



POLITECNICO
MILANO 1863

3D ISOLATED ROTOR IN HOVER

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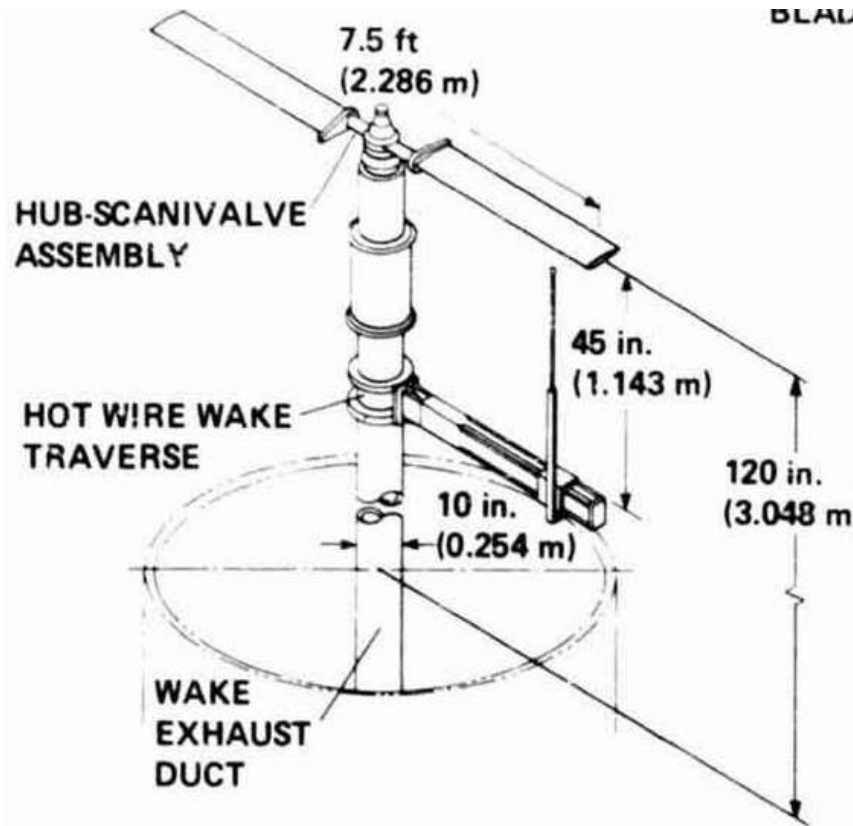
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INTRODUCTION



- Rotorcrafts – a unique vehicle with a capability of VTOL
- Many codes developed by institutions and academia. Eg: FUN3D, ROSITA etc.
- Perks of Open-source softwares

REFERENCE EXPERIMENT



- A hallmark experiment by F. X. Caradonna and C. Tung
- Symmetric NACA0012 profile

Features

<i>Chord</i>	<i>Aspect Ratio</i>	<i>Rotor radius</i>
0.19114 m	6	1.143 m

DESIGN AND SETUP

Goal: To computationally reproduce the experiment by
F. X. Caradonna and C. Tung with SU2

Procedure :

- Mesh generation (Gmsh)
- Mesh convergence
- Verification and Validation of results
- Comparison of Numerical schemes

COMPUTATIONAL MODEL: Problem specifications (1)

- Surface Geometry



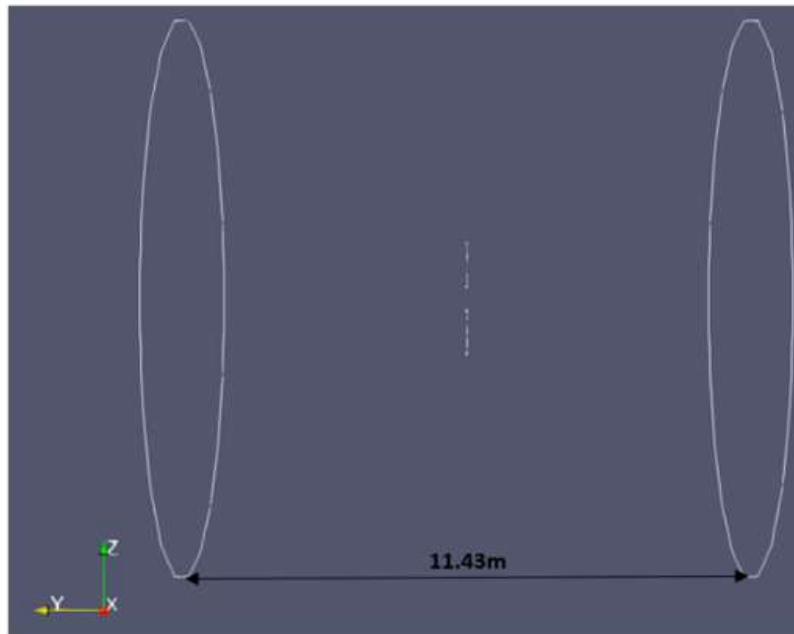
(a) Rotor diameter.



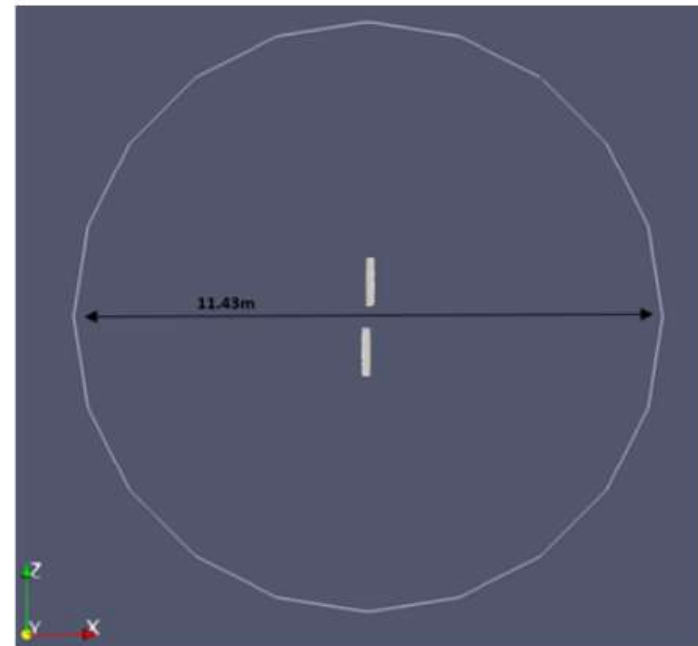
(b) Blade geometry.

COMPUTATIONAL MODEL: Problem specifications (2)

- Farfield Geometry



(a) External boundary height.



(b) External boundary diameter.

