CS 106X Lecture 18: Trees

Wednesday, February 22, 2017

Programming Abstractions (Accelerated)
Winter 2017
Stanford University
Computer Science Department

Lecturer: Chris Gregg

reading:

Programming Abstractions in C++, Section 16.1





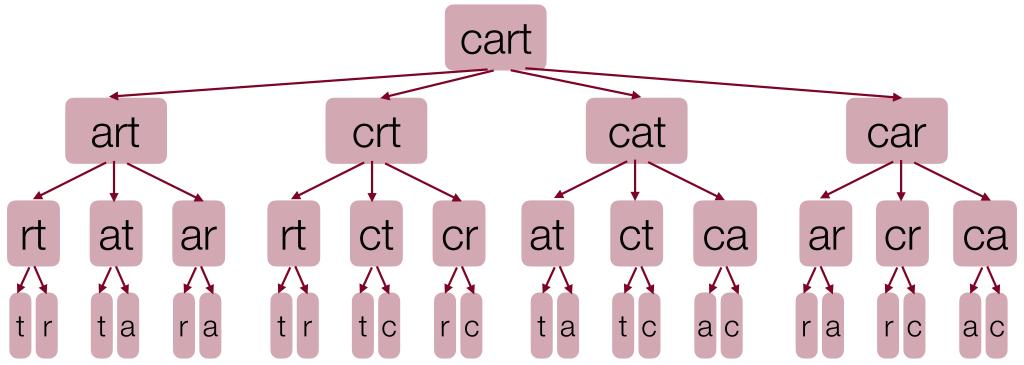
Today's Topics

- Logistics
- •Midterm Tomorrow!
- Midterm will cover up to and including Linked Lists
- •Introduction to Trees



Trees

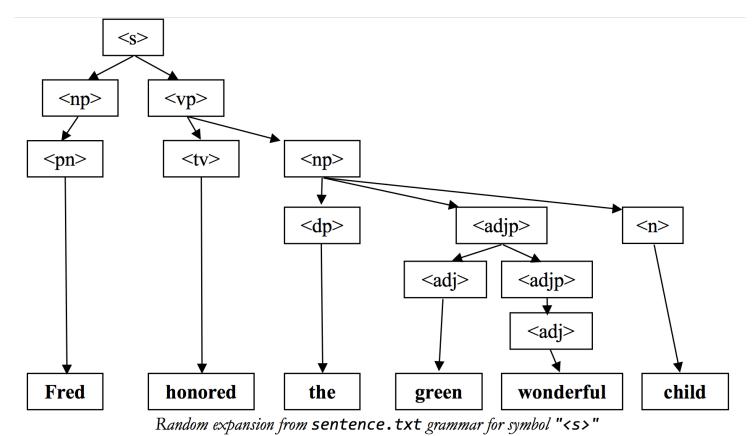
We have already seen trees in the class in the form of decision trees!





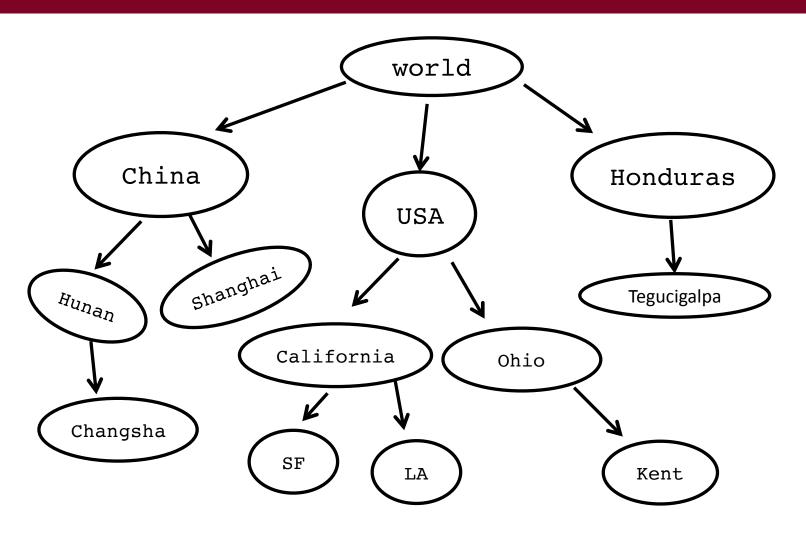
Trees

You've coded trees for recursive assignments!



