

23CHY115  
Lecture Notes

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# Chapter 1

## Young's Double Slit Experiment And Dirac Notation

In a traditional engineering curriculum, this course goes by the name of Materials Science And Engineering. The addition to the course is Computational Materials Science and AI/ML algorithms. The objective of the program is to have domain knowledge. The primary emphasis is on Materials Science And Engineering.

### Reference 1.0.1 Resources to look at for this course

Callister Jr. Rethwich

*Materials Science And Engineering.*

An Introduction (2018,10th Edition)

MIT 3.091 SC 3.091

The typical way this works is that engineers are given an objective, and materials engineering involves the usage of knowledge in choosing the right material to accomplish that objective in the most efficient way possible.

If you choose a particular material, you're choosing it because it has certain properties that will assist in the performance in the final product.

Structure is due to quantum mechanics(the realm of atoms)

In traditional engineering, we only deal with performance due to properties. The quantum mechanics involved is studied by physicists.

The reason traditional engineers do not need to know about the quantum mechanics underlying in the materials they use, is because they assume materials to be of a continuum. It is governed by calculus. It is deterministic.

Quantum mechanics is governed by probability. It is stochastic.

Thanks to advancements in computing and AI/ML, algorithms can be designed to create new materials and even predict the properties for these new materials.

## 1.1 Young's Double Slit Experiment

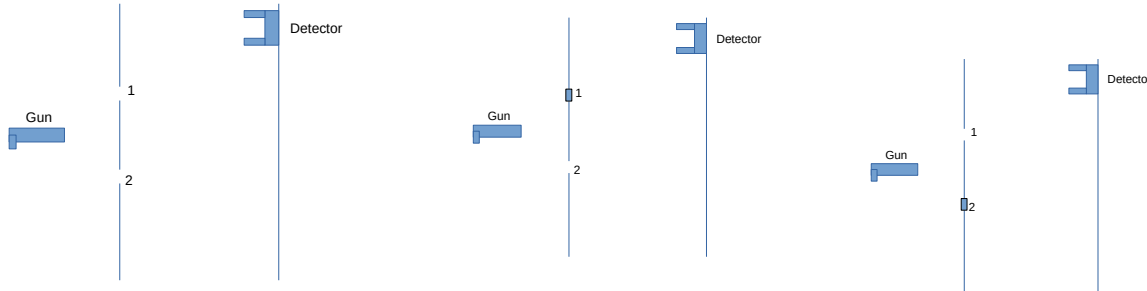
### 1.1.1 With Bullets

Here are a few details about this experiment:

- Bullets were shot to two screens, one screen with two slits.
- A detector is placed on the second screen.
- An analysis of the two screens, and the probability of the detector detecting a bullet in a given point on the second screen is performed.
- Another assumption is that the bullets are indestructible.
- When one of the slits are closed, it forms a wave, which has a local maxima at the slit which is not closed.

- When both slits are open, the maxima is at the centre of the second screen because the probability of both slits allowing the bullet to enter is twice when either one of those slits are closed.

$$P_{12} = P_1 + P_2$$



Let's say that slit one was closed, The probability as a function of the position of the detector would increase significantly.

### 1.1.2 With Water Waves

Here are a few details about this experiment:

- A tank of water is set up with the same setup of two screens, one screen having two slits.
- A detector is placed on the screen.
- An analysis of the two screens, and the probability of the detector detecting a bullet in a given point on the second screen is performed.
- Probability is measured in terms of interference, which leads to the wave curve.
- When one of the slits are closed, the probability distribution forms a wave with the local maxima situated where the slits are open.

$$I_1 = |h_1|^2$$

$$I_2 = |h_2|^2$$

- When both slits are open, the probability distribution forms this increasingly wavy graph as seen in the figure given below.

$$I_{12} = |h_1 + h_2|^2$$

$$I_{12} = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \delta$$

### 1.1.3 With Electrons

Here are a few details about this experiment:

- Replace the gun with an electron gun, which shoots electrons at a constant energy.
- It is assumed that the electrons will not pass through screen 1, unless it's through the two slits.
- The detector beeps when an electron hits it.
- 

$$P(z) = \frac{\text{no. of beeps at } z}{\text{Total no. of beeps}}$$

- When one slit is closed, the graph is the same as that of the bullets
- When both slits are open, The same graph as the wave graph was obtained.

$$P_{12} \neq P_1 + P_2$$

- On measuring the probabilities individually by adding a bulb that measures the slits, Add up the individual probabilities we get,

$$P'_{12} = P'_1 + P'_2$$

- It is impossible to arrange the light in such a way that one can tell which hole the electron went through, and at the same time not disturb the pattern.

