



# Regression: Representation Space

Paper Reading by Yunyan Yan



- **Background**
- Regression Metric Loss
- LARGE: Latent-Based Regression
- OrdinalCLIP
- Conclusion

# Background

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## □ Regression

### ⊙ 任务场景:

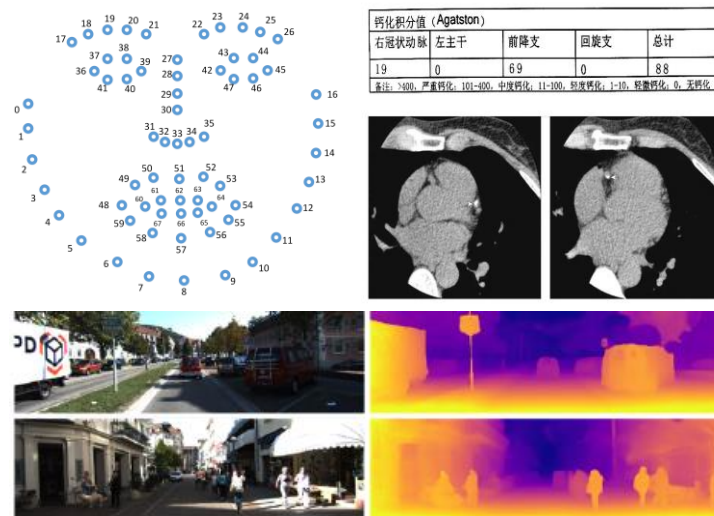
- 关键点、年龄/骨龄、单目深度
- (有序回归)病情等级、审美/评价

### ⊙ 现有方法:

- L1 & L2
- 特定先验(人脸关键点)
- 转化为分类任务

### ⊙ 问题:

- 高维特征表示+全连接 ---> 过拟合、难解释
- 特定先验 ---> 难迁移
- 分类 ---> 忽略序数关系



**一个合适的低维特征空间**

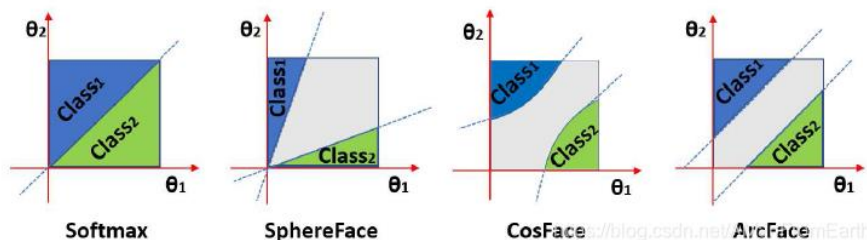
# Background

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## □ Metric Learning ---- 向量空间的映射

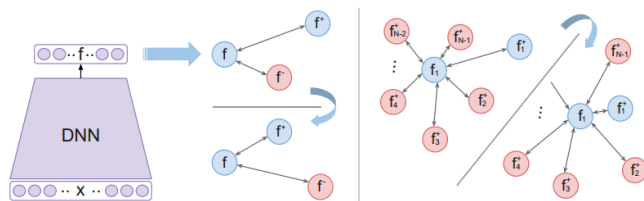
### ⊙ Proxy-based methods

- 基于分类标签
- L2-Softmax、CosFace、ArcFace



### ⊙ Pairwise-based methods

- 基于样本对
- Contrastive loss、Triplet loss、N-pair loss

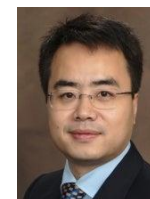




- Background
- **Regression Metric Loss**
  - ⊙ Motivation
  - ⊙ Methodology
  - ⊙ Experimental results
- LARGE: Latent-Based Regression
- OrdinalCLIP
- Conclusion

## Regression Metric Loss: Learning a Semantic Representation Space for Medical Images

Hanqing Chao, Jiajin Zhang, and Pingkun Yan(✉)



