

# Unit-3

Syntax Analyzer

Menka Patel

Department of Computer Engineering,  
UVPCE

# Overview of Syntax Analyzer

- Also called Parser
- Generate Parse Tree

# Grammar

A grammar is mainly consists of 4 tuples

$G: (S, P, N, T)$

Where,

$S$  = Start symbol

$N$  = Finite set of Non-terminals

$T$  = Finite set of terminals

$P$  = Finite set of production

$S \in N, N \cap T = \emptyset$

# Types of Grammar

1. Type-0 (Unrestricted Grammar)
2. Type-1 (Context-Sensitive Grammar)
3. Type-2 (Context-Free Grammar)
4. Type-3 (Regular Grammar)

# Type-0

- Unrestricted Grammar
- Most General Grammar
- Phrase Structure
- This grammar class can generate recursively enumerable language
- Turing machine

Rule:  $u \rightarrow v$

where,  $u \in v^* N v^*$

$v \in v^*, v = N U T$

# Type-1

- Context Sensitive Grammar
- This grammar class can generate context sensitive language
- Linear bounded automata

Rule:  $u \rightarrow v$

where,  $u \in v^* N v^*$

$v \in v^+, v = N U T$

- Restriction is  $|u| \leq |v|$
- Length increasing grammar

# Type-2

- Context Free Grammar
- This grammar class can generate context free language
- Push down automata

Rule:  $u \rightarrow v$

where,  $u \in N$

$v \in v^*, v = N \cup T$

- $E \rightarrow E + E \mid E * E \mid (E) \mid id$

# Type-3

- Regular Grammar
  - 1) Right linear grammar
  - 2) Left linear grammar
- Finite automata

Rule:  $A \rightarrow aB$

$B \rightarrow b$

Where,  $A, B \in N$

$a \in T$

$b \in T \cup \{\epsilon\}$



# Type-3

- 1) Right linear grammar: If all production of a CFG are of the form

$$A \rightarrow aB, B \rightarrow b$$

where,  $A, B \in N$ ,  $a \in T$ ,  $b \in T \cup \{\epsilon\}$

grammar is right linear grammar.

- 2) Left linear grammar: If all production of a CFG are of the form  $A \rightarrow Ba, B \rightarrow b$

where,  $A, B \in N$ ,  $a \in T$ ,  $b \in T \cup \{\epsilon\}$

grammar is left linear grammar.

# Example

1. Write the left linear and right linear grammar for the regular expression  $RE = 0(10)^*$
2. Identify the type of following grammar:

$A \rightarrow aABc \mid abC$

$CB \rightarrow BC$

$bB \rightarrow bb$

$bC \rightarrow bc$

$cC \rightarrow cc$

# Derivation Tree

- Also known as parse tree

Example:

1) What type of string generated by given grammar?

$$S \rightarrow SS \mid (S) \mid \epsilon$$

Check for the string  $((()))$  accept by grammar or not?

# Derivation Tree

- Left most derivation
- Right most derivation

Example:

2) Generate left most derivation and right most derivation for the string “id + id + id” using following grammar:

$$E \rightarrow E + E \mid E * E \mid \text{id}$$

# Restriction on CFG

- Let  $L$  be a non-empty context free language, then it can be generated by a context free grammar  $G$  with the following properties:
  1. Eliminate useless symbol
  2. Eliminate  $\epsilon$  production
  3. Eliminate unit production
  4. Eliminate cycles

# Restriction on CFG

1. Eliminate useless symbol
  - Identify and eliminate non-generating symbol
  - Identify and eliminate unreachable symbol

For Example:

$$S \rightarrow AB \mid a$$
$$A \rightarrow b$$

# Restriction on CFG

Example:

$$S \rightarrow aB \mid bX$$
$$A \rightarrow BAd \mid bSX \mid a$$
$$B \rightarrow aSB \mid bBX$$
$$X \rightarrow SBD \mid aBx \mid ad$$

# Restriction on CFG

## 2. Eliminate unit production

- $NT \rightarrow \text{one } NT \text{ symbol}$
- Unit production increases the cost of derivation

Algorithm:

While (there exists a unit production  $A \rightarrow B$ )

{

    Select a unit production  $A \rightarrow B$ , such that there exist a production  $B \rightarrow \alpha$ , where  $\alpha$  is a terminal.

