

$$\left\{ \begin{pmatrix} 1 \\ 10 \end{pmatrix}, \begin{pmatrix} 1 \\ 6 \end{pmatrix}, \begin{pmatrix} 4 \\ 11 \end{pmatrix}, \begin{pmatrix} 6 \\ 1 \end{pmatrix}, \begin{pmatrix} 7 \\ 6 \end{pmatrix}, \begin{pmatrix} 10 \\ 4 \end{pmatrix} \right\}$$

The support vectors $\begin{pmatrix} 1 \\ 6 \end{pmatrix}, \begin{pmatrix} 4 \\ 11 \end{pmatrix}, \begin{pmatrix} 7 \\ 6 \end{pmatrix}$

We will add one for the bias:

$$s_1 = \begin{pmatrix} 1 \\ 6 \\ 1 \end{pmatrix} \quad s_2 = \begin{pmatrix} 4 \\ 11 \\ 1 \end{pmatrix} \quad s_3 = \begin{pmatrix} 7 \\ 6 \\ 1 \end{pmatrix}$$

$$\alpha_1 s_1 s_1 + \alpha_2 s_2 s_1 + \alpha_3 s_3 s_1 = -1$$

$$\alpha_1 s_1 s_2 + \alpha_2 s_2 s_2 + \alpha_3 s_3 s_2 = -1$$

$$\alpha_1 s_1 s_3 + \alpha_2 s_2 s_3 + \alpha_3 s_3 s_3 = 1$$

\Downarrow

$$\alpha_1 \begin{pmatrix} 1 \\ 6 \\ 1 \end{pmatrix} \begin{pmatrix} 1 \\ 6 \\ 1 \end{pmatrix} + \alpha_2 \begin{pmatrix} 4 \\ 11 \\ 1 \end{pmatrix} \begin{pmatrix} 1 \\ 6 \\ 1 \end{pmatrix} + \alpha_3 \begin{pmatrix} 7 \\ 6 \\ 1 \end{pmatrix} \begin{pmatrix} 1 \\ 6 \\ 1 \end{pmatrix} = -1$$

$$\alpha_1 \begin{pmatrix} 1 \\ 6 \\ 1 \end{pmatrix} \begin{pmatrix} 4 \\ 11 \\ 1 \end{pmatrix} + \alpha_2 \begin{pmatrix} 4 \\ 11 \\ 1 \end{pmatrix} \begin{pmatrix} 4 \\ 11 \\ 1 \end{pmatrix} + \alpha_3 \begin{pmatrix} 7 \\ 6 \\ 1 \end{pmatrix} \begin{pmatrix} 4 \\ 11 \\ 1 \end{pmatrix} = -1$$

$$\alpha_1 \begin{pmatrix} 1 \\ 6 \\ 1 \end{pmatrix} \begin{pmatrix} 7 \\ 6 \\ 1 \end{pmatrix} + \alpha_2 \begin{pmatrix} 4 \\ 11 \\ 1 \end{pmatrix} \begin{pmatrix} 7 \\ 6 \\ 1 \end{pmatrix} + \alpha_3 \begin{pmatrix} 7 \\ 6 \\ 1 \end{pmatrix} \begin{pmatrix} 7 \\ 6 \\ 1 \end{pmatrix} = 1$$

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$$\begin{cases} 38\alpha_1 + 71\alpha_2 + 44\alpha_3 = -1 \\ 71\alpha_1 + 138\alpha_2 + 95\alpha_3 = -1 \\ 44\alpha_1 + 95\alpha_2 + 86\alpha_3 = 1 \end{cases} \Rightarrow$$

$$\alpha_1 = -0.271$$

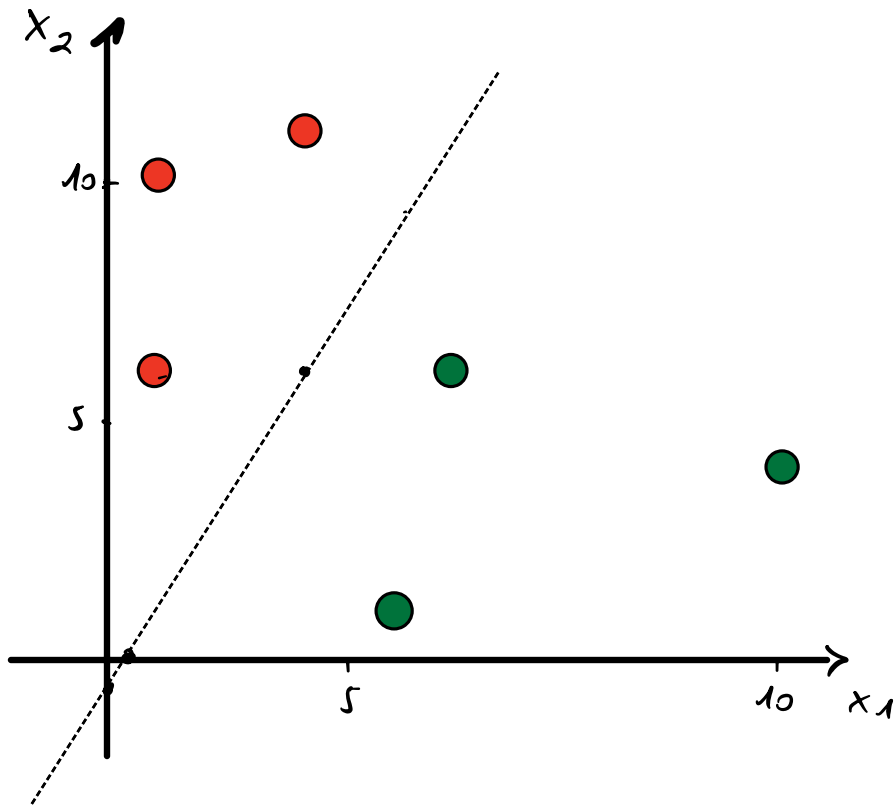
$$\alpha_2 = 0.12$$

$$\alpha_3 = 0.017$$

$$-0.271 \begin{pmatrix} 1 \\ 6 \\ 1 \end{pmatrix} + 0.12 \begin{pmatrix} 4 \\ 11 \\ 1 \end{pmatrix} + 0.017 \begin{pmatrix} 7 \\ 6 \\ 1 \end{pmatrix} = \begin{pmatrix} 0.328 \\ -0.204 \\ -0.134 \end{pmatrix}$$

Hyper plane (0.328, -0.204) offset -0.134

$$0 = 0.328x_1 - 0.204x_2 - 0.134$$



$$\sqrt{w^T \cdot w} = \sqrt{(0.328, -0.204) \begin{pmatrix} 0.328 \\ -0.204 \end{pmatrix}} = \sqrt{0.148}$$

$$\text{Margin} = \frac{2}{\sqrt{0.148}} = 5.194$$