A Computing Data Science Perspective on Gene Splice Site Identification

Hui Chong June 21, 2020

1 Abstract

As molecular biology and information technology advances, machine learning techniques have a wide range of applications in bioinformatics. In this work, on the problem of gene splicing donor site identification, on both balanced dataset and unbalanced dataset, three models (WAM [1], BN [2,3], SVM [4,5]) are evaluated comprehensively. A set of comprehensive performance metrics were also introduced in the experiments. And to detect splice signals precisely, a correction has also made to Bayesian network. The result shows that SVM has a good ability on take caring of unbalanced data while WAM and BN do not. Besides, the fitness of metrics is also tested. It shows that auPRC [6] is more sensitive to unbalanced data and so is more applicable in many situations.

2 Brief Introduction

As molecular biology has an insight into gene regulation and RNA splicing, recognition of RNA splice site became a key problem. In the recent 2 decades, several methods have been proposed to solve the problem. But their ability of take care of unbalanced data have not been tested yet. In this work, a test of WAM, BN, SVM on both balanced data and unbalanced data were performed.

2.1 Splice Site

Splice site [7], in molecular biology, is a position on RNA where RNA splicing occurs. RNA splicing is a form of RNA processing in which a newly made precursor messenger RNA (premRNA) transcript is transformed into a mature messenger RNA (mRNA). After splicing, introns (Non-coding regions) are removed and exons (Coding Regions) are joined together.

There are donor sites (5' end) and acceptor sites (3' end) within introns [28].

2.2 Models

As Biology advances, computational methods are now the only realistic way to answer many questions in modern biology [29]. For the problem of splice site recognition, there are several models have been peoposed.

Weighted Array Model [1] is a frequency-based approach. It calculate the frequency of each adjacent bases in specific positions to fill into a weight array matrix, and use weight matrix to score unknown site. It has the ability to detect some signals like common bases amoung donors. The limitation of this approach, in a machine learning perspective, is its poor ability to automatically

calculate hidden features, like GC content. There might be much more complex features that contribute to splice signal transduction.

Bayesian Network [2,3] is a Bayesian method. It learns DAG structure and conditional probabilities distribution from the data. It has the ability to take care of dependence between positions. It also has the ability to imputate the missing value of the data. and besides, it can work like a Bayesian classifier when there is conditional probability from features to label of each sample. The limitation of this approach, is its unprecise and ineffective structure learning algorithm. PC-Constraints based learning algorithm forms loops in DAG and causes errors sometimes. MMHC algorithm is too slow when there is hundreds or thousands of nodes. Structrual expectation maximization is quite good, but still needs prior expert knowledges.

Support Vector Machine [4,5] is a mature supervised learning method. It employs support vectors to maximize the margin and kernel trick to classify linearly indivisible data. This allows for significant savings in calculations. But detecting signals via SVM is not a good choice, because over three-dimensional hyper-plane within SVM cannot be visualized and analyzed. This is the flaw of SVM in data mining, it has the ability to classify but is almost useless for human interpretation of results.

3 Material and Methods

3.1 Environment

```
[27]: import pickle
      import warnings
      import importlib
      import import_ipynb
      import numpy as np
      import pandas as pd
      import seaborn as sns
      import networkx as nx
      import matplotlib.image as pli
      from Models import WAM, BN, SVM
      from Evaluator import Evaluator
      from matplotlib import pyplot as plt
      from Utils import load_data, Summary, Validation_Sum, no_box
      from IPython.display import display, Markdown, Latex, HTML
      from matplotlib.patches import ConnectionPatch
      from mpl toolkits.axes grid1.inset locator import mark inset
      from mpl_toolkits.axes_grid1.inset_locator import inset_axes
      from pgmpy.estimators import MmhcEstimator, ConstraintBasedEstimator
      plt.ion()
      plt.style.use(['science','ieee','no-latex'])
      warnings.filterwarnings("ignore")
```

importing Jupyter notebook from Utils.ipynb

3.2 Datasets

To comprehensively compare their performances, two datasets were used as data are usually unbalanced in Biology. Models may perform differently in that way. The first dataset, which is balanced,

was used to training and testing models' performance in a general way. And the second dataset is an unbalanced dataset, was used to training and thus testing their performance like real conditions. Because unbalanced data is common in Biology and even many other fields.