Department of Biomedical Engineering, Center for Biotechnology  
and Interdisciplinary Studies, Rensselaer Polytechnic Institute, Troy, NY 12180, USA  
{chaoh,zhangj41,yanp2}@rpi.edu

MICCAI 2022

伦斯勒理工学院 生物医学工程



# Motivation

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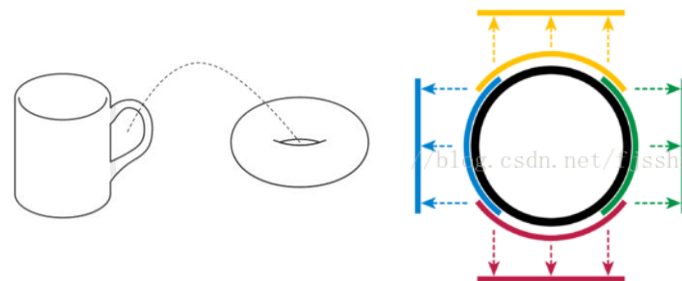
- 现有问题
  - ⊙ 高维特征缺乏可解释性
  - ⊙ 空间内在结构不明
- 本文目的
  - ⊙ 有语义的特征表示空间
  - ⊙ 与标签空间等距的低维流形
- 具体实现
  - ⊙ 表示空间的测地距离与标签空间的欧氏距离成正比
  - ⊙ 根据流形上NN计算回归结果，代替全连接层

# Methodology

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## □ Riemannian Manifold

- ⊙ 微分流形+内积
- ⊙ 局部同胚于欧氏空间  $\mathbb{R}^n$



## □ Regression Metric Loss (RM-Loss)

- ⊙ 表示空间的测地距离  $\propto$  标签空间的欧氏距离

$$D_{ij}^o = |s \times G(\mathbf{f}_i, \mathbf{f}_j) - \|\mathbf{y}_i - \mathbf{y}_j\|_2|$$

- ⊙ 局部同胚 ---> 相同拓扑结构 ---> 测地距离  $\approx$  欧氏距离

$$G(\mathbf{f}_i, \mathbf{f}_j), \mathbf{f}_j \in \mathcal{N}(\mathbf{f}_i) \quad \|\mathbf{f}_i - \mathbf{f}_j\|_2$$

$$D_{ij} = |s \times \|\mathbf{f}_i - \mathbf{f}_j\|_2 - \|\mathbf{y}_i - \mathbf{y}_j\|_2|, \quad w_{ij} = \exp\left(-\frac{\|\mathbf{y}_i - \mathbf{y}_j\|_2^2}{2\sigma^2}\right) + \alpha$$

$$l' = \frac{\sum_{i=1}^N \sum_{j=1}^N w_{ij} D_{ij}}{\sum_{i=1}^N \sum_{j=1}^N w_{ij}},$$

邻域大小    流形曲率





# Methodology

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## □ Regression Metric Loss (RM-Loss)

### ⊙ 难样本挖掘(类似于ACSL)

$$m_{ij} = \begin{cases} 1, & \text{if } w_{ij}D_{ij} > \bar{l}^{(k)} \\ 0, & \text{if } w_{ij}D_{ij} \leq \bar{l}^{(k)} \end{cases}, \quad \bar{l}^{(k)} = 0.9 \times \bar{l}^{(k-1)} + 0.1 \times \mathbb{E}^{(k)}(w_{ij}D_{ij})$$

$$\mathcal{L} = \frac{\sum_{p=1}^N \sum_{q=1}^N m_{ij} w_{ij} D_{ij}}{\sum_{p=1}^N \sum_{q=1}^N m_{ij} w_{ij}}$$

### ⊙ 推理阶段

■ 微分同胚：邻域  $\mathcal{N}^M(f_i) \subseteq M$      $\mathcal{N}^Y(y_i) \subseteq Y$  一一映射

■ NN：测试样本的欧式邻域内，取训练样本加权

$$\hat{y}_t = \frac{\sum_{f_i \in \mathcal{N}_r(f_t)} a_i y_i}{\sum_{f_i \in \mathcal{N}_r(f_t)} a_i}, \quad a_i = \exp\left(-\frac{\|f_i - f_t\|_2^2}{2(r/3)^2}\right)$$

# Experimental results

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## □ Performance comparison

**Table 1.** Regression performance and quality of the learned space on the full-size BAA and CAC datasets. The best results are in bold.

