



Faculty of Science



Intermediate Code Generation

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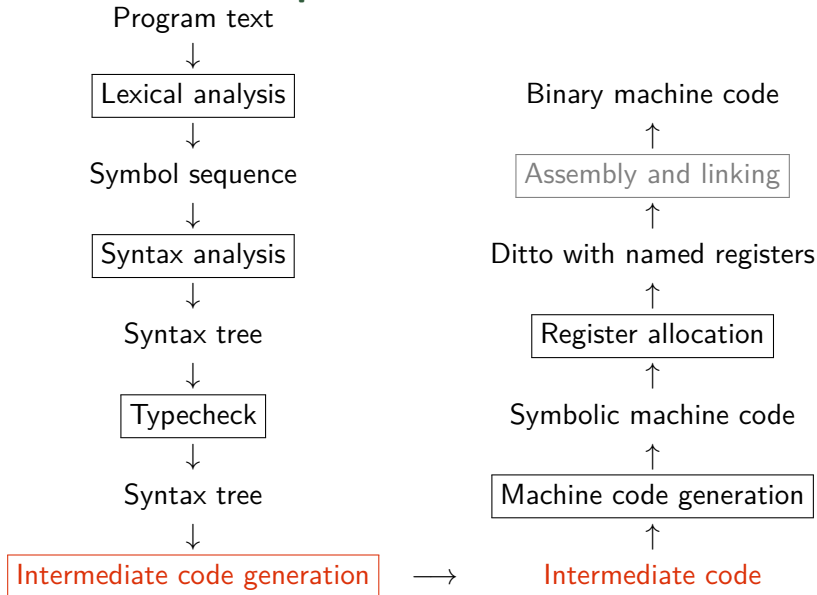
(based on Jost Berthold's slides, and with further tweaks by
Andrzej Filinski, `andrzej@di.ku.dk`)

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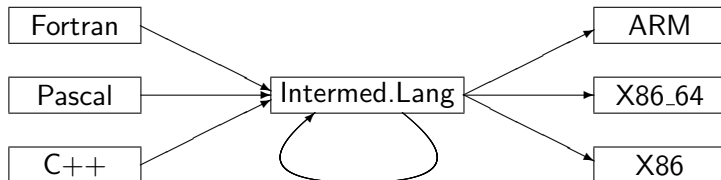
Structure of a Compiler



- 1 Why Intermediate Code?
 - Intermediate Language
 - To-Be-Translated Language
- 2 Syntax-Directed Translation
 - Arithmetic Expressions
 - Statements
 - Boolean Expressions, Sequential Evaluation
- 3 Translating More Complex Structures
 - More Control Structures
 - Arrays and Other Structured Data
 - Role of Declarations in the Translation

Why Intermediate Language (IL)?

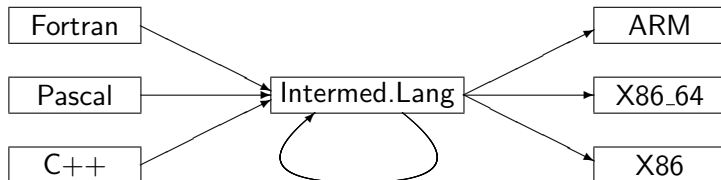
- Compilers for different platforms and languages can share parts.



- Without IL:** how many translators do I need to write to map n languages to m different architectures?

Why Intermediate Language (IL)?

- Compilers for different platforms and languages can share parts.



- Without IL:** how many translators do I need to write to map n languages to m different architectures?

Answer: $n \times m$ instead of $n + m$!

- Note:** IL and front-end(s) or back-end(s) may already exist!
 - E.g., LLVM, GCC [modern sense], JVM, .NET CLI, ...
- Machine-independent optimizations are possible.
- Also enables interpretation ...

Intermediate Language (IL)

- **Machine Independent:** unlimited number of registers and memory space, no machine-specific instructions.
- **Mid-level(s)** between source and machine languages (**tradeoff**): simpler constructs, easier to generate machine code.
- What features/constructs should IL support?
 - every translation loses information \Rightarrow use the information before losing it!
 - often a whole chain of ILs moving from higher towards lower level.
- How complex should IL's instruction be?
 - complex: good for interpretation (amortizes instruction-decoding overhead),
 - simple: can more easily generate optimal machine code.

Intermediate Language (IL)

Here: Low-level language,
but keeping functions
(procedures).

Small instructions:

- 3-address code: one
operation per expression

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$$\begin{aligned} Instrs &\rightarrow Instr, Instrs \mid Instr \\ Instr &\rightarrow \mathbf{id} := Atom \mid \mathbf{id} := \mathbf{unop} \ Atom \\ &\quad \mid \mathbf{id} := \mathbf{id} \mathbf{binop} \ Atom \end{aligned}$$

$$Atom \rightarrow \mathbf{id} \mid \mathbf{num}$$

Give examples of (in)valid programs/instructions.

