

--Question Starting--

Match the following properties of groups with their corresponding algebraic implications:

1. Closure 2. Associativity 3. Existence of Identity 4. Existence of Inverses

A. For every a, b in G , $a \cdot b$ is in G

B. For all a, b, c in G , $(a \cdot b) \cdot c = a \cdot (b \cdot c)$

C. There exists e in G such that for all a in G , $a \cdot e = a$

D. For each a in G , there exists a^{-1} in G such that $a \cdot a^{-1} = e$

Choose the correct answer from the options given below:

(1) 1-A, 2-B, 3-C, 4-D

(2) 1-B, 2-A, 3-D, 4-C

(3) 1-A, 2-C, 3-B, 4-D

(4) 1-D, 2-B, 3-A, 4-C

Answer Key: 1

Solution:

? Closure (A): Ensures the operation stays within the set.

? Associativity (B): The grouping of operations does not affect the outcome.

? Identity (C): There is an element that leaves others unchanged under the operation.

? Inverses (D): Each element has a corresponding inverse that yields the identity when combined.

Hence, Option (1) is the right answer.

--Question Starting--

Match the following graph types with their defining properties:

1. Tree 2. Bipartite Graph 3. Complete Graph 4. Eulerian Path

A. A connected graph in which any two vertices are connected by exactly one path

B. A graph whose vertices can be divided into two disjoint sets such that every edge connects a vertex from one set to the other

C. A graph where every pair of vertices is connected by an edge

D. A trail that uses every edge exactly once and starts and ends at the same vertex

Choose the correct answer from the options given below:

(1) 1-A, 2-B, 3-C, 4-D

(2) 1-B, 2-A, 3-D, 4-C

(3) 1-A, 2-B, 3-C, 4-D

(4) 1-C, 2-D, 3-A, 4-B

Answer Key: 3

Solution:

? Tree (A): A minimal connected acyclic graph.

? Bipartite Graph (B): Vertices split into two sets with edges only between sets.

? Complete Graph (C): Every pair of vertices is connected.

? Eulerian Path (D): A trail covering all edges exactly once, returning to start if Eulerian circuit.

Hence, Option (3) is the right answer.