

Let's start by 9:05 PM

L56

Greedy Classical Problems - 1

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# RECAP

## Some classical greedy problems

# 1. Activity Selection Problem

$$1 \leq N \leq 2 \times 10^5$$

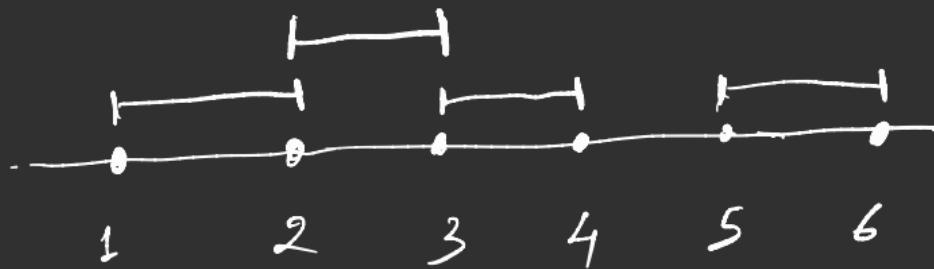
$$1 \leq S \leq E \leq 10^9$$

$N = 4$

start = [1, 3, 2, 5]

end = [2, 4, 3, 6]

ans = 3



## Intuition

- 1) Do the one that starts earlier first.
- 2) Do the one with the shortest duration first.
- 3) Do the one that ends earlier first.

1)  $\alpha$



2)  $\alpha$



3) ✓



## Solution

1) Sort by end time.

Let's  
implement

Remember the diamond problem?

1) Pick the lowest weight first  $\times$

$$w_1 = 2, v_1 = 1 \quad | \quad w_2 = 2, v_2 = 100$$

2) Pick the highest value first  $\times$

$$w_1 = 100, v_1 = 20 \quad | \quad w_2 = 1, v_2 = 99$$

3) Pick the highest  $v/w$  first  $\times$

$$\text{Cap} = 10 \quad | \quad w_1 = 2, v_1 = 80 \quad | \quad w_2 = 4, v_2 = 40 \quad | \quad w_3 = 5, v_3 = 45$$

cap = odd

v/w  $\rightarrow$  2

v=1

w=1

2 - 2 - 2 - 2 - --- - - -

0-1 Knapsack

Can't be solved using  
greedy (acc. to me)

## 2. Fractional Knapsack

# Intuition

# Solution

Let's implement

### 3.1 Job Scheduling to minimise lateness

We'll be given  $N$  jobs.

$T_i \Rightarrow$  Time taken to complete  $i^{\text{th}}$  job

$D_i \Rightarrow$  Deadline to complete  $i^{\text{th}}$  job.

We've to do all  $N$  jobs. We can do only 1 job at a time.

Minimize the maximum lateness among all the jobs.

Eg.

$N = 4$

$$T_2 = \left[ \begin{matrix} j_1 \\ j_2 \\ j_3 \\ j_4 \end{matrix}, \begin{matrix} 3 \\ 1 \\ 2 \\ 5 \end{matrix} \right]$$

$$D = [4, 10, 2, 8]$$

$j_3 \rightarrow j_1 \rightarrow j_2 \rightarrow j_4$

$$\boxed{\begin{matrix} 2, 5, 6, 11 \\ 0, 1, 0, 3 \end{matrix}}$$

$j_1 \rightarrow j_2 \rightarrow j_3 \rightarrow j_4$

$j_3 \rightarrow j_2 \rightarrow j_1 \rightarrow j_4$

$$f_1 \Rightarrow \boxed{\begin{matrix} 3, 4, 6, 11 \end{matrix}}$$

$$f_1 \Rightarrow \boxed{\begin{matrix} 0, 0, 4, 3 \end{matrix}}$$

$$f_1 \Rightarrow \boxed{\begin{matrix} 2, 3, 6, 11 \end{matrix}}$$

$$f_1 \Rightarrow \boxed{\begin{matrix} 0, 0, 2, 3 \end{matrix}}$$

$j_3 \rightarrow j_1 \rightarrow j_9 \rightarrow j_2$

$f \ni 2, 5, 10, 11$

$l_i \ni 0, 1, \underline{2}, 1$

ans = 2

Intuition  $(T_i)$

1.) Let's do the shortest job first

$$T_1 = 1, D = 10 \quad | \quad T_2 = 2, D = 2$$

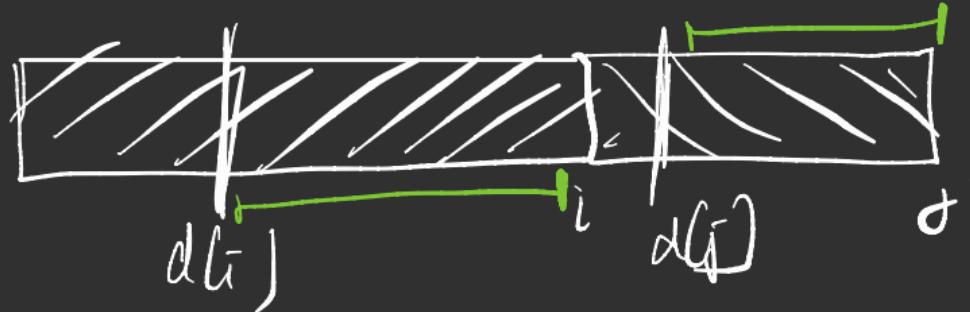
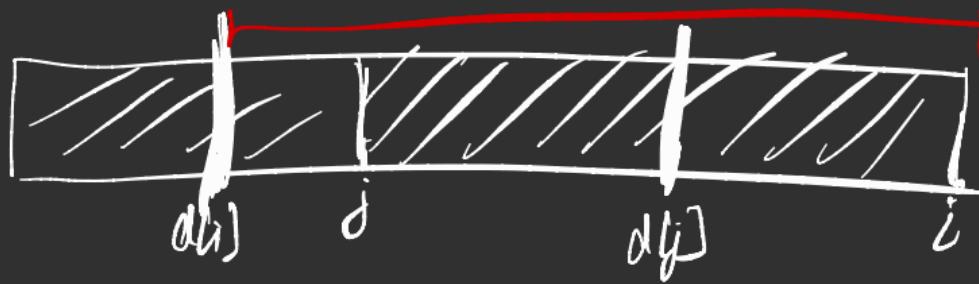
2.) Let's do tightest deadline ( $D_i$ ) first

3.) inc. order of slack time  $(D_i - T_j)$

$$T_1 = 1, D = 5 \quad | \quad T_2 = 8, D = 8$$

$Job_i$  &  $job_j$

deadline [ $i$ ] < deadline [ $j$ ]





task<sub>1</sub>  $\Rightarrow$  10am  $\Rightarrow$  8 hrs  $\Rightarrow$  6 PM

task<sub>2</sub>  $\Rightarrow$  6 PM  $\Rightarrow$  3 hrs  $\Rightarrow$  9 PM

task<sub>2</sub>  $\Rightarrow$  10am  $\Rightarrow$  3 hrs  $\Rightarrow$  1 PM

task<sub>1</sub>  $\Rightarrow$  1 PM  $\Rightarrow$  8 hrs  $\Rightarrow$  9 PM

## Solution

Earlier deadline first

Let's  
implement

# *Thank You!*

Reminder: Going to the gym & observing the trainer work out can help you know the right technique, but you'll muscle up only if you lift some weights yourself.

So, PRACTICE, PRACTICE, PRACTICE!