Method	Regression performance				Space quality			
	BAA		CAC		BAA	骨龄	CAC	冠脉钙化
	MAE↓	R <sup>2</sup> ↑	MAE↓	R <sup>2</sup> ↑	D5↓	RV↓	D5↓	RV↓
MSE	7.021*	0.947	0.762*	0.930	8.872*	0.0690*	0.869*	0.1225*
L1	6.580*	0.952	0.668*	0.927	8.799*	0.0600	0.837*	0.1249*
OrdReg	7.061*	0.944	0.684*	0.937	9.368*	0.1450*	0.844*	0.1966*
ATrip+NN	6.799*	0.951	0.647*	0.939	9.022*	0.0617	0.834*	0.0874*
ATrip+L1	6.854*	0.949	0.660*	0.930	9.055*	0.0630*	0.855*	0.0813
RM-Loss (ours)	<b>6.438</b>	<b>0.954</b>	<b>0.617</b>	<b>0.944</b>	<b>8.614</b>	<b>0.0588</b>	<b>0.769</b>	<b>0.0806</b>

\*  $p < 0.05$  in the one-tailed paired  $t$ -test. The significant test was not applied on  $R^2$ .

度量损失+NN  
效果更好

$$1 - \rho(G_M, D_Y)$$

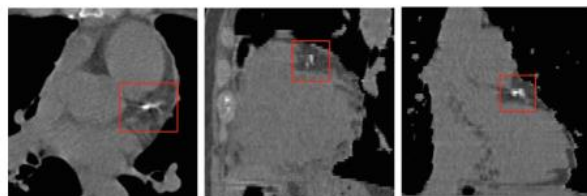
评估流形M与标签Y是否等距

Backbone: Inception-v3

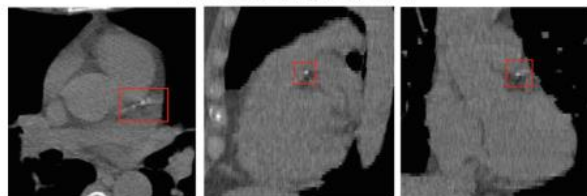
# Experimental results

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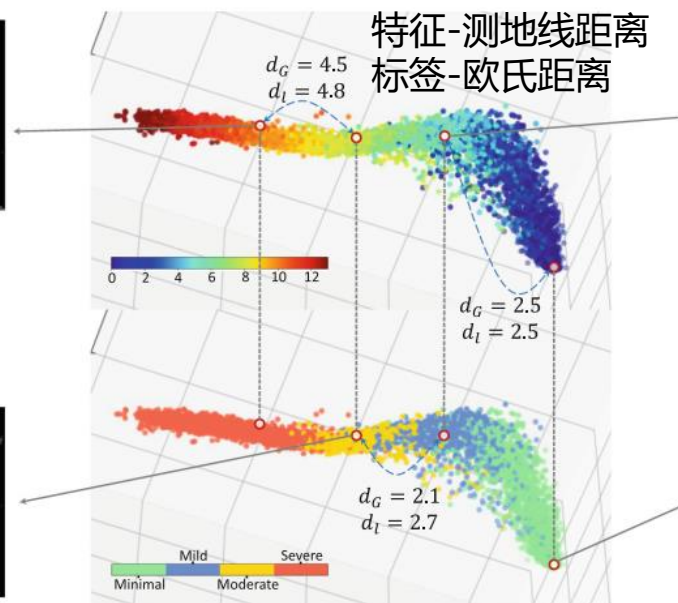
## □ Visualization on CAC