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Intermediate Language (IL)

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Small instructions:

- **3-address code:** one operation per expression
- **Memory** read/write (**M**) (address already calc'd).
- **Jump** labels, **GOTO** and conditional jump (**IF**).

$$\begin{array}{ll}
 Instrs & \rightarrow Instr, Instrs \mid Instr \\
 Instr & \rightarrow id := Atom \mid id := unop\ Atom \\
 & \mid id := id\ binop\ Atom \\
 & \mid id := M[Atom] \mid M[Atom] := id \\
 & \mid LABEL\ label \mid GOTO\ label \\
 & \mid IF\ id\ relop\ Atom \\
 & \quad THEN\ label\ ELSE\ label
 \end{array}$$

$$Atom \rightarrow id \mid num$$

Give examples of (in)valid programs/instructions.

Intermediate Language (IL)

Here: Low-level language,
but keeping functions
(procedures).

Small instructions:

- 3-address code: one operation per expression
- Memory read/write (M) (address already calc'd).
- Jump labels, GOTO and conditional jump (IF).
- Function calls and returns

<i>Prg</i>	→	<i>Fcts</i>
<i>Fcts</i>	→	<i>Fct Fcts</i> <i>Fct</i>
<i>Fct</i>	→	<i>Hdr Bd</i>
<i>Hdr</i>	→	functionid (<i>Args</i>)
<i>Bd</i>	→	[<i>Instrs</i>]
<i>Instrs</i>	→	<i>Instr</i> , <i>Instrs</i> <i>Instr</i>
<i>Instr</i>	→	id := <i>Atom</i> id := unop <i>Atom</i> id := binop <i>Atom</i> id := <i>M</i> [<i>Atom</i>] <i>M</i> [<i>Atom</i>] := id LABEL <i>label</i> GOTO <i>label</i> IF id relop <i>Atom</i> THEN <i>label</i> ELSE <i>label</i> id := CALL functionid (<i>Args</i>) RETURN id
<i>Atom</i>	→	id num
<i>Args</i>	→	id , <i>Args</i> id

Give examples of (in)valid programs/instructions.

The To-Be-Translated Language

We shall translate a simple procedural language:

- Arithmetic expressions and function calls, boolean expressions,
- conditional branching (`if`),
- two loops constructs (`while-do` and `repeat-until`).
- (Will see details as we go.)

Syntax-directed translation:

- In practice we work on the abstract syntax tree `ABSYN` (but use concrete-syntax-like notation for readability, like for interpretation and typechecking),
- Implement each syntactic category via a translation function: Arithmetic expressions, Boolean expressions, Statements.
- Code for subtrees is generated independent of context, (i.e., context is a parameter to the translation function)

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Translating Arithmetic Expressions

Expressions in Source Language

- Variables and number literals,
- unary and binary operations,
- function calls (with argument list).

$$Exp \rightarrow \begin{array}{l} \text{num} \mid \text{id} \\ \mid \text{unop } Exp \\ \mid Exp \text{ binop } Exp \\ \mid \text{id}(Exps) \end{array}$$

$$Exps \rightarrow Exp \mid Exp , Exps$$

Translating Arithmetic Expressions

Expressions in Source Language

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$$Exps \rightarrow Exp \mid Exp , Exps$$

Translation function:

$Trans_{Exp} : Exp * VTable * FTable * Location \rightarrow Instrs$

- Returns a list of intermediate code instructions *Instrs* that ...
- ... upon execution, computes *Exp*'s result in IL variable *Location*.
- (Recursive) **case analysis** on *Exp*'s abstract syntax tree **ABSYN**.
 - "Syntax-directed translation"

Symbol Tables and Helper Functions

Translation function:

$$Trans_{Exp} : Exp * VTable * FTable * Location \rightarrow Instrs$$

Symbol Tables for codegen phase

vtable : maps each variable name in source language to its corresponding IL variable name (symbolic register).

ftable : source function names to IL function labels (for `call`)

Helper Functions

- *lookup*: retrieve entry from a symbol table
- *getvalue*: retrieve value of source language literal
- *getname*: retrieve name of source language variable/operation
- *newvar*: make new intermediate code variable (side-effectful!)
- *newlabel*: make new label (for jumps in intermediate code)
- *trans_op*: translates an operator name to the name in IL.

