

# ★ ★ INDEX ★ ★

IInd Semester.

No.	Title	Page No.	Date	Staff Member's Signature
1)	Basic of R software	41	28/11/19	AM
2)	Probability distribution	44	5/12/19	} AM
3)	Binomial distribution	47	19/12/19	
4)	Normal distribution	49	2/1/20	
5)	Normal and T-test	51	16/1/2020	AM
6)	Large Sample Test	53	28/1/20	AM
7)	Small Sample test	56	6/02/2020	} AM 27-12-19
8)	Large and small test	58	13/02/20	
9)	Chi square test & ANOVA	63	20/02/20	
10	Non-parametric test	66	27/02/20	

### Source code:-

Q.1. 01

1)  $(4+6+8)/2-5$

>>> 9

2)  $2^2 + \text{abs}(-3) + \text{sqrt}(45)$

>>> 13.7080

3)  $5^3 + 7 \times 5 \times 8 + 46/5$

>>> 414.2

4)  $\text{sqrt}(4^2 + 5 \times 3 + 7/6)$

>>> 5.671567

5)  $\text{round}(46/7 + 9 \times 8)$

>>> 7.9

Q.2.

1)  $c(2,3,5,7) * 2$

>>> 4 6 10 14

2)  $c(2,3,5,7) * c(2,3)$

>>> 4 9 10 21

3)  $c(2,3,5,7) * c(2,3,6,2)$

>>> 4 9 30 14

4)  $c(1,6,2,3) * (-2,-3,-4,-1)$

>>> -2 -18 -8 -3

5)  $c(2,3,5,7) \wedge 2$

>>> 4 36 512 9 16 125

>>> 4.92549

6)  $c(4,6,8,9,4,5) \wedge c(1,2,3)$

>>> 4 36 512 9 16 125

7)  $c(6,2,7,5) / c(4,5)$

>>> 1.50 0.40 1.75 1.00

### PRACTICAL:-1

41

#### Basic of R Software.

- \* R is a Software for statistical analysis and data compute.
- \* It is an effective data handling software and outcome storage is possible.
- \* It is capable of graphical display.
- \* It is a free software.

Q1. Solve the following:-

1)  $4+6+8 \div 2-5$

2)  $2^2 + |-3| + \sqrt{45}$

3)  $5^3 + 7 \times 5 \times 8 + 46 \div 5$

4)  $\sqrt{4^2 + 5 \times 3 + 7/6}$

5) round of  $(46 \div 7 + 9 \times 8)$

Q2. Vector Calculation:-

1)  $c(2,3,5,7) * 2$

2)  $c(2,3,5,7) * c(2,3)$

3)  $c(2,3,5,7) * c(2,3,6,2)$

4)  $c(1,6,2,3) * (-2,-3,-4,-1)$

5)  $c(2,3,5,7) \wedge 2$

6)  $c(4,6,8,9,4,5) \wedge c(1,2,3)$

7)  $c(6,2,7,5) / c(4,5)$

Q.3.

1)  $x = 20$   
 $y = 30$   
 $z = 2$ , find (i)  $x^2 + y^2 + z$   
 (ii)  $\sqrt{x^2 + y}$   
 (iii)  $x^2 + y^2$ .

Q.4. Draw Matrix.

→ data = 1, 2, 3, 4, 5, 6, 7, 8.

Q.5. Find  $x + y$  and  $2x + 3y$  when  $x$ 

$$x = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 7 \\ 9 & -5 & 9 \end{bmatrix}$$

$$y = \begin{bmatrix} 10 & -5 & 7 \\ 12 & -4 & 9 \\ 15 & -6 & 5 \end{bmatrix}$$

Q.3.

1)  $x = 20$   
 $y = 30$   
 $z = 2$

(i)  $x^2 + y^2 + z$   
 >>> 27402

(ii)  $\sqrt{x^2 + y}$   
 >>> 20.73644

(iii)  $x^2 + y^2$   
 >>> 1300.

Q.4.

→  $x = \text{matrix}(\text{nrow} = 4, \text{ncol} = 2, \text{data} = c(1, 2, 3, 4, 5, 6, 7, 8))$

>>> x

>>>

	[,1]	[,2]
[1,]	1	5
[2,]	2	6
[3,]	3	7
[4,]	4	8

Q.5.

→  $x = \text{matrix}(\text{nrow} = 3, \text{ncol} = 3, \text{data} = c(4, 7, 9, -2, 0, 6, 7, 3))$

>>> x

>>>

	[,1]	[,2]	[,3]
[1,]	4	-2	6
[2,]	7	0	7
[3,]	9	-5	9



y = matrix(nrow = 3, ncol = 3, data = c(10, 12, 15, -5, -4, -6, 9, 5))

>>> y

>>> [1,] [2,] [3,]

[1,] 10 -5 7

[2,] 12 -4 9

[3,] 15 -6 5

>>> x + y

>>> [1,] [2,] [3,]

[1,] 14 -7 13

[2,] 19 -4 16

[3,] 24 -11 8

>>> 2 \* x + 3 \* y

>>> [1,] [2,] [3,]

[1,] 38 -19 33

[2,] 50 -12 41

[3,] 63 -18 21

Q.6

→ x = c(59, 20, 35, 24, 46, 56, 55, 45, 27, 22, 47, 88, 54, 40, 50, 32, 36, 29, 35, 39)

>>> breaks = seq(20, 60, 5)

>>> a = hist(x, breaks, weight = FALSE)

>>> b = table(a)

>>> c = transform(b)

>>> c

>>> [20, 25) Freq

3

[25, 30) 2

[30, 35) 1

[35, 40) 4

[40, 45) 0

[45, 50) 3

[50, 55) 4

[55, 60) 4

Q.6: mark of statistic of computer science student of A-Batch out 60.

→ MARKS = 59, 20, 35, 24, 46, 56, 55, 45, 27, 22, 47, 58, 54, 40, 50, 32, 36, 29, 35, 39.

~~A = 216~~

Probability Distribution

Q1. Check whether the following PMFs-

$$1) \begin{array}{l} x = 0 \quad 1 \quad 2 \quad 3 \quad 4 \quad 5 \\ P(x) = 0.1 \quad 0.2 \quad -0.5 \quad 0.4 \quad 0.3 \quad 0.5 \end{array}$$

→  $P(2) = -0.5$ , (can't be a probability mass function)  
 $\therefore$  PMF  $\nrightarrow 0$ .

$$2) \begin{array}{l} x = 1 \quad 2 \quad 3 \quad 4 \quad 5 \\ P(x) = 0.2 \quad 0.2 \quad 0.3 \quad 0.2 \quad 0.2 \end{array}$$

→ It cannot be a PMF, as in PMF,  $\sum P(x) = 1.1$ .

$$3) \begin{array}{l} x = 10 \quad 20 \quad 30 \quad 40 \quad 50 \\ P(x) = 0.2 \quad 0.2 \quad 0.35 \quad 0.15 \quad 0.1 \end{array}$$

→ It is PMF, because  $\sum P(x) = 1$ .

