

Let's start at 9:02 PM

L30

Merge Sort and more

*If interested, check out the System Design course.
Early Bird discount is ON.*

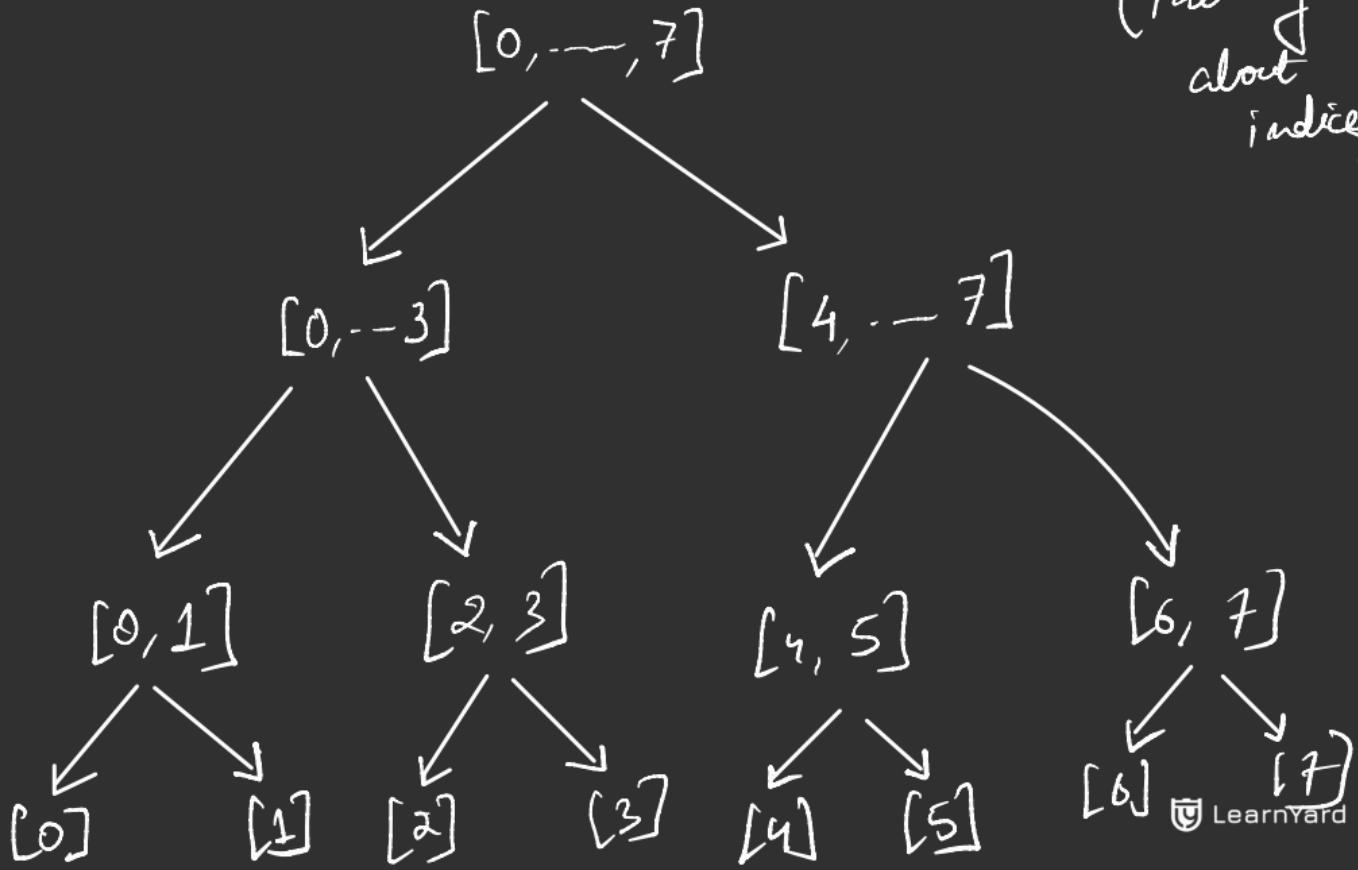
Join Discord - <https://bit.ly/ly-discord>

RECAP

Remember Insertion Sort?