    For (every non-unit production,  $B \rightarrow \alpha$ )

    Add production  $A \rightarrow \alpha$  to the grammar

    Eliminate  $A \rightarrow B$  from the grammar

}



# Restriction on CFG

## 2. Eliminate unit production

Example:

Consider the CFG and eliminate unit production from given grammar:

$$S \rightarrow AB$$

$$A \rightarrow a$$

$$B \rightarrow C \mid b$$

$$C \rightarrow D$$

$$D \rightarrow E$$

$$E \rightarrow a$$

# Restriction on CFG

## 2. Eliminate unit production

Example:

Consider the CFG and eliminate unit production from given grammar:

$$S \rightarrow A \mid bb$$

$$A \rightarrow B \mid b$$

$$B \rightarrow S \mid a$$

# Restriction on CFG

## 3. Eliminate $\epsilon$ production and nullable non terminal

➤ Eliminate the production form  $A \rightarrow \epsilon$

For Example: Consider the following grammar and remove nullable NT:

$S \rightarrow aA$

$A \rightarrow b \mid \epsilon$

# Restriction on CFG

## 3. Eliminate $\epsilon$ production and nullable non terminal

➤ Eliminate the production form  $A \rightarrow \epsilon$

For Example: Consider the following grammar and remove nullable NT:

$S \rightarrow ABAC$

$A \rightarrow aA \mid \epsilon$

$B \rightarrow bB \mid \epsilon$

$C \rightarrow c$

# Restriction on CFG

## 4. Eliminate Cycle

➤ Consider an example as follows:

