Template del Rejunte

```
#include <bits/stdc++.h>
  #define sqr(a) ((a)*(a))
3 #define rsz resize
  #define forr(i,a,b) for(int i=(a);i<(b);i++)
5 #define forn(i,n) forr(i,0,n)
  #define dforn(i,n) for(int i=n-1;i>=0;i--)
#define forall(it,v) for(auto it=v.begin();it!=v.end();it++)
  #define foreach(i, v) for(auto i:v)
  #define sz(c) ((int)c.size())
  #define zero(v) memset(v, 0, sizeof(v))
  #define pb push_back
  #define mp make_pair
   #define lb lower_bound
   #define ub upper_bound
   #define fst first
   #define snd second
   #define PI 3.1415926535897932384626
18
   using namespace std;
20
   typedef long long 11;
   typedef pair<int,int> ii;
   typedef vector<int> vi;
   typedef vector<ii> vii;
25
   int main()
26
27
     // agregar g++ -DREJUNTE en compilacin
28
     #ifdef REJUNTE
29
       freopen("input", "r", stdin);
30
       // freopen("output", "w", stdout);
31
     #endif
32
     ios::sync_with_stdio(false);
33
     cin.tie(NULL);
34
     cout.tie(NULL);
35
     return 0;
36
37 | }
```

Estructuras de datos

Set Mejorado

Esto solo compila en C++11.

```
| #include <ext/pb_ds/assoc_container.hpp>
```

```
#include <ext/pb_ds/tree_policy.hpp>
   using namespace __gnu_pbds;
   //<key,mapped type,comparator,...>
   typedef tree<int,null_type,less<int>,rb_tree_tag,
     tree_order_statistics_node_update> ordered_set;
   //find_by_order(i) devuelve iterador al i-esimo elemento
   //order_of_key(k): devuelve la pos del lower bound de k
   //Ej: 12, 100, 505, 1000, 10000.
   //order_of_key(10) == 0, order_of_key(100) == 1,
   //order_of_kev(707) == 3, order_of_kev(9999999) == 5
                                   Union Find
   struct UnionFind{
     vector<int> f,setSize; //the array f contains the parent of each node
     int cantSets;
     void init(int n)
       f.clear(); setSize.clear();
       cantSets=n;
       f.rsz(n,-1);
       setSize.rsz(n,1);
10
     int comp(int x){return (f[x]=-1?x:f[x]=comp(f[x]));}//0(1)
11
     bool join(int i,int j) //devuelve true si ya estaban juntos
12
13
       bool con=comp(i)==comp(j);
14
       if(!con)
15
       {
16
         cantSets--;
17
         setSize[comp(j)]+=setSize[comp(i)];
         setSize[comp(i)]=setSize[comp(j)]; //no suma, solo asigna
         f[comp(i)]=comp(j);
20
21
       return con;
22
23
24 };
                                   Hash Table
  //Compilar: g++ --std=c++11
```

```
//Compilar: g++ --std=c++11
struct Hash{
    size_t operator()(const ii &a)const
    {
        size_t s=hash<int>()(a.fst);
        return hash<int>()(a.snd)+0x9e3779b9+(s<<6)+(s>>2);
    }
    size_t operator()(const vector<int> &v)const
```

```
tipo get(int i, int j, int n, int a, int b){\frac{1}{0}}
       size_t s=0;
                                                                                              if(j<=a || i>=b) return neutro;
                                                                                      17
       for (auto &e : v) s^=hash<int>()(e)+0x9e3779b9+(s<<6)+(s>>2);
                                                                                              if(i<=a && b<=j) return t[n];</pre>
                                                                                              int c=(a+b)/2:
       return s:
     }
                                                                                              return operacion(get(i, j, 2*n, a, c), get(i, j, 2*n+1, c, b));
13
                                                                                      20
                                                                                      21
   unordered_set<ii, Hash> s;
                                                                                            void set(int p, tipo val){//0(lgn)
                                                                                      22
unordered_map<ii, int, Hash> m;//map<key, value, hasher>
                                                                                              for(p+=sz; p>0 && t[p]!=val;){
                                                                                               t[p]=val;
                                                                                      24
                                       RMQ
                                                                                                p/=2;
                                                                                      25
RMQ (static)
                                                                                                val=operacion(t[p*2], t[p*2+1]);
Dado un arreglo y una operacion asociativa idempotente, get(i, j) opera sobre el rango [i, j).<sup>27</sup>
Restriccion: LVL \geq ceil(logn); Usar [] para llenar arreglo y luego build().
                                                                                          }rmq;
1 struct RMO{
                                                                                          //Usage:
     #define LVL 10
                                                                                        cin >> n; rmq.init(n); forn(i, n) cin >> rmq[i]; rmq.updall();
     tipo vec[LVL] [1<<(LVL+1)];
                                                                                      RMQ (lazy)
     tipo &operator[](int p){return vec[0][p];}
     tipo get(int i, int j) {//intervalo [i,j)
                                                                                       1 //Dado un arreglo y una operacion asociativa con neutro, get(i, j) opera sobre
       int p = 31-_builtin_clz(j-i);
                                                                                              el rango [i, j).
       return min(vec[p][i],vec[p][j-(1<<p)]);
                                                                                         typedef int Elem;//Elem de los elementos del arreglo
     }
                                                                                          typedef int Alt;//Elem de la alteracion
     void build(int n) {//O(nlogn)
                                                                                          #define operacion(x,y) x+y
       int mp = 31-__builtin_clz(n);
10
                                                                                          const Elem neutro=0; const Alt neutro2=0;
       forn(p, mp) forn(x, n-(1 << p))
11
                                                                                          #define MAXN 100000//Cambiar segun el N del problema
         vec[p+1][x] = min(vec[p][x], vec[p][x+(1<<p)]);
12
                                                                                          struct RMO{
    }};
13
                                                                                           int sz;
                                                                                           Elem t[4*MAXN]:
                                                                                           Alt dirty[4*MAXN];//las alteraciones pueden ser de distinto Elem
RMQ (dynamic)
                                                                                            Elem &operator[](int p){return t[sz+p];}
1 //Dado un arreglo y una operacion asociativa con neutro, get(i, j) opera sobre
                                                                                            void init(int n){//O(nlgn)
       el rango [i, j).
                                                                                              sz = 1 \ll (32-\_builtin\_clz(n));
2 #define MAXN 100000
                                                                                              forn(i, 2*sz) t[i]=neutro;
                                                                                      14
   #define operacion(x, y) max(x, y)
                                                                                              forn(i, 2*sz) dirty[i]=neutro2;
                                                                                      15
   const int neutro=0;
                                                                                      16
   struct RMQ{
                                                                                            void push(int n, int a, int b){//propaga el dirty a sus hijos
                                                                                      17
     int sz;
                                                                                              if(dirty[n]!=0){
                                                                                      18
                                                                                               t[n]+=dirty[n]*(b-a);//altera el nodo
     tipo t[4*MAXN];
                                                                                      19
     tipo &operator[](int p){return t[sz+p];}
                                                                                               if(n<sz){
                                                                                      20
     void init(int n){//O(nlgn)
                                                                                                  dirty[2*n]+=dirty[n];
                                                                                      21
       sz = 1 \ll (32-\_builtin\_clz(n));
                                                                                                  dirty[2*n+1]+=dirty[n];
10
                                                                                      22
       forn(i, 2*sz) t[i]=neutro;
                                                                                               }
                                                                                      23
11
     }
                                                                                                dirty[n]=0;
                                                                                      24
12
                                                                                              }
     void updall(){//0(n)}
13
                                                                                      25
       dforn(i, sz) t[i]=operacion(t[2*i], t[2*i+1]);}
                                                                                      26
     tipo get(int i, int j){return get(i,j,1,0,sz);}
                                                                                           Elem get(int i, int j, int n, int a, int b){\frac{1}{0}}
```

```
else return new node(t->1, update(pos, new_val, t->r, tm, tr));
       if(j<=a || i>=b) return neutro;
28
       push(n, a, b);//corrige el valor antes de usarlo
                                                                                     24
29
       if(i<=a && b<=j) return t[n];
                                                                                         tipo get(int 1, int r, node *t, int t1, int tr){
                                                                                             if(l==tl && tr==r) return t->v;
       int c=(a+b)/2:
       return operacion(get(i, j, 2*n, a, c), get(i, j, 2*n+1, c, b));
                                                                                           int tm=(tl + tr)>>1;
                                                                                             if(r<=tm) return get(1, r, t->1, t1, tm);
     Elem get(int i, int j){return get(i,j,1,0,sz);}
                                                                                             else if(l>=tm) return get(l, r, t->r, tm, tr);
34
                                                                                          return oper(get(1, tm, t->1, tl, tm), get(tm, r, t->r, tm, tr));
     //altera los valores en [i, j) con una alteracion de val
35
                                                                                     31 }
     void alterar(Alt val, int i, int j, int n, int a, int b)\frac{1}{0(\lg n)}
36
       push(n, a, b);
37
                                                                                                                            BIGInt
       if(j<=a || i>=b) return;
38
       if(i<=a && b<=j){
39
                                                                                         #define BASEXP 6
         dirty[n]+=val;
40
                                                                                         #define BASE 1000000
         push(n, a, b);
                                                                                         #define LMAX 1000
         return;
42
                                                                                         struct bint{
43
                                                                                             int 1;
       int c=(a+b)/2;
44
                                                                                             11 n[LMAX];
       alterar(val, i, j, 2*n, a, c), alterar(val, i, j, 2*n+1, c, b);
45
                                                                                             bint(11 x=0){
       t[n]=operacion(t[2*n], t[2*n+1]);//por esto es el push de arriba
46
                                                                                                 1=1;
     }
47
                                                                                                 forn(i, LMAX){
     void alterar(Alt val, int i, int j){alterar(val,i,j,1,0,sz);}
                                                                                                     if (x) l=i+1;
49 |}rmq;
                                                                                                     n[i]=x%BASE;
RMQ (persistente)
                                                                                                     x/=BASE;
                                                                                      13
1 typedef int tipo;
                                                                                                 }
                                                                                      14
  tipo oper(const tipo &a, const tipo &b){
                                                                                             }
                                                                                      15
                                                                                             bint(string x){
       return a+b:
                                                                                      16
                                                                                             l=(x.size()-1)/BASEXP+1;
                                                                                      17
5 struct node{
                                                                                                 fill(n, n+LMAX, 0);
                                                                                      18
     tipo v; node *1,*r;
                                                                                                 ll r=1;
                                                                                      19
     node(tipo v):v(v), 1(NULL), r(NULL) {}
                                                                                                 forn(i, sz(x))
                                                                                                     n[i / BASEXP] += r * (x[x.size()-1-i]-'0');
       node(node *1, node *r) : 1(1), r(r){
                                                                                     21
           if(!1) v=r->v;
                                                                                                     r*=10; if (r==BASE)r=1;
                                                                                     22
           else if(!r) v=l->v;
                                                                                     23
           else v=oper(1->v, r->v);
                                                                                             }
11
                                                                                     24
       }
                                                                                             void out(){
                                                                                     25
12
                                                                                             cout << n[1-1];
13
   node *build (tipo *a, int tl, int tr) {//modificar para que tome tipo a
                                                                                             dforn(i, l-1) printf("%6.61lu", n[i]);//6=BASEXP!
     if (tl+1==tr) return new node(a[tl]);
                                                                                     28
15
     int tm=(tl + tr)>>1;
                                                                                           void invar(){
     return new node(build(a, tl, tm), build(a, tm, tr));
                                                                                             fill(n+1, n+LMAX, 0);
17
                                                                                             while(1>1 && !n[1-1]) 1--;
18
  node *update(int pos, int new_val, node *t, int tl, int tr){
                                                                                          }
                                                                                     32
     if (tl+1==tr) return new node(new_val);
     int tm=(tl+tr)>>1:
                                                                                         bint operator+(const bint&a, const bint&b){
21
     if(pos < tm) return new node(update(pos, new_val, t->1, tl, tm), t->r);
                                                                                           bint c:
```

