

# An experimental investigation of the around / between contrast

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# Approximation and vagueness

- (1) a. **Around 20** people came to the party.  
b. **Between 15 and 25** people came to the party.
- Both (1a) and (1b) convey **uncertainty** about an exact numerical value  $k$ . Yet (1a) is **vague** while (1b) isn't!
  - [Égré et al., 2022]: for any fixed prior distribution over  $k$ , (1a) gives rise to a more “peaked” posterior distribution than (1b) does.

We propose to test this prediction via an online probability-elicitation experiment.

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# A Bayesian model of approximation expressions

- Basic semantics: **around** and **between** denote **intervals**, but in the case of **around** the half-width of the interval is parametrized by a **free variable**  $i$ .
- A Bayesian listener  $\mathcal{L}$  processing **around**  $n$  draws inferences about both  $i$  and  $k$ . An **around**  $n$ -update then redistributes more weight to values of  $k$  closer to  $n$ .

$$\mathcal{P}_{\mathcal{L}}[k \mid \text{around } n] \propto \mathcal{P}_{\mathcal{L}}[k] \sum_{i=|n-k|}^n \mathcal{P}_{\mathcal{L}}[i]$$

- A **between**  $x$  and  $y$ -update homogeneously rescales the weights for values of  $k \in [x; y]$ , and assigns a 0-weight to values of  $k \notin [x; y]$ .

$$\mathcal{P}_{\mathcal{L}}[k \mid \text{between } x \text{ and } y] \propto \begin{cases} \mathcal{P}_{\mathcal{L}}[k] & \text{if } k \in [x; y] \\ 0 & \text{if } k \notin [x; y] \end{cases}$$

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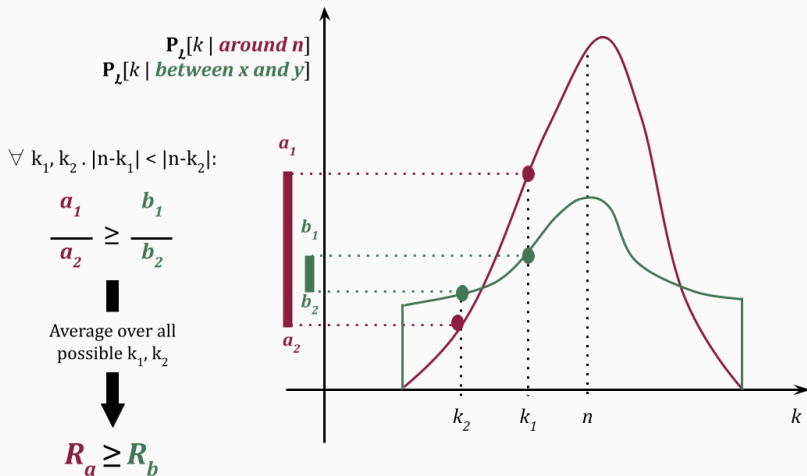
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# Prediction [Égré et al., 2022]



# Experiment

- Preregistered experiment conducted on 240 MTurk participants presented with matching **around n** ( $n=40, 50$  or  $60$ ) and **between x and y** statements.
- Two tasks designed to elicit  $R_a$  and  $R_b$ :
  - Define a suitable interval of possible numerical values compatible with the expression (around or between);
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Peter was at Mary's party yesterday. He doesn't know exactly how many people there were. He says:

**There were around 60 people.**

Please move the left and right cursors (in black) to select an interval in which you think the exact value could be, assuming that what Peter said is true.

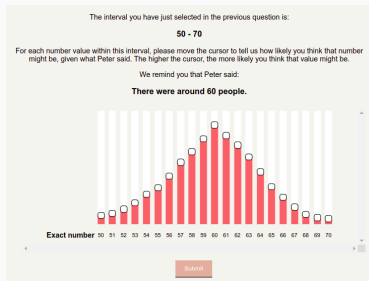
50 - 70

0 10 20 30 40 50 60 70 80 90 100 110 120

Submit

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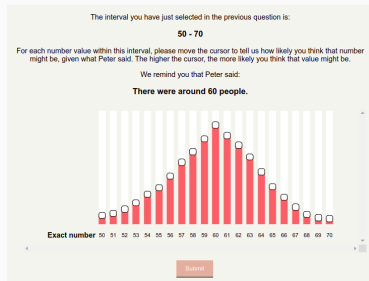
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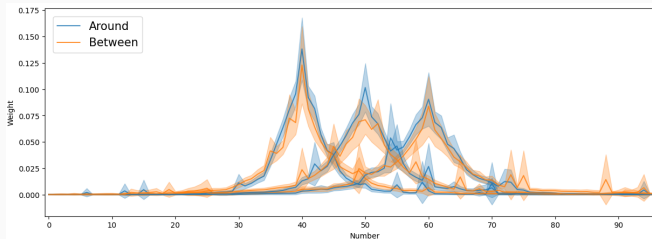
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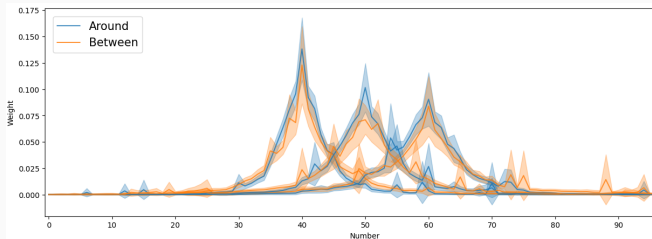


# Results



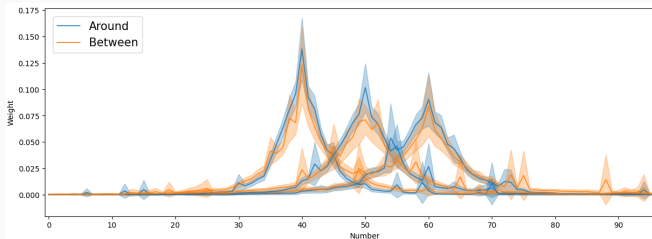
Curious about the results ?

Come see our poster !



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Bergen, L., Levy, R., and Goodman, N. (2016).  
**Pragmatic reasoning through semantic inference.**  
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**On the optimality of vagueness: “around”, “between”, and the gricean maxims.**  
*L&P.*