Generating Code for an Expression

$\text{Trans}_{\text{Exp}}: \text{Exp} * \text{VTable} * \text{FTable} * \text{Location} \rightarrow \text{Instrs}$

$\text{Trans}_{\text{Exp}}(\text{exp}, \text{vtable}, \text{ftable}, \text{place}) = \text{case exp of}$

num	$v = \text{getvalue}(\text{num})$ $[\text{place} := v]$
id	$x = \text{lookup}(\text{vtable}, \text{getname}(\text{id}))$ <i>// Can assume that source program has already been type-checked</i> $[\text{place} := x]$
unop Exp_1	$\text{place}_1 = \text{newvar}()$ $\text{code}_1 = \text{Trans}_{\text{Exp}}(\text{Exp}_1, \text{vtable}, \text{ftable}, \text{place}_1)$ $\text{op} = \text{trans_op}(\text{getname}(\text{unop}))$ $\text{code}_1 @ [\text{place} := \text{op } \text{place}_1]$
Exp_1 binop Exp_2	$\text{place}_1 = \text{newvar}()$ $\text{place}_2 = \text{newvar}()$ $\text{code}_1 = \text{Trans}_{\text{Exp}}(\text{Exp}_1, \text{vtable}, \text{ftable}, \text{place}_1)$ $\text{code}_2 = \text{Trans}_{\text{Exp}}(\text{Exp}_2, \text{vtable}, \text{ftable}, \text{place}_2)$ $\text{op} = \text{trans_op}(\text{getname}(\text{binop}))$ $\text{code}_1 @ \text{code}_2 @ [\text{place} := \text{place}_1 \text{ op } \text{place}_2]$

Generating Code for a Function Call

$Trans_{Exp}(exp, vtable, ftable, place) = \text{case } exp \text{ of}$

$id(Exps)$	$(code_1, [a_1, \dots, a_n]) = Trans_{Exps}(Exps, vtable, ftable)$ $fname = \text{lookup}(ftable, \text{getname}(id))$ $code_1 @ [place := CALL\ fname(a_1, \dots, a_n)]$
------------	---

$Trans_{Exps}$ returns the code that evaluates the function's parameters, and the list of new-intermediate variables (that hold the results).

$Trans_{Exps} : Exps * VTable * FTable \rightarrow Instrs * Args$

$Trans_{Exps}(exps, vtable, ftable) = \text{case } exps \text{ of}$

Exp	$place = \text{newvar}()$ $code_1 = Trans_{Exp}(Exp, vtable, ftable, place)$ $(code_1, [place])$
-------	--

$Exp, Exps$	$place = \text{newvar}()$ $code_1 = Trans_{Exp}(Exp, vtable, ftable, place)$ $(code_2, args) = Trans_{Exps}(Exps, vtable, ftable)$ $code_3 = code_1 @ code_2$ $args_1 = place :: args$ $(code_3, args_1)$
-------------	--

Translation Example

Assume the following symbol tables:

- $vtable = [x \mapsto v_0, y \mapsto v_1, z \mapsto v_2]$
- $ftable = [f \mapsto _F_1]$

Translation of Exp with $place = t_0$:

- $Exp = x - 3$

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$t_1 := v_0$
 $t_2 := 3$
 $t_0 := t_1 - t_2$

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Assume the following symbol tables:

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- $f table = [f \mapsto _F_1]$

Translation of Exp with $place = t_0$:

- $Exp = x - 3$

$$\begin{aligned} t_1 &:= v_0 \\ t_2 &:= 3 \\ t_0 &:= t_1 - t_2 \end{aligned}$$

Note: generated IL code **need not** be “optimal”; may get improved by later optimization and/or machine-code generation phases.

- $Exp = 3 + f(x - y, z)$

- **Hint:** When hand-translating, it's often convenient to write out the generated IL code from the bottom up.

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Assume the following symbol tables:

- $vtable = [x \mapsto v_0, y \mapsto v_1, z \mapsto v_2]$
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Translation of Exp with $place = t_0$:

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- $Exp = 3 + f(x - y, z)$

$$\begin{aligned} t_1 &:= 3 \\ t_4 &:= v_0 \\ t_5 &:= v_1 \\ t_3 &:= t_4 - t_5 \\ t_6 &:= v_2 \\ t_2 &:= \text{CALL } _F_1(t_3, t_6) \\ t_0 &:= t_1 + t_2 \end{aligned}$$

- **Hint:** When hand-translating, it's often convenient to write out the generated IL code from the bottom up.

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- **Statements**
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Translating Statements

Statements in Source Lang.

- Sequence of statements
- Assignment
- Conditional Branching
- Loops: while and repeat (simple conditions for now)

<i>Stat</i>	→	<i>Stat</i> ; <i>Stat</i> id := <i>Exp</i> if <i>Cond</i> then { <i>Stat</i> } if <i>Cond</i> then { <i>Stat</i> } else { <i>Stat</i> } while <i>Cond</i> do { <i>Stat</i> } repeat { <i>Stat</i> } until <i>Cond</i>
<i>Cond</i>	→	<i>Exp</i> relop <i>Exp</i>

We assume relational operators translate directly (using `trans_op`).