Q2.

1) Find CDF for the following PMF and sketch the graph.

$$\begin{array}{l} x = 10 \quad 20 \quad 30 \quad 40 \quad 50 \\ P(x) = 0.2 \quad 0.2 \quad 0.35 \quad 0.15 \quad 0.1 \end{array}$$

$$1) \gg \text{Prob} = (0.2, 0.2, 0.35, 0.15, 0.1)$$

$$\gg \text{Sum(Prob)}$$

$$[] 1.1$$

$$2) \gg \text{Prob} = (0.2, 0.2, 0.35, 0.15, 0.1)$$

$$\gg \text{Sum(Prob)}$$

$$[] 1$$

Q2.

$$\gg \text{Prob} = (0.2, 0.2, 0.35, 0.15, 0.1)$$

$$\gg \text{Sum(Prob)}$$

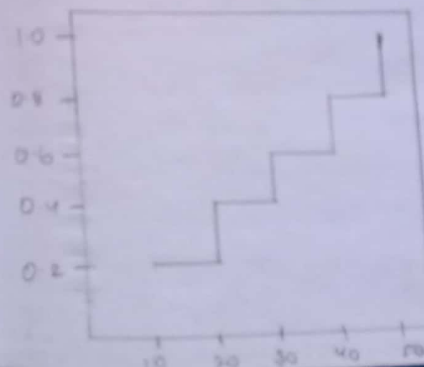
$$[] 1$$

$$\gg \text{cumSum(Prob)}$$

$$[] 0.20 \quad 0.40 \quad 0.75 \quad 0.90 \quad 1.00$$

$$\gg x = (10, 20, 30, 40, 50)$$

$$\gg \text{Plot}(x, \text{cumSum(Prob)}, "s", x\text{lab}="value", y\text{lab}="P(x)")$$



2)  $\rightarrow p_{\text{prob}} = C(0.15, 0.25, 0.1, 0.2, 0.2, 0.1)$

$\rightarrow \text{sum}(p_{\text{prob}})$

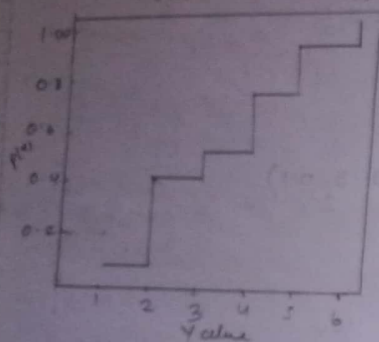
$[1]$  1.

$\rightarrow \text{cumsum}(p_{\text{prob}})$

$[1]$  0.15, 0.40, 0.50, 0.70, 0.90, 1.00

$\rightarrow x = C(1, 2, 3, 4, 5, 6)$

$\rightarrow \text{plot}(x, \text{cumsum}(p_{\text{prob}}), "s", x\text{lab}="value", y\text{lab}="P(x)")$



$$F(x) = \begin{cases} 0 & x < 10 \\ 0.2 & 10 \leq x < 20 \\ 0.4 & 20 \leq x < 30 \\ 0.75 & 30 \leq x < 40 \\ 0.90 & 40 \leq x < 50 \\ 1.00 & x \geq 50 \end{cases}$$

2) Find cdf for the following pmf and sketch the graph:-  
 $x = 1 \ 2 \ 3 \ 4 \ 5 \ 6$   
 $p(x) = 0.15 \ 0.25 \ 0.1 \ 0.2 \ 0.2 \ 0.1$

$$\rightarrow F(x) = \begin{cases} 0 & x < 1 \\ 0.15 & 1 \leq x < 2 \\ 0.40 & 2 \leq x < 3 \\ 0.50 & 3 \leq x < 4 \\ 0.70 & 4 \leq x < 5 \\ 0.90 & 5 \leq x < 6 \\ 1.00 & x \geq 6 \end{cases}$$

Q.3. Check whether the following is p.d.f or not.

$$\rightarrow (i) p(x) = 3 - 2x \quad ; \quad 0 \leq x \leq 1$$

$$\rightarrow F(x) = \int_0^x (3 - 2t) dt \\ = \left[ 3x - x^2 \right]_0^x \\ = \left[ 3(1) - (1)^2 \right] \\ = 2$$

$\therefore$  It is not a p.d.f, because  $\sum p(x) \neq 1$

pp)  $F(x) = 3x^2$  ;  $0 \leq x \leq 1$

$$\rightarrow F(x) = \int_0^x 3x^2$$

$$= [3x^3/3]_0^1$$

$$= [x^3]_0^1$$

$$= [1^3]$$

$$= 1$$

$\therefore$  It is Pdf because  $\forall \underline{F(x) = 1}$ .

✓

✓

i)  $> \text{dbinom}(x, n, p)$

ii)  $> \text{pbinom}(x, n, p)$

iii)  $> 1 - \text{pbinom}(x, n, p)$

iv)  $> \text{qbinom}(A, n, p)$

Q.1.  
 $\rightarrow > \text{dbinom}(0, 100, 0.1)$   
[1] 0.1318653

Q.2  
 $\rightarrow > \text{dbinom}(4, 12, 1/5)$   
[1] 0.1328756

ii)  $> \text{pbinom}(4, 12, 1/5)$   
[1] 0.927445

iii)  $> 1 - \text{pbinom}(5, 12, 1/5)$   
[1] 0.01940528

Q.3  
 $\rightarrow > \text{dbinom}(0:5, 5, 0.1)$   
[1] 0.59049 0.32805 0.07296 0.00810 0.00045 0.00001.

Q.4  
 $\rightarrow > \text{dbinom}(5, 12, 0.25)$   
[1] 0.1022414

ii)  $> \text{pbinom}(5, 12, 0.25)$   
[1] 0.9455974

iii)  $> 1 - \text{pbinom}(5, 12, 0.25)$   
[1] 0.00278151

iv)  $> \text{dbinom}(6, 12, 0.25)$   
[1] 0.04014945

Practical:- 0.3

Binomial distribution.

i)  $P(X=x)$

ii)  $P(X \leq x)$

iii)  $P(X > x)$

iv) if  $x$  is unknown,  
 $P_1 = P(X \leq x)$ , etc

Q1 Find the probability of exactly 10 success in 100 trials with  $p = 0.1$ .

