

# Parsing

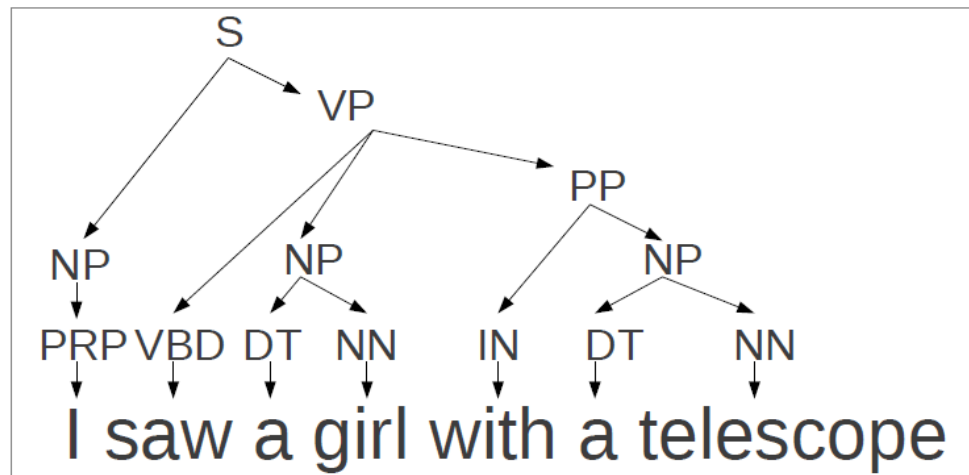
Natural Language Processing

Master in Business Analytics and Big Data

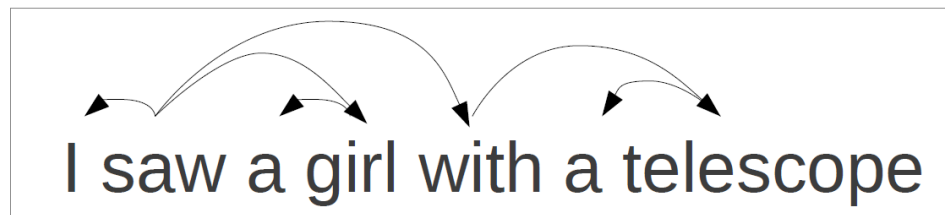
[acastellanos@faculty.ie.edu](mailto:acastellanos@faculty.ie.edu)

# Two Types of Parsing

- **Constituency:** Phrases and their recursive structure



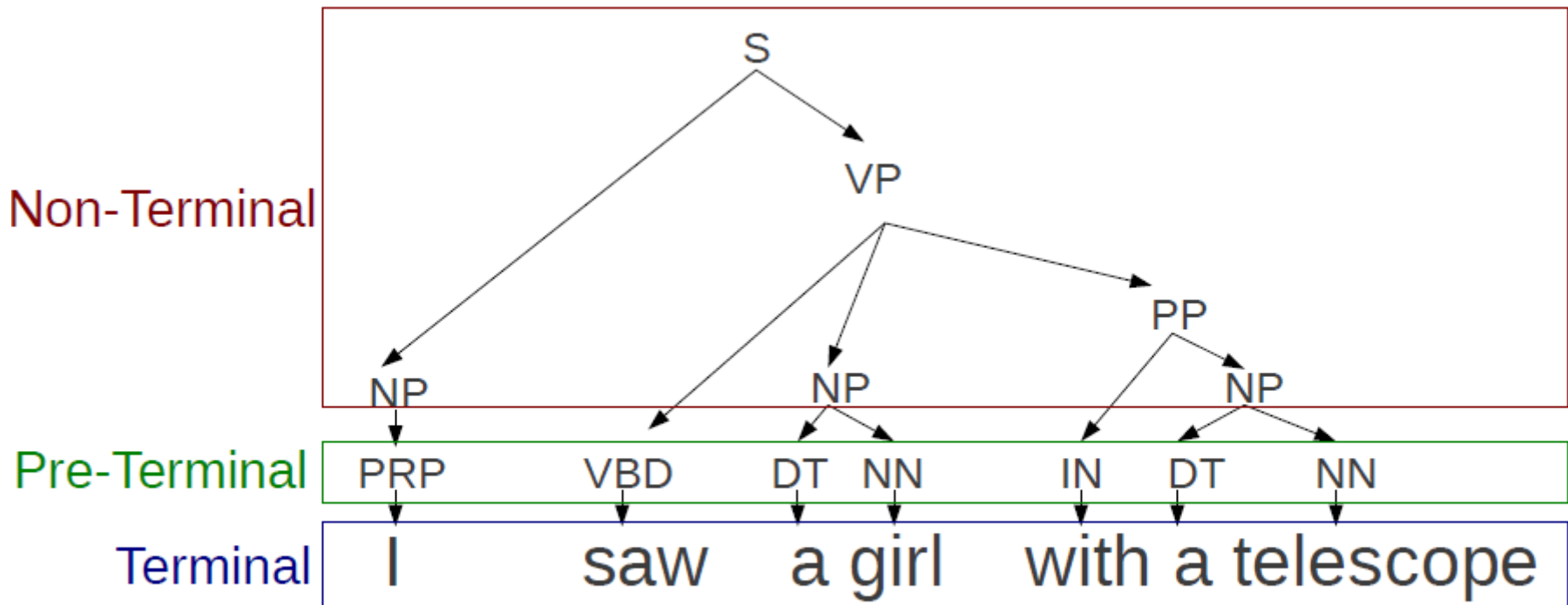
- **Dependency:** Relationships between words



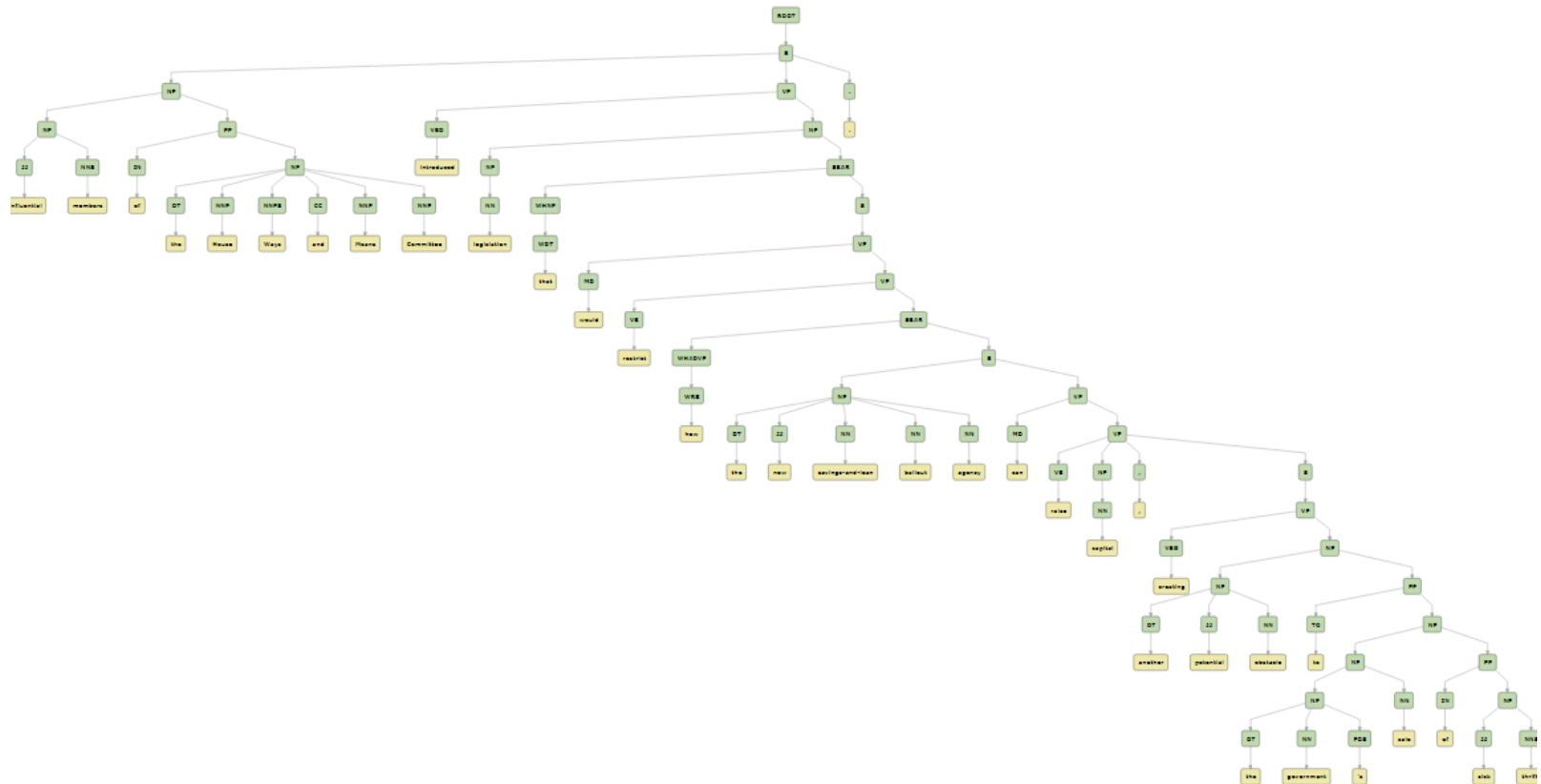
# Constituency Parsing

- Words → nested **constituents**.
- What is a **constituent**?
  - **Distribution**: unit that can appear in different places:
    - John talked [to the children] [about drugs].
    - John talked [about drugs] [to the children].
    - \*John talked drugs to the children about
  - **Substitution/expansion**:
    - I sat [on the box/right on top of the box/there].
  - **Coordination**, regular internal structure, no intrusion, fragments, semantics, ...

# Constituency Parsing

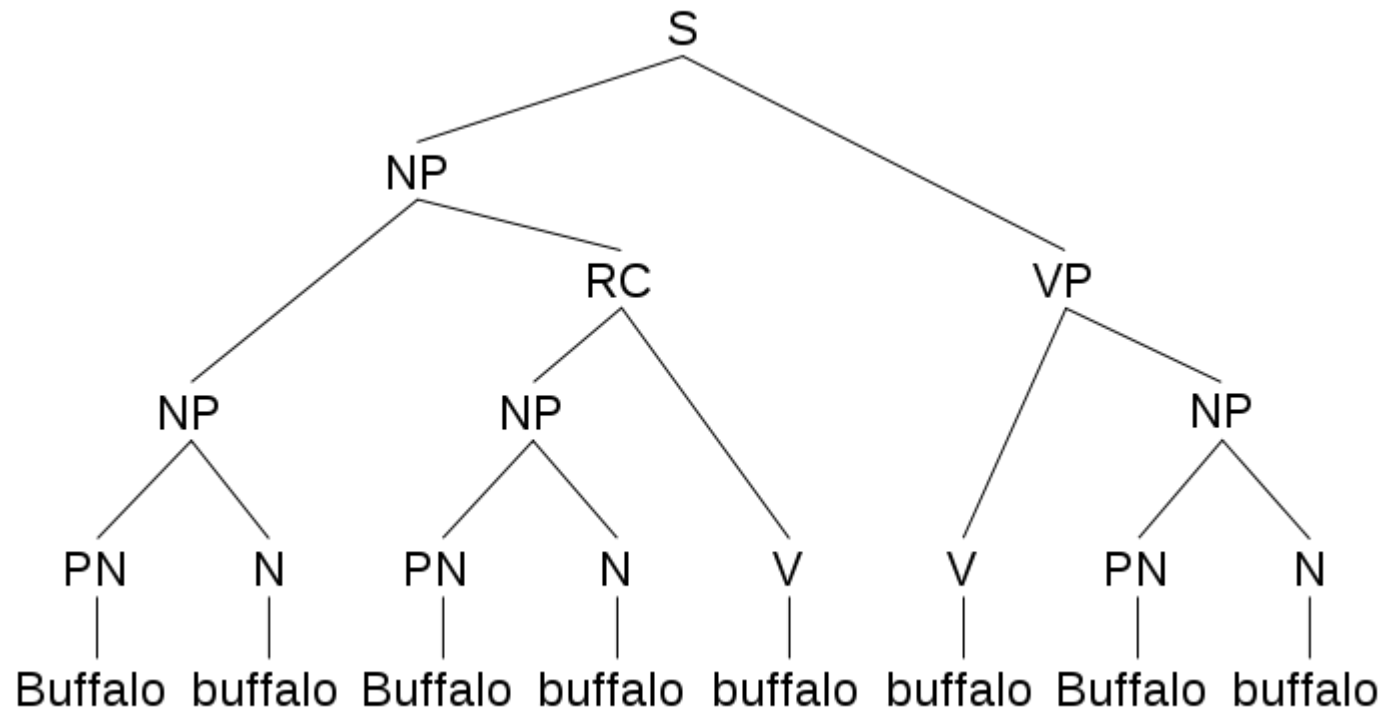


# Constituency Parsing



Influential members of the House Ways and Means Committee introduced legislation that would restrict how the new savings-and-loan bailout agency can raise capital, creating another potential obstacle to the government's sale of sick thrifts.