Translating Statements

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$$\begin{array}{lcl}
 \text{Stat} & \rightarrow & \begin{array}{l} \text{Stat} ; \text{Stat} \\ \text{id} := \text{Exp} \\ \text{if } \text{Cond} \text{ then } \{ \text{Stat} \} \\ \text{if } \text{Cond} \text{ then } \{ \text{Stat} \} \text{ else } \{ \text{Stat} \} \\ \text{while } \text{Cond} \text{ do } \{ \text{Stat} \} \\ \text{repeat } \{ \text{Stat} \} \text{ until } \text{Cond} \end{array} \\
 \text{Cond} & \rightarrow & \text{Exp } \mathbf{relop} \text{ Exp}
 \end{array}$$

We assume relational operators translate directly (using `trans_op`).

Translation function:

$$\text{Trans}_{\text{Stat}} : \text{Stat} * \text{VTable} * \text{FTable} \rightarrow \text{Instrs}$$

- As before: syntax-directed, **case analysis** on *Stat*
- Intermediate code instructions for statements

Generating Code for Sequences, Assignments,...

$Trans_{Stat} : Stat * VTable * FTable \rightarrow Instrs$

$Trans_{Stat}(stat, vtable, ftable) = \text{case } stat \text{ of}$

$Stat_1 ; Stat_2$ $code_1 = Trans_{Stat}(Stat_1, vtable, ftable)$
 $code_2 = Trans_{Stat}(Stat_2, vtable, ftable)$
 $code_1 @ code_2$

$id := Exp$ $place = lookup(vtable, getname(id))$
 $Trans_{Exp}(Exp, vtable, ftable, place)$

// Book: introduces an extra temporary, in case of subtle aliasing between $place$ and Exp

... (rest coming soon)

- Sequence of statements, sequence of code.
- Symbol tables are inherited attributes.

Generating Code for Conditional Jumps: Helper

- Helper function for loops and branches
- Evaluates *Cond*, i.e., a boolean expression, then jumps to one of two labels, depending on result

$Trans_{Cond} : Cond * Label * Label * VTable * FTable \rightarrow Instrs$

$Trans_{Cond}(cond, label_t, label_f, vtable, ftable) = \text{case } cond \text{ of}$

Exp_1	relop	Exp_2	$t_1 = \text{newvar}()$ $t_2 = \text{newvar}()$ $code_1 = Trans_{Exp}(Exp_1, vtable, ftable, t_1)$ $code_2 = Trans_{Exp}(Exp_2, vtable, ftable, t_2)$ $op = \text{trans_op}(\text{getname}(\text{relop}))$ $code_1 \ @ \ code_2 \ @ \ [IF \ t_1 \ op \ t_2 \ THEN \ label_t \ ELSE \ label_f]$
---------	--------------	---------	--

- Uses the IF of the intermediate language
- Expressions need to be evaluated before
(restricted IF: only variables and atoms can be used)

Generating Code for If-Statements

- Generate **new labels** for branches and following code
- Translate **If** statement to a **conditional jump**

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- Translate If statement to a conditional jump

$Trans_{Stat}(stat, vtable, ftable) = \text{case } stat \text{ of}$

```

if Cond     $label_t = \text{newlabel}()$ 
then Stat1  $label_f = \text{newlabel}()$ 
             $code_c = Trans_{Cond}(Cond, label_t, label_f, vtable, ftable)$ 
             $code_s = Trans_{Stat}(Stat_1, vtable, ftable)$ 
             $code_c @ [LABEL\ label_t] @ code_s @ [LABEL\ label_f]$ 

```

// Machine-code generation for most architectures will usually eliminate the fall-through jump to $label_t$.

```

if Cond     $label_t = \text{newlabel}()$ 
then Stat1  $label_f = \text{newlabel}()$ 
else Stat2  $label_e = \text{newlabel}()$ 
             $code_c = Trans_{Cond}(Cond, label_t, label_f, vtable, ftable)$ 
             $code_1 = Trans_{Stat}(Stat_1, vtable, ftable)$ 
             $code_2 = Trans_{Stat}(Stat_2, vtable, ftable)$ 
             $code_c @ [LABEL\ label_t] @ code_1 @ [GOTO\ label_e]$ 
             $@ [LABEL\ label_f] @ code_2 @ [LABEL\ label_e]$ 

```

Generating Code for Loops

- `repeat-until` loop is the easy case:
Execute body, check condition, jump back if false.
- `while` loop needs check before body, one extra label needed.

