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DAA - Tutorial - 6

Q1

Ans

Minimum spanning tree : A (MST) is a subset of the edges of a connected edge-weighted undirected graph that connects all the vertices together, without any cycles and with the minimum possible total edge weight.

Applications :-

- i) Consider n stations are to be linked using a communication network and laying of communication link b/w any two stations involve a cost.
- ii) Suppose you meant to construct highways or railroads spanning several cities then we can use the concept of minimum spanning tree.
- iii) Design LAN.
- iv) Laying pipelines connecting offshore drilling sites, refineries and consumer markets.

02

Solⁿ

Time complexity of Prim's algorithms

$$O((V+E) \log V)$$

$$\text{Space complexity} = O(V)$$

Kruskal's Algo

$$T.C \Rightarrow O(E \log V)$$

$$S.C \Rightarrow O(V)$$

Dijkstra's Algo

$$T.C \Rightarrow O(V^2)$$

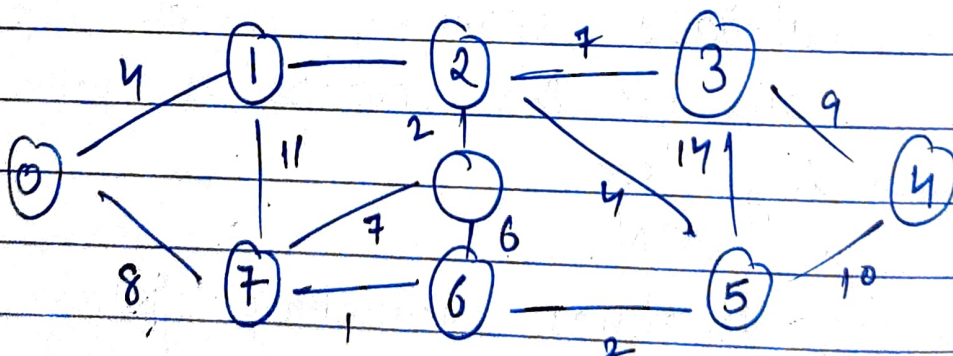
$$S.C \Rightarrow O(V^2)$$

Bellmanford Algo

$$T.C \Rightarrow O(VE)$$

$$S.C \Rightarrow O(E)$$

03

Solⁿ

Kruskali algo

0	v	w
6	7	1
5	6	2
2	8	2
0	1	4
2	5	4
6	8	6
2	3	7
7	8	7
0	7	8
1	2	8
4	3	9
4	5	10

0	v	w	
1	7	11	X
3	5	14	X

Q4

Solⁿ

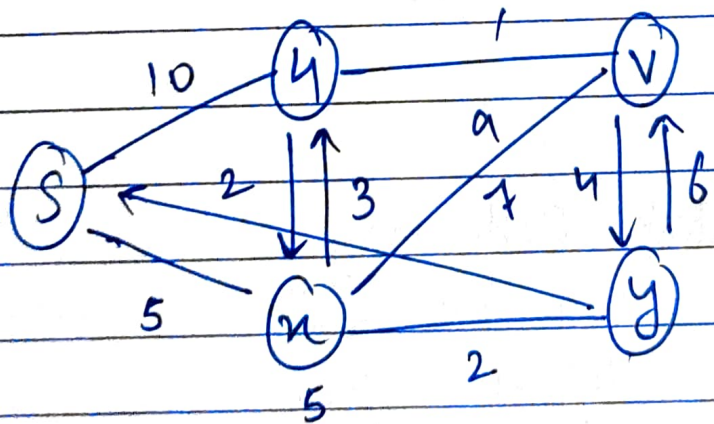
i) The shortest path may change. The reason is there may be different numbers of edges in different paths from 's' to 't'. For eg. let shortest path be of weight 15 and has edge 5. Let there be another path with 2 edge and total

weight 25. The weight of the shortest path is increased by 5×10 and become $15 + 50$.

ii) If we multiply all edges weight by 10, the shortest path don't change. The reason is simple, weight of all path from 's' to 't' get multiplied by same amount. The no. of edges on a path don't matter. It is like changing limits of weight.

Q5
Solⁿ

Dijkstra Algorithm



node	Shortest dist. from source node
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u	8
n	5
v	9
y	7

Bellmanford Algo.

1st	→	$\overset{0}{s}$	$\overset{10}{u}$	$\overset{\infty}{v}$	$\overset{5}{n}$	$\overset{\infty}{y}$
2 nd	→	$\overset{0}{s}$	$\overset{10}{u}$	$\overset{11.1}{v}$	$\overset{5}{n}$	$\overset{\infty}{y}$
3 rd	→	$\overset{0}{s}$	$\overset{8}{u}$	$\overset{9}{v}$	$\overset{5}{n}$	$\overset{7}{y}$
4th	→	$\overset{0}{s}$	$\overset{8}{u}$	$\overset{9}{v}$	$\overset{5}{n}$	$\overset{7}{y}$