# Constituency Parsing



[https://en.wikipedia.org/wiki/Buffalo\\_buffalo\\_Buffalo\\_buffalo\\_buffalo\\_buffalo\\_Buffalo\\_buffalo](https://en.wikipedia.org/wiki/Buffalo_buffalo_Buffalo_buffalo_buffalo_buffalo_Buffalo_buffalo)

# Classical (“Pre 1990”) NLP Parsing

- Wrote symbolic grammar (CFG) and lexicon

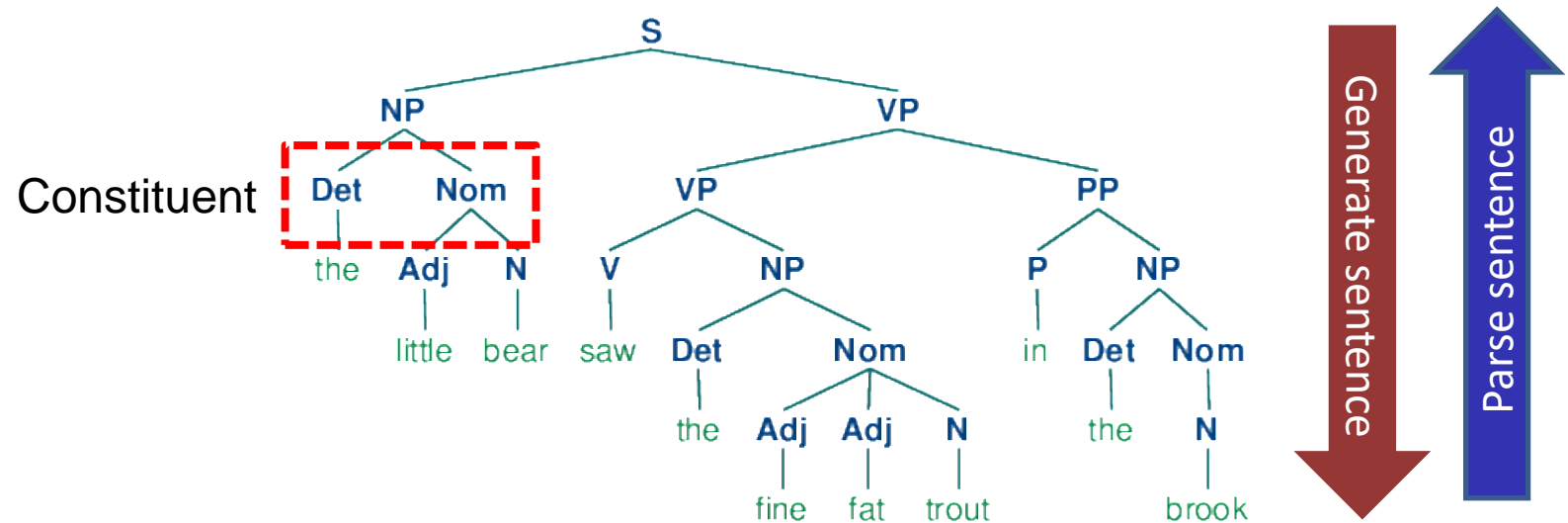
## Grammar (CFG)

$S \rightarrow NP VP$	$VP \rightarrow V NP$
$NP \rightarrow (DT) NN$	$VP \rightarrow VBP NP$
$NP \rightarrow NN NNS$	$VP \rightarrow VBP NP PP$
$NP \rightarrow NP PP$	$PP \rightarrow IN PP$

## Lexicon

$NN \rightarrow$	<i>interest</i>
$NNS \rightarrow$	<i>rates</i>
$NNS \rightarrow$	<i>raises</i>
$VBP \rightarrow$	<i>interest</i>
$VBZ \rightarrow$	<i>rates</i>

# Grammars





# Parsers

- **Build one or more constituent structure from a sentence**
  - Based on grammar productions
- **Top-down**
  - E.g. Recursive Descent Parsing
- **Bottom-up**
  - E.g. Shift-reduce parsing.

# Recursive Descent Parsing

## S -> NP VP

NP -> Det N PP

NP -> Det N

VP -> V NP PP

VP -> V NP

VP -> V

PP -> P NP

NP -> 'I'

Det -> 'the'

Det -> 'a'

N -> 'man'

N -> 'park'

N -> 'dog'

N -> 'telescope'

V -> 'ate'

V -> 'saw'

P -> 'in'

P -> 'under'

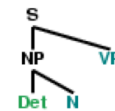
P -> 'with'

## 1. Initial stage

S

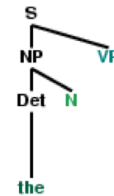
the dog saw a man in the park

## 2. Second production



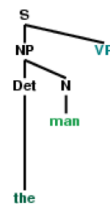
the dog saw a man in the park

## 3. Matching *the*



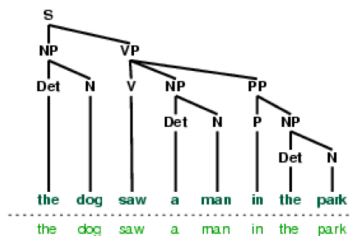
the dog saw a man in the park

## 4. Cannot match *man*

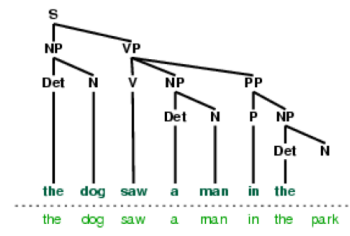


the dog saw a man in the park

## 5. Completed parse



## 6. Backtracking



<http://www.nltk.org/book/ch08.html>

# Shift-reduce parsing

## S -> NP VP

NP -> Det N PP  
NP -> Det N  
VP -> V NP PP  
VP -> V NP  
VP -> V  
PP -> P NP  
NP -> 'I'  
Det -> 'the'  
Det -> 'a'  
N -> 'man'  
N -> 'park'  
N -> 'dog'  
N -> 'telescope'  
V -> 'ate'  
V -> 'saw'  
P -> 'in'  
P -> 'under'  
P -> 'with'

### 1. Initial state

Stack	Remaining Text
	the dog saw a man in the park

### 3. After reduce shift reduce

Stack	Remaining Text
<div> <div>Det</div> <div>N</div> </div> <div>the dog</div>	saw a man in the park

### 5. After building a complex NP

Stack	Remaining Text
<div> <div>NP</div> <div>V</div> <div>NP</div> </div> <div> <div> <div>Det</div> <div>N</div> </div> <div> <div>Det</div> <div>N</div> </div> <div> <div>P</div> <div>NP</div> </div> </div> <div> <div>the dog</div> <div>saw</div> <div> <div>a man</div> <div>in the park</div> </div> </div>	

### 2. After one shift

Stack	Remaining Text
the	dog saw a man in the park

### 4. After recognizing the second NP

Stack	Remaining Text
<div> <div>NP</div> <div>V</div> <div>NP</div> </div> <div> <div> <div>Det</div> <div>N</div> </div> <div> <div>Det</div> <div>N</div> </div> </div> <div> <div>the dog</div> <div>saw</div> <div> <div>a man</div> </div> </div>	in the park

### 6. Built a complete parse tree

Stack	Remaining Text
<div> <div>S</div> </div> <div> <div> <div>NP</div> <div>VP</div> </div> </div> <div> <div> <div> <div>Det</div> <div>N</div> </div> <div> <div>V</div> <div>NP</div> </div> </div> <div> <div> <div> <div>NP</div> <div>PP</div> </div> </div> </div> </div> <div> <div> <div> <div>the dog</div> <div>saw</div> <div> <div> <div>a man</div> <div>in the park</div> </div> </div> </div> </div> </div>	

<http://www.nltk.org/book/ch08.html>

# Classical (“Pre 1990”) NLP Parsing

- Wrote symbolic grammar (CFG) and lexicon

## Grammar (CFG)

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## Lexicon

$NN \rightarrow \textit{interest}$   
 $NNS \rightarrow \textit{rates}$   
 $NNS \rightarrow \textit{raises}$   
 $VBP \rightarrow \textit{interest}$   
 $VBZ \rightarrow \textit{rates}$

- Deduct parses from words

*Fed raises interest rates 0.5 percent*

- |                                     |                    |
|-------------------------------------|--------------------|
| • Minimal grammar:                  | 36 parses          |
| • Simple 10 rule grammar:           | 592 parses         |
| • Real-size broad-coverage grammar: | millions of parses |

# Classical (“Pre 1990”) NLP Parsing

- Wrote symbolic grammar (CFG or often richer) and lexicon

$S \rightarrow NP VP$

$NP \rightarrow (DT) NN$

$NP \rightarrow NN NNS$

$NP \rightarrow NNP$

$VP \rightarrow V NP$

$NN \rightarrow interest$

$NNS \rightarrow rates$

$NNS \rightarrow raises$

$VBP \rightarrow interest$

$VBZ \rightarrow rates$

- Used deduction systems to prove parses from words

*Fed raises interest rates 0.5 percent*

- Minimal grammar:

36 parses

- Simple 10 rule grammar:

592 parses

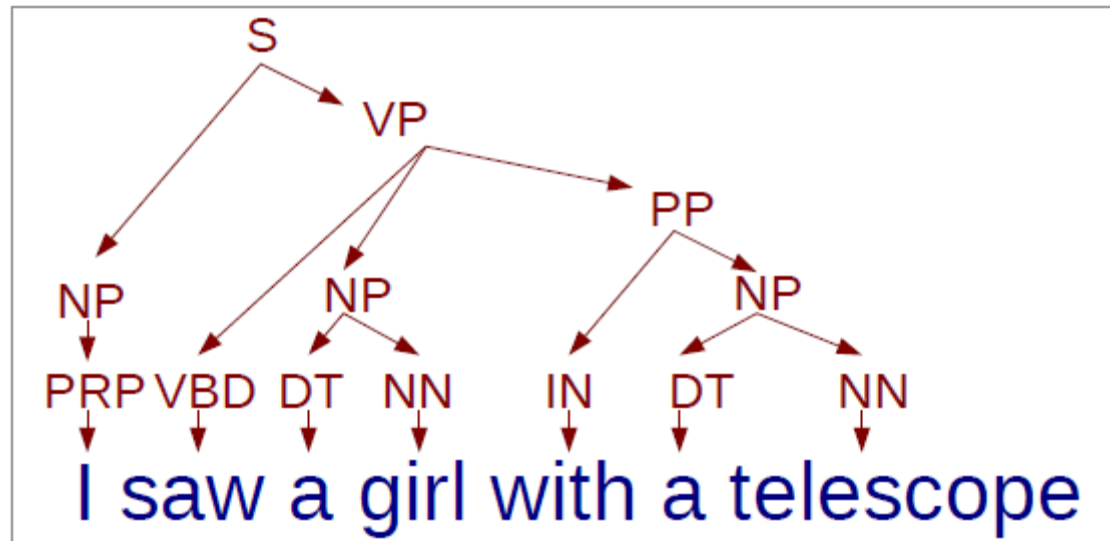
- Real-size broad-coverage grammar:

millions of parses

This scaled very badly and didn't give coverage.

