

# 2020-Sept Session-09-04-2020 shift<sup>1</sup>

## 2

AI24BTECH11016

1 1-15(MATH)

- 1) Suppose the vectors  $\mathbf{x}_1$ ,  $\mathbf{x}_2$  and  $\mathbf{x}_3$  are the solutions of the system of linear equations,  $A\mathbf{x} = \mathbf{b}$  when the vector  $\mathbf{b}$  on the right side is equal to  $\mathbf{b}_1$ ,  $\mathbf{b}_2$  and  $\mathbf{b}_3$  respectively. If  $\mathbf{x}_1 = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$ ,  $\mathbf{x}_2 = \begin{pmatrix} 0 \\ 2 \\ 1 \end{pmatrix}$ ,  $\mathbf{x}_3 = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$ ,  $\mathbf{b}_1 = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$ ,  $\mathbf{b}_2 = \begin{pmatrix} 0 \\ 2 \\ 0 \end{pmatrix}$ ,  $\mathbf{b}_3 = \begin{pmatrix} 0 \\ 2 \\ 2 \end{pmatrix}$ , then the determinant of  $A$  is equal to [Sept 2020]

- a) 2
- b)  $\frac{1}{2}$
- c)  $\frac{3}{2}$
- d) 4

- 2) If  $a$  and  $b$  are real numbers such that  $(2 + \alpha)^4 = a + b\alpha$ , where  $\alpha = \frac{-1+i\sqrt{3}}{2}$  then  $a + b$  is equal to: [Sept 2020]

- a) 33
- b) 57
- c) 9
- d) 24

- 3) The distance of the point  $\begin{pmatrix} 1 \\ -2 \\ 3 \end{pmatrix}$  from the plane  $x - y + z = 5$  measured parallel to the

line  $\frac{x}{2} = \frac{y}{3} = \frac{z}{-6}$  is: [Sept 2020]

- a)  $\frac{1}{7}$
- b) 7
- c)  $\frac{7}{5}$
- d) 1

- 4) Let  $f : (0, \infty) \rightarrow (0, \infty)$  be a differentiable function such that  $f(1) = e$  and  $\lim_{t \rightarrow x} \frac{t^2 f^2(x) - x^2 f^2(t)}{t - x} = 0$   
If  $f(x) = 1$ , then  $x$  is equal to: [Sept 2020]

- a)  $e$
- b)  $2e$
- c)  $\frac{1}{e}$
- d)  $\frac{e}{2}$

- 5) Contrapositive of the statement :

If a function  $f$  is differentiable at  $a$ , then it is also continuous at  $a$ , is: [Sept 2020]

- a) If a function  $f$  is not continuous at  $a$ , then it is not differentiable at  $a$ .

- b) If a function  $f$  is continuous at  $a$ , then it is differentiable at  $a$ .  
 c) If a function  $f$  is continuous at  $a$ , then it is not differentiable at  $a$ .  
 d) If a function  $f$  is continuous at  $a$ , then it is not differentiable at  $a$ .
- 6) The minimum value of  $2^{\sin(x)} + 2^{\cos(x)}$  is: [Sept 2020]  
 a)  $2^{1-\sqrt{2}}$   
 b)  $2^{1-\frac{1}{\sqrt{2}}}$   
 c)  $2^{-1+\sqrt{2}}$   
 d)  $2^{-1+\frac{1}{\sqrt{2}}}$
- 7) If the perpendicular bisector of the line segment joining the points  $P\left(\frac{1}{4}\right)$  and  $Q\left(\frac{k}{3}\right)$  has y-intercept equal to  $-4$ , then a value of  $k$  is: [Sept 2020]  
 a)  $-2$   
 b)  $\sqrt{15}$   
 c)  $\sqrt{14}$   
 d)  $-4$
- 8) The area (in sq. units) of the largest rectangle  $ABCD$  whose vertices **A** and **B** lie on the  $x$ -axis and vertices **C** and **D** lie on the parabola,  $y = x^2 - 1$  below the  $x$ -axis, is: [Sept 2020]  
 a)  $\frac{2}{3\sqrt{3}}$   
 b)  $\frac{4}{3}$   
 c)  $\frac{1}{3\sqrt{3}}$   
 d)  $\frac{4}{3\sqrt{3}}$
- 9) The integral  $\int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \tan^3 x \sin^2 3x (2 \sec^2 x \sin^2 3x + 3 \tan x \sin 6x) dx$  is equal to [Sept 2020]  
 a)  $\frac{9}{2}$   
 b)  $\frac{-1}{18}$   
 c)  $\frac{-1}{9}$   
 d)  $\frac{7}{18}$
- 10) If the system of equations  $x + y + z = 2$   
 $2x + 4y - z = 6$   
 $3x + 2y + \lambda z = \mu$   
 has infinitely many solutions, then [Sept 2020]  
 a)  $\lambda - 2\mu = -5$   
 b)  $2\lambda + \mu = 14$   
 c)  $\lambda + 2\mu = 14$   
 d)  $2\lambda - \mu = 5$
- 11) In a game two players A and B take turns in throwing a pair of fair dice starting with player A and total of scores on the two dice, in each throw is noted. A wins the game if he throws a total of 6 before B throws a total of 7 and B wins the game if he throws a total of 7 before A throws a total of six The game stops as soon as either of the players wins. The probability of A winning the game is : [Sept 2020]  
 a)  $\frac{5}{31}$

- b)  $\frac{31}{60}$
- c)  $\frac{30}{61}$
- d)  $\frac{5}{6}$

12) If for some positive integer  $n$ , the coefficients of three consecutive terms in the binomial expansion of  $(1+x)^{n+5}$  are in the ratio 5 : 10 : 14, then the largest coefficient in this expansion is : [Sept 2020]

- a) 792
- b) 252
- c) 462
- d) 330

13) The function

$$f(x) = \begin{cases} \frac{\pi}{4} + \tan^{-1} x & \text{if } |x| \leq 1 \\ \frac{1}{2}(|x| - 1) & \text{if } |x| > 1 \end{cases} \quad [\text{Sept 2020}]$$

- a) both continuous and differentiable on  $\mathbb{R} - \{-1\}$
- b) continuous on  $\mathbb{R} - \{-1\}$  and differentiable on  $\mathbb{R} - \{-1, 1\}$
- c) continuous on  $\mathbb{R} - \{1\}$  and differentiable on  $\mathbb{R} - \{-1, 1\}$
- d) both continuous and differentiable on  $\mathbb{R} - \{1\}$

14) The solution of the differential equation  $\frac{dy}{dx} - \frac{y+3x}{\log_e y+3x} + 3 = 0$  is: where  $c$  is a constant of integration [Sept 2020]

- a)  $x - \log_e y + 3x = c$
- b)  $x - \frac{1}{2}(\log_e y + 3x^2) = c$
- c)  $x - 2 \log_e y + 3x = c$
- d)  $y + 3x - \frac{1}{2} \log_e x^2 = c$

15) Let  $\lambda \neq 0$  be in  $\mathbb{R}$ . If  $\alpha$  and  $\beta$  are the roots of the equation,  $x^2 - x + 2\lambda = 0$  and  $\alpha$  and  $\gamma$  are the roots of the equation,  $3x^2 - 10x + 27\lambda = 0$ , then  $\frac{\beta\gamma}{\lambda}$  is equal to: [Sept 2020]

- a) 27
- b) 9
- c) 18
- d) 36