COMPUTATIONAL MODEL: Problem specifications (3)

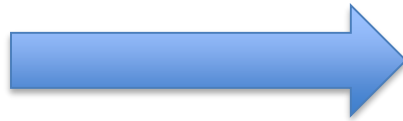
<i>Rotor radius</i>	<i>Disk Area</i>	<i>Aspect Ratio</i>	<i>Cutoff Length</i>	<i>Blade Length</i>
<i>1.143 m</i>	<i>4.104 sq m</i>	<i>6</i>	<i>0.2286 m</i>	<i>0.9144 m</i>

- Free-stream values

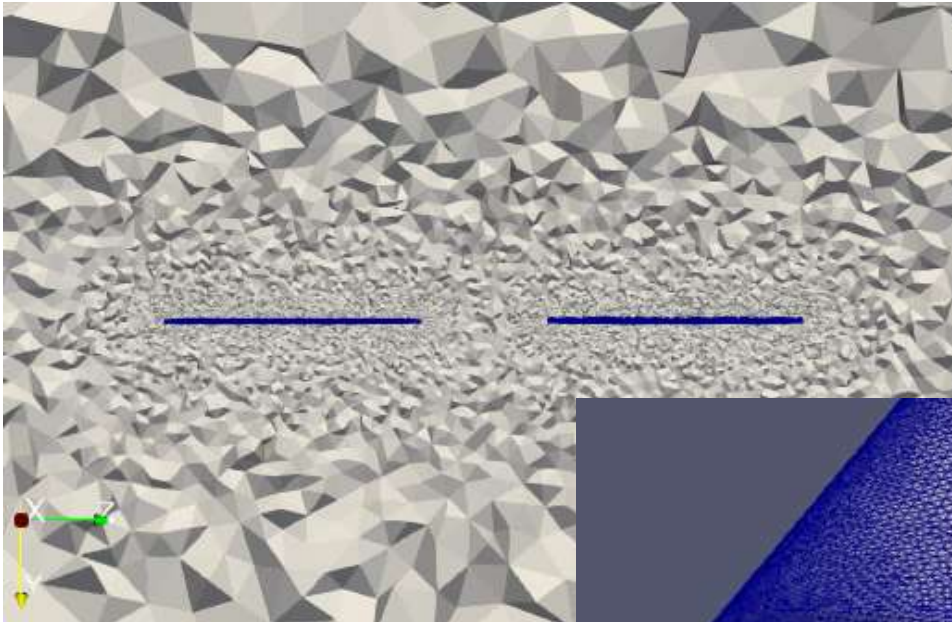
Gas constant	287.058 Nm/kgK
Spec. heat ratio	1.4
Static pressure	101325 Pa
Density	1.22498 kg/m^3
Temperature	288.15 K
Total energy per unit mass	$206789 \text{ m}^2/\text{s}^2$

MESH GENERATION

- Surface mesh
- Volume mesh

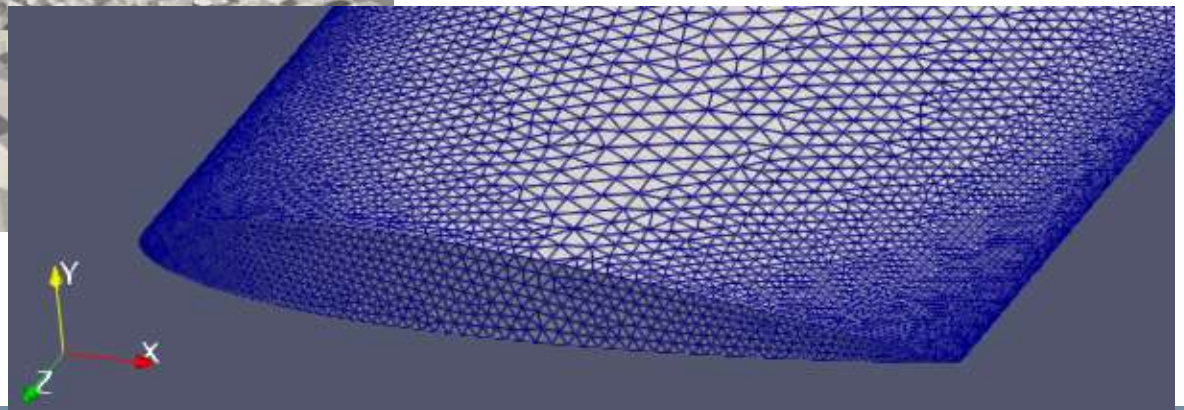


UNSTRUCTURED



Unstructured blade surface mesh

spanwise mesh section

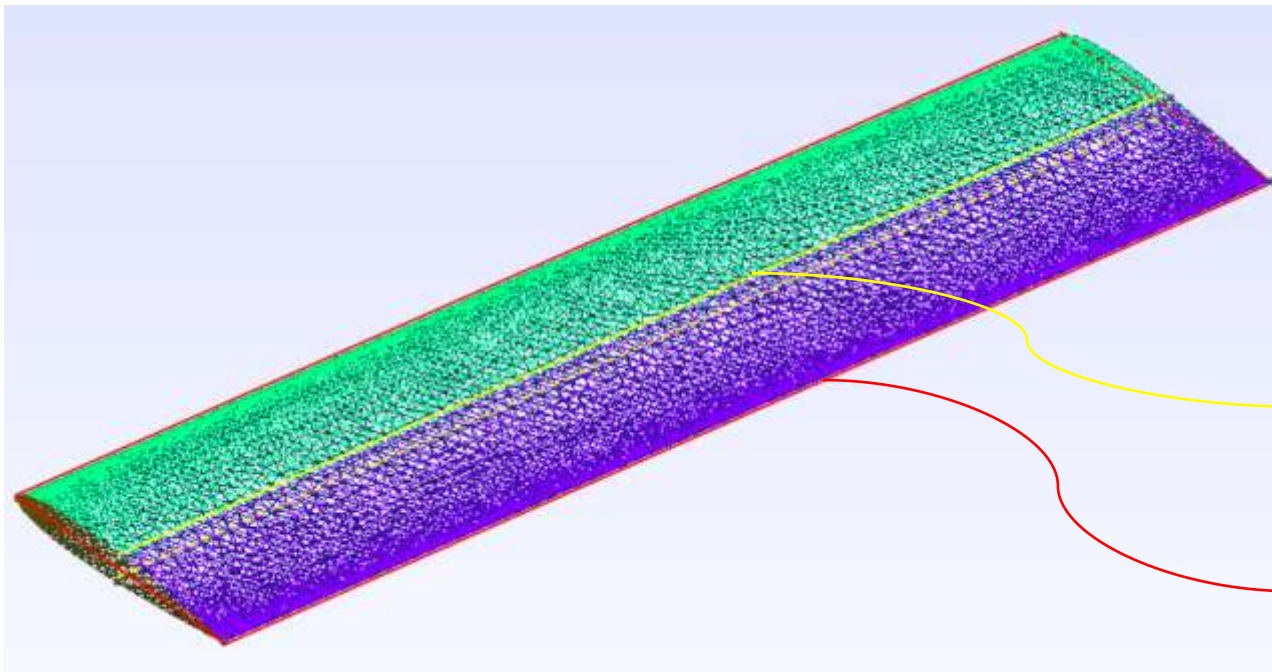


MESH GENERATION – FIELD MESHING

Parameters $\left\{ \begin{array}{l} h \\ \text{dim} \\ C \\ N \end{array} \right.$



reference dimension of surface elements
reference dimension of farfield elements
exponential profile constant
number of spanwise elements at C/2



