

$$a_0 = \tan^{-1} \left(\frac{y_1}{x_1} \right)$$

Now we have to find distance between (x_1, y_1) and (0,0):

$$distance = \sqrt{x^2 + y^2}$$

d is half of the distance.

$$d = \frac{1}{2}\sqrt{x^2 + y^2}$$

Now we use tan, you can use cos also here.

$$h^2 + d^2 = 1^2$$

$$h^2 = 1 - d^2$$

$$h = \sqrt{1 - d^2}$$

$$h = \sqrt{1 - \left(\frac{1}{2}\sqrt{x^2 + y^2}\right)^2}$$

$$h = \sqrt{1 - \frac{1}{4}(x^2 + y^2)}$$

$$h = \sqrt{\frac{4 - x^2 - y^2}{4}}$$

$$h = \frac{1}{2}\sqrt{4 - x^2 - y^2}$$

$$\theta = \tan^{-1}\left(\frac{h}{d}\right)$$

$$\theta = \tan^{-1} \left[\sqrt{\frac{4 - x_1^2 - y_1^2}{x^2 + y^2}} \right]$$

$$a_1 = a_0 + \theta$$

$$a_1 = \tan^{-1}\left(\frac{y_1}{x_1}\right) + \tan^{-1}\left[\sqrt{\frac{4-x_1^2-y_1^2}{x^2+y^2}}\right]$$

Our main target is to find (x, y):

$$(x,y) = (\cos a_1, \sin a_1)$$