Basic information of the two datasets is as follows.

```
[28]: training_set, testing_set = load_data()
    training_set1 = training_set[0:5000]
    testing_set1 = testing_set[0:5000]
    training_set2 = training_set[1500:6500].reset_index(drop=True)
    testing_set2 = testing_set[1500:6500].reset_index(drop=True)
    print(Summary(training_set1, testing_set1, training_set2, testing_set2).to_latex())
```

Table 1: Basic information of datasets

	$\mathrm{nSample}^a$	n Donor : n Pseudo b	Type
Dataset 1	10000	5278:4722	Balanced
Dataset 2	10000	2278:7722	Unbalanced

^a Number of samples in the dataset.

3.3 Feature Extraction and Encoding

To build reliable models and test their performances, high-quanlity data must be extracted. Splice site dataset, which contains 5278 donor sites and 4722 pseudo sites, was extracted from original sequence data. And only 10 bases before and after the site to be tested were extracted.

When encoding sequence features, one-hot encoder [8] was introduced. And considering simplisity of the experiments, samples with $base_{ambiguous} \in \{w, m, s, k, r, y, b, d, h, v, n, z\}$ [9] were discarded. Next, a One-hot encoder are used to encode sequence to a numeric feature vector. For instance, sequence a...t was encoded as [1, 0, 0, 0...0, 0, 0, 1]. See Preprocessing.ipynb for details.

3.4 Model Implements and Test score

The 3 models are mainly implemented using Python [10]. Besides, the Bayesian network model and Support vector machine was implemented based on Pgmpy and Scikit-learn packages [11,12]. As far as possible, these models have been designed to be practically applicable. They contain several very easy-to-use program interfaces: fit, predict_probas, predict_scores and predict_classes. For all 3 models, the fit method is used for training, and the other 3 predict methods are used for prediction. The predict_probas is used for predicting the probabilities each sample belonging to each class, the predict_scores are used for calculating the S(X), and the predict_classes are used for predicting the class to which each sample belongs, this is done by comparing the S(X) and given threshold T. Most importantly, the S(X) is calculated by:

$$S_m(X) = \ln(\frac{P_m^+(X)}{P_m^-(X)}), m \in \{wam, bn, svm\}$$
 (1)

3.5 Stratagies for WAM to perform recognition

When recognizing Gene splice site, the 3 steps were mainly used to determine the potential of each sample being a splice site. Firstly, Laplace pseudocount C_p [13] are used to smooth categorical data.

^b Proportion of donor sites and pseudo sites in the dataset.

Secondly, the weights of positive and negative submodels, which are the frequencies of adjacent base pairs in WAM, are calculated using the following formula.

$$f(x) = \frac{C_{x,p} + C_p}{N}, x \in \{aa, ac, ag, ...tt\}$$
 (2)

Where N is the total number of samples. $C_{x,p}$ is the total number of specific adjacent base pairs occurring at position p - l + 1...p in all samples. C_p is the pseudocount, and l is the length of array considered, which refers to the range of dependence between adjacent base pairs considered in experiments. And finally, the potential of unknown samples being donor sites were given by

$$S_{wam}(X) = ln(\frac{P^{+}(X)}{P^{-}(X)}) = \sum_{x=2}^{L} ln(\frac{f^{+}(x)}{f^{-}(x)})$$
(3)

Where L is the length of input sequence. Most importantly, l and C_p are set to 2 and 0.5 respectively.

3.6 Stratagies for BN to learn structures and parameters from data

To perform accurate structure and parameter learning for Bayesian network, Two algorithms were used: PC constraint-based learning algorithm [14] for structure learning and Bayesian estimation for parameters learning.

The PC algorithm learns the DAG structure in three steps [30]. First, find the graph skeleton and separating sets of removed edges. Second, orient v-structures based on separating sets. Finally, propagate orientations of v-structures to as many remaining undirected edges as possible. The Bayesian estimator then estimates conditional probability distribution for each node in the graph.

