\leftarrow	Week 3 - Problem Set Graded Quiz • 20 min

1. Suppose a MAC system (S,V) is used to protect files in a file system

2. Let (S,V) be a secure MAC defined over (K,M,T) where $M=\{0,1\}^n$ and $T=\{0,1\}^{128}$. That is, the key space is K, message space is $\{0,1\}^n$, and tag space is $\{0,1\}^{128}$. Which of the following is a secure MAC: (as usual, we use | to denote string concatenation) (i.e., V'(k,m,t) outputs $^{ hicktooldown}$ 1" if t is a valid

! Try again once you are ready

by appending a MAC tag to each file. The MAC signing algorithm ${\cal S}$

Replacing the contents of a file with the concatenation of two files

The MAC tag will fail to verify if any file data is changed.

 $V'(k, m, t) = [V(k, m, t) \text{ or } V(k, m \oplus 1^n, t)]$

is applied to the file contents and nothing else. What tampering attacks

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are not prevented by this system?

Changing the first byte of the file contents.

Changing the name of a file.

Appending data to a file.

on the file system.

Incorrect

TO PASS 80% or higher

LATEST SUBMISSION GRADE

40%

tag for either m or $m \oplus 1^n$) $igspace S'(k,m) = S(k,m\oplus m)$ and $V'(k,m,t) = V(k, m \oplus m, t)$ This should not be selected This construction is insecure because an adversary can request the tag for $m=0^{n}\,$ and thereby obtain a tag for any message. This follows from the fact that $m\oplus m=0$. $igspace S'(k,m) = S(k,m\oplus 1^n)$ and $V'(k,m,t) = V(k,m \oplus 1^n,t)$ Correct a forger for (S',V') gives a forger for (S,V). $V'ig(k,m,(t_1,t_2)ig) = \left\{egin{array}{ll} V(k,m,t_1) & ext{if } t_1 = t_2 \ ext{"0"} & ext{otherwise} \end{array}
ight.$ (i.e., $V'\left(k,m,\left(t_{1},t_{2}
ight)
ight)$ only outputs "1" if t_1 and t_2 are equal and valid) \square $S'(k,m) = \left\{egin{array}{ll} S(k,1^n) & ext{if } m=0^n \ S(k,m) & ext{otherwise} \end{array}
ight.$ and $V'(k,m) = \left\{ egin{aligned} V(k,1^n,t) & ext{if } m=0^n \ V(k,m,t) & ext{otherwise} \end{aligned}
ight.$ $S'((k_1,k_2), m) = (S(k_1,m), S(k_2,m))$ and $V'((k_1, k_2), m, (t_1, t_2)) = [V(k_1, m, t_1) \text{ and } V(k_2, m, t_2)]$ (i.e., $V'ig((k_1,k_2),m,(t_1,t_2)ig)$ outputs ``1" if both t_1 and t_2 are valid tags)

Correct a forger for (S',V') gives a forger for (S,V). 3. Recall that the ECBC-MAC uses a fixed IV (in the lecture we simply set the IV to 0). Suppose instead chose a random IV for every message being signed and include the IV in the tag. In other words, $S(k,m) := (r, \ \mathrm{ECBC}_r(k,m))$ where $\mathrm{ECBC}_r(k,m)$ refers to the ECBC function using r as the IV. The verification algorithm V given key k, message m, and tag (r,t) outputs ``1" if $t=\mathrm{ECBC}_r\left(k,m
ight)$ and outputs ``0" otherwise. The resulting MAC system is insecure. An attacker can query for the tag of the 1-block message \boldsymbol{m} and obtain the tag (r,t). He can then generate the following existential forgery: (we assume that the underlying block cipher operates on n-bit blocks) \bigcirc The tag $(r\oplus 1^n,\ t)$ is a valid tag for the 1-block message $m\oplus 1^n$. O The tag $(r, t \oplus r)$ is a valid tag for the 1-block message 0^n .

 \bigcirc The tag $(r\oplus t,\ m)$ is a valid tag for the 1-block message 0^n . $igoreal{igoreal}$ The tag $(m\oplus t,\ r)$ is a valid tag for the 1-block message 0^n . Incorrect 4. Suppose Alice is broadcasting packets to 6 recipients B_1,\dots,B_6 . Privacy is not important but integrity is. In other words, each of B_1,\dots,B_6 should be assured that the packets he is receiving were sent by Alice. Alice decides to use a MAC. Suppose Alice and B_1,\dots,B_6 all share a secret key k. Alice computes a tag for every packet she sends using key k. Each user B_i verifies the tag when receiving the packet and drops the packet if the tag is invalid. Alice notices that this scheme is insecure because user $B_{\scriptscriptstyle 1}$ can use the key k to send packets with a valid tag to users B_2,\ldots,B_6 and they will all be fooled into thinking that these packets are from Alice. Instead, Alice sets up a set of 4 secret keys $S = \{k_1, \dots, k_4\}$. She gives each user B_i some subset $S_{f i}\subseteq S$

The right half of the tag, r, is not likely to be the

result of the CBC MAC.

because he does not have k_3 or k_4 .