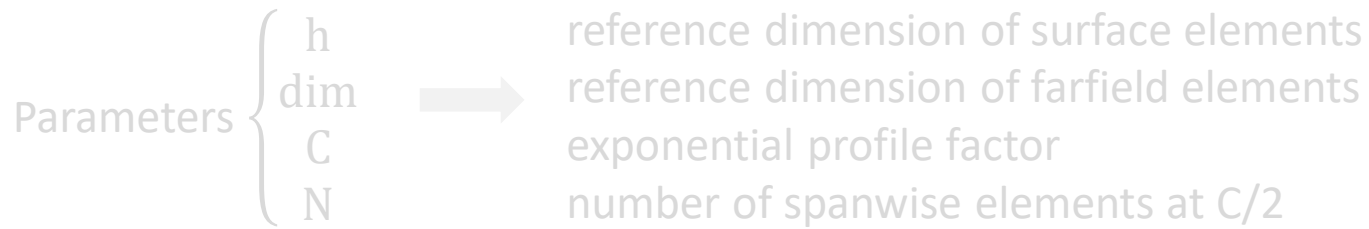
Exponential profile:

$$h = C + e^{F1 - \frac{5}{2}}$$

C/2 lines

Wing planform
perimeter

MESH GENERATION – 4 MESHES



Exponential profile:

$$h - C + e^{F1 - \frac{5}{2}}$$

	MESH 1	MESH 2	MESH 3	MESH 4
h	0.0075	0.0055	0.003	0.0025
Dim	2	2	2	2
N	75	105	150	175
C	0.065	0.0775	0.079	0.08
Elements	469804	1476898	2744096	3558951

NUMERICAL IMPLEMENTATION

Numerical approach



Finite Volume Method (FVM)

Governing equations:
COMPRESSIBLE EULER



Flight condition:
HOVERING



ROTATING FRAME

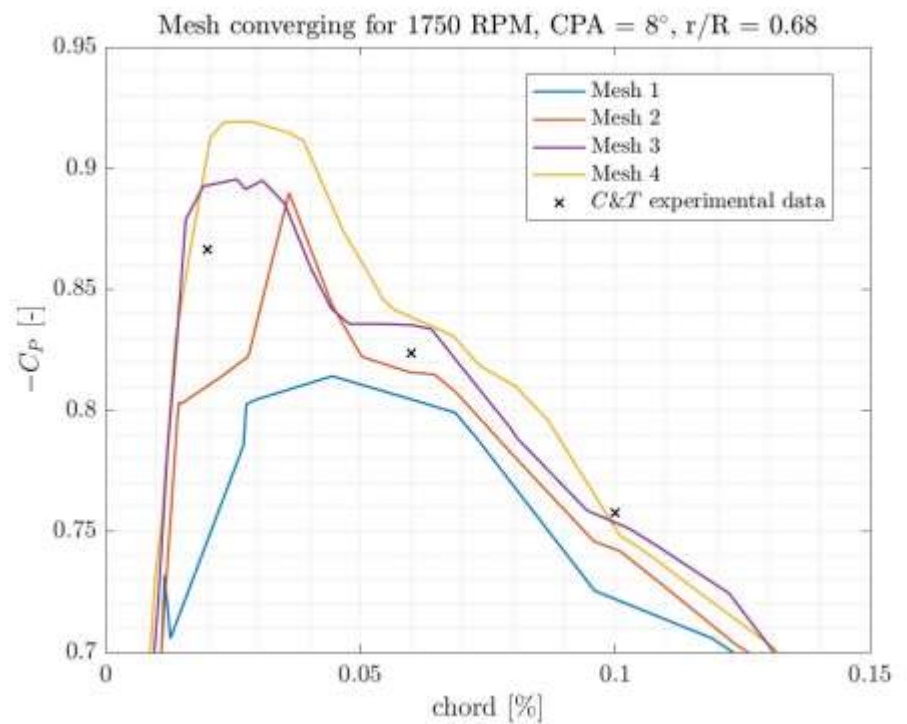
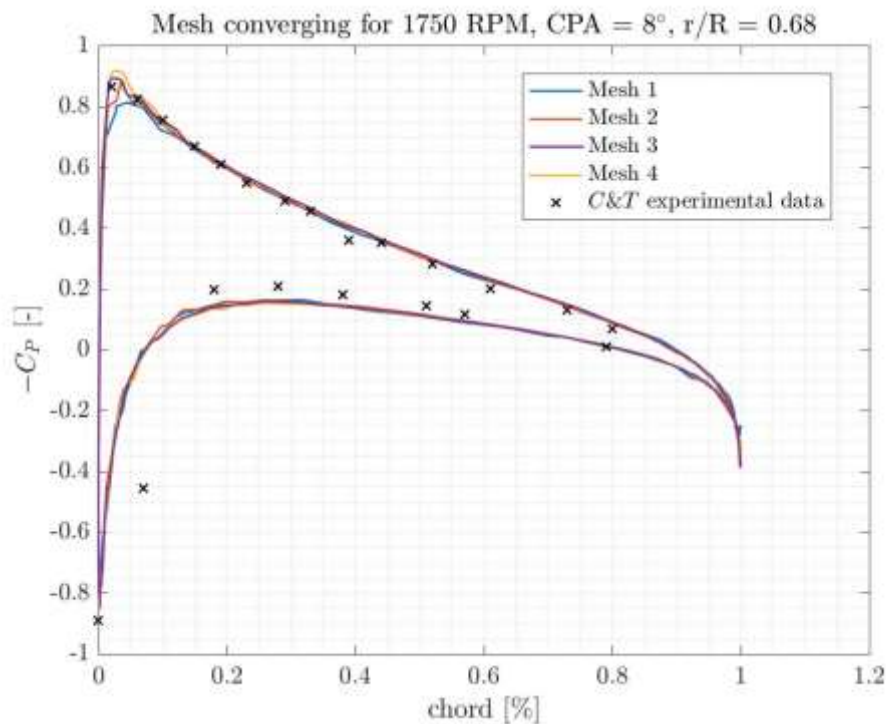
$$\begin{cases} \nabla \cdot \mathbf{F}_r(\mathbf{U}) - \mathbf{S}_r = 0 & \text{in } \Omega \\ (\mathbf{u} - \mathbf{u}_r) \cdot \mathbf{n}_s = 0 & \text{on } \Gamma_s \\ W_+ = W_\infty & \text{on } \Gamma_\infty \end{cases}$$

$$\mathbf{S}_r = \begin{Bmatrix} S_\rho \\ S_{\rho u} - \rho(\boldsymbol{\omega} \times \mathbf{u}) \\ S_E \end{Bmatrix}$$