3.7 Strategies for BN to detect splice signal

Because of Bayesian inference, Bayesian network can handle the causalty between nodes. In this project, Bayesian network have been improved to be able to calculate the splicing donor potential of DNA sequences. In which both two kinds of data are retained: the feature nodes N_f , $f \in \{-10, -9, ...10\}$ and label node N_L . In the Bayesian network, each feature node has $state_f \in \{a, c, g, t\}$ and label node has $state_L \in \{0, 1\}$. To enable Bayesian network to learn conditional probability for all nodes $N \in \{N_{-10}, N_{-9}, ...N_{10}, N_L\}$, both donor sites and pseudo sites are fitted in a Bayesian network. Finally, when predicting new sites, the Bayesian network will treat new sites as sample with missing label. It uses a missing data imputation algorithm to calculate the probability of label in each state, which then gives the donor potential. See Models.ipynb for implements and 2.3 test score for donor potential calculation.

3.8 Correction

Since Bayesian networks cannot perfectly infer causality between N_f and N_L , correction to directions of edges was performed. After construting a DAG structure, the edges from N_L to $N_f, f \in \{-10, -9, ...10\}$ are reversed (see Models.ipynb). For example, the edge $N_L \to N_{-1}$ are reversed into $N_L \leftarrow N_{-1}$.

3.9 Settings for SVM to classify splice sites

In the experiment, Gaussian Kernel function [15] were used to map vectors to higher-dimensional feature space. The γ for Gaussian Kernel are set to \$ 1/(Num_{features}\Variance_{data})\$. All

other parameters are default values (Scikit-learn version 0.23.1). See details in Sklearn documentation.

$$K(x_i, x_j) = \exp(-\gamma ||x_i - x_j||^2), \gamma > 0$$
(4)

```
class Model:
    def __init__(self):
        self.wam = WAM()
        self.bn = BN(struc_estr=ConstraintBasedEstimator)
        self.svm = SVM(kernel='rbf', gamma='scale', random_state=1, probability=True,
        verbose=True)

model_1 = Model()
model_2 = Model()
```

3.10 Cross-validation

To test the accuracy of three models, a simple cross-validation [16] was performed. In both two experiments, independent and identically distributed testing set with was selected.

3.11 Evaluation

To visualize and compare classification results of 3 models, ROC curves [17] and PR curves [18] are plotted using Matplotlib package [26,27]. To realize this, a sample-based evaluation method is introduced:

$$TP_t = \sum_{i=0}^{N} I(S_i \ge t \land L_i = 1) \tag{5}$$

$$FP_t = \sum_{i=0}^{N} I(S_i \ge t \land L_i = 0) \tag{6}$$

$$TN_t = \sum_{i=0}^{N} I(S_i < t \land L_i = 0)$$

$$\tag{7}$$

$$FN_t = \sum_{i=0}^{N} I(S_i < t \land L_i = 1)$$
(8)

where TP_t , FP_t , TP_t , TN_t are statistics for models' prediction result in specific threshold t. I(True) = 0 and I(False) = 1, L_i is label for ith sample. S_i is the score calculated based on probability for ith sample. $t \in \{-25, -24.5, -24, ...24.5, 25\}$ is the threshold used in the evaluation.

And following metrics were used in the evaluation.

$$TPR_t = \frac{TP_t}{TP_t + FN_t} \tag{9}$$

$$FPR_t = \frac{FP_t}{FP_t + TN_t} \tag{10}$$

$$Sn_t = \frac{TP_t}{TP_t + FN_t} \tag{11}$$

$$Sp_t = \frac{TN_t}{TN_t + FP_t} \tag{12}$$

$$Pr_t = \frac{TP_t}{TP_t + FP_t} \tag{13}$$

$$Rc_t = \frac{TP_t}{TP_t + FN_t} \tag{14}$$

$$F1 - score_t = \frac{2Pr_tRc_t}{Pr_t + Rc_t} \tag{15}$$

Finally, auROC (the area under ROC curve) [19] and auPRC (the area under Precision-Recall curve) [6,18] were calculated using Composite Trapezoidal rule [20]:

$$auROC = \sum_{i=1}^{N-1} \frac{(FPR_{i+1} - FPR_i)(TPR_i + TPR_{i+1})}{2}$$
 (16)

$$auPRC = \sum_{i=1}^{N-1} \frac{(Rc_{i+1} - Rc_i)(Pr_i + Pr_{i+1})}{2}$$
(17)

For implements, see Evaluator.ipynb.

