



DEPARTMENT OF MATHEMATICS

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| Course: NUMBER THEORY, VECTOR CALCULUS AND COMPUTATIONAL METHODS | QUIZ - I | Maximum marks: 10 |
| Course code: 22MA21C | First semester 2022-2023 Physics Cycle Branch: AI, BT, CD, CS, CY, IS, SPARK-P | Time: 20 Minutes Date: 05-07-2023 |

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Instructions to students: Rough work can be done at the backside of the sheet.

| Q.No | Quiz questions | M | BT | CO | | | | | | | | | | |
|------|---|----|----|-----|---|---|------|---|----|----|-----|---|----|---|
| 1.1 | Using suitable interpolation, fit a polynomial for the data <table><tr><td>x</td><td>-1</td><td>2</td><td>4</td></tr><tr><td>y</td><td>-5</td><td>4</td><td>0</td></tr></table> Ans: $4x - x^2$ | x | -1 | 2 | 4 | y | -5 | 4 | 0 | 2 | L2 | 3 | | |
| x | -1 | 2 | 4 | | | | | | | | | | | |
| y | -5 | 4 | 0 | | | | | | | | | | | |
| 1.2 | If $f(8) = 10$, $f(10) = 19$, $f(12) = 32.5$, $f(14) = 54$, $f(16) = 89.5$, then $\Delta^2 f(12) =$ _____ Ans: 14 | 1 | L1 | 1 | | | | | | | | | | |
| 1.3 | The value of $\Delta^3[(1 + 3x)(1 - 5x)(1 - 4x)]$ taking the interval of differencing $h = 1$ is _____. Ans: 360 | 1 | L1 | 1 | | | | | | | | | | |
| 1.4 | The particular solution of the initial value problem $y'' + y' + 0.25y = 0$ with $y(0) = 3$ and $y'(0) = -3.5$ is _____. Ans: $(3 - 2x)e^{-x/2}$ | 2 | L2 | 2 | | | | | | | | | | |
| 1.5 | Particular integral of $2 \frac{d^2y}{dx^2} + 3 \frac{dy}{dx} - 2y = e^{x/2}$ is _____. Ans: $\frac{xe^{x/2}}{5}$ | 1 | L2 | 2 | | | | | | | | | | |
| 1.6 | If $x = e^{-3t}$ is the solution of the differential equation $\frac{d^2x}{dt^2} + 4 \frac{dx}{dt} + kx = 0$, then $k =$ _____. Ans: $k = 3$ | 1 | L1 | 1 | | | | | | | | | | |
| 1.7 | Given <table><tr><td>x</td><td>0</td><td>2</td><td>4</td><td>6</td></tr><tr><td>f(x)</td><td>7</td><td>13</td><td>43</td><td>145</td></tr></table> The value of $f'(2) =$ _____. Ans: -3 | x | 0 | 2 | 4 | 6 | f(x) | 7 | 13 | 43 | 145 | 2 | L2 | 1 |
| x | 0 | 2 | 4 | 6 | | | | | | | | | | |
| f(x) | 7 | 13 | 43 | 145 | | | | | | | | | | |



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|--------|--|-----|----|----|---|-----|--------|---|---|----|----|---|----|---|
| 1.1 | Using suitable interpolation, fit a polynomial for the data <table><tr><td>x</td><td>-1</td><td>3</td><td>4</td></tr><tr><td>y</td><td>-4</td><td>0</td><td>6</td></tr></table> Ans: $x^2 - x - 6$ | x | -1 | 3 | 4 | y | -4 | 0 | 6 | 2 | L2 | 3 | | |
| x | -1 | 3 | 4 | | | | | | | | | | | |
| y | -4 | 0 | 6 | | | | | | | | | | | |
| 1.2 | If $f(1) = 0$, $f(1.2) = 0.128$, $f(1.4) = 0.544$, $f(1.6) = 1.296$, $f(1.8) = 2.432$, then $\nabla^2 f(1.6) =$ _____ Ans: 0.336 | 1 | L1 | 1 | | | | | | | | | | |
| 1.3 | The value of $\Delta^6[(2 - 3x)(3 - 4x^2)(2 + 5x^3)]$ taking the interval of differencing $h = 1$ is _____. Ans: 43200 | 1 | L1 | 1 | | | | | | | | | | |
| 1.4 | The particular solution of the initial value problem $9y'' + 6y' + y = 0$ with $y(0) = 4$ and $y'(0) = -\frac{13}{3}$ is _____. Ans: $(4 - 3x)e^{-x/3}$ | 2 | L2 | 2 | | | | | | | | | | |
| 1.5 | Particular integral of $4\frac{d^2y}{dx^2} + 3\frac{dy}{dx} - 10y = e^{-2x}$ is _____. Ans: $-\frac{xe^{-2x}}{13}$ | 1 | L2 | 2 | | | | | | | | | | |
| 1.6 | If the roots of the auxiliary equation are -2 and 3 , then the corresponding differential equation is _____. Ans: $\frac{d^2y}{dx^2} - \frac{dy}{dx} - 6y = 0$ | 1 | L1 | 1 | | | | | | | | | | |
| 1.7 | Given <table><tr><td>x</td><td>1</td><td>3</td><td>5</td><td>7</td></tr><tr><td>$f(x)$</td><td>2</td><td>7</td><td>16</td><td>29</td></tr></table> The value of $f'(7) =$ _____. Ans: 7.5 | x | 1 | 3 | 5 | 7 | $f(x)$ | 2 | 7 | 16 | 29 | 2 | L2 | 1 |
| x | 1 | 3 | 5 | 7 | | | | | | | | | | |
| $f(x)$ | 2 | 7 | 16 | 29 | | | | | | | | | | |