## 1.2 Dirac Notation

State is denoted by  $|A\rangle$ , it encodes all the information about the particle. The measurement operator is denoted by  $\hat{A}$ . Going back to the electron gun experiment. Under the conjecture that the electrons are waves, The state of the entire system would be,  $|A_1\rangle + |A_2\rangle$ , before measurement. There are **two** measurements in the experiment, once with the light source and then with the detector. Let's take the measurement to be  $\hat{A}$ , which includes both the light source and the detector that beeps.

$$\hat{A}(|A_1\rangle + |A_2\rangle)$$

Taking an example, a 2d plane.  
Some vector

$$\underline{v} = v_1 \hat{e}_1 + v_2 \hat{e}_2$$

, where  $\hat{e}_1 \perp \hat{e}_2$

Take another orthogonal basis  $\hat{e}_1'$  and  $\hat{e}_2'$

Then,

$$\underline{v} = v'_1 \hat{e}_1' + v'_2 \hat{e}_2'$$

In linear algebra,

$$A\vec{x} = b$$

Consider a general vector  $\vec{w}$

In which,

$$A\vec{v} = \vec{w}$$

The vector is going to be denoted as  $|v\rangle$ , and  $\hat{O}$  as the operator.

$$\hat{O} |v\rangle = |w\rangle$$

To find how much of  $\vec{v}$  is in  $\vec{w}$ , we take the projection of v onto w.

$$|v\rangle = v_1 |\hat{e}_1\rangle + v_2 |\hat{e}_2\rangle$$

For the notation, when  $\langle v|$  is written, the basis is transformed to its complex conjugate.

$\langle v| = v_1^* \langle e_1| + v_2^* \langle e_2|$ , where  $v_1^*$  and  $v_2^*$  is the corresponding complex conjugate

Performing the dot product is denoted by

$$\langle v|w\rangle = (v_1^* \langle \hat{e}_1| + v_2^* \langle \hat{e}_2|)(w_1 |\hat{e}_1\rangle + w_2 |\hat{e}_2\rangle)$$

$$\langle \hat{e}_1|\hat{e}_2\rangle = 0$$

$$\langle \hat{e}_1|\hat{e}_1\rangle = 1$$

$$v_1^* w_1 + v_2^* w_2$$

**Reference 1.2.1 Leonard Susskind**

Leonard Susskind, a lecturer at Stanford. He delivered a lecture series called “The Theoretical Minimum”, on the minimum amount of knowledge required to understand the mechanisms behind physics.

Coming back to the core of what we’re trying to solve, about state and measurement.

$$\hat{O}\vec{v} = \vec{w}$$

We learned earlier this semester that there are some vectors, that transformations do not affect. (Eigenvectors and eigenvalues.)

Take two such vectors  $v_1$  and  $v_2$ ,

$$\hat{O}\vec{v}_1 = \lambda_1\vec{v}_1$$

$$\hat{O}\vec{v}_2 = \lambda_2\vec{v}_2$$

$$\hat{O}|v_1\rangle = \lambda_1|v_1\rangle$$

$$\hat{O}|v_2\rangle = \lambda_2|v_2\rangle$$

$$|v\rangle = v'_1|v^{(1)}\rangle + v'_2|v^{(2)}\rangle$$

Reminder, this is the equation we’re working in.

$$\hat{O}|v\rangle = |w\rangle$$

Recall the double slit experiment, Going back to the electron gun experiment The two slits  $A_1$  and  $A_2$  are denoted by  $|A_1\rangle$  and  $|A_2\rangle$ . Under the conjecture that the electrons are waves, The state of the entire system before measurement would be,

$$|A_1\rangle + |A_2\rangle$$

There are **two** measurements in the experiment, once with the light source and then with the detector. Let’s take the measurement to be  $\hat{A}$ , which includes both the light source and the detector that beeps.

$$\hat{A}(|A_1\rangle + |A_2\rangle) = \{|A_1\rangle, |A_2\rangle\}$$

It becomes apparent that  $|A_1\rangle$  and  $|A_2\rangle$  are eigenvectors. Taking the vector  $|\alpha\rangle$

$$|\alpha\rangle = |A_1\rangle + |A_2\rangle$$

The state of a system is analogous to the eigenvectors of the operator.

Then,

$$\hat{A}|\alpha\rangle = \{|A_1\rangle, |A_2\rangle\}$$

$$\begin{aligned}\hat{A}(|A_1\rangle + |A_2\rangle) &= \hat{A}|A_1\rangle + \hat{A}|A_2\rangle \\ &= a_1|A_1\rangle + a_2|A_2\rangle\end{aligned}$$

Remember that,

$$|\alpha\rangle = |A_1\rangle + |A_2\rangle$$

$$\langle\alpha| = \langle A_1| + \langle A_2|$$

$$\langle\alpha|A|\alpha\rangle$$

## 1.3 Atomic Mass

### Definition 1.1: Atomic Mass

The atomic mass of an atom can be defined as the sum of the masses of protons and electrons

### Definition 1.2: Isotopes

The number of protons is the same for all atoms of an element; The number of neutrons may vary. Thus, some elements will have two or more different atomic masses, known as isotopes

### Definition 1.3: Atomic Weight

The atomic weight of an element corresponds to the weighted average of the atomic masses of the atom's naturally occurring isotopes.