11 rm = 0;

dforn(i, a.1){

```
c.1 = max(a.1, b.1);
                                                                                                      rm = rm * BASE + a.n[i]:
                                                                                      82
       11 a = 0:
                                                                                                      c.n[i] = rm / b;
       forn(i, c.1) q += a.n[i]+b.n[i], c.n[i]=q %BASE, q/=BASE;
                                                                                                     rm %= b;
       if(q) c.n[c.l++] = q;
       c.invar();
                                                                                             c.1 = a.1;
       return c;
                                                                                             c.invar();
41
                                                                                             return make_pair(c, rm);
42
   pair<bint, bool> lresta(const bint& a, const bint& b) // c = a - b
                                                                                         bint operator/(const bint&a, ll b){return ldiv(a, b).first;}
44
                                                                                         ll operator%(const bint&a, ll b){return ldiv(a, b).second;}
     bint c;
45
       c.1 = max(a.1, b.1);
                                                                                         pair < bint, bint > ldiv(const bint & a, const bint & b) {
46
       11 q = 0;
                                                                                           bint c;
47
       forn(i, c.l) q += a.n[i]-b.n[i], c.n[i]=(q+BASE) %BASE, q=(q+BASE)/BASE-1;
                                                                                             bint rm = 0;
48
       c.invar():
                                                                                             dforn(i, a.1){
       return make_pair(c, !q);
                                                                                                  if (rm.l==1 && !rm.n[0])
50
                                                                                      96
                                                                                                      rm.n[0] = a.n[i];
51
   bint& operator-= (bint& a, const bint& b){return a=lresta(a, b).first;}
                                                                                                  else{
52
   bint operator- (const bint&a, const bint&b){return lresta(a, b).first;}
                                                                                                      dforn(j, rm.l) rm.n[j+1] = rm.n[j];
   bool operator< (const bint&a, const bint&b){return !lresta(a, b).second;}
                                                                                                     rm.n[0] = a.n[i];
                                                                                     100
   bool operator <= (const bint&a, const bint&b) {return lresta(b, a).second;}
                                                                                                     rm.l++:
                                                                                     101
   bool operator==(const bint&a, const bint&b){return a <= b && b <= a;}
                                                                                                 }
                                                                                     102
   bint operator*(const bint&a, ll b){
                                                                                                 ll q = rm.n[b.1] * BASE + rm.n[b.1-1];
                                                                                     103
57
       bint c:
                                                                                                 ll u = q / (b.n[b.l-1] + 1);
                                                                                     104
58
       11 q = 0;
                                                                                                 ll v = q / b.n[b.l-1] + 1;
                                                                                     105
59
       forn(i, a.l) q += a.n[i]*b, c.n[i] = q %BASE, q/=BASE;
                                                                                                  while (u < v-1){
60
                                                                                     106
       c.1 = a.1;
                                                                                                     11 m = (u+v)/2;
                                                                                     107
61
       while(q) c.n[c.l++] = q %BASE, q/=BASE;
                                                                                                     if (b*m \le rm) u = m;
62
                                                                                     108
       c.invar();
                                                                                                      else v = m;
63
                                                                                     109
                                                                                                  }
       return c;
                                                                                     110
64
                                                                                                  c.n[i]=u;
65
                                                                                     111
   bint operator*(const bint&a, const bint&b){
                                                                                                  rm-=b*u;
66
                                                                                     112
       bint c;
                                                                                             }
67
                                                                                     113
                                                                                           c.l=a.l;
       c.1 = a.1+b.1;
                                                                                     114
68
       fill(c.n, c.n+b.1, 0);
                                                                                             c.invar();
                                                                                     115
69
       forn(i, a.1){
                                                                                             return make_pair(c, rm);
                                                                                     116
70
           11 q = 0;
                                                                                     117
71
           forn(j, b.1) q += a.n[i]*b.n[j]+c.n[i+j], c.n[i+j] = q %BASE, q/=BASE;
                                                                                         bint operator/(const bint&a, const bint&b){return ldiv(a, b).first;}
72
           c.n[i+b.1] = q;
                                                                                     bint operator%(const bint&a, const bint&b){return ldiv(a, b).second;}
73
74
                                                                                                                         Algoritmos
       c.invar();
75
       return c;
76
77
                                                                                                             Longest Increasing Subsecuence
   pair<bint, 11> ldiv(const bint& a, 11 b){// c = a / b ; rm = a % b
     bint c;
                                                                                       1 //Para non-increasing, cambiar comparaciones y revisar busq binaria
```

//Given an array, paint it in the least number of colors so that each color

turns to a non-increasing subsequence.

```
3 //Solution:Min number of colors=Length of the longest increasing subsequence
                                                                                               forn(i, t){ //intervalos cerrado abiertos !!! importante!!
                                                                                       17
  int N, a[MAXN];//secuencia y su longitud
                                                                                                   Qu &q=qs[i];
                                                                                       18
5 | ii d[MAXN+1];//d[i]=ultimo valor de la subsecuencia de tamanio i
                                                                                                   while(cl>q.1) add(--cl);
                                                                                        19
                                                                                                   while(cr<q.r) add(cr++);</pre>
   int p[MAXN];//padres
                                                                                                   while(cl<q.1) remove(cl++);</pre>
   vector<int> R;//respuesta
                                                                                       21
   void rec(int i){
                                                                                                   while(cr>q.r) remove(--cr);
                                                                                       22
                                                                                                   ans[q.id]=curans;
     if(i==-1) return;
                                                                                       23
     R.push_back(a[i]);
                                                                                               }
                                                                                       24
                                                                                       25 }
     rec(p[i]);
11
12
   int lis(){//O(nlogn)
13
     d[0] = ii(-INF, -1); forn(i, N) d[i+1]=ii(INF, -1);
                                                                                                                              Strings
14
     forn(i, N){
15
       int j = upper_bound(d, d+N+1, ii(a[i], INF))-d;
16
                                                                                                                               KMP
       if (d[j-1].first < a[i]&&a[i] < d[j].first){</pre>
17
         p[i]=d[j-1].second;
18
                                                                                           vector<int> b; //back table b[i] maximo borde de [0..i)
         d[j] = ii(a[i], i);
                                                                                           void kmppre(string &P) //by gabina with love
19
       }
20
     }
                                                                                             b.clear();
21
     R.clear();
                                                                                             b.rsz(P.size());
22
     dforn(i, N+1) if(d[i].first!=INF){
23
                                                                                             int i = 0, j=-1; b[0]=-1;
       rec(d[i].second);//reconstruir
                                                                                             while(i<sz(P))</pre>
24
       reverse(R.begin(), R.end());
25
       return i;//longitud
                                                                                               while(j>=0 && P[i] != P[j]) j=b[j];
26
     }
27
                                                                                               i++, j++;
                                                                                       10
     return 0;
                                                                                               b[i] = j;
^{28}
                                                                                       11
29 }
                                                                                       12
                                                                                       13
                                         Mo's
                                                                                           void kmp(string &T,string &P) //Text, Pattern -- O(|T|+|P|)
O(q*\sqrt{n})
                                                                                       15
                                                                                             kmppre(P);
                                                                                       16
1 | int n,sq;
                                                                                             int i=0, j=0;
struct Qu{//queries [1, r]
                                                                                       17
                                                                                             while(i<sz(T))
                                                                                       18
       //intervalos cerrado abiertos !!! importante!!
                                                                                       19
       int 1, r, id;
                                                                                               while(j>=0 && T[i]!=P[j]) j=b[j];
                                                                                       20
   }qs[MAXN];
                                                                                               i++, j++;
                                                                                       21
   int ans[MAXN], curans;//ans[i]=ans to ith query
                                                                                               if(j==sz(P))
                                                                                       22
   bool bymos(const Qu &a, const Qu &b){
                                                                                       23
       if(a.l/sq!=b.l/sq) return a.l<b.l;</pre>
                                                                                                 //P encontrado en T empezando en [i-j,i)
                                                                                       24
       return (a.l/sq)&1? a.r<b.r : a.r>b.r;
                                                                                                 j=b[j];
                                                                                       25
10 }
                                                                                               }
                                                                                       26
void mos(){
                                                                                       27
       forn(i, t) qs[i].id=i;
12
                                                                                       28 }
       sort(qs, qs+t, bymos);
13
       int cl=0, cr=0;
14
                                                                                                                             Z function
       sq=sqrt(n);
15
                                                                                        1 //z[i]=length of longest substring starting from s[i] that is prefix of s
       curans=0;
```

```
vector<int> z;
   void zFunction(string &s)
     int n=s.size();
     for(int i=1,1=0,r=0;i<n;i++)
       if(i<=r)
       z[i]=min(r-i+1,z[i-1]);
       while(i+z[i] \le k s[z[i]] == s[i+z[i]])
       z[i]++;
11
       if(i+z[i]-1>r)
12
       l=i, r=i+z[i]-1;
13
14
15
   void match(string &T, string &P) //Text, Pattern -- O(|T|+|P|)
16
17
     string s=P;
18
     s+='$'; //here append a character that is not present in T
19
     s.append(T);
20
     z.clear();
21
     z.rsz(s.size(),0);
22
     zFunction(s);
23
     forr(i,P.size()+1,s.size())
24
       if(z[i]==P.size()); //match found, idx = i-P.size()-1
25
26 | }
                                         Trie
1 struct trie{
     map<char, trie> m;
     void add(const string &s, int p=0)
       if(s[p]) m[s[p]].add(s, p+1);
     void dfs()
       //Do stuff
       forall(it, m)
       it->second.dfs();
11
12
<sub>13</sub> | };
                                     Manacher
1 string s;
1 int d1[MAXN];//d1[i]=long del maximo palindromo impar con centro en i
int d2[MAXN];//d2[i]=analogo pero para longitud par
4 //0 1 2 3 4
```

```
5 //a a b a a <--d1[2]=3
   //a a a a <--d2[2]=2 (estan uno antes)
   void manacher() // O(|S|) - find longest palindromic substring
     int l=0, r=-1, n=sz(s);
     forn(i, n)
10
11
       int k=(i>r? 1 : min(d1[l+r-i], r-i));
       while(i+k<n && i-k>=0 && s[i+k]==s[i-k]) ++k;
13
       d1[i] = k--;
14
       if(i+k > r) l=i-k, r=i+k;
15
16
     1=0, r=-1;
17
     forn(i, n)
18
19
       int k=(i>r? 0 : min(d2[1+r-i+1], r-i+1))+1;
       while(i+k-1 \le k = 0 \ k \le [i+k-1] == s[i-k]) k++;
21
       d2[i] = --k:
       if(i+k-1 > r) l=i-k, r=i+k-1;
23
24
25 }
```

Aho Corasick

```
struct Trief
     map<char, Trie> next;
     Trie* tran[256]://transiciones del automata
     int idhoja, szhoja;//id de la hoja o O si no lo es
     //link lleva al sufijo mas largo, nxthoja lleva al mas largo pero que es hoja
     Trie *padre, *link, *nxthoja;
     char pch;//caracter que conecta con padre
     //Trie(): tran(), idhoja(), padre(), link() {}
     //coment linea de arriba porque me daba errores usarla.
     void insert(const string &s, int id=1, int p=0) //id>0!!!
10
     {
11
       if(p<sz(s))</pre>
12
13
         Trie &ch=next[s[p]];
14
         tran[(int)s[p]]=&ch;
15
         ch.padre=this, ch.pch=s[p];
16
         ch.insert(s, id, p+1);
17
       }
18
       else idhoja=id, szhoja=sz(s);
19
20
     Trie* get_link()
21
22
       if(!link)
23
```

```
24
         if(!padre) link=this;//es la raiz
25
         else if(!padre->padre) link=padre;//hijo de la raiz
         else link=padre->get_link()->get_tran(pch);
       return link;
29
     }
30
     Trie* get_tran(int c)
31
32
       if(!tran[c]) tran[c] = !padre? this : this->get_link()->get_tran(c);
33
       return tran[c];
34
35
     Trie *get_nxthoja()
36
37
       if(!nxthoja) nxthoja = get_link()->idhoja? link : link->nxthoja;
38
       return nxthoja;
39
     }
40
     void print(int p)
41
42
       if(idhoja) cout << "found_" << idhoja << "_uat_position_" << p-szhoja <<
43
           endl:
       if(get_nxthoja()) get_nxthoja()->print(p);
44
     }
45
     void matching(const string &s, int p=0) //O(|s| + tamao palabras)
46
47
       print(p); if(p<sz(s)) get_tran(s[p])->matching(s, p+1);
48
50 };
```

Geometría

Punto

```
1 | struct pto{
     double x, y;
    pto(double x=0, double y=0):x(x),y(y){}
    pto operator+(pto a){return pto(x+a.x, y+a.y);}
     pto operator-(pto a){return pto(x-a.x, y-a.y);}
    pto operator+(double a){return pto(x+a, y+a);}
     pto operator*(double a){return pto(x*a, y*a);}
     pto operator/(double a){return pto(x/a, y/a);}
     //dot product, producto interno:
     double operator*(pto a){return x*a.x+y*a.y;}
10
     //module of the cross product or vectorial product:
11
     //if a is less than 180 clockwise from b, a^b>0
12
    double operator^(pto a){return x*a.y-y*a.x;}
```

```
//returns true if this is at the left side of line gr
     bool left(pto q, pto r){return ((q-*this)^(r-*this))>0;}
     bool operator<(const pto &a) const{return x<a.x-EPS || (abs(x-a.x)<EPS && y<a
         .y-EPS);}
   bool operator == (pto a) {return abs(x-a.x) < EPS && abs(y-a.y) < EPS;}
     double norm(){return sqrt(x*x+y*y);}
     double norm_sq(){return x*x+y*y;}
20
   double dist(pto a, pto b){return (b-a).norm();}
   typedef pto vec;
   double angle(pto a, pto o, pto b){
     pto oa=a-o, ob=b-o;
25
     return atan2(oa^ob, oa*ob);}
   //rotate p by theta rads CCW w.r.t. origin (0,0)
   pto rotate(pto p, double theta){
     return pto(p.x*cos(theta)-p.y*sin(theta),
        p.x*sin(theta)+p.y*cos(theta));
32 }
```