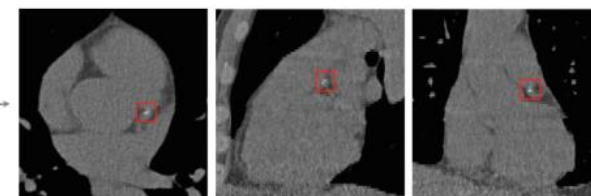
Label: 10.09, pred: 10.18  
Sever



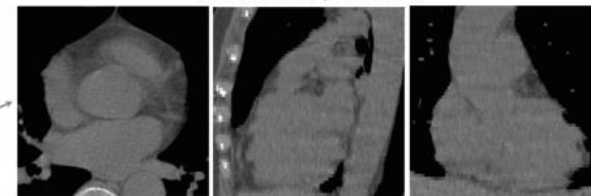
Moderate  
Label: 7.57, pred: 7.64



特征表示空间



Label: 4.84, pred: 4.93  
Mild



Minimal  
Label: 0.00, pred: 0.07

# Experimental results

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## □ Ablation Study

**Table 2.** Ablation study of  $\sigma$ ,  $\alpha$ , and  $m$  on BAA dataset. The best results are in bold.

过拟合 -----> 欠拟合 -----> 线性空间

邻域大小  
流形曲率  
难例挖掘

$\sigma$	0.25	0.5	1.0	1.5	$+\infty$	0.5			
$\alpha$	0.1					0.0	0.2	0.3	0.1
$m$	w/								w/o
MAE↓	6.555	<b>6.438</b>	6.642	6.759	6.823	6.496	6.591	6.741	6.520
$R^2 \uparrow$	0.953	<b>0.954</b>	0.952	0.951	0.950	<b>0.954</b>	0.953	0.951	0.953
D5↓	8.726	<b>8.614</b>	8.905	8.930	9.096	8.707	8.875	8.786	8.717
RV↓	0.0614	<b>0.0588</b>	0.0658	0.0659	0.0699	0.0650	0.0614	0.0677	0.0641

- ⊙  $\sigma$ 的取值非常接近临床诊断边界：骨龄(24 m;  $\sigma=0.5$ , 20.6 m); CAC(10;  $\sigma=1.5$ , 8)
- ⊙  $\alpha$ 全局控制曲率

# Experimental results

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## □ Performance on 10%-size datasets

**Table 3.** The regression performance and the learned space quality on the 10%-size BAA and CAC dataset with the best results in bold.

Method	Regression performance				Space quality			
	10% BAA		10% CAC		10% BAA		10% CAC	
	MAE↓	$R^2$ ↑	MAE↓	$R^2$ ↑	D5↓	RV↓	D5↓	RV↓
MSE	8.721*	0.917	0.946*	0.895	11.204*	0.1054*	1.102*	0.1706*
L1	9.173*	0.906	0.875*	0.894	11.682*	0.1133*	1.028*	0.1529*
OrdReg	9.226*	0.908	0.849*	0.906	11.821*	0.2485*	1.010*	0.2189*
ATrip+NN	8.733*	0.911	0.861*	0.907	10.990	0.1018*	1.056*	0.1547*
ATrip+L1	9.017*	0.914	0.875*	0.908	11.208*	0.1016*	1.012*	0.1142
RM-Loss (ours)	<b>8.071</b>	<b>0.926</b>	<b>0.797</b>	<b>0.912</b>	<b>10.974</b>	<b>0.0878</b>	<b>0.971</b>	<b>0.1114</b>

\*  $p < 0.05$  in the one-tailed paired  $t$ -test. The significant test was not applied on  $R^2$ .



