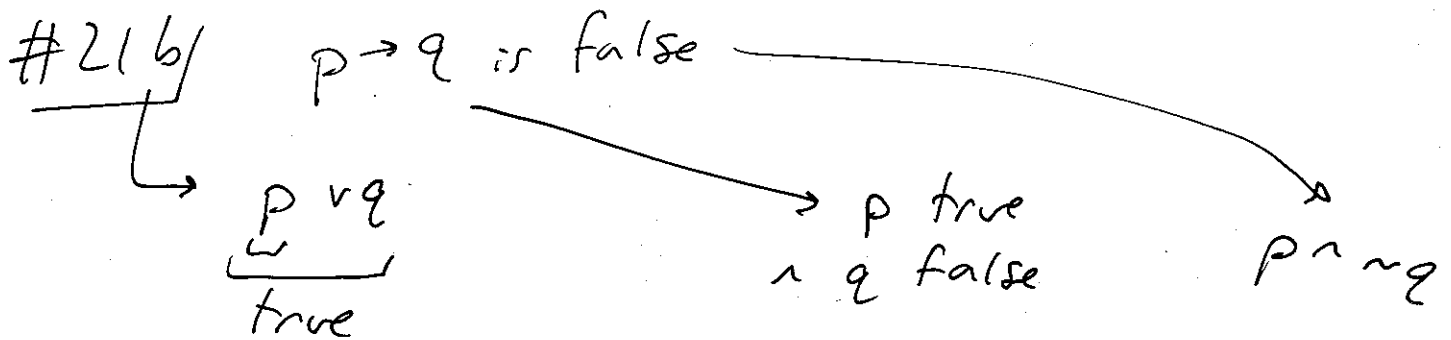


Pg 28 (Handout)



#21c/ $q \rightarrow p$ true by default
false

2a $(p \wedge q)$
2b $(p \vee q)$ } Negate

You have 3 baskets:

-2-

- one with apples only
- one with oranges only
- one with both

The labels on each basket are all wrong.

Pick one fruit from one basket and
then correctly label all 3 baskets

An airline has 100 passengers in line to board.

Passenger 1 ~~has a ticket for seat 1~~
passenger 2 has a ticket for seat 2
etc...

But passenger 1 decides to ignore the rule
and randomly picks a seat instead.

Every other passenger tries to go to their
original seat; if it's occupied already
they randomly pick another seat instead.

What's the probability that passenger 100
ends up in their original seat?

Arguments

- 3 -

statements are true or false
arguments are valid or invalid

dfn: Argument: A sequence of statements (propositions) that ends with a conclusion.

{ If Socrates is a man, then Socrates is mortal.
Socrates is a man.
 \therefore Socrates is mortal.

valid argument form:
$$\begin{array}{l} p \rightarrow q \\ p \\ \therefore q \end{array}$$
 } valid argument form.

dfn: argument form: a sequence of statement forms

dfn: An argument form is VALID when and only when, no matter what particular statements are substituted for the statement variables in its premises:

IF the premises are ALL true,
THEN the conclusion is true.

example:
$$\begin{array}{l} p \rightarrow q \\ p \\ \hline \therefore q \end{array}$$
 } a valid argument form

premise
premise
premise
conclusion

| p | q | p → q |
|-----|---|--------------------|
| (T) | T | (T) ← critical row |
| T | F | F |
| F | T | T |
| F | F | T |

premise 2 conclusion premise 1

conclusion is true
∴ valid arg. form.

Q: Is this valid!

$p \vee (q \vee r)$ premise 1

$\sim r$ premise 2

$\therefore p \vee q$ conclusion

A)

| p | q | r | $\sim r$ | $q \vee r$ | $p \vee (q \vee r)$ | $p \vee q$ |
|---|---|---|----------|------------|---------------------|------------|
| T | T | T | F | T | T | T |
| T | T | F | T | T | T | T |
| T | F | T | F | T | T | T |
| T | F | F | T | F | F | F |
| F | T | T | F | T | T | T |
| F | T | F | T | F | F | F |
| F | F | T | F | T | T | T |
| F | F | F | T | F | F | F |

CR T

looks valid so far
keep going

CR T

looks valid still
keep going

CR T

looks valid again
keep going

F

CONCLUSION

all CR's
have a
true conclusion

ex.

① I am 10 ft or 20 ft or 30 ft tall

② I am not 10 ft tall

\therefore I am 20 ft or 30 ft tall

\therefore This is
a valid arg.
form.

This is valid reasoning
False conclusion

Prosecutor tries to show
they're dealing with
a CR. Defense tries
to show they're
NOT.

Valid? Prove it.