$A \rightarrow B$

$B \rightarrow C$

$C \rightarrow A \mid c$

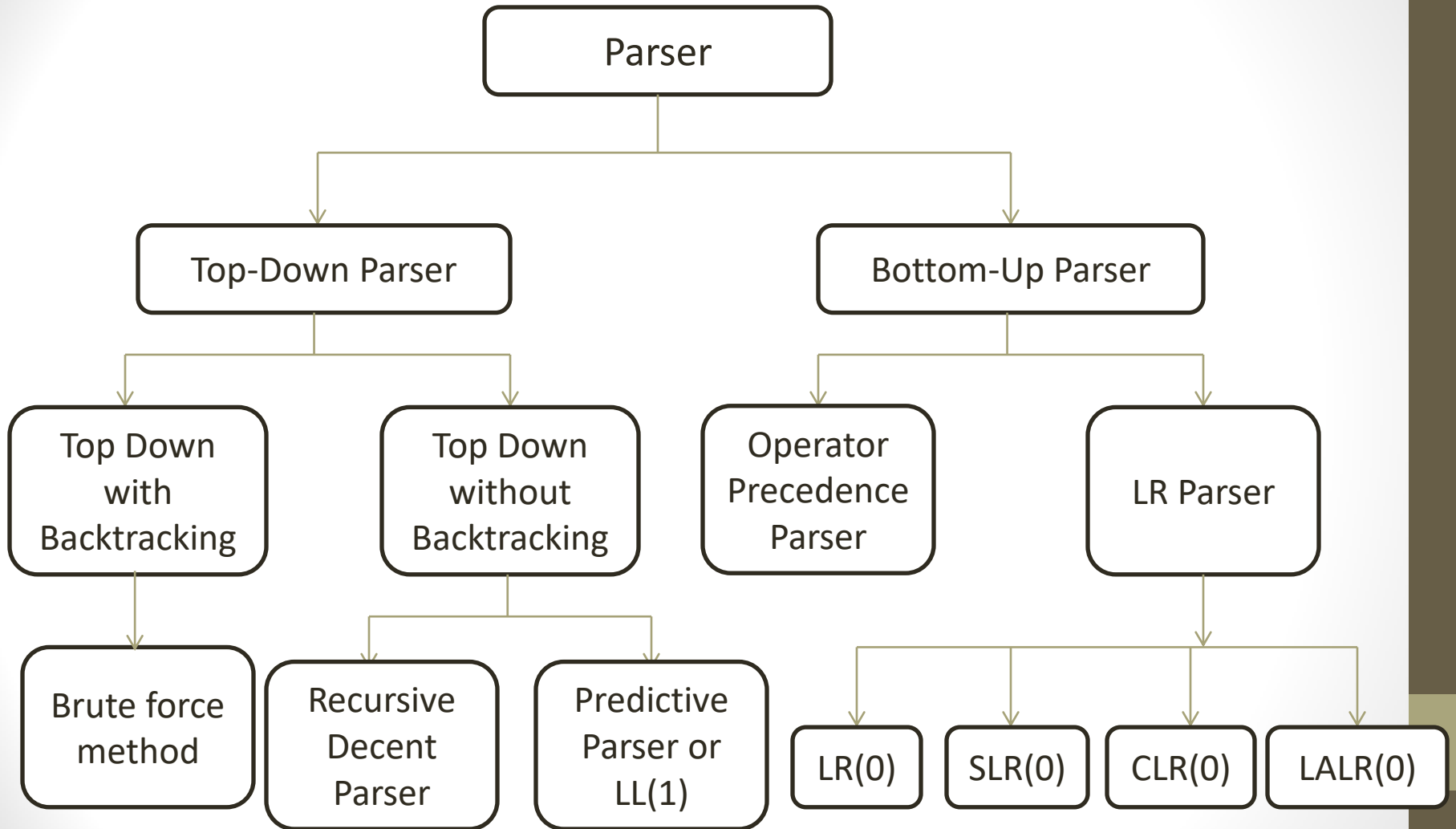
# Restriction on CFG

Example: Eliminate  $\epsilon$  and unit production from following grammar:

$$S \rightarrow A \mid BAabB$$
$$A \rightarrow abA \mid a$$
$$B \rightarrow bB \mid \epsilon$$

# Parser

- A parser for any grammar is a program that takes string  $W$  as input and produces either a parse tree for  $W$ , if  $W$  is a valid sentence of grammar or an error message indicating that  $W$  is not a valid sentence of given grammar, as output.
- A goal of parsing is to determine the syntactic validity for a source string.





# Top Down Parsing

- It is attempts to find the left most derivation for the input string  $W$ , since string  $W$  is scanned by the parser left to right, one symbol/token at a time, and the left most derivation generates the leaves of the parse tree in left-to-right order, which matches the input scan order.
- Derivation of string

# Example

$S \rightarrow aTUe$

$T \rightarrow Tbc \mid b$

$U \rightarrow d$

Derive string 'abbcdde' from given grammar using Top-Down Parser.

# Issues of CFG

- Following are the issues of CFG for the programming languages for top-down parsing:
  1. Left Recursion and Indirect left recursion
  2. Left Factoring
  3. Ambiguity

# Issues of CFG

## 1. Left Recursion

➤ If the left most symbol on the right side is the same as the non-terminal on the left side.

➤ For Example:

$$A \rightarrow A\alpha \mid \beta$$

# Example

$$E \rightarrow E + T \mid T$$
$$T \rightarrow T * F \mid F$$
$$F \rightarrow (E) \mid I$$
$$I \rightarrow a \mid b \mid c$$

Remove left recursion from given CFG.

# Example

$S \rightarrow A$

$A \rightarrow Ad \mid Ae \mid aB \mid aC$

$B \rightarrow bBC \mid f$

$C \rightarrow g$

Remove left recursion from given CFG.