Q2 Suppose there are 12 MCA. each question has 5 options out of which one is correct. Find the probability of having  
i) exactly 4 correct answers.  
ii) at least 4 correct answers.  
iii) more than 5 correct answers.

Q3 Find the complete distribution when  $n=5$  and  $p=0.1$ .

Q4  $n=12$ ,  $p=0.25$ , find the following probability distribution  
i)  $P(X=5)$

ii)  $P(X \leq 5)$

iii)  $P(X > 5)$

iv)  $P(5 \leq X < 7)$



Q.5 Probability of a sales man making a sale to a customer is 0.15. Find the probability of  
 (i) No sales out of 10 customers i.e.  $x=0$   
 (ii) More than 3 sales out of 10 customers.

Q.6 A sales man has a 20% probability of making a sale to a customer out of 30 customers. What is the minimum number of sales he can make with 80% probability? ( $n, p$ ).

Q.7  $X$  follows binomial distribution with  $n=10$ ,  $p=0.3$ : plot the graph of pmf and cdf.

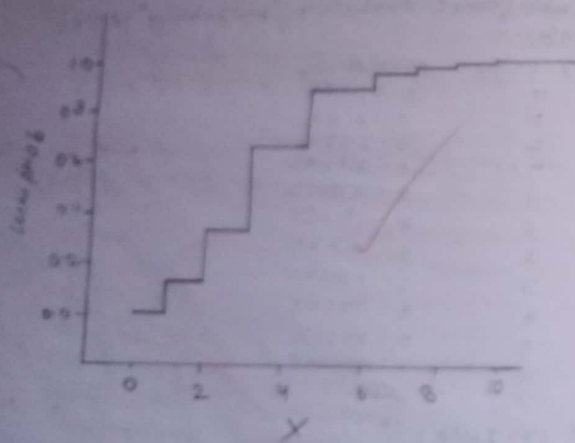
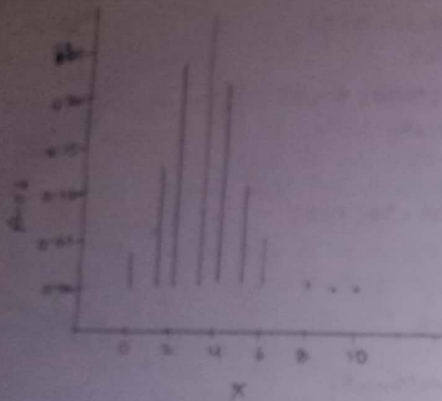
Q.5  
 $\rightarrow$  (i)  $> \text{dbinom}(0, 10, 0.15)$   
 [1] 0.1968744  
 (ii)  $> 1 - \text{pbinom}(3, 10, 0.15)$   
 [1] 0.3522746.

Q.6  
 $\rightarrow > \text{qbinom}(0.88, 30, 0.2)$   
 [1] 9.

Q.7  
 $\rightarrow n=10; p=0.3$   
 $\rightarrow x=0:n$   
 $\rightarrow \text{prob} = \text{dbinom}(x, n, p)$   
 $\rightarrow \text{lumprob} = \text{pbinom}(x, n, p)$   
 $\rightarrow \text{data.frame}("X\text{-value}" = x, "probability" = prob)$   
 $\rightarrow \text{print(d)}$

	X-Value	Probability
1	0	0.02824
2	1	0.12106
3	2	0.25342
4	3	0.26682
5	4	0.20012
6	5	0.10201
7	6	0.03635
8	7	0.009001
9	8	0.00144
10	9	0.00013
11	10	0.00005

$> \text{plot}(x, \text{prob}, "n")$   
 $> \text{plot}(x, \text{lumprob}, "s")$



Practical - 04

13

Topic: Normal distribution

- 1)  $P(X=x) = \text{dnorm}(x, \mu, \sigma)$
- 2)  $P(X \leq x) = \text{pnorm}(x, \mu, \sigma)$
- 3)  $P(X > x) = 1 - \text{pnorm}(x, \mu, \sigma)$
- 4) To generate random no. from a normal distribution (n random numbers) the R code is  $\text{rnorm}(n, \mu, \sigma)$

Problem 3-

A random variable  $X$  follow normal distribution with mean  $\mu = 12$  and standard deviation  $\sigma = 3$ . Find (i)  $P(X \leq 15)$  (ii)  $P(10 < X \leq 14)$  (iii)  $P(X > 14)$  (iv) Generate 5 observations (random numbers)

Sol:  $\mu = 12, \sigma = 3$   
 $P_1 = \text{pnorm}(15, 12, 3)$   
 $[1] 0.8413447$   
 $\text{cat}("P(X \leq 15) = ", P_1)$   
 $P(X \leq 15) = 0.8413447$

(ii)  $P_2 = \text{pnorm}(13, 12, 3) - \text{pnorm}(10, 12, 3)$   
 $[1] 0.3790661$   
 $\text{cat}("P(10 < X \leq 13) = ", P_2)$   
 $P(10 < X \leq 13) = 0.3790661$

(iii)  $P_3 = 1 - \text{pnorm}(14, 12, 3)$   
 $[1] 0.254925$

cat ("P(X > 14) = ", P3)  
 $P(X > 14) = 0.2524925$

(iv)  $\text{rnorm}(5, 12, 3)$

[1] 9.212365 13.690854 10.085173 6.972833  
 14.892886

Q.2. X follows normal distribution with  $\mu = 10$ ,  
 $\sigma = 12$ , find (i)  $P(X \leq 7)$  (ii)  $P(5 < X < 12)$   
 (iii)  $P(X > 12)$  (iv) Generate 10 observations.  
 (v) Find K such that  $P(X < K) = 0.4$ .

→ (i)  $\mu = 10$ ,  $\sigma = 12$

> P1 =  $\text{pnorm}(7, 10, 12)$

[1] 0.0668072

(ii)  $P2 = \text{pnorm}(5, 10, 2) - \text{pnorm}(12, 10, 2)$

[1] 0.0351351

(iii)  $P3 = 1 - \text{pnorm}(12, 10, 2)$

[1] 0.1586583

(iv)  $\text{rnorm}(10, 10, 2)$

[1] 7.334054 10.213002 11.319129 10.721121  
 9.335311 12.591149 8.894187 11.601452  
 6.324594 12.396941

(v)  $\text{qnorm}(0.4, 10, 2)$

[1] 9.493306

Q.3 Generate five random no. from normal distribution with mean = 15, S.D = 4. Find sample mean, median, S.D, print it.