4 Results and Discussion

In this section we discuss the result of two experiments.

4.1 Model Training

Three models were trained here. WAM and BN were trained and tested using sequence features, and SVM was trained and tested using numerical features. The numerical features were encoded using one-hot encoder (see 2.3 feature extraction).

```
[]: model_1.wam.fit(training_set1['Seq. features'], training_set1['IsDonor'])
model_2.wam.fit(training_set2['Seq. features'], training_set2['IsDonor'])
```

4.2 Test scores Calculation

The test scores for models were calculated here.

4.3 Result on two datasets

Here all results of three models in both two experiments were compared. Above all, The results show that all three models detected splice signal in a way. Their auROC are very close to 1, which means they can perfectly classify donor sites from Pseudo sites. But in contrast, Both auROC and auPRC showed that SVM has a higher accuracy than the other (Fig. 1). Moreover, SVM are more robust when trained and tested on unbalanced dataset than BN and WAM. The auPRC can show performance decline significantly while auROC cannot when models were trained on unbalanced data.

```
[ ]: evaltr_1.Save_figs(trange, suffix='1')
evaltr_2.Save_figs(trange, suffix='2')
```

```
[12]: evaltr_1.Cal_metrics(trange).to_csv('../Figures/Table_S2.a.csv', index=False) evaltr_2.Cal_metrics(trange).to_csv('../Figures/Table_S2.b.csv', index=False)
```

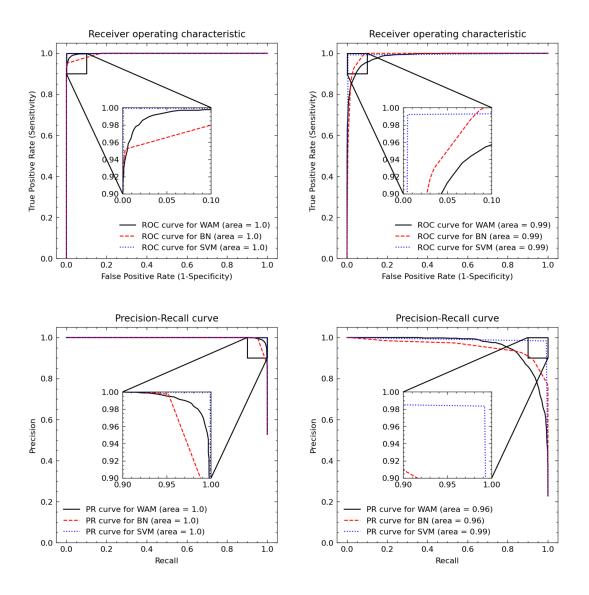


Figure 1: Overall comparison for models on balanced data (left) and unbalanced data (right).

4.4 Model selection

In the experiments, their performances are slightly different since their strategies of detecting splice signals are different. But obviously, there is a situation that unbalanced data affects, compare to the first experiment, their metrics in the second experiment has significantly declined, especially auPRC for WAM and BN.

4.4.1 Weighted Array Model

WAM shows decent accuracy in the experiments considering its low cost of computating power. It has the ability to discover low level features of splice site (Fig. 2), but higher level feature detection remains impossible. As Weighted array model calculate adjacent bases frequencies at each position, it can only detect common adjacent bases near the splice sites. In both two experiments, WAM has detected the information well (see Fig. 1). The result shows that GG, GT, TA bases are more

frequent near splice site. This agrees with some of the facts that have been found [28].