Orden Radial de Puntos

```
struct Cmp{//orden total de puntos alrededor de un punto r
     pto r;
     Cmp(pto r):r(r) {}
     int cuad(const pto &a) const{
       if(a.x > 0 && a.y >= 0)return 0;
       if(a.x <= 0 && a.y > 0)return 1;
       if(a.x < 0 && a.y <= 0)return 2;
       if(a.x >= 0 \&\& a.y < 0)return 3;
       assert(a.x ==0 && a.y==0);
       return -1;
11
     bool cmp(const pto&p1, const pto&p2)const{
       int c1 = cuad(p1), c2 = cuad(p2);
13
       if(c1==c2) return p1.y*p2.x<p1.x*p2.y;</pre>
14
           else return c1 < c2;
15
16
       bool operator()(const pto&p1, const pto&p2) const{
17
       return cmp(pto(p1.x-r.x,p1.y-r.y),pto(p2.x-r.x,p2.y-r.y));
18
19
20 };
```

Linea

```
int sgn(ll x){return x<0? -1 : !!x;}
struct line{</pre>
```

```
line() {}
                                                                                      6 bool inter(rect a, rect b, rect &r){
     double a,b,c;//Ax+By=C
                                                                                           r.lw=pto(max(a.lw.x, b.lw.x), max(a.lw.y, b.lw.y));
    //pto MUST store float coordinates!
                                                                                           r.up=pto(min(a.up.x, b.up.x), min(a.up.y, b.up.y));
     line(double a, double b, double c):a(a),b(b),c(c){}
                                                                                         //check case when only a edge is common
     // TO DO chequear porque paso problema metiendo negativo el C (-(todo el
                                                                                           return r.lw.x<r.up.x && r.lw.y<r.up.y;
         calculo como esta))
                                                                                      11 }
     line(pto p, pto q): a(q.y-p.y), b(p.x-q.x), c(a*p.x+b*p.y) {}
                                                                                                                            Circulo
     int side(pto p){return sgn(ll(a) * p.x + ll(b) * p.y - c);}
10
                                                                                         vec perp(vec v){return vec(-v.y, v.x);}
   bool parallels(line 11, line 12){return abs(11.a*12.b-12.a*11.b)<EPS;}
                                                                                        line bisector(pto x, pto y){
   pto inter(line 11, line 12){//intersection
                                                                                           line l=line(x, y); pto m=(x+y)/2;
     double det=11.a*12.b-12.a*11.b;
13
                                                                                           return line(-1.b, 1.a, -1.b*m.x+1.a*m.y);
     if(abs(det) < EPS) return pto(INF, INF); //parallels</pre>
14
     return pto(12.b*11.c-11.b*12.c, 11.a*12.c-12.a*11.c)/det;
                                                                                         struct Circle{
16 | }
                                                                                           pto o;
                                     Segmento
                                                                                           double r;
                                                                                           Circle(pto x, pto y, pto z){
1 | struct segm{
                                                                                             o=inter(bisector(x, y), bisector(y, z));
     pto s,f;
                                                                                             r=dist(o, x);
                                                                                      11
     segm(pto s, pto f):s(s), f(f) {}
                                                                                      12
     pto closest(pto p) {//use for dist to point
                                                                                           pair<pto, pto> ptosTang(pto p){
                                                                                      13
        double 12 = dist_sq(s, f);
                                                                                             pto m=(p+o)/2;
        if(12==0.) return s;
                                                                                             tipo d=dist(o, m);
        double t = ((p-s)*(f-s))/12;
                                                                                             tipo a=r*r/(2*d);
        if (t<0.) return s;//not write if is a line
                                                                                             tipo h=sqrt(r*r-a*a);
                                                                                      17
        else if(t>1.)return f;//not write if is a line
                                                                                             pto m2=o+(m-o)*a/d;
                                                                                      18
        return s+((f-s)*t);
                                                                                             vec per=perp(m-o)/d;
                                                                                      19
     }
11
                                                                                             return make_pair(m2-per*h, m2+per*h);
                                                                                      20
       bool inside(pto p){return abs(dist(s, p)+dist(p, f)-dist(s, f))<EPS;}</pre>
                                                                                      21
13
                                                                                      22
                                                                                         //finds the center of the circle containing p1 and p2 with radius r
   //NOTA: Si los segmentos son coolineales solo devuelve un punto de interseccion 24
                                                                                         //as there may be two solutions swap p1, p2 to get the other
   pto inter(segm s1, segm s2){
                                                                                         bool circle2PtsRad(pto p1, pto p2, double r, pto &c){
       if(s1.inside(s2.s)) return s2.s; //Fix cuando son colineales
17
                                                                                                 double d2=(p1-p2).norm_sq(), det=r*r/d2-0.25;
                                                                                      26
       if(s1.inside(s2.f)) return s2.f; //Fix cuando son colineales
18
                                                                                                 if(det<0) return false;</pre>
                                                                                      27
     pto r=inter(line(s1.s, s1.f), line(s2.s, s2.f));
19
                                                                                                 c=(p1+p2)/2+perp(p2-p1)*sqrt(det);
                                                                                      28
       if(s1.inside(r) && s2.inside(r)) return r;
20
                                                                                                 return true;
                                                                                      29
     return pto(INF, INF);
21
                                                                                      30
22 |}
                                                                                         #define sqr(a) ((a)*(a))
                                                                                         #define feq(a,b) (fabs((a)-(b))<EPS)</pre>
                                    Rectangulo
                                                                                         pair<tipo, tipo > ecCuad(tipo a, tipo b, tipo c){//a*x*x+b*x+c=0
                                                                                           tipo dx = sqrt(b*b-4.0*a*c);
1 struct rect{
     //lower-left and upper-right corners
                                                                                           return make_pair((-b + dx)/(2.0*a), (-b - dx)/(2.0*a));
     pto lw, up;
                                                                                      36
                                                                                         pair<pto, pto> interCL(Circle c, line 1){
                                                                                      37
5 //returns if there's an intersection and stores it in r
                                                                                           bool sw=false;
```

//stores convex hull of P in S, CCW order

```
if((sw=feq(0,1.b))){}
                                                                                             c = !c:
     swap(1.a, 1.b);
                                                                                    11
     swap(c.o.x, c.o.y);
                                                                                         return c;
                                                                                    13 | }
     pair<tipo, tipo> rc = ecCuad(
                                                                                                             Punto en Poligono Convexo
     sqr(l.a)+sqr(l.b),
                                                                                    O(\log n)
     2.0*1.a*1.b*c.o.y-2.0*(sqr(1.b)*c.o.x+1.c*1.a),
     sqr(1.b)*(sqr(c.o.x)+sqr(c.o.y)-sqr(c.r))+sqr(1.c)-2.0*1.c*1.b*c.o.y
                                                                                       void normalize(vector<pto> &pt) //delete collinear points first!
     );
                                                                                    2
47
     pair<pto, pto> p( pto(rc.first, (l.c - l.a * rc.first) / l.b),
                                                                                         //this makes it clockwise:
48
               pto(rc.second, (1.c - 1.a * rc.second) / 1.b) );
                                                                                         if(pt[2].left(pt[0], pt[1])) reverse(pt.begin(), pt.end());
     if(sw){
                                                                                         int n=sz(pt), pi=0;
50
     swap(p.first.x, p.first.y);
                                                                                         forn(i, n)
51
     swap(p.second.x, p.second.y);
                                                                                           if(pt[i].x<pt[pi].x || (pt[i].x==pt[pi].x && pt[i].y<pt[pi].y))</pre>
52
53
                                                                                         vector<pto> shift(n);//puts pi as first point
     return p;
54
                                                                                         forn(i, n) shift[i]=pt[(pi+i)%n];
55
   pair<pto, pto> interCC(Circle c1, Circle c2){
                                                                                         pt.swap(shift);
                                                                                    11
     line 1:
                                                                                    12
     1.a = c1.o.x-c2.o.x;
                                                                                       bool inPolygon(pto p, const vector<pto> &pt)
     1.b = c1.o.y-c2.o.y;
                                                                                    14
     1.c = (sqr(c2.r) - sqr(c1.r) + sqr(c1.o.x) - sqr(c2.o.x) + sqr(c1.o.y)
                                                                                         //call normalize first!
60
     -sqr(c2.o.y))/2.0;
                                                                                         if(p.left(pt[0], pt[1]) || p.left(pt[sz(pt)-1], pt[0])) return false;
61
     return interCL(c1, 1);
                                                                                         int a=1, b=sz(pt)-1;
62
63 | }
                                                                                          while(b-a>1)
                                                                                    19
                               Area de poligono
                                                                                           int c=(a+b)/2;
                                                                                           if(!p.left(pt[0], pt[c])) a=c;
double area(vector<pto> &p){//0(sz(p))
                                                                                           else b=c;
     double area=0;
     forn(i, sz(p)) area+=p[i]^p[(i+1)%sz(p)];
                                                                                         return !p.left(pt[a], pt[a+1]);
     //if points are in clockwise order then area is negative
     return abs(area)/2:
                                                                                                                  Chequeo de Convex
7 //Area ellipse = M_PI*a*b where a and b are the semi axis lengths
_{8} //Area triangle = sqrt(s*(s-a)(s-b)(s-c)) where s=(a+b+c)/2
                                                                                       bool isConvex(vector<int> &p){//O(N), delete collinear points!
                              Punto en poligono
                                                                                         int N=sz(p);
                                                                                         if(N<3) return false;
1 //checks if v is inside of P, using ray casting
                                                                                         bool isLeft=p[0].left(p[1], p[2]);
2 //works with convex and concave.
                                                                                         forr(i, 1, N)
   //excludes boundaries, handle it separately using segment.inside()
                                                                                           if(p[i].left(p[(i+1)%N], p[(i+2)%N])!=isLeft)
bool inPolygon(pto v, vector<pto>& P) {
                                                                                             return false:
     bool c = false;
                                                                                         return true: }
    forn(i, sz(P)){
       int j=(i+1)\%sz(P);
                                                                                                                       Convex Hull
       if((P[j].y>v.y) != (P[i].y > v.y) &&
```

