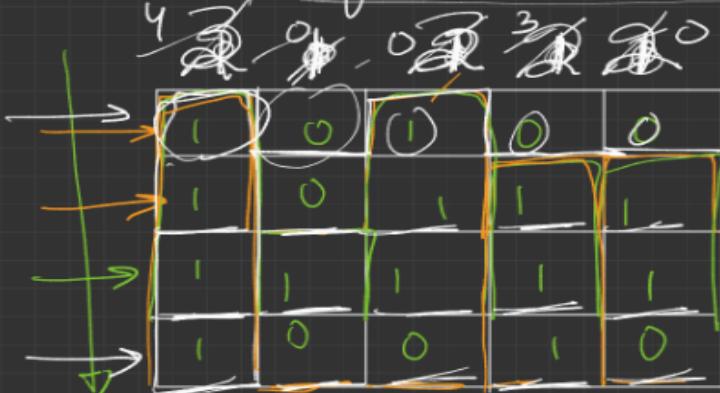
Maximum Rectangle With All 1s:

→ Maximal Rectangles

i/p → $n \times m$ matrix
 $\begin{matrix} 0 & 1 \\ 1 & 0 \end{matrix}$



→ Largest area in a histogram ✓



$O(n \times (m+n))$

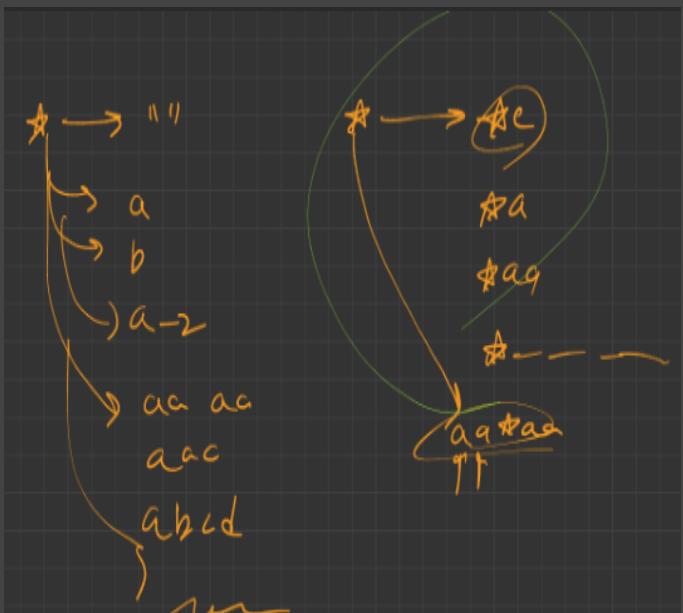
WildCard Pattern Matching By Recursion / Top-Down Approach / Bottom-Up Approach / Space Optimization Approach:

→ WildCard Pattern Matching

? → matches with any single character

* → matches any sequence of char

✓ str = "a b c d e"
 ✓ pattern = "a * c ? e"
 Valid pattern



$s = "a\ a"$ \rightarrow In Valid pattern
 $p = "\ \ a"$

$s = "abc"$
 $p = "(\)"$ \rightarrow Valid pattern
 abc

$s = "f\ b"$
 $p = "[\]"$ \rightarrow Invalid pattern

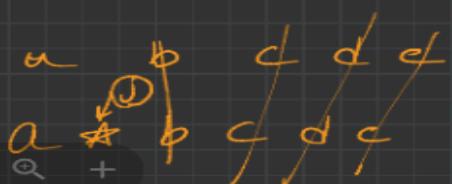
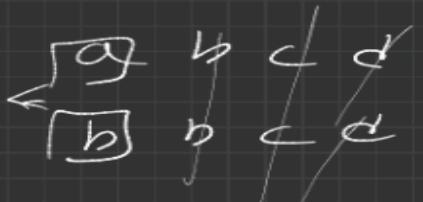
Open with Google Docs

str = "a b c d e"
pattern = "a * c d e"

if (match,
 f(str, pattern, i-1, j-1);
else if (pattern[j] == '*'
{ return f(str, pattern, i, j-1) \rightarrow ϵ 's
 f(str, pattern, i-1, j) \rightarrow * \rightarrow * }
else return false;

