## Reddit LADR Study Group Chapter 1

1.A Problem 1.

$$\frac{1}{a+bi} \cdot \frac{a-bi}{a-bi} = \frac{a-bi}{a^2+b^2} = \frac{a}{a^2+b^2} - \frac{b}{a^2+b^2}i$$

so we take  $c=\frac{a}{a^2+b^2}$  and similar for d. Note that  $a^2+b^2=|a+bi|^2$  and it is often helpful to think of complex operations in terms of the modulus. In effect what we've seen is  $1/z=\frac{\overline{z}}{z\overline{z}}=\frac{\overline{z}}{|z|^2}$ .

## 1.B

## Problem 1.

From the definitions this requires showing that  $\vec{v}$  is the element such that if added to  $-\vec{v}$  the result is  $\vec{0}$ . But this just follows again from the definition.

## 1.C

Problem 1.

(a) and (d) are subspaces, the others are not. You can rule out (b) because it does not contain  $\vec{0}$ . You can rule out (c) by additivity:  $\begin{bmatrix} 1\\1\\0 \end{bmatrix}$ ,  $\begin{bmatrix} 0\\1\\1 \end{bmatrix}$  are each in the set but their sum is not.