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## **LARGE: Latent-Based Regression through GAN Semantics**

Yotam Nitzan\*  
Tel-Aviv University

Rinon Gal\*  
Tel-Aviv University

Ofir Brenner  
Tel-Aviv University

Daniel Cohen-Or  
Tel-Aviv University



CVPR 2022

以色列特拉维夫大学

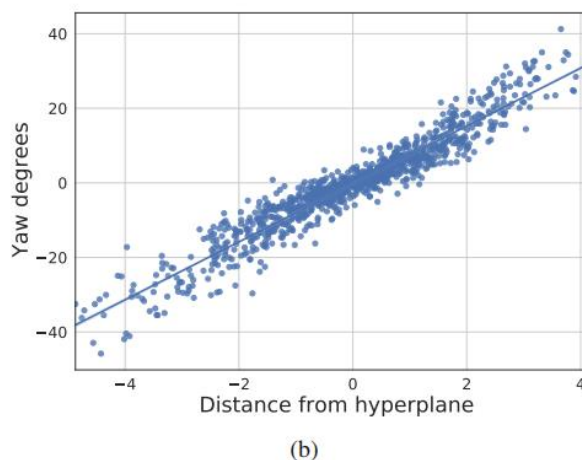
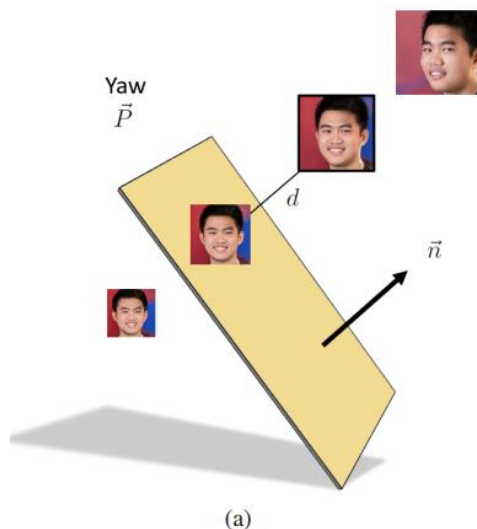


