#### 1

# Assignment 3

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Abstract—This document uses the properties of a parallelogram to prove a statement

Download latex-tikz codes from

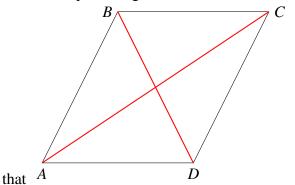
https://github.com/AddagallaSatyanarayana/AI5006/tree/master/Assignment3/assignment3.tex

## 1 Problem

Prove that the sum of the squares of diagonals of parallelogram is equal to the sum of the squares of its sides.

#### 2 Explanation

Given a parallelogram ABCD we have to prove



$$\|\mathbf{A} - \mathbf{C}\|^2 + \|\mathbf{B} - \mathbf{D}\|^2 =$$

$$\|\mathbf{A} - \mathbf{B}\|^2 + \|\mathbf{B} - \mathbf{C}\|^2 + \|\mathbf{D} - \mathbf{C}\|^2 + \|\mathbf{A} - \mathbf{D}\|^2$$
(2.0.1)

### 3 Solution

The diagonals of parallelogram are

$$A - C = (A - D) + (D - C)$$
 (3.0.1)

$$B - D = (A - D) - (A - B)$$
 (3.0.2)

The sum of the squares of diagonals is

$$\|\mathbf{A} - \mathbf{C}\|^2 + \|\mathbf{B} - \mathbf{D}\|^2 =$$

$$\|(\mathbf{A} - \mathbf{D}) + (\mathbf{D} - \mathbf{C})\|^2 + \|(\mathbf{A} - \mathbf{D}) + (\mathbf{A} - \mathbf{B})\|^2$$
(3.0.3)

$$\|\mathbf{A} - \mathbf{C}\|^{2} + \|\mathbf{B} - \mathbf{D}\|^{2} =$$

$$\|\mathbf{A} - \mathbf{D}\|^{2} + \|\mathbf{D} - \mathbf{C}\|^{2} + 2\|\mathbf{A} - \mathbf{D}\|\|\mathbf{D} - \mathbf{C}\| +$$

$$\|\mathbf{A} - \mathbf{D}\|^{2} + \|\mathbf{A} - \mathbf{B}\|^{2} - 2\|\mathbf{A} - \mathbf{D}\|\|\mathbf{A} - \mathbf{B}\| \quad (3.0.4)$$

In the parallelogram ABCD

$$\|\mathbf{A} - \mathbf{D}\| = \|\mathbf{B} - \mathbf{C}\| \tag{3.0.5}$$

$$\|\mathbf{A} - \mathbf{B}\| = \|\mathbf{D} - \mathbf{C}\| \tag{3.0.6}$$

Simplifying equation (3.0.4),(3.0.5) and (3.0.6)

$$\|\mathbf{A} - \mathbf{C}\|^2 + \|\mathbf{B} - \mathbf{D}\|^2 =$$

$$\|\mathbf{A} - \mathbf{B}\|^2 + \|\mathbf{B} - \mathbf{C}\|^2 + \|\mathbf{D} - \mathbf{C}\|^2 + \|\mathbf{A} - \mathbf{D}\|^2$$
(3.0.7)

The equations (2.0.1) and (3.0.7) are same,hence proved