(v.x < (P[i].x - P[j].x) * (v.y-P[j].y) / (P[i].y - P[j].y) + P[j].x))

```
2 //left must return >=0 to delete collinear points!
                                                                                              int a=-1, b=n-1;
                                                                                       27
   void CH(vector<pto>& P, vector<pto> &S){
                                                                                              while(b-a>1) { int m = (a+b)/2;
                                                                                       28
     S.clear();
                                                                                                if(fbin(x, m)) b=m;
     sort(P.begin(), P.end());//first x, then y
                                                                                                else a=m:
     forn(i, sz(P)){//lower hull
                                                                                       31
       while(sz(S) \ge 2 \&\& S[sz(S)-1].left(S[sz(S)-2], P[i])) S.pop_back();
                                                                                              return (acc(b).m*x+acc(b).h)*(mx?-1:1);
                                                                                       32
                                                                                                   //query 0(1)
       S.pb(P[i]);
     }
                                                                                              while(pos>0 && fbin(x, pos-1)) pos--;
                                                                                       34
                                                                                              while(pos<n-1 && !fbin(x, pos)) pos++;</pre>
     S.pop_back();
10
     int k=sz(S);
                                                                                              return (acc(pos).m*x+acc(pos).h)*(mx?-1:1);
11
     dforn(i, sz(P)){//upper hull
                                                                                       37
12
       while(sz(S) >= k+2 \&\& S[sz(S)-1].left(S[sz(S)-2], P[i])) S.pop_back();
                                                                                       38 } ch;
13
       S.pb(P[i]);
14
                                                                                                                Convex Hull Trick Dinamico
     S.pop_back();
16
                                                                                         const ll is_query = -(1LL<<62);</pre>
17 | }
                                                                                          struct Line {
                                                                                              11 m, b;
                                Convex Hull Trick
                                                                                              mutable multiset<Line>::iterator it;
struct Line{tipo m,h;};
                                                                                              const Line *succ(multiset<Line>::iterator it) const;
   tipo inter(Line a, Line b){
                                                                                              bool operator<(const Line& rhs) const {</pre>
                                                                                                  if (rhs.b != is_query) return m < rhs.m;</pre>
       tipo x=b.h-a.h, y=a.m-b.m;
       return x/y+(x\%y?!((x>0)^(y>0)):0);//==ceil(x/y)
                                                                                                  const Line *s=succ(it);
                                                                                                  if(!s) return 0;
   struct CHT {
                                                                                                  11 x = rhs.m;
     vector<Line> c;
                                                                                                  return b - s \rightarrow b < (s \rightarrow m - m) * x;
     bool mx;
                                                                                              }
                                                                                       12
     int pos;
                                                                                       13
     CHT(bool mx=0):mx(mx),pos(0){}//mx=1 si las query devuelven el max
                                                                                          struct HullDynamic : public multiset<Line>{ // will maintain upper hull for
10
     inline Line acc(int i){return c[c[0].m>c.back().m? i : sz(c)-1-i];}
                                                                                              maximum
11
     inline bool irre(Line x, Line y, Line z){
                                                                                              bool bad(iterator y) {
12
                                                                                       15
       return c[0].m>z.m? inter(y, z) <= inter(x, y)
                                                                                                  iterator z = next(y);
                                                                                       16
13
                             : inter(y, z) >= inter(x, y);
                                                                                                  if (y == begin()) {
                                                                                       17
14
     }
                                                                                                       if (z == end()) return 0;
15
                                                                                       18
     void add(tipo m, tipo h) {//0(1), los m tienen que entrar ordenados
                                                                                                       return y->m == z->m && y->b <= z->b;
                                                                                       19
16
           if (mx) m*=-1, h*=-1;
17
                                                                                       20
       Line l=(Line){m, h};
                                                                                                   iterator x = prev(y);
18
                                                                                                  if (z == end()) return y->m == x->m && y->b <= x->b;
           if(sz(c) && m==c.back().m) { 1.h=min(h, c.back().h), c.pop_back(); if( 22
19
                                                                                                  return (x->b - y->b)*(z->m - y->m) >= (y->b - z->b)*(y->m - x->m);
               pos) pos--; }
           while(sz(c) \ge 2 \&\& irre(c[sz(c)-2], c[sz(c)-1], 1)) { c.pop_back(); if( _{24}
20
                                                                                              iterator next(iterator y){return ++y;}
               pos) pos--; }
                                                                                       25
                                                                                              iterator prev(iterator y){return --y;}
           c.pb(1);
                                                                                       26
21
                                                                                              void insert_line(ll m, ll b) {
                                                                                       27
22
     inline bool fbin(tipo x, int m) {return inter(acc(m), acc(m+1))>x;}
                                                                                                  iterator y = insert((Line) { m, b });
23
                                                                                       28
     tipo eval(tipo x){
                                                                                                  y->it=y;
24
                                                                                       29
       int n = sz(c):
                                                                                                   if (bad(y)) { erase(y); return; }
25
                                                                                       30
       //query con x no ordenados O(lgn)
                                                                                                   while (next(y) != end() && bad(next(y))) erase(next(y));
                                                                                       31
```

21

22 // Primitiva de sqrt(r*r - x*x) como funcion double de una variable x.

```
while (y != begin() && bad(prev(y))) erase(prev(y));
                                                                                     inline double primitiva(double x,double r)
32
       }
                                                                                     24
33
       11 eval(ll x) {
                                                                                           if (x \ge r) return r*r*M_PI/4.0;
                                                                                     25
           Line l = *lower_bound((Line) { x, is_query });
                                                                                           if (x \le -r) return -r*r*M PI/4.0:
                                                                                          double raiz = sqrt(r*r-x*x);
           return 1.m * x + 1.b;
                                                                                           return 0.5 * (x * raiz + r*r*atan(x/raiz));
37
   }h;
                                                                                     29
   const Line *Line::succ(multiset<Line>::iterator it) const{
                                                                                         double interCircle(VC &v)
       return (++it==h.end()? NULL : &*it);}
                                                                                     31
                                                                                           vector<double> p; p.reserve(v.size() * (v.size() + 2));
                                                                                     32
                                Cortar poligono
                                                                                           forn(i,sz(v)) p.push_back(v[i].c.x + v[i].r), p.push_back(v[i].c.x - v[i].r)
1 //cuts polygon Q along the line ab
                                                                                           forn(i,sz(v)) forn(j,i)
   //stores the left side (swap a, b for the right one) in P
                                                                                     34
  void cutPolygon(pto a, pto b, vector<pto> Q, vector<pto> &P){
                                                                                     35
                                                                                             Circle &a = v[i], b = v[j];
     P.clear():
                                                                                     36
                                                                                             double d = (a.c - b.c).norm();
    forn(i, sz(Q)){
                                                                                     37
                                                                                             if (fabs(a.r - b.r) < d \&\& d < a.r + b.r)
                                                                                     38
       double left1=(b-a)^(Q[i]-a), left2=(b-a)^(Q[(i+1)\%sz(Q)]-a);
                                                                                     39
       if(left1>=0) P.pb(Q[i]);
                                                                                               double alfa = acos((sqr(a.r) + sqr(d) - sqr(b.r)) / (2.0 * d * a.r));
                                                                                     40
       if(left1*left2<0)
                                                                                              pto vec = (b.c - a.c) * (a.r / d);
         P.pb(inter(line(Q[i], Q[(i+1)\%sz(Q)]), line(a, b)));
                                                                                     41
                                                                                               p.pb((a.c + rotate(vec, alfa)).x), p.pb((a.c + rotate(vec, -alfa)).x);
     }
                                                                                     42
                                                                                             }
                                                                                     43
11 }
                                                                                          }
                                                                                     44
                            Intersección de Circulos
                                                                                           sort(p.begin(), p.end());
                                                                                     45
                                                                                           double res = 0.0;
                                                                                     46
1 struct event {
                                                                                           forn(i,sz(p)-1)
                                                                                     47
     double x: int t:
                                                                                     48
     event(double xx, int tt) : x(xx), t(tt) {}
                                                                                             const double A = p[i], B = p[i+1];
                                                                                     49
     bool operator <(const event &o) const { return x < o.x; }</pre>
                                                                                             VE ve; ve.reserve(2 * v.size());
                                                                                             forn(j,sz(v))
                                                                                     51
   typedef vector<Circle> VC;
                                                                                     52
  typedef vector<event> VE;
                                                                                               const Circle &c = v[j];
                                                                                     53
                                                                                              double arco = primitiva(B-c.c.x,c.r) - primitiva(A-c.c.x,c.r);
                                                                                     54
   double cuenta(VE &v, double A, double B)
                                                                                              double base = c.c.y * (B-A);
                                                                                     55
10
                                                                                               ve.push_back(event(base + arco,-1));
     sort(v.begin(), v.end());
11
                                                                                               ve.push_back(event(base - arco, 1));
                                                                                     57
     double res = 0.0, lx = ((v.empty())?0.0:v[0].x);
12
                                                                                     58
     int contador = 0;
13
                                                                                             res += cuenta(ve,A,B);
                                                                                     59
     forn(i,sz(v))
14
     { //intersection de todos (contador == n), union de todos (contador > 0)
15
                                                                                          return res;
                                                                                     61
       //conjunto de puntos cubierto por exacta k Circulos (contador == k)
16
                                                                                     62 | }
       if (contador == n) res += v[i].x - lx;
17
       contador += v[i].t, lx = v[i].x;
                                                                                                                        Rotar Matriz
18
     }
19
                                                                                      1 //rotates matrix t 90 degrees clockwise
     return res;
20
```

//using auxiliary matrix t2(faster)

3 | void rotate()

Matemática

Identidades

```
\begin{array}{l} \sum_{i=0}^{n}\binom{n}{i}=2^{n} \\ \sum_{i=0}^{n}i\binom{n}{i}=n*2^{n-1} \\ \sum_{i=0}^{n}i\binom{n}{i}=n*2^{n-1} \\ \sum_{i=m}^{n}i=\frac{n(n+1)}{2}-\frac{m(m-1)}{2}=\frac{(n+1-m)(n+m)}{2} \\ \sum_{i=0}^{n}i=\sum_{i=1}^{n}i=\frac{n(n+1)}{2} \\ \sum_{i=0}^{n}i^{2}=\frac{n(n+1)(2n+1)}{6}=\frac{n^{3}}{3}+\frac{n^{2}}{2}+\frac{n}{6} \\ \sum_{i=0}^{n}i(i-1)=\frac{8}{6}(\frac{n}{2})(\frac{n}{2}+1)(n+1) \text{ (doubles)} \rightarrow \text{Sino ver caso impar y par} \\ \sum_{i=0}^{n}i^{3}=\left(\frac{n(n+1)}{2}\right)^{2}=\frac{n^{4}}{4}+\frac{n^{3}}{2}+\frac{n^{2}}{4}=\left[\sum_{i=1}^{n}i\right]^{2} \\ \sum_{i=0}^{n}i^{4}=\frac{n(n+1)(2n+1)(3n^{2}+3n-1)}{30}=\frac{n^{5}}{5}+\frac{n^{4}}{2}+\frac{n^{3}}{3}-\frac{n}{30} \\ \sum_{i=0}^{n}i^{p}=\frac{(n+1)^{p+1}}{p+1}+\sum_{k=1}^{p}\frac{B_{k}}{p-k+1}\binom{p}{k}(n+1)^{p-k+1} \\ r=e-v+k+1 \\ \text{Teorema de Pick: (Area, puntos interiores y puntos en el borde)} \\ A=I+\frac{B}{2}-1 \end{array}
```

Ec. Caracteristica

```
\begin{aligned} a_0T(n) + a_1T(n-1) + ... + a_kT(n-k) &= 0 \\ p(x) &= a_0x^k + a_1x^{k-1} + ... + a_k \\ \text{Sean } r_1, r_2, ..., r_q \text{ las raices distintas, de mult. } m_1, m_2, ..., m_q \\ T(n) &= \sum_{i=1}^q \sum_{j=0}^{m_i-1} c_{ij} n^j r_i^n \end{aligned}
```

Las constantes c_{ij} se determinan por los casos base.

Teorema Chino del Resto

$$y = \sum_{j=1}^{n} (x_j * (\prod_{i=1, i \neq j}^{n} m_i)_{m_j}^{-1} * \prod_{i=1, i \neq j}^{n} m_i)$$

```
//Chinese remainder theorem (special case): find z such that
//z % m1 = r1, z % m2 = r2. Here, z is unique modulo M = lcm(m1, m2).

//Return (z, M). On failure, M = -1.

ii chinese_remainder_theorem(int m1, int r1, int m2, int r2)

{ //{xx,yy,d} son variables globales usadas en extendedEuclid
extendedEuclid(m1, m2);

if (r1%d != r2%d) return make_pair(0,-1);
return mp(sumMod(xx*r2*m1, yy*r1*m2, m1*m2) / d, m1*m2 / d);

//Chinese remainder theorem: find z such that z % m[i] = r[i] for all i.
//Note that the solution is unique modulo M = lcm_i (m[i]).
//Return (z, M). On failure, M = -1.
```

```
//Note that we do not require the a[i]'s to be relatively prime.
   ii chinese_remainder_theorem(const vector<int> &m, const vector<int> &r)
15
     ii ret=mp(r[0], m[0]);
     forr(i,1,m.size())
17
18
       ret=chinese_remainder_theorem(ret.snd, ret.fst, m[i], r[i]);
19
       if (ret.snd==-1) break;
21
22
     return ret;
                                 GCD & LCM
 int gcd(int a, int b) {return b? gcd(b,a%b) : a;}
 int lcm(int a, int b) {return a*(b/gcd(a,b));}
                              Euclides Extendido
   //ecuacin diofntica lineal
   //sea d=\gcd(a,b); la ecuacin a * x + b * y = c tiene soluciones enteras si
   //d|c. La siguiente funcin nos sirve para esto. De forma general ser:
   //x = x0 + (b/d)n
                        x0 = xx*c/d
   //y = y0 - (a/d)n
                        y0 = yy*c/d
   11 xx,yy,d;
   void extendedEuclid(ll a, ll b) \frac{1}{a} * xx + b * yy = d
     if (!b) {xx=1; yy=0; d=a; return;}
     extendedEuclid (b,a%b);
10
11
     ll x1=yy;
     11 y1=xx-(a/b)*yy;
     xx=x1; yy=y1;
13
14 | }
                                 Combinatoria
   void cargarComb()//O(MAXN^2)
     forn(i, MAXN+1) //comb[i][k]=i tomados de a k = i!/(k!*(i-k)!)
       comb[0][i]=0;
       comb[i][0]=comb[i][i]=1;
       forr(k, 1, i) comb[i][k]=(comb[i-1][k-1]+comb[i-1][k]) %MOD;
```

ll lucas (ll n, ll k, int p)

11 aux = 1:

while (n + k)