# Motivation

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## □ 特征表达空间

- ⊙ GAN--图像编辑：语义解耦
- ⊙ GAN--潜在空间：成功的语义信息编码



## □ 本文思路

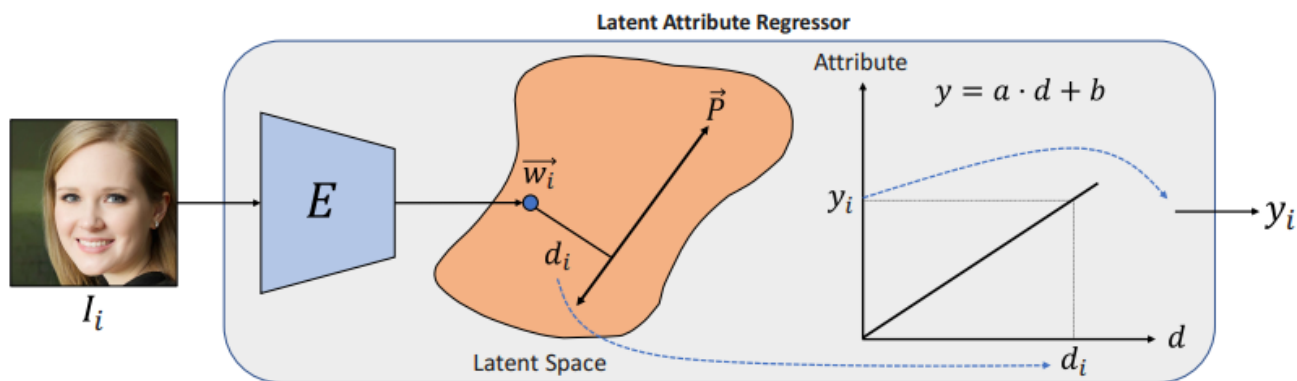
- ⊙ 微调预训练GAN模型，校准距离，沿属性方向回归



# Methodology

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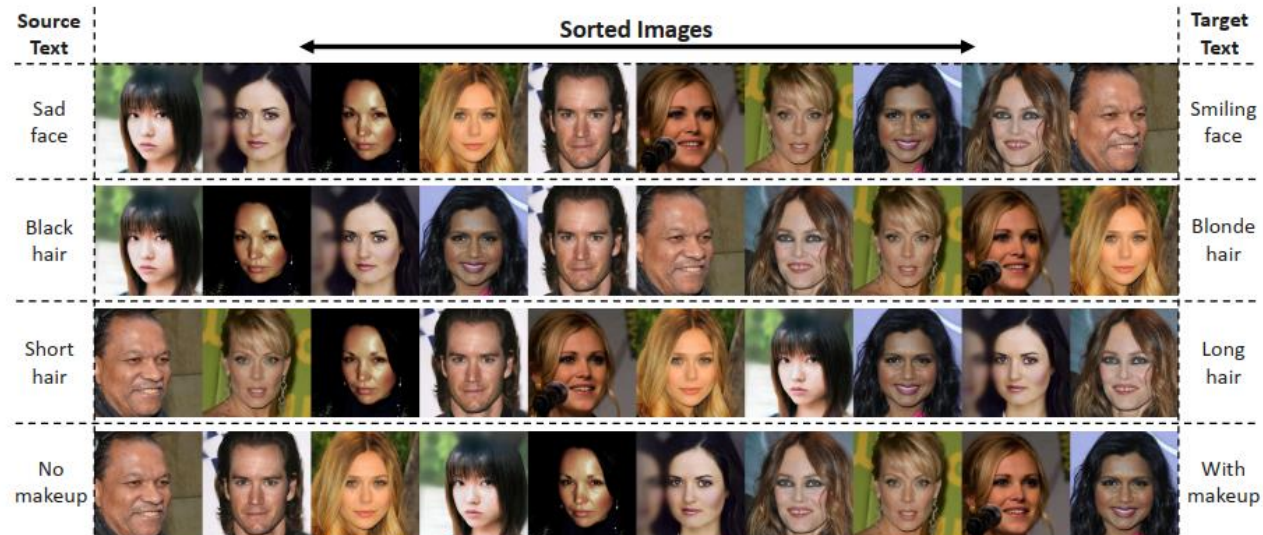
## □ Latent-based Regression



- ◉ 编码到超平面的距离
- ◉ StyleGAN的四个隐空间：高斯先验，GAN映射，每层分配，仿射变换  $\mathcal{Z}, \mathcal{W}, \mathcal{W}+$  and  $\mathcal{S}$
- ◉ 不同层表达不同属性，对每层学习权重(不同层梯度平均幅度)

# Visualization

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- Background
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## OrdinalCLIP: Learning Rank Prompts for Language-Guided Ordinal Regression

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Wanhua Li<sup>\*,1</sup>, Xiaoke Huang<sup>\*,1</sup>, Zheng Zhu<sup>2</sup>, Yansong Tang<sup>1</sup>, Xiu Li<sup>1</sup>, Jie Zhou<sup>1</sup>, Jiwen Lu<sup>†,1</sup>

<sup>1</sup>Tsinghua University <sup>2</sup>PhiGent Robotics

wanhua016@gmail.com hxx21@mails.tsinghua.edu.cn

zhengzhu@ieee.org {tang.yansong, li.xiu}@sz.tsinghua.edu.cn

{jzhou, lujiwen}@tsinghua.edu.cn



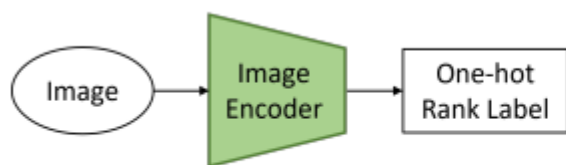
NIPS 2022

清华大学 鲁继文

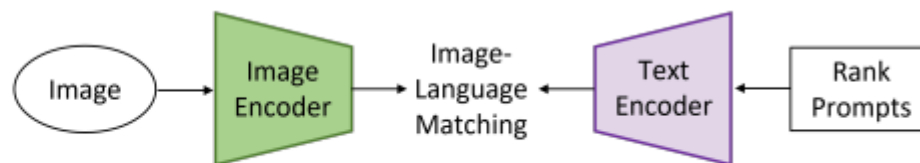
# Motivation

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- 任务
  - ⊙ 有序分类
- 现有方法：
  - ⊙ 连续 ---> 离散
  - ⊙ 全连接层建模序数
- 本文思路
  - ⊙ 语言先验学习分级概念
  - ⊙ CLIP隐空间，图像-语言对齐，共同约束概念学习缓解过拟合