50

X follows  $X \sim N(30, 100)$   $\mu = 30$ ,  $\sigma = 10$  find  
 (i)  $P(X \leq 40)$  (ii)  $P(X > 25)$  (iii)  $P(25 < X < 35)$   
 (iv) Find K such that  $P(X < K) = 0.6$

Q.4  
 →  $P1 = \text{pnorm}(40, 30, 10)$

> P1  
 [1] 0.8413447

(ii)  $P2 = 1 - \text{pnorm}(35, 30, 10)$

> P2  
 [1] 0.3085375

(iii)  $P3 = \text{pnorm}(35, 30, 10) - \text{pnorm}(25, 30, 10)$

> P3

[1] 0.382949

(iv)  $P4 = \text{qnorm}(0.6, 30, 10)$

[1] 32.53347

Q.5

→  $X = \text{rnorm}(5, 15, 4)$

> X  
 [1] 14.13244 17.49037 18.15842 15.87174 10.78590

> am =  $\text{mean}(X)$

> am

[1] 15.20777

> me =  $\text{median}(X)$

> me

[1] 15.87174

> Variance =  $(n-1) * \text{var}(X) / n$

> Variance

[1] 7.006958

```

> sd
[1] 2.647066
> cat("Sample mean is =", am)
Sample mean is = 15.28777
> cat("Sample median is =", me)
Sample median is = 15.87174
> cat("Sample sd is =", sd)
Sample sd is = 2.647066

```

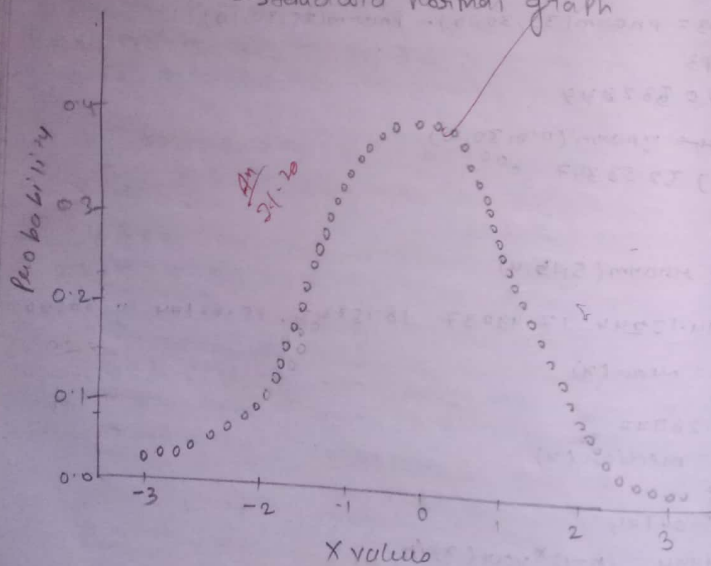
Q.5. Plot the standard normal graph.

→  $x = \text{seq}(-3, 3, \text{by} = 0.1)$

$y = \text{dnorm}(x)$

$\text{plot}(x, y, \text{xlab} = "x \text{ values}", \text{ylab} = "probability", \text{main} = "standard normal graph")$

Standard normal graph



Ans: Normal and t-Test.

Test the hypothesis,  $\mu = 15$  against  $H_1: \mu \neq 15$   
 $H_0: \mu = 15$ . Random sample of size 400 is drawn and it is calculated the sample mean is 14 and standard deviation is 3. Test the hypothesis at 5% level of significance.

→ Formula: Theory formula

R-Software formula  
 $\mu_0 = 15, \bar{x} = 14, s_d = 3$   
 $n = 400$   
 $Z_{\text{calc}} = (\bar{x} - \mu_0) / (s_d / \sqrt{n})$

$[2] = 6.666667$

→  $\text{cat}("Calculate the value of z is =", z_{\text{calc}})$

→ Calculate the value of  $z$  is  $-6.666667$

$P\text{-value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{calc}})))$

$[1] = 2.616796e-11$

∴ the p-value is less than ~~product~~ 0.05 but  
 we reject  $H_0 = 15$

Q.2. Test the  $H_0: \mu = 10$  against  $H_1: \mu \neq 10$  random sample of size 400 is drawn standard deviation is 2.5 with sample mean 10.2. Test the hypothesis at 5% level of significance.

→  $\mu_0 = 10$

$\bar{x} = 10.2$



$$s_d = 2.25$$

$$n = 400$$

$$z_{cal} = (m_x - m_0) / (s_d / \sqrt{n})$$

$$[1] 1.777778$$

cat ("calculate the value of z's", zcal)

calculate the value of z's = 1.777778

$$pvalue = 2 * (1 - pnorm(abs(zcal)))$$

pvalue

$$[1] 0.07544086$$

∴ pvalue more than 0.05

∴ we accept the  $H_0 \approx 10$

Q3. Test the hypothesis  $H_0$  proportion of smokers in a college is 0.2. A sample is collected at 11. It is calculated the sample population at 0.125. Test the hypothesis at 5% level of significance (sample size is 41).

$$\rightarrow p = 0.2$$

$$p_0 = 0.125$$

$$n = 400$$

$$Q = 1 - p$$

$$Q$$

$$[1] 0.8$$

$$z_{cal} = (p - p_0) / \sqrt{(p * Q / n)}$$

zcal

$$[1] -3.75$$

$$pvalue = 2 * (1 - pnorm(abs(zcal)))$$

pvalue

$$[1] 0.0001768346$$

∴ pvalue is less than 0.05  
∴ we reject the  $H_0 \approx 0.2$

52

Q4. Last year farmers lost 20% of their crops, a random sample of 60 fields are collected and it is found that 9 fields of crops are insect polluted. Test the hypothesis at 1% level of significance.

$$\rightarrow p = 0.2$$

$$p = 0.16$$

$$n = 60$$

$$Q = 1 - p$$

$$Q$$

$$[1] 0.8$$

$$z_{cal} = (p - p_0) / \sqrt{(p * Q / n)}$$

zcal

$$[1] -0.9682458$$

$$pvalue = 2 * (1 - pnorm(abs(zcal)))$$

pvalue

$$[1] 0.3320219$$

∴ pvalue is less than greater than 0.05

∴ we accept the  $H_0 \approx 0.2$

Q5. Test the hypothesis  $H_0: \mu = 12.5$  from the following sample at 5% level of significance.

$$\rightarrow x = (12.25, 11.97, 12.15, 12.08, 12.31, 12.28, 11.94, 11.89, 12.16, 12.04)$$

$$n = \text{length}(x)$$

$$[1] 10$$

$$m_x = \text{mean}(x)$$

$$m_x$$

$$12.107$$

$$\text{variance} = (n - 1) * \text{var}(x) / n$$

$$\text{variance}$$

$$[1] 0.019521$$

$SD = 12.5$   
 $t = (Mx - Mo) / (SD / \sqrt{n})$   
 $t = 8.894809$   
 $P\text{-value} = 2 * (1 - \text{pnorm}(\text{abs}(t)))$   
 $P\text{-value}$   
 $[1] 0$

$\frac{8.89}{16.12}$

## PRACTICAL: 06

53

AIM 8- ~~large~~ <sup>large</sup> Sample test.