{ //Calcula (n,k)%p teniendo comb[p][p] precalculado.

```
aux = (aux * comb[n \%p][k \%p]) \%p;
       n/=p, k/=p;
     return aux;
19 |}
                 Exponenciación de Matrices y Fibonacci
   #define SIZE 350
   int NN:
   void mul(double a[SIZE][SIZE], double b[SIZE][SIZE])
     double res[SIZE] [SIZE] = {{0}};
     forn(i, NN) forn(j, NN) forn(k, NN) res[i][j]+=a[i][k]*b[k][j];
     forn(i, NN) forn(j, NN) a[i][j]=res[i][j];
   void powmat(double a[SIZE][SIZE], int n, double res[SIZE][SIZE])
10
     forn(i, NN) forn(j, NN) res[i][j]=(i==j);
     while(n)
13
       if(n&1) mul(res, a), n--;
       else mul(a, a), n/=2;
17
   struct M22{
                // |a b|
     tipo a,b,c,d;// |c d| -- TIPO
     M22 operator*(const M22 &p) const {
     return (M22){a*p.a+b*p.c, a*p.b+b*p.d, c*p.a+d*p.c,c*p.b+d*p.d};}
22
   M22 operator (const M22 &p, int n)
   {//VER COMO SE PUEDE PONER DENTRO DEL STRUCT
     if(!n) return (M22){1, 0, 0, 1};//identidad
     M22 q=p^(n/2); q=q*q;
27
     return n %2? p * q : q;
28
29
   ll fibo(ll n)//calcula el fibonacci enesimo en O(logN)
31
32
     M22 \text{ mat}=(M22)\{0, 1, 1, 1\}^n;
33
     return mat.a*f0+mat.b*f1;//f0 v f1 son los valores iniciales
34
35 | }
                            Operaciones Modulares
1 | ll mulMod(ll a,ll b,ll m=MOD) //O(log b)
```

```
2 | { //returns (a*b) %c, and minimize overfloor
     11 x=0, y=a\%m;
     while(b>0)
       if (b\%2==1) x=(x+y)\%m;
       y=(y*2)%m;
        b/=2;
     return x\m;
    ll expMod(ll b,ll e,ll m=MOD) //O(\log b)
13
      if(!e) return 1;
14
     11 q = \exp Mod(b, e/2, m);
     q=mulMod(q,q,m);
     return e%2? mulMod(b,q,m) : q;
18
    11 sumMod(ll a,ll b,ll m=MOD)
20
      a\%=m;
21
      b%=m;
      if(a<0) a+=m:
     if(b<0) b+=m:
     return (a+b) %m;
26
   11 difMod(ll a,ll b,ll m=MOD)
27
28
      a%=m;
29
      b%=m;
     if(a<0) a+=m;
     if(b<0) b+=m;
     11 ret=a-b;
     if(ret<0) ret+=m;</pre>
     return ret;
35
36
   11 divMod(ll a,ll b,ll m=MOD)
38
     return mulMod(a,inverso(b),m);
40 | }
```

Funciones de Primos

Sea $n = \prod p_i^{k_i}$, fact(n) genera un map donde a cada p_i le asocia su k_i

```
#define MAXP 100000 //no necesariamente primo
int criba[MAXP+1];
void crearCriba()
{
```

```
int w[] = \{4,2,4,2,4,6,2,6\};
                                                                                        51
     for(int p=25;p<=MAXP;p+=10) criba[p]=5;</pre>
                                                                                             ll p=it->fst, k=it->snd; ++it;
                                                                                             forn(_, k+1) divisores(f, divs, it, n), n*=p;
     for(int p=9;p<=MAXP;p+=6) criba[p]=3;</pre>
     for(int p=4;p<=MAXP;p+=2) criba[p]=2;</pre>
     for(int p=7,cur=0;p*p<=MAXP;p+=w[cur++&7]) if (!criba[p])</pre>
                                                                                           11 cantDivs(map<11,11> &f)
     for(int j=p*p;j<=MAXP;j+=(p<<1)) if(!criba[j]) criba[j]=p;</pre>
                                                                                        56
                                                                                             ll ret=1;
11
                                                                                        57
   vector<int> primos;
                                                                                              forall(it, f) ret*=(it->second+1);
   void buscarPrimos()
                                                                                              return ret;
13
14
                                                                                            11 sumDivs(map<11,11> &f)
     crearCriba();
15
     forr (i,2,MAXP+1) if (!criba[i]) primos.push_back(i);
                                                                                        62
16
                                                                                             11 ret=1;
17
                                                                                              forall(it, f)
   //factoriza bien numeros hasta MAXP^2
   void fact(ll n,map<ll,ll> &f) //0 (cant primos)
                                                                                               11 pot=1, aux=0;
   { //llamar a buscarPrimos antes
                                                                                               forn(i, it->snd+1) aux+=pot, pot*=it->fst;
     forall(p, primos){
                                                                                               ret*=aux:
22
                                                                                        68
       while(!(n %*p))
                                                                                        69
23
                                                                                             return ret;
24
         f[*p]++;//divisor found
25
                                                                                        71
         n/=*p;
26
                                                                                            ll eulerPhi(ll n) // con criba: O(lg n)
27
                                                                                        74
28
     if(n>1) f[n]++;
                                                                                             map<11,11> f;
29
                                                                                              fact(n,f);
30
                                                                                             ll ret=n;
31
   //factoriza bien numeros hasta MAXP
                                                                                              forall(it, f) ret-=ret/it->first;
   void fact2(ll n,map<ll,ll> &f) //0 (lg n)
                                                                                              return ret;
   { //llamar a crearCriba antes
     while (criba[n])
                                                                                            11 eulerPhi2(11 n) // 0 (sqrt n)
35
     {
36
                                                                                        82
       f[criba[n]]++;
                                                                                             11 r = n:
37
       n/=criba[n];
                                                                                              forr(i,2,n+1)
                                                                                        84
38
                                                                                        85
39
     if(n>1) f[n]++;
                                                                                                if((ll)i*i>n) break;
40
                                                                                                if(n\%i==0)
                                                                                        87
41
42
   //Usar asi: divisores(fac, divs, fac.begin()); NO ESTA ORDENADO
                                                                                                  while(n\%i==0) n/=i;
   void divisores(map<11,11> &f,vector<11> &divs,map<11,11>::iterator it,11 n=1)
                                                                                                  r = r/i;
                                                                                                }
45
     if(it==f.begin()) divs.clear();
     if(it==f.end())
                                                                                              if (n != 1) r= r/n;
47
     {
                                                                                              return r;
48
       divs.pb(n);
                                                                                        95 | }
       return;
```

Phollard's Rho |bool es_primo_prob(ll n, int a) 2 if(n==a) return true; 11 s=0.d=n-1: while(d%2==0) s++,d/=2; 11 x=expMod(a,d,n); if((x==1) || (x+1==n)) return true; forn(i,s-1) x=mulMod(x, x, n);if(x==1) return false; if(x+1==n) return true; 12 } 13 return false; 14 15 bool rabin (ll n) //devuelve true si n es primo 17 if(n==1) return false; 18 const int ar[]={2,3,5,7,11,13,17,19,23}; 19 forn(j,9) if(!es_primo_prob(n,ar[j])) return false; 20 return true; 21 22 ll rho(ll n) 23 24 if((n&1)==0) return 2:25 11 x=2, y=2, d=1;26 11 c=rand()%n+1; 27 while(d==1) 28 29 x=(mulMod(x,x,n)+c)%n;30 y=(mulMod(y,y,n)+c)%n;31 y=(mulMod(y,y,n)+c)%n;32 if(x-y>=0) d=gcd(n,x-y); 33 else d=gcd(n,y-x); 34 } 35 return d==n? rho(n):d; 36 37 void factRho (ll n,map<ll,ll> &f) //O (lg n)^3 un solo numero 39 if (n == 1) return; if (rabin(n)) 41 { 42 f[n]++; 43 return;

```
45
     11 factor = rho(n);
     factRho(factor,f);
     factRho(n/factor,f);
49 }
                                      Inversos
   #define MAXMOD 15485867
   11 inv[MAXMOD];//inv[i]*i=1 mod MOD
   void calc(int p) //0(p)
     inv[1]=1:
     forr(i,2,p) inv[i]=p-((p/i)*inv[p%i])%p;
   int inverso(int x) //0(\log x)
     return expMod(x, eulerPhi(MOD)-2);//si mod no es primo(sacar a mano)
     return expMod(x, MOD-2);//si mod es primo
11
12 }
                                    Fracciones
  struct frac{
     int p,q;
     frac(int p=0,int q=1):p(p),q(q) {norm();}
     void norm()
       int a=gcd(q,p);
       if(a) p/=a, q/=a;
       else q=1;
       if (q<0) q=-q, p=-p;
10
     frac operator+(const frac& o)
11
12
       int a=gcd(o.q,q);
13
       return frac(p*(o.q/a)+o.p*(q/a),q*(o.q/a));
14
15
     frac operator-(const frac& o)
16
17
       int a=gcd(o.q,q);
18
       return frac(p*(o.q/a)-o.p*(q/a),q*(o.q/a));
19
20
     frac operator*(frac o)
21
22
       int a=gcd(o.p,q), b=gcd(p,o.q);
23
       return frac((p/b)*(o.p/a),(q/a)*(o.q/b));
24
25
```

```
frac operator/(frac o)
27
       int a=gcd(o.q,q), b=gcd(p,o.p);
       return frac((p/b)*(o.q/a),(q/a)*(o.p/b));
     bool operator<(const frac &o) const{return p*o.q < o.p*q;}</pre>
31
     bool operator==(frac o){return p==o.p&&q==o.q;}
32
33 | };
```

Simpson

```
double integral (double a, double b, int n=10000) //0(n), n=cantdiv
2
     double area=0, h=(b-a)/n, fa=f(a), fb;
     forn(i, n)
       fb=f(a+h*(i+1));
       area+=fa+ 4*f(a+h*(i+0.5)) +fb, fa=fb;
    }
     return area*h/6.;
10 }
```

Tablas v cotas (Primos, Divisores, Factoriales, etc)

```
Factoriales
                   11! = 39.916.800
 0! = 1
 1! = 1
                   12! = 479.001.600 \ (\in int)
 2! = 2
                   13! = 6.227.020.800
 3! = 6
                   14! = 87.178.291.200
 4! = 24
                   15! = 1.307.674.368.000
 5! = 120
                   16! = 20.922.789.888.000
 6! = 720
                   17! = 355.687.428.096.000
 7! = 5.040
                   18! = 6.402.373.705.728.000
 8! = 40.320
                   19! = 121.645.100.408.832.000
 9! = 362.880
                   20! = 2.432.902.008.176.640.000 (\in tint)
 10! = 3.628.800
                   21! = 51.090.942.171.709.400.000
max signed tint = 9.223.372.036.854.775.807
max unsigned tint = 18.446.744.073.709.551.615
```

Primos

 $2\ 3\ 5\ 7\ 11\ 13\ 17\ 19\ 23\ 29\ 31\ 37\ 41\ 43\ 47\ 53\ 59\ 61\ 67\ 71\ 73\ 79\ 83\ 89\ 97\ 101\ 103\ 107\ 109\ 113_{1289904147324\ 4861946401452}$ 127 131 137 139 149 151 157 163 167 173 179 181 191 193 197 199 211 223 227 229 233 239 241 251 257 263 269 271 277 281 283 293 307 311 313 317 331 337 347 349 353 359 367 373 379 383 389 397 401 409 419 421 431 433 439 443 449 457 461 463 467 479 487 491 499 503 509 521 523 541 547 557 563 569 571 577 587 593 599 601 607 613 617 619 631 641 643 647 $653\ 659\ 661\ 673\ 677\ 683\ 691\ 701\ 709\ 719\ 727\ 733\ 739\ 743\ 751\ 757\ 761\ 769\ 773\ 787\ 797\ 809$ 811 821 823 827 829 839 853 857 859 863 877 881 883 887 907 911 919 929 937 941 947 953 967 971 977 983 991 997 1009 1013 1019 1021 1031 1033 1039 1049 1051 1061 1063 1069 1087 | #define INF 1e9

 $1091\ 1093\ 1097\ 1103\ 1109\ 1117\ 1123\ 1129\ 1151\ 1153\ 1163\ 1171\ 1181\ 1187\ 1193\ 1201\ 1213\ 1217$ $1223\ 1229\ 1231\ 1237\ 1249\ 1259\ 1277\ 1279\ 1283\ 1289\ 1291\ 1297\ 1301\ 1303\ 1307\ 1319\ 1321\ 1327$ 1361 1367 1373 1381 1399 1409 1423 1427 1429 1433 1439 1447 1451 1453 1459 1471 1481 1483 $1487\ 1489\ 1493\ 1499\ 1511\ 1523\ 1531\ 1543\ 1549\ 1553\ 1559\ 1567\ 1571\ 1579\ 1583\ 1597\ 1601\ 1607$ $1609\ 1613\ 1619\ 1621\ 1627\ 1637\ 1657\ 1663\ 1667\ 1669\ 1693\ 1697\ 1699\ 1709\ 1721\ 1723\ 1733\ 1741$ $1747\ 1753\ 1759\ 1777\ 1783\ 1787\ 1789\ 1801\ 1811\ 1823\ 1831\ 1847\ 1861\ 1867\ 1871\ 1873\ 1877\ 1879$ $1889\ 1901\ 1907\ 1913\ 1931\ 1931\ 1933\ 1949\ 1951\ 1973\ 1979\ 1987\ 1993\ 1997\ 1999\ 2003\ 2011\ 2017\ 2027$ 2029 2039 2053 2063 2069 2081

Primos cercanos a 10^n

9941 9949 9967 9973 10007 10009 10037 10039 10061 10067 10069 10079 99961 99971 99989 99991 100003 100019 100043 100049 100057 100069 999959 999961 999979 999983 1000003 1000033 1000037 1000039 9999943 9999971 9999973 9999991 10000019 10000079 10000103 10000121 99999941 99999959 99999971 99999989 100000007 100000037 100000039 100000049 999999893 999999929 999999937 1000000007 1000000009 1000000021 1000000033

Cantidad de primos menores que 10^n

```
\pi(10^1) = 4; \pi(10^2) = 25; \pi(10^3) = 168; \pi(10^4) = 1229; \pi(10^5) = 9592
\pi(10^6) = 78.498; \pi(10^7) = 664.579; \pi(10^8) = 5.761.455; \pi(10^9) = 50.847.534
\pi(10^{10}) = 455.052.511; \pi(10^{11}) = 4.118.054.813; \pi(10^{12}) = 37.607.912.018
```

Números Catalanes

Utiles para problemas de Combinatoria

$$Cat(n) = \frac{\binom{2n}{n}}{n+1} = \frac{(2n)!}{n! (n+1)!}$$

Con $Cat(0) = 1$.