(a) Existing Methods for Ordinal Regression

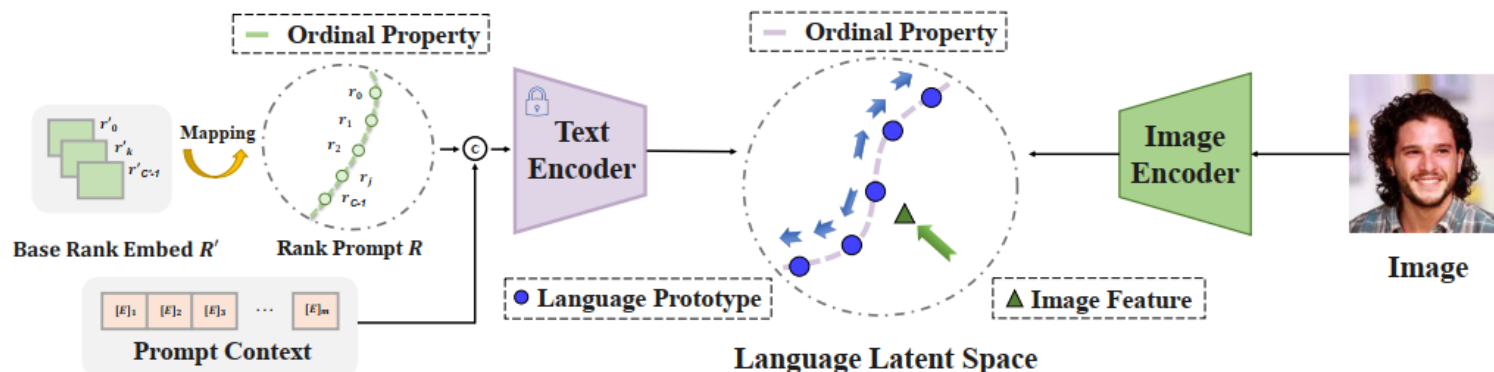


(b) Language Powered Paradigm for Ordinal Regression (Ours)

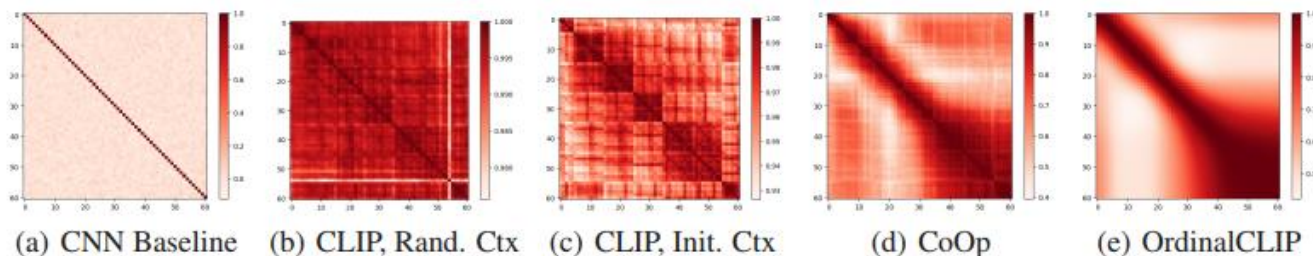
# Methodology

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## OrdinalCLIP



- 语言模型固定(推理时无需使用), 图像编码可学习
- 内积计算相似度, KL散度约束接近单位阵
- 上下文可学习, 序数插值嵌入
- CLIP直接用于序数回归的效果较差(人工prompt序数关系差)







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# Conclusion

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- 特征表示空间
  - ⊙ 度量学习约束
  - ⊙ 具有优秀性质的预训练模型隐空间
    - GAN
    - CLIP





# Thanks for Attention!