Let's come to Merge Sort

(Talking
about
indices)



Merge 2 sorted Arrays

left = [1, 3, 5, 5]
ⁱ⁼⁴
_↓

right = [2, 6, 7]
^{j=3}
_↑

ans = [1, 2, 3, 5, 5, 6, 7]

pseudo-code

merge2sorted(—)

int[] ms(arr, n) {

if ($n = 2^1$)
return arr;

int[] left \Rightarrow equal to the first half of arr

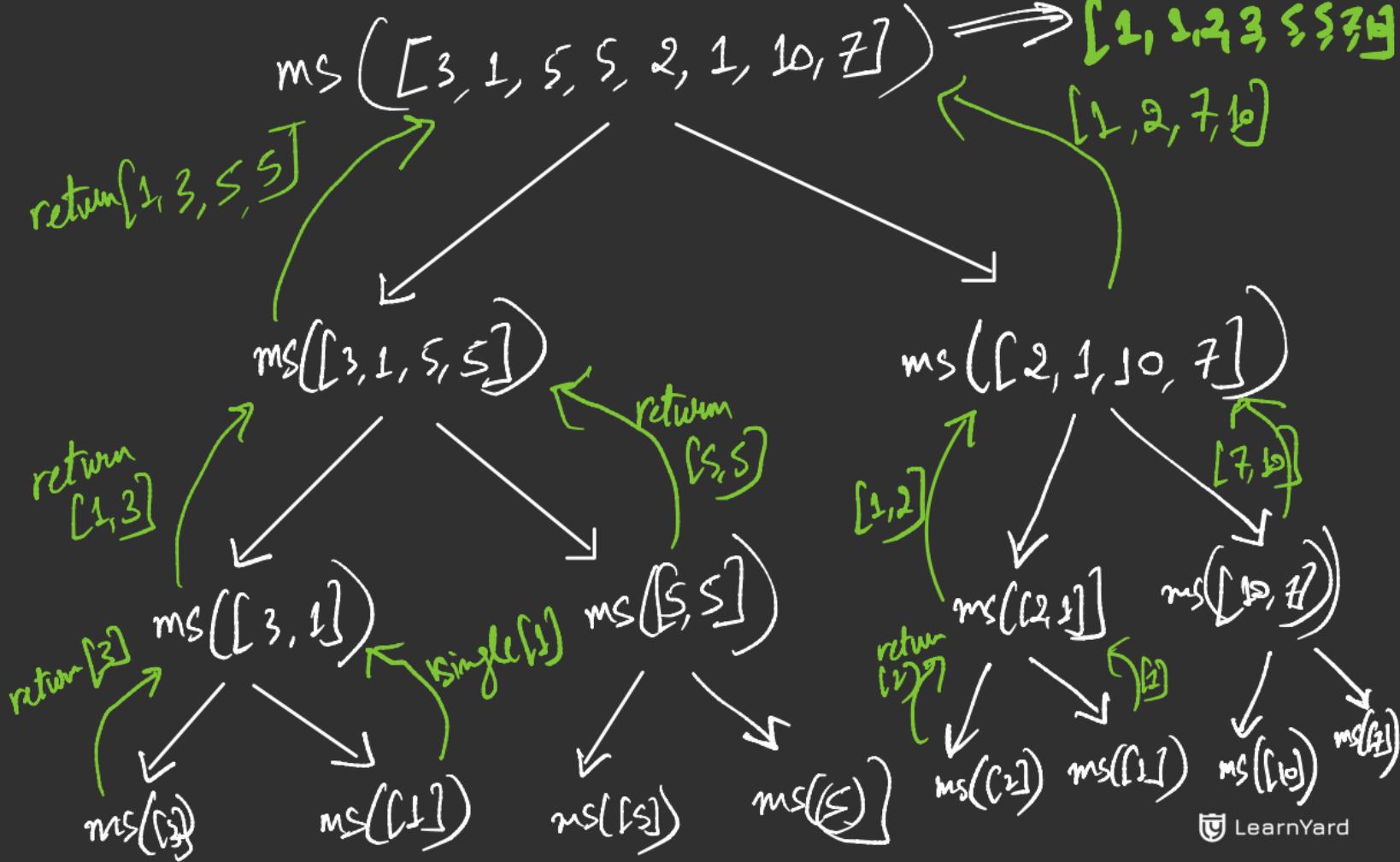
int[] right \Rightarrow equal to the second half of arr

left \leftarrow ms(left, size(left));

right \leftarrow ms(right, size(right));

return merge2sorted(left, right);