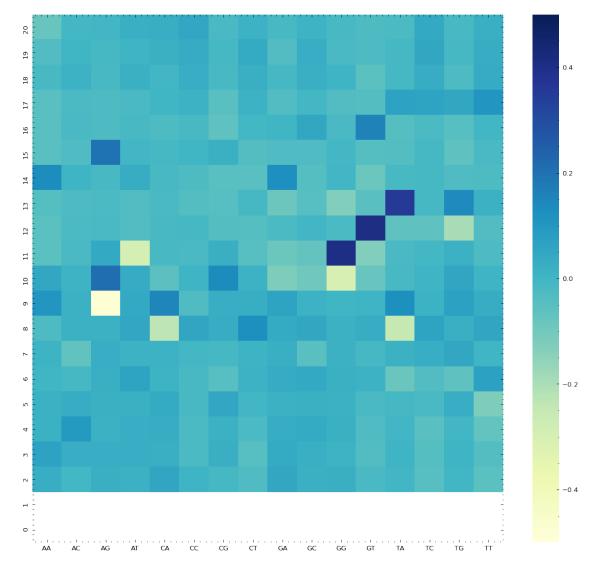


Figure 2: Visualization of the difference in W of WAM $(W_{donor,2} - W_{pseudo,2})^1$.

The result also shows that there is a performance decline in experiment 2 (Fig. 1). The main reason of this is that donor information contained in second training dataset is much less than first

¹Experiment 2.

dataset (Fig. 1 & 3). In other words, the frequency of some adjacent bases within each position near the donor sites are lower in the unbalanced dataset (Fig. 3). The model cannot learn weights, which were informatively comprehensive enough, to precisely classify donor site in that situation (Fig. 1). Thus, To build a reliable WAM model, the information contained in true splice sites and pseudo sites need to be very comprehensive.

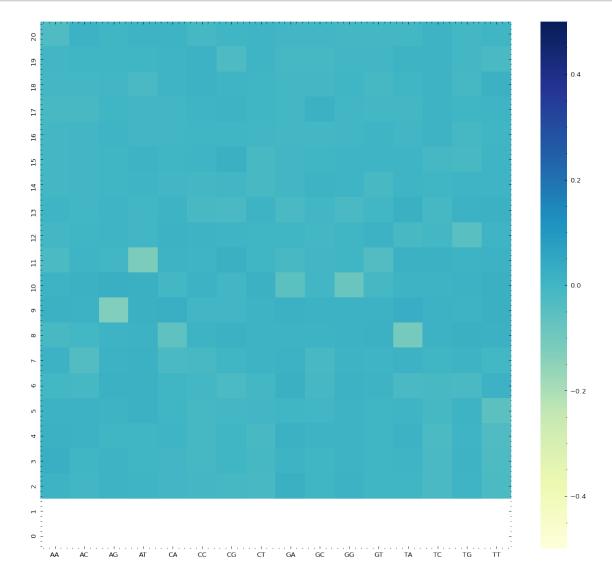


Figure 3: Visualization of the difference in D_{exp} across experiments $(D_1 - D_2)^2$.

 $^{^{2}}D_{exp} = W_{donor,exp} - W_{pseudo,exp}$

4.4.2 Bayesian Network

Bayesian network uses $\chi^2 - test$ [21] and conditional independent test, to build the dependency graph for each position near the splice site and also donor potential. In both two experiments, BN has detected the conditional dependence between positions and donor potential (Fig. 4).

But there are some imperfections. First, directions of edges in the graph may learn wrong due to separated learning algorithm (Fig. 4). During structure learning, if there is an edge $N_0 \to N_{-1}$, there will not be an edge $N_0 \leftarrow N_{-1}$ because of its DAG structure. But on choromosome, it is common that adjacent positions affects each other. One way to address this limitation is to combine the structure learning and the parameter learning. When there are mutual influences, just discard edge with less influence. Or when detecting splice signals, I just wanna keep $N_0 \leftarrow N_{-1}$ cause N_0 is the site. Second, BN's learning algorithm utilizes $\chi^2 - test$ and conditional independent test and so more sensitive to unbalanced data (Fig. 4) [14]. So there is a significant performance decline for BN compare to SVM (Fig. 1). Furthermore, BN is susceptible to not only information contained in dataset, but also distribution of data compares with WAM. This would explain the fact that performance declines in experiment 2.