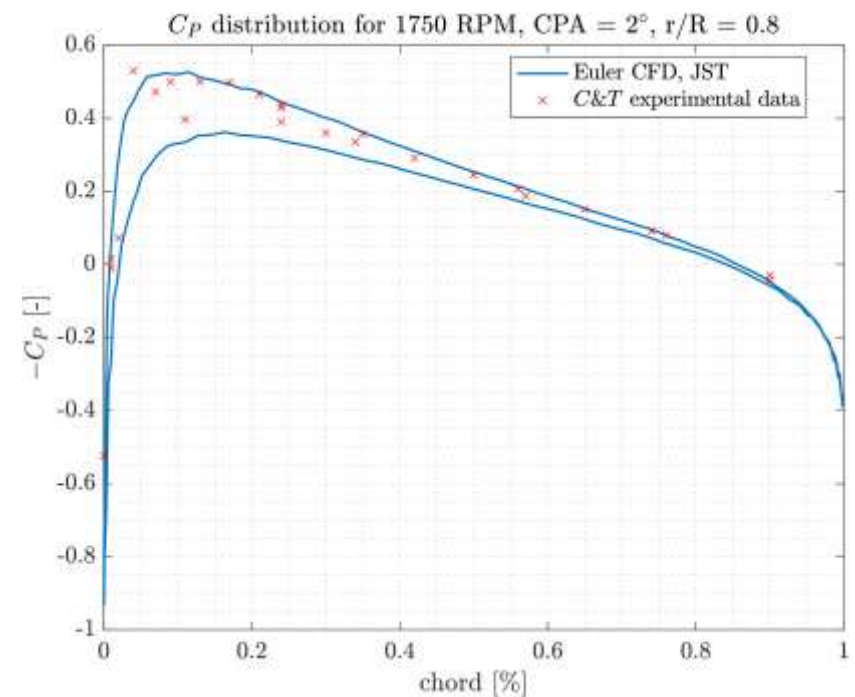
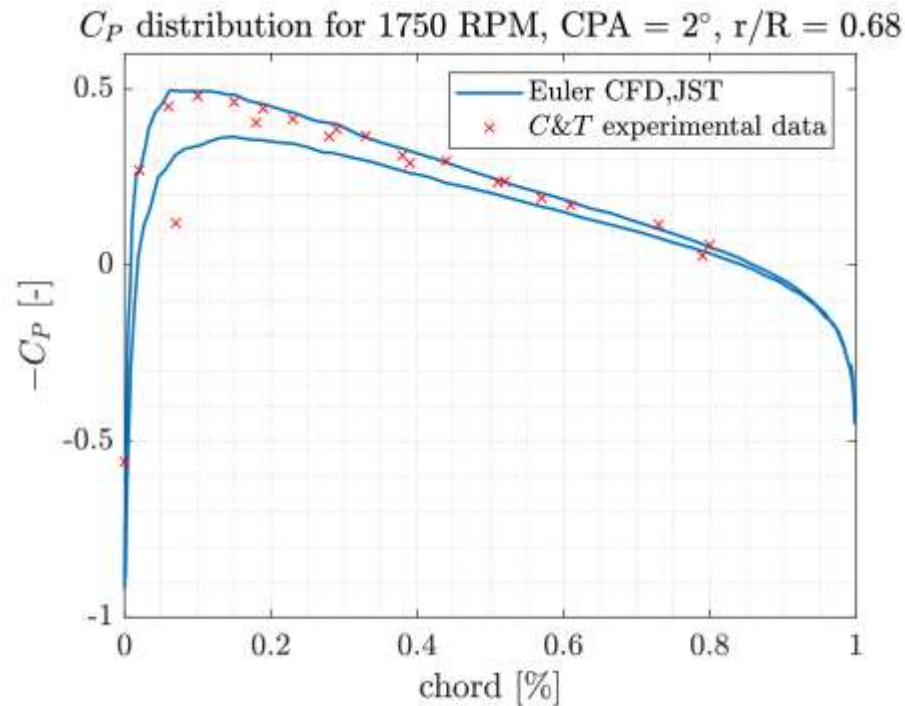
$$\mathbf{F}_r = \begin{Bmatrix} \rho(\mathbf{u} - \mathbf{u}_r) \\ \rho \mathbf{u} \otimes (\mathbf{u} - \mathbf{u}_r) + \mathcal{I}P \\ E(\mathbf{u} - \mathbf{u}_r) + P\mathbf{u} \end{Bmatrix}$$

$$\mathbf{u}_r = \boldsymbol{\omega} \times \mathbf{r}$$

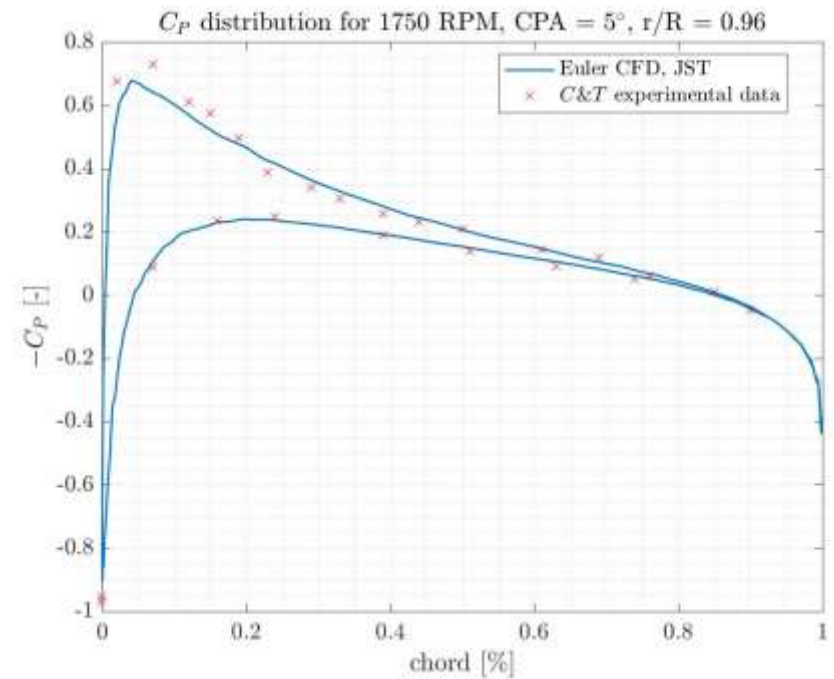
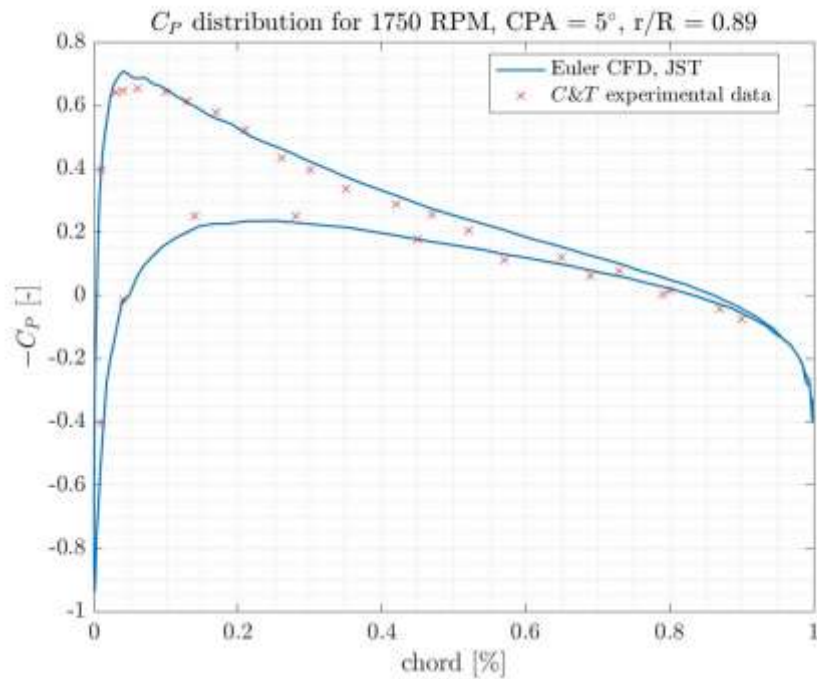
1750 RPM: Mesh Convergence