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$Trans_{Stat}(stat, vtable, ftable) = \text{case } stat \text{ of}$

```
repeat Stat   $label_f = \text{newlabel}()$ 
until Cond   $label_t = \text{newlabel}()$ 
              $code_1 = Trans_{Stat}(Stat, vtable, ftable)$ 
              $code_2 = Trans_{Cond}(Cond, label_t, label_f, vtable, ftable)$ 
              $[LABEL\ label_f] @ code_1 @ code_2 @ [LABEL\ label_t]$ 
```

```
while Cond   $label_s = \text{newlabel}()$ 
do Stat      $label_t = \text{newlabel}()$ 
             $label_f = \text{newlabel}()$ 
             $code_1 = Trans_{Cond}(Cond, label_t, label_f, vtable, ftable)$ 
             $code_2 = Trans_{Stat}(Stat, vtable, ftable)$ 
             $[LABEL\ label_s] @ code_1$ 
               $@ [LABEL\ label_t] @ code_2 @ [GOTO\ label_s]$ 
               $@ [LABEL\ label_f]$ 
```

Translation Example

- Symbol table **vtable**: $[x \mapsto v_0, y \mapsto v_1, z \mapsto v_2]$
- Symbol table **ftable**: $[\text{getInt} \mapsto \text{libIO_getInt}]$

```
x := 3;  
y := getInt();  
z := 1;  
while y > 0 do  
  {y := y - 1;  
   z := z * x}
```

Note: using the simplified translation of assignments from earlier slide, \neq Book.

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```
v_0 := 3  
v_1 := CALL libIO_getInt()  
v_2 := 1
```

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Note: using the simplified translation of assignments from earlier slide, \neq Book.

```
v_0 := 3  
v_1 := CALL libIO_getInt()  
v_2 := 1  
  LABEL l_s  
    t_1 := v_1  
    t_2 := 0  
    IF t_1 > t_2 THEN l_t else l_f  
  LABEL l_t
```

```
    GOTO l_s  
  LABEL l_f
```

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v_0 := 3
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v_2 := 1
LABEL l_s
  t_1 := v_1
  t_2 := 0
  IF t_1 > t_2 THEN l_t else l_f
  LABEL l_t
    t_3 := v_1
    t_4 := 1
    v_1 := t_3 - t_4

GOTO l_s
LABEL l_f

```

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v_0 := 3
v_1 := CALL libIO_getInt()
v_2 := 1
LABEL l_s
  t_1 := v_1
  t_2 := 0
  IF t_1 > t_2 THEN l_t else l_f
  LABEL l_t
    t_3 := v_1
    t_4 := 1
    v_1 := t_3 - t_4
    t_5 := v_2
    t_6 := v_0
    v_2 := t_5 * t_6
  GOTO l_s
LABEL l_f
```

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More Complex Conditions, Boolean Expressions

Boolean Expressions as Conditions

- Arithmetic expressions (esp. integer variables) used as Boolean
- Logical operators (not, and, or)
- Boolean expressions used in arithmetics

$$\begin{array}{lcl} \textit{Cond} & \rightarrow & \textit{Exp} \textit{ relop } \textit{Exp} \\ & & | \textit{Exp} \\ & & | \text{not } \textit{Cond} \\ & & | \textit{Cond} \text{ and } \textit{Cond} \\ & & | \textit{Cond} \text{ or } \textit{Cond} \\ \textit{Exp} & \rightarrow & \dots \mid \textit{Cond} \end{array}$$

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 \text{Cond} & \rightarrow & \text{Exp relop Exp} \\
 & & | \text{Exp} \\
 & & | \text{not Cond} \\
 & & | \text{Cond and Cond} \\
 & & | \text{Cond or Cond} \\
 \\
 \text{Exp} & \rightarrow & \dots | \text{Cond}
 \end{array}$$

We extend the translation functions $Trans_{Exp}$ and $Trans_{Cond}$:

- Interpret numeric values as Boolean expressions:
0 treated as false, all other values as true.
- Conversely, truth values as arithmetic expressions:
false is 0, true is 1

Numbers and Boolean Values, Negation

Expressions as Boolean values, negation:

$\text{Trans}_{\text{Cond}} : \text{Cond} * \text{Label} * \text{Label} * \text{VTable} * \text{FTable} \rightarrow \text{Instrs}$

$\text{Trans}_{\text{Cond}}(\text{cond}, \text{label}_t, \text{label}_f, \text{vtable}, \text{ftable}) = \text{case cond of}$

...

$\text{Exp} \quad t = \text{newvar}()$

$\text{code} = \text{Trans}_{\text{Exp}}(\text{Exp}, \text{vtable}, \text{ftable}, t)$

$\text{code} @ [\text{IF } t \neq 0 \text{ THEN } \text{label}_t \text{ ELSE } \text{label}_f]$

$\text{not Cond} \quad \text{Trans}_{\text{Cond}}(\text{Cond}, \text{label}_f, \text{label}_t, \text{vtable}, \text{ftable})$

...

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$\text{Exp} \quad t = \text{newvar}()$
 $\text{code} = \text{Trans}_{\text{Exp}}(\text{Exp}, \text{vtable}, \text{ftable}, t)$
 $\text{code} @ [\text{IF } t \neq 0 \text{ THEN } \text{label}_t \text{ ELSE } \text{label}_f]$

$\text{not Cond} \quad \text{Trans}_{\text{Cond}}(\text{Cond}, \text{label}_f, \text{label}_t, \text{vtable}, \text{ftable})$

...

Conversion of Boolean values to numbers (by jumps):

$\text{Trans}_{\text{Exp}} : \text{Exp} * \text{VTable} * \text{FTable} * \text{Location} \rightarrow \text{Instr}$

$\text{Trans}_{\text{Exp}}(\text{exp}, \text{vtable}, \text{ftable}, \text{place}) = \text{case exp of}$

...

$\text{Cond} \quad \text{label}_1 = \text{newlabel}()$
 $\text{label}_2 = \text{newlabel}()$
 $t = \text{newvar}()$
 $\text{code} = \text{Trans}_{\text{Cond}}(\text{Cond}, \text{label}_1, \text{label}_2, \text{vtable}, \text{ftable})$
 $[t := 0] @ \text{code} @ [\text{LABEL } \text{label}_1, t := 1] @ [\text{LABEL } \text{label}_2, \text{place} := t]$

// Book: stores result directly into final destination, not via t: *unsafe* with simplified trans. of assignments.

Sequential Evaluation of Conditions

Short-circuiting conjunction and disjunction may look like ordinary (infix) functions, but they are not!

Microsoft (R) F# Interactive version 12.4.0.0 for F# 7.0

