

# Assignment 4

## Foundations of Machine Learning

IIT-Hyderabad  
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### Questions: Programming

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### 5. Logistic Regression: (7 marks)

*Implementation contains a class of Logistic Regression with methods that calculate y, sigmoid, error, loss, updation of weights for iteration. b, w, learning rate, iterations can be specified as hyper parameters. Implementation also contains normalization of features it tries to fit the given model and hyper parameters and learn b and w here it is  $\theta_0, \theta_1, \theta_2$ , and use sigmoid of  $f_{\theta}(x_1, x_2) = \theta_0 + \theta_1 x_1 + \theta_2 x_2$ .*

*If sigmoid  $> 0.5$  then class is predicted as 1 otherwise it is 0.*

- (a) (3 marks) Implement your own code for a logistic regression classifier, which is trained using gradient descent and cross-entropy error as the error function.

| Index | $x_1$ | $x_2$ | y |
|-------|-------|-------|---|
| 1     | 0.346 | 0.780 | 0 |
| 2     | 0.303 | 0.439 | 0 |
| 3     | 0.358 | 0.729 | 0 |
| 4     | 0.602 | 0.863 | 1 |
| 5     | 0.790 | 0.753 | 1 |
| 6     | 0.611 | 0.965 | 1 |

| Index | $x_1$ | $x_2$ | y |
|-------|-------|-------|---|
| 1     | 0.959 | 0.382 | 0 |
| 2     | 0.750 | 0.306 | 0 |
| 3     | 0.395 | 0.760 | 0 |
| 4     | 0.823 | 0.764 | 1 |
| 5     | 0.761 | 0.874 | 1 |
| 6     | 0.844 | 0.435 | 1 |

Table 1: Train Set   Table 2: Test Set

- (b) Consider the training set and test set given in Tables 1 and 2. We use the linear model  $f_{\theta}(x_1, x_2) = \theta_0 + \theta_1 x_1 + \theta_2 x_2$  and the logistic regression function  $\sigma(f_{\theta}(x_1, x_2)) = \frac{1}{1 + \exp^{-f_{\theta}(x_1, x_2)}}$ . Consider the initial weights as  $\theta_0 = -1, \theta_1 = 1.5, \theta_2 = 0.5$ , and learning rate as 0.1 (for gradient descent).

- i. (1 mark) What is the logistic model  $P(\hat{y} = 1|x_1, x_2)$  and its cross-entropy error function?

As we know the logistic model for  $P(\hat{y} = 1|x_1, x_2)$  by substituting  $\theta, \theta_1, \theta_2$  given as -1, 1.5, 0.5

$$f_0(x_1, x_2) = 1.5 * x_1 + 0.5 * x_2 - 1$$

Cross Entropy Error Function is

**loss = (-target \* np.log(actual) - (1 - target) \* np.log(1 - actual)).mean()** where target is the desired value and actual is the value from model i.e.  $\hat{y}$

- ii. (1 mark) Use gradient descent to update  $\theta_0, \theta_1, \theta_2$  for one iteration. Write down the updated logistic regression model.

As we can see after one iteration values of  $W = [1.51234756, 0.50790003]$  and  $b = -0.9980220558745176$

Hence model before first iteration is

$$f_0(x_1, x_2) = 1.5 * x_1 + 0.5 * x_2 - 1$$

After first iteration it is

$$f_0(x_1, x_2) = 1.51234756 * x_1 + 0.50790003 * x_2 - 0.9980220558745176$$

- iii. (2 mark) At convergence of gradient descent, use the model to make predictions for all the samples in the test dataset. Calculate and report the accuracy, precision and recall to evaluate this model.

Accuracy :

0.6666666666666666

Precision :

0.6

Recall :

1.0