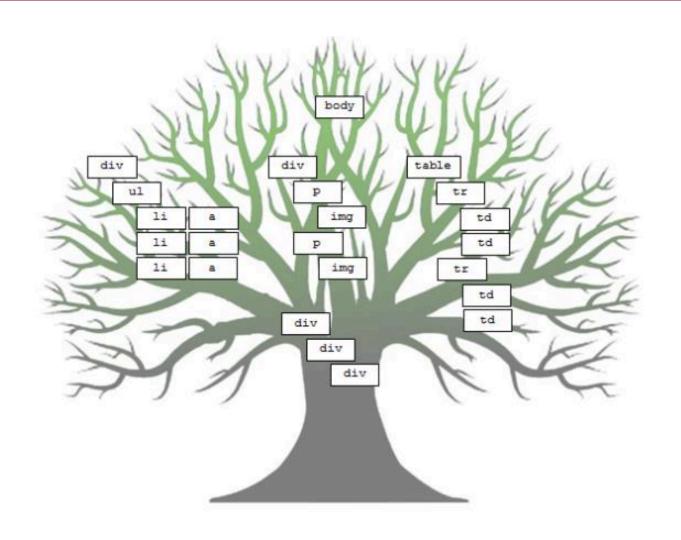


Trees Can Describe Hierarchies





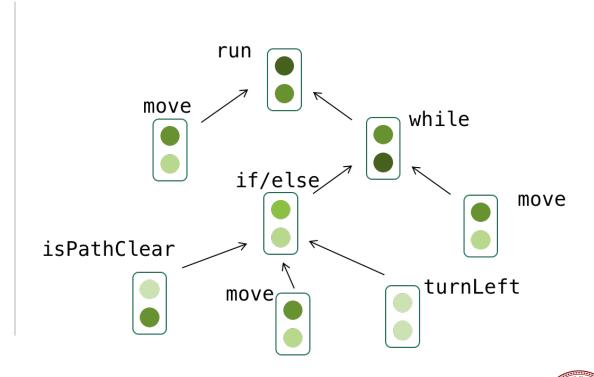
Trees Can Describe Websites (HTML)





Trees Can Describe Programs

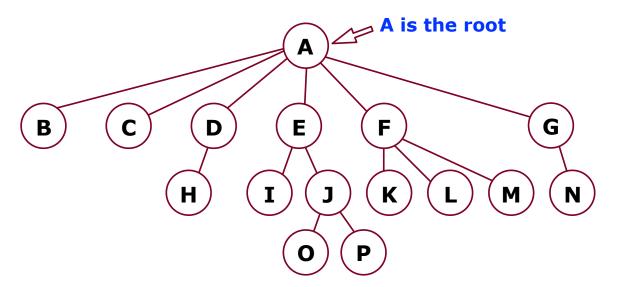
```
// Example student solution
function run() {
    // move then loop
    move();
    // the condition is fixed
    while (notFinished()) {
        if (isPathClear()) {
            move();
        } else {
            turnLeft();
        }
        // redundant
        move();
    }
}
```



* This is a figure in an academic paper written by a recent CS106 student!

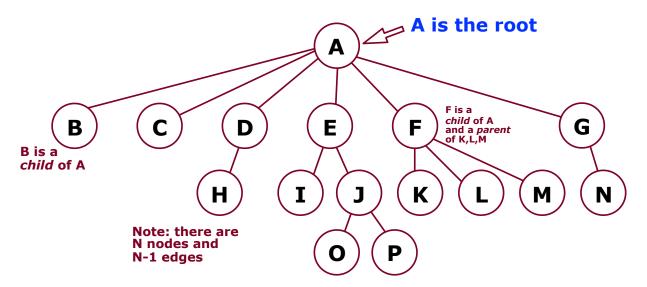
Trees are inherently recursive

What is a Tree (in Computer Science)?



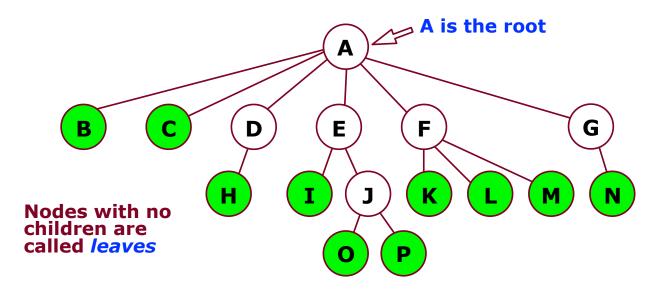


What is a Tree (in Computer Science)?



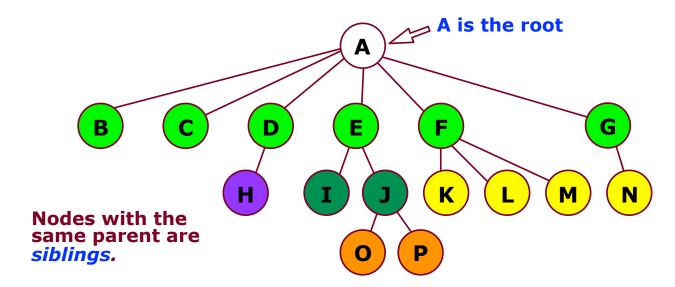


What is a Tree (in Computer Science)?

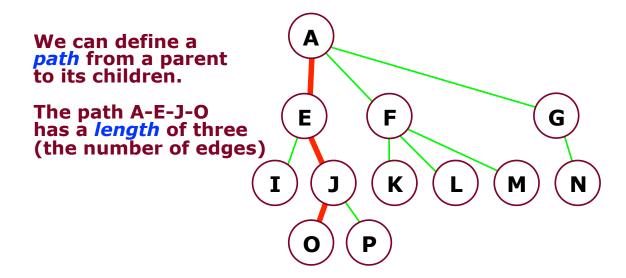




What is a Tree (in Computer Science)?



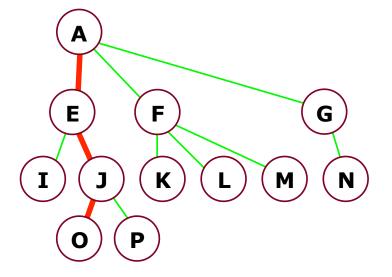






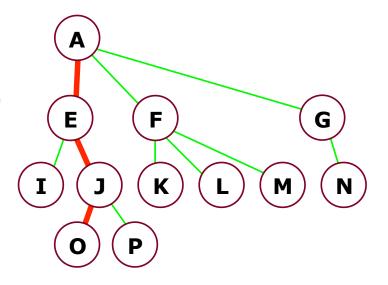
The *depth* of a node is the length from the root. The depth of node J is 2. The depth of the root is 0.

The *height* of a node is the longest path from the node to a leaf. The height of node F is 1. The height of all leaves is 0.





The height of a tree is the height of the root (in this case, the height of the tree is 3.





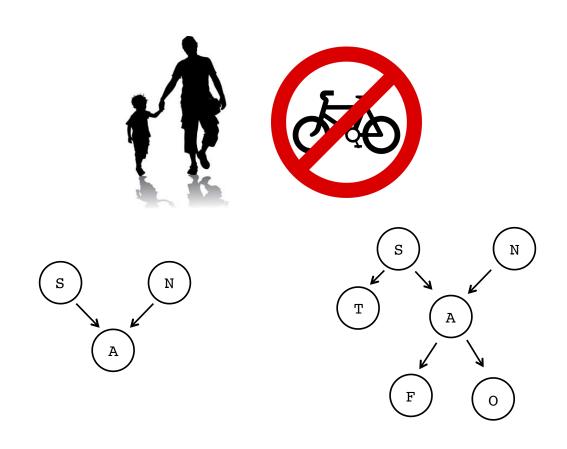
Trees can have only one parent, and cannot have cycles