# Probabilistic Parsing

- Given a sentence  $X$ , predict its most probable parse tree  $T$



$$\operatorname{argmax}_Y P(T|X)$$

# Probabilistic Generative Parsing

- We assume some **probabilistic model** generated the sentence  $X$  and the **parse tree**  $T$  jointly

$$P(T, X)$$

- The **parse tree** with highest **joint probability** given  $X$  also has the highest **conditional probability**.

$$\operatorname{argmax}_Y P(T|X) = \operatorname{argmax}_Y P(T, X)$$

# Probabilistic Generative Parsing

- **PCFG Learning**

$$P(A \rightarrow BC) = P(B, C|A) = \frac{\text{count}(A \rightarrow BC)}{\text{count}(A \rightarrow \setminus *)}$$

```
tbank_grammar = nltk.grammar.induce_pcfg(Nonterminal('S'), tbank_productions)
```

[https://www.nltk.org/modules/nltk/grammar.html#induce\\_pcfg](https://www.nltk.org/modules/nltk/grammar.html#induce_pcfg)

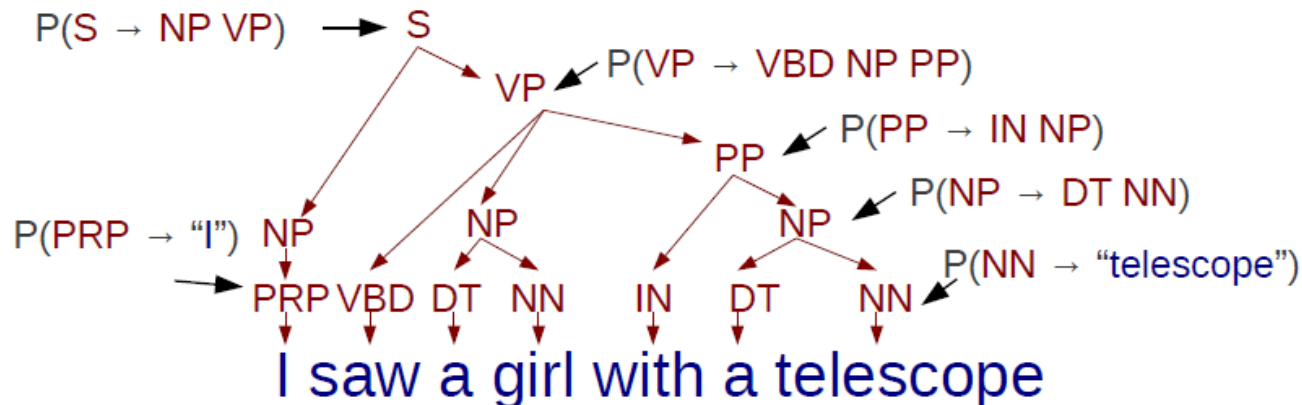


# Probabilistic Context Free Grammar

- A **context-free grammar** is a tuple  $\langle N, T, S, R \rangle$ 
  - $N$  : the set of non-terminals
    - Phrasal categories: S, NP, VP, ADJP, etc.
    - Parts-of-speech (pre-terminals): NN, JJ, DT, VB
  - $T$  : the set of terminals (the words)
  - $S$  : the start symbol
    - Often written as ROOT or TOP
  - $R$  : the set of rules
    - Of the form  $X \rightarrow Y_1 Y_2 \dots Y_k$ , with  $X, Y_i \in N$
    - Examples:  $S \rightarrow NP VP$ ,  $VP \rightarrow VP CC VP$
- A **PCFG** adds:
  - A top-down production probability per rule  $P(Y_1 Y_2 \dots Y_k \mid X)$

# Probabilistic Context Free Grammar

- **PCFG**: Define probability for each node



- **Parse tree** probability is product of node probabilities

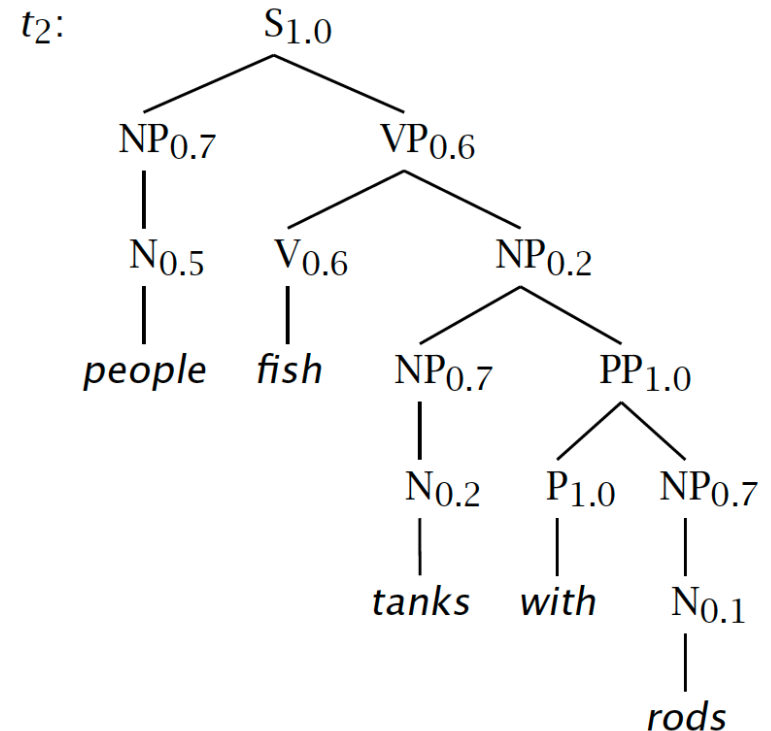
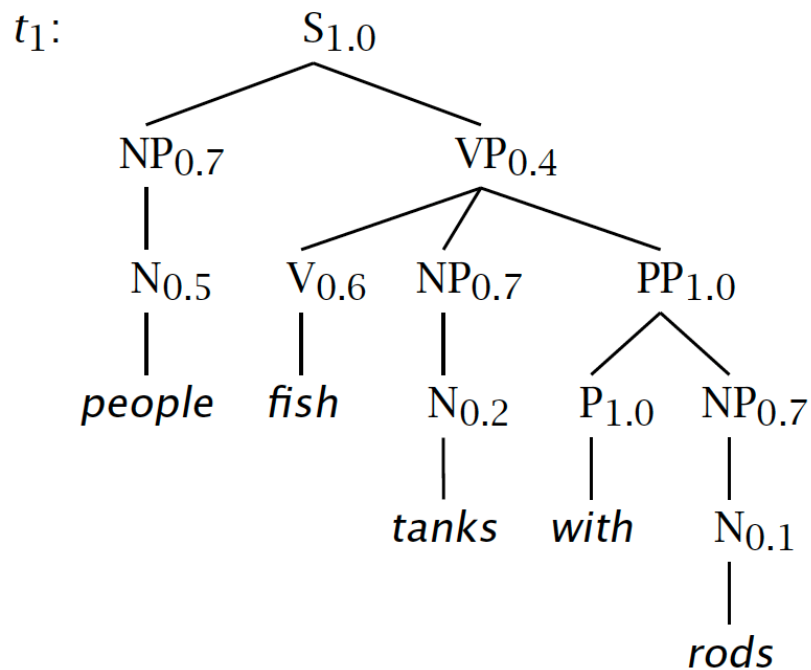
$$\begin{aligned}
 &P(S \rightarrow NP VP) * P(NP \rightarrow PRP) * P(PR \rightarrow "I") * P(VP \rightarrow VBD NP PP) * \\
 &P(VBD \rightarrow "saw") * P(NP \rightarrow DT NN) * P(DT \rightarrow "a") * P(NN \rightarrow "girl") * P(PP \rightarrow IN NP) * \\
 &P(IN \rightarrow "with") * P(NP \rightarrow DT NN) * P(DT \rightarrow "a") * P(NN \rightarrow "telescope")
 \end{aligned}$$

# PCFG Example

$S \rightarrow NP VP$	1.0	$N \rightarrow people$	0.5
$VP \rightarrow V NP$	0.6	$N \rightarrow fish$	0.2
$VP \rightarrow V NP PP$	0.4	$N \rightarrow tanks$	0.2
$NP \rightarrow NP NP$	0.1	$N \rightarrow rods$	0.1
$NP \rightarrow NP PP$	0.2	$V \rightarrow people$	0.1
$NP \rightarrow N$	0.7	$V \rightarrow fish$	0.6
$PP \rightarrow P NP$	1.0	$V \rightarrow tanks$	0.3
		$P \rightarrow with$	1.0

# PCFG Example

**S** = people fish tanks with rods



# PCFG Example

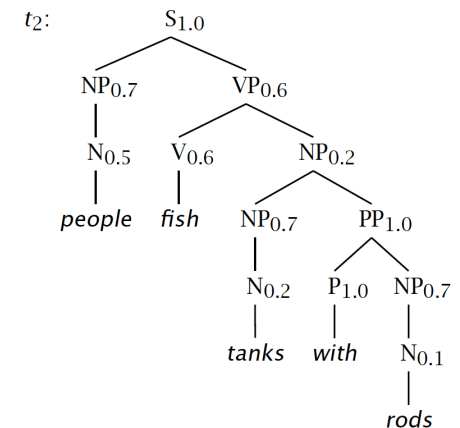
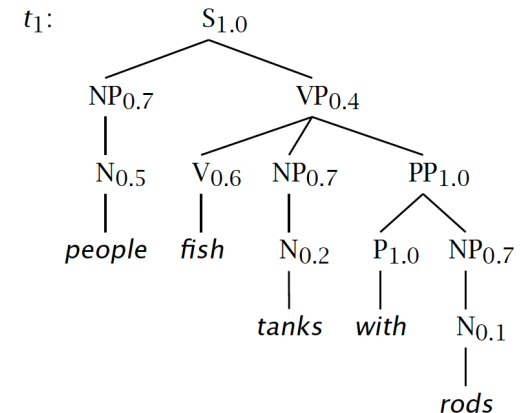
- $$P(t_1) = 1.0 \times 0.7 \times 0.4 \times 0.5 \times 0.6 \times 0.7 \times 1.0 \times 1.0 \times 0.2 \times 0.7 \times 0.1$$

$$= \mathbf{0.0008232}$$

- $$P(t_2) = 1.0 \times 0.7 \times 0.6 \times 0.5 \times 0.6 \times 0.2 \times 1.0 \times 0.2 \times 1.0 \times 0.7 \times 0.1$$