```
> (+);;  
val it : (int -> int -> int) = <fun:it@1>  
> (&&);;  
val it : (bool -> bool -> bool) = <fun:it@2-1>  
  
> (+) 3 4;;  
val it : int = 7  
> (&&) false (failwith "oops");;  
val it : bool = false  
  
> let myplus = (+) in myplus 3 4;;  
val it : int = 7  
> let myand = (&&) in myand false (failwith "oops");;  
System.Exception: oops  
...
```

Need to treat them specially in compiler.

Sequential Evaluation by “Jumping Code”

$\text{Trans}_{\text{Cond}} : \text{Cond} * \text{Label} * \text{Label} * \text{VTable} * \text{FTable} \rightarrow \text{Instrs}$

$\text{Trans}_{\text{Cond}}(\text{cond}, \text{label}_t, \text{label}_f, \text{vtable}, \text{ftable}) = \text{case cond of}$

...

Cond_1	$\text{label}_{\text{next}} = \text{newlabel}()$
and	$\text{code}_1 = \text{Trans}_{\text{Cond}}(\text{Cond}_1, \text{label}_{\text{next}}, \text{label}_f, \text{vtable}, \text{ftable})$
Cond_2	$\text{code}_2 = \text{Trans}_{\text{Cond}}(\text{Cond}_2, \text{label}_t, \text{label}_f, \text{vtable}, \text{ftable})$
	$\text{code}_1 @ [\text{LABEL } \text{label}_{\text{next}}] @ \text{code}_2$

Cond_1	$\text{label}_{\text{next}} = \text{newlabel}()$
or	$\text{code}_1 = \text{Trans}_{\text{Cond}}(\text{Cond}_1, \text{label}_t, \text{label}_{\text{next}}, \text{vtable}, \text{ftable})$
Cond_2	$\text{code}_2 = \text{Trans}_{\text{Cond}}(\text{Cond}_2, \text{label}_t, \text{label}_f, \text{vtable}, \text{ftable})$
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Logics of and and or encoded by jumps.

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Translated like an arithmetic operation (bitwise and/or). Right results for **false** ~ 0 , **true** ~ 1 , but...

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 - Intermediate Language
 - To-Be-Translated Language
- 2 Syntax-Directed Translation
 - Arithmetic Expressions
 - Statements
 - Boolean Expressions, Sequential Evaluation
- 3 Translating More Complex Structures
 - More Control Structures
 - Arrays and Other Structured Data
 - Role of Declarations in the Translation

More Control Structures

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- A while-loop is enough

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 $Alts \rightarrow num : Stat \mid num : Stat, Alts$
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 - When “falling through” (e.g., C, Java): **if-then-else** and **goto**.

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(parameters to translation function $Trans_{Stat}$)

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considered harmful (Dijkstra 1968)

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Translating Arrays (of `int` elements)

Extending the Source Language

- Array elements used as an expression
- Assignment to an array element
- Array elements accessed by an index (expression)

$Exp \rightarrow \dots \mid Idx$

$Stat \rightarrow \dots \mid Idx := Exp$

$Idx \rightarrow \mathbf{id} [Exp]$

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- Array elements accessed by an index (expression)

$$\begin{array}{ll} \text{Exp} & \rightarrow \dots \mid \text{Idx} \\ \text{Stat} & \rightarrow \dots \mid \text{Idx} := \text{Exp} \\ \text{Idx} & \rightarrow \mathbf{id} [\text{Exp}] \end{array}$$

Again we *extend* $\text{Trans}_{\text{Exp}}$ and $\text{Trans}_{\text{Stat}}$.

- Arrays stored in pre-allocated memory area, generated code will use memory access instructions.
- Static (compile-time) or dynamic (run-time) allocation possible.

Generating Code for Address Calculation

- *vtable* entry for *id* contains the *base address of the array*.
- Elements are `int` here, so 4 bytes per element for address.

$Trans_{Idx} : Idx * VTable * FTable \rightarrow Instrs * Location$

$Trans_{Idx}(index, vtable, ftable) = \text{case } index \text{ of}$