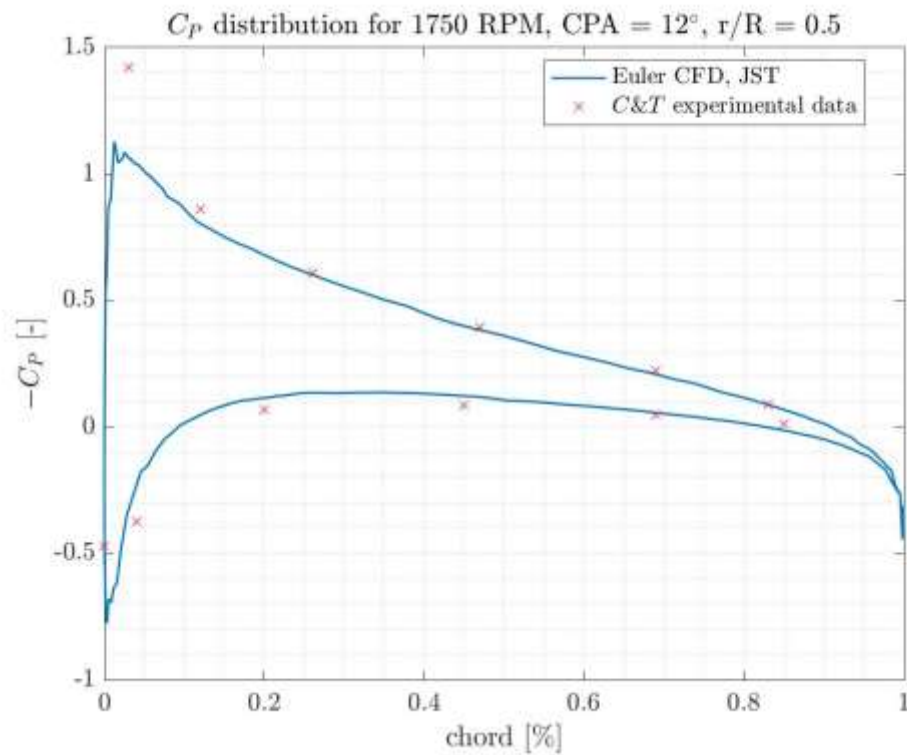
1750 RPM: C_p Plot, 2° CPA



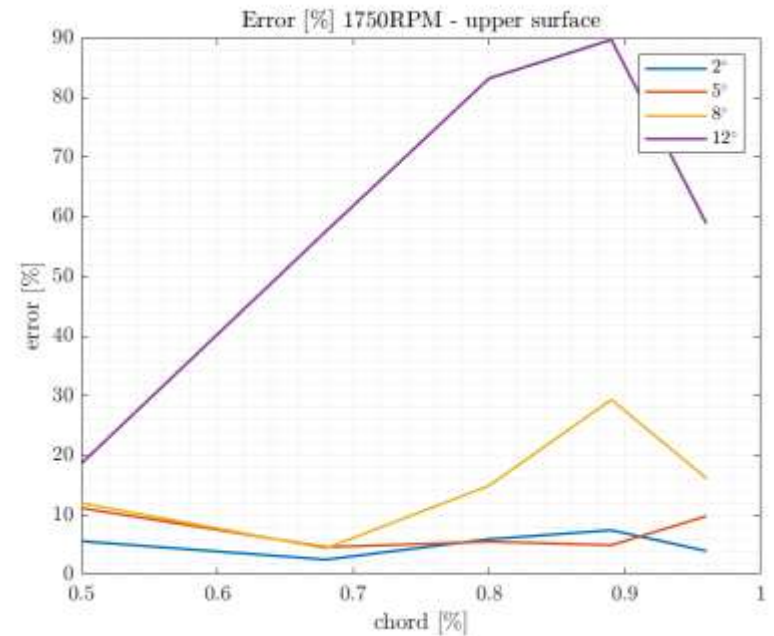
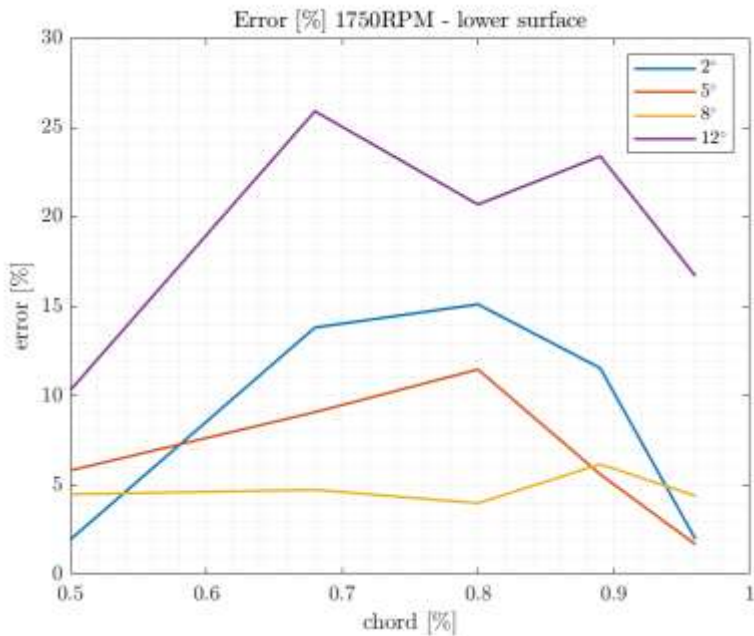
1750 RPM: C_p Plot, 5° CPA



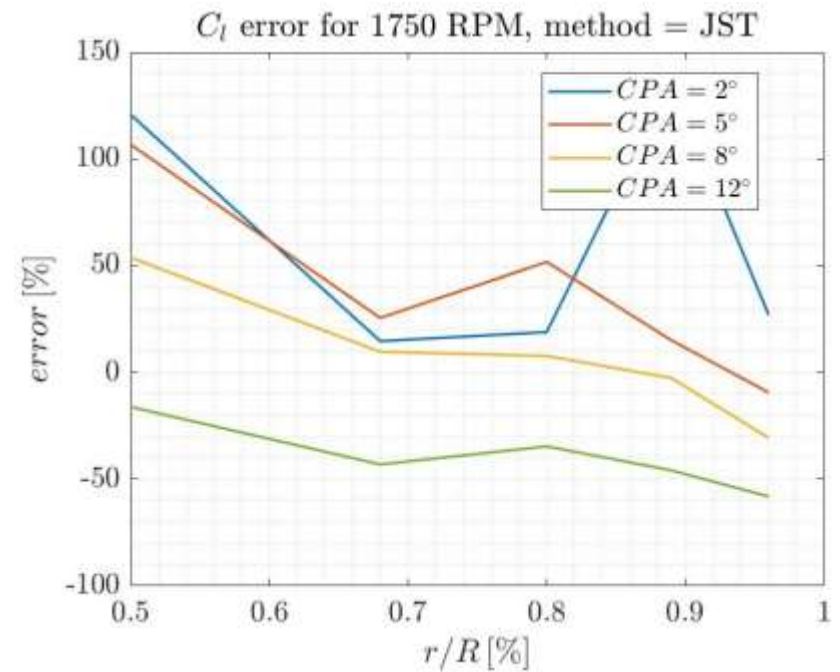
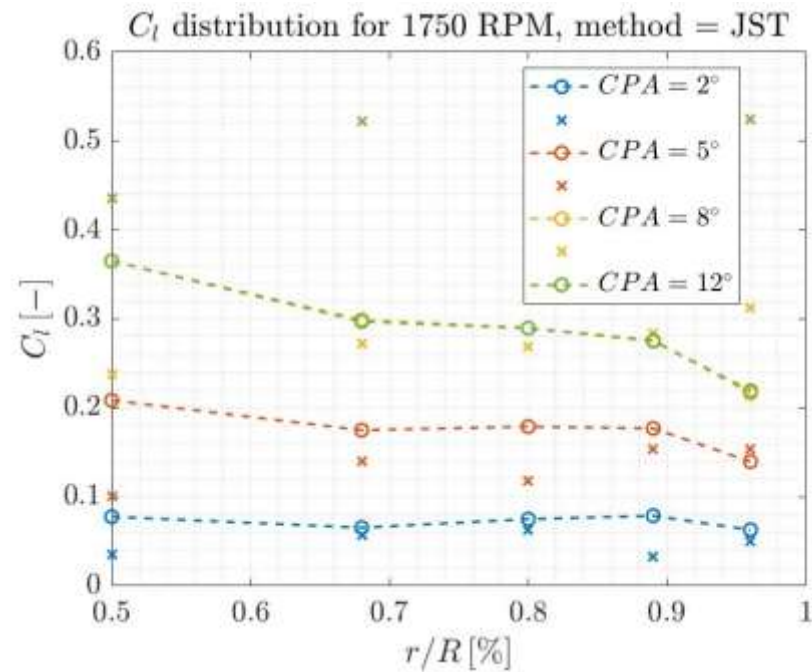
1750 RPM: C_p Plot, 12° CPA