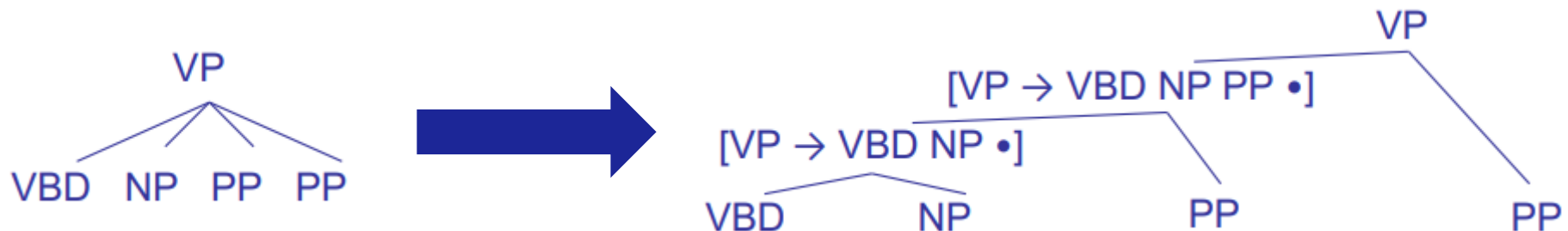
$$= \mathbf{0.00024696}$$

- PCFG would choose  $t_1$



# Chomsky Normal Form

- All rules are of the form  $X \rightarrow Y Z$  or  $X \rightarrow w$ 
  - $X, Y, Z \in N$  and  $w \in T$
  - Empties and unaries are removed recursively
  - n-ary rules  $\rightarrow$  new nonterminals ( $n > 2$ )
- Doesn't change the weak generative capacity of a CFG
  - That is, it recognizes the same language
- Makes parsing easier!



# Chomsky Normal Form

$S \rightarrow NP VP$

$VP \rightarrow V NP$

$VP \rightarrow V NP PP$

$NP \rightarrow NP NP$

$NP \rightarrow NP PP$

$NP \rightarrow N$

$NP \rightarrow e$

$PP \rightarrow P NP$

$N \rightarrow \textit{people}$

$N \rightarrow \textit{fish}$

$N \rightarrow \textit{tanks}$

$N \rightarrow \textit{rods}$

$V \rightarrow \textit{people}$

$V \rightarrow \textit{fish}$

$V \rightarrow \textit{tanks}$

$P \rightarrow \textit{with}$

# Chomsky Normal Form

## Step 1: Remove epsilon rules

$S \rightarrow NP VP$

$VP \rightarrow V NP$

$VP \rightarrow V NP PP$

$NP \rightarrow NP NP$

$NP \rightarrow NP PP$

$NP \rightarrow N$

**$NP \rightarrow e$**

$PP \rightarrow P NP$

Recognizing the  
same language?  
For every rule with  
NP, create a unary  
rule

$N \rightarrow people$

$N \rightarrow fish$

$N \rightarrow tanks$

$N \rightarrow rods$

$V \rightarrow people$

$V \rightarrow fish$

$V \rightarrow tanks$

$P \rightarrow with$



# Chomsky Normal Form

## Step 1: Remove epsilon rules

$S \rightarrow NP VP$

$S \rightarrow VP$

$VP \rightarrow V NP$

$VP \rightarrow V$

$VP \rightarrow V NP PP$

$VP \rightarrow V PP$

$NP \rightarrow NP NP$

$NP \rightarrow NP$

$NP \rightarrow NP PP$

$NP \rightarrow PP$

$NP \rightarrow N$

$PP \rightarrow P NP$

$PP \rightarrow P$

$N \rightarrow \textit{people}$

$N \rightarrow \textit{fish}$

$N \rightarrow \textit{tanks}$

$N \rightarrow \textit{rods}$

$V \rightarrow \textit{people}$

$V \rightarrow \textit{fish}$

$V \rightarrow \textit{tanks}$

$P \rightarrow \textit{with}$

# Chomsky Normal Form

## Step 2: Remove unary rules

$S \rightarrow NP VP$

$S \rightarrow VP$

$VP \rightarrow V NP$

$VP \rightarrow V$

$VP \rightarrow V NP PP$

$VP \rightarrow V PP$

$NP \rightarrow NP NP$

$NP \rightarrow NP$

$NP \rightarrow NP PP$

$NP \rightarrow PP$

$NP \rightarrow N$

$PP \rightarrow P NP$

$PP \rightarrow P$

Recognizing the  
same language?  
Work your way  
down to  
propagate

$N \rightarrow people$

$N \rightarrow fish$

$N \rightarrow tanks$

$N \rightarrow rods$

$V \rightarrow people$

$V \rightarrow fish$

$V \rightarrow tanks$

$P \rightarrow with$

# Chomsky Normal Form

## Step 2: Remove unary rules

S  $\rightarrow$  NP VP  
VP  $\rightarrow$  V NP  
S  $\rightarrow$  V NP  
VP  $\rightarrow$  V  
**S  $\rightarrow$  V**  
VP  $\rightarrow$  V NP PP  
S  $\rightarrow$  V NP PP  
VP  $\rightarrow$  V PP  
S  $\rightarrow$  V PP  
NP  $\rightarrow$  NP NP  
NP  $\rightarrow$  NP  
NP  $\rightarrow$  NP PP  
NP  $\rightarrow$  PP  
NP  $\rightarrow$  N  
PP  $\rightarrow$  P NP  
PP  $\rightarrow$  P

Just added a  
unary rule!  
Need to apply  
until they are all  
gone

N  $\rightarrow$  *people*  
N  $\rightarrow$  *fish*  
N  $\rightarrow$  *tanks*  
N  $\rightarrow$  *rods*  
V  $\rightarrow$  *people*  
V  $\rightarrow$  *fish*  
V  $\rightarrow$  *tanks*  
P  $\rightarrow$  *with*

# Chomsky Normal Form

## Step 2: Remove unary rules

S → NP VP  
VP → V NP  
S → V NP  
VP → V  
**S → V**  
VP → V NP PP  
S → V NP PP  
VP → V PP  
S → V PP  
NP → NP NP  
NP → NP  
NP → NP PP  
NP → PP  
NP → N  
PP → P NP  
PP → P

Just added a  
unary rule!  
Need to apply  
until they are all  
gone

N → *people*  
N → *fish*  
N → *tanks*  
N → *rods*  
V → *people*  
V → *fish*  
V → *tanks*  
P → *with*

# Chomsky Normal Form

## Step 2: Remove unary rules

S → NP VP  
VP → V NP  
S → V NP  
VP → V  
~~S → V~~  
VP → V NP PP  
S → V NP PP  
VP → V PP  
S → V PP  
NP → NP NP  
NP → NP  
NP → NP PP  
NP → PP  
NP → N  
PP → P NP  
PP → P

Just added a  
unary rule!  
Need to apply  
until they are all  
gone

N → *people*  
N → *fish*  
N → *tanks*  
N → *rods*  
V → *people*  
V → *fish*  
V → *tanks*  
P → *with*

# Chomsky Normal Form

## Step 2: Remove unary rules

$S \rightarrow NP VP$

$VP \rightarrow V NP$

$S \rightarrow V NP$

~~$VP \rightarrow V$~~

$VP \rightarrow V NP PP$

$S \rightarrow V NP PP$

$VP \rightarrow V PP$

$S \rightarrow V PP$

$NP \rightarrow NP NP$

$NP \rightarrow NP$

$NP \rightarrow NP PP$

$NP \rightarrow PP$

$NP \rightarrow N$

$PP \rightarrow P NP$

$PP \rightarrow P$

$N \rightarrow \textit{people}$

$N \rightarrow \textit{fish}$

$N \rightarrow \textit{tanks}$

$N \rightarrow \textit{rods}$

$V \rightarrow \textit{people}$

$V \rightarrow \textit{fish}$

$V \rightarrow \textit{tanks}$

$P \rightarrow \textit{with}$

# Chomsky Normal Form

## Step 2: Remove unary rules

$S \rightarrow NP VP$   
 $VP \rightarrow V NP$   
 $S \rightarrow V NP$   
 $VP \rightarrow V NP PP$   
 $S \rightarrow V NP PP$   
 $VP \rightarrow V PP$   
 $S \rightarrow V PP$   
 $NP \rightarrow NP NP$   
 ~~$NP \rightarrow NP$~~   
 $NP \rightarrow NP PP$   
 $NP \rightarrow PP$   
 ~~$NP \rightarrow N$~~   
 $PP \rightarrow P NP$   
 $PP \rightarrow P$

Recognizing the  
same language?  
Yes!

Only place N  
appears  
So can get rid of  
it altogether

$N \rightarrow people$   
 $N \rightarrow fish$   
 $N \rightarrow tanks$   
 $N \rightarrow rods$   
 $V \rightarrow people$   
 $V \rightarrow fish$   
 $V \rightarrow tanks$   
 $P \rightarrow with$

# Chomsky Normal Form

## Step 2: Remove unary rules

$S \rightarrow NP VP$   
 $VP \rightarrow V NP$   
 $S \rightarrow V NP$   
 $VP \rightarrow V NP PP$   
 $S \rightarrow V NP PP$   
 $VP \rightarrow V PP$   
 $S \rightarrow V PP$   
 $NP \rightarrow NP NP$   
 $NP \rightarrow NP PP$   
 ~~$NP \rightarrow PP$~~   
 $PP \rightarrow P NP$   
 ~~$PP \rightarrow P$~~

$NP \rightarrow people$   
 $NP \rightarrow fish$   
 $NP \rightarrow tanks$   
 $NP \rightarrow rods$   
 $V \rightarrow people$   
 $S \rightarrow people$   
 $VP \rightarrow people$   
 $V \rightarrow fish$   
 $S \rightarrow fish$   
 $VP \rightarrow fish$   
 $V \rightarrow tanks$   
 $S \rightarrow tanks$   
 $VP \rightarrow tanks$   
 $P \rightarrow with$   
 $PP \rightarrow with$