Q1 Let the population mean [the amount spent by <sup>per</sup> customer in a restaurant] is 250. A sample of 100 customers selected. The sample mean is calculated is 275 and S.D is 30. Test the hypothesis that the population mean 250 or not at the level of 5% significance.

Q2 In a random sample of one thousand student it is found that 750 use blue pen. Test the hypothesis that the population proportion is 0.6 at 1% level of significance.

Sol:  
 $\rightarrow Mx = 275, SD = 30, n = 100$   
 $> Mx = 275$   
 $> SD = 30$   
 $> n = 100$   
 $> mo = 250$   
 $> z_{cal} = (Mx - Mo) / (SD / \sqrt{n})$   
 $> z_{cal}$   
 $[1] 8.333333$

cat ("Calculate the value of  $z_{1\%} = z_{cal}$ ")  
 cat ("Calculate the value of  $z_{1\%} = 8.333333$ ")  
 $> P\text{-value} = (1 - \text{pnorm}(\text{abs}(z_{cal}))) * 2$   
 $> P\text{-value}$

$[1] 0$   
 cat ("Calculate the value of  $P\text{-value}$  is 0")  
 cat ("Calculate the value of  $P\text{-value}$  is 0")

Q.2  $\pi$

$\rightarrow p = 0.8$

$p = 750/1000$

$n = 1000$

$Q: 1-p$

$z_{cal} = (p - P) / (\sqrt{P * Q / n})$

$z_{cal}$

$> -3.952847$

$\text{cat}(\text{"calculate } z_{cal} = ", z_{cal})$

$z_{calculated} z_{cal} = -3.952847$

$p\text{-value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{cal})))$

$p\text{-value}$

$[2] 7.72268e-05$

$\text{cat}(\text{"calculate pvalue is = ", pvalue})$

$\text{calculate pvalue is } = 7.72268e-05$

Q.3 Two random sample of size 1000 and 2000 are drawn from two population with the same standard deviation 2.5. The sample mean are 67.5 and 68 respectively. Test the hypothesis  $H_0: \mu_1 = \mu_2$  against  $H_1: \mu_1 \neq \mu_2$  at 5% level of significance.

Q.4 A study of noise level in two hospital given below. Test the claim that of two hospital have same level of noise and 1% of level of significance.

	Hospital A	Hospital B
Size	84	34
mean	61.2	59.4
S.D	7.9	7.5

Q.5 In a sample of 600 student in a college 400 use blue ink. In another college 54 for a sample of 900 student 450 use blue ink. Test the hypothesis that the proportion of student using blue ink in two college are equal or not at 1% level of significance.

$H_0: \mu_1 = \mu_2$

$H_1: \mu_1 \neq \mu_2$

$n_1 = 1000$

$n_2 = 2000$

$\bar{x}_1 = 67.5$

$\bar{x}_2 = 68$

$s_{d1} = 2.5$

$s_{d2} = 2.5$

$z_{cal} = (\bar{x}_1 - \bar{x}_2) / \sqrt{(s_{d1}^2/n_1) + (s_{d2}^2/n_2)}$

$z_{cal}$

$[2] 5.163978$

$\text{cat}(\text{"calculate } z_{cal} \text{ is = ", } z_{cal})$

$\text{calculate } z_{cal} \text{ is } = 5.163978$

$p\text{-value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{cal})))$

$p\text{-value}$

$[2] 2.417564e-05$

$\text{cat}(\text{"calculate pvalue is = ", pvalue})$

$\text{calculate pvalue is } = 2.417564e-05$

$\therefore H_0$  is rejected

Q.4

$H_0: \mu_1 = \mu_2$

$H_1: \mu_1 \neq \mu_2$

$n_1 = 84$

$n_2 = 34$

$\bar{x}_1 = 61.2$

$\bar{x}_2 = 59.4$

```

> s01 = 7.9
> s02 = 7.5
> zcal = (m1 - m2) / sqrt((s01^2/n1) + (s02^2/n2))
> zcal
[1] 1.1628528
> pvalue = (1 - pnorm(abs(zcal)))
> pvalue
[1] 0.245021
> cat("calculate pvalue = ", pvalue)
> calculate pvalue = 0.245021
It is accepted because it is less than 0.05

```

0.5

→  $H_0: P_1 = P_2$  against  $H_1: P_1 \neq P_2$

```

> n1 = 600
> n2 = 900
> p1 = 400/600
> p2 = 450/900
> p = (n1 * p1 + n2 * p2) / (n1 + n2)
> p
[1] 0.5666667

```

```

> q = 1 - p
> zcal = (p1 - p2) / sqrt(p * q * (1/n1 + 1/n2))
> zcal
[1] 0.01772648
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 1.753222e-10

```

```

> cat("calculate pvalue = ", pvalue)
[1] 1.753222e-10
It is rejected it is less than 0.01

```

```

H0: P1 = P2 against H1: P1 ≠ P2
> n1 = 200
> n2 = 200
> p1 = 44/200
> p2 = 30/200
> p = (n1 * p1 + n2 * p2) / (n1 + n2)
> p
[1] 1.85

```

```

> q = 1 - p
> zcal = (p1 - p2) / sqrt(p * q * (1/n1 + 1/n2))
> zcal
[1] 1.802741

```

```

> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 0.07142888

```

```

> cat("calculate pvalue = ", pvalue)
calculate pvalue = 0.07142888
It is accepted because it is more than 0.05

```

2.3.07.20



Practical: 7Aim 8 - Sample Sample Test

Q1. The marks of 10 student are given by  
63, 63, 66, 67, 68, 69, 70, 70, 71, 72.  
Test the hypothesis that the sample comes  
from population with average marks 66 at  
5% level of significance.