Finally, classical integrated BN is in a position to detect not only dependence between positions, but also dependences between positions and donor potential, because it learns parameters from all data, donor sites and pseudo sites. While expanded Bayesian networks [22] can just detect dependence between positions, because it learns positive and negative BNs' parameters using positive and negative data respectively.

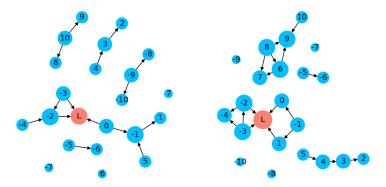


Figure 4: Graph for Bayesian network. G_1 (left) and G_2 (right).

4.4.3 Support Vector Machine

Support Vector machines have performed best and nearly the same in the experiments. The result shows that SVM has the potential to take care of unbalanced data. There are several benefits using SVM.

First, SVM was appropriate to provide for classification. It has the highest accuracy amoung all three models used in the experiments. The margin maximal and kernel trick gives it ability to classify very complex data. One more important feature of SVM is that only support vectors are important in order to classification. The rest can be ignored. This can easily reduce the computing power needed.

Second, when dealing with unbalanced data, the number of support vectors can be slightly the same for each class (Table S1). This makes its accuracy slightly the save as first experiment (Fig. 1). It handled the unbalanced data elegantly.

Third. There are several mature optimization algorithms with low time complexity and sophisticated software tools [11,23,25]. They were nicely implemented, make SVM's training and prediction fast. However, Visualization of the hyper-plane and high-dimensional space is impossible. Although its accuracy is excellent. It still likes a black box. We cannot know which feature are the most important or what kind of the signals were detected.

Table S1: Number of support vectors in SVM

	Donor	Pseudo
SVM 1	350	352
SVM 2	543	509

4.5 Metrics

In the experiments, we used TPR, FPR, Sn, Sp, Rc, Pr, F1 - score, auROC, auPRC metrics to evaluate performances of models. The result shows that auPRC is more sensitive to unbalanced data than auROC (Fig. 1).

Simple mathamatical formulation: Here we note $D = Num_p(TP, FN) - Num_n(FP, TN)$ as the difference between two classes. $TPR(Num_p)$, $Sn(Num_p)$ and $Rc(Num_p)$ are independent with Num_n , and $FPR(Num_n)$, $Sp(Num_n)$ are independent on Num_p , so they are independent with D. Pr is the only metric that is dependent on D. So $auPRC = \sum_{i=1}^{N-1} \frac{(Rc_{i+1} - Rc_i)(Pr_i + Pr_{i+1})}{2}$ can enlarge the difference of performance when comparing different models on unbalanced data.

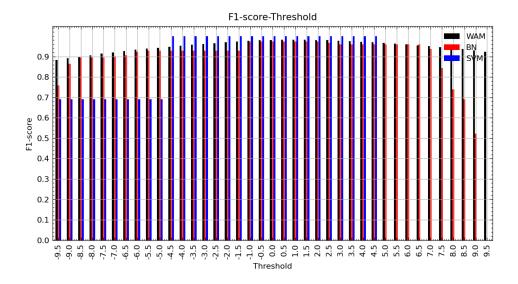
When comparing models on an unbalanced dataset, we should not miss Pr and auPRC. Besides, $F1 - score = \frac{2PrRc}{Pr+Rc}$ also has ability to enlarge this kind of difference.

4.6 Threshold selection

F1-score [24] is another important metric. Since Pr and Rc are paradoxical sometimes, we cannot have highest Rc and Pr at the same time. When selection thresholds, we use F1-score instead.

The result shows that all F1-score reach its peak at $t \approx 0$. So t=0 is a suitable threshold for 3 models. For other metrics involved in threshold selection, see Table S2.a and S2.b.

```
[18]: fs = ['../Figures/F1_t_1.png', '../Figures/F1_t_2.png']
  figs = [pli.imread(i) for i in fs]
  figure, (ax1, ax2) = plt.subplots(2, 1, dpi=200, figsize=(12,12))
  plt.subplots_adjust(left=0.0,bottom=0.0,top=1,right=1);
  no_box(ax1); ax1.imshow(figs[0]);no_box(ax2); ax2.imshow(figs[1]);plt.tight_layout()
```