# Chomsky Normal Form

## Step 3: Binarize

$S \rightarrow NP VP$

$VP \rightarrow V NP$

$S \rightarrow V NP$

**$VP \rightarrow V NP PP$**

**$S \rightarrow V NP PP$**

$VP \rightarrow V PP$

$S \rightarrow V PP$

$NP \rightarrow NP NP$

$NP \rightarrow NP PP$

$PP \rightarrow P NP$

$NP \rightarrow people$

$NP \rightarrow fish$

$NP \rightarrow tanks$

$NP \rightarrow rods$

$V \rightarrow people$

$S \rightarrow people$

$VP \rightarrow people$

$V \rightarrow fish$

$S \rightarrow fish$

$VP \rightarrow fish$

$V \rightarrow tanks$

$S \rightarrow tanks$

$VP \rightarrow tanks$

$P \rightarrow with$

$PP \rightarrow with$

# Chomsky Normal Form

## Step 3: Binarize

$S \rightarrow NP VP$

$VP \rightarrow V NP$

$S \rightarrow V NP$

$VP \rightarrow V @VP\_V$

$@VP\_V \rightarrow NP PP$

$S \rightarrow V @S\_V$

$@S\_V \rightarrow NP PP$

$VP \rightarrow V PP$

$S \rightarrow V PP$

$NP \rightarrow NP NP$

$NP \rightarrow NP PP$

$PP \rightarrow P NP$

$NP \rightarrow people$

$NP \rightarrow fish$

$NP \rightarrow tanks$

$NP \rightarrow rods$

$V \rightarrow people$

$S \rightarrow people$

$VP \rightarrow people$

$V \rightarrow fish$

$S \rightarrow fish$

$VP \rightarrow fish$

$V \rightarrow tanks$

$S \rightarrow tanks$

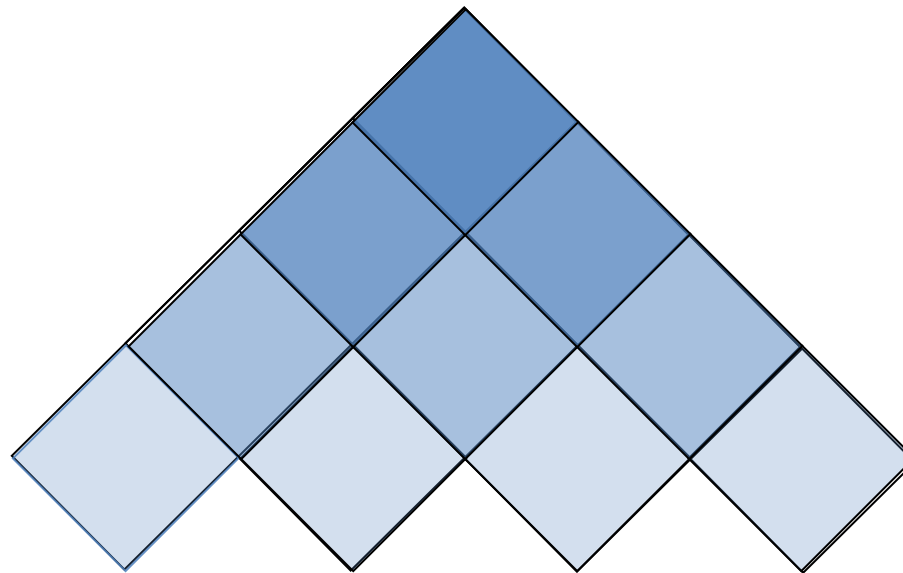
$VP \rightarrow tanks$

$P \rightarrow with$

$PP \rightarrow with$

# CKY Algorithm

- Cocke-Kasami-Younger



fish people fish tanks

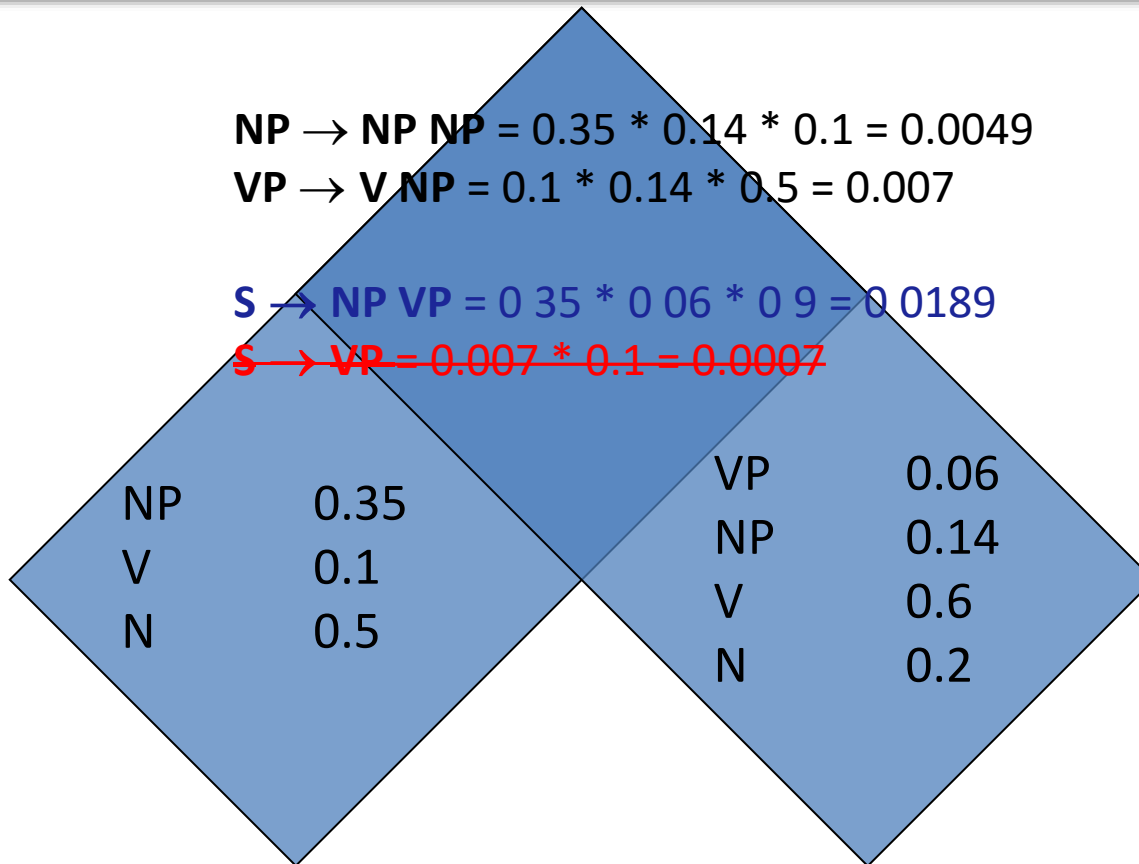
# CKY Algorithm

$$\text{NP} \rightarrow \text{NP NP} = 0.35 * 0.14 * 0.1 = 0.0049$$

$$\text{VP} \rightarrow \text{V NP} = 0.1 * 0.14 * 0.5 = 0.007$$

$$\text{S} \rightarrow \text{NP VP} = 0.35 * 0.06 * 0.9 = 0.0189$$

~~$$\text{S} \rightarrow \text{VP} = 0.007 * 0.1 = 0.0007$$~~



people

fish

## PCFG

$\text{S} \rightarrow \text{NP VP}$	0.9
$\text{S} \rightarrow \text{VP}$	0.1
$\text{VP} \rightarrow \text{V NP}$	0.5
$\text{VP} \rightarrow \text{V}$	0.1
$\text{VP} \rightarrow \text{V @VP\_V}$	0.3
$\text{VP} \rightarrow \text{V PP}$	0.1
$\text{@VP\_V} \rightarrow \text{NP PP}$	1.0
$\text{NP} \rightarrow \text{NP NP}$	0.1
$\text{NP} \rightarrow \text{NP PP}$	0.2
$\text{NP} \rightarrow \text{N}$	0.7
$\text{PP} \rightarrow \text{P NP}$	1.0

# CKY Parsing: A Worked Example

$S \rightarrow NP VP$	0.9
$S \rightarrow VP$	0.1
$VP \rightarrow V NP$	0.5
$VP \rightarrow V$	0.1
$VP \rightarrow V @VP\_V$	0.3
$VP \rightarrow V PP$	0.1
$@VP\_V \rightarrow NP PP$	1.0
$NP \rightarrow NP NP$	0.1
$NP \rightarrow NP PP$	0.2
$NP \rightarrow N$	0.7
$PP \rightarrow P NP$	1.0

$N \rightarrow people$	0.5
$N \rightarrow fish$	0.2
$N \rightarrow tanks$	0.2
$N \rightarrow rods$	0.1
$V \rightarrow people$	0.1
$V \rightarrow fish$	0.6
$V \rightarrow tanks$	0.3
$P \rightarrow with$	1.0

# CKY Parsing: A Worked Example

	0	fish	1	people	2	fish	3	tanks	4
0									
1	score[0][1]		score[0][2]		score[0][3]		score[0][4]		
2			score[1][2]		score[1][3]		score[1][4]		
3					score[2][3]		score[2][4]		
4							score[3][4]		

# CKY Parsing: A Worked Example

$S \rightarrow NP VP$	0.9
$S \rightarrow VP$	0.1
$VP \rightarrow V NP$	0.5
$VP \rightarrow V$	0.1
$VP \rightarrow V @VP\_V$	0.3
$VP \rightarrow V PP$	0.1
$@VP\_V \rightarrow NP PP$	1.0
$NP \rightarrow NP NP$	0.1
$NP \rightarrow NP PP$	0.2
$NP \rightarrow N$	0.7
$PP \rightarrow P NP$	1.0
$N \rightarrow \textit{people}$	0.5
$N \rightarrow \textit{fish}$	0.2
$N \rightarrow \textit{tanks}$	0.2
$N \rightarrow \textit{rods}$	0.1
$V \rightarrow \textit{people}$	0.1
$V \rightarrow \textit{fish}$	0.6
$V \rightarrow \textit{tanks}$	0.3
$P \rightarrow \textit{with}$	1.0

	0	fish	1	people	2	fish	3	tanks	4
0									
1									
2									
3									
4									

# CKY Parsing: A Worked Example

$S \rightarrow NP VP$	0.9
$S \rightarrow VP$	0.1
$VP \rightarrow V NP$	0.5
$VP \rightarrow V$	0.1
$VP \rightarrow V @VP\_V$	0.3
$VP \rightarrow V PP$	0.1
$@VP\_V \rightarrow NP PP$	1.0
$NP \rightarrow NP NP$	0.1
$NP \rightarrow NP PP$	0.2
$NP \rightarrow N$	0.7
$PP \rightarrow P NP$	1.0
$N \rightarrow people$	0.5
$N \rightarrow fish$	0.2
$N \rightarrow tanks$	0.2
$N \rightarrow rods$	0.1
$V \rightarrow people$	0.1
$V \rightarrow fish$	0.6
$V \rightarrow tanks$	0.3
$P \rightarrow with$	1.0

	0	fish	1	people	2	fish	3	tanks	4
0	$N \rightarrow fish\ 0.2$ $V \rightarrow fish\ 0.6$								
1				$N \rightarrow people\ 0.5$ $V \rightarrow people\ 0.1$					
2						$N \rightarrow fish\ 0.2$ $V \rightarrow fish\ 0.6$			
3								$N \rightarrow tanks\ 0.2$ $V \rightarrow tanks\ 0.1$	

```

for i=0; i<#(words); i++
  for A in nonterms
    if A -> words[i] in grammar
      score[i][i+1][A] = P(A -> words[i]);
    
```



# CKY Parsing: A Worked Example

$S \rightarrow NP VP$	0.9
$S \rightarrow VP$	0.1
$VP \rightarrow V NP$	0.5
$VP \rightarrow V$	0.1
$VP \rightarrow V @VP\_V$	0.3
$VP \rightarrow V PP$	0.1
$@VP\_V \rightarrow NP PP$	1.0
$NP \rightarrow NP NP$	0.1
$NP \rightarrow NP PP$	0.2
$NP \rightarrow N$	0.7
$PP \rightarrow P NP$	1.0