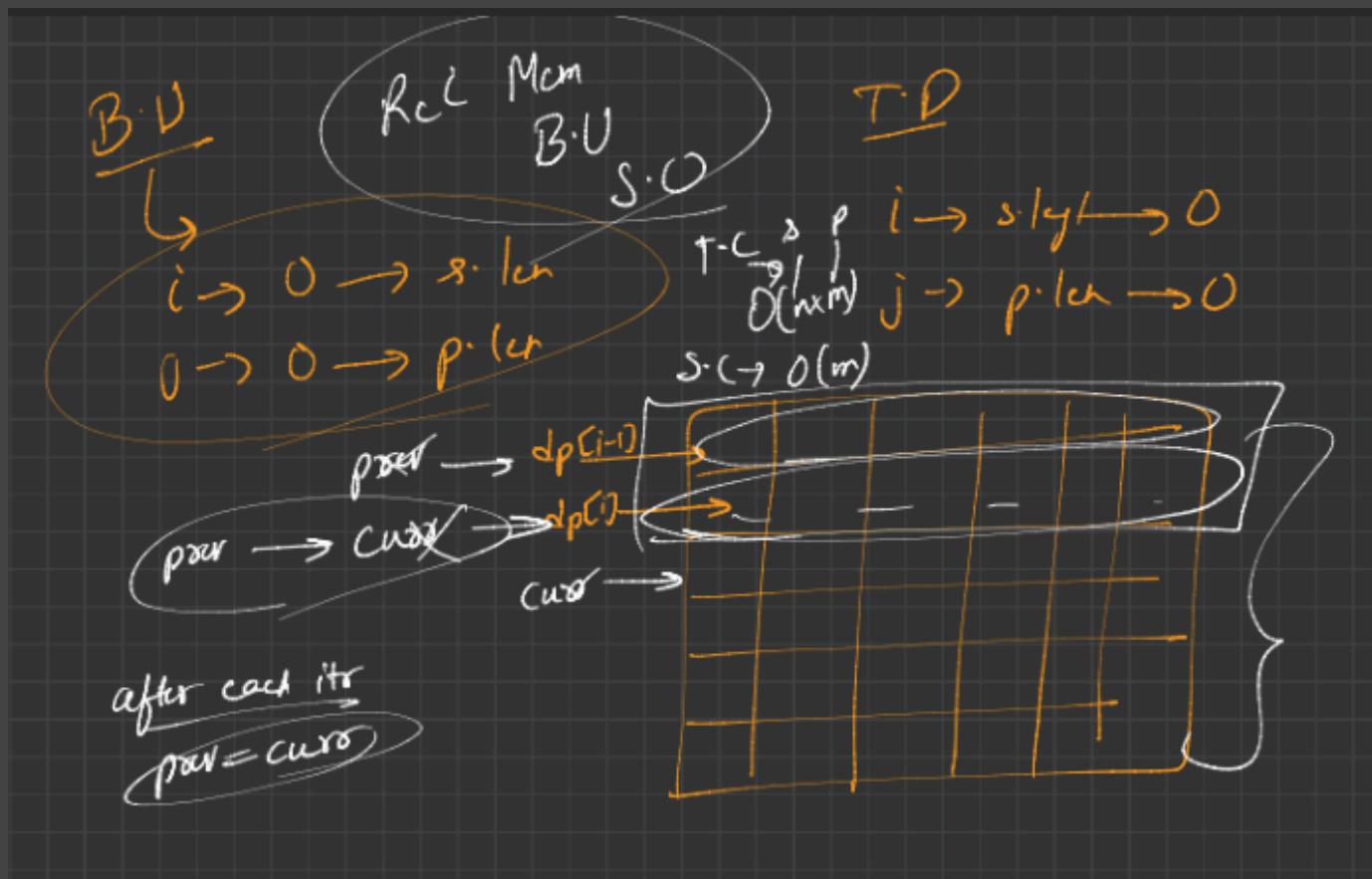
match
 $\rightarrow str[i] == pattern[j]$
 $\rightarrow pattern[j] == '?'$