-6-

$$p \rightarrow q \vee \sim r \quad \text{i.e. } p \rightarrow (q \vee \sim r)$$

$$q \rightarrow p \wedge r$$

$$\therefore p \rightarrow r$$

| p | q | r | $\sim r$ | $q \vee \sim r$ | $p \rightarrow q \vee \sim r$ | $p \wedge r$ | $q \rightarrow p \wedge r$ | $p \rightarrow r$ | CR? |
|---|---|---|----------|-----------------|-------------------------------|--------------|----------------------------|-------------------|---------|
| T | T | T | F | T | T | T | T | T | go on ✓ |
| T | T | F | T | T | T | F | F | F | stop ✓ |
| T | F | T | F | F | F | T | T | T | ✓ |
| T | F | F | T | T | T | F | F | F | ✓ |
| F | T | T | F | T | T | T | T | T | ✓ |
| F | T | F | T | T | T | F | F | F | ✓ |
| F | F | T | F | F | F | T | T | T | ✓ |
| F | F | F | T | T | T | F | F | F | ✓ |

(p1)
(p2)

(c)

invalid

$P \rightarrow q$
 P
 $\therefore q$

| P | q | $P \rightarrow q$ |
|------|-----|-------------------------|
| (T) | T | (T) ✓ valid ; only 1 CR |
| T | F | F |
| F | T | T |
| F | F | T |
| (P1) | (C) | (P2) |

└──────────┘
2 premises

Some valid argument forms (rules of inference)

| | | |
|--|---------------|--------------|
| $P \rightarrow q$ P $\therefore q$ | modus ponens | } know these |
| <hr/> $P \rightarrow q$ $\sim q$ $\therefore \sim p$ | modus tollens | |

Valid?

If we are in Canada, then Mickey Mouse is prime minister.

We are in Canada

∴ Mickey Mouse is prime minister.

VALID ; has the form of modus ponens

Valid?

If we are in Canada then we are bordered by }
the Pacific + Atlantic oceans.

We are bordered by the Pacific + Atlantic oceans.

∴ we are in Canada.

Invalid

CONVERSE ERROR

Ask an American: True premise
True premise
False conclusion

True even
if an
American
says it.

If Shaun is a cheater then Shaun sits in the
back row.

Shaun sits in the back row
Shaun is a cheater

CONVERSE ERROR

If interest rates are going up
then stock market prices are going down.

Interest rates are not going up.

∴ Stock market prices are not going down.

Invalid

INVERSE ERROR

Q) Can you have a valid argument
with a false conclusion?

$P \rightarrow Q$
 P
∴ Q

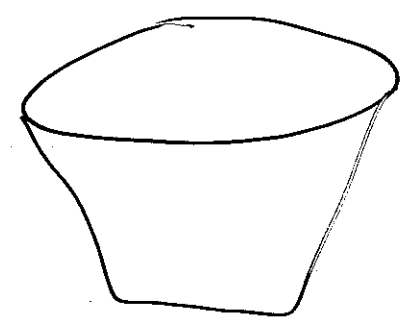
yes

| P | Q | $P \rightarrow Q$ |
|------|-----|-------------------|
| T | T | T |
| T | F | F |
| F | T | T |
| F | F | T |
| (P2) | (C) | (P1) |

CR VALID

Arrow points to the row where P is True and Q is False (T, F, F).

All the
balls in
the bowl
are red.



T or F

TRUE

Tanyana Shemura

Andrew Wiles

Nova ^{PS}

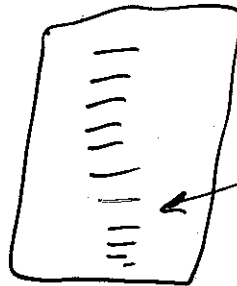
Fermat's Last Thm

400

Modular
Forms

elliptic
curves

+ - * /



Valid?

$p \rightarrow q$
 $q \rightarrow r$
 $\therefore p \rightarrow r$

VALID?

Law of
transitivity

| | | | (P1) | (P2) | (C) | |
|---|---|---|-------------------|-------------------|-------------------|-------|
| P | q | r | $p \rightarrow q$ | $q \rightarrow r$ | $p \rightarrow r$ | CR? |
| T | T | T | T | T | T | ✓ |
| T | T | F | T | F | F | False |
| T | F | T | F | T | T | True |
| T | F | F | F | F | T | True |
| T | T | T | T | T | T | ✓ |
| T | T | F | T | F | F | False |
| T | F | T | T | T | T | ✓ |
| T | F | F | T | F | T | ✓ |
| F | T | T | F | T | T | ✓ |
| F | T | F | F | F | T | ✓ |
| F | F | T | T | T | T | ✓ |
| F | F | F | T | F | T | ✓ |

VALID

Handout: Rd pg 33-40
 1.3 especially fallacies

-11-
 -11-

Valid? $P \rightarrow Q$
 $Q \rightarrow P$
 $\therefore P \vee Q$

| P | Q | $P \rightarrow Q$ | $Q \rightarrow P$ | $P \vee Q$ | |
|---|---|-------------------|-------------------|------------|----------------|
| T | T | T | T | T | looks valid... |
| T | F | F | T | F | |
| F | T | T | F | F | |
| F | F | T | T | F | not valid! |
| | | (P1) | (P2) | (C) | |

Homework: Handout:
 1.3 page 41

4
 10
 11
 136
 23
 28
 32
 38
 40

NOTE:
 assignment
 questions:
 No need to
 Simplify

$P \rightarrow Q$
 $\sim P$
 $\therefore \sim Q$ } invert
 error