$N \rightarrow \textit{people}$	0.5
$N \rightarrow \textit{fish}$	0.2
$N \rightarrow \textit{tanks}$	0.2
$N \rightarrow \textit{rods}$	0.1
$V \rightarrow \textit{people}$	0.1
$V \rightarrow \textit{fish}$	0.6
$V \rightarrow \textit{tanks}$	0.3
$P \rightarrow \textit{with}$	1.0

```
// handle unaries
boolean added = true
while added
    added = false
    for A, B in nonterms
        if score[i][i+1][B] > 0 && A->B in grammar
            prob = P(A->B)*score[i][i+1][B]
            if(prob > score[i][i+1][A])
                score[i][i+1][A] = prob
                back[i][i+1][A] = B
            added = true
```

	fish	1	people	2	fish	3	tanks	4
0	$N \rightarrow \text{fish } 0.2$ $V \rightarrow \text{fish } 0.6$ <b><math>NP \rightarrow N 0.14</math></b> <b><math>VP \rightarrow V 0.06</math></b> <b><math>S \rightarrow VP 0.006</math></b>							
1		$N \rightarrow \text{people } 0.5$ $V \rightarrow \text{people } 0.1$ <b><math>NP \rightarrow N 0.35</math></b> <b><math>VP \rightarrow V 0.01</math></b> <b><math>S \rightarrow VP 0.001</math></b>						
2				$N \rightarrow \text{fish } 0.2$ $V \rightarrow \text{fish } 0.6$ <b><math>NP \rightarrow N 0.14</math></b> <b><math>VP \rightarrow V 0.06</math></b> <b><math>S \rightarrow VP 0.006</math></b>				
							$N \rightarrow \text{tanks } 0.2$ $V \rightarrow \text{tanks } 0.1$ <b><math>NP \rightarrow N 0.14</math></b> <b><math>VP \rightarrow V 0.03</math></b> <b><math>S \rightarrow VP 0.003</math></b>	

```
s
true

e
nonterms
[i+1][B] > 0 && A->B in grammar
(A->B)*score[i][i+1][B]
> score[i][i+1][A])
i][i+1][A] = prob
[i+1][A] = B
= true
```

# CKY Parsing: A Worked Example

$S \rightarrow NP VP$	0.9
$S \rightarrow VP$	0.1
$VP \rightarrow V NP$	0.5
$VP \rightarrow V$	0.1
$VP \rightarrow V @VP\_V$	0.3
$VP \rightarrow V PP$	0.1
$@VP\_V \rightarrow NP PP$	1.0
$NP \rightarrow NP NP$	0.1
$NP \rightarrow NP PP$	0.2
$NP \rightarrow N$	0.7
$PP \rightarrow P NP$	1.0
$N \rightarrow people$	0.5
$N \rightarrow fish$	0.2
$N \rightarrow tanks$	0.2
$N \rightarrow rods$	0.1
$V \rightarrow people$	0.1
$V \rightarrow fish$	0.6
$V \rightarrow tanks$	0.3
$P \rightarrow with$	1.0

	0	1	2	3	4
fish	$N \rightarrow fish\ 0.2$ $V \rightarrow fish\ 0.6$ $NP \rightarrow N\ 0.14$ $VP \rightarrow V\ 0.06$ $S \rightarrow VP\ 0.006$	$NP \rightarrow NP\ NP\ 0.0049$ $VP \rightarrow V\ NP\ 0.105$ $S \rightarrow NP\ VP\ 0.00126$			
people		$N \rightarrow people\ 0.5$ $V \rightarrow people\ 0.1$ $NP \rightarrow N\ 0.35$ $VP \rightarrow V\ 0.01$ $S \rightarrow VP\ 0.001$	$NP \rightarrow NP\ NP\ 0.0049$ $VP \rightarrow V\ NP\ 0.007$ $S \rightarrow NP\ VP\ 0.0189$		
fish			$N \rightarrow fish\ 0.2$ $V \rightarrow fish\ 0.6$ $NP \rightarrow N\ 0.14$ $VP \rightarrow V\ 0.06$ $S \rightarrow VP\ 0.006$	$NP \rightarrow NP\ NP\ 0.00196$ $VP \rightarrow V\ NP\ 0.042$ $S \rightarrow NP\ VP\ 0.00378$	
tanks				$N \rightarrow tanks\ 0.2$ $V \rightarrow tanks\ 0.1$ $NP \rightarrow N\ 0.14$ $VP \rightarrow V\ 0.03$ $S \rightarrow VP\ 0.003$	

```

prob=score[begin][split][B]*score[split][end][C]*P(A->BC)
if (prob > score[begin][end][A])
    score[begin][end][A] = prob
    back[begin][end][A] = new Triple(split,B,C)

```

# CKY Parsing: A Worked Example

$S \rightarrow NP VP$	0.9
$S \rightarrow VP$	0.1
$VP \rightarrow V NP$	0.5
$VP \rightarrow V$	0.1
$VP \rightarrow V @VP\_V$	0.3
$VP \rightarrow V PP$	0.1
$@VP\_V \rightarrow NP PP$	1.0
$NP \rightarrow NP NP$	0.1
$NP \rightarrow NP PP$	0.2
$NP \rightarrow N$	0.7
$PP \rightarrow P NP$	1.0
$N \rightarrow people$	0.5
$N \rightarrow fish$	0.2
$N \rightarrow tanks$	0.2
$N \rightarrow rods$	0.1
$V \rightarrow people$	0.1
$V \rightarrow fish$	0.6
$V \rightarrow tanks$	0.3
$P \rightarrow with$	1.0

	fish	people	fish	tanks
0	N → fish 0.2 V → fish 0.6 NP → N 0.14 VP → V 0.06 S → VP 0.006	NP → NPNP 0.0049 VP → VNP <b>0.105</b> S → VP 0.0105		
1		N → people 0.5 V → people 0.1 NP → N 0.35 VP → V 0.01 S → VP 0.001	NP → NPNP 0.0049 VP → V NP 0.007 S → NP VP 0.0189	
2			N → fish 0.2 V → fish 0.6 NP → N 0.14 VP → V 0.06 S → VP 0.006	NP → NPNP 0.00196 VP → V NP <b>0.042</b> S → VP 0.0042
3				N → tanks 0.2 V → tanks 0.1 NP → N 0.14 VP → V 0.03 S → VP 0.003

```
varies
ded = true
d
false
in nonterms
P(A->B)*score[begin][end][B];
b > score[begin][end][A]
e[begin][end][A] = prob
[begin][end][A] = B
d = true
```

```
//handle unaries
boolean added = true
while added
    added = false
    for A, B in nonterms
        prob = P(A->B)*score[begin][end][B];
        if prob > score[begin][end][A]
            score[begin][end][A] = prob
            back[begin][end][A] = B
            added = true
```

# CKY Parsing: A Worked Example

$S \rightarrow NP VP$	0.9
$S \rightarrow VP$	0.1
$VP \rightarrow V NP$	0.5
$VP \rightarrow V$	0.1
$VP \rightarrow V @VP\_V$	0.3
$VP \rightarrow V PP$	0.1
$@VP\_V \rightarrow NP PP$	1.0
$NP \rightarrow NP NP$	0.1
$NP \rightarrow NP PP$	0.2
$NP \rightarrow N$	0.7
$PP \rightarrow P NP$	1.0
$N \rightarrow people$	0.5
$N \rightarrow fish$	0.2
$N \rightarrow tanks$	0.2
$N \rightarrow rods$	0.1
$V \rightarrow people$	0.1
$V \rightarrow fish$	0.6
$V \rightarrow tanks$	0.3
$P \rightarrow with$	1.0

	0	1	2	3	4
	fish	people	fish	tanks	
0	$N \rightarrow fish\ 0.2$ $V \rightarrow fish\ 0.6$ $NP \rightarrow N\ 0.14$ $VP \rightarrow V\ 0.06$ $S \rightarrow VP\ 0.006$	$NP \rightarrow NP\ 0.0049$ $VP \rightarrow V\ NP\ 0.105$ $S \rightarrow VP\ 0.0105$	$NP \rightarrow NP\ NP\ 0.0000686$ $VP \rightarrow V\ NP\ 0.00147$ $S \rightarrow NP\ VP\ 0.000882$		
1		$N \rightarrow people\ 0.5$ $V \rightarrow people\ 0.1$ $NP \rightarrow N\ 0.35$ $VP \rightarrow V\ 0.01$ $S \rightarrow VP\ 0.001$	$NP \rightarrow NP\ NP\ 0.0049$ $VP \rightarrow V\ NP\ 0.007$ $S \rightarrow NP\ VP\ 0.0189$		
2			$N \rightarrow fish\ 0.2$ $V \rightarrow fish\ 0.6$ $NP \rightarrow N\ 0.14$ $VP \rightarrow V\ 0.06$ $S \rightarrow VP\ 0.006$	$NP \rightarrow NP\ NP\ 0.00196$ $VP \rightarrow V\ NP\ 0.042$ $S \rightarrow VP\ 0.0042$	
3				$N \rightarrow tanks\ 0.2$ $V \rightarrow tanks\ 0.1$ $NP \rightarrow N\ 0.14$ $VP \rightarrow V\ 0.03$ $S \rightarrow VP\ 0.003$	

```

for split = begin+1 to end-1
  for A,B,C in nonterms
    prob=score[begin][split][B]*score[split][end][C]*P(A->BC)
    if prob > score[begin][end][A]
      score[begin][end][A] = prob
      back[begin][end][A] = new Triple(split,B,C)

```

# CKY Parsing: A Worked Example

$S \rightarrow NP VP$	0.9
$S \rightarrow VP$	0.1
$VP \rightarrow V NP$	0.5
$VP \rightarrow V$	0.1
$VP \rightarrow V @VP\_V$	0.3
$VP \rightarrow V PP$	0.1
$@VP\_V \rightarrow NP PP$	1.0
$NP \rightarrow NP NP$	0.1
$NP \rightarrow NP PP$	0.2
$NP \rightarrow N$	0.7
$PP \rightarrow P NP$	1.0
$N \rightarrow people$	0.5
$N \rightarrow fish$	0.2
$N \rightarrow tanks$	0.2
$N \rightarrow rods$	0.1
$V \rightarrow people$	0.1
$V \rightarrow fish$	0.6
$V \rightarrow tanks$	0.3
$P \rightarrow with$	1.0

	0	1	2	3	4
	fish	people	fish	tanks	
0	$N \rightarrow fish\ 0.2$ $V \rightarrow fish\ 0.6$ $NP \rightarrow N\ 0.14$ $VP \rightarrow V\ 0.06$ $S \rightarrow VP\ 0.006$	$NP \rightarrow NP\ NP\ 0.0049$ $VP \rightarrow V\ NP\ 0.105$ $S \rightarrow VP\ 0.0105$	$NP \rightarrow NP\ NP\ 0.0000686$ $VP \rightarrow V\ NP\ 0.00147$ $S \rightarrow NP\ VP\ 0.000882$		
1		$N \rightarrow people\ 0.5$ $V \rightarrow people\ 0.1$ $NP \rightarrow N\ 0.35$ $VP \rightarrow V\ 0.01$ $S \rightarrow VP\ 0.001$	$NP \rightarrow NP\ NP\ 0.0049$ $VP \rightarrow V\ NP\ 0.007$ $S \rightarrow NP\ VP\ 0.0189$	$NP \rightarrow NP\ NP\ 0.0000686$ $VP \rightarrow V\ NP\ 0.000098$ $S \rightarrow NP\ VP\ 0.01323$	
2			$N \rightarrow fish\ 0.2$ $V \rightarrow fish\ 0.6$ $NP \rightarrow N\ 0.14$ $VP \rightarrow V\ 0.06$ $S \rightarrow VP\ 0.006$	$NP \rightarrow NP\ NP\ 0.00196$ $VP \rightarrow V\ NP\ 0.042$ $S \rightarrow VP\ 0.0042$	
3				$N \rightarrow tanks\ 0.2$ $V \rightarrow tanks\ 0.1$ $NP \rightarrow N\ 0.14$ $VP \rightarrow V\ 0.03$ $S \rightarrow VP\ 0.003$	