f(str, pattern, i, j)
* \rightarrow [empty string]
Koi bhi

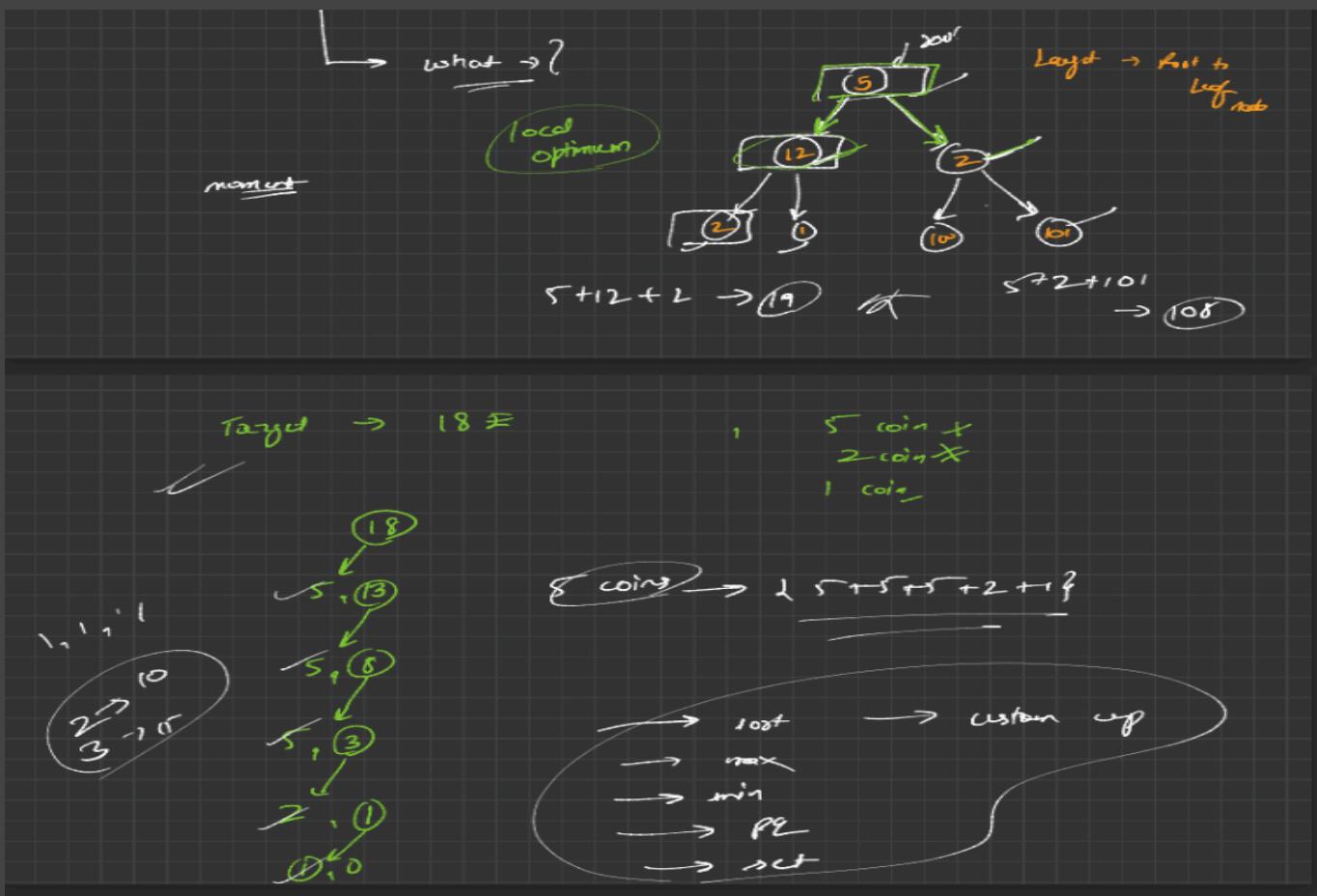


$s \rightarrow a \underline{b} c | d c$
 $p \rightarrow \boxed{c?c}$

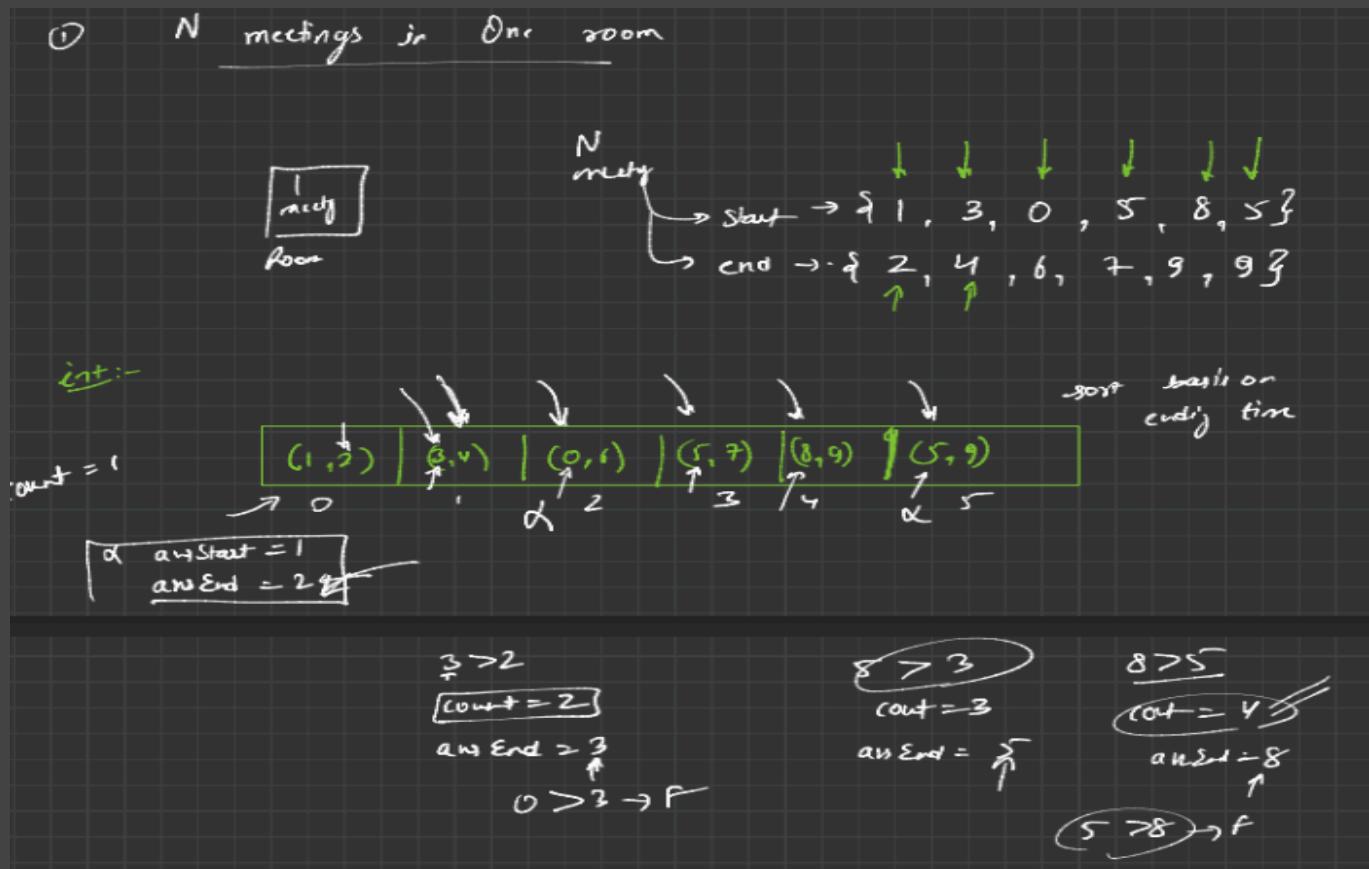
$s \rightarrow \underline{a} b c$ $p \rightarrow \boxed{b} \underline{a} \underline{c}$ <i>I.P</i>	$s \rightarrow \underline{a} b c$ $p \rightarrow \boxed{\star} \underline{a} \underline{b} c$ <i>E.S</i> <i>N.P</i>
--	--