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|------|---|-----|-----|-----|----|----|------|-----|-----|-----|-----|---|----|---|
| 1.1 | Using suitable interpolation, fit a polynomial for the data <table border="1"><tr><td>x</td><td>2</td><td>4</td><td>5</td></tr><tr><td>y</td><td>0</td><td>6</td><td>12</td></tr></table> Ans: $x^2 - 3x + 2$ | x | 2 | 4 | 5 | y | 0 | 6 | 12 | 2 | L2 | 3 | | |
| x | 2 | 4 | 5 | | | | | | | | | | | |
| y | 0 | 6 | 12 | | | | | | | | | | | |
| 1.2 | If $f(0.2) = 0.0350$, $f(0.4) = 0.1170$, $f(0.6) = 0.2165$, $f(0.8) = 0.2995$, $f(1) = 0.3340$, then $\Delta^2 f(0.8) =$ _____ Ans: Does not exist | 1 | L1 | 1 | | | | | | | | | | |
| 1.3 | The value of $\Delta^3[(1-x)(1-3x)(1-5x)]$ taking the interval of differencing $h = 2$ is _____. Ans: -720 | 1 | L1 | 1 | | | | | | | | | | |
| 1.4 | The particular solution of the boundary value problem $y'' + y = 0$ with $y(0) = 1$ and $y\left(\frac{\pi}{2}\right) = 2$ is _____. Ans: $\cos x + 2 \sin x$ | 2 | L2 | 2 | | | | | | | | | | |
| 1.5 | Particular integral of $\frac{d^2y}{dx^2} + 4\frac{dy}{dx} + 5y = 3^x + e^x$ is _____. Ans: $\frac{e^x}{10} + \frac{3^x}{(\log_e 3)^2 + 4 \log_e 3 + 5}$ | 1 | L2 | 2 | | | | | | | | | | |
| 1.6 | If the complementary function of the differential equation is $y = (c_1 + c_2x)e^{-2x}$, then the corresponding differential equation is _____. Ans: $\frac{d^2y}{dx^2} + 4\frac{dy}{dx} + 4y = 0$ | 1 | L1 | 1 | | | | | | | | | | |
| 1.7 | Given <table border="1"><tr><td>x</td><td>20</td><td>25</td><td>30</td><td>35</td></tr><tr><td>f(x)</td><td>354</td><td>332</td><td>291</td><td>260</td></tr></table> The value of $f'(30) =$ _____. Ans: -10.1 | x | 20 | 25 | 30 | 35 | f(x) | 354 | 332 | 291 | 260 | 2 | L2 | 1 |
| x | 20 | 25 | 30 | 35 | | | | | | | | | | |
| f(x) | 354 | 332 | 291 | 260 | | | | | | | | | | |



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|--------|--|-----|-----|-----|---|-----|--------|-----|-----|-----|-----|---|----|---|
| 1.1 | Using suitable interpolation, fit a polynomial for the data <table border="1"><tr><td>x</td><td>3</td><td>4</td><td>8</td></tr><tr><td>y</td><td>5</td><td>8</td><td>0</td></tr></table> Ans: $-x^2 + 10x - 16$ | x | 3 | 4 | 8 | y | 5 | 8 | 0 | 2 | L2 | 3 | | |
| x | 3 | 4 | 8 | | | | | | | | | | | |
| y | 5 | 8 | 0 | | | | | | | | | | | |
| 1.2 | If $f(1) = 7.4036$, $f(2) = 7.7815$, $f(3) = 8.1311$, $f(4) = 8.4554$, $f(5) = 8.7574$, then $\nabla^2 f(4) =$ _____ Ans: -0.0253 | 1 | L1 | 1 | | | | | | | | | | |
| 1.3 | The value of $\Delta^4[(1 - 2x)(1 - 3x)(1 - 5x)(1 - 6x)]$ taking the interval of differencing $h = 2$ is _____. Ans: 69120 | 1 | L1 | 1 | | | | | | | | | | |
| 1.4 | The particular solution of the initial value problem $9y'' - 25y = 0$ with $y(0) = 0$ and $y'(0) = -5$ is _____. Ans: $-1.5e^{\frac{5x}{3}} + 1.5e^{-\frac{5x}{3}}$ | 2 | L2 | 2 | | | | | | | | | | |
| 1.5 | Particular integral of $3\frac{d^2y}{dx^2} - 2\frac{dy}{dx} - 5y = e^{5x/3}$ is _____. Ans: $\frac{xe^{\frac{5x}{3}}}{8}$ | 1 | L2 | 2 | | | | | | | | | | |
| 1.6 | If $x = e^{-t}$ is the solution of the differential equation $\frac{d^2x}{dt^2} - 6\frac{dx}{dt} - nx = 0$, then $n =$ _____. Ans: $n = 7$ | 1 | L1 | 1 | | | | | | | | | | |
| 1.7 | Given <table border="1"><tr><td>x</td><td>1</td><td>4</td><td>7</td><td>10</td></tr><tr><td>$f(x)$</td><td>416</td><td>240</td><td>212</td><td>135</td></tr></table> The value of $f'(1) =$ _____. Ans: -105.2222 | x | 1 | 4 | 7 | 10 | $f(x)$ | 416 | 240 | 212 | 135 | 2 | L2 | 1 |
| x | 1 | 4 | 7 | 10 | | | | | | | | | | |
| $f(x)$ | 416 | 240 | 212 | 135 | | | | | | | | | | |