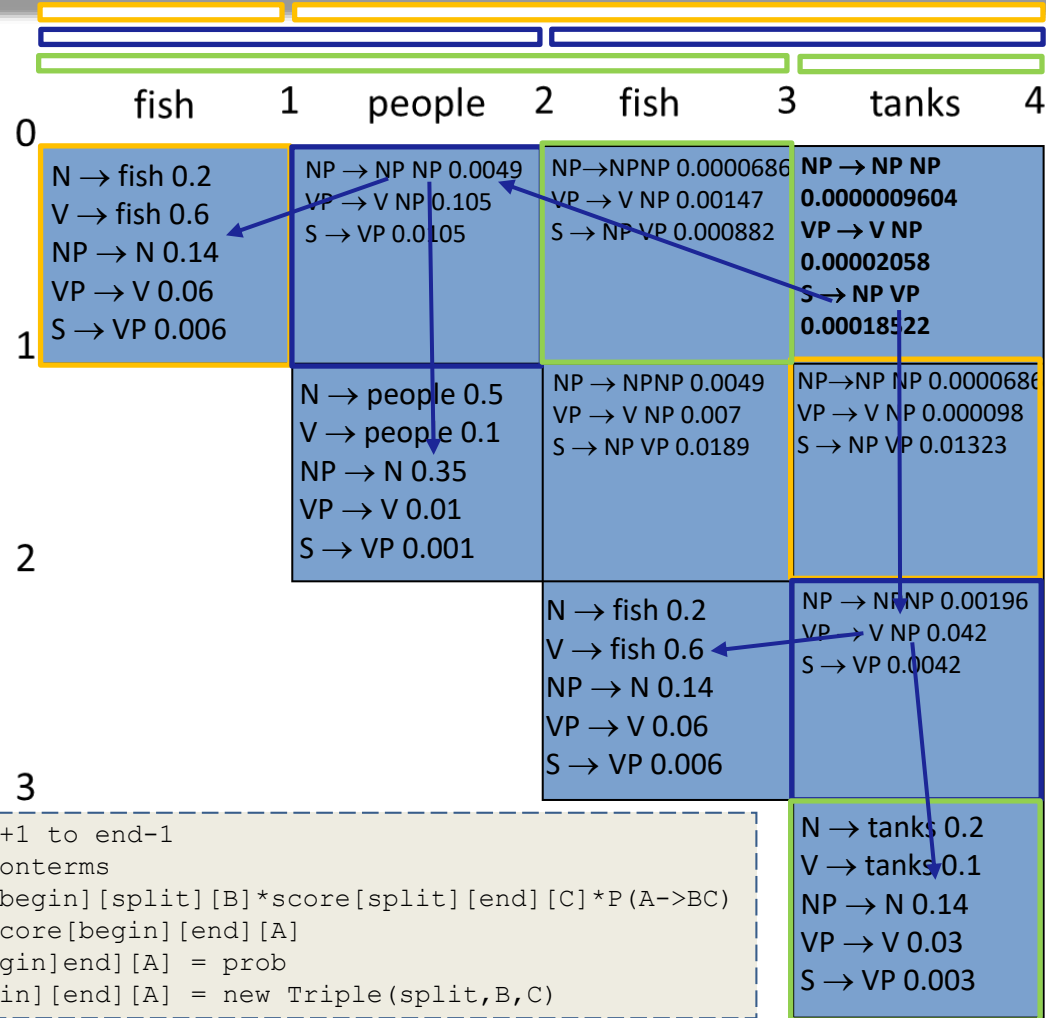
```

for split = begin+1 to end-1
  for A,B,C in nonterms
    prob=score[begin][split][B]*score[split][end][C]*P(A->BC)
    if prob > score[begin][end][A]
      score[begin][end][A] = prob
      back[begin][end][A] = new Triple(split,B,C)

```

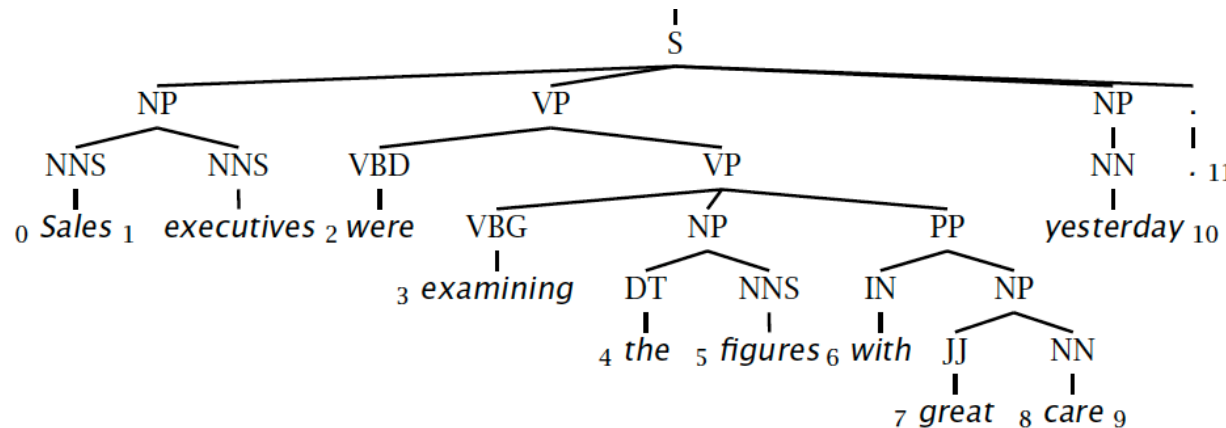
# CKY Parsing: A Worked Example

$S \rightarrow NP VP$	0.9
$S \rightarrow VP$	0.1
$VP \rightarrow V NP$	0.5
$VP \rightarrow V$	0.1
$VP \rightarrow V @VP\_V$	0.3
$VP \rightarrow V PP$	0.1
$@VP\_V \rightarrow NP PP$	1.0
$NP \rightarrow NP NP$	0.1
$NP \rightarrow NP PP$	0.2
$NP \rightarrow N$	0.7
$PP \rightarrow P NP$	1.0
$N \rightarrow people$	0.5
$N \rightarrow fish$	0.2
$N \rightarrow tanks$	0.2
$N \rightarrow rods$	0.1
$V \rightarrow people$	0.1
$V \rightarrow fish$	0.6
$V \rightarrow tanks$	0.3
$P \rightarrow with$	1.0

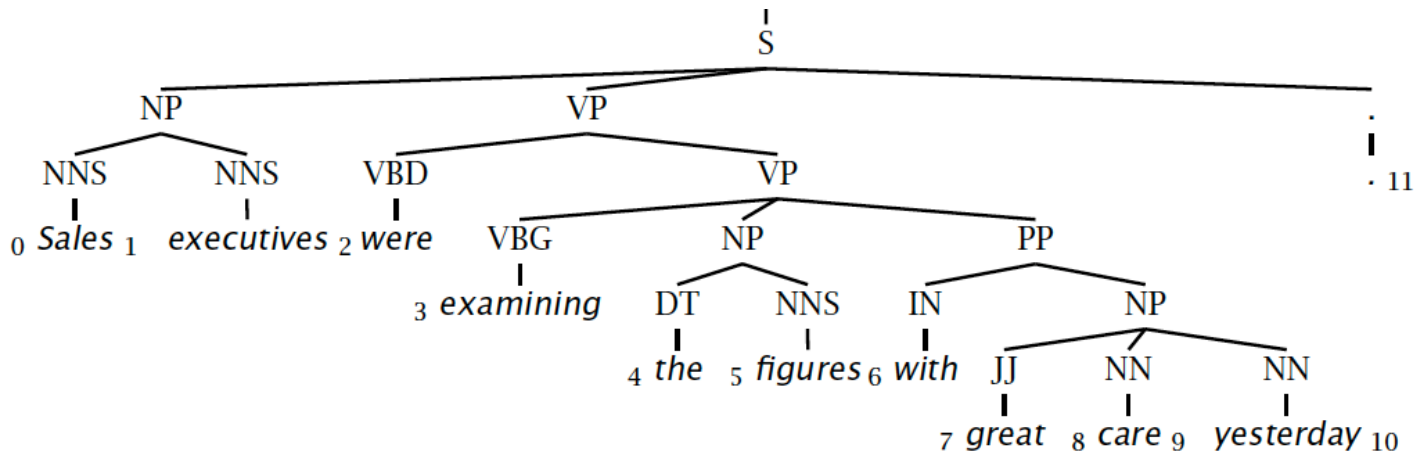


# Evaluating constituency parsing

Gold standard brackets: S-(0:11), NP-(0:2), VP-(2:9), VP-(3:9), NP-(4:6), PP-(6:9), NP-(7,9), NP-(9:10)



Candidate brackets: S-(0:11), NP-(0:2), VP-(2:10), VP-(3:10), NP-(4:6), PP-(6:10), NP-(7,10)



# Evaluating constituency parsing

## Gold standard brackets:

S-(0:11), NP-(0:2), VP-(2:9), VP-(3:9), NP-(4:6), PP-(6-9), NP-(7,9), NP-(9:10)

## Candidate brackets:

S-(0:11), NP-(0:2), VP-(2:10), VP-(3:10), NP-(4:6), PP-(6-10), NP-(7,10)

Labeled Precision                       $3/7 = 42.9\%$

Labeled Recall                          $3/8 = 37.5\%$

LP/LR F1                                40.0%

Tagging Accuracy                       $11/11 = 100.0\%$

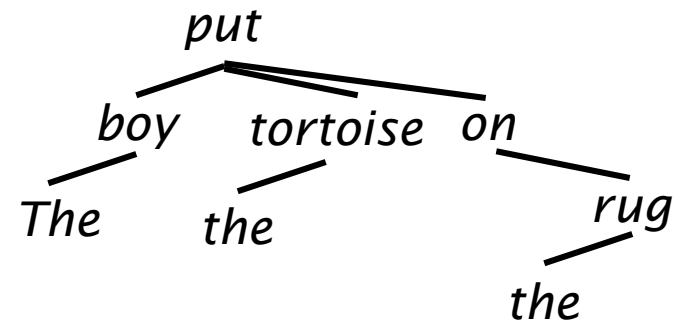
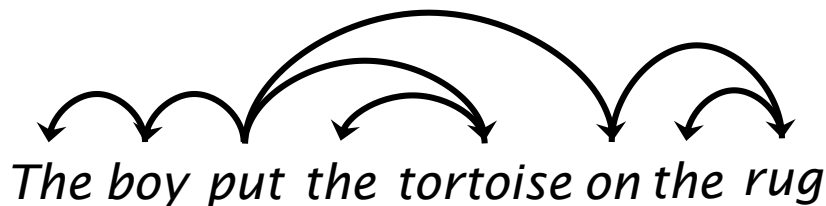
Penn WSJ parsing accuracy: about **73% LP/LR F1**



# Dependency Parsing

## • Dependency structure

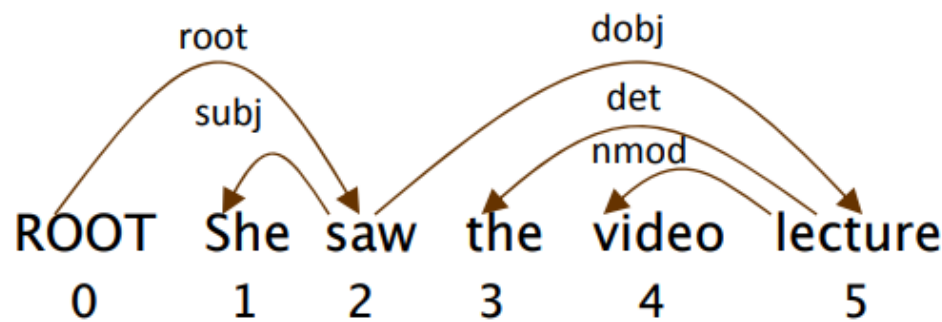
- Which **words depend on** (modify or are arguments of) **which other words**.
- Defined as **directed graph**  $G = (V, E)$ 
  - **Connected**: For every node  $i \in V$  there is a node  $j \in V$ , such that  $i \rightarrow j$  or  $j \rightarrow i$
  - **Acyclic**: No cycles
  - **Single-head**: Have only one parent (except for root token)
- Captures the **syntactic relations**