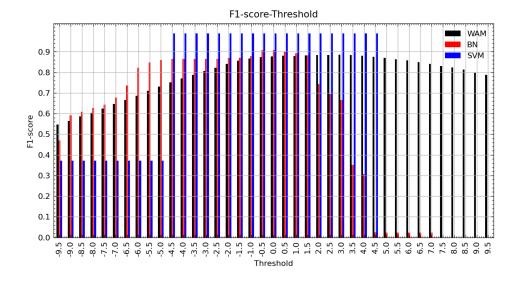


Figure 5: Visualization for F1-score & Threshold across experiments exp_1 (top) and exp_2 (bottom).

5 Conclusion and Prospect

Some facts have been found after these attempts. First, **Weighted Array Model** is good at detecting dependence between adjacent positions and costs lowest computing power. Second, **Bayesian network** still suffers from learning algorithm. PC-Contraint based algorithm and MMHC algorithm still not perfect and are so time consuming. It takes me 10 hours to train a Bayesian network. Third, **Support Vector Machine** is very accurate and fast when dealing with small dataset. Finally, when dataset is unbalanced, A very wise choice would be selecting not only auROC but also auPRC as metrics to evaluate models. Or make dataset balanced before training, some methods have been proposed to complete this.

The Pros and Cons of models are arranged below.

Model	Pros	Cons
WAM	Low cost of computing power, Splice signal detection, Easy to visualize	Accuracy not perfect
BN	Easy to visualize, Causual relationship inference, Splice signal detection	Immature learning algorithms, accuracy still not perfect
SVM	Extreamely high accuracy, Fast and mature learning algorithm [23,25]	Cannot visualize, Black box

5.1 Limitations and Prospect

There are still some limitations about this work. First, the information contained in datasets are different, this may cause a little accuracy decline. Second, the dataset used in the experiments are still too small, only 5000 samples are used to training models.

Corresponding with limitations, there are two experiments need to be done in the future. First, make information-equal datasets to repeat the experiments. Second, experiments on larger datasets need to be done as the proportion of donor sites is near 10^{-3} or even smaller.

6 Availability

Dataset was provided by Prof. Zhou of Huazhong University of Science and Technology. Source code of this project are hosted on Github. Besides, to encourage others to reproduce this project, all source code involved in this report was remained. Anyone can configure dependence environment can easily reproduce it.

Making research projects more reproducible is highly recommended here.

7 Acknowledgements

First of all, I would like to extend my sincere gratitude to Professor Yanhong Zhou, for his valuable knowledge and experience in bioinformatic data mining that I've gained. I am deeply grateful of his patient teaching during the COVID-19 epidemic.

Second, I am also deeply indebted to all the other researchers and geeks in Bioinformatics and Data Mining for their great works and wonderful programming experiences and skills shared on the web. I cannot finish this project without them.

Finally, Special thanks should go to my parents, girlfriend and also other friends, for their continuous support and encouragement.