→  $H_0: \mu = 66$

>  $x = c(\dots)$

>  $t = \text{test}(x)$

data: x

$t = 68.319$ ,  $df = 9$ ,  $p\text{-value} = 1.558e-13$

alternative hypothesis: true mean is not equal  
to 0.5% confidence interval.

65.65171 70.1432

Sample estimates:

mean of x

67.9

> Since value of p is less than 0.05  
we reject the  $H_0: \mu = 66$ .

>  $\text{los} = 0.05$

>  $p\text{-value} = 1.558e-13$

> if ( $p\text{-value} > 0.05$ ) {cat("accept  $H_0$ ")} else {cat("reject  $H_0$ ")}

reject  $H_0$ .

Q2. 2 groups of student score following marks.  
Test the hypothesis that there is no significant  
difference between the 2 groups.

GP1: 18, 22, 21, 17, 20, 17, 23, 20, 22, 21

GP2: 16, 20, 24, 21, 20, 18, 13, 15, 17, 21. 56

→  $H_0$  there is no difference between two groups.

>  $x = c(\dots)$

>  $y = c(\dots)$

>  $t = \text{test}(x, y)$

data: x and y.

$t = 2.2573$ ,  $df = 16.376$ ,  $p\text{-value} = 0.03798$ .

Alternate hypothesis: true difference is means is not  
equal to 0. 5 percent confidence interval.

0.1628205 5.0371795

Sample estimates:

mean of x mean of y

20.1 17.5

>  $\text{los} = 0.05$

>  $p\text{-value} = 0.03798$

> if ( $p\text{-value} > 0.05$ ) {cat("accept  $H_0$ ")} else {cat("reject  $H_0$ ")}

reject  $H_0$ .

Q3. The sales of 6 shop before & After a special  
campaign given below:-

before: 53, 28, 37, 48, 50, 42.

After: 80, 29, 30, 55, 56, 45

Test the hypothesis that Campaign is effective or not.

→  $H_0$  there is no significance difference of sales  
before and after campaign.

> x = c(1, 1, 1, 1, 1)

> y = c(1, 1, 1, 1, 1)

> t.test(x, y, paired=T, alternative="greater")  
paired t-test

data: x and y

t = -2.7815, df = 5, p-value = 0.9806

alternative hypothesis: true difference in means is greater than 0.95 percent confidence interval

-6.03545 in f

sample estimates:

mean of differences  
-3.5

> los = 0.05

> pvalue = 0.9806

> if (Pvalue > 0.05) {cat("accept H0")} else {cat("reject H0")}

reject H0

Q4. Two medicines are apply to 2 groups of patient respectively.

Group 1: 10, 12, 13, 11, 14

Group 2: 8, 9, 12, 14, 15, 10, 9

Is there any significance difference between 2 medicine

→ No there is no significance difference between medicine and patient

> x = c(1, 1, 1, 1, 1)

> y = c(1, 1, 1, 1, 1)

> t.test(x, y)

> pvalue = 0.4406

> if (Pvalue > 0.05) {cat("accept H0")} else {cat("reject H0")}

accept H0

∵ pvalue is less than 0.05 we reject H0.  
No there is no significance difference between weight after and before.

Q5. The following are the weight before and after diet program. Is a diet program effective  
before: 120, 125, 115, 130, 123, 119  
After: 100, 114, 95, 90, 115, 99

→ No there is no significance difference between weight after and before

> x = c(1, 1, 1, 1, 1)

> y = c(1, 1, 1, 1, 1)

> t.test(x, y, paired=T, alternative="less")

> pvalue = 0.9963

> if (Pvalue > 0.05) {cat("accept H0")} else {cat("reject H0")}

accept H0

∵ pvalue is greater than 0.05 we accept H0

pt

### Practical: 08 Large and Small test:

Q.1

→  $H_0: \mu = 55$ 

Q.1 The arithmetic mean of a sample of 100 items from a large population is 52. If the standard is 7, test the hypothesis that the population mean is 55 against the alternative it is more than 55 at 5% LOS.

Q.2 In a big city 350 out of 700 males are found to be smokers. Does the information supports that exactly half of the males in the city are smokers? Test at 1% LOS.

Q.1  
→  $H_0: \mu = 55$   
→  $H_1: \mu > 55$

→  $n = 100$ →  $\bar{Mx} = 52$ →  $M_0 = 55$ →  $sd = 7$ →  $Z_{cal} = (\bar{Mx} - M_0) / (sd / (\sqrt{n}))$ →  $Z_{cal}$ [2]  $-4.285714$ → cat('calculate  $Z_{cal}$  is =',  $Z_{cal}$ )calculate  $Z_{cal}$  is =  $-4.285714$ .→  $pvalue = 2 * (1 - \text{pnorm}(\text{abs}(Z_{cal})))$ →  $pvalue$ [3]  $1.82153e-05$ → cat('calculate  $pvalue$  is =',  $pvalue$ )calculate  $pvalue$  is =  $1.82153e-05$ ∴  $pvalue$  is less than  $0.05$ ∴  $H_0$  is reject at 5% level of significance.

Q.2

→  $H_0: p = 0.5$ →  $n = 700$ →  $p = 0.5$ →  $p = 350/700$ →  $q = 1 - p$ →  $Z_{cal} = (p - P) / (\sqrt{P * q / n})$ →  $Z_{cal}$ → cat('calculate  $Z_{cal}$  is =',  $Z_{cal}$ )calculate  $Z_{cal}$  is = 0→  $pvalue = 2 * (1 - \text{pnorm}(\text{abs}(Z_{cal})))$ →  $pvalue$ 

[2] 1

∴  $H_0: P = 15\%$   
 $H_0$  is accepted at 1% level of significance

Q3.

Let

→  $n_1 = 1800$

→  $n_2 = 1500$

→  $p_1 = 0.02$

→  $p_2 = 0.01$

→  $P = (n_1 \times p_1 + n_2 \times p_2) / (n_1 + n_2)$

→  $P$

0.014

→  $q = 1 - P$

0.986

→  $z_{cal} = (p_1 - p_2) / \sqrt{P \times q \times (1/n_1 + 1/n_2)}$

→  $z_{cal}$

2.02892

→  $z_{tab}$  (calculate  $z_{cal}$ ,  $z_{tab}$ )

calculate  $z_{tab}$  2.02642

→  $P\text{-value} = 2 \times [1 - \text{Pnorm}(\text{abs}(z_{cal}))]$

→  $P\text{-value}$

0.0370886

→  $z_{cal}$  (calculate  $P\text{-value}$ ,  $P\text{-value}$ )

calculate  $P\text{-value}$  0.0370886

∴  $H_0$  is rejected for  $\alpha = 0.05$

∴  $H_0$  is accepted at 1% level of significance

Q4.

→  $H_0: \mu = 99$

→  $n = 400$

→  $\mu = 99$

→  $\sigma = 100$

→  $d = 9$

→  $z_{cal} = (\bar{x} - \mu) / (\sigma / \sqrt{n})$

→  $z_{cal}$

2.5

Q3. Thousand article from a factory-A are found to have 2% defectives. 1500 articles from a 2nd factory-B are found to have 1% defective. Test at 5% LOS that the two factory are similar or not.

Q4. A sample of size 400 was drawn at a sample mean is 99. Test at 5% LOS that the sample comes from a population with mean 100 and variance 64.



Q.5. The flower stems are selected and the heights are found to be (cm) 63, 63, 68, 69, 71, 71, 72. Test the hypothesis that the mean height is 66 or not at 1% LOS.

Q.6. Two random samples were drawn from 2 normal populations and their values are A- 66, 67, 75, 76, 82, 84, 88, 90, 92 B- 64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97. Test whether the population have the same variance at 5% LOS.

7 pvalue = cat("calculate zcal", zcal)  
 calculate zcal = 2.5  
 7 pvalue = 2 \* (1 - pnorm(abs(zcal)))  
 7 pvalue  
 [1] 0.01241933  
 7 cat("calculate pvalue", pvalue)  
 calculate pvalue = 0.01241933  
 ∴ pvalue is less than 0.05  
 ∴ H<sub>0</sub> is rejected at 5% level of significance.

Q.5 H<sub>0</sub>:  $\mu = 66$   
 $\rightarrow \chi^2 ( \dots )$   
 7 t-test (n)  
 one sample t-test

data: x  
 t = 48.94, df = 6, p-value = 5.522e-09  
 alternative hypothesis: true  $\mu$  is not equal to 66  
 95 percent confidence interval:  
 64.66479 71.62692  
 Sample estimates:  
 mean of x  
 68.14286  
 > los = 0.01  
 > if (pvalue > 0.01) { cat("accept H<sub>0</sub>") } else { cat("reject H<sub>0</sub>") }  
 [2] "Reject H<sub>0</sub>".

Q.6 H<sub>0</sub>:  $\sigma_1^2 = \sigma_2^2$   
 $\rightarrow \chi^2 ( \dots )$   
 $\rightarrow y = ( \dots )$   
 var.test(x, y)

F test to compare two variances  
 data: x and y  
 F = 0.70686, num df = 8, denom df = 10, p-value = 0.638

alternate hypothesis: true ratio of variance is not equal to 1

95 percent confidence interval:

0.1873 662 3 0.360383

sample estimation:

ratio of variance 0.306567

$\alpha = 0.05$

$\Rightarrow$  if (pvalue > 0.05) then accept  $H_0$  else reject  $H_0$

> reject  $H_0$

$H_0: \mu = 1200$   $H_1: \mu \neq 1200$

$n = 100$

$\bar{x} = 1150$

$s.d = 125$

$z_{cal} = (x - \mu) / (s.d / \sqrt{n})$

$z_{cal} = (1150 - 1200) / (125 / \sqrt{100})$

$z_{cal} = -4$

$z_{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z_{cal})))$

$z_{pvalue} = 0.000124$

$0.000124 < 0.05$

$\therefore$  pvalue less than 0.05

$\therefore H_0$  is rejected the value at 5% level of significance

Q.8

$n_1 = 200$

$n_2 = 300$

$p_1 = 44/200$

$p_2 = 56/300$

$\bar{p} = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$

$z_{cal} = (p_1 - p_2) / \sqrt{\bar{p}(1 - \bar{p}) * (1/n_1 + 1/n_2)}$

$z_{cal} = (0.22 - 0.1867) / \sqrt{0.2033 * (1/200 + 1/300)}$

$z_{cal} = 1.14$

7. A company producing light bulbs finds that mean life span of the population of bulbs is 1200 hours with s.d. 125. A sample of 100 bulbs have mean 1150 hours. Test whether the difference between population and sample mean is significantly different?

8. From each of two consignments of apples, a sample of size 200 is drawn and number of bad apples are counted. Test whether the proportion of rotten apples in two assignments are significantly different at 1% LOS?

	Sample size	No. of bad apples
Consignment 1	200	44
Consignment 2	300	56

Test (2) 0.9128709

~~7 pvalue = (1 - pnorm(abs(zcal))) \* 2~~

62

7 pvalue = 2 \* (1 - pnorm(abs(zcal))) \*

7 pvalue

(2) 0.3613101

∴ pvalue is less greater than 0.05

∴ Ho is accepted the value at 5% level of significance.

*Am*

## Problem 2: Chi-Square test & ANOVA (Analysis of Variance)

Q1: Use the following data to test whether the condition of home & condition of child are independent or not.

Cond. Child	Cond. Home	
clean	clean	dirty
	70	50
fairly clean	80	20
dirty	35	45

H0: Condition of Home & child are independent

> x = c(70, 80, 35, 50, 20, 45)

> m = 3

> n = 2

> y = matrix(x, nrow = m, ncol = n)

> y

	[1,]	[1,2]
[1,]	70	50
[2,]	80	20
[3,]	35	45

> pv = chisq.test(y)

> pv

Pearson's Chi-Squared test  
data: y

Chi-Squared = 25.646

df = 2

p-value = 2.698e-06

// They are dependent.

As p-value is less than 0.05 we reject the hypothesis at 5% level of significance.

Q2: Test the hypothesis that vaccination & diseases are independent or not.

	Vaccine	
Disease	Affected	Not-Affected
Affected	30	46
Not-affected	35	37

H0: Disease & Vaccine are independent

> x = c(30, 35, 46, 37)

> m = 2

> n = 2

> y = matrix(x, nrow = m, ncol = n)

> y

	[1,]	[1,2]
[1,]	30	46
[2,]	35	37

> pv = chisq.test(y)

> pv

Pearson's Chi-Squared test with Yates  
continuity correction



data: y

$r^2\text{-square} = 2.0235$

$df = 2$

$p\text{-value} = 0.1545$

$\therefore p\text{-value}$  is more than 0.05, we accept the hypothesis at 5% level of significance  
// They are INDEPENDENT

Q3 Perform a ANOVA for the following data.

TYPE	OBSERVATIONS
A	50, 52
B	53, 55, 53
C	60, 58, 52, 56
D	52, 54, 54, 55

Ho: The mean's are equal for A, B, C, D.