```

id[Exp]  base = lookup(vtable, getname(id))
         addr = newvar()
         code1 = TransExp(Exp, vtable, ftable, addr)
         code2 = code1 @ [addr := addr*4, addr := addr+base]
         (code2, addr)

```

// Unless C-like language, should also generate code to check that index value is within array bounds!

Returns:

- Code to calculate the absolute address ...
- of the array element *in memory* (corresponding to `index`), ...
- ... and a new variable (*addr*) containing that address.

Generating Code for Array Access

Address-calculation code: in expression and statement translation.

- Read access inside expressions:

$Trans_{Exp}(exp, vtable, ftable, place) = \text{case } exp \text{ of}$

...

$Idx \quad (code_1, address) = Trans_{Idx}(Idx, vtable, ftable)$
 $code_1 @ [place := M[address]]$

- Write access in assignments:

$Trans_{Stat}(stat, vtable, ftable) = \text{case } stat \text{ of}$

...

$Idx := Exp \quad (code_1, address) = Trans_{Idx}(Index, vtable, ftable)$
 $t = newvar()$
 $code_2 = Trans_{Exp}(Exp, vtable, ftable, t)$
 $code_1 @ code_2 @ [M[address] := t]$

Multi-Dimensional Arrays

Arrays in Multiple Dimensions

- Only a small change to previous grammar: *Idx* can now be **recursive**.
- Needs to be mapped to an address in one dimension.

$$\begin{array}{ll} Exp & \rightarrow \dots \mid Idx \\ Stat & \rightarrow \dots \mid Idx := Exp \\ Idx & \rightarrow \mathbf{id}[Exp] \mid Idx[Exp] \end{array}$$

Multi-Dimensional Arrays

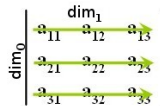
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$$\begin{array}{ll}
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 \end{array}$$

- Arrays stored in **row-major** or **column-major** order.

Standard: row-major, index of $a[k][l]$ is $k \cdot \text{dim}_1 + l$
 (Index of $b[k][l][m]$ is $k \cdot \text{dim}_1 \cdot \text{dim}_2 + l \cdot \text{dim}_2 + m$)



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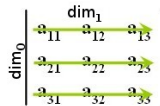
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- Address calculation **need to know sizes** in each dimension.
Symbol table: base address and list of array-dimension sizes.
- Need to change $Trans_{Idx}$, i.e., add recursive index calculation.

Address Calculation in Multiple Dimensions

$$Trans_{idx}(index, vtable, ftable) =$$

$$(code_1, t, base, []) = \text{Calc}_{idx}(index, vtable, ftable)$$
$$code_2 = code_1 @ [t := t * 4, t := t + base]$$
$$(code_2, t)$$

Address Calculation in Multiple Dimensions

$$\begin{array}{l}
 \text{Trans}_{\text{Idx}}(\text{index}, \text{vtable}, \text{fable}) = \\
 \hline
 (\text{code}_1, t, \text{base}, []) = \text{Calc}_{\text{Idx}}(\text{index}, \text{vtable}, \text{fable}) \\
 \text{code}_2 = \text{code}_1 @ [t := t * 4, t := t + \text{base}] \\
 \hline
 (\text{code}_2, t)
 \end{array}$$

Recursive index calculation, multiplies with dimension at each step.

$$\begin{array}{l}
 \text{Calc}_{\text{Idx}}(\text{index}, \text{vtable}, \text{fable}) = \text{case index of} \\
 \hline
 \text{id}[\text{Exp}] \quad (\text{base}, \text{dims}) = \text{lookup}(\text{vtable}, \text{getname}(\text{id})) \\
 \quad \text{addr} = \text{newvar}() \\
 \quad \text{code} = \text{Trans}_{\text{Exp}}(\text{Exp}, \text{vtable}, \text{fable}, \text{addr}) \\
 \quad (\text{code}, \text{addr}, \text{base}, \text{tail}(\text{dims})) \\
 \hline
 \text{Index}[\text{Exp}] \quad (\text{code}_1, \text{addr}, \text{base}, \text{dims}) = \text{Calc}_{\text{Idx}}(\text{Index}, \text{vtable}, \text{fable}) \\