8 References

- 1. M.O. Zhang, T.G. Marr, Α weight array method for splicing signal anal-Bioinformatics, vsis, Volume 9. Issue 5. October 1993. Pages 499-509. https://doi.org/10.1093/bioinformatics/9.5.499
- 2. Sinha, R., Hiller, M., Pudimat, R. et al. Improved identification of conserved cassette exons using Bayesian networks. BMC Bioinformatics 9, 477 (2008). https://doi.org/10.1186/1471-2105-9-477
- 3. Pearl J. Bayesian networks: A model of self-activated memory for evidential reasoning[C]//Proceedings of the 7th Conference of the Cognitive Science Society, University of California, Irvine, CA, USA. 1985: 15-17.
- Sonnenburg, S., Schweikert, G., Philips, P. et al. Accurate splice site prediction using support vector machines. BMC Bioinformatics 8, S7 (2007). https://doi.org/10.1186/1471-2105-8-S10-S7
- 5. Cortes, C., Vapnik, V. Support-vector networks. Mach Learn 20, 273–297 (1995). https://doi.org/10.1007/BF00994018
- 6. Boyd K, Eng K H, Page C D. Area under the precision-recall curve: point estimates and confidence intervals[C]//Joint European conference on machine learning and knowledge discovery in databases. Springer, Berlin, Heidelberg, 2013: 451-466.
- 7. Gilbert W. Why genes in pieces?. Nature. 1978;271(5645):501. doi:10.1038/271501a0
- 8. deeplizard. One-hot Encoding explained. YouTube. 2018-01-12 [2019-09-08]
- 9. Nomenclature for Incompletely Specified Bases in Nucleic Acid Sequences, NC-IUB, 1984.
- 10. Oliphant T E. Python for scientific computing[J]. Computing in Science & Engineering, 2007, 9(3): 10-20.
- 11. Pedregosa F, Varoquaux G, Gramfort A, et al. Scikit-learn: Machine learning in Python[J]. the Journal of machine Learning research, 2011, 12: 2825-2830.
- 12. Ankan A, Panda A. pgmpy: Probabilistic graphical models using python[C]//Proceedings of the 14th Python in Science Conference (SCIPY 2015). 2015.
- 13. C.D. Manning, P. Raghavan and M. Schütze (2008). *Introduction to Information Retrieval*. Cambridge University Press, p. 260.
- P. Spirtes, C. Glymour, and R. Scheines. Causation, prediction, and search. Springer-Verlag, New York, 1993.
- 15. Vert J P, Tsuda K, Schölkopf B. A primer on kernel methods[J]. Kernel methods in computational biology, 2004, 47: 35-70.
- 16. Stone M. Cross-validatory choice and assessment of statistical predictions[J]. Journal of the Royal Statistical Society: Series B (Methodological), 1974, 36(2): 111-133.
- 17. Fawcett, Tom (2006); An introduction to ROC analysis, Pattern Recognition Letters, 27, 861–874.
- 18. Boyd K, Eng K H, Page C D. Area under the precision-recall curve: point estimates and confidence intervals[C]//Joint European conference on machine learning and knowledge discovery in databases. Springer, Berlin, Heidelberg, 2013: 451-466.

- 19. Hanley JA, McNeil BJ. A method of comparing the areas under receiver operating characteristic curves derived from the same cases. *Radiology*. 1983;148(3):839-843. doi:10.1148/radiology.148.3.6878708
- 20. Ossendrijver M. Ancient Babylonian astronomers calculated Jupiter's position from the area under a time-velocity graph. *Science*. 2016;351(6272):482-484. doi:10.1126/science.aad8085
- 21. McHugh M L. The chi-square test of independence[J]. Biochemia medica: Biochemia medica, 2013, 23(2): 143-149.
- 22. Chen T M, Lu C C, Li W H. Prediction of splice sites with dependency graphs and their expanded bayesian networks[J]. Bioinformatics, 2005, 21(4): 471-482.
- 23. Platt J. Sequential minimal optimization: A fast algorithm for training support vector machines [J]. 1998.
- 24. Sasaki, Yutaka. (2007). The truth of the F-measure. Teach Tutor Mater.
- 25. Chang C C, Lin C J. LIBSVM: A library for support vector machines[J]. ACM transactions on intelligent systems and technology (TIST), 2011, 2(3): 1-27.
- 26. J. D. Hunter, "Matplotlib: A 2D Graphics Environment", Computing in Science & Engineering, vol. 9, no. 3, pp. 90-95, 2007
- 27. Waskom, M. et al., 2017. mwaskom/seaborn: v0.8.1 (September 2017), Zenodo. Available at: https://doi.org/10.5281/zenodo.883859.
- 28. Wikipedia contributors. RNA In (2020,June 17). splicing. Wikipedia, TheFreeEncyclopedia. Retrieved 01:09, June 20, 2020, from https://en.wikipedia.org/w/index.php?title=RNA splicing&oldid=962973627
- 29. Compeau P, Pevzner P A. Bioinformatics Algorithms: An Active Learning Approach. La Jolla[M]. CA: Active Learning Publishers, 2018.
- 30. Li H, Cabeli V, Sella N, et al. Constraint-based causal structure learning with consistent separating sets[C]//Advances in Neural Information Processing Systems. 2019: 14257-14266.

[]: