

# Linear Regression

# Linear regression

In linear regression, the equation that describes the feature-target relationships is  $Y=mX+C$  where  $X$  and  $Y$  are vectors that describe the feature and target variable respectively.

# Multiple Linear Regression

In a multiple linear regression case, we are interested in the impact of not only one, but many different features, on the target variable.

The equation can be written as  $Y = m_1X_1 + m_2X_2 + C$  where  $m_1$  and  $m_2$  are the coefficients of features  $X_1$  and  $X_2$  respectively.

# Polynomial Regression

For polynomial regression, we might use higher powers of  $X$  to describe  $Y$ , as described in

$$Y = m_1 X + m_2 X^2 + C$$

where  $m_1$  and  $m_2$  are coefficients of the first and second powers of the factor.

# Performance Metrics

**Mean Absolute Error (MAE)**

**Mean Squared Error (MSE)**

**Root Mean Squared Error (RMSE)**

**The coefficient of determination (R-squared )**

# Mean Absolute Error

**Mean Absolute Error (MAE)** is the mean of the absolute value of the errors. It is calculated as:

$$MAE = \frac{1}{n} \sum |y - \hat{y}|$$

Diagram illustrating the MAE formula components:

- $\frac{1}{n}$ : Divide by the total number of data points
- $\sum$ : Sum of
- $y$ : Actual output value
- $\hat{y}$ : Predicted output value
- $|y - \hat{y}|$ : The absolute value of the residual

# Mean Squared Error

**Mean Squared Error (MSE)** is the mean of the squared errors and is calculated as:

$$MSE = \frac{1}{n} \sum \left( \underbrace{y - \hat{y}}_{\substack{\text{The square of the difference} \\ \text{between actual and} \\ \text{predicted}}} \right)^2$$

# Root Mean Squared Error

**Root Mean Squared Error (RMSE)** is the square root of the mean of the squared errors:

$$\text{RMSE} = \sqrt{\frac{1}{n} \sum_{j=1}^n (y_j - \hat{y}_j)^2}$$



# R-squared

**R-squared** - The coefficient of determination

$$r = \frac{n(\sum xy) - (\sum x)(\sum y)}{\sqrt{[n\sum x^2 - (\sum x)^2][n\sum y^2 - (\sum y)^2]}}$$

x : Actual value

y: Predicted value