✓ Correct

size)

0 6

O 5

4

○ n

✓ Correct

H'(m) = H(0)

H'(m) = H(m)[0, ..., 31]

 $H'(m) = H(m) \| H(m)$

(i.e. output the first 32 bits of the hash)

 $H_{2}\left(x
ight) ,y$ are a collision for H_{1} .

 $H_{1}\left(x
ight) ,H_{1}\left(y
ight)$ are a collision for H_{2} .

igcup Either $H_2\left(x
ight),H_2\left(y
ight)$ are a collision for H_1 or

If $H_{2}\left(H_{1}\left(x
ight)
ight)=H_{2}\left(H_{1}\left(y
ight)
ight)$ then

lacksquare Either x,y are a collision for H_1 or

x,y are a collision for H_2 .

✓ Correct

a collision finder for H^\prime gives a collision finder for H .

compute the tag for a long message m comprising of n AES blocks.

to compute the tag for m^\prime from the tag for m and the MAC key? (in this question please ignore

message padding and simply assume that the message length is always a multiple of the AES block

Let m' be the n-block message obtained from m by flipping the

last bit of m (i.e. if the last bit of m is b then the last bit

of m' is $b \oplus 1$). How many calls to AES would it take

in M such that H(x) = H(y) = H(z)? O(|T|^{2/3}) $O(|T|^{1/2})$ ○ O(|T|) $O(|T|^{1/3})$ ✓ Correct An informal argument for this is as follows: suppose we samples is n choose 3 which is $O(n^3)$. For a particular triple x,y,z to be a 3-way collision we need H(x)=H(y)and H(x)=H(z). Since each one of these two events happens with probability $1/\lvert T \rvert$ (assuming H behaves like a random function) the probability that a particular triple is a 3-way collision is $O(1/|T|^2)$. Using the union bound, the probability that some triple is a 3-way collision is $O(n^3/|T|^2)$ and since we want this probability to be close to 1, the bound on \boldsymbol{n} follows.

10. Let H:M o T be a random hash function where $|M|\gg |T|$ (i.e. the size of M is much larger than the size of T). In lecture we showed that finding a collision on H can be done with $O(|T|^{1/2})$ random samples of $\boldsymbol{H}.$ How many random samples would it take until we obtain a three way collision, namely distinct strings $x,y,z\,$ collect n random samples. The number of triples among the n

Incorrect You did not choose an option. 9. Repeat the previous question, but now to find a collision for the compression function $f_2(x,y) = \operatorname{AES}(x,x) \bigoplus y$ Which of the following methods finds the required (x_1,y_1) and (x_2,y_2) ? igotimes Choose x_1, x_2, y_1 arbitrarily (with $x_1
eq x_2$) and set $y_2 = y_1 \oplus x_1 \oplus AES(x_2, x_2)$ \bigcirc Choose x_1, x_2, y_1 arbitrarily (with $x_1
eq x_2$) and set $y_2 = AES(x_1, x_1) \oplus AES(x_2, x_2)$ \bigcirc Choose x_1, x_2, y_1 arbitrarily (with $x_1
eq x_2$) and set $y_2 = y_1 \oplus AES(x_1, x_1)$ \bigcirc Choose x_1, x_2, y_1 arbitrarily (with $x_1
eq x_2$) and set $y_2 = y_1 \oplus AES(x_1, x_1) \oplus AES(x_2, x_2)$ Incorrect This does not work