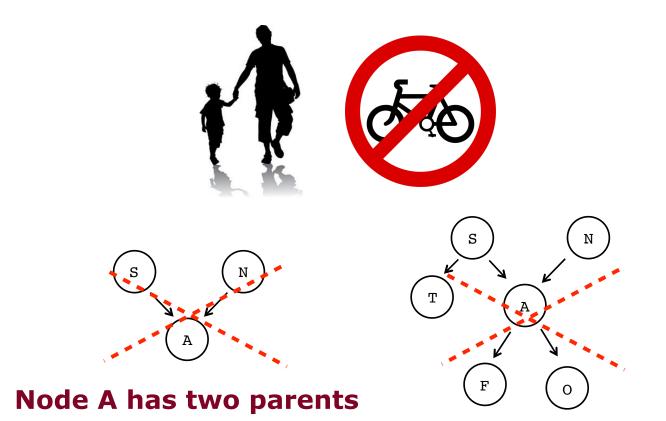


Trees can have only one parent, and cannot have cycles





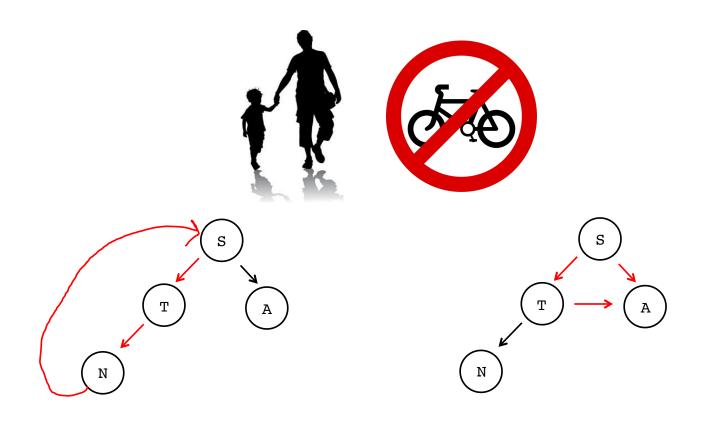
Trees can have only one parent, and cannot have cycles



Node A has two parents

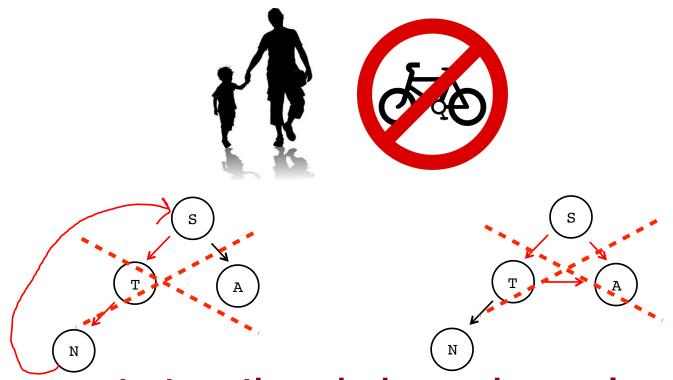


Trees can have only one parent, and cannot have cycles



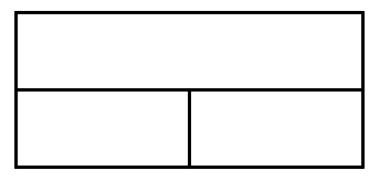


Trees can have only one parent, and cannot have cycles



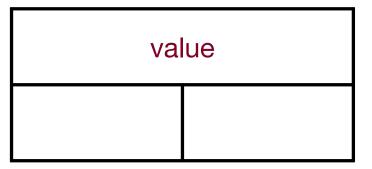








Binary Tree:





Binary Tree:

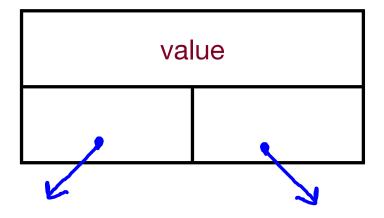
value

Linked List

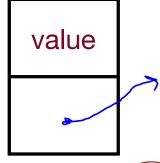
value



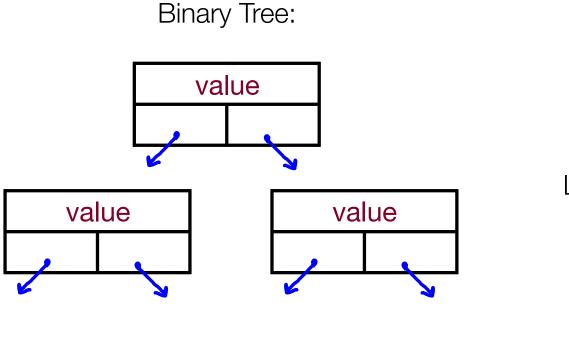
Binary Tree:

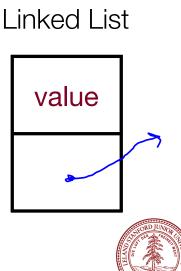


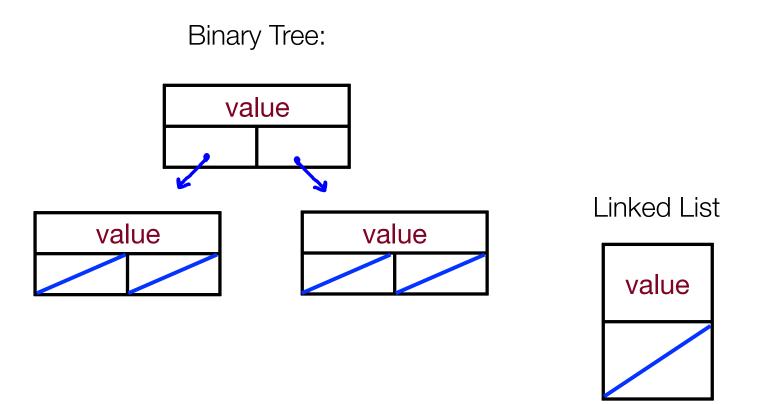
Linked List







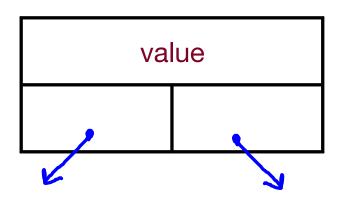




The Most Important Slide

Binary Tree:

```
struct Tree {
    string value;
    Tree *left;
    Tree *right;
};
```

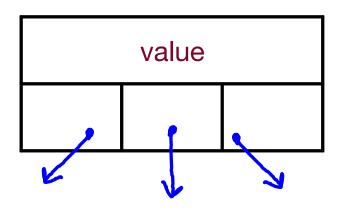




We Can Have Ternary Trees (or any number, n)

Ternary Tree:

```
struct Tree {
    string value;
    Tree *left;
    Tree *middle;
    Tree *right;
};
```

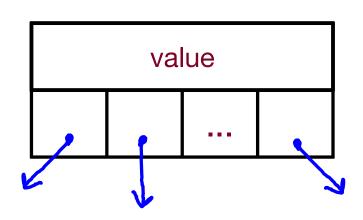




We Can Have Ternary Trees (or any number, n)

N-ary Tree:

```
struct Tree {
    string value;
    Vector<Tree *> children;
};
```





Trees can be defined as either structs or classes

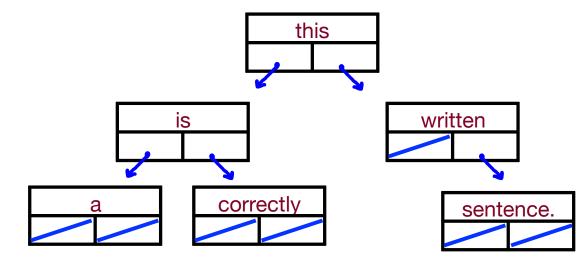
```
struct Tree {
   string value;
   Tree * left;
   Tree * right;
};
```

```
class Tree {
private:
    string value;
    Vector<Tree *> children;
};
```



```
struct Tree {
    string value;
    Tree * left;
    Tree * right;
};
```

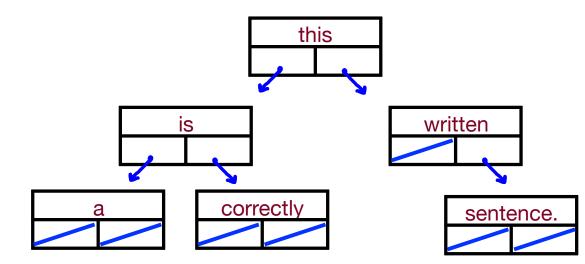
- 1.Pre-order
- 2.In-order
- 3.Post-order
- 4.Level-order





```
struct Tree {
    string value;
    Tree * left;
    Tree * right;
};
```

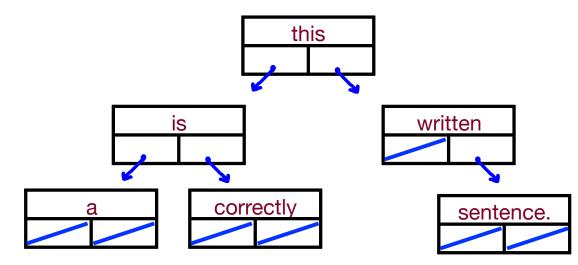
- 1.Pre-order
- 2.In-order
- 3.Post-order
- 4.Level-order
- 1.Do something
- 2.Go left
- 3.Go right





```
struct Tree {
    string value;
    Tree * left;
    Tree * right;
};
```

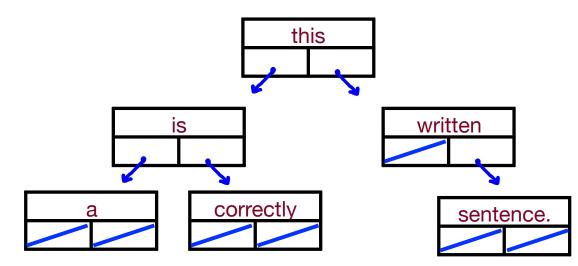
- 1.Pre-order
- 2.In-order
- 3.Post-order
- 4.Level-order
- 1.Go left
- 2.Do something
- 3.Go right





```
struct Tree {
    string value;
    Tree * left;
    Tree * right;
};
```