# Methods of Dependency Parsing

- **Dynamic programming** (like in the CKY algorithm)
- **Graph algorithms**
- **Constraint Satisfaction**
  - Edges are eliminated that don't satisfy hard constraints
- **“Deterministic parsing”**
  - Greedy choice of attachments guided by machine learning classifiers

# Evaluation



Unlabeled Attachment Score (UAS)  
 Labeled Attachment Score (LAS)  
 Label Accuracy (LA)

$$\text{UAS} = 4 / 5 = 80\%$$

$$\text{LAS} = 2 / 5 = 40\%$$

$$\text{LA} = 3 / 5 = 60\%$$

## Gold

1	She	2	subj
2	saw	0	root
3	the	5	det
4	video	5	nmod
5	lecture	2	dobj

## Parsed

1	She	2	subj
2	saw	0	root
3	the	4	det
4	video	5	vmod
5	lecture	2	iobj

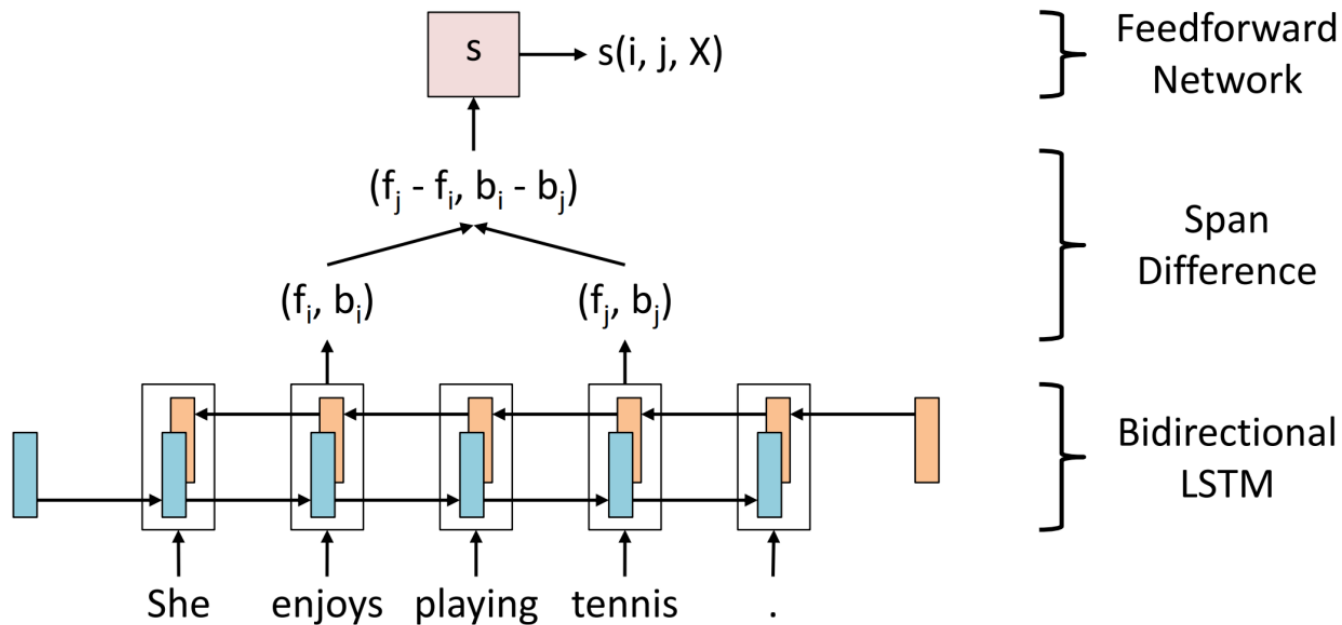
# Evaluation: State of the art

- The **CoNLL-X (2006) shared task** provides evaluation numbers for various dependency parsing approaches over 13 languages

Parser	UAS%
Sagae and Lavie (2006) ensemble of dependency parsers	92.7
Charniak (2000) generative, constituency	92.2
Collins (1999) generative, constituency	91.7
McDonald and Pereira (2005) – MST graph-based dependency	91.5
Yamada and Matsumoto (2003) – transition-based dependency	90.4

# Evaluation: State of the art

- Neural Approaches: **Neural Span Parser**



# Evaluation: State of the art

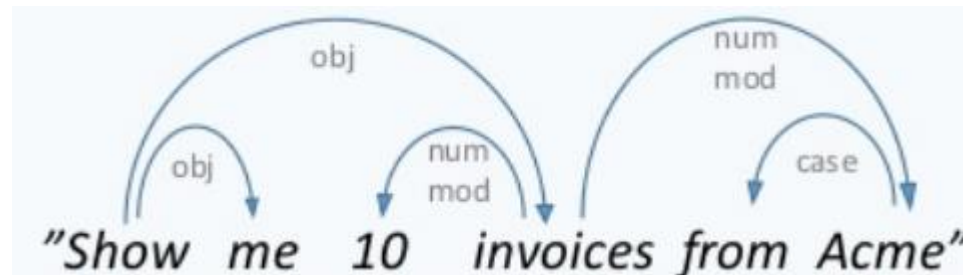
- Neural Approaches: **Neural Span Parser**

Parser	F
Automatic splitting (Petrov 2006)	89.6
Non-neural re-ranking parser (Charniak 2005)	91.0
Neural span parser (Stern 2017)	91.7
State-of-the-art neural (Kitaev 2018)	93.6
+ extra unlabeled data (Kitaev 2018)	95.1

# Why Parsing

## • Chatbot

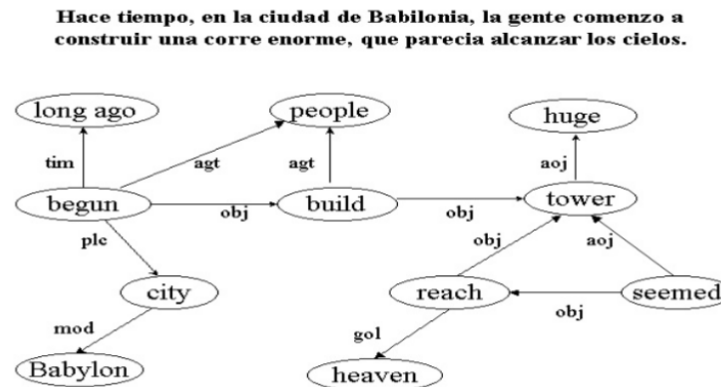
- Identify root of the user request
- Extract related objects



show(invoices) → invoices = ACME  
→ num(invoices) = 10

# Why Parsing

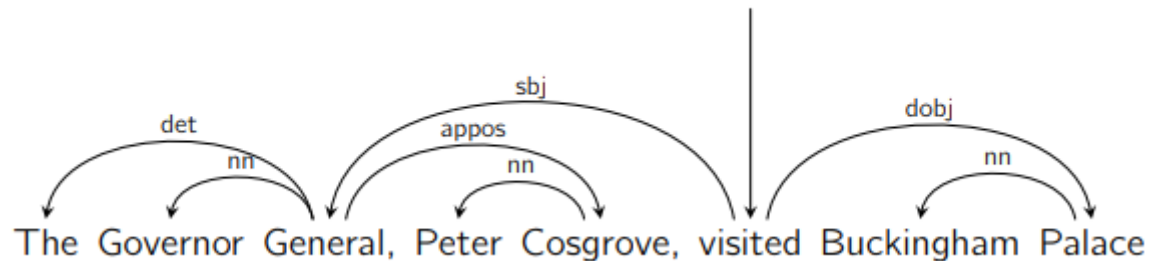
- Chatbot
  - **Machine Translation**
    - Extract a language-agnostic representation such as UNL
- [http://www.unlweb.net/wiki/index.php/Introduction to UNL](http://www.unlweb.net/wiki/index.php/Introduction_to_UNL)





# Why Parsing

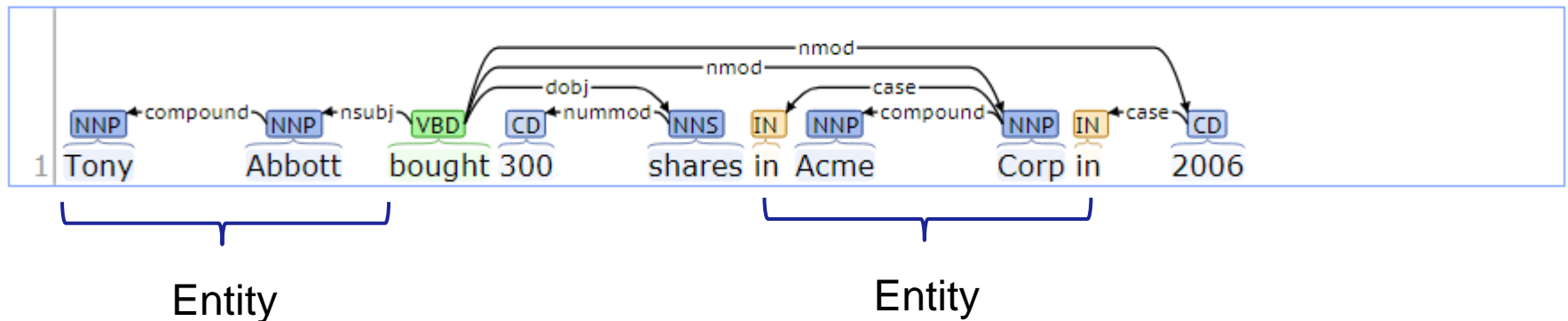
- Chatbot
- Machine Translation
- Relation Extraction



**Who is the governor general?**

# Why Parsing

- Chatbot
- Machine Translation
- Relation Extraction
- **Enhance NER**



# Why Parsing

- **Chatbot**
- **Machine Translation**
- **Relation Extraction**
- **Enhance NER**
- **Many more...**
  - A survey of parsing and its applications:  
<http://web.science.mq.edu.au/~mjohnson/papers/Johnson15ParsingSurvey.pdf>

# Practicals

- NLTK Parsers are outdated and slow
- Use Stanford Parser
  - Download CoreNLP server: <https://stanfordnlp.github.io/CoreNLP/corenlp-server.html>

```
from nltk.parse.corenlp import CoreNLPDependencyParser
dep_parser = CoreNLPDependencyParser(url='http://localhost:9000')

parse, = dep_parser.raw_parse('The quick brown fox jumps over the lazy dog.')
print(parse.tree())
```

The	DT	4	det
quick	JJ	4	amod
brown	JJ	4	amod
fox	NN	5	nsubj
jumps	VBZ	0	ROOT
over	IN	9	case
the	DT	9	det
lazy	JJ	9	amod
dog	NN	5	nmod
.	.	5	punct

# Practicals

- NLTK Parser are outdate and slow
- Use Stanford Parser
- or spacy
  - <https://spacy.io/usage/linguistic-features#dependency-parse>

```
import spacy

nlp = spacy.load('en')
doc = nlp('The quick brown fox jumps over the lazy dog.')
```

- Practical examples:  
<https://shirishkadam.com/2016/12/23/dependency-parsing-in-nlp/>