Diferentes aplicaciones:

- 1. Contar la cantidad de diferentes arboles binarios con n nodos que se pueden armar.
- 2. Contar las formas en que un polígono convexo de n+2 lados puede ser triangulado.
- 3. Contar la cantidad de caminos monotonos a lo largo de los lados de una grilla n*n, que no cruzan la diagonal.
- 4. Contar el número de expresiones que contienen n pares de paréntesis correctamente colocados

Primeros 25 Catalanes

 $1\ 1\ 2\ 5\ 14\ 42\ 132\ 429\ 1430\ 4862\ 16796\ 58786\ 208012\ 742900\ 2674440\ 9694845\ 35357670$ $129644790\ 477638700\ 1767263190\ 6564120420\ 24466267020\ 91482563640\ 343059613650$

Grafos

Dijkstra

```
5 void floyd(){//O(N^3)
2 | int N;
3 #define MAX_V 250001
                                                                                       forn(k, N) forn(i, N) if(G[i][k]!=INF) forn(j, N) if(G[k][j]!=INF)
4 | vector<ii> G[MAX_V];
                                                                                         G[i][j]=min(G[i][j], G[i][k]+G[k][j]);
   //To add an edge use
                                                                                        bool inNegCycle(int v){
  | #define add(a, b, w) G[a].pb(make_pair(w, b))
  ll dijkstra(int s, int t){//0(|E| log |V|)
                                                                                         return G[v][v]<0;}
     priority_queue<ii, vector<ii>, greater<ii> > Q;
                                                                                        //checks if there's a neg. cycle in path from a to b
     vector<ll> dist(N, INF); vector<int> dad(N, -1);
                                                                                        bool hasNegCycle(int a, int b){
     Q.push(make_pair(0, s)); dist[s] = 0;
                                                                                          forn(i, N) if(G[a][i]!=INF && G[i][i]<0 && G[i][b]!=INF)
10
     while(sz(Q)){
                                                                                            return true;
11
       ii p = Q.top(); Q.pop();
                                                                                          return false;
                                                                                    15
12
       if(p.snd == t) break;
                                                                                     16 }
13
       forall(it, G[p.snd])
14
                                                                                                                          Kruskal
         if(dist[p.snd]+it->first < dist[it->snd]){
15
           dist[it->snd] = dist[p.snd] + it->fst;
16
                                                                                       // Minimun Spanning Tree in O(e log e)
           dad[it->snd] = p.snd;
17
                                                                                       bool operator<(const Ar& a, const Ar &b){return a.w<b.w;}
           Q.push(make_pair(dist[it->snd], it->snd)); }
18
                                                                                        vector<Ar> E;
     }
                                                                                        11 kruskal(){
19
     return dist[t];
20
                                                                                            11 cost=0;
     if(dist[t]<INF)//path generator</pre>
21
                                                                                            sort(E.begin(), E.end());//ordenar aristas de menor a mayor
       for(int i=t; i!=-1; i=dad[i])
22
                                                                                            uf.init(n);
         printf("%d%c", i, (i==s?'\n':','));}
23
                                                                                            forall(it, E){
                                                                                                if(uf.comp(it->a)!=uf.comp(it->b)){//si no estan conectados
                                  Bellman-Ford
                                                                                                    uf.unir(it->a, it->b);//conectar
    /Mas lento que Dijsktra, pero maneja arcos con peso negativo
                                                                                                    cost+=it->w;
                                                                                     11
  vector<ii> G[MAX_N];//ady. list with pairs (weight, dst)
                                                                                                }
                                                                                     12
   int dist[MAX_N];
                                                                                     13
  void bford(int src){//O(VE)
                                                                                            return cost;
                                                                                     14
     dist[src]=0;
                                                                                     15 }
    forn(i, N-1) forn(j, N) if(dist[j]!=INF) forall(it, G[j])
                                                                                                                            Prim
       dist[it->snd]=min(dist[it->snd], dist[j]+it->fst);
                                                                                        vector<ii> G[MAXN];
                                                                                        bool taken[MAXN];
  bool hasNegCycle(){
                                                                                        priority_queue<ii, vector<ii>, greater<ii> > pq;//min heap
    forn(j, N) if(dist[j]!=INF) forall(it, G[j])
                                                                                        void process(int v){
       if(dist[it->snd]>dist[j]+it->fst) return true;
12
                                                                                            taken[v]=true;
     //inside if: all points reachable from it->snd will have -INF distance(do bfs
13
                                                                                            forall(e, G[v])
                                                                                                if(!taken[e->second]) pq.push(*e);
     return false;
14
15 }
                                                                                        // Minimum Spanning Tree in O(n^2)
                                                                                        11 prim(){
                                 Floyd-Warshall
                                                                                            zero(taken);
1 // Camino minimo en grafos dirigidos ponderados, en todas las parejas de nodos. 12
                                                                                            process(0);
2 //G[i][j] contains weight of edge (i, j) or INF
                                                                                            11 cost=0;
3 //G[i][i]=0
                                                                                            while(sz(pq)){
                                                                                     14
4 int G[MAX_N][MAX_N];
                                                                                                ii e=pq.top(); pq.pop();
```

```
if(!taken[e.second]) cost+=e.first, process(e.second);
       }
17
       return cost;
19 }
                                   Kosaraju SCC
Componente Fuertemente Conexa
1 #define MAXN 1000000
2 | vector<int> G[MAXN], gt[MAXN]; //Limpiar si se corre mas de una vez
   //nodos 0...N-1; componentes 0...cantcomp-1
  int comp[MAXN],N,cantcomp,used[MAXN];
5 | stack<int> pila;
                                                                                        15
  void add(int a, int b){ G[a].pb(b);gt[b].pb(a);}
                                                                                        16
   void dfs1(int nodo)
                                                                                        18
8
     used[nodo]=1:
     forall(it,G[nodo]) if(!used[*it]) dfs1(*it);
                                                                                        20
     pila.push(nodo);
                                                                                        21
11
                                                                                        22
12
   void dfs2(int nodo)
                                                                                        23
13
14
     used[nodo]=2;
                                                                                        25
15
     comp[nodo] = cantcomp-1;
                                                                                        26
16
     forall(it,gt[nodo]) if(used[*it]!=2) dfs2(*it);
                                                                                        27
17
                                                                                        28
18
   void kosaraju()
                                                                                        29
19
                                                                                        30
20
     cantcomp=0;
21
     memset(used,0,sizeof(used));
                                                                                        32
22
     forn(i,N) if(!used[i]) dfs1(i);
                                                                                        33
23
     while(!pila.empty())
                                                                                        34
24
                                                                                        35
25
       if(used[pila.top()]!=2)
                                                                                        36
26
       {
                                                                                        37
27
         cantcomp++;
                                                                                        38
28
         dfs2(pila.top());
29
                                                                                        40
30
       pila.pop();
32
33 | }
                              2-SAT + Tarjan SCC
```

```
//We have a vertex representing a var and other for his negation.
//Every edge stored in G represents an implication. To add an equation of the form a||b, use addor(a, b)
//MAX=max cant var, n=cant var
```

```
#define addor(a, b) (G[neg(a)].pb(b), G[neg(b)].pb(a))
   vector<int> G[MAX*2];
   //idx[i]=index assigned in the dfs
   //lw[i]=lowest index(closer from the root) reachable from i
   int lw[MAX*2], idx[MAX*2], qidx;
   stack<int> q;
   int qcmp, cmp[MAX*2];
   //verdad[cmp[i]]=valor de la variable i
   bool verdad[MAX*2+1];
   int neg(int x) { return x>=n? x-n : x+n;}
   void tin(int v){
     lw[v]=idx[v]=++qidx;
     q.push(v), cmp[v]=-2;
     forall(it, G[v]){
       if(!idx[*it] || cmp[*it]==-2){
         if(!idx[*it]) tjn(*it);
         lw[v]=min(lw[v], lw[*it]);
       }
     if(lw[v]==idx[v]){
       int x:
       do{x=q.top(); q.pop(); cmp[x]=qcmp;}while(x!=v);
       verdad[qcmp] = (cmp[neg(v)] < 0);</pre>
       qcmp++;
   //remember to CLEAR G!!!
   bool satisf(){\frac{}{0}}
     memset(idx, 0, sizeof(idx)), qidx=0;
     memset(cmp, -1, sizeof(cmp)), qcmp=0;
     forn(i, n){
       if(!idx[i]) tjn(i);
       if(!idx[neg(i)]) tjn(neg(i));
     forn(i, n) if(cmp[i] == cmp[neg(i)]) return false;
     return true:
41 | }
```

Puntos de Articulación

```
int N;
vector<int> G[1000000];

//V[i]=node number(if visited), L[i]= lowest V[i] reachable from i
int qV, V[1000000], L[1000000], P[1000000];
void dfs(int v, int f){
    L[v]=V[v]=++qV;
```

```
new UTNTeam() - UTN FRSF
     forall(it, G[v])
       if(!V[*it]){
         dfs(*it, v);
         L[v] = min(L[v], L[*it]);
         P[v] += L[*it] >= V[v];
12
       else if(*it!=f)
13
         L[v]=min(L[v], V[*it]);
14
15
   int cantart() { //0(n)
16
     qV=0;
17
     zero(V), zero(P);
18
     dfs(1, 0); P[1]--;
19
     int q=0;
     forn(i, N) if(P[i]) q++;
  return q;
23 }
                     Least Common Ancestor + Climb
1 | const int MAXN=100001, LOGN=20;
   //f[v][k] holds the 2^k father of v
   //L[v] holds the level of v
  int N, f[MAXN][LOGN], L[MAXN];
   //call before build:
  void dfs(int v, int fa=-1, int lvl=0){//generate required data
    f[v][0]=fa, L[v]=lvl;
     forall(it, G[v])if(*it!=fa) dfs(*it, v, lvl+1); }
   void build(){//f[i][0] must be filled previously, O(nlgn)
     forn(k, LOGN-1) forn(i, N) f[i][k+1]=f[f[i][k]][k];}
   #define lg(x) (31-\_builtin\_clz(x))//=floor(log2(x))
   int climb(int a, int d){\frac{1}{0(lgn)}}
     if(!d) return a:
     dforn(i, lg(L[a])+1) if(1<<i<=d) a=f[a][i], d-=1<<i;
       return a;}
15
   int lca(int a, int b){\frac{1}{0}}
     if(L[a]<L[b]) swap(a, b);</pre>
17
     a=climb(a, L[a]-L[b]);
18
     if(a==b) return a;
19
     dforn(i, lg(L[a])+1) if(f[a][i]!=f[b][i]) a=f[a][i], b=f[b][i];
20
     return f[a][0]; }
21
   int dist(int a, int b) {//returns distance between nodes
     return L[a]+L[b]-2*L[lca(a, b)];}
                         Heavy Light Decomposition
```

```
vector<int> G[MAXN]:
int treesz[MAXN];//cantidad de nodos en el subarbol del nodo v
```

```
int dad[MAXN];//dad[v]=padre del nodo v
   void dfs1(int v, int p=-1){//pre-dfs
     dad[v]=p;
     treesz[v]=1:
     forall(it, G[v]) if(*it!=p){
       dfs1(*it, v);
       treesz[v]+=treesz[*it];
10
11
   //PONER Q EN O !!!!!
   int pos[MAXN], q;//pos[v]=posicion del nodo v en el recorrido de la dfs
   //Las cadenas aparecen continuas en el recorrido!
   int cantcad;
   int homecad [MAXN];//dada una cadena devuelve su nodo inicial
   int cad[MAXN];//cad[v]=cadena a la que pertenece el nodo
   void heavylight(int v, int cur=-1){
     if(cur==-1) homecad[cur=cantcad++]=v;
     pos[v]=a++:
     cad[v]=cur;
     int mx=-1:
22
     forn(i, sz(G[v])) if(G[v][i]!=dad[v])
23
       if(mx==-1 || treesz[G[v][mx]] < treesz[G[v][i]]) mx=i;</pre>
24
     if(mx!=-1) heavylight(G[v][mx], cur);
25
     forn(i, sz(G[v])) if(i!=mx && G[v][i]!=dad[v])
       heavylight(G[v][i], -1);
27
28
    //ejemplo de obtener el maximo numero en el camino entre dos nodos
   //RTA: max(query(low, u), query(low, v)), con low=lca(u, v)
   //esta funcion va trepando por las cadenas
   int query(int an, int v){//O(logn)
32
     //si estan en la misma cadena:
     if(cad[an] == cad[v]) return rmq.get(pos[an], pos[v]+1);
     return max(query(an, dad[homecad[cad[v]]]),
35
            rmq.get(pos[homecad[cad[v]]], pos[v]+1));
36
37 | }
```