 \quad d = \text{head}(\text{dims}) \\
 \quad t = \text{newvar}() \\
 \quad \text{code}_2 = \text{Trans}_{\text{Exp}}(\text{Exp}, \text{vtable}, \text{fable}, t) \\
 \quad \text{code}_3 = \text{code}_1 @ \text{code}_2 @ [\text{addr} := \text{addr} * d, \text{addr} := \text{addr} + t] \\
 \quad (\text{code}_3, \text{addr}, \text{base}, \text{tail}(\text{dims})) \\
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 \end{array}$$

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Declarations are necessary

- to allocate space for arrays,
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Declarations and scope

- Statements following a declarations can see declared data.
- Declaration of variables and arrays
- Here: Constant size, one dimension

$$\begin{array}{ll} Stat & \rightarrow Decl; Stat \\ Decl & \rightarrow \text{int } \mathbf{id} \\ & | \text{int } \mathbf{id}[\mathbf{num}] \end{array}$$

Function $Trans_{Decl} : Decl * VTable \rightarrow Instrs * VTable$

- translates declarations to code and new symbol table.

Translating Declarations to Scope and Allocation

Code with local scope (extended symbol table):

$$\begin{array}{l}
 \text{Trans}_{Stat}(stat, vtable, ftable) = \text{case } stat \text{ of} \\
 \hline
 Decl ; Stat_1 \quad (code_1, vtable_1) = \text{Trans}_{Decl}(Decl, vtable) \\
 \quad \quad \quad code_2 = \text{Trans}_{Stat}(Stat_1, vtable_1, ftable) \\
 \quad \quad \quad code_1 @ code_2 \\
 \hline
 \end{array}$$

Translating Declarations to Scope and Allocation

Code with local scope (extended symbol table):

$$\frac{\text{Trans}_{Stat}(stat, vtable, ftable) = \text{case } stat \text{ of}}{\begin{array}{l} Decl ; Stat_1 \quad (\text{code}_1, \text{vtable}_1) = \text{Trans}_{Decl}(Decl, vtable) \\ \text{code}_2 = \text{Trans}_{Stat}(Stat_1, \text{vtable}_1, ftable) \\ \text{code}_1 @ \text{code}_2 \end{array}}$$

Building the symbol table and allocating:

$\text{Trans}_{Decl} : Decl * VTable \rightarrow Instrs * VTable$

$\text{Trans}_{Decl}(decl, vtable) = \text{case } decl \text{ of}$

int id	$t_1 = \text{newvar}()$ $\text{vtable}_1 = \text{bind}(\text{vtable}, \text{getname}(\text{id}), t_1)$ $([], \text{vtable}_1)$
--------	--

int id[num]	$t_1 = \text{newvar}()$ $\text{vtable}_1 = \text{bind}(\text{vtable}, \text{getname}(\text{id}), t_1)$ $\text{size} = 4 * \text{getvalue}(\text{num}) \quad // \text{ compile-time calculation, cf. Book}$ $([t_1 := HP, HP := HP + \text{size}], \text{vtable}_1)$
-------------	--

... where HP is the IL variable containing the **heap pointer**, indicating the first free space in a managed heap at runtime; used for dynamic allocation.

Other Structures that Require Special Treatment

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- Records and Unions
 - Linear in memory. Field types and sizes can be different.
 - Field selector known at compile time: compute offset from base.

Coming up

- LAB today: Fasto's RiscV and CodeGen modules
- Wednesday (with Robert):
 - Machine-code generation from IL (with code-pattern selection)
- (Thursday: info meeting about 3rd-year BSc electives)
 - Aud. 1 (and 6, 8), HCØ, 16:15–18:00
 - See separate announcement
- Monday next week:
 - Optimizations in the Fasto compiler
- (Tuesday, May 23, 15–18: “Open house” at ITX exam house:)
 - **Register** and attend if you've never tried ITX at South Campus
 - See link on Absalon or in your study messages.