

Let's start at 9:02PM

L65

Dynamic Programming : Mixed Problems 1

Join Discord - <https://bit.ly/ly-discord>

RECAP

Let's dive right into it

1. Make the Fence Great Again

$$N = 3$$

$$A = [2, 2, 3]$$

$$B = [4, 1, 5]$$

$$\Rightarrow [3, 2, 3]$$

\Downarrow

4

$$\Rightarrow [2, 4, 3]$$

$$1+1=2$$

$$N = 3$$

$$A = [2, 2, 2]$$

$$B = [3, 10, 6]$$



$$\begin{array}{ccc} [3, & 2, & 3] \\ \downarrow & & \downarrow \\ 3 & & 6 \end{array}$$

$$\text{ans} = 9$$

Intuition

$$\{a_i, a_{i+1}, a_{i+2}\}$$



a_{i-1}

a_i

a_{i+1}



A_i

A_{i-1}

A_i

A_{i+1}



$$\geq (a_i + 3)$$

5 5 5 \Rightarrow 5 6 5

5 5 6 \Rightarrow 5 7 6

6 5 7 \Rightarrow 6 5 7

9 5 8

$$a[i] \Rightarrow 0 \text{ cost}$$

$$a[i] + 1 \Rightarrow 1 \times b[i] \text{ cost}$$

$$a[i] + 2 \Rightarrow 2 \times b[i] \text{ cost}$$

$dp[i] = \text{ans for } a[i \dots n-1]$

$dp[i][j] \Rightarrow \text{ans for } a[i \dots n-1]$

o/1/2 given $a[i]$ is going to be incremented
exactly j times.

$$f(i, j)$$

$$\text{curCost} = j + b[i]$$

$$\begin{array}{l} // a[i] + j \\ (0/1/2) \end{array}$$

$$\underline{\text{future cost}} \leadsto f(i+1, 0) \Rightarrow a[i+1]$$

$$\leadsto f(i+1, 1) \Rightarrow a[i+1] + 1$$

$$\leadsto f(i+1, 2) \Rightarrow a[i+1] + 2$$

Solution

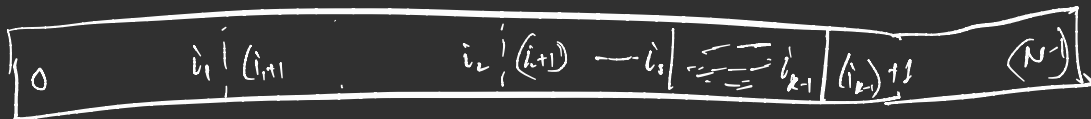
Let's implement

2. Beautiful Partitioning

0-based

$$i_1, i_2, i_3, \dots, i_{k-1}$$

$$i_1 < i_2 < i_3 < \dots < i_{k-1} < N-1$$



$$\text{pre}[i_1] > 0$$

$$\text{pre}[i_2] > \text{pre}[i_1]$$

$$\text{pre}[i_3] > \text{pre}[i_2]$$

⋮

$$\text{pre}[i_{k-1}] > \text{pre}[i_{k-2}]$$

$$\text{pre}[N-1] > \text{pre}[i_{k-1}]$$

$$0 < \boxed{\text{pre}[i_1] < \text{pre}[i_2] \dots \text{pre}[i_{k-2}] < \text{pre}[i_{k-1}]} < \text{pre}[N-1]$$

- 1) All $\text{pre}[i]$ values are positive.
- 2) All $\text{pre}[i]$ values should be less than $\text{pre}[N-1]$
- 3.)* They should form an increasing subsequence
(K-1)

Intuition

$pre[0], pre[1], \dots, pre[n-2], pre[n-1]$

vector<int> v;

for (int i = 0; i < n; ++i)
if ($pre[i] > 0$ && $pre[i] < pre[n-1]$)
v.push_back(pre[i]);

if ($LIS(v) \geq k-1$)
YES

else NO;

Solution

Let's implement

Thank You!

Reminder: Going to the gym & observing the trainer work out can help you know the right technique, but you'll muscle up only if you lift some weights yourself.

So, PRACTICE, PRACTICE, PRACTICE!