Assignment-1

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PROBLEM

Question 2.17:
Three cards are drawn successively, without replacement from a pack of 52 well shuffled cards. What is the probability that first two cards are kings and the third card drawn is an ace?

SOLUTION

Let X_i where $i \in \{1, 2, 3\}$ be random variables which represent the outcome of the card drawn on the *ith* turn such that the random varaibles X_i take values $\{0, 1, 2\}$. Also, Let:

1) $X_i = 0$ represents King card is drawn
2) $X_i = 1$ represents Ace card is drawn
3) $X_i = 2$ represents neither King nor Ace cards are drawn

Using Conditional Probability we can write

$$\Pr(X_2 = 0|X_1 = 0) = \frac{\Pr(X_1 = 0, X_2 = 0)}{\Pr(X_1 = 0)} \quad (0.0.1)$$

If the events are independent of each other we can write

$$\Pr(X_2 = 0|X_1 = 0) = \Pr(X_2 = 0) \quad (0.0.2)$$

Therefore from (0.0.1) and (0.0.2)

$$\Pr(X_1 = 0, X_2 = 0) = \Pr(X_1 = 0) \times \Pr(X_2 = 0) \quad (0.0.3)$$

We need to find $\Pr(X_1 = 0, X_2 = 0, X_3 = 1)$. Using (0.0.3) we can write

$$\Pr(X_1 = 0, X_2 = 0, X_3 = 1) = \Pr(X_1 = 0) \times$$
$$\Pr(X_2 = 0) \times \Pr(X_3 = 1) \quad (0.0.4)$$

$$\implies \Pr(X_1 = 0, X_2 = 0, X_3 = 1) = \frac{4}{52} \times \frac{3}{51} \times \frac{4}{50}$$
$$= 0.000362$$
$$(0.0.5)$$

Therefore, the required Probability is 0.000362.