Centroid Decomposition

```
vector<int> G[MAXN];
bool taken[MAXN];//poner todos en FALSE al principio!!
int padre[MAXN];//padre de cada nodo en el centroid tree
int szt[MAXN];
void calcsz(int v, int p) {
  szt[v] = 1;
 forall(it,G[v]) if (*it!=p && !taken[*it])
    calcsz(*it,v), szt[v]+=szt[*it];
```

```
10 }
   void centroid(int v=0, int f=-1, int lvl=0, int tam=-1) \frac{1}{0}
     if(tam==-1) calcsz(v, -1), tam=szt[v];
     forall(it. G[v]) if(!taken[*it] && szt[*it]>=tam/2)
       {szt[v]=0; centroid(*it, f, lvl, tam); return;}
     taken[v]=true;
     padre[v]=f;
     forall(it, G[v]) if(!taken[*it])
17
       centroid(*it, v, lvl+1, -1);
18
19 }
                                  Ciclo Euleriano
int n,m,ars[MAXE], eq;
vector<int> G[MAXN];//fill G,n,m,ars,eq
3 | list<int> path;
int used[MAXN];
  bool usede[MAXE];
   queue<list<int>::iterator> q;
   int get(int v){
     while(used[v]<sz(G[v]) && usede[ G[v][used[v]] ]) used[v]++;</pre>
     return used[v];
10
   void explore(int v, int r, list<int>::iterator it){
11
     int ar=G[v][get(v)]; int u=v^ars[ar];
12
     usede[ar]=true;
13
     list<int>::iterator it2=path.insert(it, u);
14
     if(u!=r) explore(u, r, it2);
15
     if(get(v)<sz(G[v])) q.push(it);</pre>
16
17
   void euler(){
     zero(used), zero(usede);
19
     path.clear();
20
     q=queue<list<int>::iterator>();
21
     path.push_back(0); q.push(path.begin());
22
     while(sz(a)){
23
       list<int>::iterator it=q.front(); q.pop();
24
       if(used[*it] < sz(G[*it])) explore(*it, *it, it);</pre>
^{25}
     }
26
     reverse(path.begin(), path.end());
27
28
   void addEdge(int u, int v){
29
     G[u].pb(eq), G[v].pb(eq);
30
     ars[eq++]=u^v;
32 }
```

Diametro Árbol

```
vector<int> G[MAXN]; int n,m,p[MAXN],d[MAXN],d2[MAXN];
   int bfs(int r, int *d) {
     queue<int> q;
     d[r]=0; q.push(r);
     int v;
     while(sz(q)) { v=q.front(); q.pop();
       forall(it,G[v]) if (d[*it]==-1)
         d[*it]=d[v]+1, p[*it]=v, q.push(*it);
     return v://ultimo nodo visitado
10
11
   vector<int> diams; vector<ii> centros;
   void diametros(){
13
     memset(d,-1,sizeof(d));
     memset(d2,-1,sizeof(d2));
     diams.clear(), centros.clear();
     forn(i, n) if(d[i]==-1){
17
       int v.c:
18
       c=v=bfs(bfs(i, d2), d);
19
       forn(_,d[v]/2) c=p[c];
20
       diams.pb(d[v]);
21
       if(d[v]&1) centros.pb(ii(c, p[c]));
22
       else centros.pb(ii(c, c));
23
24
25 }
```

Componentes Biconexas y Puentes

```
vector<int> G[MAXN]:
   struct edge{
     int u,v, comp;
     bool bridge;
   vector<edge> e;
   void addEdge(int u, int v)
     G[u].pb(sz(e)), G[v].pb(sz(e));
10
     e.pb((edge){u,v,-1,false});
11
12
   //d[i]=id de la dfs
   //b[i]=lowest id reachable from i
   int d[MAXN], b[MAXN], t;
   int nbc;//cant componentes
   int comp[MAXN];//comp[i]=cant comp biconexas a la cual pertenece i
   void initDfs(int n)
19 {
```

```
zero(G), zero(comp);
     e.clear();
     forn(i,n) d[i]=-1;
     nbc = t = 0:
   stack<int> st;
   void dfs(int u,int pe) //0(n + m)
27
     b[u]=d[u]=t++;
28
     comp[u]=(pe!=-1);
29
     forall(ne,G[u]) if(*ne!=pe)
30
31
       int v=e[*ne].u ^ e[*ne].v ^ u;
32
       if(d[v]==-1)
33
       {
34
         st.push(*ne);
35
         dfs(v,*ne);
36
         if(b[v]>d[u]) e[*ne].bridge=true; // bridge
37
         if(b[v]>=d[u]) // art
38
         {
39
            int last;
40
            do
41
42
              las=st.top(); st.pop();
43
              e[last].comp=nbc;
44
            }while(last!=*ne);
45
            nbc++;
46
            comp[u]++;
47
48
         b[u]=min(b[u],b[v]);
49
50
       else if(d[v]<d[u]) // back edge</pre>
51
       {
52
         st.push(*ne);
53
         b[u]=min(b[u], d[v]);
54
55
     }
56
57 }
                                      Hungarian
```

```
//Dado un grafo bipartito completo con costos no negativos, encuentra el matching perfecto de minimo costo.

#define tipo double

tipo cost[N][N], lx[N], ly[N], slack[N]; //llenar: cost=matriz de adyacencia int n, max_match, xy[N], yx[N], slackx[N], prev2[N]; //n=cantidad de nodos

bool S[N], T[N]; //sets S and T in algorithm
```

```
6 | void add_to_tree(int x, int prevx) {
     S[x] = true, prev2[x] = prevx;
     forn(y, n) if (lx[x] + ly[y] - cost[x][y] < slack[y] - EPS)
       slack[y] = lx[x] + ly[y] - cost[x][y], slackx[y] = x;
10
   void update_labels(){
     tipo delta = INF;
     forn (y, n) if (!T[y]) delta = min(delta, slack[y]);
     form (x, n) if (S[x]) lx[x] -= delta;
     forn (y, n) if (T[y]) ly[y] += delta; else slack[y] -= delta;
15
16
   void init_labels(){
17
     zero(lx), zero(ly);
18
     form (x,n) form(y,n) lx[x] = max(lx[x], cost[x][y]);
20
   void augment() {
     if (max_match == n) return;
     int x, y, root, q[N], wr = 0, rd = 0;
     memset(S, false, sizeof(S)), memset(T, false, sizeof(T));
     memset(prev2, -1, sizeof(prev2));
25
     forn (x, n) if (xy[x] == -1){
26
       q[wr++] = root = x, prev2[x] = -2;
27
       S[x] = true: break: }
28
     forn (y, n) slack[y] = lx[root] + ly[y] - cost[root][y], slackx[y] = root;
     while (true){
30
       while (rd < wr){
31
         x = q[rd++];
32
         for (y = 0; y < n; y++) if (cost[x][y] == lx[x] + ly[y] && !T[y]){
33
           if (vx[v] == -1) break; T[v] = true;
34
           q[wr++] = yx[y], add_to_tree(yx[y], x); }
35
         if (y < n) break; }</pre>
36
       if (y < n) break;
37
       update_labels(), wr = rd = 0;
38
       for (y = 0; y < n; y++) if (!T[y] \&\& slack[y] == 0){
39
         if (yx[y] == -1)\{x = slackx[y]; break;\}
40
         else{
41
           T[y] = true;
42
           if (!S[yx[y]]) q[wr++] = yx[y], add_to_tree(yx[y], slackx[y]);
43
         }}
44
       if (y < n) break; }
45
     if (y < n){
       max_match++;
47
       for (int cx = x, cy = y, ty; cx != -2; cx = prev2[cx], cy = ty)
         ty = xy[cx], yx[cy] = cx, xy[cx] = cy;
49
       augment(); }
50
51 }
```

void remove(int u, int v) //to remove an edge

```
52 | tipo hungarian(){
                                                                                      39
     tipo ret = 0; max_match = 0, memset(xy, -1, sizeof(xy));
                                                                                             if(u>v) swap(u,v);
                                                                                      40
     memset(yx, -1, sizeof(yx)), init_labels(), augment(); //steps 1-3
                                                                                             q.pb((Query){DEL, u, v});
                                                                                      41
     forn (x,n) ret += cost[x][xy[x]]; return ret;
                                                                                             int prev = last[ii(u,v)];
                                                                                             match[prev] = sz(q)-1;
56 | }
                                                                                      43
                                                                                             match.pb(prev);
                                                                                      44
                            Dynamic Connectivity
                                                                                      45
                                                                                           void query() //to add a question (query) type of query
struct UnionFind {
                                                                                      47
     int n, comp;
                                                                                             q.pb((Query){QUERY, -1, -1}), match.pb(-1);
                                                                                      48
     vector<int> pre,si,c;
                                                                                      49
     UnionFind(int n=0):n(n), comp(n), pre(n), si(n, 1) {
                                                                                           void process() //call this to process queries in the order of q
                                                                                      50
       forn(i,n) pre[i] = i; }
                                                                                      51
     int find(int u){return u==pre[u]?u:find(pre[u]);}
                                                                                             forn(i,sz(q)) if (q[i].type == ADD && match[i] == -1) match[i] = sz(q);
                                                                                      52
     bool merge(int u, int v)
                                                                                             go(0,sz(q));
                                                                                      54
       if((u=find(u))==(v=find(v))) return false;
                                                                                           void go(int 1, int r)
       if(si[u]<si[v]) swap(u, v);</pre>
10
                                                                                      56
       si[u]+=si[v], pre[v]=u, comp--, c.pb(v);
11
                                                                                             if(l+1==r)
                                                                                      57
       return true;
12
                                                                                             {
                                                                                      58
13
                                                                                               if (q[1].type == QUERY)//Aqui responder la query usando el dsu!
                                                                                      59
     int snap(){return sz(c);}
14
                                                                                                 res.pb(dsu.comp);//aqui query=cantidad de componentes conexas
                                                                                      60
     void rollback(int snap)
15
                                                                                               return:
                                                                                      61
16
                                                                                      62
       while(sz(c)>snap)
17
                                                                                             int s=dsu.snap(), m = (1+r) / 2;
                                                                                      63
18
                                                                                             forr(i,m,r) if(match[i]!=-1 && match[i]<1) dsu.merge(q[i].u, q[i].v);</pre>
                                                                                      64
         int v = c.back(); c.pop_back();
19
                                                                                             go(1,m);
                                                                                      65
         si[pre[v]] -= si[v], pre[v] = v, comp++;
20
                                                                                             dsu.rollback(s);
                                                                                      66
21
                                                                                             s = dsu.snap();
                                                                                      67
     }
22
                                                                                             forr(i,1,m) if(match[i]!=-1 && match[i]>=r) dsu.merge(q[i].u, q[i].v);
                                                                                      68
23
                                                                                             go(m,r);
   enum {ADD,DEL,QUERY};
                                                                                             dsu.rollback(s);
   struct Query {int type,u,v;};
                                                                                      71
   struct DynCon{//bidirectional graphs; create vble as DynCon name(cant_nodos)
                                                                                      72 };
     vector<Query> q;
27
     UnionFind dsu;
28
                                                                                                                             Flow
     vector<int> match,res;
29
     map<ii,int> last;//se puede no usar cuando hay identificador para cada arista
30
                                                                                                                        Edmond Karp
          (mejora poco)
     DynCon(int n=0):dsu(n){}
     void add(int u, int v) //to add an edge
                                                                                         #define MAX_V 1000
32
                                                                                         #define INF 1e9
33
       if(u>v) swap(u,v);
                                                                                         //special nodes
34
       q.pb((Query){ADD, u, v}), match.pb(-1);
                                                                                         #define SRC 0
35
       last[ii(u,v)] = sz(q)-1;
                                                                                         #define SNK 1
36
     }
                                                                                         map<int, int> G[MAX_V];//limpiar esto -- unordered_map mejora
37
```