1750 RPM: Cp error %



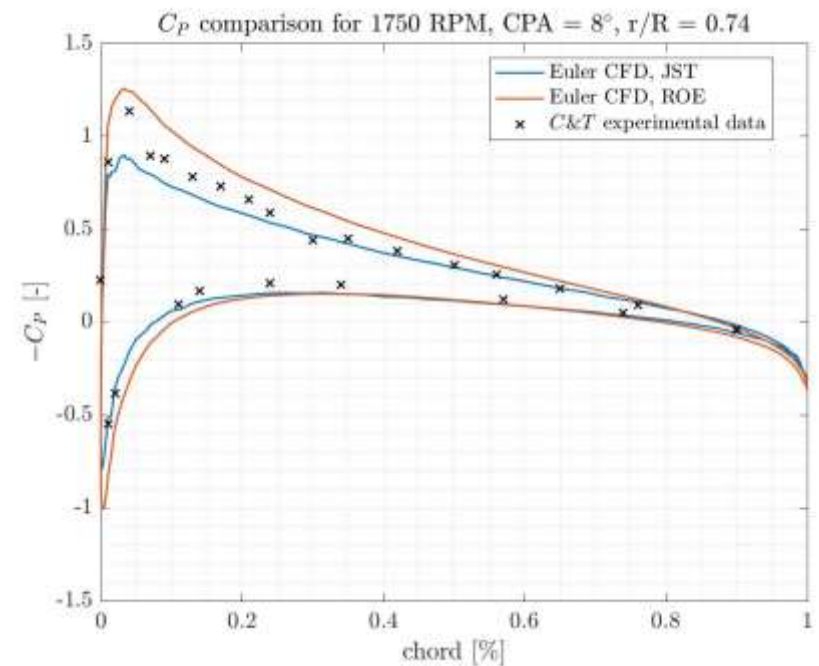
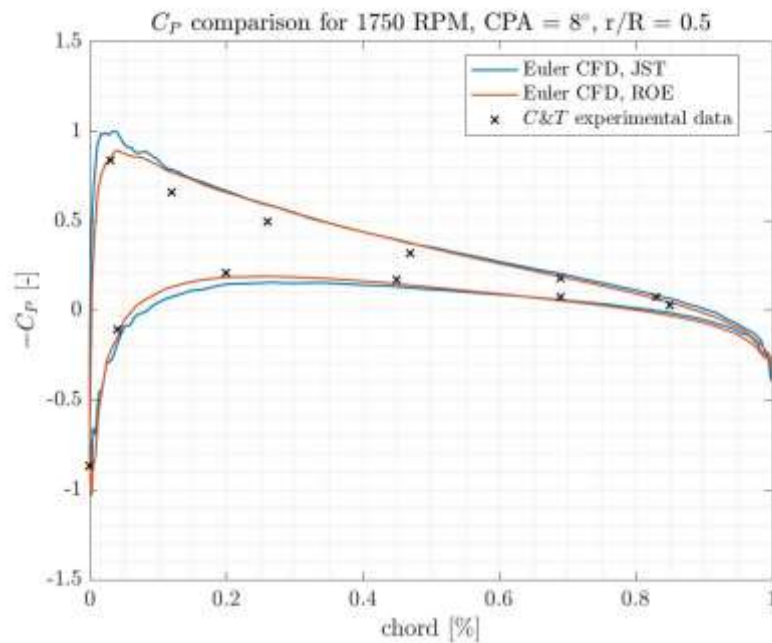
1750 RPM: Sectional lift coefficient



1750 RPM: Thrust Coefficient

	2°	5°	8°	12°
<i>C&T</i>	<i>NA</i>	<i>0.00218</i>	<i>0.00455</i>	<i>0.00807</i>
<i>Euler</i>	<i>0.00103</i>	<i>0.00251</i>	<i>0.00413</i>	<i>0.00418</i>

1750 RPM: JST vs ROE 2° order (1)



1750 RPM: JST vs ROE 2° order (2)

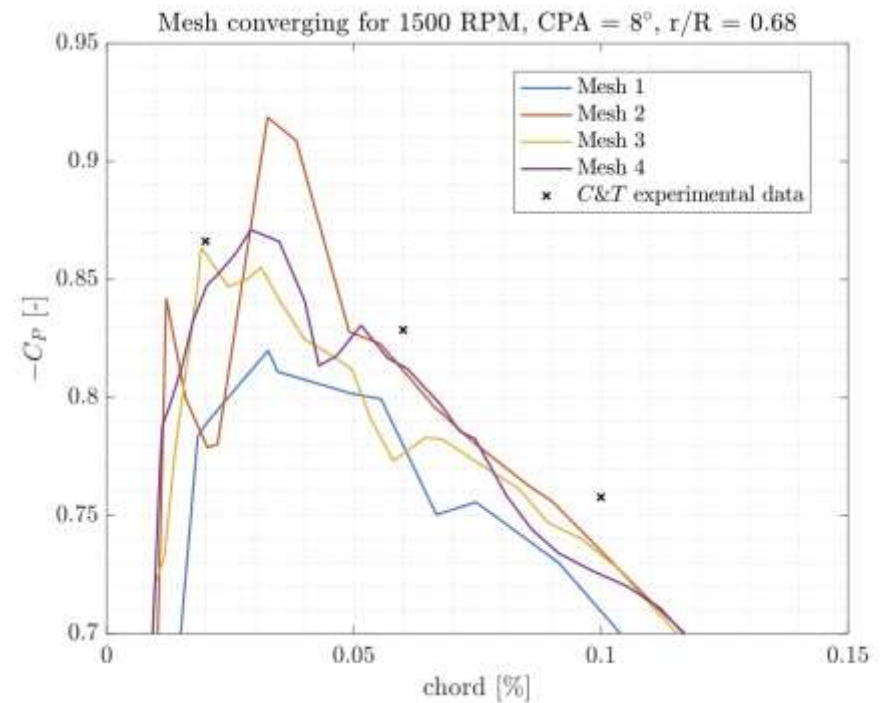
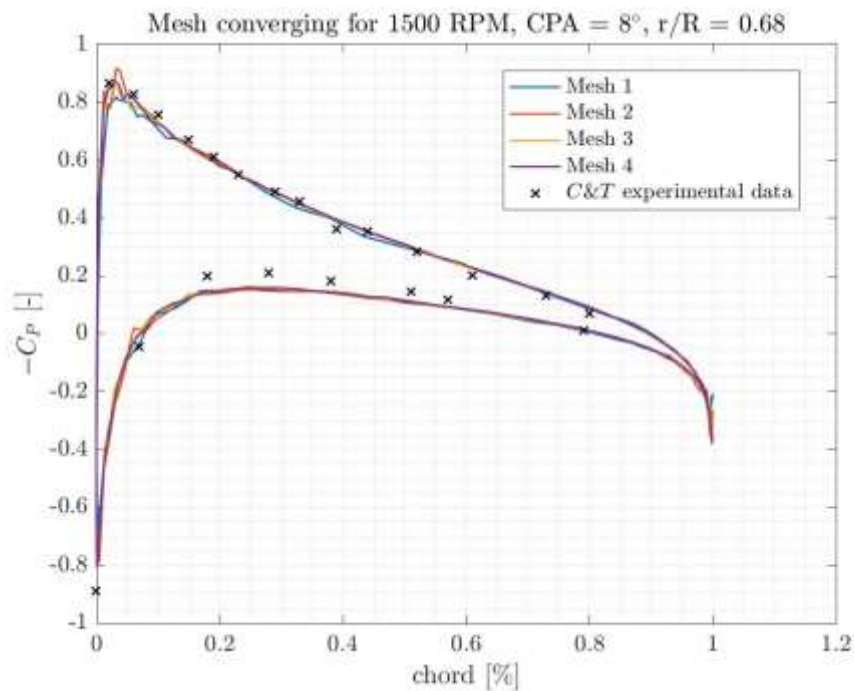
Sectional lift coefficients