$x_1 = (50, 52)$

$x_2 = (53, 55, 53)$

$x_3 = (60, 58, 52, 56)$

$x_4 = (52, 54, 54, 55)$

$d = \text{stack}(\text{list}(b1=x_1, b2=x_2, b3=x_3, b4=x_4))$

$\text{names}(d)$

$[1] \text{"value"} \text{"ind"}$

$\text{one way.test}(\text{value} \sim \text{ind}, \text{data} = d, \text{var.equal} = T)$

One-way analysis of means

data: value and ind

$F = 11.735$   $df = 3$   $\text{denom df} = 9$   $p\text{-value} = 0.008$

$\therefore p\text{-value}$  is less than 0.05 we reject the hypothesis

$\text{anova} = \text{aov}(\text{value} \sim \text{ind}, \text{data} = d)$

$\text{summary}(\text{anova})$

	DF	Sum	Mean Sq	F value
ind	3	21.06	23.687	11.73
Residuals	9	18.12	2.019	

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Q4 Following data gives a life of times of 4 brands.

Type	Life
A	20, 23, 18, 2, 18, 22, 24
B	18, 15, 17, 20, 16, 14
C	21, 19, 22, 17, 20
D	15, 14, 18, 18, 14, 16

Ho: The mean's of A, B, C, D are equal

$x_1 = (20, 23, 18, 2, 18, 22, 24)$

$x_2 = (18)$

$x_3 = (11)$

$x_4 = (10)$

$d = \text{stack}(\text{list}(b1=x_1, b2=x_2, b3=x_3, b4=x_4))$

$\text{names}(d)$

$[1] \text{"value"} \text{"ind"}$

$\text{one way.test}(\text{value} \sim \text{ind}, \text{data} = d, \text{var.equal} = T)$

One-way analysis of means

data: value & ind

$F = 6.8445$   $\text{num df} = 3$   $\text{denom df} = 20$

$p\text{-value} = 6.002349$

∴ p-value is less than 0.05 we reject the hypothesis

anova = aov (value ~ nd, data = d)

→ summary (anova)

	df	sumsq	meansq
md	3	91.94	30.647
Residuals	20	89.06	4.453

signif. code: 0.001 '\*\*\*' 0.01 '\*\*' 0.05 '\*' 0.1 '.' 1 ''

→ read.csv ("C:/Users/admin/Desktop/marks.csv")

→ x

	Stats	Maths
1	60	60
2	45	48
3	42	47
4	15	20
5	37	25
6	36	27
7	49	37
8	59	58
9	20	25
10	27	27

→ am = mean (x\$Stats)

→ am

→ 37

→ am1 = mean (x\$Maths)

→ m1 = median (x\$Stats)

→ m1

→ 38.5

→ m2 = median (x\$Maths)

→ 37

→ n = length (x\$Stats)

→ n

→ 10

→ sd = sqrt ((n-1) \* var (x\$Stats) / n)

→ sd

→ 12.64911

→ n1 = length (x\$Maths)

→ n1

→ 10

→ sd1 = sqrt ((n1-1) \* var (x\$Maths) / n1)

→ sd1

→ 15.2

→ cor (x\$Stats, x\$Maths)

→ 0.830618

0.27

## PRACTICAL: 10

### Topic: Non-parametric test

Q1. Following are the amount of Sulphur dioxide emitted by industry in 20 days. Apply sign test to test the hypothesis that the population median is 21.5 at 5% level of significance?

17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20,  
17, 6, 24, 14, 15, 23, 24, 26

$H_0$ : population median is 21.5

$x = ( \dots )$

$me = 21.5$

$sp = \text{length}(x[x > me])$

$sn = \text{length}(x[x < me])$

$n = sp + sn$

$n$

23 20

$pV = \text{pbinom}(sp, n, 0.5)$

$pV$

0.4119015

$\therefore pV$  is more than 0.05

$\therefore$  we accept the hypothesis at 5% level of significance.

[Note: if the Alternative is (4) median not equal to something  $H_1: me > 0.01$  equal to  $me < \dots$   $pV = \text{pbinom}(n, n, 0.5)$ ]

Following is a list of 10 observation apply sign test, to test the hypothesis that the population median is 625 against the Alternative it is more than 625.

$x = 612, 619, 631, 628, 643, 640, 655, 649, 670, 663$

$H_0$ : Median is 625

$x = ( \dots )$

$me = 625$

$sp = \text{length}(x[x > me])$

$sn = \text{length}(x[x < me])$

$n = sp + sn$

$n$

10

$pV = \text{pbinom}(sp, n, 0.5)$

$pV$

0.0546875

$\therefore$  the  $pV$  is more than 0.05

$\therefore$  the hypothesis is accept at 5% level of significance.

Q2. Following are value of the factor sample test the hypothesis that the population median is 60 against the Alternative it is more than 60 at 5% level using Wilcoxon Signed Rank Test.

$x = 63, 65, 60, 89, 61, 71, 58, 51, 69, 62, 63, 39, 72, 69, 48, 66, 72, 63, 87, 69$

$H_0$ : population median = 60

$H_1: \dots > 60$

$x = ( \dots )$

$\rightarrow$  wilcox.test( $x$ , ~~data~~  $\text{alternative} = "greater"$ ,  $mu = 60$ )

Wilcoxon signed rank test with continuity correction.

data: x

$V = 145$ ,  $p\text{-value} = 0.02298$

alternative hypothesis: true location is greater than 60

Note: If the alternative is "less" and if alternative is not equal to then we prefer "two sided".  
~~alt = "less"~~ or ~~alt = "two sided"~~

Q.4. Using WSR test the population median is 12 or less than 12.

$x = 15, 17, 24, 25, 20, 21, 32, 28, 12, 25, 24, 26$

$H_0$ : population median is 12

$x = ( \dots )$

$> \text{wilcox.test}(x, \text{alt} = "less", \mu = 12)$

Wilcoxon signed rank test with continuity correction

data: x

$V = 66$ ,  $p\text{-value} = 0.9986$

alternative hypothesis: true location is less than 12.

Q.5. The weights of students before and after they stop smoking are given below. Using WSR test that there is no significance change.

weight before

65

75

78

62

72

weight after

72

74

72

66

$H_0$ : before and after there is no change

$H_1$ : there is change.

$x = (65, 72, 75, 62, 72)$

$y = (72, 74, 72, 66, 78)$

$d = x - y$

$[d] = 1 \ 3 \ -4 \ -1$

Wilcoxon signed rank test with continuity correction.

data: d

$V = 4.5$ ,  $p\text{-value} = 0.4082$

alternative hypothesis: true location is not equal to 0.

Ans  
27-2-20