7 //To add an edge use

```
8 | #define add(a, b, w) G[a][b]=w
  int f, p[MAX_V];
  void augment(int v, int minE)
     if(v==SRC) f=minE;
     else if(p[v]!=-1)
14
       augment(p[v], min(minE, G[p[v]][v]));
15
       G[p[v]][v]-=f, G[v][p[v]]+=f;
16
17
18
   11 maxflow()//O(min(VE^2,Mf*E))
19
20
     11 Mf=0:
21
     do
23
       f=0;
24
       char used[MAX_V]; queue<int> q; q.push(SRC);
25
       zero(used), memset(p, -1, sizeof(p));
26
       while(sz(q))
27
28
         int u=q.front(); q.pop();
29
         if(u==SNK) break:
30
         forall(it, G[u])
31
           if(it->snd>0 && !used[it->fst])
32
           used[it->fst]=true, q.push(it->fst), p[it->fst]=u;
33
34
       augment(SNK, INF);
35
       Mf+=f;
36
     }while(f);
37
     return Mf;
38
39
                                      Min Cut
1 //Suponemos un grafo con el formato definido en Edmond Karp o Push relabel
  bitset<MAX_V> type, used; //reset this
   void dfs1(int nodo)
```

forall(it,G[nodo]) if(!type[it->fst] && it->snd>0) dfs1(it->fst);

type.set(nodo);

void dfs2(int nodo)

used.set(nodo);

forall(it,G[nodo])

9

```
if(!type[it->fst])
13
       {
14
         //edge nodo -> (it->fst) pertenece al min_cut
15
         //y su peso original era: it->snd + G[it->fst][nodo]
         //si no existia arista original al revs
17
18
       else if(!used[it->fst]) dfs2(it->fst);
19
20
21
   void minCut() //antes correr algn maxflow()
22
23
     dfs1(SRC);
24
     dfs2(SRC);
25
     return;
27 }
```

Push Relabel

```
#define MAX_V 1000
   int N;//valid nodes are [0...N-1]
   #define INF 1e9
   //special nodes
   #define SRC 0
   #define SNK 1
   map<int, int> G[MAX_V];//limpiar esto -- unordered_map mejora
   //To add an edge use
   #define add(a, b, w) G[a][b]=w
   11 excess[MAX_V];
   int height[MAX_V], active[MAX_V], cuenta[2*MAX_V+1];
   queue<int> Q;
13
   void enqueue(int v)
14
15
     if (!active[v] && excess[v] > 0) active[v]=true, Q.push(v);
16
17
   void push(int a, int b)
19
     int amt = min(excess[a], ll(G[a][b]));
20
     if(height[a] <= height[b] || amt == 0) return;</pre>
21
     G[a][b]-=amt, G[b][a]+=amt;
     excess[b] += amt, excess[a] -= amt;
     enqueue(b);
25
   void gap(int k)
27
     forn(v, N)
28
29
```

Edge(int u, int v, ll cap): u(u), v(v), cap(cap), flow(0) {}

```
6 |};
       if (height[v] < k) continue;</pre>
30
       cuenta[height[v]]--;
                                                                                           struct Dinic {
31
       height[v] = max(height[v], N+1);
                                                                                              int N;
       cuenta[height[v]]++;
                                                                                              vector<Edge> E;
       enqueue(v);
                                                                                              vector<vector<int>> g;
                                                                                              vector<int> d, pt;
35
                                                                                             Dinic(int N): N(N), E(O), g(N), d(N), pt(N) {} //clear and init
36
   void relabel(int v)
                                                                                              void addEdge(int u, int v, ll cap)
38
                                                                                        14
                                                                                                if (u != v)
     cuenta[height[v]]--;
39
                                                                                        15
     height[v] = 2*N;
40
                                                                                        16
                                                                                                  E.emplace_back(Edge(u, v, cap));
     forall(it, G[v])
                                                                                        17
41
                                                                                                  g[u].emplace_back(E.size() - 1);
     if(it->snd) height[v] = min(height[v], height[it->fst] + 1);
42
                                                                                        18
     cuenta[height[v]]++;
                                                                                                  E.emplace_back(Edge(v, u, 0));
     enqueue(v);
                                                                                                  g[v].emplace_back(E.size() - 1);
44
45
                                                                                        21
   ll maxflow() //0(V^3)
46
                                                                                        22
                                                                                              bool BFS(int S, int T)
                                                                                        23
47
     zero(height), zero(active), zero(cuenta), zero(excess);
                                                                                        24
48
     cuenta[0]=N-1; cuenta[N]=1;
                                                                                                queue<int> q({S});
49
                                                                                        25
                                                                                               fill(d.begin(), d.end(), N + 1);
     height[SRC] = N;
50
                                                                                        26
     active[SRC] = active[SNK] = true;
                                                                                                d[S] = 0;
51
                                                                                        27
                                                                                                while(!q.empty())
     forall(it, G[SRC])
                                                                                        28
52
     {
                                                                                        29
53
       excess[SRC] += it->snd;
                                                                                                  int u = q.front(); q.pop();
54
                                                                                        30
       push(SRC, it->fst);
                                                                                                  if (u == T) break;
                                                                                        31
55
                                                                                                  for (int k: g[u])
                                                                                        32
56
     while(sz(Q))
                                                                                                  {
                                                                                        33
57
                                                                                                    Edge &e = E[k];
                                                                                        34
58
       int v = Q.front(); Q.pop();
                                                                                                    if (e.flow < e.cap && d[e.v] > d[e.u] + 1)
59
                                                                                        35
       active[v]=false;
60
                                                                                        36
       forall(it, G[v]) push(v, it->fst);
                                                                                                      d[e.v] = d[e.u] + 1;
61
                                                                                        37
       if(excess[v] > 0)
                                                                                                      q.emplace(e.v);
                                                                                        38
62
       cuenta[height[v]] == 1? gap(height[v]):relabel(v);
                                                                                                    }
                                                                                        39
63
     }
                                                                                                  }
                                                                                        40
64
     11 mf=0;
65
                                                                                        41
     forall(it, G[SRC]) mf+=G[it->fst][SRC];
                                                                                                return d[T] != N + 1;
66
                                                                                        42
     return mf:
67
                                                                                        43
68 }
                                                                                              11 DFS(int u, int T, 11 flow = -1)
                                                                                        44
                                                                                        45
                                        Dinic
                                                                                                if (u == T || flow == 0) return flow;
                                                                                                for (int &i = pt[u]; i < g[u].size(); ++i)</pre>
                                                                                        47
struct Edge {
                                                                                        48
     int u, v;
                                                                                                  Edge &e = E[g[u][i]];
                                                                                        49
     11 cap, flow;
                                                                                                  Edge &oe = E[g[u][i]^1];
     Edge() {}
```

if (d[e.v] == d[e.u] + 1)

```
52
            11 amt = e.cap - e.flow;
53
            if (flow != -1 \&\& amt > flow) amt = flow;
             if (ll pushed = DFS(e.v, T, amt))
               e.flow += pushed;
57
               oe.flow -= pushed;
58
               return pushed;
59
          }
61
62
       return 0;
63
64
     11 maxFlow(int S,int T)
65
66
       11 \text{ total} = 0;
67
        while(BFS(S, T))
68
69
          fill(pt.begin(), pt.end(), 0);
70
          while (ll flow = DFS(S, T)) total += flow;
71
72
       return total;
73
     }
74
<sub>75</sub> | };
```

Min cost - Max flow

```
const int MAXN=10000:
2 typedef ll tf;
3 typedef 11 tc;
4 const tf INFFLUJO = 1e14;
  const tc INFCOSTO = 1e14;
  struct edge {
    int u, v;
     tf cap, flow;
     tc cost;
     tf rem() { return cap - flow; }
10
11
   int nodes; //numero de nodos
   vector<int> G[MAXN]; // limpiar!
   vector<edge> e; // limpiar!
   void addEdge(int u, int v, tf cap, tc cost)
15
16
    G[u].pb(sz(e)); e.pb((edge){u,v,cap,0,cost});
17
     G[v].pb(sz(e)); e.pb((edge)\{v,u,0,0,-cost\});
tc dist[MAXN], mnCost;
```

```
int pre[MAXN];
   tf cap[MAXN], mxFlow;
   bool in_queue[MAXN];
   void flow(int s, int t)
25
     zero(in_queue);
     mxFlow=mnCost=0;
     while(1)
29
       fill(dist, dist+nodes, INFCOSTO); dist[s] = 0;
30
       memset(pre, -1, sizeof(pre)); pre[s]=0;
31
       zero(cap); cap[s] = INFFLUJO;
32
       queue<int> q; q.push(s); in_queue[s]=1;
       while(sz(q))
34
       {
35
         int u=q.front(); q.pop(); in_queue[u]=0;
36
         for(auto it:G[u])
37
38
            edge &E = e[it];
39
            if(E.rem() && dist[E.v] > dist[u] + E.cost + 1e-9) // ojo EPS
40
41
              dist[E.v]=dist[u]+E.cost;
42
              pre[E.v] = it;
43
              cap[E.v] = min(cap[u], E.rem());
44
             if(!in_queue[E.v]) q.push(E.v), in_queue[E.v]=1;
45
46
47
48
       if (pre[t] == -1) break;
49
       mxFlow +=cap[t];
50
       mnCost +=cap[t]*dist[t];
51
       for (int v = t; v != s; v = e[pre[v]].u)
52
53
         e[pre[v]].flow += cap[t];
54
         e[pre[v]^1].flow -= cap[t];
55
       }
56
57
58 }
```

Utils

Convertir string a num e viceversa

```
#include <sstream>
string num_to_str(int x){
   ostringstream convert;
```

```
convert << x;
return convert.str();
}

int str_to_num(string x){
   int ret;
   istringstream (x) >> ret;
   return ret;
}
```

Truquitos para entradas/salidas

```
//Cantidad de decimales
cout << setprecision(2) << fixed;
//Rellenar con espacios(para justificar)
cout << setfill(''_') << setw(3) << 2 << endl;
//Leer hasta fin de linea
// hacer cin.ignore() antes de getline()
while(getline(cin, line)){
  istringstream is(line);
  while(is >> X)
      cout << X << "_";
      cout << endl;
}</pre>
```

Comparación de Double

```
const double EPS = 1e-9;
    x == y <=> fabs(x-y) < EPS
    x > y <=> x > y + EPS
    x >= y <=> x > y - EPS
```

Iterar subconjuntos

```
for(int sbm=bm; sbm; sbm=(sbm-1)&bm)
```

Limites

Mejorar Lectura de Enteros

```
//Solo para enteros positivos
inline void Scanf(int& a)
{
    char c = 0;
```

```
while(c<33) c = getc(stdin);
a = 0;
while(c>33) a = a*10 + c - '0', c = getc(stdin);
}
```

Compilar C++11 con g++

Dos opciones, útil en Linux.

```
g++ -std=c++11 {file} -o {filename}
g | g++ -std=c++0x {file} -o {filename}
```

Funciones Utiles

Algo	Params	Función
fill, fill_n	f, 1 / n, elem	void llena [f, l) o [f,f+n) con elem
lower_bound, upper_bound	f, l, elem	it al primer ultimo donde se puede insertar elem para que quede ordenada
сору	f, l, resul	hace $resul+i=f+i \ \forall i$
find, find_if, find_first_of	f, l, elem	it encuentra $i \in [f,l)$ tq. $i=elem$,
	/ pred / f2, l2	$\operatorname{pred}(i), i \in [f2,l2)$
count, count_if	f, l, elem/pred	cuenta elem, pred(i)
search	f, 1, f2, 12	busca $[f2,l2) \in [f,l)$
replace, replace_if	f, l, old	cambia old / pred(i) por new
	/ pred, new	
lexicographical_compare	f1,11,f2,12	$bool \text{ con } [f1,l1]_{i}[f2,l2]$
accumulate	f,1,i,[op]	$T = \sum \text{oper de [f,l)}$
inner_product	f1, 11, f2, i	$T = i + [f1, l1) \cdot [f2,)$
partial_sum	f, l, r, [op]	$r+i = \sum /oper de [f,f+i] \forall i \in [f,l)$
builtin_ffs	unsigned int	Pos. del primer 1 desde la derecha
builtin_clz	unsigned int	Cant. de ceros desde la izquierda.
builtin_ctz	unsigned int	Cant. de ceros desde la derecha.
builtin_popcount	unsigned int	Cant. de 1's en x.
builtin_parity	unsigned int	1 si x es par, 0 si es impar.
builtin_XXXXXX11	unsigned 11	= pero para long long's.