either $H_{1}\left(x
ight) =H_{1}\left(y
ight)$ and x
eq y , thereby giving us a collision on H_1 . Or $H_1(x)
eq H_1(y)$ but $H_2(H_1(x))=H_2(H_1(y))$ giving us a collision on H_2 . Either way we obtain a collision on H_1 or H_2 as required. 8. In this question you are asked to find a collision for the compression function: $f_1(x,y) = AES(y,x) \bigoplus y$ where $\operatorname{AES}(x,y)$ is the AES-128 encryption of y under key x. Your goal is to find two distinct pairs (x_1,y_1) and (x_2,y_2) such that $f_1(x_1,y_1)=f_1(x_2,y_2)$. Which of the following methods finds the required (x_1,y_1) and (x_2,y_2) ? Choose x_1,y_1,y_2 arbitrarily (with $y_1 \neq y_2$) and let $v := AES(y_1,x_1)$. Set $x_2=AES^{-1}(y_2,\ v\oplus y_2)$ \bigcirc Choose x_1,y_1,y_2 arbitrarily (with $y_1
eq y_2$) and let $v := AES(y_1,x_1)$. Set $x_2 = AES^{-1}(y_2,\ v \oplus y_1 \oplus y_2)$ \bigcirc Choose x_1,y_1,x_2 arbitrarily (with $x_1
eq x_2$) and let $v := AES(y_1,x_1)$. Set $y_2 = AES^{-1}(x_2,\ v \oplus y_1 \oplus x_2)$ \bigcirc Choose x_1,y_1,y_2 arbitrarily (with $y_1
eq y_2$) and let $v := AES(y_1,x_1)$. Set $x_2 = AES^{-1}(y_2,\ v \oplus y_1)$

✓ Correct a collision finder for H^\prime gives a collision finder for H . H'(m) = H(m[0,...,|m|-2])(i.e. hash m without its last bit) 7. Suppose H_1 and H_2 are collision resistant hash functions mapping inputs in a set M to $\{0,1\}^{256}$. Our goal is to show that the function $H_2\left(H_1\left(m
ight)
ight)$ is also collision resistant. We prove the contra-positive: suppose $H_2(H_1(\cdot))$ is not collision resistant, that is, we are given $x \neq y$ such that $H_2\left(H_1\left(x\right)\right) = H_2\left(H_1\left(y\right)\right)$. We build a collision for either H_1 or for H_2 . This will prove that if H_1 and H_2 are collision resistant then so is $H_2(H_1(\cdot)).$ Which of the following must be true: \bigcirc Either x,y are a collision for H_2 or $H_{1}\left(x
ight) ,H_{1}\left(y
ight)$ are a collision for H_{1} . \bigcirc Either $x,H_{1}\left(y
ight)$ are a collision for H_{2} or

Correct You would decrypt the final CBC MAC encryption step done using k_2 , the decrypt the last CBC MAC encryption step done using $k_{
m l}$, flip the last bit of the result, and re-apply the two encryptions. 6. Let H:M
ightarrow T be a collision resistant hash function. Which of the following is collision resistant: (as usual, we use | to denote string concatenation) $I'(m) = H(m) \bigoplus H(m \oplus 1^{|m|})$ (where $m\oplus 1^{|m|}$ is the complement of m) This should not be selected This construction is not collision resistant because H(000) = H(111). H'(m) = H(m||m)

of the keys. When Alice transmits a packet she appends 4 tags to it by computing the tag with each of her 4 keys. When user B_i receives a packet he accepts it as valid only if all tags corresponding to his keys in S_i are valid. For example, if user B_1 is given keys $\{k_1,k_2\}$ he will accept an incoming packet only if the first and second tags are valid. Note that B_1 cannot validate the 3rd and 4th tags How should Alice assign keys to the 6 users so that no single user can forge packets on behalf of Alice and fool some other user? $S_1 = \{k_1, k_2\}, S_2 = \{k_1, k_3, k_4\}, S_3 = \{k_1, k_4\}, S_4 = \{k_2, k_3\}, S_5 = \{k_2, k_3, k_4\}, S_6 = \{k_3, k_4\}$ $S_1 = \{k_1\}, S_2 = \{k_2, k_3\}, S_3 = \{k_3, k_4\}, S_4 = \{k_1, k_3\}, S_5 = \{k_1, k_2\}, S_6 = \{k_1, k_4\}$ $S_1 = \{k_1, k_2\}, S_2 = \{k_1, k_3\}, S_3 = \{k_1, k_4\}, S_4 = \{k_2, k_3, k_4\}, S_5 = \{k_2, k_3\}, S_6 = \{k_3, k_4\}$ $S_1 = \{k_2, k_3\}, S_2 = \{k_2, k_4\}, S_3 = \{k_3, k_4\}, S_4 = \{k_1, k_2\}, S_5 = \{k_1, k_3\}, S_6 = \{k_1, k_4\}$ Every user can only generate tags with the two keys he has. Since no set S_i is contained in another set S_j , no user ican fool a user j into accepting a message sent by i. 1/1 point 5. Consider the encrypted CBC MAC built from AES. Suppose we

1/1 point

0 / 1 point

1/1 point

0 / 1 point

0 / 1 point

1/1 point

0 / 1 point

Due Nov 18, 1:29 PM IST

GRADE 40%

0 / 1 point

0 / 1 point