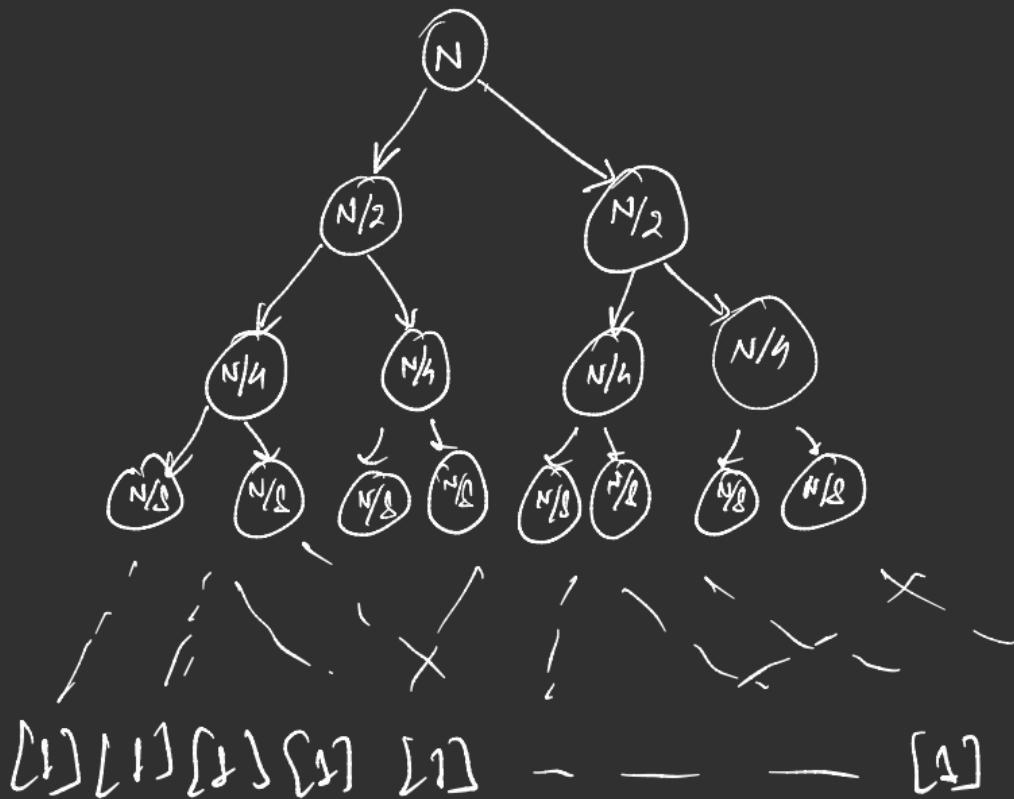
}



Let's Implement

Trying using
recursion
tree

Let's understand the time complexity



$$\left(\begin{array}{l} T(N) = 2 * T(N/2) + N \\ \\ 2 * T(N/2) = 4 * T(N/4) + N \\ \\ 4 * T(N/4) = 8 * T(N/8) + N \\ \\ \vdots \\ \\ K * T(2) = 2K * T(1) + N \end{array} \right)$$

$$T(N) = N + \underbrace{N + N + N + \dots}_{\log_2 N} = N$$

$$T(N) = O(N * \log N)$$

1. What is the total number of levels in the recursion tree while using merge sort on an array of 8 elements?

- A. 1
- B. 2
- C. 3
- D. 4

1. What is the total number of levels in the recursion tree while using merge sort on an array of 8 elements?

- A. 1
- B. 2
- C. 3
- D. 4

Solution :

[XXXXXXX] - Level 0

[XXX] - [XXX] - Level 1

[XX] - [XX] - [XX] - [XX] - Level 2

[X]-[X]-[X]-[X]-[X]-[X]-[X] - Level 3

2. What is the total number of nodes in the recursion tree while using merge sort on an array of 4 elements?

- A. 3
- B. 7
- C. 9
- D. 12

2. What is the total number of nodes in the recursion tree while using merge sort on an array of 4 elements?

- A. 3
- B. 7
- C. 9
- D. 12

Solution :

[XXXX] -> level 0 : nodes 1

[XX] - [XX] -> level 1 : nodes 2

[X]-[X]-[X]-[X] -> level 2 : nodes 4

Total Nodes = $1 + 2 + 4 = 7$

3. What is the auxiliary space complexity of the merge sort algorithm discussed?

- A. $O(1)$
- B. $O(n)$
- C. $O(n \log n)$
- D. $O(\log n)$

3. What is the auxiliary space complexity of the merge sort algorithm discussed?

- A. $O(1)$
- B. $O(n)$
- C. $O(n \log n)$
- D. $O(\log n)$

Solution : We need an array of length n to merge two arrays.

Let's understand space complexity

$$N + \frac{N}{2} + \frac{N}{4} - - -$$

$\log_2 N$

space $\Rightarrow O(N)$

4. Can we parallelly sort two partitions in merge sort to speed up the process? 

- A. False
- B. True

4. Can we parallelly sort two partitions in merge sort to speed up the process? 

- A. False
- B. True

Solution : Since two portions are independent of each other we can start sorting both the portions at the same instant to save time.

Let's solve 1 problem? xD

Given an array, find its inversion count.

$\{2, 4, 1, 3, 5\}$

$(2, 1)$ \Rightarrow 3
 $(4, 1)$
 $(4, 3)$

Implementation is homework.
(Codes will be shared in both C++ and Java)

Thank You!

Reminder: Going to the gym & observing the trainer work out can help you know the right technique, but you'll muscle up only if you lift some weights yourself.

So, PRACTICE, PRACTICE, PRACTICE!