r/R	<i>0.50</i>	<i>0.68</i>	<i>0.8</i>	<i>0.89</i>	<i>0.96</i>
<i>C&T</i>	0.2374	0.2728	0.2690	0.2865	0.3125
<i>JST</i>	0.3566	0.2857	0.2825	0.2735	0.2088
<i>ROE</i>	0.2831	0.3481	0.3986	0.3832	0.2948

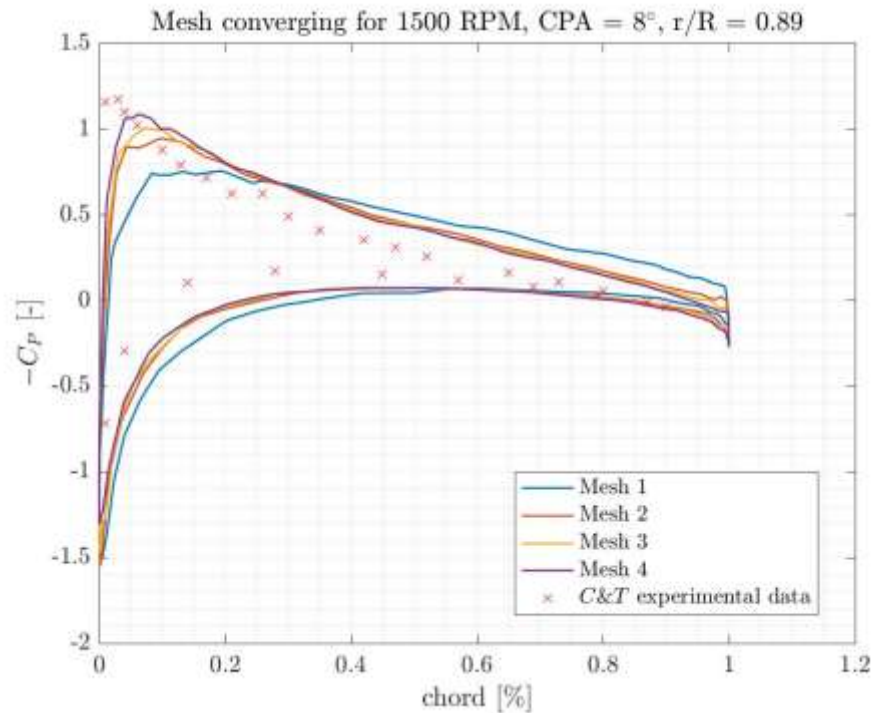
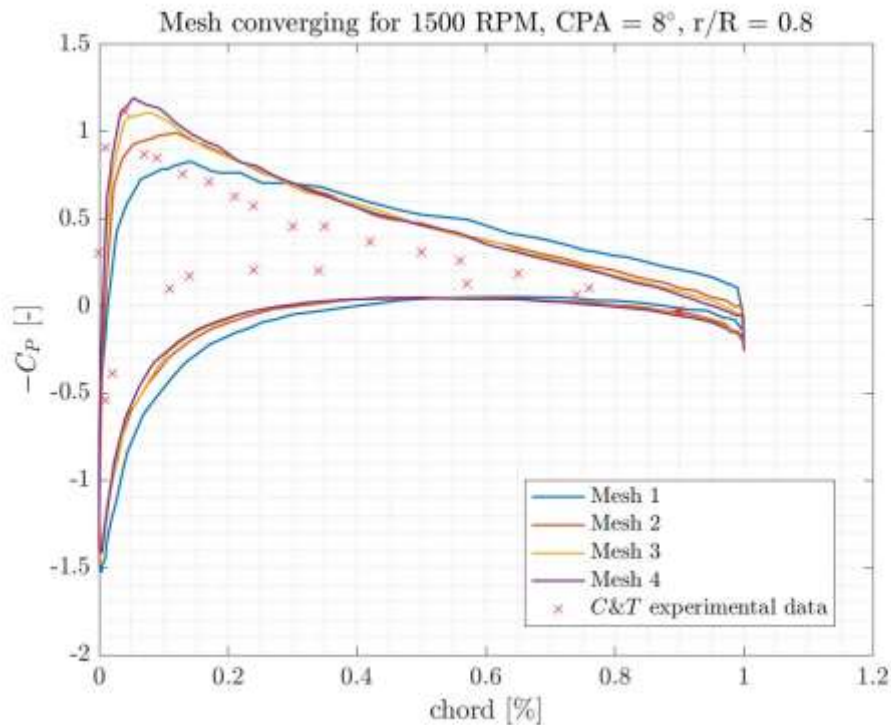
1500 RPM Case

- JST 2nd order
 $CPA = 2^\circ, 5^\circ, 8^\circ, 12^\circ$
- ROE 1st order
 $CPA = 8^\circ$

