

Assignment-1

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Download all python codes from

<https://github.com/AdilSalfi/AI1103/tree/main/Assignment-1>

and latex-tikz codes from

<https://github.com/AdilSalfi/AI1103/tree/main/Assignment-1/Codes>

PROBLEM

Question 2.17:

Three cards are drawn successively, without replacement from a pack of 52 well shuffled cards. What is the probability that first two cards are kings and the third card drawn is an ace?

SOLUTION

Let X_i where $i \in \{1, 2, 3\}$ be random variables which represent the outcome of the card drawn on the i th turn such that the random variables X_i take values $\{0, 1, 2\}$

- 1) $X_i = 0$ represents King card is drawn
- 2) $X_i = 1$ represents Ace card is drawn
- 3) $X_i = 2$ represents neither King nor Ace cards are drawn

We need to find $\Pr(X_1 = 0, X_2 = 0, X_3 = 1)$

Using Conditional Probability and the fact that the Random Variables are independent of each other we can write

$$\begin{aligned}\Pr(X_1 = 0, X_2 = 0, X_3 = 1) &= \Pr(X_1 = 0) \times \\ &\Pr(X_2 = 0|X_1 = 0) \times \\ &\Pr(X_3 = 1|X_1 = 0, X_2 = 0) \quad (0.0.1)\end{aligned}$$

$$\begin{aligned}\Pr(X_1 = 0, X_2 = 0, X_3 = 1) &= \frac{4}{52} \times \frac{3}{51} \times \frac{4}{50} \quad (0.0.2) \\ &= 0.000362\end{aligned}$$

Therefore, the required Probability is 0.000362