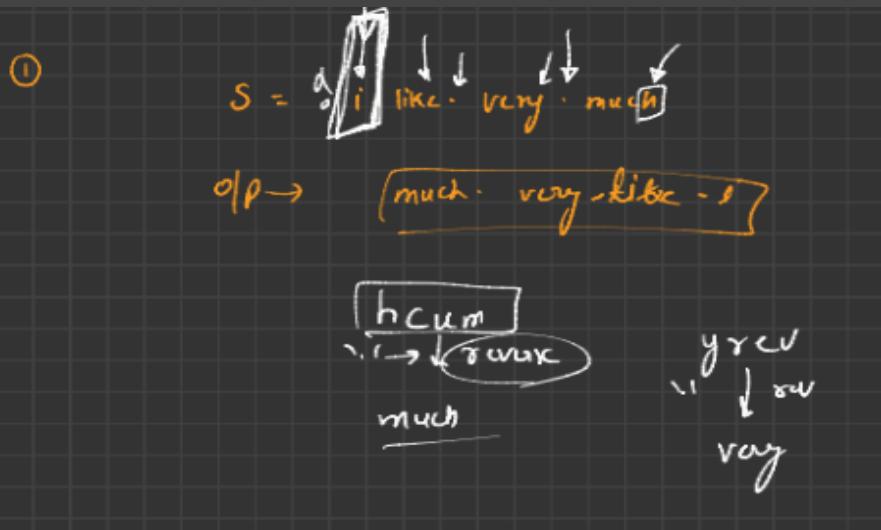
Greedy Algorithm



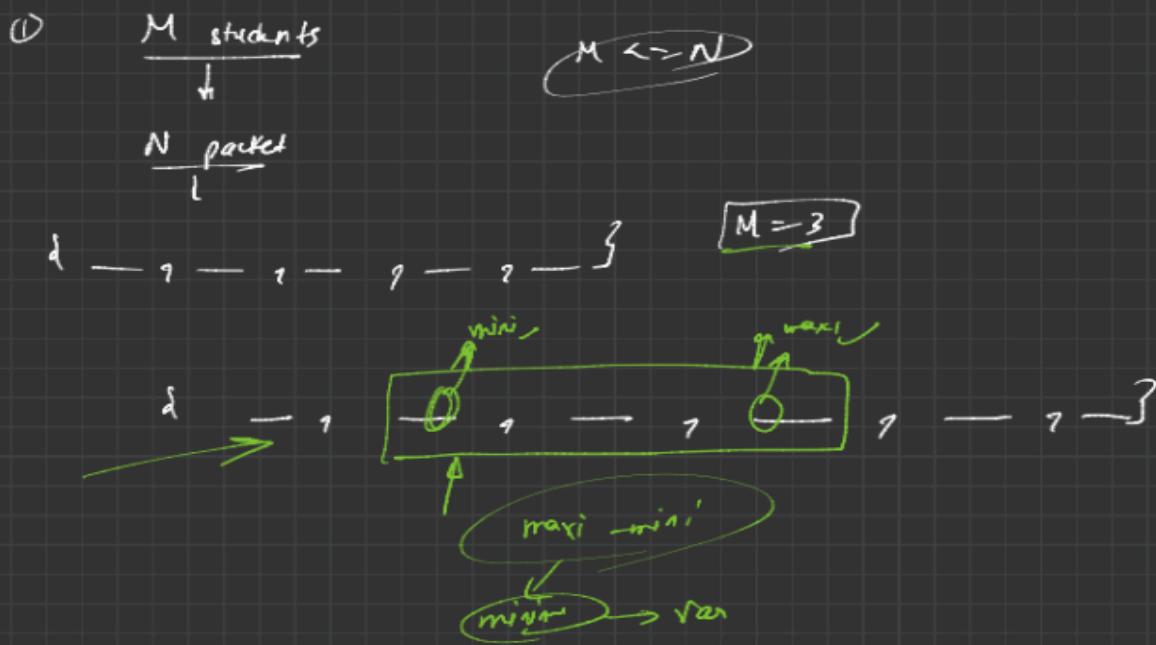
N Meetings In One Room:



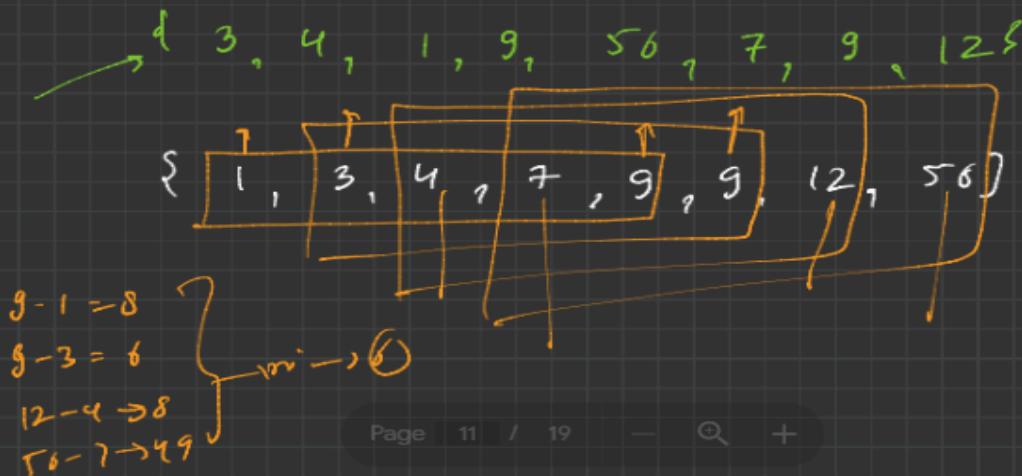
Reverse Words In A Given String:



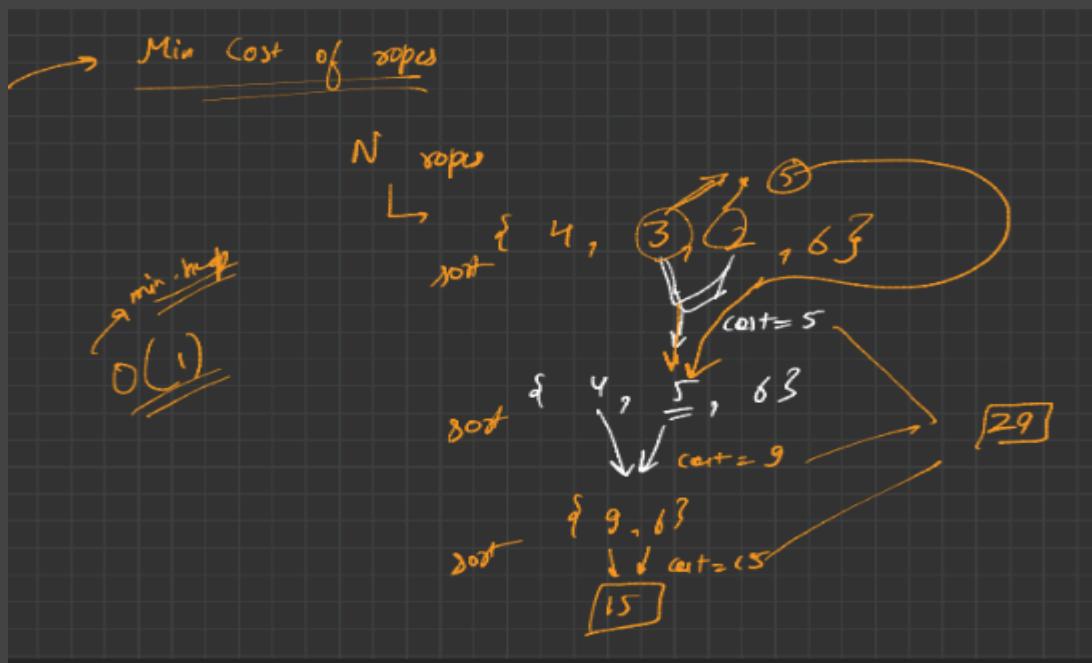
Chocolate Distribution Problem:



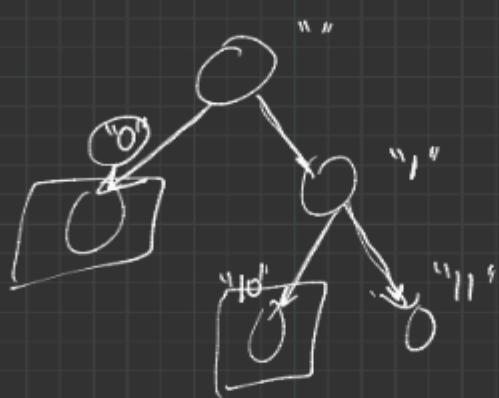
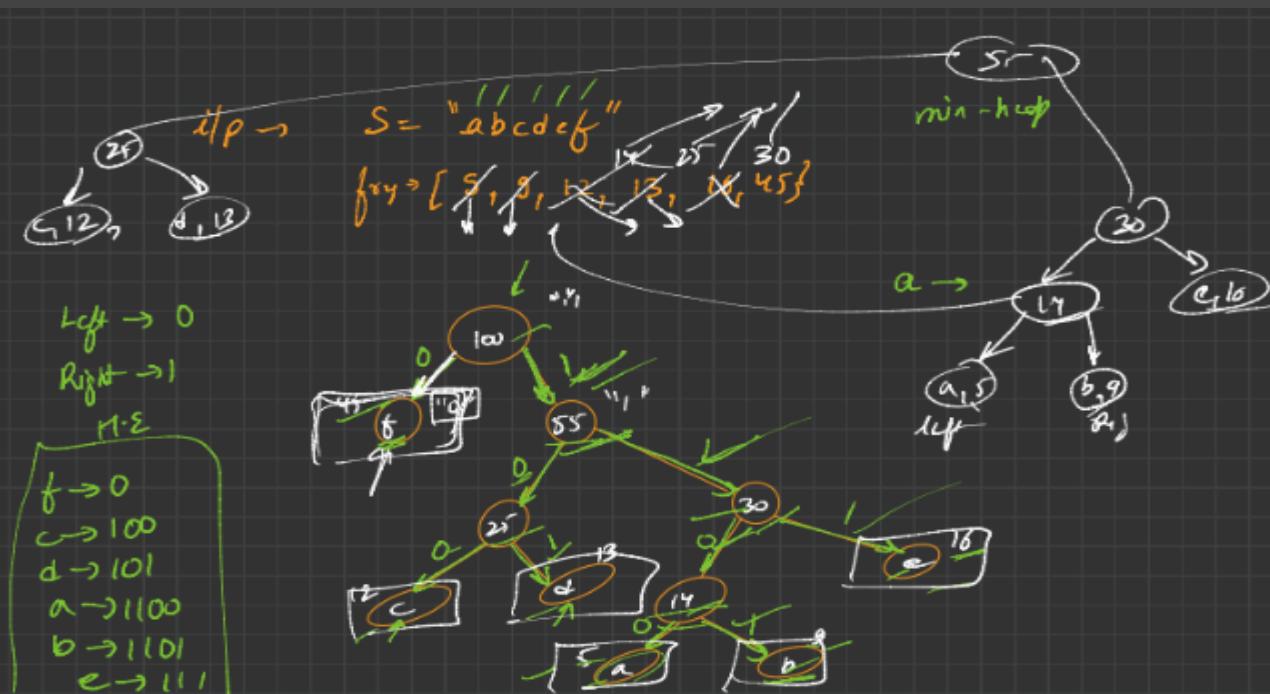
$$N = 8, \quad M = 5$$



Minimum Cost Of Ropes:

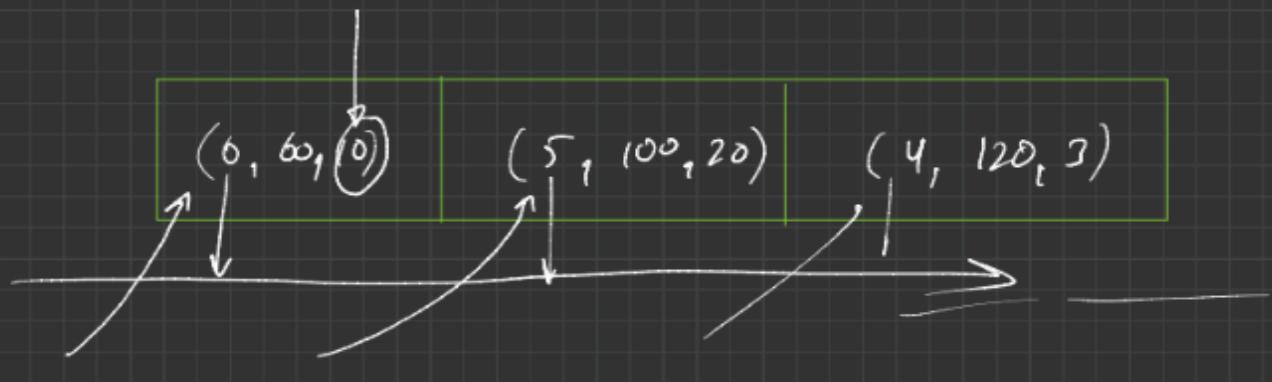
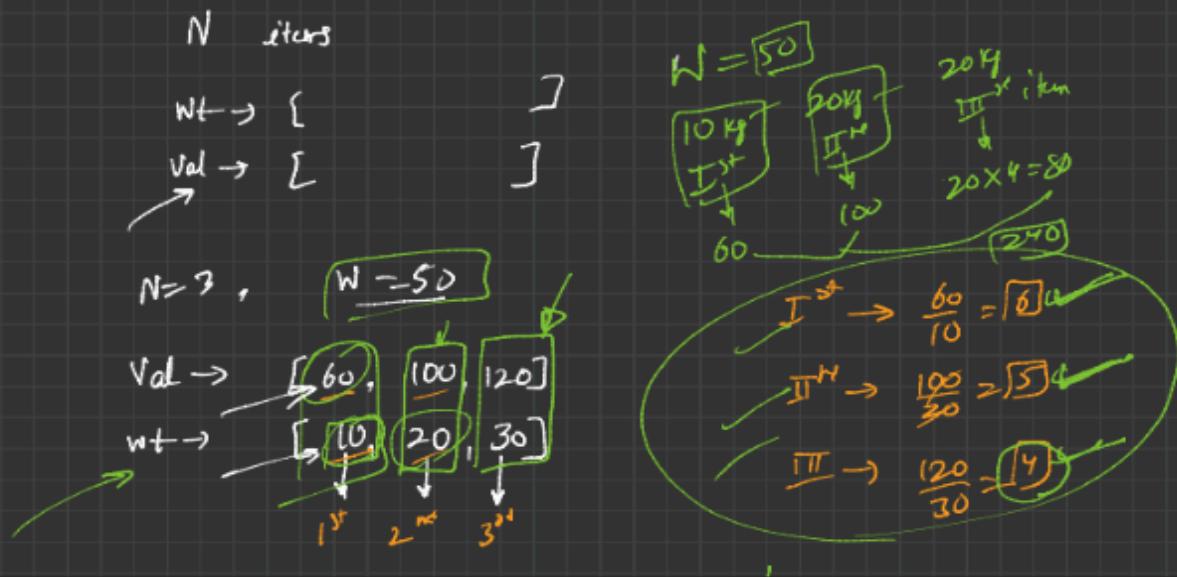


Huffman Encoding:



Fractional KnapSack:

→ Fractional Knapsack:



Job Sequencing:

→ Job Sequencing Problem:

<u>Job</u>	<u>Jobs</u>	<u>Deadline</u>	<u>Profit</u>
1		4	20
2		1	10
3		1	40
4		1	30

$(4_0, 3, 1)$	$(3_0, 4, 1)$	$(2_0, 1, 4)$	$(1_0, 2, 1)$
p i_d $\text{dead}(t)$			

curr Job Index $\rightarrow 1 \cancel{2} \cancel{3} 4$

$$\text{profit} = 40 > 30$$

$i_d \rightarrow 3$

$\text{deadline} \rightarrow 4$

29/60