### Definition 1.4: Atomic mass unit

The atomic mass unit(amu) may be used to compute atomic weight. 1 amu is defined as  $\frac{1}{12}$  of the atomic mass of the most common isotope of carbon 12 ( $^{12}\text{C}$ )( $A = 12.00000$ )

With this scheme, the masses of protons and neutrons are slightly larger than unity, and

$$A \approx Z + N$$

$$\text{Weighted Average} = \frac{\sum wx}{\sum w} \quad (\text{w is the fraction of occurrence and x is the values given.})$$

# Chapter 2

## Coding

### 2.1 Metrics For Algorithms

$\frac{TP}{FN + TP} = \frac{TP}{P}$	Recall/Sensitivity/True Positive rate
$\frac{FP}{TN + FP} = \frac{FP}{N}$	False Positive Rate/False Alarm Rate
$\frac{TN}{TN + FP} = \frac{TN}{N} = 1 - (FPR)$	Specificity/True Negative Rate
$\frac{TP}{TP + FP}$	Precision
$\frac{FN}{FN + TP} = \frac{FN}{P}$	False Negative Rate
$\frac{TP + TN}{P + N} = \frac{TP + TN}{TP + TN + FP + FN}$	Accuracy

### 2.2 Confusion Matrix Function

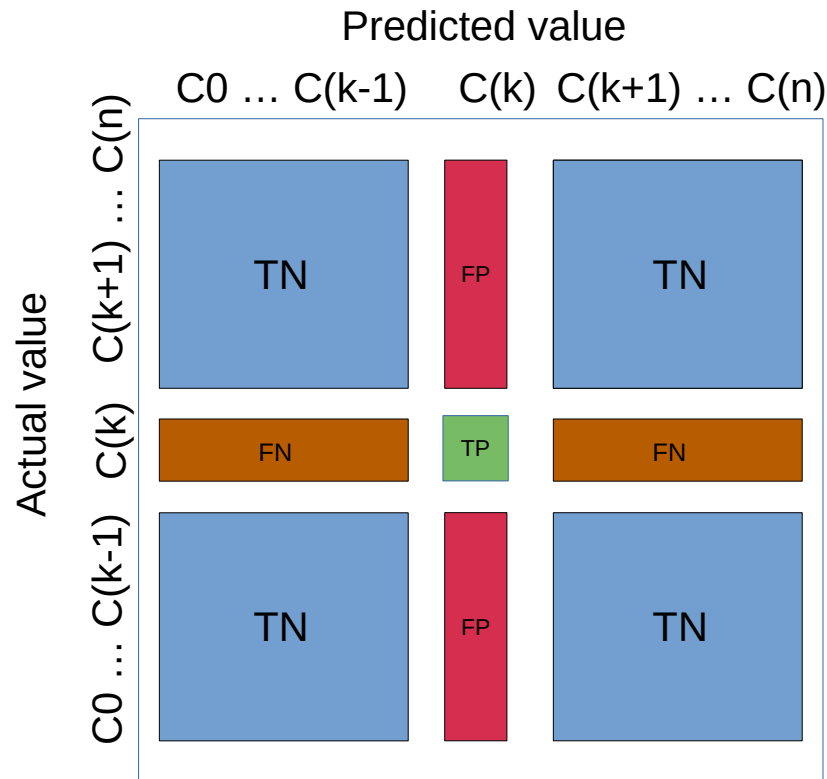
```
1 def confusion_matrix_binary(actual, predicted):
2     tp = fp = tn = fn = 0
3
4     for i in range(len(actual)):
5         if actual[i] == 1 and predicted[i] == 1:
6             tp += 1
7         elif actual[i] == 0 and predicted[i] == 1:
8             fp += 1
9         elif actual[i] == 0 and predicted[i] == 0:
10            tn += 1
11        elif actual[i] == 1 and predicted[i] == 0:
12            fn += 1
13    return tp, fp, tn, fn
```

#### Definition 2.1: F-Score

The F-score is the harmonic mean of Precision and Recall

$$F = 2 \times \frac{\text{Precision} \times \text{Recall}}{\text{Precision} + \text{Recall}}$$

$$\text{F1 Score} = \frac{TP}{TP + \frac{1}{2}(FP + FN)}$$



## 2.3 Micro Averaging

$$\text{Micro Precision} = \frac{NetTP}{NetTP + NetFP}$$

$$\text{Micro Recall} = \frac{NetTP}{NetTP + NetFN}$$

## 2.4 SciKitLearn Functions For Measuring Accuracy

```

1  import sklearn.metrics
2  accuracy_score = accuracy_score(y_true, y_pred) # returns accuracy
3  confusion_matrix(y_true, y_pred, normalize = all/pred/true/none) # returns confusion matrix
4  classification_report(y_true, y_pred, target_names = target_names) # returns classification
   report
5  f1_score(y_true, y_pred) # returns f1, f1-micro, f1-macro and f1-weighted

```



## 2.5 Numpy Functions

```
1 import numpy as np
2 a = np.array() # Returns a numpy matrix
3 a.ndim # Returns no. of dimensions
4 a.shape # Returns dimensions of a
5 a=np.random.random((m,n))# Returns random matrix
```