

```
import collections
```

```
class TreeNode:
```

```
    def __init__(self, val=0, left=None, right=None):
```

```
        self.val = val
```

```
        self.left = left
```

```
        self.right = right
```

```
class Codec:
```

```
    def serialize(self, root):
```

```
        """Encodes a tree to a single string using level-order traversal (BFS)."""
```

```
        if not root:
```

```
            return "null"
```

```
        queue = collections.deque([root])
```

```
        result = []
```

```
        while queue:
```

```
            node = queue.popleft()
```

```
            if node:
```

```
                result.append(str(node.val))
```

```
                queue.append(node.left)
```

```
                queue.append(node.right)
```

```
            else:
```

```
                result.append("null") # Mark null nodes
```

```
        return ",".join(result)
```

```
    def deserialize(self, data):
```

```
"""Decodes the string back into a binary tree using BFS."""
```

```
if data == "null":
```

```
    return None
```

```
nodes = data.split(",")
```

```
root = TreeNode(int(nodes[0]))
```

```
queue = collections.deque([root])
```

```
index = 1
```

```
while queue:
```

```
    node = queue.popleft()
```

```
    if nodes[index] != "null":
```

```
        node.left = TreeNode(int(nodes[index]))
```

```
        queue.append(node.left)
```

```
    index += 1
```

```
    if nodes[index] != "null":
```

```
        node.right = TreeNode(int(nodes[index]))
```

```
        queue.append(node.right)
```

```
    index += 1
```

```
return root
```

```
# Example Usage
```

```
codec = Codec()
```

```
root = TreeNode(1, TreeNode(2), TreeNode(3, TreeNode(4), TreeNode(5)))
```

```
serialized = codec.serialize(root)
```

```
print("Serialized:", serialized)
```

```
deserialized = codec.deserialize(serialized)
print("Deserialized Root Value:", deserialized.val)
```

```
from collections import deque
```

```
class MaxFlow:
```

```
    def __init__(self, graph):
        self.graph = [row[:] for row in graph] # Copy graph to preserve original
        self.V = len(graph) # Number of vertices
```

```
    def bfs(self, source, sink, parent):
```

```
        """Finds an augmenting path using BFS and fills parent array."""
```

```
        visited = [False] * self.V
```

```
        queue = deque([source])
```

```
        visited[source] = True
```

```
        while queue:
```

```
            u = queue.popleft()
```

```
            for v in range(self.V):
```

```
                if not visited[v] and self.graph[u][v] > 0: # If capacity exists
```

```
                    queue.append(v)
```

```
                    visited[v] = True
```

```
                    parent[v] = u # Store path
```

```
            if v == sink: # If sink is reached, return True
```

```
        return True
    return False
```

```
def ford_ulkerson(self, source, sink):
    """Returns the maximum flow from source to sink."""
    parent = [-1] * self.V
    max_flow = 0

    while self.bfs(source, sink, parent): # While augmenting path exists
        path_flow = float('Inf')
        v = sink

        # Find the bottleneck (minimum capacity in path)
        while v != source:
            u = parent[v]
            path_flow = min(path_flow, self.graph[u][v])
            v = u

        # Update residual capacities
        v = sink
        while v != source:
            u = parent[v]
            self.graph[u][v] -= path_flow
            self.graph[v][u] += path_flow # Reverse flow
            v = u

        max_flow += path_flow # Add to total flow

    return max_flow
```

Example Usage

```
graph = [[0, 16, 13, 0, 0, 0],  
         [0, 0, 10, 12, 0, 0],  
         [0, 4, 0, 0, 14, 0],  
         [0, 0, 9, 0, 0, 20],  
         [0, 0, 0, 7, 0, 4],  
         [0, 0, 0, 0, 0, 0]]
```

```
max_flow_solver = MaxFlow(graph)
```

```
source, sink = 0, 5
```

```
print("Maximum Flow:", max_flow_solver.ford_fulkerson(source, sink))
```

```
def min_edit_distance(word1, word2):
```

```
    m, n = len(word1), len(word2)
```

```
    dp = [[0] * (n + 1) for _ in range(m + 1)]
```

```
    # Initialize base cases
```

```
    for i in range(m + 1):
```

```
        dp[i][0] = i # Deleting all characters from word1
```

```
    for j in range(n + 1):
```

```
        dp[0][j] = j # Inserting all characters to word1
```

```
    # Fill DP table
```

```
    for i in range(1, m + 1):
```

```
        for j in range(1, n + 1):
```

```
            if word1[i - 1] == word2[j - 1]: # No change needed
```

```

        dp[i][j] = dp[i - 1][j - 1]
    else:
        dp[i][j] = min(
            dp[i - 1][j] + 1, # Delete
            dp[i][j - 1] + 1, # Insert
            dp[i - 1][j - 1] + 1 # Replace
        )

    return dp[m][n]

# Example Usage
word1 = "kitten"
word2 = "sitting"
print("Edit Distance:", min_edit_distance(word1, word2))

```

```

class TreeNode:
    def __init__(self, val=0, left=None, right=None):
        self.val = val
        self.left = left
        self.right = right

def inorder_traversal(root, elements):
    """Helper function to perform in-order traversal."""
    if root:
        inorder_traversal(root.left, elements)

```

```
elements.append(root.val)

inorder_traversal(root.right, elements)
```

```
def kth_smallest_element(root, k):
    elements = []
    inorder_traversal(root, elements)
    return elements[k - 1] # k-th smallest (1-based index)
```

```
# Example Usage
```

```
root = TreeNode(3)
root.left = TreeNode(1)
root.left.right = TreeNode(2)
root.right = TreeNode(4)
```

```
k = 2
print("K-th Smallest Element:", kth_smallest_element(root, k))
```

```
def max_product_subarray(nums):
    if not nums:
        return 0 # Edge case: Empty list

    max_product = min_product = result = nums[0]

    for i in range(1, len(nums)):
```

```
if nums[i] < 0: # Swap max & min when encountering a negative number
```

```
    max_product, min_product = min_product, max_product
```

```
max_product = max(nums[i], max_product * nums[i])
```

```
min_product = min(nums[i], min_product * nums[i])
```

```
result = max(result, max_product) # Update global max
```

```
return result
```

```
# Example Usage
```

```
nums = [2, 3, -2, 4]
```

```
print("Maximum Product Subarray:", max_product_subarray(nums))
```

```
from collections import defaultdict
```

```
def find_all_paths(graph, start, end, path=[], all_paths=[]):
```

```
    path.append(start) # Add current node to path
```

```
    if start == end:
```

```
        all_paths.append(list(path)) # Store a copy of the valid path
```

```
    else:
```

```
        for neighbor in graph[start]: # Explore neighbors
```

```
            if neighbor not in path: # Avoid cycles
```

```
                find_all_paths(graph, neighbor, end, path, all_paths)
```



```
path.pop() # Backtrack to explore other paths  
return all_paths
```

```
# Example Usage
```

```
graph = {  
    0: [1, 2],  
    1: [3],  
    2: [3, 4],  
    3: [5],  
    4: [5],  
    5: []  
}
```

```
start_node, end_node = 0, 5  
all_paths = find_all_paths(graph, start_node, end_node)  
print("All Paths:", all_paths)
```