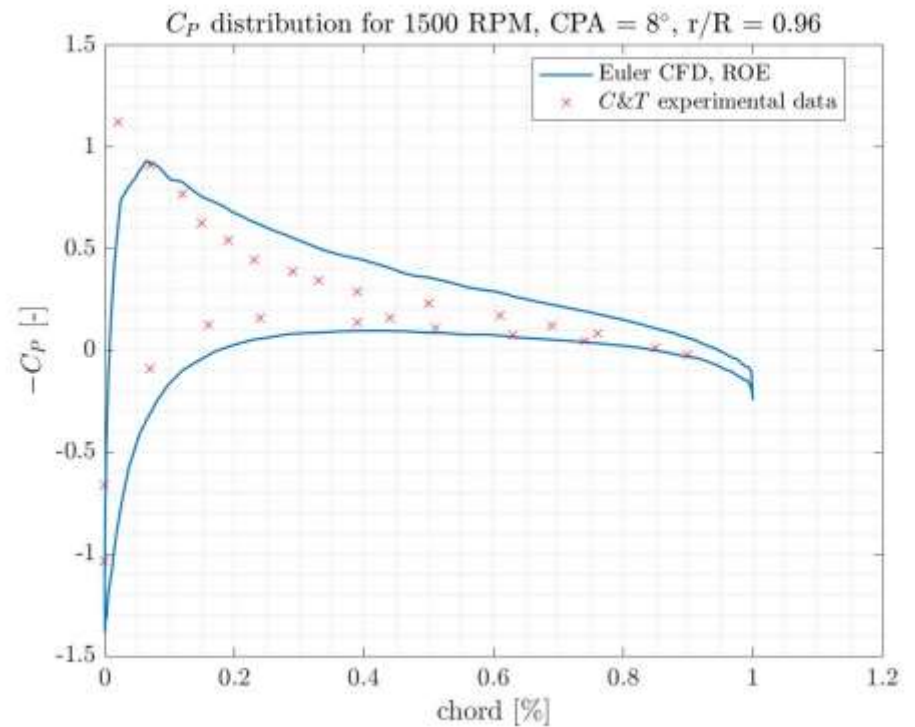
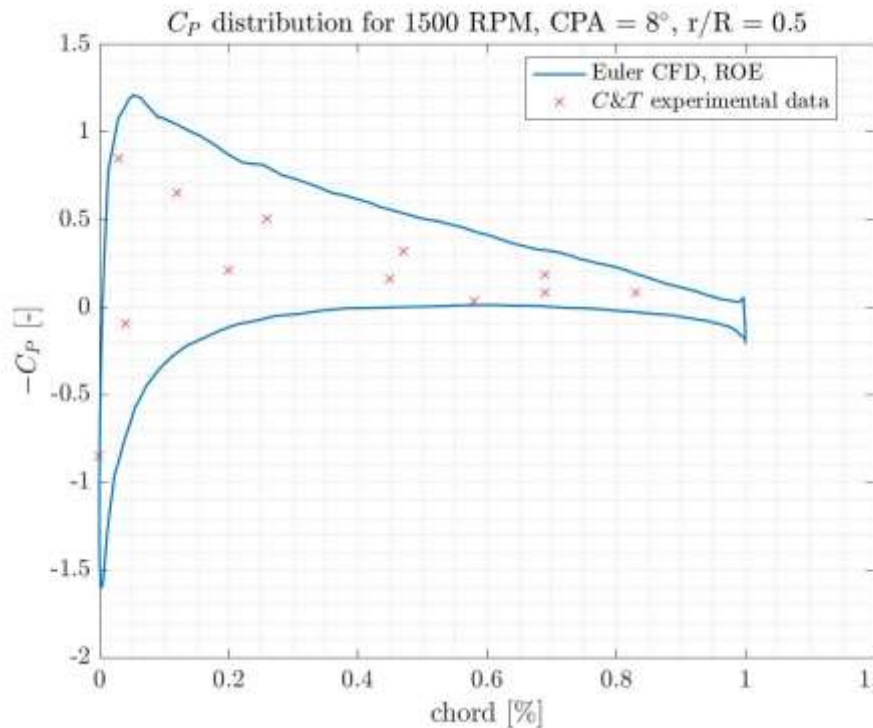
1500 RPM: 2nd order JST, Mesh convergence



1500 RPM: 1st order ROE, mesh convergence



1500 RPM: 1st order ROE, Pressure coefficient results



1500 RPM, 1st order ROE, lift and thrust coefficients

CPA = 8°

r/R [-]	C&T	CFD	Error [%]
0.50	0.2409	0.6475	169
0.68	0.2638	0.6158	133
0.80	0.2633	0.5738	118
0.89	0.2760	0.5053	83
0.96	0.3052	0.4067	33

Sectional lift coefficient

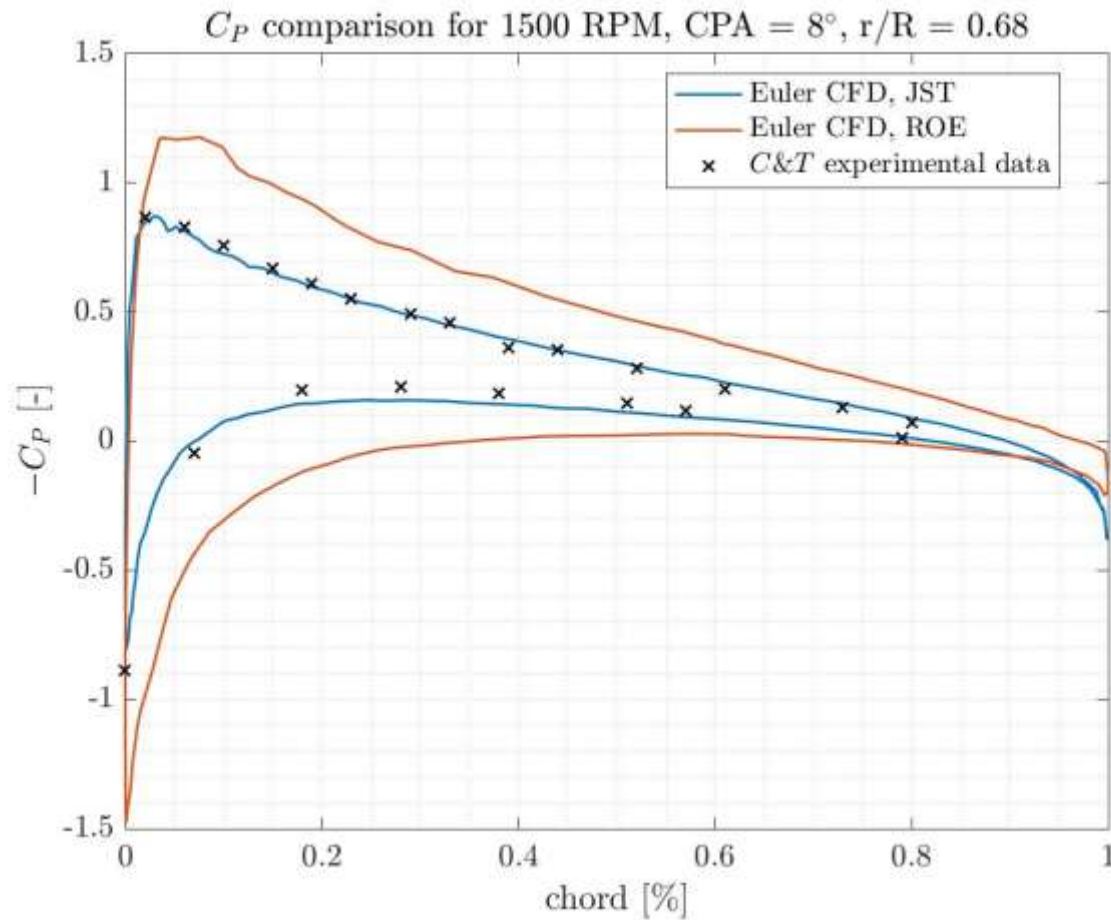
Comparison CFD results vs. empirical data.

CFD	0.00771
C&T 1750 RPM	0.00459
C&T 1250 RPM	0.00455

Thrust coefficient

Comparison CFD results vs. empirical data.

1500 RPM: 2nd order JST vs 1st order ROE



Conclusions

- Generally most accurate results for small CPAs
- Numerical issues
 - Structured mesh for blades are unfeasible with the meshing software used
 - Limited computational power
 - Problem geometry simplification
 - Euler numerical scheme not accurate

Thank you for attention!

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