- 1.Pre-order
- 2.In-order
- 3.Post-order
- 4.Level-order
- 1.Go left
- 2.Go right
- 3.Do something

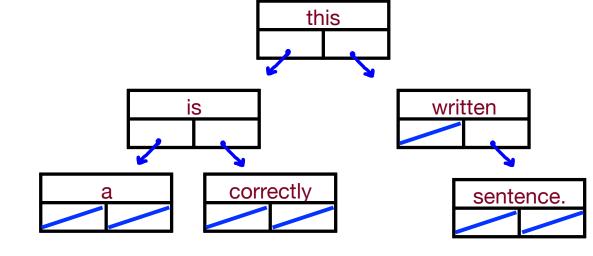




```
struct Tree {
    string value;
    Tree * left;
    Tree * right;
};
```

There are multiple ways to traverse the nodes in a binary tree:

- 1.Pre-order
- 2.In-order
- 3.Post-order
- 4.Level-order



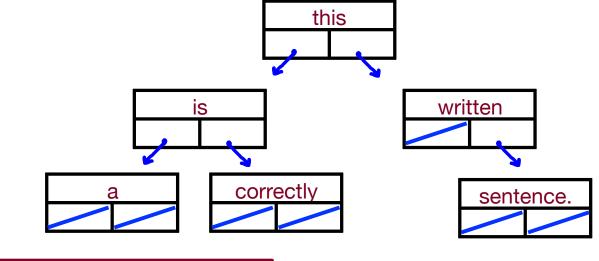
Hmm...can we do this recursively? We want to print the levels: 0, 1, 2 from left-to-right order



```
struct Tree {
    string value;
    Tree * left;
    Tree * right;
};
```

There are multiple ways to traverse the nodes in a binary tree:

- 1.Pre-order
- 2.In-order
- 3.Post-order
- 4.Level-order



Not easy recursively...let's use a queue!

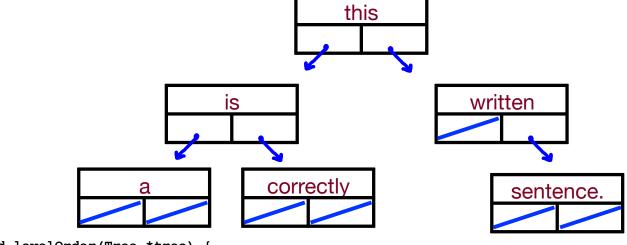
- 1. Enqueue root
- 2. While queue is not empty:
 - a. dequeue node
 - b. do something with node
 - c. enqueue left child of node if it exists
 - d. enqueue right child of node if it exists

should look familiar...word ladder?



Let's write some code

```
struct Tree {
   string value;
   Tree * left;
   Tree * right;
};
void preOrder(Tree * tree) {
  if(tree == NULL) return;
  cout<< tree->value <<" ";</pre>
  preOrder(tree->left);
  preOrder(tree->right);
void inOrder(Tree * tree) {
                                       void levelOrder(Tree *tree) {
  if(tree == NULL) return;
                                           Queue<Tree *>treeQueue;
  inOrder(tree->left);
  cout<< tree->value <<" ";</pre>
  inOrder(tree->right);
}
void postOrder(Tree * tree) {
  if(tree == NULL) return;
  postOrder(tree->left);
  postOrder(tree->right);
                                              }
  cout<< tree->value << " ";</pre>
                                          }
```



```
treeQueue.enqueue(tree);
while (!treeQueue.isEmpty()) {
    Tree *node = treeQueue.dequeue();
    cout << node->value << " ";</pre>
   if (node->left != NULL) {
        treeQueue.enqueue(node->left);
    if (node->right != NULL) {
        treeQueue.enqueue(node->right);
```



References and Advanced Reading

· References:

- https://en.wikipedia.org/wiki/Tree (data structure)
- •http://pages.cs.wisc.edu/~vernon/cs367/notes/8.TREES.html

Advanced Reading:

- •http://www.cs.cmu.edu/~adamchik/15-121/lectures/Trees/trees.html
- •Great set of tree-type questions:
 - •http://cslibrary.stanford.edu/110/BinaryTrees.html

